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# **REVIEW**

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# Understanding nano-engineered particle-cell interactions: biological insights from mathematical models

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Understanding the interactions between nano-engineered particles and cells is necessary for the rational design of particles for therapeutic, diagnostic and imaging purposes. In particular, the informed design of particles relies on the quantification of the relationship between the physicochemical properties of the particles and the rate at which cells interact with, and subsequently internalise, particles. Quantitative models, both mathematical and computational, provide a powerful tool for elucidating this relationship, as well as for understanding the mechanisms governing the intertwined processes of interaction and internalisation. Here we review the different types of mathematical and computational models that have been used to examine particle-cell interactions and particle internalisation. We detail the mathematical methodology for each type of model, the benefits and limitations associated with the different types of models, and highlight the advances in understanding gleaned from the application of these models to experimental observations of particle internalisation. We discuss the recent proposal and ongoing community adoption of standardised experimental reporting, and how this adoption is an important step toward unlocking the full potential of modelling approaches. Finally, we consider future directions in quantitative models of particle-cell interactions and highlight the need for hybrid experimental and theoretical investigations to address hitherto unanswered questions.

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## 1 Introduction

Understanding the mechanisms involved with the cellular association and internalisation of nano-engineered particles remains a key research challenge. 1,2 There is significant potential for targeted drug and gene delivery, as well as the delivery of labelling and imaging agents, through the use of nanoengineered particles.3-6 However, the interactions between particles and cells are exceedingly complex and are not yet fully understood.7-10 This is not for a lack of effort: in the last ten years, the number of papers published per year relating to particle endocytosis or internalisation has increased threefold.† Increasingly, there is a realisation that mathematical and computational approaches can provide insight into the complicated physical, chemical and biological processes involved in the association and internalisation of particles. 11-13 Here we focus on the various mathematical and computational techniques that have been used to provide quantitative insight into particle-cell interactions and the subsequent internalisation of particles by cells. Note that throughout this review we refer to nano-engineered particles to be consistent with the Food and Drug Administration's terminology for nanotechnology: "products that contain or are manufactured using materials in the nanoscale range."14 This is a more broad definition than the use of the word "nanoparticles", which implies that the particles have a diameter less than 100 nm, as particles created with nano-engineering techniques may have diameters in the hundreds of nanometres.

The process of nano-engineered particle-cell interaction and internalisation first involves a particle arriving at the cell membrane. To arrive at the cell membrane, particles must travel through a fluid such as human blood or cell culture media. During this journey, particles will interact with free proteins present in the fluid. 15,16 A layer of proteins, known as

† Number of Scopus search results for ("nanoparticle" OR "particle") AND ("endocytosis" OR "internalisation") in 2019 and 2009.



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a protein corona, is formed via the adsorption of proteins to the particle surface. 15,16 As such, the identity of the particle at the moment of particle-cell contact depends both on the protein content of the corona, as well as the physicochemical properties of the particle. 15,16 Reviews of this process can be found elsewhere. 15,16 Upon arrival at the cell membrane, particles can bind to receptors present on the membrane through either specific or non-specific interactions. 17,18 Subsequently, at the beginning of the endocytosis process, the process by which the cell internalises external substances, the cell membrane begins to develop a budding structure (Fig. 1). The specific type of budding structure, such as clathrin-coated pits, caveolae or phagocytic invaginations, depends on the type of cell and the properties of the particle.8,9,17,19,20 In general, the budding structure ultimately fully envelops the particle and forms a vesicle, which can contain receptors and various extracellular material as well as the particle.18 Once inside the cytoplasm, in many endocytic pathways, the vesicle fuses with an early endosome. As the endosome matures, the acidity increases and hence the material contained within the endosome may be subject to degradation.18 The material within the endosome can also be recycled to the cell membrane, a process referred to as exocytosis. There are a range of endocytic pathways that are involved in the internalisation of nano-engineered particles, such as phagocytosis, macropinocytosis, clathrin-mediated endocytosis and clathrin-independent endocytosis, which includes caveolae-mediated endocytosis.7,19,21,22 Certain endocytosis mechanisms are restricted to specialised cell types. 19 In particular, phagocytosis, which is the primary mechanism of internalisation for larger particles with a diameter around 1 μm, only occurs in phagocytes, such as neutrophils, macrophages and monocytes.7,20 In general, there is a size-dependent relationship between the size of the particle and the dominant endocytic pathway.21-26 Previous research by Rejman et al.21 suggests that clathrin-mediated endocytosis is the preferred pathway for particles up to 200 nm in diameter. However, this observation is in conflict with the observation that clathrincoated vesicles are typically 60-120 nm in diameter,27 as 200 nm diameter particles cannot be fully enclosed by 60-120 nm diameter vesicles. This highlights the uncertainty about which specific internalisation pathway is employed to internalise particles of a particular size. Suen and Chau<sup>22</sup> report that only caveolae-mediated endocytosis occurs for 250 nm particles, caveolae-mediated endocytosis dominates clathrin-mediated endocytosis for 50 nm particles, and that there is no preference for either endocytosis pathway for 120 nm particles. Suen and Chau22 also find that the uptake rate of the particles depends on the particle size, with 50 nm particles internalised most rapidly and 250 nm particles internalised slowest. Shape, charge and surface chemistry have also been demonstrated to influence the rate of endocytosis, as well as influence cell fate.28-39 In this review we predominantly focus on receptormediated endocytosis as a pathway for particle interaction and internalisation, rather than phagocytosis or macropinocytosis. In particular, we focus on the role of mathematical and computational models to provide insight into how the

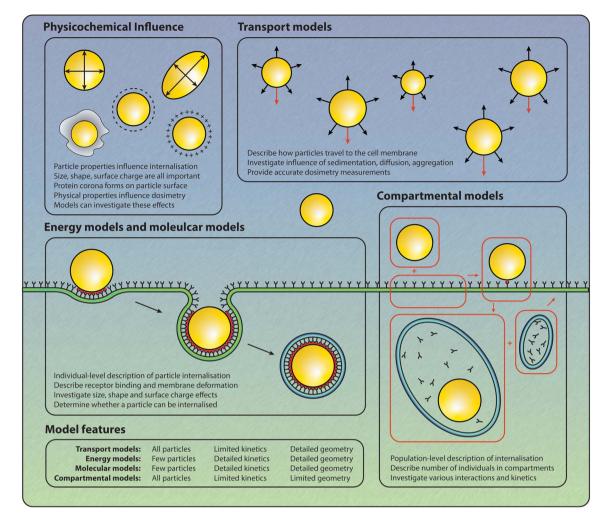


Fig. 1 Schematic of particle-cell interactions and the various modelling approaches applied to different components of the interaction and internalisation process.

physicochemical properties of nano-engineered particles influence interaction and internalisation.

In general, the use of mathematical and computational models provides a range of valuable benefits, particularly when employed in concert with experimental data. Mathematical models can be utilised to provide insight into specific mechanisms that may not be obtainable from experimental data. Further, models can be employed to integrate sets of experimental data, which may not have originated from within the same laboratory, to generate additional information compared to the individual datasets. Once sufficient data has been integrated, synthesised and analysed, predictions obtained from mathematical models can be used to inform future experimental designs via prediction of de novo interactions or behaviour.

Quantitative predictions about the strength of interaction and the rate of internalisation based on particle characteristics would be invaluable for the rational design of particles in the context of drug delivery and imaging. As such, mathematical models have been employed in an attempt to understand and quantify the effect of size, shape, charge and surface chemistry

on particle-cell interactions and internalisation. 40-44 Broadly, mathematical models of the internalisation process can be classified into four types of models, as shown in Fig. 1:

- Compartmental models, which describe the temporal evolution of the number of various entities, including particles, receptors and vesicles. In these models interac tions between particles and cellular entities are assumed to occur in a spatially-independent manner, which gives rise to systems of ordinary differential equations.
- *Energy models*, which describe the wrapping of particles by the cell membrane, and give insight into the balance between the energy gained from particle-receptor binding and the energy required for membrane deformation.
- Molecular models, which model the interaction and internalisation process by evaluating Newton's laws of motion for each atom. Such models provide great insight but are prohibitively computationally expensive for simulations on all but the smallest temporal and spatial scales: and.
- Transport models, which describe the transport process of particles in fluid, and the removal of particles from the

fluid by cellular interaction and internalisation. In both in vitro and in vivo experiments, the particles are trans ported to the cell membrane via fluid. Hence, to fully understand the internalisation of particles by cells, the processes by which the particles arrive at the cells must be considered.

In this review we provide information regarding the assumptions and techniques involved in each type of model, as well as the benefits and limitations of a particular type of model. We discuss the collective insight obtained from analysing and simulating the models in the context of particle internalisation, as well as the potential for each model to interface with experimental data. We highlight the ongoing community adoption of recently-proposed experimental reporting standards a welcome step towards a future where experimental data and mathematical models can be readily combined to generate further insight. Finally, we discuss future opportunities for interdisciplinary work involving experimental and theoretical approaches to answer questions about particle-cell interactions and particle internalisation that cannot currently be resolved.

# A brief introduction to mathematical modelling

Mathematical modelling is a flexible tool that can be employed to extract additional insight from experimental observations. Once a mathematical model has been formulated and parameterised (fitted to data), the model can be used to extrapolate beyond the range of the data used in model fitting, to investigate different potential mechanisms and to formulate new hypotheses. The flexibility in mathematical modelling means that there are a multitude of choices that must be made when selecting the class of model for a particular application. However, it is rarely immediately obvious which choices will best represent the system of interest. In this section we introduce the modelling choices that must be considered along with the benefits, drawbacks and assumptions associated with each class of model. We briefly discuss the methods of obtaining solutions to different classes of models, and present examples of each class of model in the context of particle-cell interaction

and internalisation in Table 1. Detailed discussion about the insight obtained about particle-cell interaction and internalisation from the application of these models can be found in the following sections. In this section we subdivide models according to the type of mathematical formalism that is used to describe the particle-cell interaction and internalisation, showing that these fall into several distinct mathematical categories according to the model features. In contrast, in subsequent sections, we focus on different aspects of particlecell interaction and internalisation, and in each case provide a review of the different mathematical models that have been developed, and the insights that have been gained from these models.

#### **Differential equations**

A common class of mathematical models are differential equation models.65,66 In differential equation models, a key assumption is that the quantity of interest, such as the number of particles or receptors, can be represented as a continuous variable (i.e. not restricted to integers).65 This assumption is appropriate provided that the quantity of interest is not limited to small numbers. 65 Additionally, outside of specific classes of differential equations, these models do not include stochastic effects such as environmental or demographic stochasticity.66 One implication of this is that all entities represented by a single quantity of interest are identical. 63 Further, given an initial state for the quantities of interest and a set of parameter values, the solution trajectory will always be the same.65 Stochastic effects are most important at small values of the quantity of interest.67 Differential equation models can be separated into three main categories: ordinary differential equations (ODEs), partial differential equations (PDEs) and stochastic differential equations (SDEs).66

ODE models are the simplest type of differential equation model, and describe the evolution of the quantities(s) of interest in time based on the interactions between entities. An example ODE model of particle-receptor binding is68

$$\frac{\mathrm{d}C(t)}{\mathrm{d}t} = f(P(t), R(t)) - g(C(t)),$$

Table 1 Classification of mathematical models, as well as information about the features of each class of model, including the typical method of solution for those models. Other solutions methods may be applicable, but are not mentioned unless widely used. Additionally, examples of the particle-cell interaction and internalisation models that can be described using each class of model are provided, alongside select references

Model class	Model features	Interaction/internalisation model	Select references
Ordinary differential equation	Continuous variables,	Compartmental models	22, 42 and 45-51
•	deterministic, analytic and	Energy and force models	25
	numerical solutions	Molecular models	52
Partial differential equation	Continuous variables, spatial	Compartmental models	53
-	effects, deterministic, numerical	Energy and force models	41 and 44
	solutions	Transport models	54-56
Stochastic differential equation	Continuous variables, stochastic effects, numerical solutions	Compartmental models	57
Deterministic discrete model	Discrete variables, deterministic,	Energy and force models	58
	numerical solutions	Transport models	59 and 60
Stochastic discrete model	Discrete variables, stochastic	Compartmental models	61 and 62
	effects, numerical solutions	Transport models	63 and 64

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where C(t) is the number of particle–receptor complexes, P(t) is the number of unbound particles and R(t) is the number of unbound receptors. The functions f(P(t), R(t)) and g(C(t))represent the binding and disassociation of complexes, respectively. Therefore, this equation states that the number of complexes increases due to particle-receptor binding and decreases due to the disassociation of complexes. ODE models involve an assumption that space does not play a role in the evolution of the quantities of interest, that is, that entities are well-mixed within a compartment. The simplicity of ODE models is appealing as various avenues are available to obtain model solutions. In certain cases, analytic solutions are obtainable; that is, a formula exists to calculate the exact solution.66 In other cases, behaviour of the system can be obtained through phase-space analysis, 66 where properties of the trajectory of the variables can be determined qualitatively, even without an exact formula for the solution. In the case where the ODE model is too complicated to obtain a solution via analytic approaches, numerical solutions to ODE models are readily obtainable through differential equation software packages such as Matlab's ODE suite69 or Python's SciPy package.70 Numerical solutions are approximate solutions that are obtained computationally by discretising the relevant time period into a finite number of time steps.71 While numerical solutions are approximate, the error between the true solution and the approximate solution can typically be reduced to an arbitrarily low value by increasing the number of time steps considered.71

The assumption that spatial effects are unimportant can be relaxed through the use of PDE models, where the role of space is explicitly considered.<sup>66</sup> An example PDE model of particle-receptor binding is

$$\frac{\partial C(x,\ t)}{\partial t} = \frac{\partial^2 C(x,\ t)}{\partial x^2} + f(P(x,\ t),\ R(x,\ t)) - g(C(x,\ t)),$$

where the variables are defined as above, but with an additional dependence on location; that is, the number of complexes at a location can only increase by particles and receptors binding at that location. The first term describes the diffusion of particle–receptor complexes, representing the undirected motion of the complexes. A drawback to this approach is that obtaining solutions to PDE models is typically significantly more complicated, compared to ODE models.<sup>71</sup> It is rare to obtain analytic solutions to PDE models, and obtaining numerical solutions can require specialist knowledge.<sup>66</sup>

SDE models allow for stochastic effects to be incorporated within a differential equation framework.<sup>66</sup> An example SDE model of particle–receptor binding is

$$dC(t) = f(P(t), R(t))dt - g(C(t))dt + dW(t),$$

where W(t) is a Wiener process, defined such that the difference in W(t) between any two time points is an independent random variable, <sup>66</sup> which can be considered as a random (or noisy) perturbation to the process of complex binding and disassociation. Again, analytic solutions to SDE models are uncommon, and numerical solutions are more complicated to obtain compared to ODE models. <sup>66</sup> Critically, each solution trajectory

for an SDE model will be different, which captures the influence of stochastic effects. The range of potential differential equation models highlights the trade-off between the model detail required to adequately describe the process of interest, and the added complexity of obtaining solutions to more complicated models.

Force-based models such as molecular dynamics models can be considered as another type of differential equation model. <sup>52</sup> Here, the change in location of individuals (typically molecules) occurs due to the velocity of individuals which, in turn, changes due to the force experienced by each individual according to Newton's laws of motion. The interaction forces between individuals relies on a specified potential function (or force field). <sup>52</sup> Due to the large number of individuals, analytic solutions to the system of equations cannot typically be obtained. Numerical solutions are possible *via* integration through time, though the structure of the interactions between individuals means that these solutions are limited in terms of the time and space that can be represented. <sup>72</sup> Further detail can be found in the section on molecular dynamics models.

#### Discrete models

Another class of mathematical models are *discrete models*. Instead of treating the quantity of interest as a continuous variable, the variable is restricted to integer states.<sup>73</sup> As such, discrete models are well-suited for describing processes that occur with small numbers of entities.<sup>67</sup> The model evolves by considering how single events can change the integer state of the system. For example, consider the above model where we describe the evolution of the number of particle–receptor complexes over time. In a discrete framework, we can describe this through

$$C_k = f(i, j)C_{k-1} + g(k+1)C_{k+1} - f(i, j)C_k - g(k)C_k$$

where i, j and k are the number of particles, receptors and complexes, respectively, and  $C_k$  is the probability that we have k complexes. This evolves corresponding to potential binding or disassociation events that result in an increase or decrease in the number of complexes. This can be solved simultaneously for all i, j and k values to obtain a probability distribution for the number of particles, receptors and complexes. Discrete models can be implemented in a deterministic way, as above, where the expected rate of each event is considered,  $^{67}$  or in a stochastic manner, where an event is selected with a specified probability.  $^{73}$  A stochastic discrete model of the particle–receptor binding process is

$$C_t = C_{t-1} + X(P_{t-1}, R_{t-1}, C_{t-1}),$$

where  $P_t$ ,  $R_t$  and  $C_t$  is the number of particles, receptors and complexes at time t, respectively, and  $X(\cdot)$  is a random variable such that  $X(P_{t-1}, R_{t-1}, C_{t-1}) = 1$  if a binding event occurs and  $X(P_{t-1}, R_{t-1}, C_{t-1}) = -1$  if a disassociation event occurs, where the rates of binding and disassociation depend on the number of particles, receptors and complexes.<sup>73</sup> The standard approach to obtain solutions to such models is numerical simulation.

Discrete models are flexible, as the rates of each event can be easily specified, and typically rely on fewer assumptions than differential equation models. However, systems with large numbers of states become computationally intensive to simulate. 67 Further, if stochastic effects are included in the transition events, a large number of numerical simulations must be performed to obtain the representative average behaviour of the system.<sup>67</sup> Similar to ODE models, the influence of spatial effects is typically neglected in discrete models, but can be included at the cost of additional computational complexity.

## Compartmental models

To investigate the insight obtained about particle-cell interaction and internalisation via mathematical approaches, we first consider compartmental models of particle-cell interactions and particle internalisation. Compartmental models are relatively commonly employed to describe the internalisation process, 22,42,45-47,49-51,74 and have been widely used to describe the related process of the binding and internalisation of molecules.68 A schematic of the processes considered in compartmental models is presented in Fig. 2, where compartments represent "species" such as particles, receptors and particlereceptor complexes. The simplest type of compartmental model involves only receptors and particles, and describes the evolution of the number of particle-receptor complexes.68

#### Receptor binding

Given a number of receptors,  $[R]_F$ , and a number density of particles,  $[P]_{F}$ , the evolution of the density of particle-receptor complexes,  $[P - R]_F$ , can be represented as

$$[P]_{\mathrm{F}} + [R]_{\mathrm{F}} \stackrel{k_{\mathrm{b}}}{\longleftrightarrow} [P - R]_{\mathrm{F}},$$

where  $k_b$  is a constant that represents the binding rate between the receptors and particles, and  $k_d$  is a constant that represents the disassociation of the particle-receptor complex.68 The subscript F highlights that these species are present in the fluid, rather than inside the cell. This model is relatively simple, but provides a platform for more detailed compartmental models, which have been employed to obtain insight into particle internalisation. 22,42,47,49,74,75 In particular, this model relies on the assumption that the number of receptors is essentially unchanged, implying that there are significantly more receptors on the cell membrane than particles arriving at the cell membrane. To evaluate whether this assumption is valid, the

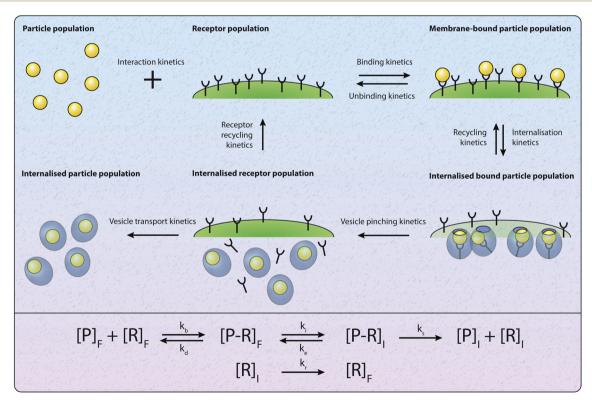


Fig. 2 Schematic of the processes involved in compartmental models of particle-cell interactions and particle internalisation. Nano-engineered particles interact with receptors and subsequently become bound to the cell membrane. The particles are either internalised or unbind from the receptors. Internalised particles can either be recycled or the vesicles can detach from the cell membrane and are subsequently transported through the cytosol, while the receptors are recycled back to the cell membrane. This process can be modelled via the chemical reaction, which describes the evolution of the number of particles in the fluid,  $[P]_F$ , the number of receptors on the outside of the cell,  $[R]_F$ , the number of particle-receptor complexes on the outside of the cell,  $[P-R]_F$ , the number of internalised particle-receptor complexes,  $[P-R]_F$ , the number of internalised particles,  $[P]_1$ , and the number of internalised receptors,  $[R]_1$ . This is equivalent to the above schematic. The k parameters represent the rates of particle-receptor binding  $(k_b)$ , particle-receptor unbinding  $(k_d)$ , particle-receptor internalisation  $(k_i)$ , particle-receptor exocytosis  $(k_e)$ , internalised particle-cell unbinding  $(k_s)$  and receptor recycling  $(k_r)$ , respectively.

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transport of the particles through fluid to the cell membrane must be well understood.54 The model further assumes that there is no local spatial variation in the receptors or particles, the particles are roughly the same size as the receptors, and that the particles can only be bound to a single receptor at a time. Given the influence of size effects on particle internalisation<sup>21,22</sup> and the number of experiments performed with particles of different sizes, it is reasonable to assume that incorporating size dependence is important. Additionally, this type of model does not describe the internalisation of the particle-receptor complex. The influence of each of these assumptions has been investigated via extensions to the basic model.42,47,53 For example, Kolhar et al.74 extend this simple model of particle binding to incorporate an shape-dependent binding rate that relies on an energy balance approach, and demonstrate that under shear flow, elongated particles are more likely to bind to the cell membrane due to the increase in surface area in contact with the membrane.

#### Internalisation

To incorporate the endocytosis of receptor-bound particles, an additional step can be introduced where the particle-receptor complex is internalised. Specifically, the complex is internalised and separates into the individual particle and receptor. The receptor is immediately exocytosed (recycled) and the particle remains within the cell, and is now denoted  $[P]_{\rm I}$ . Mathematically, this is represented

$$[P]_{\mathrm{F}} + [R]_{\mathrm{F}} \stackrel{k_{\mathrm{b}}}{\longleftrightarrow} [P - R]_{\mathrm{F}} \stackrel{k_{\mathrm{i}}}{\to} [P]_{\mathrm{I}} + [R]_{\mathrm{F}},$$

where  $k_i$  is the rate of internalisation. Again, this model is relatively simplistic and does not explicitly account for size effects, and relies on the assumption that all internalised particles remain within the cell rather than being exoctyosed. Belli et al.47 introduce an additional conservation equation to reflect the change in density of available particles at the cell surface. To account for inhibition of particle endocytosis, Suen et al.22 introduce an additional step where the particle-receptor complex can bind with an inhibitor. The resulting inhibited complex can still be internalised, albeit at a significantly reduced rate, and both the inhibitor and receptor are immediately exocytosed upon separation after internalisation. The authors acknowledge that inhibitors do not actually bind to the particle-receptor complex, and instead present the above model as a potential method for incorporating endocytic inhibition.<sup>22</sup> The model is used to investigate two types of inhibitor to elucidate which endocytosis pathway is employed to uptake folate-decorated particles in retinal pigment epithelium cells.22 Hauert et al.53 implement the kinetic internalisation model as a reaction term in a reaction-diffusion framework. This allows for the evaluation of the particle and receptor concentration across a spatial domain that represents tumour tissue.53 The authors find that incorporating a delay before particle binding occurs allows for the particles to diffuse throughout the tissue, thereby interacting with more cells compared to instantaneous binding.53 Byun and Jung57 consider a stochastic differential

equation approach, with an age-structured model to account for endosomal trafficking. Importantly, the stochastic nature of the model allows for the ever-present variability in experimental data to be described, as well as the extinction time for the delivery of particles to be calculated.<sup>57</sup> Slabu *et al.*<sup>75</sup> consider a three-stage model, where particles are either bound to the membrane, endocytosed or exocytosed. By calibrating their model to a suite of experimental data, the authors demonstrate that differences in the number of internalised particles between cell lines can be attributed to differences in the rate of endocytosis, rather than the rate of exocytosis or adsorption to the membrane.<sup>75</sup>

#### Multivalent binding

Ohta et al.49 present an extended model that incorporates additional detail in terms of allowing multiple receptors to bind to a particle, includes particle exocytosis, and includes an explicit description of the number of receptors within the cell. Particles can bind to a receptor to form a complex, and the complex can either be internalised or disassociate. The complex can bind to additional receptors during the internalisation processes, corresponding to receptors on the cell membrane that are within the invaginated area. As the complex is internalised into an endosome, the pH level decreases and a portion of complexes will disassociate. If a complex disassociates, the receptors are exocytosed back to the cell membrane while the particle remains within the cell. Alternatively, if a complex does not disassociate, the entire complex is recycled back to the cell membrane. To simplify the corresponding system of equations, an assumption is made that the total number of receptors is conserved. Ohta et al.49 employ this model to investigate the uptake and recycling of quantum dots, and find that the parameter governing the dissociation rate of the internalised complex significantly influences the ultimate accumulation of the quantum dots.

To account for the formation of particle clusters on the cell membrane, Jin et al.42 propose a model that allows a particlereceptor complex to bind to other complexes. If a particle binds to a receptor, it forms a single complex. These complexes diffuse on the cell membrane,41,42 which allows for the complex to interact with other particle-receptor complexes. The complexes can bind together to form complexes with two particles and two receptors which, in turn, can bind to other single complexes to form complexes with three particles and three receptors. Hence the model describes the evolution of the number of complexes with i particles and i receptors. 42 Each of these clusters can be internalised with a rate that depends on the radius of the cluster.42 The internalisation rate arises from the work of Gao et al.,41 who consider receptor diffusion on the cell membrane in response to a particle binding to receptors at a point, and the corresponding energy required to internalise the particle. This work is discussed in detail in the following section.

Aires *et al.*<sup>45</sup> consider a similar compartmental model where multiple binding events can occur. In contrast with the model presented by Jin *et al.*,<sup>42</sup> particles are functionalised with multiple ligands, each of which can bind to a receptor on the

cell surface. This model is consistent with the observation that arises from the analysis of Lunov et al.,76 who find that between two and twenty receptors are involved in the endocytosis of a nano-engineered particle. The initial receptor-ligand binding can arise from either specific or non-specific interactions. After the initial binding, the number of receptor-ligand connections can either increase or decrease, with the rate of increase depending on the number of free receptors remaining in the system. Aires et al.45 use the model to investigate different particle targeting strengths and the subsequent relative impact on tumorigenic cells and non-tumorigenic cells for particle capsules containing the chemotherapeutic drug gemcitabine. The authors find that an increase in the strength of specific interactions due to functionalisation results in the preferential killing of tumorigenic cells compared to both nonfunctionalised particles and free drug molecules. 45

Bai et al. 46,77 also consider a model where particles can bind to multiple receptors. However, in contrast with previous models where the particles are assumed to be in a static fluid, the model presented by Bai et al. 46,77 considers particles that are immersed in a flowing fluid. The authors find that the shear rate is less important in determining the number of particles internalised than the rate of ligand-receptor bond formation and rupture, as the formation and rupture rates are not significantly influenced by the rate of shear flow. In fact, the rate of bond rupture in shear flow did not change significantly compared to static culture. As washing cells after incubation to dislodge particles that are not fully endocytosed is a common component of experimental protocols,78 the observation that shear flow does not induce additional bond rupture may inform experimental protocols in the future.

The major strength of compartmental models is that it is relatively straightforward to compare the model predictions with experimental data. For example, a standard experimental measurement is the number of internalised or associated particles. The majority of compartmental models directly predict the number of internalised particles, and hence comparison between the model and experimental data is not complicated. Further, compartmental models are typically a system of ordinary differential equations, which can be numerically solved using standard differential equation software packages. As such, there is not a high barrier to obtaining predictions from compartmental models. However, the ease in obtaining model predictions and comparisons with data comes at a cost; complicated mechanisms are replaced by abstract parameters, which may not provide insight into the underlying mechanisms. Compartmental models also typically ignore information about spatial processes, such as particles arriving at the fluid-cell interface, which makes comparisons between experiments problematic. As such, there is a trade-off to be considered; between the ease of solution and the need to incorporate more complicated biological and physical processes in the model.

#### Pharmacokinetic approaches

Other types of compartmental models that have been employed to examine particle internalisation include physiologically-

based pharmacokinetic (PBPK) models.48,79-86 PBPK models incorporate physiological and anatomical detail regarding the interconnection of the organs and tissue throughout the body to analyse and predict the biodistribution of a substance of interest. One benefit of PBPK models is that it is relatively straightforward to compare predictions about biodistribution with in vivo experimental data. Typically, each organ or tissue component is represented by a compartment with anatomical knowledge informing the transition between compartments.48 Li et al.83 present a model containing seven compartments: blood, body, gastrointestinal tract, kidneys, liver, lungs and spleen. The blood consisted of two sub-regions for arterial and venous blood, and a lumen and urine sub-region for the gastrointestinal tract and kidney, respectively, provides a route for excretion.83 The authors find that a model where the transport across cell membranes is the limiting factor rather than the blood flow describes the biodistribution for PEG-vlated particles more accurately.83 However, the model does not explicitly include internalisation. Subsequently, a number of models have been proposed that include the influence of particle internalisation, 48,79,80,84-86 which is critical for understanding how particles remain within the circulatory system. The model presented by Bachler<sup>79,80</sup> allows for particles to undergo phagocytosis in a size-dependent manner in the lung, liver and spleen components whereas the model presented by Li et al. 84 involves the assumption that phagocytosis can occur in each component. Carlander et al.48 employ a modified version of the model presented by Li et al. 83 for a suite of particles and three different sets of membrane permeability coefficients. Carlander et al.48 are able to describe the biodistribution of all four types of particles considered and note that the difference in particle properties significantly alter the biokinetic parameters. This result is consistent with prior expectations, as the type of circulation pathway for particles is strongly size-dependent.87,88 For example, particles with a diameter of less than 10 nm are cleared by the renal system whereas particles with a diameter greater than 200 nm leave the blood stream and build up in both the liver and spleen.87 Lin et al.86 develop a PBPK model that is capable of describing the biodistribution of gold particles for mice, rats and pigs. A major benefit of PBPK models is that they can be readily calibrated to available experimental data, as highlighted by the recent meta-analysis of Cheng et al.89 In this meta-analysis, the authors sought to explain the consistently low delivery efficiency of particles to solid tumours, and as a result of the modelling analysis, attribute the delivery efficiency to low permeability at the tumour site.89 Additional detail regarding PBPK models for particle biodistribution can be found in the reviews by Moss and Siccardi<sup>90</sup> and by Li et al. 12

# Energy and force models

Another approach for the theoretical analysis of certain pathways for particle internalisation is to consider how the cell membrane can elastically envelop a particle that is bound to the receptors on the cell surface, as presented in Fig. 3.40,41,44,91-93 As the ligands on the surface of the particle bind to the receptors on the cell membrane, the membrane deforms at the location of Review

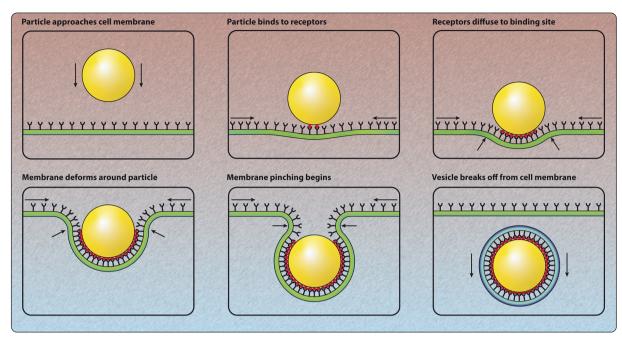


Fig. 3 Schematic of the processes involved in energy and force models of particle-cell interactions and particle internalisation. The particle arrives at the cell membrane and binds to the receptors on the cell membrane. The free energy made available through the particle-receptor binding is balanced by the energy required to deform the membrane around the particle. Receptors diffuse to the location of the bound particle. Ultimately, if internalisation is successful, the particle is enveloped by the membrane and the corresponding vesicle pinches off from the membrane and is transported through the cytosol.

the bound ligand-receptor complex due to the specific or nonspecific interaction between the ligand and the receptor. 9,25,93 Hence the energy associated with this interaction needs to be sufficiently strong to overcome the energy required to bend and/ or stretch the cell membrane.9,93 As the receptors bind to the particles, the distribution of the receptors on the cell surface becomes clustered at the locations of the particles. 40,41,44,91,92 This induces a concentration gradient in the receptor density and, consequently, the unbound receptors are driven towards the particles via diffusive motion.

## Rigid nano-engineered particles

Gao et al.41 were among the first to propose and analyse such a model, and considered receptors that could rapidly diffuse towards the location of a cylindrical or spherical particle bound to a cell membrane. Gao et al.41 demonstrate that the evolution of the receptor density is analogous to a Stefan problem that describes the moving interface between ice and water. By combining the solution to the Stefan problem with a balance between the energy obtained from receptor-ligand binding and the energy required for receptor transport, Gao et al.41 obtain the time required for the particle to be wrapped by the cell membrane. These results highlight the effect of size on particle internalisation, with particles under a critical radius of approximately 24 nm unable to enter the cell through membrane deformation. Additionally, the presence of an optimal particle radius at 27-30 nm, with respect to wrapping time, is consistent with certain experimental observations.41 Decuzzi and Ferrari40 extend the model presented by Gao et al.41

to include non-specific interactions between particles and cell receptors, which can either be attractive or repulsive. Intuitively, if these interactions are repulsive, both the wrapping time and the minimum particle size that can undergo internalisation increase. Conversely, if the interactions are attractive, smaller particles can undergo internalisation and the wrapping time decreases. In the case of non-specific interaction, Di Michele et al.94 demonstrate that allowing ligands to diffuse freely on the surface of a particle inhibits the internalisation of the particle. Tseng and Huang<sup>95</sup> combine an energy balance model with a model of fluid flow and examine the ability of a particle to undergo internalisation in different flow regimes. The authors find that the fluid motion can inhibit internalisation due to energy dissipation in the fluid.95 Banerjee et al.58 develop a model that combines stochastic binding events with a free energy description of pit formation and predict that particles with a diameter of approximately 60 nm are internalised most efficiently. Deng et al.96 implement a stochastic energy-based model of clathrin-mediated endocytosis, where the presence of clathrin affects the intrinsic curvature and bending rigidity of the cell membrane. The authors demonstrate that particle size is a key mediator of internalisation, as particles below a threshold size are unable to be internalised in the model,96 consistent with the results obtained in previous modelling studies.

#### Elastic nano-engineered particles

Thus far, all of the analysis of energy-based particle internalisation has been performed in the context of rigid particles that

are unable to change orientation during the internalisation process. Yi et al. 97 investigate particles that can undergo elastic deformation. Intuitively, elastic particles are less able to undergo complete wrapping than comparable rigid particles. The binding of rigid particles to the cell membrane allows only the membrane to deform, whereas for elastic particles both the membrane and the particle deform. 97-100 This approach has also been applied to the problem of exocytosis of elastic particles. 101 The result of inhibited wrapping for elastic particles is also observed for a similar model that contains stochastic receptorligand binding, rather than instantaneous deterministic binding. 100 Elastic particles can undergo asymmetric wrapping, in contrast to stiff particles which undergo reorientation in the same parameter regimes.99 Rotation during the internalisation process appears in both molecular and particle dynamics simulations,43 and allows for the maximisation of the contact area between the particle and the cell membrane. The optimal particle radius and corresponding wrapping time decrease with the density of receptors on the cell membrane 100 and do not appear to be significantly influenced by nonlinear spacing of ligands on the particle surface.102

#### Non-spherical nano-engineered particles

While the work by Decuzzi and Ferrari only considered spherical particles, extensions to non-spherical shapes have been presented.44,92 Richards and Endres44 extend the model to consider shapes that are not symmetrical around the vertical axis. Richards and Endres<sup>44</sup> show that non-spherical shapes are engulfed at a rate proportional to the local curvature at the interface between the bound particle and the free receptors. This is in contrast with spherical shapes, which are engulfed proportional to the square root of time.41 If the shape is sufficiently prolate with respect to the axis perpendicular to the membrane, the initially high curvature in contact with the cell membrane prevents the particle being engulfed. Alternatively, if the shape is sufficiently oblate, the particle becomes partially engulfed, as the curvature is initially small enough for engulfment but the particle eventually becomes stuck due to the increase in curvature towards the middle of the particle. In between these two extremes, the particle becomes engulfed, and Richards and Endres<sup>44</sup> demonstrate that prolate spheroids are engulfed faster than both spheres and oblate spheroids. For nanomaterials that approach one-dimensionality, membrane tension of the cell determines whether the dominant direction of the particle is perpendicular or parallel to cell membrane during internalisation.103

### Multiple nano-engineered particles

As surface receptors must move across the cell membrane toward a particle, the presence of multiple particles on the cell membrane may influence the wrapping time. Raatz et al. 104 examine whether membrane wrapping of multiple particles within a single invagination is energetically favourable compared to individual wrapping of particles. The authors find that, provided the repulsive interaction between the particles only occurs over a limited range, it is favourable for particles to

undergo co-operative wrapping, up to a threshold particle radius.104 Zhang et al.25 consider a thermodynamic approach where many particles are able to be internalised simultaneously, provided that the cell is at thermodynamic equilibrium. The authors find an optimal particle diameter of approximately 25 nm, which is consistent with the results obtained from the single particle internalisation model of Gao et al.41 The thermodynamic model of Zhang et al.25 also predicts an upper limit of approximately 60 nm, above which internalisation can stall due to a lack of receptors. It is important to note that other, non-receptor mediated, forms of endocytosis can occur above this limit. Richards and Endres<sup>13</sup> review similar energy-based models in the context of phagocytosis, which, while a distinct form of internalisation, shares certain similarities with receptor-mediated endocytosis. Yuan and Zhang105 also consider a thermodynamic approach and investigate the interplay between receptor density and particle size with respect to the time taken for internalisation to occur. Yuan and Zhang<sup>105</sup> find that a minimum time exists in terms of these two parameters, and corresponds to a particle with a diameter of approximately 28 nm.

Energy balance models provide an elegant approach for analysing the internalisation of particles. In particular, these models are well-suited for the investigation of the influence of the physicochemical parameters of the particles on the rate of endocytosis, as well as whether the internalisation process is successful or whether the process stalls. While these models examine the energetic process of the wrapping process in considerable detail, the models do not consider the energy that must be expended by the cell in the membrane fission process, which may alter the overall fate of the particle. 106,107 While extensions to multiple particles have been presented, 25,104 energy balance models are less appropriate for population-level analysis of particle internalisation, compared to compartmental models. Population-level measures, such as the number of internalised or membrane-bound particles, are standard experimental measurements. It is difficult to extrapolate analysis of the wrapping time of a single particle to the internalisation of a specific particle dose, and hence it is not straightforward to interface energy balance models with standard experimental data. Additionally, it is difficult to incorporate information about the time course of dosage in the models. Therefore, there is potential for the development of multiscale approaches that embed realistic particle-membrane interactions within a population-level framework. These multiscale approaches would incorporate high fidelity descriptions of particle-cell interactions while still being able to provide insight into the evolution of the number of internalised particles in a cell.

#### 5 Molecular models

Molecular dynamics provides a method for accurately modelling the movement of individual atoms via Newton's laws of motion. 23,52,93,108,109 Such an approach provides unparalleled spatial and temporal resolution of particle internalisation. However, the computational power required to simulate each

Review atom restricts both the spatial and temporal domains of the

process of interest that can be simulated.<sup>72</sup> As such, molecular dynamics simulations are not a panacea for all unresolved questions regarding the mechanisms governing particle internalisation. The simulations are typically limited to, at most, microseconds, 110 compared to the seconds required for a typical endocytic event.111 Coarse-grain approximations, where the motion of clusters of atoms are modelled instead of individual atoms, allow for the simulation of processes on larger domains for longer times due to the decrease in the number of agents simulated. 93,108,109 The reduction in the number of atoms comes at a price, as certain structural details that may be important are neglected, such as hydrogen bonds.72 However, coarse-grained models have been successfully employed to describe the internalisation of various individual particles. 108,109 Huang et al. 108 examine the internalisation of spherocylindrical particles for a range of aspect ratios. Similar to results obtained from the energy balance models, Huang et al. 108 find that there exists an optimal size for the internalisation of spherical particles, with respect to the time required for the particle to be enveloped by the membrane. Additionally, the authors find that particles with a sufficiently high aspect ratio that approach narrow-end first undergo a rotation such that the particles "lay down" on the membrane before being internalised.108 As the particles are internalised, they again undergo rotation, which ultimately results in the particle being in a "standing up" position. Shen et al.112 investigate the membrane wrapping efficiency for a range of particle shapes, sizes and surface stiffnesses, and find that surface stiffness has a greater influence on wrapping efficiency for particles with larger diameters. Yue and Zhang<sup>113</sup> implement a dissipative particle dynamics model to examine whether particle internalisation is enhanced in the presence of multiple particles. The authors find that the process is cooperative provided that the particle diameter is below a threshold value. 113 Hence sufficiently small particles will cluster together on the cell membrane and are internalised together, whereas larger particles will be internalised individually.113 Similar results are observed by Xiong et al.,114 albeit in a coarse-grained framework. Several reviews of molecular dynamics in the context of particle internalisation have been published in recent years and hence we refer the interested reader to these reviews for detailed information. 17,23,52,115-117 Similar to the energy balance models, molecular models provide great insight into the internalisation of individual particles but have difficulty informing population-level

# Transport models

While mathematical models of particle transport through fluid do not solely describe the internalisation process, such models provide important insight into the time course of particles that arrive at the fluid-cell interface. Accurate quantification of the number of particles that interact with cells is critical for consistent dosimetry estimates, which is of key importance for nanotoxicology and nanomedicine. 118-130 The dose metric corresponding to the particle mass initially immersed in the fluid,

measures, such as the overall number of internalised particles.

referred to the administered dose, does not contain this information. As particle transport is both diameter- and materialdependent, 118,128,131 it is not straightforward to robustly compare experiments that use different particles via the administered dose. Metrics that involve the particle surface area have been proposed, but again do not incorporate the amount of particles that interact with the cells. 124,125,132 As such, an alternative metric that describes the number of particles that arrive at the fluidcell interface, referred to as the delivered dose, has been proposed.<sup>54,118,127,128,131,133,134</sup> The delivered dose is typically obtained from a mathematical model of particle transport. Notable dosimetry models that have been widely employed and validated135 in nanotoxicology and bionanoscience include the "In vitro Sedimentation Diffusion Dosimetry (ISDD)" model118 (and its extension, the ISD3 model<sup>136</sup>), the "Distorted Grid" model<sup>120</sup> and the "Bionano Interaction Kinetics Estimator" (BIKE) model.<sup>55</sup> Importantly, the code for all of these models can be freely obtained and can be implemented in a straightforward manner. Here we provide a relatively brief review of particle transport models; additional information can be found in the review of in vitro dosimetry by Cohen et al.54

#### Partial differential equations

The standard approach for calculating the delivered dose is to numerically solve a partial differential equation model. This approach provides the time course of the mass or number of particles that arrive at the cell surface, as well as the distribution of the particles throughout the fluid, as shown in Fig. 4. Typically, these models will describe particles undergoing both diffusion and sedimentation.11,56,118,120,121,136-141 The relative contributions of diffusion and sedimentation to the overall rate of transport depends on the size and density of the particles. In particular, the sedimentation velocity of a particle increases linearly with the difference between the particle density and the fluid density, and increases quadratically with the particle diameter. 118,133 In contrast, the rate of diffusion is inversely proportional to the particle diameter. 118,133 Corrections to the rate of diffusion for high-aspect ratio particles have been introduced.142 Dosimetry models have been successfully employed to investigate the influence of sedimentation on particle-cell association and internalisation in various experimental geometries, 137,138,141,143,144 and to investigate the mechanisms of internalisation. 120 Johnston and Crampin 56 present a method for analytically determining the influence of particle polydispersity on the delivered dose, and find that representative amounts of polydispersity can influence the delivered dose by a factor of two. The importance of accurately estimating polydispersity is highlighted by the study of Petersen et al.,145 who show that employing different techniques for measuring the particle size distribution can result in different estimates of the delivered dose. Schneider et al.146 demonstrate that the sonication of particles to disrupt aggregate formation has a significant impact on the ratio of administered dose to delivered dose. Cohen et al. 147 approximate the output from a sedimentation-diffusion model with a sigmoidal function with a single free parameter that represents the rate of

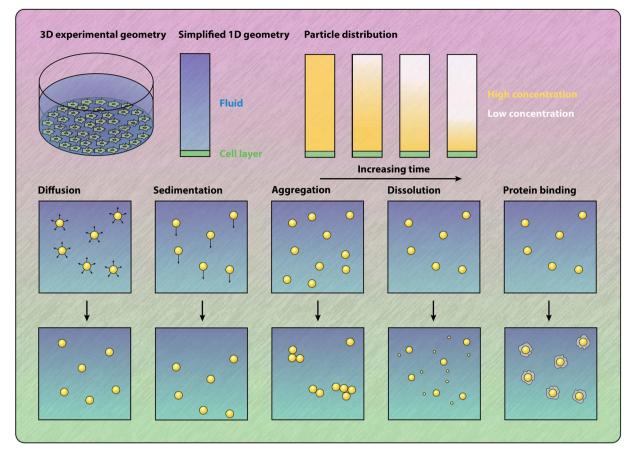


Fig. 4 Schematic of the processes and geometry involved in models of particle transport. Comparison between typical experimental geometry and the corresponding dimensionally-reduced mathematical geometry. Influence of different mechanisms on particle properties and location. Diffusion results in the random motion of the particles. Sedimentation results in the motion of the particles in the direction of gravitational acceleration. Aggregation results in the clustering of multiple particles, increasing the diameter and altering the density of the particles. Dissolution decreases the diameter of the particles and also produces individual ions. Protein binding results in the formation of a protein corona on the particle surface, increasing the diameter and altering the density of the particles.

deposition for a particular particle and media combination. Calculating this parameter value for a library of particle-media pairs allows for rapid quantification and comparison of the ability for particles to interact with the cells. The standard sedimentation-diffusion models make the assumption that particles are non-interacting and hence do not dynamically form aggregates during the transport process. Aggregation influences both the effective density and diameter of the particles and can be included in the model. 133,148 However. formation of particle aggregates is typically assumed to occur before the transport process and hence particle aggregation is static in the model.148 The review by Moore et al.149 highlights the importance of understanding particle aggregation in cell culture media, and notes that current theoretical approaches for describing the formation of aggregates cannot fully explain all colloidal systems. Significantly, Moore et al. 150 note that even the method by which particles are introduced to cell culture experiments can influence the association and internalisation of the particles. The authors show that an initially concentrated dose of particles results in more particle-cell interactions compared to a well-mixed particle solution. 150

Extensions to the ISDD model to incorporate the change in particle size due to dissolution in the media have recently been presented.136 Thomas et al.136 use the extended ISD3 model to investigate the internalisation of silver particles, as well as the uptake of silver ions, which are present in the system as a result of dissolution. Grabinski et al.151 consider transport in an in vitro experiment containing dynamic flow and find that the influence of sedimentation is significantly reduced in the presence of shear flow. Another extension considered is a threedimensional model of sedimentation and diffusion.152 The standard one dimensional nature of the model is no longer sufficient to calculate the delivered dose for cell populations that grow on both the sides and bottom of a culture dish, which occurs for cell lines that must be incubated over multiple cell doubling times to differentiate sufficiently to realise their full function.152 The wide range of experimental factors that have been demonstrated to significantly impact the delivered dose, and hence impact the rate of particle-cell interaction and particle internalisation, highlights the need for experimental protocols to be robustly described such that dosimetry calculations can be performed. Without dosimetry calculations it is

exceedingly difficult to draw conclusions between experiments due to potential disparities in the number of particles interacting with cells.

#### Stochastic models

Review

An alternative approach for describing particle transport is to employ stochastic methods, where the transport of individual particles is described explicitly with Monte Carlo simulations. 61,62,64 While it is more straightforward to incorporate particle interactions in such models, the inherent stochasticity typically increases the computational effort required to obtain population-level behaviour. Rodriguez-Lorenzo et al.64 implement a random walk process of sedimentation and diffusion for a polydisperse particle population and demonstrate that the delivered dose depends on the degree of polydispersity. Mukherjee et al.62 extend the dynamic agglomeration model presented by Liu et al.61 to describe the agglomeration, diffusion, sedimentation and dissolution of particles in a direct simulation Monte Carlo framework. Mukherjee et al. 62 employ their model to examine the influence of each type of mechanism on the particle population characteristics, as well as the delivered dose. By accounting for the delivered dose, calculated from a stochastic model of aggregation, sedimentation and diffusion, Liu et al.122 are able to compare the toxicity for a range of metal oxide particles.

#### **Internalisation in transport models**

In models of particle transport the influence of particle internalisation manifests itself through a condition on the boundary of the experimental domain. As these models are primarily focused on describing the transport processes, this condition is typically not as sophisticated as the models described in the previous sections. Historically, in much of the literature, a strong distinction has not been made between the processes of cell membrane binding and particle internalisation. Instead, the number of "associated" particles is typically reported, which is a catch-all term for particles that are either bound strongly to the cell membrane or have been internalised.<sup>55</sup> For example, a common assumption is that particles bind to the cell membrane and are instantly internalised, 118,136,138,140 thereby avoiding the build-up of particles on the cell surface. This assumption results in a dosage estimate that is the upper bound on the delivered dose, as there is no inhibition of particle association. However, it is possible that the particles are deposited on the cell surface sufficiently rapidly such that is not possible for all of the particles to associate with the cell.120,134 Hence a gradient in the particle density will form towards the location of the cell, inhibiting the transport of particles to the cell. This can be described in several ways. The simplest approach is to employ a flux-limited condition, where only a fixed proportion of the particles that arrive at the cell surface associate, and the remainder of the particles remain in the fluid.56 DeLoid et al.120 account for this phenomenon by describing the particle association as a Langmuir isotherm adsorption process. This approach imposes a maximum particle density on the cell surface, and inhibits association as

the density increases.<sup>120</sup> Faria *et al.*<sup>55</sup> conducted a thorough investigation into boundary conditions that represent particlecell association by calibrating a transport model with a range of boundary conditions to a library of particle-cell association data. These boundary conditions represent particle-cell association as either: (i) instantaneous; (ii) proportional to the particle density; (iii) proportional to the particle density but limited by cell surface area; (iv) proportional to the particle density but limited by the finite particle capacity of a cell; or (v) a combination of (iii) and (iv).<sup>55</sup> The authors demonstrate conclusively that the finite particle capacity of a cell is a key factor in particle internalisation. Further, the authors provide a freely-available methodology for extracting quantitative estimates from data to allow for comparison between experiments.<sup>153</sup>

Models that incorporate particle transport, stochastic particle behaviour, and internalisation kinetics have been successfully employed to understand the phenomenon of heterogeneity in particle dosage at an individual cell level. 59,60,63,154,155 Heterogeneity in particle dosage has potentially severe consequences for particle-based therapeutics, as successful treatment may rely on each cell internalising a threshold number of drug-loaded particles. Particle internalisation, on a particle-by-particle case, can be considered as a random event. 60 As such, heterogeneity in particle dosage on a cell population level can be described via appropriate statistical distributions and has been attributed to the cell cycle due to changes in cell surface area. 59 By extending the particle internalisation and transport model of Faria et al.55 to account for stochastic particle behaviour, Johnston et al.63 demonstrate that the heterogeneity in particle dosage can be explained by accounting for three factors: (i) stochastic particle motion; (ii) heterogeneity in the rate of particle-cell association, and; (iii) heterogeneity in the finite particle capacity of cells. Further, the authors show that all three factors are needed to explain experimental observations.63 This systematic unpacking of complex phenomena to reveal the key governing mechanisms highlights the insight that can be gained by combining mathematical models and particle-cell experiments. As described in the previous sections, there are many sophisticated approaches to explicitly model particle internalisation, and hence there remains significant potential for developing techniques that interface particle transport models with models of particle internalisation to obtain hitherto unknown information regarding particle-cell interactions and particle internalisation.

# 7 Mathematical models and standardisation of experimental reporting

Throughout this review, we have highlighted the role that mathematical modelling plays in obtaining insight into particle-cell interactions and particle internalisation. Mathematical models have additional benefit in that they can be retroactively calibrated to previously-published experimental data to gain new insight.<sup>89</sup> However, for the full value of this

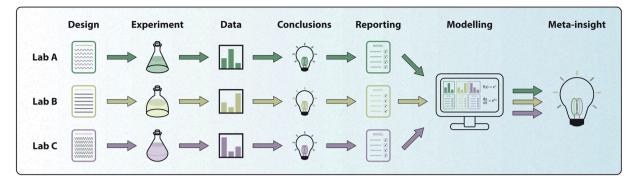


Fig. 5 Schematic highlighting how standardised reporting of experimental protocol can facilitate additional insight *via* mathematical models. In this example, three labs perform an experiment using three different experimental designs. The three labs interpret their data and draw appropriate conclusions. If the experimental protocol is reported following community standards, modelling approaches can be employed to synthesise the data and gain further insight.

benefit to be realised, the details of the experiments need to be reported in a consistent and accessible way. We present an example of how a combination of standardised reporting and mathematical modelling can result in additional insight in Fig. 5. In 2018, the minimum information reporting in bio-nano experimental literature (MIRIBEL) standard was proposed. 156 This standard provides a reporting checklist for details regarding materials characterisation, biological characterisation and experimental protocol. Crucially, the information that is provided in this checklist allows for the relevant parameters in mathematical models of particle-cell interactions and particle internalisation to be established, and for the models' full predictive and analytic power to be realised. Models provide a method for the unbiased and robust comparison of experiments performed with different particles, different cell lines and in different laboratory conditions. 156,157 This robust comparison would allow for collective insight to be gathered by combining data from experiments performed all over the world. However, for this insight to be realised, experimental data must be made available and standards in experimental reporting must be followed. For example, it is now well accepted that particle density strongly influences particle-cell interactions via sedimentation. 137,138,141,143,144 If standardised experimental reporting had been adhered to, then previous experimental data could be revisited via models that now account for sedimentation effects to determine whether the original conclusions drawn regarding particle-cell interactions are appropriate. As it stands now, it is impossible to effectively compare conclusions from recent investigations into particle-cell interactions, where the aforementioned range of confounding variables are reported and accounted for via mathematical modelling, with investigations conducted before the advent of standardised experimental reporting, where information about confounding variables is scarce. However, the future is bright, as the bionanoscience community has begun to embrace the MIRIBEL standards. This suggests that both meta- and retrospectiveanalyses via mathematical modelling will become significantly easier to conduct, thereby value-adding to published experimental studies.

## 8 Outlook and conclusions

Understanding nano-engineered particle-cell interactions and particle internalisation remains a key area of research in bionanoscience. Due to the complex intertwining of a variety of biological, physical and chemical processes, the critical mechanisms governing the internalisation of the particles and the interactions between particles and cells are yet to be completely elucidated. Mathematical and computational models provide a method for obtaining insight into a simplified view of particle-cell interactions. Energy balance and molecular models have been utilised to examine how particle shape, particle size and the strength of specific interactions of particles with cell receptors can influence how rapidly, or indeed whether, an individual particle will undergo internalisation. Promisingly, the results from these models are consistent with experimental observations. Compartmental models are able provide information about the time course of the number of particles that have been internalised by an individual cell and, again, have been successfully calibrated to experimental internalisation data. These past successes highlight the need for future investigations to driven through a marriage of experimental and theoretical approaches. Models are able to generate predictions that can inform experimental direction, thereby providing a rational basis for future experimental design choices. In turn, the experimental data, reported according to established community guidelines,156 provides insight into the features of the models that may be inappropriate, or highlight the need for the inclusion of more sophisticated mechanisms in the model. However, the number of experimental investigations of particle-cell interactions still dwarfs the number of theoretical, or hybrid experimental-theoretical investigations. Hence there is significant opportunity for high impact interdisciplinary work involving both experimentalists and theoreticians.

Current mathematical and computational models have made important developments toward understanding various aspects of particle-cell interactions and particle internalisation. However, other aspects are yet to be explored comprehensively. In particular, the signalling processes initialised by the binding of particles to the receptors on the cell membrane and the Review

subsequent downstream cellular effects remain an open problem from a modelling perspective. Additionally, spatiotemporal population-level descriptions of the prevalence of internalised particles are relatively sparse in the literature. While these models are perhaps more complicated than current models, there is significant potential for the systematic development of such models in concert with experimental data. It is critical for newly-developed models to be designed with experimental limitations in mind, as otherwise models run the risk of being overly complicated and may contain parameters or variables that cannot be reliably estimated or investigated, respectively, with current experimental techniques. For example, it is not common in experimental protocols to distinguish between internalised particles and particles that are merely bound to the

cell membrane. 55,158,159 To robustly calibrate the model, either

the mathematical model must calculate the number of associ-

ated particles, 55,63 rather than internalised particles, or more

complex experimental protocols must be implemented. 158,159

Another likely fruitful avenue for future research is the combi-

nation of existing models of particle internalisation in a multi-

scale framework. In such a framework, conclusions about

population-level behaviour can be drawn without the model

being both computationally and analytically intractable, while still incorporating detailed information about individual particle-cell interactions.

Mathematical and computational approaches provide a powerful tool for understanding particle-cell interactions and particle internalisation. However, there is still significant room for both the development of novel models of particle internalisation and for interdisciplinary investigations incorporating both experimental data and existing models. Significant strides have been made in recent years with respect to understanding how the physicochemical properties of particles influence the rate of internalisation but many open questions remain. We believe that hybrid theoretical and experimental investigations represent a fruitful opportunity for answering questions that

## Author contributions

appear intractable currently.

Conceptualisation (STJ, MF, EJC); data curation (STJ, MF, EJC); investigation (STJ); visualisation (STJ); writing – original draft (STJ); writing – review and editing (STJ, MF, EJC); funding acquisition (EJC).

## Conflicts of interest

The authors declare that there are no conflicts of interest.

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## Notes and references

- 1 A. H. Faraji and P. Wipf, *Bioorg. Med. Chem.*, 2009, **17**, 2950–2962.
- 2 E. A. Sykes, J. Chen, G. Zheng and W. C. Chan, *ACS Nano*, 2014, **8**, 5696–5706.
- 3 D. Bobo, K. J. Robinson, J. Islam, K. J. Thurecht and S. R. Corrie, *Pharm. Res.*, 2016, **33**, 2373–2387.
- 4 Y. Gao, Y. Chen, X. Ji, X. He, Q. Yin, Z. Zhang, J. Shi and Y. Li, *ACS Nano*, 2011, 5, 9788–9798.
- 5 J.-H. Lee, Y.-M. Huh, Y.-W. Jun, J.-W. Seo, J.-T. Jang, H.-T. Song, S. Kim, E.-J. Cho, H.-G. Yoon, J.-S. Suh and J. Cheon, *Nat. Med.*, 2007, 13, 95–99.
- 6 Y. Yan, A. P. Johnston, S. J. Dodds, M. M. Kamphuis, C. Ferguson, R. G. Parton, E. C. Nice, J. K. Heath and F. Caruso, *ACS Nano*, 2010, 4, 2928–2936.
- 7 I. Canton and G. Battaglia, Chem. Soc. Rev., 2012, 41, 2718–2739.
- 8 N. D. Donahue, H. Acar and S. Wilhelm, *Adv. Drug Delivery Rev.*, 2019, **143**, 68–96.
- 9 A. E. Nel, L. Mädler, D. Velegol, T. Xia, E. M. Hoek, P. Somasundaran, F. Klaessig, V. Castranova and M. Thompson, *Nat. Mater.*, 2009, 8, 543.
- 10 L. Treuel, X. Jiang and G. U. Nienhaus, J. R. Soc., Interface, 2013, 10, 20120939.
- 11 G. M. DeLoid, J. M. Cohen, G. Pyrgiotakis and P. Demokritou, *Nat. Protoc.*, 2017, 12, 355.
- 12 M. Li, P. Zou, K. Tyner and S. Lee, AAPS J., 2017, 19, 26-42.
- 13 D. M. Richards and R. G. Endres, Rep. Prog. Phys., 2017, 80, 126601.
- 14 Food and Drug Administration, 2014, FDA-2010-D-0530.
- 15 P. Del Pino, B. Pelaz, Q. Zhang, P. Maffre, G. U. Nienhaus and W. J. Parak, *Mater. Horiz.*, 2014, 1, 301–313.
- 16 C. Ge, J. Tian, Y. Zhao, C. Chen, R. Zhou and Z. Chai, *Arch. Toxicol.*, 2015, 89, 519–539.
- 17 X. C. He, M. Lin, F. Li, B. Y. Sha, F. Xu, Z. G. Qu and L. Wang, *Nanomedicine*, 2015, **10**, 121–141.
- 18 P. V. Rewatkar, R. G. Parton, H. S. Parekh and M.-O. Parat, *Adv. Drug Delivery Rev.*, 2015, **91**, 92–108.
- 19 G. J. Doherty and H. T. McMahon, *Annu. Rev. Biochem.*, 2009, 78, 857-902.
- 20 L. Shang, K. Nienhaus and G. U. Nienhaus, *J. Nanobiotechnol.*, 2014, **12**, 5.
- 21 J. Rejman, V. Oberle, I. S. Zuhorn and D. Hoekstra, *Biochem. J.*, 2004, 377, 159–169.
- 22 W.-L. L. Suen and Y. Chau, *J. Pharm. Pharmacol.*, 2014, **66**, 564–573.
- 23 H.-M. Ding and Y.-Q. Ma, Nanoscale Horiz., 2018, 3, 6-27.
- 24 Y. Shan, S. Ma, L. Nie, X. Shang, X. Hao, Z. Tang and H. Wang, *Chem. Commun.*, 2011, 47, 8091–8093.
- 25 S. Zhang, J. Li, G. Lykotrafitis, G. Bao and S. Suresh, Adv. Mater., 2009, 21, 419–424.
- 26 J. Zhao and M. H. Stenzel, *Polym. Chem.*, 2018, **9**, 259–272.
- 27 M. Kaksonen and A. Roux, *Nat. Rev. Mol. Cell Biol.*, 2018, 19, 313.

28 A. Albanese, P. S. Tang and W. C. Chan, *Annu. Rev. Biomed. Eng.*, 2012, 14, 1–16.

Nanoscale Advances

- 29 M. S. Boyles, L. Young, D. M. Brown, L. MacCalman, H. Cowie, A. Moisala, F. Smail, P. J. Smith, L. Proudfoot, A. H. Windle and V. Stone, *Toxicol. in Vitro*, 2015, 29, 1513–1528.
- 30 M. Björnmalm, M. Faria, X. Chen, J. Cui and F. Caruso, *Langmuir*, 2016, 32, 10995–11001.
- 31 B. D. Chithrani and W. C. Chan, *Nano Lett.*, 2007, 7, 1542–1550.
- 32 C. Kinnear, T. L. Moore, L. Rodriguez-Lorenzo, B. Rothen-Rutishauser and A. Petri-Fink, *Chem. Rev.*, 2017, **117**, 11476–11521.
- 33 R. Pan, G. Liu, Y. Li, Y. Wei, S. Li and L. Tao, *Nanoscale*, 2018, **10**, 8269–8274.
- 34 R. Podila and J. M. Brown, *J. Biochem. Mol. Toxicol.*, 2013, 27, 50-55.
- 35 S. Sharifi, S. Behzadi, S. Laurent, M. L. Forrest, P. Stroeve and M. Mahmoudi, *Chem. Soc. Rev.*, 2012, 41, 2323–2343.
- 36 N. P. Truong, M. R. Whittaker, C. W. Mak and T. P. Davis, Expert Opin. Drug Delivery, 2015, 12, 129–142.
- 37 E. A. Untener, K. K. Comfort, E. I. Maurer, C. M. Grabinski, D. A. Comfort and S. M. Hussain, ACS Appl. Mater. Interfaces, 2013, 5, 8366–8373.
- 38 X. Wang, X. Hu, J. Li, A. C. M. Russe, N. Kawazoe, Y. Yang and G. Chen, *Biomater. Sci.*, 2016, 4, 970–978.
- 39 W. Wang, K. Gaus, R. D. Tilley and J. J. Gooding, *Mater. Horiz.*, 2019, 6, 1538–1547.
- 40 P. Decuzzi and M. Ferrari, *Biomaterials*, 2007, **28**, 2915–2922.
- 41 H. Gao, W. Shi and L. B. Freund, *Proc. Natl. Acad. Sci. U. S. A.*, 2005, **102**, 9469–9474.
- 42 H. Jin, D. A. Heller, R. Sharma and M. S. Strano, *ACS Nano*, 2009, 3, 149–158.
- 43 Y. Li, T. Yue, K. Yang and X. Zhang, *Biomaterials*, 2012, 33, 4965–4973.
- 44 D. M. Richards and R. G. Endres, *Proc. Natl. Acad. Sci. U. S. A.*, 2016, **113**, 6113–6118.
- 45 A. Aires, J. Cadenas, R. Guantes and A. Cortajarena, *Nanoscale*, 2017, **9**, 13760–13771.
- 46 F. Bai, J. Wu and R. Sun, Math. Biosci., 2018, 295, 55-61.
- 47 V. Belli, D. Guarnieri, M. Biondi, F. della Sala and P. A. Netti, *Colloids Surf.*, *B*, 2017, **149**, 7–15.
- 48 U. Carlander, D. Li, O. Jolliet, C. Emond and G. Johanson, *Int. J. Nanomed.*, 2016, **11**, 625.
- 49 S. Ohta, S. Inasawa and Y. Yamaguchi, *Biomaterials*, 2012, 33, 4639–4645.
- 50 M.-S. Martina, V. Nicolas, C. Wilhelm, C. Ménager, G. Barratt and S. Lesieur, *Biomaterials*, 2007, **28**, 4143–4153.
- 51 C. Wilhelm, F. Gazeau, J. Roger, J. Pons and J.-C. Bacri, *Langmuir*, 2002, **18**, 8148–8155.
- 52 H.-M. Ding and Y.-Q. Ma, Small, 2015, 11, 1055-1071.
- 53 S. Hauert, S. Berman, R. Nagpal and S. N. Bhatia, *Nano Today*, 2013, 8, 566–576.
- 54 J. M. Cohen, G. M. DeLoid and P. Demokritou, *Nanomedicine*, 2015, **10**, 3015–3032.

- 55 M. Faria, K. F. Noi, Q. Dai, M. Björnmalm, S. T. Johnston, K. Kempe, F. Caruso and E. J. Crampin, *J. Controlled Release*, 2019, 307, 355–367.
- 56 S. T. Johnston, M. Faria and E. J. Crampin, *J. R. Soc.*, *Interface*, 2018, **15**, 20180364.
- 57 J. H. Byun and I. H. Jung, *Applied Mathematical Modelling*, 2020, 79, 300–313.
- 58 A. Banerjee, A. Berezhkovskii and R. Nossal, *Phys. Biol.*, 2016, 13, 016005.
- 59 P. Rees, J. W. Wills, M. R. Brown, C. M. Barnes and H. D. Summers, *Nat. Commun.*, 2019, **10**, 1–8.
- 60 H. D. Summers, P. Rees, M. D. Holton, M. R. Brown, S. C. Chappell, P. J. Smith and R. J. Errington, *Nat. Nanotechnol.*, 2011, 6, 170–174.
- 61 H. H. Liu, S. Surawanvijit, R. Rallo, G. Orkoulas and Y. Cohen, *Environ. Sci. Technol.*, 2011, 45, 9284–9292.
- 62 D. Mukherjee, B. F. Leo, S. G. Royce, A. E. Porter, M. P. Ryan, S. Schwander, K. F. Chung, T. D. Tetley, J. Zhang and P. G. Georgopoulos, *J. Nanopart. Res.*, 2014, 16, 2616.
- 63 S. T. Johnston, M. Faria and E. J. Crampin, J. R. Soc., Interface, 2020, 17, 20200221.
- 64 L. Rodriguez-Lorenzo, B. Rothen-Rutishauser, A. Petri-Fink and S. Balog, *Part. Part. Syst. Charact.*, 2015, **32**, 321–333.
- 65 M. Braun, C. S. Coleman, D. A. Drew and W. F. Lucas, *Differential equation models*, Springer, 1983, vol. 1.
- 66 D. Zwillinger, *Handbook of differential equations*, Gulf Professional Publishing, 1998, vol. 1.
- 67 S. T. Johnston, M. J. Simpson and E. J. Crampin, *Proc. R. Soc. A*, 2020, 476, 20200089.
- 68 D. A. Lauffenburger and J. Linderman, *Receptors: models for binding, trafficking, and signaling*, Oxford University Press, 1993.
- 69 L. F. Shampine and M. W. Reichelt, SIAM Journal on Scientific Computing, 1997, 18, 1–22.
- 70 P. Virtanen, R. Gommers, T. E. Oliphant, M. Haberland, T. Reddy, D. Cournapeau, E. Burovski, P. Peterson, W. Weckesser, J. Bright, et al., Nat. Methods, 2020, 17, 261–272.
- 71 W. H. Press, H. William, S. A. Teukolsky, A. Saul, W. T. Vetterling and B. P. Flannery, *Numerical recipes 3rd edition: the art of scientific computing*, Cambridge University Press, 2007.
- 72 J. A. Nash, A. L. Kwansa, J. S. Peerless, H. S. Kim and Y. G. Yingling, *Bioconjugate Chem.*, 2017, 28, 3–10.
- 73 D. G. Kendall, Ann. Math. Stat., 1948, 19, 1-15.
- 74 P. Kolhar, A. C. Anselmo, V. Gupta, K. Pant, B. Prabhakarpandian, E. Ruoslahti and S. Mitragotri, *Proc. Natl. Acad. Sci. U. S. A.*, 2013, 110, 10753–10758.
- 75 I. Slabu, A. A. Roeth, U. M. Engelmann, F. Wiekhorst, E. M. Buhl, U. P. Neumann and T. Schmitz-Rode, *Nanotechnology*, 2019, 30, 184004.
- 76 O. Lunov, V. Zablotskii, T. Syrovets, C. Röcker, K. Tron, G. U. Nienhaus and T. Simmet, *Biomaterials*, 2011, 32, 547–555.
- 77 F. Bai and R. Sun, Biophys. Rev. Lett., 2019, 14, 75-99.
- 78 J. M. Chan, P. M. Valencia, L. Zhang, R. Langer and O. C. Farokhzad, *Cancer Nanotechnology*, Springer, 2010, pp. 163–175.

Review

79 G. Bachler, N. von Goetz and K. Hungerbühler, *Int. J. Nanomed.*, 2013, **8**, 3365.

- 80 G. Bachler, N. von Goetz and K. Hungerbuhler, *Nanotoxicology*, 2015, **9**, 373–380.
- 81 R. Chen and J. E. Riviere, Wiley Interdiscip. Rev.: Nanomed. Nanobiotechnol., 2017, 9, 1–31.
- 82 M. Li, K. T. Al-Jamal, K. Kostarelos and J. Reineke, ACS Nano, 2010, 4, 6303–6317.
- 83 M. Li, Z. Panagi, K. Avgoustakis and J. Reineke, *Int. J. Nanomed.*, 2012, 7, 1345.
- 84 D. Li, G. Johanson, C. Emond, U. Carlander, M. Philbert and O. Jolliet, *Nanotoxicology*, 2014, **8**, 128–137.
- 85 Z. Lin, N. A. Monteiro-Riviere and J. E. Riviere, *Nanotoxicology*, 2016, **10**, 162–172.
- 86 Z. Lin, N. A. Monteiro-Riviere, R. Kannan and J. E. Riviere, *Nanomedicine*, 2016, **11**, 107–119.
- 87 N. Hoshyar, S. Gray, H. Han and G. Bao, *Nanomedicine*, 2016, 11, 673-692.
- 88 J. Tan, S. Shah, A. Thomas, H. D. Ou-Yang and Y. Liu, *Microfluid. Nanofluid.*, 2013, 14, 77–87.
- 89 Y.-H. Cheng, C. He, J. E. Riviere, N. A. Monteiro-Riviere and Z. Lin, *ACS Nano*, 2020, **14**, 3075–3095.
- 90 D. M. Moss and M. Siccardi, *Br. J. Pharmacol.*, 2014, **171**, 3963–3979.
- 91 G. Bao and X. R. Bao, *Proc. Natl. Acad. Sci. U. S. A.*, 2005, **102**, 9997–9998.
- 92 P. Decuzzi and M. Ferrari, Biophys. J., 2008, 94, 3790-3797.
- 93 S. Zhang, H. Gao and G. Bao, ACS Nano, 2015, 9, 8655–8671.
- 94 L. Di Michele, P. K. Jana and B. M. Mognetti, *Phys. Rev. E*, 2018, 98, 032406.
- 95 Y.-H. Tseng and H. Huang, *J. Comput. Phys.*, 2014, 273, 143–159.
- 96 H. Deng, P. Dutta and J. Liu, *Biochim. Biophys. Acta*, 2018, **1862**, 2104–2111.
- 97 X. Yi, X. Shi and H. Gao, Phys. Rev. Lett., 2011, 107, 098101.
- 98 H. Tang, H. Zhang, H. Ye and Y. Zheng, *J. Appl. Phys.*, 2016, **120**, 114701.
- 99 X. Yi and H. Gao, Phys. Rev. E, 2014, 89, 062712.
- 100 X. Yi and H. Gao, Nanoscale, 2017, 9, 454-463.
- 101 X. Yi and H. Gao, ACS Biomater. Sci. Eng., 2017, 3, 2954–2961.
- 102 L. Li, Y. Zhang and J. Wang, Open Sci., 2017, 4, 170063.
- 103 X. Yi, X. Shi and H. Gao, Nano Lett., 2014, 14, 1049-1055.
- 104 M. Raatz, R. Lipowsky and T. R. Weikl, *Soft Matter*, 2014, **10**, 3570–3577.
- 105 H. Yuan and S. Zhang, Appl. Phys. Lett., 2010, 96, 033704.
- 106 O. Daumke, A. Roux and V. Haucke, Cell, 2014, 156, 882-892.
- 107 S. Morlot, V. Galli, M. Klein, N. Chiaruttini, J. Manzi, F. Humbert, L. Dinis, M. Lenz, G. Cappello and A. Roux, Cell, 2012, 151, 619–629.
- 108 C. Huang, Y. Zhang, H. Yuan, H. Gao and S. Zhang, *Nano Lett.*, 2013, **13**, 4546–4550.
- 109 R. Vácha, F. J. Martinez-Veracoechea and D. Frenkel, *Nano Lett.*, 2011, 11, 5391–5395.
- 110 J. R. Perilla, B. C. Goh, C. K. Cassidy, B. Liu, R. C. Bernardi, T. Rudack, H. Yu, Z. Wu and K. Schulten, *Curr. Opin. Struct. Biol.*, 2015, 31, 64–74.

- 111 M. Shamir, Y. Bar-On, R. Phillips and R. Milo, *Cell*, 2016, **164**, 1302.
- 112 Z. Shen, H. Ye, X. Yi and Y. Li, ACS Nano, 2018, 13, 215-228.
- 113 T. Yue and X. Zhang, ACS Nano, 2012, 6, 3196-3205.
- 114 K. Xiong, J. Zhao, D. Yang, Q. Cheng, J. Wang and H. Ji, *Soft Matter*, 2017, **13**, 4644–4652.
- 115 M. Ramezanpour, S. Leung, K. Delgado-Magnero, B. Bashe, J. Thewalt and D. Tieleman, *Biochim. Biophys. Acta, Biomembr.*, 2016, **1858**, 1688–1709.
- 116 G. Rossi and L. Monticelli, *Biochim. Biophys. Acta*, *Biomembr.*, 2016, **1858**, 2380–2389.
- 117 M. Shamsi, A. Mohammadi, M. K. Manshadi and A. Sanati-Nezhad, J. Controlled Release, 2019, 307, 150–165.
- 118 P. M. Hinderliter, K. R. Minard, G. Orr, W. B. Chrisler, B. D. Thrall, J. G. Pounds and J. G. Teeguarden, *Part. Fibre Toxicol.*, 2010, 7, 36.
- 119 S. M. Hussain, D. B. Warheit, S. P. Ng, K. K. Comfort, C. M. Grabinski and L. K. Braydich-Stolle, *Toxicol. Sci.*, 2015, **147**, 5–16.
- 120 G. M. DeLoid, J. M. Cohen, G. Pyrgiotakis, S. V. Pirela, A. Pal, J. Liu, J. Srebric and P. Demokritou, *Part. Fibre Toxicol.*, 2015, 12, 32.
- 121 N. Feliu, X. Sun, R. A. Alvarez Puebla and W. J. Parak, *Langmuir*, 2017, 33, 6639–6646.
- 122 R. Liu, H. H. Liu, Z. Ji, C. H. Chang, T. Xia, A. E. Nel and Y. Cohen, *ACS Nano*, 2015, **9**, 9303–9313.
- 123 D. Lichtenstein, T. Meyer, L. Böhmert, S. Juling, C. Fahrenson, S. Selve, A. Thünemann, J. Meijer, I. Estrela-Lopis, A. Braeuning and A. Lampen, *Langmuir*, 2017, 33, 13087–13097.
- 124 G. Oberdörster, E. Oberdörster and J. Oberdörster, *Environ. Health Perspect.*, 2005, **113**, 823.
- 125 G. Oberdörster, E. Oberdörster and J. Oberdörster, *Environ. Health Perspect.*, 2007, **115**, 290.
- 126 A. K. Pal, D. Bello, J. Cohen and P. Demokritou, *Nanotoxicology*, 2015, 9, 871–885.
- 127 U. Taylor, C. Rehbock, C. Streich, D. Rath and S. Barcikowski, *Nanomedicine*, 2014, **9**, 1971–1989.
- 128 J. G. Teeguarden, P. M. Hinderliter, G. Orr, B. D. Thrall and J. G. Pounds, *Toxicol. Sci.*, 2006, **95**, 300–312.
- 129 J. W. Wills, H. D. Summers, N. Hondow, A. Sooresh, K. E. Meissner, P. A. White, P. Rees, A. Brown and S. H. Doak, ACS Nano, 2017, 11(12), 11986–12000.
- 130 K. Wittmaack, Environ. Health Perspect., 2007, 115, 187.
- 131 R. A. Khanbeigi, A. Kumar, F. Sadouki, C. Lorenz, B. Forbes, L. A. Dailey and H. Collins, *J. Controlled Release*, 2012, **162**, 259–266.
- 132 R. Duffin, L. Tran, D. Brown, V. Stone and K. Donaldson, *Inhalation Toxicol.*, 2007, **19**, 849–856.
- 133 L. K. Limbach, Y. Li, R. N. Grass, T. J. Brunner, M. A. Hintermann, M. Muller, D. Gunther and W. J. Stark, *Environ. Sci. Technol.*, 2005, 39, 9370–9376.
- 134 G. Rischitor, M. Parracino, R. La Spina, P. Urbán, I. Ojea-Jiménez, E. Bellido, A. Valsesia, S. Gioria, R. Capomaccio, A. Kinsner-Ovaskainen, D. Gilliland, F. Rossi and P. Colpo, *Part. Fibre Toxicol.*, 2016, 13, 47.

Nanoscale Advances

- 135 T. Kowoll, S. Fritsch-Decker, S. Diabaté, G. U. Nienhaus, D. Gerthsen and C. Weiss, I. Nanobiotechnol., 2018, 16, 100.
- 136 D. G. Thomas, J. N. Smith, B. D. Thrall, D. R. Baer, H. Jolley, P. Munusamy, V. Kodali, P. Demokritou, J. Cohen and J. G. Teeguarden, Part. Fibre Toxicol., 2018, 15, 6.
- 137 E. C. Cho, Q. Zhang and Y. Xia, Nat. Nanotechnol., 2011, 6, 385.
- 138 J. Cui, M. Faria, M. Björnmalm, Y. Ju, T. Suma, S. T. Gunawan, J. J. Richardson, H. Heidari, S. Bals, E. J. Crampin and F. Caruso, Langmuir, 2016, 32, 12394-12402.
- 139 G. DeLoid, J. M. Cohen, T. Darrah, R. Derk, L. Rojanasakul, G. Pyrgiotakis, W. Wohlleben and P. Demokritou, Nat. Commun., 2014, 5, 3514.
- 140 V. Hirsch, C. Kinnear, L. Rodriguez-Lorenzo, C. A. Monnier, B. Rothen-Rutishauser, S. Balog and A. Petri-Fink, Nanoscale, 2014, 6, 7325-7331.
- 141 A. Spyrogianni, I. K. Herrmann, M. S. Lucas, J.-C. Leroux and G. A. Sotiriou, Nanomedicine, 2016, 11, 2483-2496.
- 142 S. R. Price, C. Kinnear and S. Balog, Nanoscale, 2019, 11, 5209-5214.
- 143 A. Spyrogianni, G. A. Sotiriou, D. Brambilla, J.-C. Leroux and S. E. Pratsinis, J. Aerosol Sci., 2017, 108, 56-66.
- 144 C. Y. Watson, G. M. DeLoid, A. K. Pal and P. Demokritou, Small, 2016, 12, 3172-3180.
- 145 E. J. Petersen, A. R. M. Bustos, B. Toman, M. E. Johnson, M. Ellefson, G. C. Caceres, A. L. Neuer, Q. Chan, J. W. Kemling, B. Mader, K. Murphy and M. Roesslein, Environ. Sci.: Nano, 2019, 6, 2876-2896.
- 146 T. Schneider, M. Westermann and M. Glei, Colloids Surf., A, 2020, 601, 125026.
- 147 J. Cohen, G. DeLoid, G. Pyrgiotakis and P. Demokritou, Nanotoxicology, 2013, 7, 417-431.

- 148 G. Sharma, V. Kodali, M. Gaffrey, W. Wang, K. R. Minard, N. J. Karin, J. G. Teeguarden and B. D. Thrall, Nanotoxicology, 2014, 8, 663-675.
- 149 T. L. Moore, L. Rodriguez-Lorenzo, V. Hirsch, S. Balog, D. Urban, C. Jud, B. Rothen-Rutishauser, M. Lattuada and A. Petri-Fink, Chem. Soc. Rev., 2015, 44, 6287-6305.
- 150 T. L. Moore, D. A. Urban, L. Rodriguez-Lorenzo, A. Milosevic, F. Crippa, M. Spuch-Calvar, S. Balog, B. Rothen-Rutishauser, M. Lattuada and A. Petri-Fink, Sci. Rep., 2019, 9, 1-9.
- 151 C. Grabinski, M. Sharma, E. Maurer, C. Sulentic, R. Mohan Sankaran and S. Hussain, Nanotoxicology, 2016, 10, 74-83.
- 152 L. Böhmert, L. König, H. Sieg, D. Lichtenstein, N. Paul, A. Braeuning, A. Voigt and A. Lampen, Part. Fibre Toxicol.,
- 153 Bionano Interaction Kinetics Estimator, accessed: 2020-09-04, http://bionano.xyz/estimator.
- 154 J. C. G. Jeynes, C. Jeynes, M. J. Merchant and K. J. Kirkby, Analyst, 2013, 138, 7070-7074.
- 155 T. Turnbull, M. Douglass, N. H. Williamson, D. Howard, R. Bhardwaj, M. Lawrence, D. J. Paterson, E. Bezak, B. Thierry and I. M. Kempson, ACS Nano, 2019, 13, 5077-5090.
- 156 M. Faria, M. Björnmalm, K. J. Thurecht, S. J. Kent, R. G. Parton, M. Kavallaris, A. P. Johnston, J. J. Gooding, S. R. Corrie, B. J. Boyd, et al., Nat. Nanotechnol., 2018, 13, 777-785.
- 157 S. Ashraf, A. Hassan Said, R. Hartmann, M.-A. Assmann, N. Feliu, P. Lenz and W. J. Parak, Angew. Chem., Int. Ed., 2020, 59, 5438-5453.
- 158 S. K. Mann, E. Czuba, L. I. Selby, G. K. Such and A. P. Johnston, Pharm. Res., 2016, 33, 2421-2432.
- 159 L. I. Selby, L. Aurelio, D. Yuen, B. Graham and A. P. Johnston, ACS Sens., 2018, 3, 1182-1189.