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The impact of site selectivity and disorder on the thermoelectric properties of $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ solid solutions: $\text{Yb}_{21}\text{Mn}_{4-x}\text{Cd}_x\text{Sb}_{18}$ and $\text{Yb}_{21-y}\text{Ca}_y\text{Mn}_4\text{Sb}_{18}$ [†]

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Thermoelectric materials can convert heat into electricity. They are used to generate electricity when other power sources are not available or to increase energy efficiency by recycling waste heat. The $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ phase was previously shown to have good thermoelectric performance due to its large Seebeck coefficient ($\sim 290 \mu\text{V K}^{-1}$) and low thermal conductivity ($0.4 \text{ W m}^{-1} \text{ K}^{-1}$). These characteristics stem respectively from the unique $[\text{Mn}_4\text{Sb}_{10}]^{22-}$ subunit and the large unit cell/site disorder inherent in this phase. The solid solutions, $\text{Yb}_{21}\text{Mn}_{4-x}\text{Cd}_x\text{Sb}_{18}$ ($x = 0, 0.5, 1.0, 1.5$) and $\text{Yb}_{21-y}\text{Ca}_y\text{Mn}_4\text{Sb}_{18}$ ($y = 3, 6, 9, 10.5$) have been prepared, their structures characterized and thermoelectric properties from room temperature to 800 K measured. A detailed look into the structural disorder for the Cd and Ca solid solutions was performed using synchrotron powder X-ray diffraction and pair distribution function methods and shows that these are highly disordered structures. The substitution of Cd gives rise to more metallic behavior whereas Ca substitution results in high resistivity. As both Cd and Ca are isoelectronic substitutions, the changes in properties are attributed to changes in the electronic structure. Both solid solutions show that the thermal conductivities remain extremely low ($\sim 0.4 \text{ W m}^{-1} \text{ K}^{-1}$) and that the Seebeck coefficients remain high ($> 200 \mu\text{V K}^{-1}$). The temperature dependence of the carrier mobility with increased Ca substitution, changing from approximately T^{-1} to $T^{-0.5}$, suggests that another scattering mechanism is being introduced. As the bonding changes from polar covalent with Yb to ionic for Ca, polar optical phonon scattering becomes the dominant mechanism. Experimental studies of the Cd solid solutions result in a max zT of ~ 1 at 800 K and, more importantly for application purposes, a $zT_{\text{avg}} \sim 0.6$ from 300 K to 800 K.

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Introduction

Thermoelectric materials can provide a clean energy alternative when employed in a device to regenerate electrical power from waste heat. These devices are inherently renewable and environmentally friendly making them an enticing alternative to fossil fuels. Wide-scale application of thermoelectrics and commercialization is currently being held back by modest

device conversion efficiency.¹ Efficiencies can be improved by developing new and better materials² and/or through engineering considerations. The thermal to electrical conversion efficiency of a thermoelectric material is described by the figure of merit $zT = \frac{\alpha^2 T}{\rho \kappa}$ where α is the Seebeck coefficient, T is the temperature, ρ is the electrical resistivity, and κ is the thermal conductivity. To be an efficient thermoelectric material, low thermal conductivity, low resistivity, and high Seebeck coefficient are required to maximize the figure of merit, zT . The simultaneous optimization of these parameters (α , ρ , κ) is a naturally conflicting goal because of their interconnected relationship with the charge carrier concentration (n) of the material. This has led to many different strategies for optimization in the thermoelectric community. One common avenue is to first start from intrinsically low thermal conductivity materials (those with large unit cells) to provide a good starting point for optimization. One class of low thermal conductivity materials can be identified as charge-balanced and semiconducting Zintl compounds. The type of bonding in Zintl

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compounds can fall anywhere in between ionic, covalent, or metallic and because of this flexibility, one may imagine that a large number of unique and undiscovered compounds are possible. The subset of Zintl phases with complex unit cells gives rise to more phonon modes leading to increased phonon scattering and lower thermal conductivity. Examples of such materials include $\text{Yb}_{14}\text{MnSb}_{11}$,^{3,4} Zn–Sb phases,^{5–7} and $\text{Ti}_2\text{Ag}_{12}\text{Te}_{7+\delta}$.⁸ Other optimization strategies include: electronic structure modification (*e.g.* increasing the density of states (DOS) near the Fermi level) either through substitutional doping demonstrated in PbTe ,⁹ defect control,¹⁰ and nanostructuring/compositing for decreased thermal conductivity¹¹ or improved electronic and mechanical properties.¹²

Our previous study on the parent $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ (referred to as 21-4-18) compound showed that extremely low values of thermal conductivity ($\sim 0.4 \text{ W m}^{-1} \text{ K}^{-1}$)¹³ can be achieved due to the complex structural disorder inherent within the system.^{13,14} Paired with a high Seebeck coefficient ($\sim 290 \mu\text{V K}^{-1}$) given largely from the unique $[\text{Mn}_4\text{Sb}_{10}]^{22-}$ anion substructure, the intrinsic phase without any optimization shows a peak zT of ~ 0.75 at 800 K. Optimization of this compound was achieved through carrier concentration manipulation with the doping of sodium into the structure, increasing the maximum zT to ~ 0.8 and ZT_{avg} from 0.34 to 0.49 over the entire temperature range (300–800 K).¹³ Here, the term ZT_{avg} refers to the average zT across

the specified temperature range calculated from the integration method.¹⁵ Sodium doping improves the ZT_{avg} and brings the thermoelectric compatibility factor(s) of the 21-4-18 phase closer to other top performing thermoelectric materials making it more desirable for practical applications.¹³ Since thermoelectric devices depend on segmentation of different materials, maximal efficiencies are only achieved if the compatibility factors of said materials are similar.

$\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ can be understood using a Zintl formalism of electron counting. The unit cell ($Z = 4$) (Fig. 1) contains 1 linear $[\text{Mn}_4\text{Sb}_{10}]^{22-}$ anion, 2 dumbbell $[\text{Sb}_2]^{4-}$ anions, 4 isolated Sb^{3-} anions, and 21 Yb^{2+} cations making it charge-balanced.

Building on our previous work, herein we present the structure and thermoelectric properties of the $\text{Yb}_{21}\text{Mn}_{4-x}\text{Cd}_x\text{Sb}_{18}$ ($x = 0, 0.5, 1.0, 1.5$) and $\text{Yb}_{21-y}\text{Ca}_y\text{Mn}_4\text{Sb}_{18}$ ($y = 3, 6, 9, 10.5$) solid solutions. Although both Cd and Ca can be considered to be 2+ and therefore substitute isoelectronically for Mn^{2+} and Yb^{2+} respectively, the physical properties change drastically and cannot be explained using electron counting rules. Instead, it is necessary to consider how each solid solution changes the electronic structure to rationalize the physical properties that emerge for each solid solution. $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ is a half metallic compound with Mn^{2+} having a half filled d band.¹³ Cd was chosen as it has a filled d orbital and as such was expected to remove the half metallicity to

Fig. 1 (a) Unit cell of the $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ structure ($a = 16.930(3) \text{ \AA}$, $b = 17.029(3) \text{ \AA}$, $c = 16.693(3) \text{ \AA}$, $\beta = 92.61(3)^\circ$, $C2/c$) viewed down the c -axis.¹³ Yb atoms represented in grey, Mn atoms in light green, and Sb atoms in dark green. (b) Polyhedral view of the $[\text{Mn}_4\text{Sb}_{10}]^{22-}$ tetramer stacking shown along the (111) direction, without atoms for clarity. (c) Inter-tetramer coordination shown parallel to the b -axis.

improve the electrical transport. Ca substitution was expected to increase electron donation to the clusters and thereby increase the Seebeck coefficients further. The Cd substitution in general makes the 21-4-18 phase more metallic while Ca has the opposite effect. In particular, introduction of the ionic Ca species reveals that the dominant carrier scattering mechanism can be tuned in Zintl phases and thereby providing a new avenue for thermoelectric properties optimization. The introduction of Cd and Ca into the 21-4-18 system shows the high flexibility and tunability of this structure type. This study focuses on isovalent substitutions on the A and M site in the $A_{21}M_4Pn_{18}$ system (where A is a 2+ rare-earth metal or alkali-earth element, M is a transition metal, and Pn is a pnictogen). The observed change in the physical properties for each solid solution is therefore only due to changes in the electronic band structure topology and not a combination of changes in band structure and carrier concentration as would be the case from aliovalent doping studies.

Experimental section

Synthesis

The polycrystalline $Yb_{21}Mn_{4-x}Cd_xSb_{18}$ ($x = 0.5, 1.0, 1.5$) and $Yb_{21-y}Ca_yMn_4Sb_{18}$ ($y = 3, 6, 9, 10.5$) samples were successfully synthesized using ball-milling and sintering processes, similar to that described previously.¹³ Attempts to synthesize the $x = 2.0$ sample resulted in the presence of $Yb_{11}Sb_{10}$ impurity; therefore, the maximum composition of $x = 1.5$ was investigated. The Yb filings (Metall Rare Earth Limited, 99.99%), Ca pieces (Sigma Aldrich, 99.99%) Mn pieces (Alfa Aesar, 99.95%), Cd shots (Alfa Aesar, 99.95%) and Sb shots (Alfa Aesar, 99.999%) were loaded into a stainless steel ball-mill (50 mL vial using 3 stainless steel 0.5" balls) under Ar atmosphere (< 1 ppm H_2O) in their appropriate stoichiometries (10 g total mass), and sealed inside a Mylar bag. The contents were milled for 1 h in a SPEX 8000 M High-Energy ball mill. For additional homogeneity, the resulting powder was ground thoroughly under Ar atmosphere, resealed in a Mylar bag, and subsequently milled for an additional hour. The mixture was then placed into 8 cm long Nb tubes, crimped and welded in an arc welder under partial Ar pressure, and jacketed in a fused silica tube under vacuum. The reaction was heated to 650 °C (100 °C h^{-1}), sintered for 7 days, and allowed to slowly cool down to room temperature.

Densification of the powders for physical property measurements was done using spark plasma sintering (SPS) using a Dr Sinter SPS-2050 system. Approximately 2–3 g of material was sieved through a 200 mesh filter and loaded into a 12.7 mm graphite die. The SPS chamber was evacuated until < 12 Pa and an initial pressure of 6 kN was applied to the die. The mixture was heated to 535 °C in 6 minutes, heated to 585 °C in 1 minute, followed by 45 minutes of dwell time. The pressure was adjusted monotonically to 11 kN upon compression of the mixture. All pellets obtained were $> 95\%$ dense (Archimedes' method) from this method.

Synchrotron powder X-ray diffraction

Synchrotron powder X-ray diffraction data were collected at the Argonne National Laboratory using the 11-BM beamline of the Advanced Photon Source (APS), Argonne National Laboratory. The samples were placed into Kapton capillaries, sealed with epoxy and the scattering data collected in transmission mode. Because of the highly absorbing nature of the samples, the powders were diluted with SiO_2 until $\mu R \approx 1$. A wavelength of $\lambda = 0.457884$ Å was used and the data were measured at room temperature. A comparison was completed with Rietveld refinement using the 11 BM data with our previously reported structure¹³ and a more recently reported disordered structural model of 21-4-18.¹⁴ The recently published model contains more independent parameters¹⁴ and yielded a slightly lower R_{wp} value of ~ 5.9 compared to our previous model which obtained a R_{wp} value of ~ 6.1 . The atomic positions and atomic displacement parameters of both models were refined.

Pair distribution function

Synchrotron X-ray total scattering measurements on the $Yb_{21}Mn_{4-x}Cd_xSb_{18}$ ($x = 0, 0.5, 1.0, 1.5$) and $Yb_{21-y}Ca_yMn_4Sb_{18}$ ($y = 3, 6, 9, 10.5$) samples were carried out at 11-ID-B beamline ($\lambda = 0.2115$ Å) at the Advanced Photon Source, Argonne National Laboratory using a 2D plate detector. The powders were sealed inside polyimide capillaries using epoxy and the data were collected at room temperature. The data images were analyzed using General Structure Analysis System-II (GSAS-II) program¹⁶ where they were azimuthally integrated, resulting in a 1D pattern. The experimental parameters were calibrated using CeO_2 as the standard material. The pair distribution functions (PDFs) were obtained through the PDFgetX3 software¹⁷ using a Q_{max} of 23.47 Å⁻¹ and were corrected for background diffraction from the air/capillary. The $G(r)$ functions were modelled with the PDFgui software¹⁸ using the results from Rietveld refinement of the powder X-ray synchrotron data as starting parameters. Overall, the lattice parameters, atomic displacement parameters (ADPs) and atomic positions were refined. Reverse Monte Carlo (RMC) fitting of the PDFs was done with RMCprofile software¹⁹ using a $8 \times 8 \times 8$ supercell (88 064 atoms). The simulations were constrained with bond valence sum rules in order to keep the model chemically sound. A minimum distance restraint was applied to prevent any unreasonably short atomic pairs. Convergence was achieved after approximately 100 h on a standard PC. The resultant structural model from RMC was tested on 11 BM powder data using Rietveld refinement and resulted in a slightly higher R value (5.908 vs. 5.833 originally), as expected since the RMC model captures local structural features.

Thermoelectric property measurements

A Linseis LSR-3 instrument was used for resistivity and Seebeck coefficient measurements using the 4-probe method from 350 K to 800 K under He atmosphere. Samples were cut into bars (~ 10 mm $\times$ 2 mm $\times$ 2 mm) and measured using 8 mm probes. Many samples were measured to ensure reproducibility

of the data and were cross-checked by measurements at the Jet Propulsion Laboratory (JPL). The Seebeck coefficient measured at JPL employed a light pulse technique with W/Nb thermocouples.²⁰ A custom system (4-point probe) was used to measure the electrical resistivity and Hall voltage simultaneously under dynamic vacuum, from which, the carrier density and mobility were derived.²¹

Thermal diffusivity (D) was measured using a Netzsch LFA 457 instrument under vacuum up to 800 K. The sample disks were polished flat and an even graphite coating was applied. The heat capacity (C_p) was estimated using the Dulong–Petit method, and the density (d) was measured by Archimedes' method. The thermal conductivity (κ) was then calculated using the formula $\kappa = DdC_p$.

Compositional analysis

The samples were mounted in epoxy and polished to a smooth, flat surface. Elemental analysis was carried out using energy dispersive spectroscopy (EDS) using a FEI Scios DualBeam SEM/FIB with a window-less Oxford Instruments X-max50, 50 mm² silicon drift detector. Backscattered electron images

were collected with an accelerating voltage of 20 kV and a current of 1.6 nA.

Results and discussion

Crystal structure

The synchrotron powder X-ray diffraction patterns (Fig. 2) of all the prepared polycrystalline samples ($x = 0, 0.5, 1.0, 1.5$) and $y = 3.0, 6.0, 9.0, 10.5$) remain in the monoclinic $C2/c$, α -Ca₂₁Mn₄Sb₁₈ structure type. No impurity phases were apparent in either the Cd or Ca solid solution series. During Rietveld refinement, the relative Mn/Cd and Yb/Ca occupancies were allowed to refine freely on each of the 4 Mn/Cd sites and the 11 Yb/Ca sites that converged to values close to nominal loading composition (see ESI† (Tables S1 and S2)). Subsequent refinements constrained the total Mn/Cd and Yb/Ca occupancies to the nominal composition, with little to no change in R_{wp} (see ESI† (Tables S1 and S2)). Substitution of the transition metal site (Mn) with Cd was found to exhibit site preference within the [Mn₄Sb₁₀]^{22−} tetramer chain, where the Cd atoms prefer to

Fig. 2 Synchrotron powder X-ray diffraction data collected at room temperature for (a) Yb₂₁Mn_{4-x}Cd_xSb₁₈ ($x = 0, 0.5, 1.0, 1.5$) and (b) Yb_{21-y}Ca_yMn₄Sb₁₈ ($y = 3.0, 6.0, 9.0, 10.5$) with $\lambda = 0.457884$ Å. (c) A representative Rietveld refinement for sample Yb₂₁Mn_{2.5}Cd_{1.5}Sb₁₈ where data are shown in black, calculated fit in red, difference in grey, and Bragg reflections in blue. Rietveld refinement parameters and results can be found in ESI† (Tables S1 and S2).

Fig. 3 Percent site occupancies of the (a) Cd series ($\text{Yb}_{21}\text{Mn}_{4-x}\text{Cd}_x\text{Sb}_{18}$, $x = 0.5, 1.0, 1.5$) and (b) Ca series ($\text{Yb}_{21-y}\text{Ca}_y\text{Mn}_4\text{Sb}_{18}$, $y = 3.0, 6.0, 9.0, 10.5$) determined from Rietveld refinement of synchrotron X-ray powder diffraction data.

reside on the terminal sites (Mn1/Cd1 and Mn4/Cd4) of the tetramer unit and the Mn atoms prefer to occupy the central two sites (Mn2/Cd2 and Mn3/Cd3) within the tetramer (see Fig. 3a). In fact, the Mn2 site is completely devoid of Cd for the compositions investigated. We believe that the Cd site preference for the terminal sites of the tetramer unit arise from their intrinsically softer, longer bonds. The terminal sites are directly next to an octahedrally coordinated Yb atom (Yb11) which has previously been shown to exhibit rattling and disorder¹³ and the softer bonds of the Cd atoms would be more accommodating of any local distortions on the octahedral site. Additionally, a comparison of the (Mn, Cd)–(Mn, Cd) distances within the tetramer chain reveal that the Mn2–Mn3/Cd3 bond distance is the shortest among all the TM–TM bonds in the tetramer unit. It is reasonable to expect that the Mn atoms would prefer to sit on the two sites that are closest to each other to give rise to the strongest exchange coupling. With additional Cd doping, the tetramer structure evolves such that the Mn1/Cd1 atom begins to segregate away from the other atoms (*i.e.* Mn1/Cd1–Mn2

distance increases from 3.64(3) Å to 4.004(2) Å for $x = 0$ and $x = 1.5$, respectively) while the total length of the tetramer chain remains relatively constant (*i.e.* Mn1/Cd1–Mn4/Cd4 distance ranges from 8.74(3) Å to 8.724(2) Å for $x = 0$ and $x = 1.5$, respectively).

Substituting Ca on the rare earth site (Yb) did not result in any site preference (see Fig. 3b). Overall, the Ca atoms are spread fairly evenly on all of the 11 sites which is probably due to the similarity in their 6-coordinate ionic radii (Ca: 1.00 Å *vs.* Yb: 1.02 Å) and bonding. The lack of site preference for the Ca atoms has been previously observed in the $\text{Yb}_{14-x}\text{Ca}_x\text{MnSb}_{11}$ system.²²

Pair distribution function

Small box modelling. Fig. 4a shows the experimental pair distribution functions for the Cd and Ca solid solution series. The peaks that show up in the $G(r)$ are broad, indicative of the large number of atoms (and atom pairs) in the unit cell. The model obtained from Rietveld refinement of the X-ray

Fig. 4 (a) Pair distribution functions ($G(r)$) of $\text{Yb}_{21}\text{Mn}_{4-x}\text{Cd}_x\text{Sb}_{18}$ ($x = 0, 0.5, 1.0, 1.5$, black, purple, blue, teal respectively) and $\text{Yb}_{21-y}\text{Ca}_y\text{Mn}_4\text{Sb}_{18}$ ($y = 3.0, 6.0, 9.0, 10.5$, red, orange, gold, brown respectively) within an r range of 1.5–20 Å. (b) The $G(r)$ fit for $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ up to $r = 70$ Å. Data are given by black dots, fit is provided in red, and the difference in blue.

synchrotron data was used as a starting point in the PDF refinements. Analysis was completed up to a $r_{\max} = 70 \text{ \AA}$, a range of approximately 4 unit cell lengths from the origin, and thus this study is focused on the local to intermediate structural regime (Fig. 4b shows a representative fit for $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ with $r_{\min} = 1.5 \text{ \AA}$ and $r_{\max} = 70 \text{ \AA}$). Any peaks in the $G(r)$ less than $1.5 \text{ \AA}$ were considered to be unphysical and was chosen as the lower bound (*i.e.* $r_{\min}$) for analysis. The lattice constants, atomic displacement parameters (ADP), and atomic positions were refined. Refinements of site occupancy did not converge and led to unphysical values. For the ADP refinement, each individual element (*i.e.* Yb, Mn, Sb) was assigned one ADP to avoid over parameterization regardless of their different crystallographic sites. The results from fitting the $G(r)$ with $r_{\min} = 1.5 \text{ \AA}$ to an incrementally increasing $r_{\max}$ up to $r_{\max} = 70 \text{ \AA}$, is shown in the ESI† (Fig. S1 and S2). The results obtained from Rietveld refinement were used as a starting model for the PDF refinement. The unit cell parameters and ADP start to converge close to the values obtained from Rietveld refinement after approximately $35 \text{ \AA}$ (see ESI† Fig. S1 and S2), corresponding to a length of approximately two unit cells. The converged values from the small box PDF refinement are extremely close to that obtained from Rietveld refinement (see Fig. 5).

Both the lattice parameter and unit cell volume obtained from the Rietveld refinements and PDF refinements follow the same trend. With increasing Cd substitution, lattice parameters a and c both increase while b decreases, resulting in an overall increase in unit cell volume from $x = 0$ to $x = 1.5$. For the Ca solid solution series, there is a similar trend. Lattice parameters a and c both increase, while b stays relatively the same resulting in the unit cell volume increase across the series.

To directly see the contribution of individual atom–atom pairs to the pair distribution function, the partial pair distribution function curves were plotted in Fig. 6 for the parent ($x = 0$) $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ sample. The overall PDF ($G(r)$) is obtained by summing all the partial PDFs ($G(r)$) with appropriate weighting coefficients, *i.e.* $G(r) = \sum_{i,j} c_i c_j b_i b_j (g_{ij}(r) - 1)$. The contribution of a particular atom pair depends upon the concentration of the particular atom (c_i, c_j) and the scattering factor (b_i, b_j). Because Yb and Sb make up most of the formula unit in this system (large c), and since Yb and Sb have larger scattering factors in comparison to Mn, the largest atom–atom pair contributions to $G(r)$ are from the Yb–Yb, Yb–Sb, Sb–Sb pairs.

Fig. 5 Lattice parameters and unit cell volume obtained from Rietveld refinement (filled circles) of the X-ray synchrotron data and the small box modelling (open circles) of total scattering X-ray synchrotron data ($G(r)$ with $r_{\max} = 70 \text{ \AA}$, see ESI† (Tables S3 and S4)). (a and c) Lattice parameters and unit cell volume of Cd solid solution. (b and d) Lattice parameters and unit cell volume of the Ca solid solution.

Fig. 6 Partial pair distribution functions for $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ ($x = 0$) to deconvolute the contribution of each atom–atom pair to the total pair distribution function.

Reverse Monte Carlo (RMC) modelling. After the small box modelling, we turned to RMC or “big box” modelling, because it is not restricted by symmetry and hence can better capture any short-range order present in the samples. In the RMC simulations, an initial configuration of atoms is modified through successive steps until the obtained model is in agreement with the experimental data using a Monte Carlo algorithm. The changes to the structure are proposed as random and then tested to see if there is an improvement in the fitting. If the change results in a better fit, it is accepted. If the change results in a worse fit, the change is accepted according to a probability algorithm. By accepting “bad” changes, this method of fitting prevents getting stuck in local minimum states. Bond valence sum restrictions were set in order to keep the model chemically sound and to avoid any unphysical bond lengths.

The $G(r)$ function was modelled according to an $8 \times 8 \times 8$ supercell for all the different compositions (Fig. 7a). For the solid solutions, the Cd and Ca atoms were randomly distributed among their respective sites for the initial configuration prior to refinement. During the refinement, the Mn and Cd atoms were allowed to swap places with equal probability for the Cd solid solutions, and similarly, the Yb and Ca atoms were allowed to swap with equal probability for the Ca solid solutions.

An excellent fit over the whole r range of the PDF is obtained (Fig. 7b) given the small supercell that was used. For visualization, the distribution of the atomic positions in the $8 \times 8 \times 8$ supercell were superimposed onto a single unit cell (*i.e.* point cloud distributions, Fig. 8a) for $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ and the two most highly substituted samples of Cd and Ca (Fig. 8b, and c). There are two structural models for $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ based on single crystal data^{13,14} and both give rise to similar Rietveld refinements of the data, as noted above. The RMC model cannot support or discard either of these models because the aforementioned models are based on long range ordering in single crystal samples while the current analysis is looking at local ordering in powder samples.

The results from the RMC modeling suggest a highly disordered structure that is unique and separate from the average model obtained through Rietveld refinement. Fig. 9 shows the site occupations of Cd and Ca substituted samples obtained from the RMC simulations. The simulations show that there is some degree of site preference for both the Ca and Cd atoms in the local structure that is distinct from the average structure.

For example, in the $x = 1.5$ sample, the Cd atoms populate the Mn2/Cd2 site and Mn3/Cd3 site the most, whereas in the Rietveld refinement, Cd atoms reside on the terminal Mn1/Cd1 and Mn4/Cd4 sites the most (refer back to Fig. 3). Additionally, in the Ca solid solutions, Rietveld refinement showed that the Ca atoms were roughly evenly distributed across all 11 Yb sites while the RMC simulations show some degree of site

Fig. 7 (a) Refined supercell ($8 \times 8 \times 8$) for $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ after RMC simulations. (b) The $G(r)$ fit obtained from RMC modelling. The finite size of the supercell is apparent from the $r_{\text{max}} \approx 67$ Å. Data are shown by black dots, fit curve is the red solid line, and the difference is shown by the blue solid line.

Fig. 8 Point cloud distributions of (a) $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$ (b) $\text{Yb}_{21}\text{Mn}_{2.5}\text{Cd}_{1.5}\text{Sb}_{18}$ (c) $\text{Yb}_{10.5}\text{Ca}_{10.5}\text{Mn}_4\text{Sb}_{18}$ showing cation site and transition metal site occupations from RMC simulations. Yb atoms are in gray, Mn atoms in light green, Sb atoms in dark green, Cd atoms in blue, and Ca atoms in red. Other point cloud distributions can be found in ESI,† Fig. S3.

Fig. 9 Percent site occupancies of the (a) Cd series ($\text{Yb}_{21}\text{Mn}_{4-x}\text{Cd}_x\text{Sb}_{18}$, $x = 0.5, 1.0, 1.5$) and (b) Ca series ($\text{Yb}_{21-y}\text{Ca}_y\text{Mn}_4\text{Sb}_{18}$, $y = 3.0, 6.0, 9.0, 10.5$) determined from RMC simulations of synchrotron total X-ray scattering data.

preference. To verify whether or not these results are local structural features, further simulations were performed. The final structural model for $y = 10.5$ was chosen as a representative sample and was allowed to randomly swap the Yb and Ca atoms with absolute probability for more than 12 h. The resultant structure (and fit) was compared to the model prior to swapping which resulted in a substantially worse agreement with the experimental data (see ESI,† Fig. S4) providing additional evidence of the local ordering. From the total scattering experiments, it is clear that there are local structural features on the nanoscale domain that are missed by the Rietveld refinement. These domains are approximately ~ 70 Å long with no obvious signs of long range order that could be observed within the $8 \times 8 \times 8$ supercell model.

Compositional analysis

All the samples after the SPS process were $>95\%$ dense. Backscattered electron images of a representative polished pellet surface of $x = 0.5$ is shown in Fig. 10. The compositions of all the samples were found to be within approximately 1 at% of the nominal stoichiometry (see ESI,† Table S5) according to

EDS. Since the Ca K-edge (4.0381 keV) overlaps heavily with the Sb L-edges (L-I edge: 4.6983 keV, L-II edge: 4.3804 keV, L-III edge: 4.1322 keV), quantification of the Ca amount in the Ca solid solution samples was not reliable using EDS. Instead, we refer the reader to the refined compositions obtained *via* synchrotron powder X-ray diffraction data (see ESI,† Table S2).

Electronic transport properties

Fig. 11a shows the temperature dependent Hall measurements for the Cd-substituted series yielding a large carrier concentration (cc) of $n_{\text{H}} > 1 \times 10^{20} \text{ h}^+ \text{ cm}^{-3}$ for all samples. Although the isoelectronic substitution of Cd^{2+} with Mn^{2+} is not expected to change the carrier concentration from basic electron counting, the cc can be seen to steadily increase with Cd substitution. Since Cd is more electronegative than Mn, it will provide a more incomplete electron transfer to the anions to yield a higher p-type cc for the solid solutions. Stated another way, the larger electronegativity of Cd will result in lower energy atomic orbitals compared to Mn (Koopmans' Theorem)²³ providing more states for the holes to occupy, leading to a larger cc. The increase in cc with Cd content is reflected in the electrical resistivity data

Fig. 10 Representative backscattered electron images from a dense pellet of $\text{Yb}_{21}\text{Mn}_{4-x}\text{Cd}_x\text{Sb}_{18}$ ($x = 0.5$) collected with 20 kV electron beam (left) and elemental mapping (right). Images of other Cd solid solutions can be found in ESI† (Fig. S5 and S6).

Fig. 11 Transport properties of $\text{Yb}_{21}\text{Mn}_{4-x}\text{Cd}_x\text{Sb}_{18}$ ($x = 0, 0.5, 1.0, 1.5$). (a) Hall carrier concentration (n_H), (b) resistivity (ρ), (c) Hall mobility (μ_H), (d) Seebeck coefficient (α). See ESI† for Pisarenko plot (Fig. S7).

(Fig. 11b). All samples show metallic behaviour with increasing temperature before transitioning into semiconducting behaviour above 600 K. There is a peak in resistivity at about 600 K that shifts to higher temperatures with additional Cd content signaling

an increase in the band gap. The Hall mobility is shown in Fig. 11c and stays relatively constant with the additional Cd doping. The Seebeck coefficient (Fig. 11d) steadily decreases with Cd content because of the increase in cc and is

consistent with the temperature dependence of the electrical transport data.

The thermoelectric transport properties for the Ca solid solution series are shown in Fig. 12. With additional Ca substitution, the carrier density decreases accordingly, dropping an order of magnitude from $\sim 1 \times 10^{20} \text{ h}^+ \text{ cm}^{-3}$ ($y = 0$) to $\sim 2 \times 10^{19} \text{ h}^+ \text{ cm}^{-3}$ ($y = 10.5$) at room temperature. Since Ca^{2+} is more ionic than Yb^{2+} and less electronegative, samples with more Ca will donate more e^- density into the system lowering the hole carrier concentration. As Ca is incorporated, Yb f states near the Fermi level are removed. The loss of these Yb states results in the observed decrease in carrier concentration as there are less places for the holes to populate the valence band. In addition to the drop in cc, the cc slope is also increased for the Ca-substituted samples compared to the parent ($x = 0$) sample. The electrical resistivity increases with Ca content and shows an exponential increase in the room temperature value. The high temperature slope-change of the electrical resistivity (similar to the Cd series) shifts to higher temperature with Ca content and marks the point of minority carrier activation or bipolar conduction, consistent with the temperature dependence of the cc. The carrier mobility decreases steadily with additional Ca content and decreases its temperature dependence from approximately T^{-1} to $T^{-0.5}$. The temperature dependence of

mobility is a combination of all the different scattering mechanisms at play, but is usually dominated by acoustic phonon scattering at high T which will yield $T^{-1.5}$ for nondegenerate semiconductors and T^{-1} for degenerate systems.²⁴ The gradual shift in temperature dependence to $T^{-0.5}$ with increased Ca substitution suggests that another scattering mechanism is being introduced. As the material becomes more polar with Ca substitution, the lattice becomes more polarizable, increasing the degree of electron-phonon interaction (*i.e.* Fröhlich constant (α)) to make polar optical phonon scattering the dominant mechanism²⁵ and suggests polaron formation. Compared to $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$, the $y = 3$ sample experiences an initial drop in Seebeck which may be due to the loss in Yb f states, before increasing with additional Ca content.

Thermal transport properties

Thermal conductivities were calculated from measurements of thermal diffusivity using eqn (1):

$$\kappa = DdC_p \quad (1)$$

where D is thermal diffusivity, d is the sample density, and C_p is the heat capacity. The Dulong–Petit law was used to estimate the heat capacity. The total thermal conductivity (κ) can be expressed as the sum of the lattice (κ_{lat}) and electronic (κ_e) contributions ($\kappa = \kappa_{\text{lat}} + \kappa_e$).

Fig. 12 Transport properties of $\text{Yb}_{21-y}\text{Ca}_y\text{Mn}_4\text{Sb}_{18}$ (a) Hall carrier concentration (n_H), (b) resistivity (ρ), (c) Hall mobility (μ_H), (d) Seebeck coefficient (α). See ESI† for Pisarenko plot (Fig. S7).

Fig. 13 (a) Total thermal conductivity of Cd-substituted series ($\text{Yb}_{21}\text{Mn}_{4-x}\text{Cd}_x\text{Sb}_{18}$) and (b) total thermal conductivity of Ca-substituted series ($\text{Yb}_{21-y}\text{Ca}_y\text{Mn}_4\text{Sb}_{18}$).

With increasing Cd and Ca content, the total thermal conductivity increases slightly (see Fig. 13a and b). In general, on a large scale the thermal conductivity of all the samples are not changed drastically from $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$, with the maximal changes amounting to approximately $\sim 0.2 \text{ W m}^{-1} \text{ K}^{-1}$. From the Wiedemann–Franz law, the electronic part of the thermal conductivity is given by $\kappa_e = L\sigma T$, where L was approximated with an accuracy within 0.5% of a single parabolic band model calculation.²⁶ The electronic contribution was subtracted from the total thermal conductivity to yield the lattice thermal conductivity (see ESI† Fig. S8). The lattice thermal conductivity can be seen to slightly increase for both solid solutions and may be due to the difference in defect formation energies of the substituted elements where previously Yb defects were calculated to be more energetically favourable than Ca defects.²⁷

Room temperature measurements of speed of sound yield a transverse and longitudinal value of $v_t = 1774 \text{ m s}^{-1}$ and 3006 m s^{-1} respectively for the pristine sample of $\text{Yb}_{21}\text{Mn}_4\text{Sb}_{18}$. A corresponding Debye temperature of $\theta_D \approx 192 \text{ K}$ for $x = 0$ sample was calculated from eqn (2) and (3) where v_m is the mean speed of sound, v_l and v_t are the longitudinal and transverse speeds of sound respectively.

$$\theta_D = \frac{v_m \hbar}{k_b} \left(\frac{6\pi^2}{V} \right)^{1/3} \quad (2)$$

$$v_m^3 = \frac{3}{v_l^{-3} + 2v_t^{-3}} \quad (3)$$

From Cahill *et al.*,²⁸ an estimate of the lower limit of thermal conductivity ($\kappa_{\min}$) can be calculated from eqn (4).

$$\kappa_{\min} = \left(\frac{\pi}{6} \right)^{1/3} \frac{k_b}{V^{2/3}} \sum_i v_i \left(\frac{T}{\theta_i} \right)^2 \int_0^{\theta_i/T} \frac{x^3 e^x}{(e^x - 1)^2} dx \quad (4)$$

where V is the average atomic volume, v_i is the i th sound mode (three in total – two transverse, one longitudinal), and $\theta_i =$

$\frac{v_i \hbar}{k_b} \left(\frac{6\pi^2}{V} \right)^{1/3}$ is the frequency cutoff for the i th polarization in

units of K. The lattice thermal conductivity of the samples can be seen to drop below $\kappa_{\min}$ which may be due to shortcomings of the Lorenz number calculation and the assumptions of the single parabolic band model.²⁹

Figure of merit

The figure of merit, zT , plots are shown in Fig. 14 where we see a max $zT \sim 0.92$ is achieved for the $x = 1.5$ ($\text{Yb}_{21}\text{Mn}_{2.5}\text{Cd}_{1.5}\text{Sb}_{18}$) sample. The ZT_{avg} of this sample is 0.61 from 300 K to 800 K, calculated from the integration method, making it the highest for the 21-4-18 compositions reported to date. There is a large improvement over the whole temperature range at this Cd concentration and this result is important for practical thermoelectric device implementation. For the Ca-substituted series, the figure of merit ultimately decreases with increasing amounts of Ca mainly due to the large increase in resistivity. However, the change in scattering mechanism and the possibility of keeping the low thermal conductivity while tuning the carrier

Fig. 14 Figure of merit (zT) plots for Cd-substituted samples ($\text{Yb}_{21}\text{Mn}_{4-x}\text{Cd}_x\text{Sb}_{18}$) and Ca-substituted samples ($\text{Yb}_{21-y}\text{Ca}_y\text{Mn}_4\text{Sb}_{18}$).

concentration *via* aliovalent substitution provides a new avenue towards additional *zT* improvements.

Conclusion

The two solid solutions of $\text{Yb}_{21}\text{Mn}_{4-x}\text{Cd}_x\text{Sb}_{18}$ ($x = 0, 0.5, 1.0, 1.5$) and $\text{Yb}_{21-y}\text{Ca}_y\text{Mn}_4\text{Sb}_{18}$ ($y = 3, 6, 9, 10.5$) have been successfully synthesized using high temperature annealing of the elements followed by spark plasma sintering for densification. Building upon our previous work, this study continues to show the highly disordered nature of the 21-4-18 system from total X-ray synchrotron diffraction studies (pair distribution function) and from synchrotron powder X-ray diffraction. The average structure obtained from Rietveld refinement has been observed to differ from the local structure determined from reverse Monte Carlo simulations of PDF data in terms of the site occupation of the Cd and Ca to give rise to nanodomains within the material. In general, the 21-4-18 phase becomes more metallic with Cd substitution and more insulating with Ca substitution. The highest *zT* ~ 1 is achieved at 800 K by the material with stoichiometry $\text{Yb}_{21}\text{Mn}_{2.5}\text{Cd}_{1.5}\text{Sb}_{18}$. Even though these substitutions are in principle, isoelectronic substitutions, the systematic change in the physical properties show that one cannot solely rely on electron counting rules to rationalize these results. These studies show that the carrier scattering mechanism can be tuned through ionic substitutions to make the material more polar and in particular for the 21-4-18 system, that the correct optimization strategy is to increase the carrier concentration. Given that there are many possibilities within the 21-4-18 structures, even higher *zT*s are possible with further optimization and expansion of the possible solid solutions.

Conflicts of interest

The authors declare no competing financial interest.

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