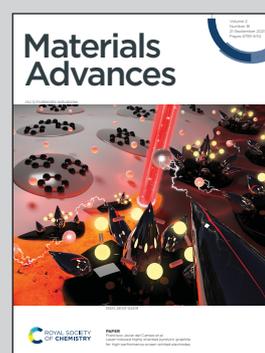


Showcasing research from Professor Jaime Alvarez's laboratory, Materials Physics Department, Centro de Investigación en Materiales Avanzados S.C. Unidad Monterrey, Mexico.

A novel enhanced performance thermal rectifier based on NPG functionalized carbon fibers

It has been estimated that the amount of waste heat is about 80% of the consumed global energy. Consequently, it has recently been considered as the dominating root cause of current global warming and carbon footprint. Thus, thermal rectifiers, which are a one way heat transfer solid state devices, could become an essential platform for a thermally efficient energy consumption society. Present research provides a newfangled strategy to get enhanced performance thermal rectifiers based on partially functionalized carbon fibers with organic phase change materials, which amazingly accomplishes rectification factors up to 3.

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# A novel enhanced performance thermal rectifier based on NPG functionalized carbon fibers

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Theoretically, a thermal rectifier is a one-way heat transfer solid state device. If these components become a reality, they will significantly impact on thermal energy recycling and management. In this work, by grafting neopentylglycol (NPG) molecules to carboxylic acid functional groups (–COOH) on the surface of a carbon fiber (CF), a novel two-segmented thermal rectifier has been implemented to efficiently enhance the rectification factor. The device controls the heat by way of the existing first order phase transition in NPG, which triggers rotational molecular reorientations at a prescribed temperature. Thermal measurements of the diode show that the device is able to conduct almost three-fold more heat in the forward bias than in the reverse one. Furthermore, for the restricted class of symmetries established by NPG, and by using anisotropic heat conduction theory in solids, we demonstrate that the experimental (2.95) and predicted (3) rectification factors match quite well. Thereby, such systems possess a significantly enhanced rectification factor which depends on the principal thermal conductivity tensor components present in each phase. Hence, partially functionalized carbon fibers with NPG are newfangled candidate materials which can provide avenues to achieve high performance thermal diodes *via* surface chemical functionalization.

## 1. Introduction

Major global energy losses can be identified as waste heat; estimations reveal that 80% of the global primary energy consumption is lost after conversion processes giving rise to the dominating root cause of current global warming and carbon footprint.<sup>1–3</sup> Therefore, even reclaiming a small portion of such waste heat would itself nearly satisfy the electricity needs of the planet.<sup>4</sup> Nowadays, the main promising way to recover waste heat is *via* thermoelectric devices. Thermoelectricity enabling direct conversion of heat into electricity using thermoelectric converters is a promising energy technology, which is under intense research to provide a solution to thermal energy recovery and management. The performance of a thermoelectric material is evaluated by the dimensionless figure of merit,  $ZT$ , which is defined as  $ZT = S^2\sigma T/k$ , where  $\sigma$  and  $k$  are the electrical and thermal conductivity respectively,  $S$  is the Seebeck coefficient and  $T$  is the absolute temperature.

The enhancement of  $ZT$  is not an easy task because these physical parameters are interdependent, and an improvement in one of these properties affects adversely another one. Hence, the development of high-performance thermoelectric materials is very challenging. Recently, materials' nanostructuring was used to increase the thermoelectric performance; theoretically Dresselhaus *et al.*<sup>5</sup> have shown that quantum wires as well as superlattices<sup>6</sup> have the potential to achieve a significant increase in  $ZT$  compared with bulk materials. In this sense, carbon nanostructures and carbon based composites such as carbon nanotubes (CNTs), graphene as well as polymer-based carbon composites have experienced rapid development as TE materials because of their intrinsic ultrahigh electrical conductivity and light weight which have led to high TE performance and superior flexibility.<sup>7–9</sup> However, by using only such current thermoelectric conventional strategies it is a challenge to recycle wide-scale waste heat and reuse it for further purposes. Hence, an alternative solution to the waste heat problem would be the development of solid state thermal devices which could help to recover it.

In a thermal domain, the thermal diode is an analogue to the renowned electrical diode, a device where heat current  $q$  preferentially flows in the forward than in the reverse direction,  $q_f > q_r$ . Hence, such thermal rectifiers could have a huge impact not only as thermal energy harvesting devices but also as heat control solid state devices.<sup>10,11</sup>

The performance of a thermal rectifier is evaluated by the rectification factor  $R$ , which is defined as  $R = q_f/q_r$ . In practice, a

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value of  $R \geq 10$  is a required limit to deem the effect useful for actual applications. Nevertheless, the primary limit for the application of this technology is the relatively low thermal rectification factor accomplished by current materials. In this sense, in bulk materials thermal rectification has mainly been achieved *via* the temperature dependence of the thermal conductivity, and the acoustic impedance mismatch between the constituent materials;<sup>12–19</sup> whereas in nanomaterials, the dominant mechanisms for thermal rectification are phonon spectral overlap, phonon spectral mismatch, and phonon spatial confinement.<sup>20–27</sup> Evidently, in spite of the several strategies proposed, neither bulk nor molecular mechanisms have evidenced that the rectification factor can reach one order of magnitude. For instance, by using the aforementioned strategies, the best reported rectification factor at the bulk scale is  $R \sim 2$  for a thermal diode based on icosahedral quasicrystals placed between two heat reservoirs kept at 900 K and 300 K<sup>28</sup> respectively. On the other hand, at the nanoscale, an amazing value of  $R \sim 3.3$  was achieved with inorganic nanolayers *via* interfacial thermal boundary resistance.<sup>29</sup> The problem with nanostructured rectifiers is that they are too thin to establish appreciable temperature gradients and to withstand large heat fluxes, not to mention that most of the proposed architectures<sup>30–33</sup> require coupling and layout between individual atoms, which are very difficult to accomplish in practice. Hence, too much work remains to be done in order to achieve a practical thermal rectifier at room temperature. At the beginning of this decade, an alternative strategy to accomplish enhanced performance thermal rectifiers using solid-state junctions based on phase-change materials showed great potential, and rectification factors of  $\sim 1.14$ <sup>34</sup> at 55 K, as well as  $\sim 1.5$ ,<sup>35</sup> and  $\sim 1.7$ <sup>36</sup> at room temperature were achieved *via* first and second order phase transitions respectively. Such results demonstrated that PCMs are promising next-generation thermal rectifying materials. Lately, following the potential of PCMs for obtaining enhanced performance thermal rectifiers at room temperature, an  $R \sim 2$  was achieved in a heterojunction diode based on organic PCMs.<sup>37</sup> Although most of the thermal diodes based on PCMs reported so far present relatively low thermal rectification factors,<sup>34–43</sup> theoretical analysis has shown their potential to maximize their rectification factor by giving some criteria.<sup>44,45</sup> In this sense, a value of  $R \sim 2.6$  was reported in a dual phase change organic thermal diode constituted by the junction of an octadecane-impregnated polystyrene foam (PFH-O) and poly(*N*-isopropylacrylamide) (PNIPAM) under ambient conditions.<sup>46</sup> Besides, recently, an  $R \sim 2.7$  was accomplished in a thermal diode consisting of two slabs of Ag chalcogenides.<sup>47</sup> Fig. 1 shows an evolution map for experimental thermal diodes based on PCMs. Thus, motivated by the promising results obtained in the former PCM based thermal diodes, in the present research through the development of novel diode architecture, an enhanced performance thermal rectifier with  $R \sim 2.95$  has been used at room temperature. The device is based on a partially functionalized carbon fiber with NPG molecules which manipulates the heat *via* molecular transformations above the transition temperature.

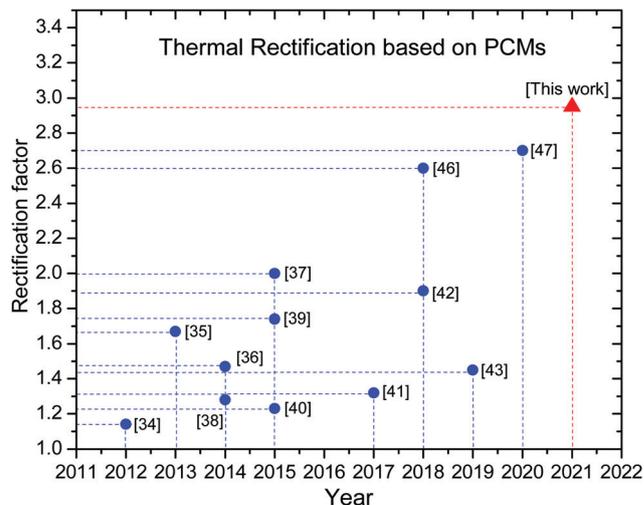


Fig. 1 Experimental thermal rectification map based on solid–solid phase change materials.

## 2. Thermal diode concept

Fig. 2a depicts the proposed architecture for a thermal diode based on a partially functionalized carbon fiber which gives rise to a two-segment material. One of the ends is the segment with the carboxylic acid functional groups on the surface of the carbon fiber, and the second one is the NPG functionalized end.

The molecular configuration of NPG is shown in Fig. 2b. Five carbon atoms consist of the centered tetrahedron, where two are attached to hydrogen atoms in the methyl group ( $-\text{CH}_3$ ), while another two form the hydroxymethyl group ( $-\text{CH}_2-\text{OH}$ ). Basically, NPG presents a lattice transition occurring at a temperature of  $T_t \sim 320$  K, which is confirmed by differential scanning calorimetry (DSC), as shown later.

Below this transition temperature, NPG molecules have a layered structure ordered on a monoclinic lattice or  $\alpha$ -phase with space group  $P2_1/C$ , where hydroxyl groups within the same layer form hydrogen bonds between O and H atoms. At just a few Kelvin degrees above  $T_t$ , this ordered  $\alpha$ -phase transforms into a disordered isotropic cubic FCC lattice or  $\gamma$ -phase with intermolecular hydrogen bond rotation, as shown in Fig. 3a.<sup>48</sup>

This crystalline structure changing from a monoclinic configuration to a face centered cubic form is confirmed *via* XRD patterns where the (011) Bragg peak disappears from the low temperature phase to a high temperature phase, as evidenced by the XRD patterns shown in Fig. 3b at 300 K and 340 K, respectively. Explicit dynamic aspects of NPG transformation can be found in the literature.<sup>48–52</sup> In the low temperature  $\alpha$  phase NPG exists in an associated state because the intermolecular hydrogen bonds come into being; when the temperature is going up at  $T_t$ , the intermolecular hydrogen bonds will weaken. This action causes the corresponding hydroxyl bond to strengthen gradually prompting the  $-\text{OH}$  absorption band to move to a higher wave number.

In Fig. 4a, the infrared spectra portions of the NPG at 300 K and 340 K show a strong absorption centered at about  $3300\text{ cm}^{-1}$  and  $3400\text{ cm}^{-1}$  respectively. A wave number shift



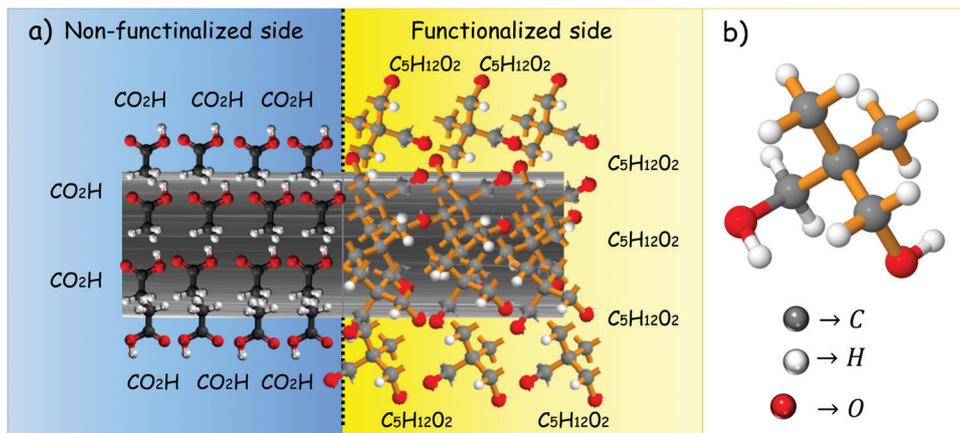


Fig. 2 (a) Proposed thermal diode architecture based on an NPG functionalized carbon fiber, and (b) molecular configuration of NPG.

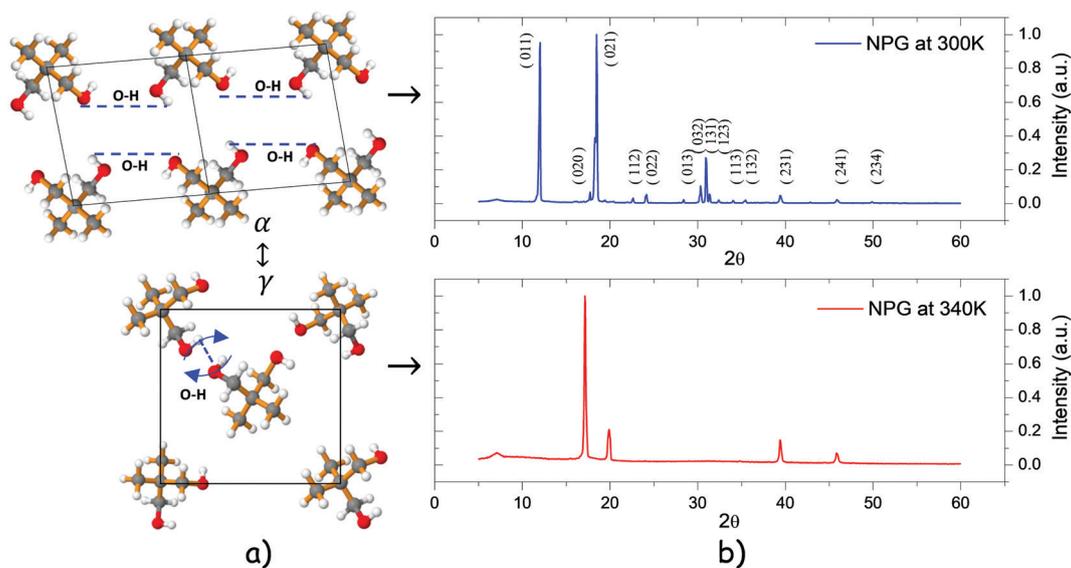


Fig. 3 (a) Crystallographic plane of the monoclinic( $\alpha$ ) and cubic phase( $\gamma$ ) of NPG before and after transition, and (b) XRD patterns corresponding to the monoclinic( $\alpha$ ) and cubic phase( $\gamma$ ).

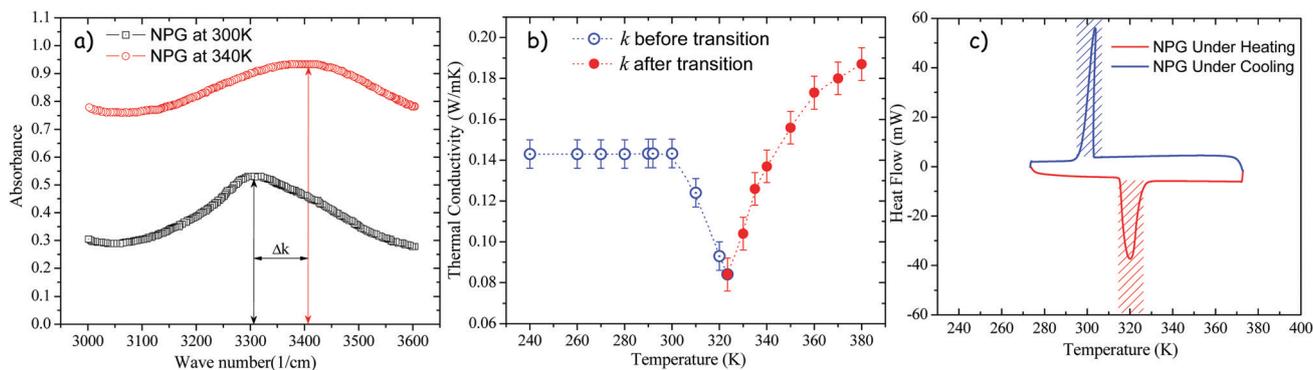


Fig. 4 (a) Infrared absorption spectra of NPG at 300 K and 340 K. (b) Temperature dependent thermal conductivity of NPG, and (c) DSC of NPG.

of  $k \sim 100 \text{ cm}^{-1}$  is identified with the  $-\text{OH}$  stretching band. Since the  $-\text{OH}$  groups are most directly involved in bonding of

the NPG, this absorption band can sense the changes in the crystal-line structure occurring during the solid-solid transformation.





the forward bias mode the NPG functionalized segment will accomplish quicker the  $\gamma$ -phase transition than in the reverse bias mode. This is because, in the forward bias mode, the NPG functionalized segment is in contact directly with the heat source, whereas in the reverse bias mode it is not, which delays the phase transition. Therefore, once the  $\gamma$ -phase transition is achieved in either reverse or forward bias, the thermal diode will start with a sudden rise in the heat flux at certain prescribed temperatures, named the breakdown temperature and forward temperature respectively. Such temperatures will control the on-state and breakdown-state of the device, similar to the forward voltage and breakdown voltage in electronic diodes. Evidently, an important content of NPG molecules attached along the functionalized segment must be accomplished to ensure an intra- and inter-molecular heat transfer along the NPG segment. In this sense, the amount of grafted NPG molecules will depend on the amount of COOH molecules attached to the carbon fiber surface, as the content of COOH increases, NPG molecule content will also increase and *vice versa*. Thereby, it is crucial to achieve a great deal of grafted NPG molecules because NPG is directly related to the rectification effect, and a lack in the content of NPG will blur the rectification effect in the device. However, it is well known that chemical functionalization of surfaces has been demonstrated to be an important strategy to modify energy carrier transport mechanisms in carbonaceous materials.<sup>53</sup> Thereby, a substantial content of COOH organic molecules covalently attached to the surface gives rise to the formation of localized defect sites, which will act as surficial scattering centers for electrons and phonons. Undoubtedly, it will affect the device performance by altering the thermal conductance of the device, which will delay or hasten the transition of the NPG segment.

### 3. Experimental procedure

#### Materials and NPG functionalization of carbon fibers

First, the polyacrylonitrile (PAN)-based carbon fibers (CFs) from Toray Industries were cleaned by reflux with acetone (Certified ACS  $\geq 99.5\%$ , Fisher Chemical) for 24 hours. Then, these CF were ultrasonically cleaned with ethanol (absolute, ACS, Fermont), methanol (Optima™, LC/MS, Fisher Chemical) and Deionized Water (of  $18.2 \text{ MW cm}^{-1}$  resistivity), each for 30 minutes. The carboxylic functionalization of the CFs was done by a 3 : 1 (v/v) mixture of concentrated sulfuric acid ( $\text{H}_2\text{SO}_4$ , 95–98% ACS, FCC, VWR Chemicals BDH and Nitric acid ( $\text{HNO}_3$ , 68–70%, ARISTAR, ACS, VWR Chemicals BDH) for 2 hours at  $80^\circ\text{C}$ . For the neutralization of acid residues by carboxylic functionalization, the CFs have been subjected to hydrogen peroxide ( $\text{H}_2\text{O}_2$ , 30%, BAKER ANALYZED, ACS, J.T. Baker) immersion for 12 hours. After this treatment, one end of the CFs was covered by one solution at 10 wt% of polymethyl methacrylate (PMMA, average  $M_w \sim 996\,000$  by GPC, powder, Sigma-Aldrich) in anisole (anhydrous, 99.7%, Sigma-Aldrich). Another free end of the CFs was refluxed by one aqueous solution at 15 wt% and 5 M of 2,2-dimethyl-1,3-propanediol (neopentyl glycol, 99%, Alfa Aesar) in  $\text{H}_2\text{SO}_4$  (95–98% ACS, FCC, VWR Chemicals BDH), respectively.

To etch the section of the covered CFs by PMMA, this was immersed in an aqueous solution of 1M sodium hydroxide (NaOH, BAKER ANALYZED, A.C.S. Reagent, J.T. Baker). Next, this same section treated with NaOH was placed in concentrated glacial acetic acid (99.96%, CTR) for 24 hours to remove the PMMA completely. Subsequently, the two sections of the CFs were cleaned with a methanol solution: water (1 : 1 by volume) to dissolve the PMMA residues and to remove any organic impurity formed during the process.

#### Characterization

NPG crystalline structure transformation from a monoclinic configuration to face centered cubic form was confirmed by DRX patterns using a Panalytical Empyrean diffractometer with an Anton Paar HTK 16N high temperature chamber using a Cu-K $\alpha$  radiation X-ray source. Furthermore, crystalline phase identification was carried out *via* the crystallographic software X'Pert High Score Plus based on the International Centre for Diffraction Data (ICDD). NPG transition temperatures are provided in DSC analysis, and they were measured by the TA Instruments Q200 DSC equipped with a refrigerated cooling system based on liquid nitrogen. The sample was cooled down to  $0^\circ\text{C}$  at  $5^\circ\text{C}$  per min, followed by heating from  $0$  to  $100^\circ\text{C}$  at  $5^\circ\text{C}$  per min and then cooled down to  $0^\circ\text{C}$  at  $5^\circ\text{C}$  per min. Besides, NPG FTIR spectra were measured on a Thermo-Nicolet spectrophotometer model 6700. Likewise, the functionalization process leads to an inclusion of NPG chemical moieties on the carbon fiber surface, which was verified by X-ray photoelectron spectroscopy (XPS) *via* the analysis of the high resolution C1s spectra of the functionalized and non-functionalized carbon fiber segments through a Thermo-Fisher Scientific ESCALAB 250Xi XPS system with an Al-K $\alpha$  radiation X-ray source.

Bulk NPG temperature dependent thermal conductivities were measured from 240 K to 380 K by a Hot Disk M1 system combined with a closed cycle cryostat from ARS Systems. NPG samples 1 cm in thickness and 4 cm diameter were situated on either side of the Kapton 8563 sensor with an input power of 100 mW for 10 s.

#### NPG functionalized carbon fiber diode dimensions

A thermal rectifier consists of a total length of 10 cm, of which approximately 5 cm length corresponds to the functionalized side, and the remaining 5 cm to the non-functionalized segment. Each end of the segments was attached to each of the suspended heaters with a heat conductive epoxy.

#### Q- $\Delta T$ transfer characteristics of the thermal diode

To supply heat in reverse and forward bias mode, a DC electrical current sweep with regular increments of the order of mA is applied to the  $\sim 100 \Omega$  Pt thin film resistive heater by using the Keithley 6221 AC/DC power supply; the thin planar Pt heater is placed on the surface of the pyrolytic graphite plate, and it has dimensions of 3 mm in width and 4 mm in length. By waiting long enough at each current increment, this action gives rise to several steady state temperature rises  $\Delta T$  on the thermal diode at both modes.



Temperature rises are detected *via* the data acquisition card model NI-9210 C Series Temperature Input Module from national instruments. In this way, a set of  $\Delta T$  and their corresponding heat fluxes  $Q$  are obtained, then finally the transfer curve  $Q-\Delta T$  can be plotted. To ensure measurement repeatability, each measurement was performed at least 10 times, and the results shown in Fig. 9 are the average of the whole set of measurements. It is worth mentioning that the sample was suspended during the measurements so as to avoid significant lateral heat flow leaks which could affect significantly the measurements due to convective and conduction effects. Measurement details are shown in Section 4.2.

## 4. Results: experiment and theory

Chemical functionalization of surfaces is an important strategy to engineer functional materials by tailoring the properties of the base structure. In this sense, in the present research a novel two-segment thermal diode based on a partially functionalized carbon fiber is successfully developed. One of the segments of the carbon fiber is functionalized with NPG as the PCM material, whereas the second one is the segment with the carboxylic acid functional groups. Because of the NPG functionalized section, the thermal diode is characterized by presenting opposing thermal conductivity trends at a prescribed temperature leading to a thermal rectification factor as high as 2.95; which, to the best of our knowledge, is the highest thermal rectification factor demonstrated by a PCM thermal diode material to date.

### 4.1. Thermal rectifier making: grafting of the NPG functionalities onto the carbon fiber surface

Before surface functionalization, the as-received carbon fibers were subjected to a cleaning process to remove sizing agent, and then they were washed using deionized water followed by a 3 : 1 acid treatment of concentrated  $H_2SO_4:HNO_3$  at 80 °C for 2 h, and dried at 70 °C for 24 h to obtain COOH-carbon fibers. After acid treatment, carbon fibers with a carboxylic acid group were partially further functionalized in a solution of  $H_2O/NPG/H_2SO_4$  under ultrasonic vibration for 48 h which afforded NPG-carbon fiber. Surface functionalization process details are shown in the Experimental procedure section.

To confirm the presence of NPG onto the carbon fibers surface, XPS spectra were carried out. Fig. 6 shows the high resolution C1s spectra of the COOH-carbon fiber segment (red solid line), and that of the NPG functionalized carbon fiber segment (black solid line). By comparing both spectra, a broadening of the peak located at 284.7 eV of the NPG functionalized segment is evident. Such broadening is related to the existence of the NPG functionalities and represents an increment in the relative component areas of around 10% with regard to the COOH-carbon fiber segment. Although the presence of hydrogen cannot be quantified by XPS, the broadening of the main peak indicates the increase of  $sp^3$  hybridized carbon atoms, which is mainly attributed to the incorporation of hydrogen,<sup>54</sup> in this case from NPG. As shown in Fig. 7a and b, each spectrum is

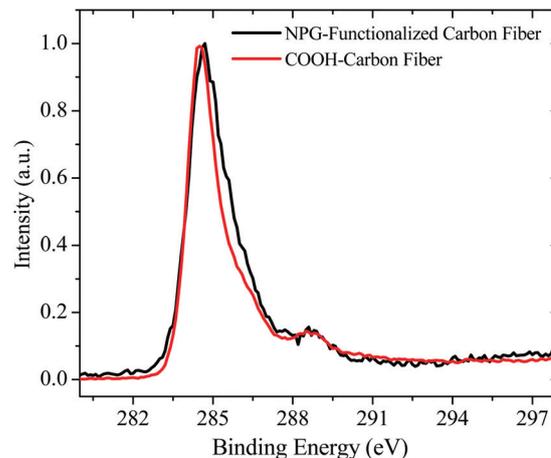


Fig. 6 Normalized XPS C1s spectra of carbon fiber with and without NPG functionalization.

decomposed into five components, specifically C=C (284.7 eV- $sp^2$ ), C-C (285.4 eV- $sp^3$ ), C-OH (286.5 eV), C=O (287.5 eV) and COOH (289.0 eV) as labeled in both figures. By inspecting carefully the C1s peak, both COOH-carbon fiber and NPG-carbon fiber reveals the presence of hydroxyl and carboxyl groups as indicated by the well-pronounced peaks around 286.5 and 289.1 eV respectively. The ratios of the area under the respective Gaussian curve (for C-OH and COOH curves) were calculated and the percentages are shown in Table 1, from which we found that the NPG-functionalization treatment caused an increase in the ratio of adsorbed oxygen (27.84% + 11.56% = 39.4%) in the carbon fiber compared to the initial carbon fiber (17.90 + 11.52 = 29.42%). These results clearly indicate that the functionalization procedure increases hydroxyl content due to the NPG chains.

The surface morphologies for the COOH-carbon fiber, and NPG functionalized carbon fiber segments were examined by SEM. As shown in Fig. 7c, the COOH-carbon fiber segment presented a relatively soft surface constituted of narrow grooves distributed in parallel along the longitudinal direction of the fiber. Nevertheless, as shown in Fig. 7d, the NPG functionalized carbon fiber segment presented differences in the surface morphologies after grafting the NPG chains. Moreover, it can also prove that NPG chains were grafted onto the carbon fiber surface successfully.

### 4.2. Thermal measurements

In the present research, because of the extremely low thermal mass of the functionalized carbon fiber, as well as to avoid uncertainties due to radiation and convection heat losses, the  $Q-\Delta T$  transfer characteristics of the thermal diode have been obtained through a lab custom set-up based on the absolute method.<sup>55</sup> In this technique, a temperature difference  $\Delta T$  across the sample is measured in response to an applied amount of heating power  $Q$ . Hence, the thermal conductance of the thermal rectifier in the forward and reverse bias is given by the slope of  $Q$  versus  $\Delta T$  sweep at fixed base temperature. Basically, the sample is installed between two suspended thin film Pt heaters which have embedded onto their surface



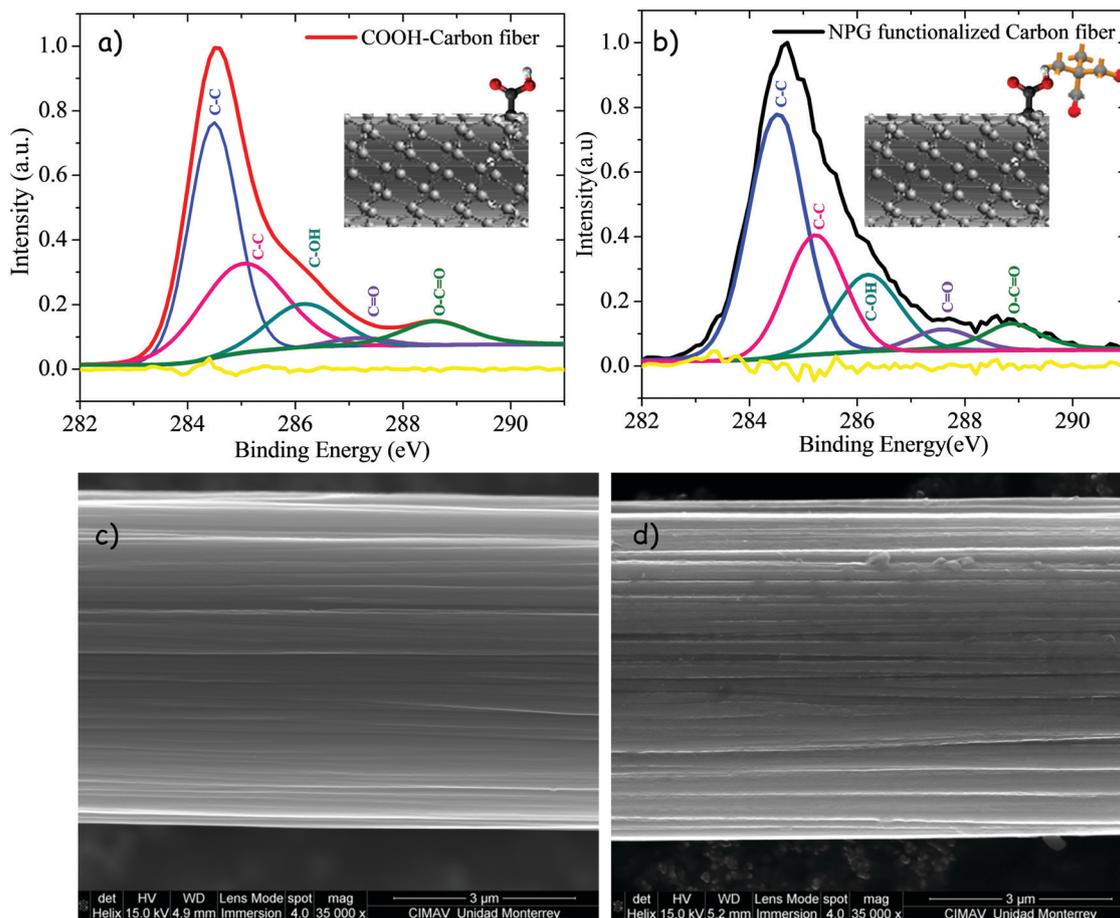


Fig. 7 High resolution C1s XPS spectra of carbon fibers (a) before and (b) after functionalization, and SEM images of carbon fibers (c) before and (d) after functionalization at 35 000X magnification.

**Table 1** Summarized fraction of areas under the respective Gaussian curves of  $sp^2C$ ,  $sp^3C$ , C–OH, C=O, and COOH for carbon fibers before and after functionalization

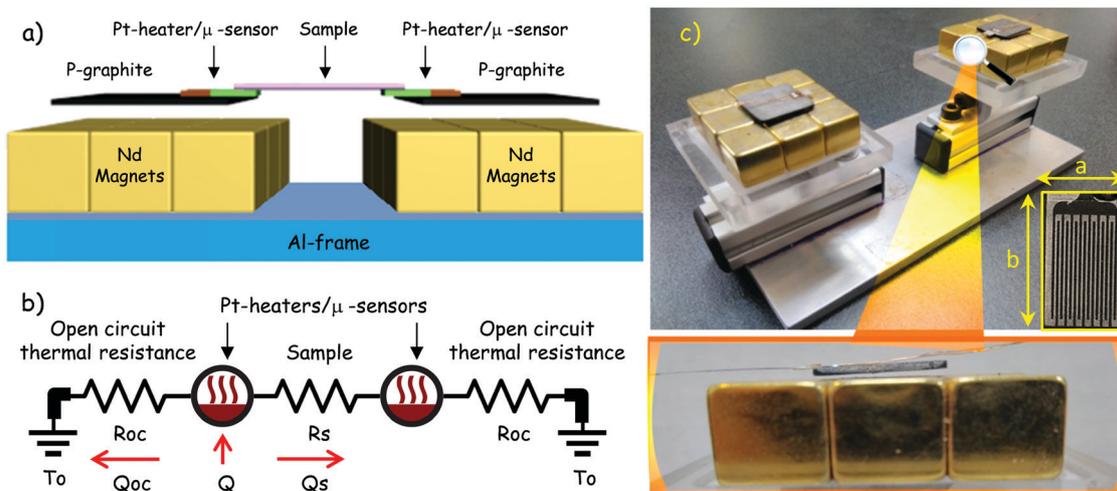
Component peak	Binding energy (eV)	COOH-Carbon fiber (relative component areas %)	NPG-Carbon fiber (relative component areas %)
C–C( $sp^2$ )	284.7	31.44	30.41
C–C( $sp^3$ )	285.4	21.76	19.48
C–OH	286.5	17.90	27.84
C=O	287.5	11.38	10.71
COOH	289.0	11.52	11.56

a type-K micro-thermocouple that works as a temperature sensor. With the aim to minimize heat loss by conduction with the surroundings, the heater/sensor system is placed onto the surface of a thin plate of pyrolytic graphite, which subsequently is suspended *via* magnetic levitation above the magnetic field of a neodymium permanent magnet. In this way, conduction heat leaks to the surroundings will be limited significantly, and will be subjected only to wiring. The illustrative experimental set up is shown in Fig. 8a, and it is merely a schematic and generalized picture of the implemented real system. In terms of driving heat conduction losses due to wiring, wires with a high

thermal resistance are desirable. Thus, the diameter of wires must be as small as possible and possess low thermal conductivity. We have used low thermal conductivity Manganin wires with 0.003" in diameter for heater power wiring. Manganin is a relatively low thermal conductivity material ( $\sim 20 \text{ W mK}^{-1}$ ), yet one that also has reasonable values of electrical resistivity ( $\sim 40 \times 10^{-8} \Omega \text{ m}$ ). Besides, type-K micro-thermocouples with 0.0025" in diameter were also used for temperature sensing. Heat loss through the connection wires has been calculated and it is typically less than 5% in our experimental design. Along with heat leak minimization by conduction, magnetic levitation also provides a stable position to the thermal diode by avoiding elongations and contractions that could induce significant uncertainties during measurements, this is due to the existing piezoresistivity effects in carbon fibers.<sup>56</sup>

Likewise, to avoid heat losses by convection, the best way to minimize these convection losses is to do the measurements with the sample in a moderate vacuum ( $10^{-4}$  to  $10^{-5}$  torr); we accomplished  $10^{-6}$  torr during measurements. Moreover, heat loss due to radiation effects between the surroundings and the sample can be substantial. In our actual experimental set-up, a thermally anchored radiation shield is used in order to protect the equipment from thermal fluctuations coming from the



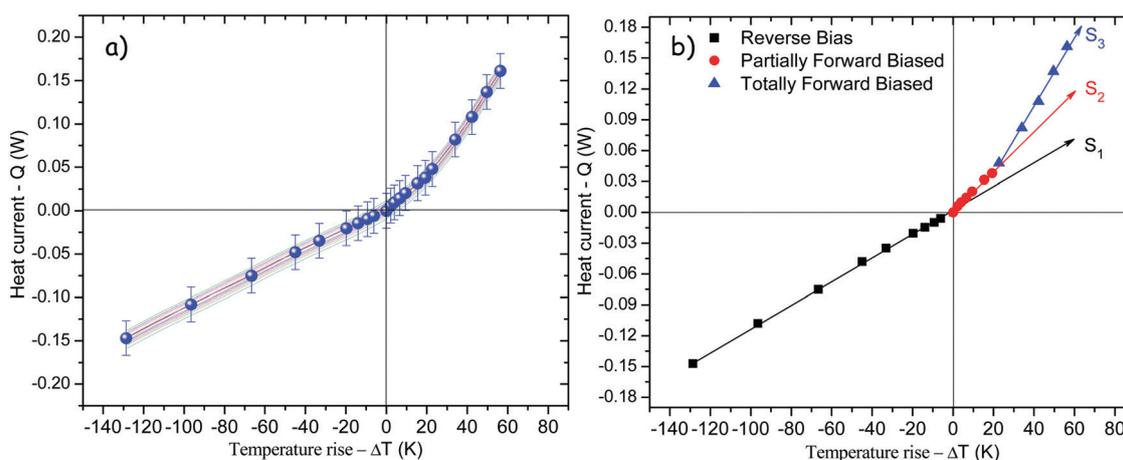


**Fig. 8** (a) Illustrative scheme depicting the experimental set-up of the measurement cell, (b) equivalent thermal circuit of the measurement cell, and (c) actual measurement cell, inset shows the planar Pt heater, here  $a = 3$  mm, and  $b = 4$  mm, and magnification shows the levitated system to avoid lateral heat losses.

surroundings. It is worth mentioning that our measurements were performed at 300 K where the radiation uncertainties are in the order of approx. 3%, at significantly lower temperatures (e.g. 100 K) or at significantly higher temperatures (e.g. 850 K) the measurement uncertainty due to heat loss to the environment is somewhat greater and is in the order of about 7%. Fig. 8b shows the equivalent thermal circuit of the measurement device. The thermal resistances defined by  $R_{oc}$  represent the vacuum gap between the magnet and the heater/sensor system, for this reason they can be approached as infinite thermal resistances or open circuit thermal resistances. The base temperature is represented as  $T_o$ , and  $R_s$  is the thermal resistance of the sample. Evenly,  $Q = Q_{oc} + Q_s$ , represent the input heating power, a portion  $Q_{oc}$  is conducted to the surroundings *via*  $R_{oc}$ , and the rest  $Q_s$  is conducted into the sample. Hence, if it is assumed that  $R_{oc} \rightarrow \infty$ , then  $Q = Q_s$ , and the thermal conductance of the sample can

be experimentally estimated from the slope of the plot  $Q$  versus  $\Delta T$ . Fig. 8c presents an optical image of the measurement cell, magnification shows one of the pyrolytic graphite plates levitating, which includes the heater and sample attached onto its surface (see the inset).

On the other hand, forward bias mode is considered when heat is applied directly to the NPG-functionalized segment, whereas in reverse bias, heat is applied directly to the non-functionalized segment. Therefore, lattice transition in the NPG-functionalized segment must be achieved quicker under forward bias than in reverse bias conditions giving rise to nonlinear heat conduction. Fig. 9a presents  $Q-\Delta T$  transfer characteristics of the thermal diode at 300 K base temperature. In this figure solid lines correspond to ten consecutive measurements, whereas discrete solid symbols represent the average of ten measurements. Furthermore, for clarity during



**Fig. 9**  $Q-\Delta T$  transfer characteristics for (a) ten consecutive measurements of the thermal diode, and (b) measurement average of the thermal rectifier at 300 K base temperature. Solid lines in both plots represent the best linear fit to experimental data, whereas the slope  $S_i$  stands for thermal conductance of the device respectively.



analysis, Fig. 9b shows the average values corresponding to the ten measurements. Evidently, in reverse bias mode (solid black squares) a linear behavior is observed at least in the range from  $-150$  mW to slightly above  $0$  mW. Such behavior could be interpreted as if the supplied heat was not enough to increase the temperature above  $320$  K at the interface between the non-functionalized side and the functionalized side. Hence, the NPG-functionalized segment never starts the solid–solid transition. However, in forward bias mode asymmetric heat conduction is observed with regard to the reverse bias mode. In fact, lattice transition starts almost immediately after the heat is supplied, which is unveiled by the slope change from  $S_1$  to  $S_2$  in the plot  $Q-\Delta T$ . Besides, this change from  $S_1$  to  $S_2$  could be interpreted as if only a portion along the NPG-functionalized segment had been lattice transformed (solid red circles). Once the supplied heat is enough to completely accomplish the lattice transition of the NPG-functionalized segment, a second change in the slope from  $S_2$  to  $S_3$  is unveiled in the plot of  $Q-\Delta T$  (solid blue triangles). Such changes in the slope represent changes in the thermal conductance of the device, meaning that in reverse bias the device will conduct less heat than in forward bias because it presents a lower thermal conductance  $S_1$  as compared to either  $S_2$  or  $S_3$ .

Table 2 shows the experimental thermal conductance values, as well as the thermal rectification factors obtained from the ratio between the thermal conductances in the forward and reverse bias modes. Hypothetically, if thermal conductance had not presented change under forward and reverse bias, then  $Q-\Delta T$  would be linear in both conditions indicating a rectification factor 1, as it is in the case of linear thermal devices better known as thermal barriers or thermal resistances.<sup>57</sup> On the other hand, in the partially transformed condition,  $R \sim 1.8$ , whereas  $R \sim 2.95$  for a totally transformed NPG-functionalized segment, meaning that the NPG-functionalized segment experiences temperatures well above  $320$  K giving rise to phase transition, and therefore to an increase in its thermal conductance.

### 4.3. Analytical results

To analyze and validate the findings, we have used an analytical model based on the thermal conductivity tensor theory which has been demonstrated to predict accurately the thermal rectification factor of thermal diodes based on phase change materials with lattice transitions.<sup>58</sup> According to Duhamel's generalization of Fourier's law of heat conduction, the local heat flux under a 3D orthogonal coordinate system ( $x, y, z$ ) is

given by<sup>59</sup>

$$\vec{q} = - \begin{bmatrix} q_x \\ q_y \\ q_z \end{bmatrix} = - \begin{bmatrix} k_{11} & k_{12} & k_{13} \\ k_{21} & k_{22} & k_{23} \\ k_{31} & k_{32} & k_{33} \end{bmatrix} \begin{bmatrix} \partial T / \partial x \\ \partial T / \partial y \\ \partial T / \partial z \end{bmatrix} = \left[ k_{ij}^{(x,y,z)} \right] \vec{\nabla} T \quad (1)$$

where  $k_{ij}^{(x,y,z)}$  stands for the thermal conductivity components of the anisotropic material, which relates the temperature gradient field  $\vec{\nabla} T$  to the heat flux vector  $\vec{q}$ . Here, we are concerned with the thermal conductivity tensors of the crystalline structure of NPG which changes from a monoclinic configuration to face centered cubic during transition.

In the monoclinic configuration, due to symmetry considerations some of the components become zero; hence, the thermal conductivity tensor is given by<sup>60</sup>

$$\mathbf{k}_m = \begin{bmatrix} k_{11} & k_{12} & 0 \\ k_{21} & k_{22} & 0 \\ 0 & 0 & k_{33} \end{bmatrix} \quad (2)$$

In the cubic configuration, in addition to some components being zero, also  $k_{11} = k_{22} = k_{33}$ ; hence, the thermal conductivity tensor is given by<sup>60</sup>

$$\mathbf{k}_c = \begin{bmatrix} k_{11} & 0 & 0 \\ 0 & k_{11} & 0 \\ 0 & 0 & k_{11} \end{bmatrix} \quad (3)$$

However, if the monoclinic-cubic transition is due to the rotational molecular reorientations caused by the temperature gradient vector applied to  $k_{ij}^{(x,y,z)}$ , then  $\vec{\nabla} T$  must point in the  $\hat{r}$  direction given by

$$\hat{r} = \begin{bmatrix} \sin \theta \cos \varnothing \\ \sin \theta \sin \varnothing \\ \cos \theta \end{bmatrix} \quad (4)$$

where  $\theta$  and  $\varnothing$  angles indicate that the NPG chains could be randomly oriented over all directions.

In the case of our thermal diode, under reverse thermal bias, the NPG functionalized segment will be directly in contact with the cold end of the temperature gradient; thus, it will be in the monoclinic lattice or  $\alpha$ -phase. Therefore, under this condition the sample will experience a heat flux defined by

$$\vec{q}_m = -\mathbf{k}_m \hat{r} \cdot \vec{\nabla} T \quad (5)$$

Conversely, under forward thermal bias, the NPG functionalized segment will be directly in contact with the hot end of the temperature gradient; thus, it will be in the cubic lattice or  $\gamma$ -phase. Therefore, under this condition the sample will experience a heat flux defined by

$$\vec{q}_c = -\mathbf{k}_c \hat{r} \cdot \vec{\nabla} T \quad (6)$$

Besides, it is only the component of  $\vec{q}$  that is aligned with  $\vec{\nabla} T$  that contributes to the net heat flux. Thus we are interested in

**Table 2** Experimental thermal conductances and the thermal rectification factors of the thermal rectifier based on NPG-functionalized carbon fiber at  $300$  K base temperature

$Q-\Delta T$ [Slope(W/K)]	$R = S_i/S_1$	NPG segment
$S_1 = 1.14 \times 10^{-3}$	1	Non-transformed
$S_2 = 2.05 \times 10^{-3}$	$\sim 1.8$	Partially transformed
$S_3 = 3.36 \times 10^{-3}$	$\sim 2.95$	Totally transformed



the net values of the scalars  $q_{nm} = \vec{q}_m \cdot \hat{r}$ , and  $q_{nc} = \vec{q}_c \cdot \hat{r}$ , here  $q_{nm}$  and  $q_{nc}$  stand for the net heat fluxes of the monoclinic and cubic phases respectively.

For the monoclinic phase, using the thermal conductivity tensor given in eqn (2), as well as combining eqn (4) and (5) yields

$$q_{nm} = -(k_{11} \sin^2 \theta \cos^2 \varphi + k_{12} \sin^2 \theta \sin \varphi \cos \varphi + k_{21} \sin^2 \theta \sin \varphi \cos \varphi + k_{22} \sin^2 \theta \sin^2 \varphi + k_{33} \cos^2 \theta) \vec{\nabla} T \quad (7)$$

If we compare eqn (7) with the isotropic form of Fourier's law of the net heat conduction,  $q_n = -k_{ef} \vec{\nabla} T$ , then it can be identified by analogy the effective thermal conductivity  $k_{efm}$  for the monoclinic phase as

$$k_{efm} = k_{11} \sin^2 \theta \cos^2 \varphi + k_{12} \sin^2 \theta \sin \varphi \cos \varphi + k_{21} \sin^2 \theta \sin \varphi \cos \varphi + k_{22} \sin^2 \theta \sin^2 \varphi + k_{33} \cos^2 \theta \quad (8)$$

Finally, in order to obtain the total thermal conductivity of the monoclinic phase  $k_{tm}$ , it is necessary to take into account all the possible orientations of the NPG chains; thus, by averaging eqn (8) over all directions we get:

$$k_{tm} = \frac{1}{4\pi} \int \int k_{efm} \sin \theta d\theta d\varphi = \frac{1}{4\pi} \int_0^\pi \int_0^{2\pi} k_{efm} \sin \theta d\theta d\varphi \quad (9)$$

By combining eqn (8) and (9), and carrying out  $\varphi$  and  $\theta$  integration, the total thermal conductivity of the monoclinic phase is given by

$$k_{tm} = \frac{1}{3}k_{11} + \frac{1}{3}k_{22} + \frac{1}{3}k_{33} \quad (10)$$

Likewise, the total heat flux of the monoclinic phase can be expressed as

$$q_{tm} = -k_{tm} \vec{\nabla} T \quad (11)$$

Following in analogy to the previously described procedure, the net heat flux of the cubic phase can be expressed as

$$q_{nc} = -(k_{11}) \vec{\nabla} T \quad (12)$$

Again, by comparing eqn (12) with the isotropic form of Fourier's law of the net heat conduction,  $q_n = -k_{ef} \vec{\nabla} T$ , then it can be identified by analogy of the effective thermal conductivity  $k_{efc}$  for the monoclinic phase as

$$k_{efc} = k_{11} \quad (13)$$

Now, by averaging eqn (13) over all directions

$$k_{tc} = \frac{1}{4\pi} \int \int k_{efc} \sin \theta d\theta d\varphi = \frac{1}{4\pi} \int_0^\pi \int_0^{2\pi} k_{11} \sin \theta d\theta d\varphi \quad (14)$$

The total thermal conductivity of the cubic phase  $k_{tc}$  yields simply

$$k_{tc} = k_{11} \quad (15)$$

Likewise, the total heat flux of the cubic phase can be expressed as

$$q_{tc} = -k_{tc} \vec{\nabla} T \quad (16)$$

Conventionally, the performance of a thermal rectifier is evaluated by the rectification factor  $R$ , which is defined as  $R = q_c/q_m$ . In our specific case, the rectification factor is obtained by the ratio between the total heat flux of the cubic phase and the total heat flux of the monoclinic phase  $R = q_{tc}/q_{nc}$ , which correspond to the phases presented in the device under forward and reverse thermal bias respectively. Hence, by combining eqn (11) and (16), the rectification factor can be approached as

$$R = \frac{q_{tc}}{q_{tm}} = \frac{k_{tc}}{k_{tm}} = \frac{3k_{11}}{k_{11} + k_{22} + k_{33}} \quad (17)$$

Evidently, according to eqn (17), in order to estimate the rectification factor it is necessary to know the thermal conductivity tensor components of the NPG in the monoclinic and cubic phase. Besides, clearly eqn (17) establishes a limit to  $R$  which is related to the main axes  $k_{ij}$  tensor components. Nevertheless, by observing the experimental total thermal conductivity of NPG shown in Fig. 4b it can be concluded that  $k_{tm} < 1$ , and  $k_{tc} < 1$ . Therefore, the components  $k_{ij}$  must be  $k_{ij} \ll 1$ , so if we assume that  $k_{22} + k_{33} \ll 1$ , then eqn (17) can be expressed as

$$R(k_{11}, \varepsilon) = \frac{3k_{11}}{k_{11} + \varepsilon} \quad (18)$$

where  $\varepsilon$  stands for  $\varepsilon = k_{22} + k_{33}$ .

The asymptotic behavior of the function  $R(k_{11}, \varepsilon)$  with respect to  $\varepsilon$  may depend upon  $k_{11}$ , where  $k_{11}$  can be seen as an independent variable; in which case we say that the expansion is non-uniform. Eqn (18) can be rewritten as

$$R(k_{11}, \varepsilon) = 3k_{11} \left[ \frac{1}{k_{11} + \varepsilon} \right] \quad (19)$$

Clearly, always  $k_{11} > 0$ , as well as  $\varepsilon \rightarrow 0^+$ , thus  $R$  can be approached as

$$R(k_{11}, \varepsilon) \sim 3k_{11} \left[ \frac{1}{k_{11}} \left( 1 - \frac{\varepsilon}{k_{11}} + \frac{\varepsilon^2}{k_{11}^2} - \dots \right) \right] \sim 3 \left( 1 - \frac{\varepsilon}{k_{11}} + \frac{\varepsilon^2}{k_{11}^2} - \dots \right) \quad (20)$$

By analyzing eqn (20), it can be concluded that as  $\varepsilon$  approaches zero the value of  $R \sim 3$ . This is an important contribution of the present research work; in phase change materials with lattice transitions, the rectification factor seems to be limited by the ratio of their corresponding thermal conductivity tensor components. Thus, for the restricted class of symmetries of interest in this work, the ratio between the principal axes of the effective thermal conductivity tensor which defines the thermal rectification factor tends to three; amazingly the value obtained for the proposed thermal rectifier once the cubic phase is completely accomplished is  $R \sim 2.95$ . Fig. 10 shows the behavior of eqn (18) as a function of  $k_{11}$ , and  $\varepsilon$ . The function  $R(k_{11}, \varepsilon)$  defines a surface given by an infinity set of  $(k_{11}, \varepsilon)$  data.



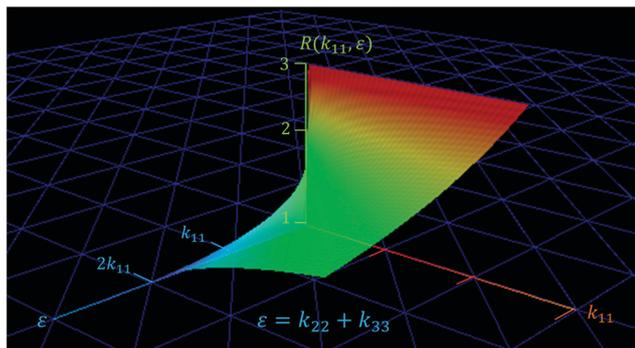


Fig. 10 Thermal rectification as a function of the main components of the thermal conductivity tensor of the NPG.

Evidently, for positive values of  $k_{11}$ , and  $\varepsilon$ ; as  $\varepsilon \rightarrow 0^+$ , quickly  $R \rightarrow 3$  (upper red zone in the plot), whereas for values of  $\varepsilon \gg 0$ , and  $k_{11} \gg 0$ ,  $R \ll 3$  (lower green zone in the plot).

On the other hand, it is well known that carbon fibers are comprised of graphite crystallites arranged as polycrystals along the fiber axis.<sup>61,62</sup> Therefore, reflecting the orientation distribution of graphite crystallites, carbon fibers exhibit anisotropic thermal properties presenting a hexagonal symmetry with five components in the thermal conductivity tensor,<sup>54</sup> which are defined by

$$\mathbf{k}_{\text{cf}} = \begin{bmatrix} k_{xx} & k_{xy} & 0 \\ -k_{xy} & k_{yy} & 0 \\ 0 & 0 & k_{zz} \end{bmatrix} \quad (21)$$

where  $\mathbf{k}_{\text{cf}}$  represents the thermal conductivity tensor of the carbon fiber, and  $k_{xx} = k_{yy}$ ; this restriction holds in the special case of a single-phase system as long as the constituent material has the required hexagonal, tetragonal, or trigonal symmetry, such as polycrystalline graphite.

If we now consider the carbon fiber as a polycrystalline wire one grain in diameter and many grains long, then by applying a similar procedure to that previously described, the total thermal conductivity of the carbon fiber can be expressed as

$$k_{\text{tcf}} = \frac{3k_{xx}k_{yy}k_{zz}}{k_{xx}k_{yy} + k_{xx}k_{zz} + k_{yy}k_{zz}} \quad (22)$$

Moreover, because of the NPG anisotropy, the temperature isotherms are no longer necessarily parallel to the heat flux adiabats. Therefore, taking into consideration such anisotropic effects, the effective thermal conductivity of the thermal diode can be approached as

$$k_{\text{Tef}} = \frac{k_{\text{ti}}}{1 + k_{\text{ti}} \left( \frac{1}{3k_{xx}} + \frac{1}{3k_{yy}} + \frac{1}{3k_{zz}} \right)} \quad (23)$$

where  $k_{\text{ti}}$  stands for  $k_{\text{tc}}$ , and  $k_{\text{tm}}$ ; *i.e.*  $i = \text{c, m}$  depending on the NPG phase present in the thermal diode. Evidently, thermal conductivity of the carbon fiber is bigger than the thermal conductivity of NPG; thus, by assuming this consideration as valid, eqn (23) transforms into  $k_{\text{Tef}} \sim k_{\text{ti}}$ . Hence, because of the

relatively high thermal conductivity of carbon fiber, the total effective thermal conductivity in the forward and reverse thermal bias can entirely be defined by  $k_{\text{tc}}$ , and  $k_{\text{tm}}$  respectively. For this reason, in the present research the limit in the rectification factor has been approached through eqn (17). Equally, this kind of rectification factor is both measured and analyzed with our analytical theory, and these values match quite well.

## Conclusions

In the present research, we have developed and theoretically analyzed a novel thermal rectifier architecture that consists of a PAN-carbon fiber partially functionalized with NPG, which is a phase change material. This promising architecture shows an enhanced performance as compared to the previously reported thermal diodes based on phase change materials. A maximum thermal rectification ratio of  $\sim 2.95$  has been estimated from the experimental results, which, to the best of our knowledge, is the highest thermal rectification ratio demonstrated by a thermal diode based on a phase change material to date. Furthermore, such a result has theoretically been confirmed by using the thermal conductivity tensor theory for anisotropic heat conduction of solids, and these values match quite well. In this sense, guided by our analytical theory, we might infer that in lattice transition phase change materials, the rectification factor seems to be limited by the ratio of the principal thermal conductivity tensor components present in each phase, which is an important contribution of the present research. Hence, the obtained results are paramount to the development of enhanced performance thermal diodes for thermal energy harvesting, and management.

## Author contributions

J. A. Q. developed and supervised the conceptualization and methodology of the project, and wrote the original draft, and funding acquisition. M. A. C. C. synthesized materials and samples, as well as carried out chemical, structural and morphological analysis. J. A. L. G. implemented the experimental procedure for thermal characterization of materials and devices. All authors contributed equally to data examination and discussion.

## Conflicts of interest

The authors declare no conflict of interest.

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