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# Reversible electrowetting transitions on superhydrophobic surfaces

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An electric field applied across the interface has been shown to enable transitions from the Cassie to the Wenzel state on superhydrophobic surfaces with miniature corrugations. Molecular dynamics (MD) simulations manifest the possibility of reversible cycling between the two states when narrow surface wells support spontaneous expulsion of water in the absence of the field. With approximately 1 nm sized wells between the surface asperities, the response times to changes in the electric field are of  $O(0.1)$  ns, allowing up to GHz frequency of the cycle. Because of the orientation preferences of interfacial water in contact with the solid, the phenomenon depends on the polarity of the field normal to the interface. The threshold field strength for the Cassie-to-Wenzel transition is significantly lower for the field pointing from the aqueous phase to the surface; however, once in the Wenzel state, the opposite field direction secures tighter filling of the wells. Considerable hysteresis revealed by the delayed water retraction at decreasing field strength indicates the presence of moderate kinetic barriers to expulsion. Known to scale approximately with the square of the length scale of the corrugations, these barriers preclude the use of increased corrugation sizes while the reduction of the well diameter necessitates stronger electric fields. Field-controlled Cassie-to-Wenzel transitions are therefore optimized by using superhydrophobic surfaces with nanosized corrugations. Abrupt changes indicate a high degree of cooperativity reflecting the correlations between the wetting states of interconnected wells on the textured surface.

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## 1 Introduction

Electrowetting allows the precise tuning of solid–liquid interfacial tension by the adjustment of the applied electric field across the interface.<sup>1,2</sup> This method is applicable in various geometries including corrugated surfaces.<sup>3,4</sup> When the surface material is sufficiently hydrophobic, a corrugated surface in contact with water can exist either in the fully permeated Wenzel state or in the Cassie state where liquid maintains contact with the top area of the asperities but minimizes the energetically unfavorable solid/liquid area by avoiding the wells between pillars.<sup>5–7</sup> Transitions between the two states, driven by changes in the pressure, temperature, or applied field, are subject to strong hysteresis that typically prevents the recovery of the Cassie state<sup>4</sup> when it becomes thermodynamically favored. Kinetic barriers between the two states can be significantly reduced by using nanocorrugated surfaces<sup>8,9</sup> or a multi-level topography extending to the nanoscale regime.<sup>10</sup> Because of shortened timescales associated with cavitation in

nanosized wells,<sup>11,12</sup> molecular simulations present a valuable tool to study this regime.<sup>8,9</sup>

In the present work, we use molecular dynamics simulations to explore the possibility of reversible cycling between the Cassie state favored in the unperturbed system and the Wenzel state induced by the applied electric field. The persistence of the metastable Wenzel state after the cessation of the external field<sup>4</sup> is related to the free-energy cost associated with the liquid/vapor area ( $a_{lv}$ ) created during vapor cavitation in the wells. In the case of macroscopic corrugations, activation free energy (dominated by the term  $a_{lv}\gamma$  where  $\gamma$  is the surface tension)<sup>12–15</sup> can substantially exceed thermal energy ( $kT$ ). In nanometer-sized pores with cavity surfaces  $a_{lv}$  of  $O(\text{nm}^2)$ , on the other hand, the barriers can descend to  $O(10) kT$  and are readily overcome by thermal fluctuations.<sup>8,9</sup> At the same time, narrower wells are harder to turn to the Wenzel state as the required pressure or electric stress<sup>16</sup> increases roughly in proportion to the inverse confinement diameter,  $d^{-1}$ .<sup>17</sup> Following previous work, we model the superhydrophobic surface as a pillared surface with ‘wells’ corresponding to the free space between the four adjacent pillars, and diameter  $d$  is determined by the spacing between the opposite pillars.<sup>8</sup> A similar topology with somewhat increased dimensions was examined in ref. 9. Our study explores if surface wells

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sufficiently narrow to expel water in the absence of an external field can still be wetted under experimentally realizable electric fields. Our molecular dynamics simulations manifest the existence of a regime of pore widths where hydrophobic grooves wet at achievable fields and hysteresis is adequately alleviated to allow the transition in both directions, enabling significant wettability changes under reversible electric control. At near-molecular dimensions of the corrugations where most of the water molecules in the well are in contact with the surface, the necessary field strength is shown to depend on the *polarity* of the field orienting the molecules in the hydration layer. Earlier studies revealed a stronger wetting propensity in fields pointing from the nonpolar solid into the aqueous phase (by convention, this direction is defined as a positive field).<sup>18,19</sup> On a superhydrophobic surface, positive field results in a more compact well filling in the completed Wenzel state. However, when the substrate consists of decorated graphene, alignment in the negative field supports attractive correlations among water dipoles *across* the sheet facilitating the initial wetting of the wells. In these cases, the threshold field strength triggering intrusion is *lowered* in the negative (outgoing) field although it ultimately leads to a somewhat inferior filling of the wells. With nanosized corrugations, response times indicated by the simulations in changing field or from fluctuation relaxation are typically within a sub-nanosecond range. Because transitions between the Cassie and Wenzel states involve the exchange of water between the wells and the aqueous phase just above the surface, the observed timescales and transition field strengths (of  $O(10^{-3}) \text{ \AA}^{-1}$ ) should be at most weakly affected by the size of the sampled area and are hence equally applicable to macroscopic surfaces with identical corrugations.

## 2 Model and methods

### 2.1 The model system

Our model system is designed for studies of reversibility and dynamics of wetting transitions between the Cassie and Wenzel states on a nanopillared surface submerged in water under ambient conditions. The transition from the superhydrophobic Cassie state to the water-permeated Wenzel state is induced by a localized electric field spanning the interface. To ensure the surface's ability to support a stable Cassie state, we employ a surface topology tested in an earlier study<sup>8</sup> of field-free systems. The nanostructured surface consists of a graphene-like monolayer with bi-atomic posts (two-atom wide and two-atom tall) carved out of (hypothetical) 2nd and 3rd graphitic layers atop the continuous bottom sheet (Fig. 1).

The stoichiometric surface-coverage (ratio of the number of pillar atoms in either of the top two layers divided by the number of atoms in the bottom graphene layer) is 1/16. Because of the horizontal shift of consecutive graphite layers, the posts are not entirely vertical as shown in the side view of the system in Fig. 2b. A full description of the pillar topology is given in an earlier study.<sup>8</sup> The precise positions of pillar atoms correspond to the 3rd system in Fig. 1 of that work. Since the Lennard-Jones

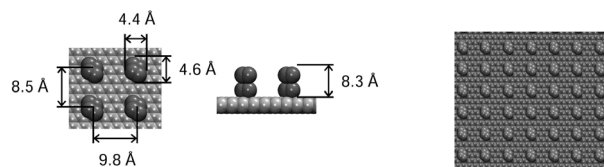


Fig. 1 Topological details (left) and top view (right) of the corrugated surface. The posts of specified dimensions are planted along lateral ( $x, y$ ) directions on the surface, which spans the entire box in the  $y$  direction, while it is of finite width smaller than the width of the box in the  $x$  direction. The system is periodically replicated along the  $x$  and  $y$  directions.

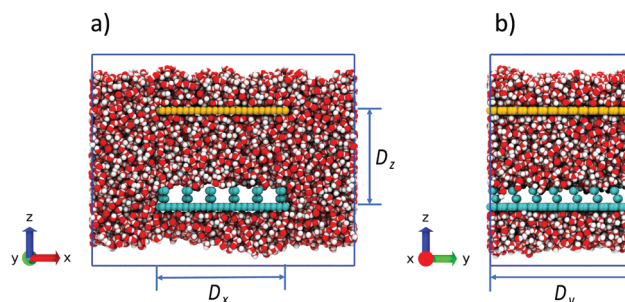


Fig. 2 Side views of field-free (the Cassie state) simulation box from the (a)  $y$  and (b)  $x$  directions. The superhydrophobic surface is shown in cyan and the weakly hydrophilic confinement wall at height  $D_z = 40 \text{ \AA}$  in yellow. The superhydrophobic area has a finite width ( $54 \text{ \AA}$ ) along the  $x$  axis. In view of lateral periodicity, the surface is of infinite length in the  $y$  direction.

diameter of carbon atoms ( $\sim 3.2 \text{ \AA}$ ) considerably exceeds the distance among the covalently bonded atoms in graphene, the projected area of a two-atom wide pillar is  $\sim 2.3$  times bigger than for a pair of graphene atoms, bringing the surface fraction  $f$  covered by the pillars close to  $f = 1/7$ , well above the stoichiometric coverage. The sterically excluded volume of the pillars (volume inaccessible to the centers of water molecules) extends to the height of  $\sim 8.3 \text{ \AA}$ . The Wenzel roughness factor  $r$  defined as the relative increase of the solvent-accessible surface area due to the corrugations is  $r \sim 5.1$ .

All carbon atom positions are kept fixed during the simulation. The length of the sheet in the  $y$  direction,  $D_y$ , is  $59.6 \text{ \AA}$  and is periodically replicated according to laterally periodic boundary conditions. The length  $D_y$  corresponds to 7 rows of posts and 7 grooves (Fig. 2b) inside the simulation box. Surface width along the  $x$  direction  $D_x = 54 \text{ \AA}$ . This width accommodates 6 rows of posts and 5 grooves of consecutive wells. To maintain constant pressure of the bulk-like environment, the field-exposed region spanning the space between the corrugated surface and a hydrophilic plate at the height  $D_z = 40 \text{ \AA}$  is embedded in a bigger reservoir between a pair of repulsive surfaces placed at the top and bottom of the simulation box to conserve the number of molecules in the system. The width of the box along the  $x$  axis equals twice the width of the corrugated surface enabling the free flow of water between the bulk and confined phases (Fig. 2a). The upper surface placed  $40 \text{ \AA}$  above the corrugated one has



identical dimensions but is weakly hydrophilic and devoid of corrugations (Fig. 2). The simulation box size is  $110 \text{ \AA} \times 59.6 \text{ \AA} \times 96.7 \text{ \AA}$ . The height ( $96.7 \text{ \AA}$ ) does not include the free space added between the replicated boxes in the vertical dimension to accommodate the 2-dimensional periodic conditions.<sup>20</sup> The system is filled with water from a previously equilibrated bulk while removing redundant molecules at the positions of vapor pockets or overlapping with the walls. Two  $5 \text{ \AA}$  wide slab-shaped bubbles parallel to the two surfaces at the top and bottom of the box (Fig. 2) are left empty in order to allow the system to self-barostat<sup>21–23</sup> when the electric field is applied. The net number of water molecules in the box is 13 494. Fig. 2 shows the snapshots of the box in the absence of the field when the system is in the Cassie state.

## 2.2 Simulation method and force field

Molecular dynamics simulations were performed using the modified version of the LAMMPS package,<sup>24</sup> which includes the in-house setup to model the localized electric field inside the confinement. The field smoothly fades away at the boundary with the unperturbed reservoir.<sup>17,23</sup>

To enable continuity and facilitate comparisons with previous studies,<sup>8,9,18,25–37</sup> water was modelled using the SPC/E potential<sup>38</sup> known for satisfactory performance in characterizing the dielectric properties of interfacial water.<sup>39,40</sup> The nanostructured surface was characterized by Lennard-Jones parameters for carbon atoms  $\sigma_{cc} = 3.2145 \text{ \AA}$  and  $\epsilon_{cc} = 0.151 \text{ kJ mol}^{-1}$  (systems 1–7 of Werder and coworkers<sup>41</sup>). The cutoff distance of  $11 \text{ \AA}$  was used to truncate Lennard-Jones and real-space electrostatic interactions. The PPPM algorithm was used for long-range electrostatics. Due to the presence of the two vapor pockets, the periodic boundary conditions were limited to the  $xy$  directions along with the Yeh-Berkowitz Ewald sum correction.<sup>20</sup> The two repulsive walls placed at the top and bottom faces of the simulation box interacted with water *via* a harmonic repulsion with a spring constant of  $40 \text{ kJ \AA}^{-1}$  and cutoff distance of  $5 \text{ \AA}$ . Serving solely as a barrier preventing any vapor molecules from escaping from the box, the precise form of this short-range repulsion showed no visible effects on the conditions of the system. Nose-Hoover thermostat acting on water molecules was applied to maintain the temperature at  $300 \text{ K}$ .

The upper confinement wall devoid of corrugations (yellow) was rendered slightly hydrophilic by using Lennard-Jones parameters for wall atoms  $\sigma_w = 3.2145 \text{ \AA}$  and  $\epsilon_w = 0.489 \text{ kJ mol}^{-1}$ , which correspond to the water/wall contact angle just below  $90^\circ$  in the absence of water on the opposite side of the sheet.<sup>41,42</sup> When water is present on both sides, the contact angle is reduced to  $\sim 82^\circ$ ,<sup>42,43</sup> which proves sufficient to trigger spontaneous filling of the *laterally finite* confinement between the superhydrophobic bottom surface and the weakly hydrophilic one on the top when the simulation starts with an initially empty confinement. Fig. 3 shows the equilibrium density profile of water in the simulation cell in the Cassie regime in the absence of an electric field.

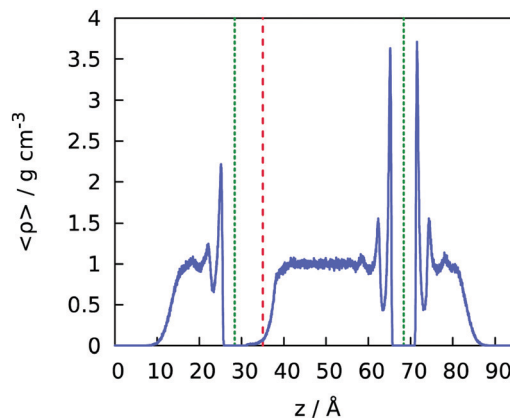


Fig. 3 Water density profile along the normal to the surfaces in the simulated system with wall-wall separation  $D_z = 40 \text{ \AA}$  in the Cassie state (no electric field). The green-dotted line on the left corresponds to the positions of the bottom graphene layer of the superhydrophobic surface and the second green line marks the upper (hydrophilic) wall of the confinement. The red-dashed line denotes the height of the centers of carbon atoms at the top of the pillars. The space between the left green and red lines includes surface wells permeated by water when the system is in the Wenzel state.

Lennard-Jones interactions among the distinct atom species (here denoted by subscripts a and b) were determined according to the Lorentz-Berthelot mixing rules<sup>44</sup>  $\epsilon_{ab} = (\epsilon_{aa}\epsilon_{bb})^{1/2}$  and  $\sigma_{ab} = (\sigma_{aa} + \sigma_{bb})/2 \text{ \AA}$ . With the above choices, the contact angle of water on the superhydrophobic surface calculated from the extrapolated nanodroplet contour as described in full detail in ref. 8 was  $150 \pm 10^\circ$ .

## 2.3 Localized electric field

To restrict the applied electric field to the confinement, we adopt the formulation previously developed for the disk-like shape of the pore. The unscreened (input) field  $E_z^i = E_0$  is presumed to be uniform within the confinement area corresponding to  $r < r_{in}$  (Fig. 4), where  $r$  denotes the absolute distance from the  $y$  axis. In this region,  $E_x^i = E_y^i = 0$ . To secure a smooth fading of the field at the confinement boundaries, necessary for correct integration of equations of motion,<sup>17,23</sup> the field decays from its core value to zero over the interval  $r_{out} \geq r \geq r_{in}$ , with  $r_{out} = D_x/2$ . The decay is described by the expression<sup>45</sup>

$$E_z^i(r) = f(r)E_0 \quad (1)$$

where  $f$  represents the smoothing function

$$f(r) = 1 \text{ if } r < r_{in},$$

$$f(r) = \frac{1}{2}(\cos(r_s) + 1) \text{ if } r_{in} < r < r_{out} \quad (2)$$

and

$$f(r) = 0 \text{ if } r > r_{out}$$

Since  $\mathbf{E}$  is a conservative vector field, the variation of  $E_z$  with  $r$  implies the simultaneous variation of  $E_x$  inside the transition



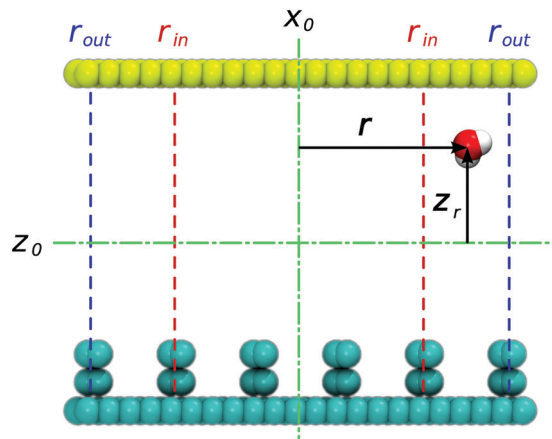


Fig. 4 Partitioning of the confinement along coordinate  $x$ . The central region between the red vertical lines corresponds to the uniform field and the outer regions between the blue and red lines feature a gradual decay of the field vanishing at the confinement boundary ( $|x| = r_{\text{out}}$ ).

region  $r_{\text{in}} < r < r_{\text{out}}$

$$E_x^i(r_s, z_r) = -\frac{\pi}{2} \sin(r_s) \frac{z_r}{r_{\text{out}} - r_{\text{in}}} E_0 \quad (3)$$

where  $r_s = \frac{r - r_{\text{in}}}{r_{\text{out}} - r_{\text{in}}}$  and  $z_r = z - z_0$ .

with  $z_0 = D_z/2$ . As described in detail in the former work,<sup>45</sup> the above formulation prevents the temperature drift observed in the MD simulation in the presence of a discontinuous electric field. The  $\sim 1$  nm wide transition window  $r_{\text{out}} \geq |x| \geq r_{\text{in}}$  coincided with the area occupied by the two edge grooves ( $r_{\text{out}} \sim 26$  Å and  $r_{\text{in}} \sim 16$  Å) such that a uniform field of maximal strength ( $E_0$ ) pervaded the three central grooves on the surface.

### 3. Results and discussion

#### 3.1 Reversibility of superhydrophobic transition

Below we present the results for water infiltration into and evacuation from the wells observed when the surface was exposed to a slowly increasing electric field to span a predetermined interval of strengths. At a maximal field, the process was reversed and the field gradually returned to zero. The cycle was repeated several times in two distinct sets of runs, one with a positive field (pointing from the superhydrophobic surface to the liquid) and the other with a negative field.

The field strength was controlled through the imposition of a uniform (non-screened) field  $E_z = E_0$ , applied in the aqueous core inside the confinement over lateral distances  $|x| < r_{\text{in}}$ . At distances  $r_{\text{in}} < |x| < r_{\text{out}} = D_x/2$ , the field  $E_z$  gradually decays and reaches zero at  $x = \pm D_x/2$  (see Fig. 4 and eqn (1)–(3)). While the applied field  $E_0$  represents the natural input for molecular simulations in a dielectrically nonuniform system, the actual, spatially varying field modified by dielectric screening emerges as a result of the simulation. In our system,  $E_0$  was increased from 0 to  $0.12 \text{ V Å}^{-1}$  in increments of  $0.005 \text{ V Å}^{-1}$  every 100 ps over 2.4 ns when the trend was reversed. We estimated the *mean* strength of the actual (screened) field inside the confined

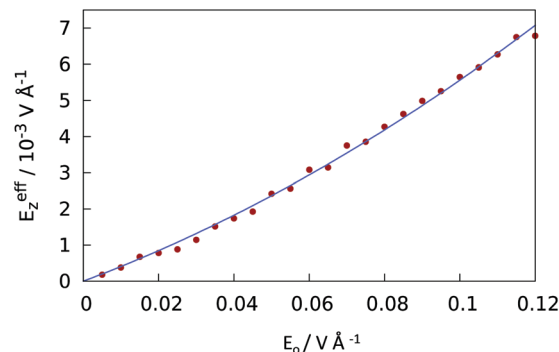


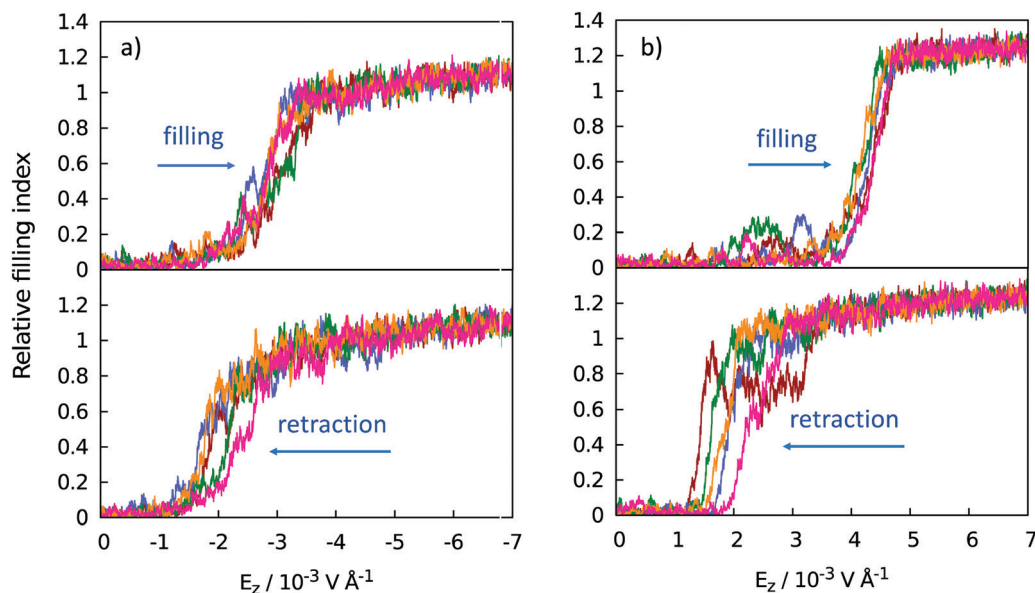
Fig. 5 Average screened electric field  $E_z^{\text{eff}}$  spanning the aqueous slab in the confinement as a function of the input (nonscreened) field  $E_0$ . The ratio  $E_0/E_z^{\text{eff}} \sim 25.5$  at  $E_z = 0$  and  $\sim 17$  at the strongest field provides an estimate for the effective dielectric constant ( $\langle 1/\epsilon \rangle^{-1}$ ) inside the water slab at different field strengths. Reduction with the field reflects dielectric saturation.

aqueous phase from the calculated water polarization<sup>46</sup> as described in ref. 23. Fig. 5 shows the average *dielectrically screened* field,  $E_z^{\text{eff}}$ , in the confined aqueous slab above the superhydrophobic surface as a function of the nonscreened input field  $E_0$ .  $E_z^{\text{eff}}$  varies between 0 and  $0.007 \text{ V Å}^{-1}$ , which corresponds to the spatially averaged  $z$  component of the (tensorial) dielectric constant  $\langle 1/\epsilon_{zz} \rangle^{-1}$  between  $25.5 \pm 1$  at vanishing fields and  $17 \pm 1$  at the strongest field considered. The zero-field value of  $\langle 1/\epsilon_{zz} \rangle^{-1}$  agrees well with the linear response result for the static dielectric constant in SPC/E water in a hydrophobic slit<sup>40</sup> of width 3.1 nm (this width is essentially equal to the separation between the asperity tips and the upper confining wall in our system). In all results presented below, we report  $E_z^{\text{eff}}$  values deduced from the input  $E_0$  using the smooth calibration curve from Fig. 5. Since there is no uncertainty in  $E_0$ , the accuracy of the reported  $E_z^{\text{eff}}$  values depends solely on any systematic imprecision of the calibration. Given the large number of points used to determine the calibration curve, any uncertainty of the curve is much smaller than for individual points and hence insignificant for present purposes. Furthermore, eventual imprecision can only lead to a systematic error without affecting *relative* field strengths when comparing the results for a narrow range of fields in the proximity to the Cassie-to-Wenzel transition. The maximal effective field considered ( $E_z^{\text{eff}} = \pm 0.007 \text{ V Å}^{-1}$ ) is well below the decomposition field  $E_d$  of water ( $E_d \sim 0.3 \text{ V Å}^{-1}$ )<sup>47</sup> and about an order of magnitude weaker than fields in ion channels, reverse micelles, near polyelectrolyte chains<sup>48–51</sup> or at the tip/solution interface in AFM measurements.<sup>52</sup> Experimentally, deionized water in a micron-sized capacitor was shown to sustain static field of strength  $0.012 \text{ V Å}^{-1}$  over long times when current is prevented by adequate insulation and the stability is increased further by descending to submicron pores.<sup>53</sup>

Fig. 6 illustrates the filling and evacuation transitions observed under the influence of the cycling field. Transitions are reflected in water uptake or release by the wells, quantified in terms of the relative filling index for all the wells on the substrate. Index 0 applies to the Cassie state, and values at or







**Fig. 6** Relative filling of the wells on the superhydrophobic surface as a function of the average (dielectrically screened) electric field  $E_z^{\text{eff}}$  in water above the surface. (a) The negative (downward) field pointing from the aqueous phase to the superhydrophobic surface. (b) The positive (upward) field. Top panels: Intrusion curves observed as the field gradually increases. Bottom panels: Retraction curves describing delayed expulsion of water in weakening field. The arrows show the direction of the change. Pronounced hysteresis is explained in terms of activation barrier to expulsion. The negative (downward) field enables transition to the Wenzel state at lower field strength; however, the plateau uptake of water in the wells is stronger in the positive field. Five repeated cycles (denoted with different colors) are shown for each system.

above 1 apply to the Wenzel state of the superhydrophobic surface. Index 1.00 corresponds to 275 water molecules confined inside the grooves on the entire surface measured at the minimal field securing a complete Wenzel state, *i.e.*, negative (downward) field  $E_z^{\text{eff}} \sim -0.0033 \text{ V Å}^{-1}$ . Continued compression brings the filling index well above 1.00 with further strengthening of the field.

Simulation results show that transitions between the Cassie and Wenzel states can be controlled reversibly by the external electric field. Distinct intrusion field strengths are observed for different polarities of the field. While field strengths we consider have a small impact on the structure of liquid water<sup>32,46</sup> they can affect the liquid/solid interaction. Enhanced surface wettability<sup>18,19</sup> demonstrated in fields pointing toward the aqueous phase (positive field in the present setup) explains superior filling of the wells under positive fields. The threshold intrusion field is, however, weaker when the field is negative. This is possible since molecular orientations relative to the surface only become significant at close contact, corresponding to compressed situations in well-established Wenzel states. At the early stage of intrusion, there are very few contacts with the wall and the alignment with the negative field (hydrogens pointing toward the surface) is preferable with respect to long-range dipole correlations with water molecules in the polarized hydration layer *below* the substrate surface. Dipolar correlations across thin surfaces like graphene have been well established<sup>42,43</sup> and the molecules below the sheet show preference for hydrogens pointing slightly away from the sheet.<sup>18,35,43</sup> This causes unfavorable interactions with water dipoles aligned by the positive field. The disadvantage,

reflected in a shallow barrier to intrusion in the positive field, is outweighed by orienting water/wall forces<sup>18,54</sup> cooperating with the field-induced alignment when the molecules are brought into direct contact with the sheet in a complete Wenzel transition. With our simplified model surface, preferred water orientations stem solely from generic steric effects and the trend to optimize hydrogen bonding among the water molecules without addressing the possibility of additional orienting effects that can be expected on polar surfaces.<sup>37,55–57</sup>

The presence of a barrier to water infiltration into the wells is also indicated by the spread of sampled intrusion field strengths in repeated runs under the positive field. According to the above arguments, the advantage of earlier transition to the Wenzel state in the negative field should diminish with the increasing thickness of the substrate.

The appreciable hysteresis shown in Fig. 6 and the strong size-dependence of kinetic barriers to water expulsion from the wells indicate that reversible cycling would be hard or impossible in wider wells. Narrower wells, on the other hand, require stronger intrusion fields.<sup>17</sup> The reversible electric control of the Cassie-to-Wenzel transitions illustrated in the above examples is hence of primary interest on superhydrophobic surfaces with nanosized corrugations.

Abrupt changes between the Cassie and Wenzel states on the entire surface illustrated in Fig. 6 point to cooperative processes where most of the wells fill or evacuate together. In view of the connectedness of the wells on a pillared surface, wetting or dewetting of an individual well affects the filling probability of its neighbors. To quantify this correlation, we define a spatial correlation function  $C(r_i, r_j)$  between two wells



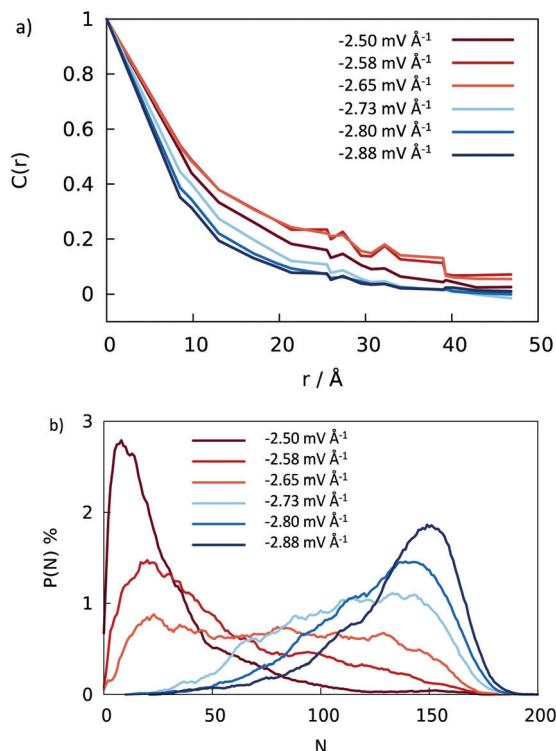


Fig. 7 (a) Spatial correlation among the numbers of water molecules residing in distinct wells at center-to-center distance  $r = r_i - r_j$  on a superhydrophobic surface for a set of negative (downward) fields  $E_z^{\text{eff}}$  close to the onset of the Cassie-to-Wenzel transition. (b) Probability distributions (in arbitrary units) of well filling quantified by the number of water molecules  $N$  residing inside the *three central grooves* comprising 21 wells.  $N \geq 165$  corresponds to fully filled (Wenzel state) wells. The curves show equilibrium probabilities for a set of effective fields  $E_z^{\text{eff}}$  in the proximity of the Cassie-to-Wenzel transition, which is indicated at the average field of  $\sim -2.7 \pm 0.1 \text{ mV \AA}^{-1}$ .

with well center positions  $r_i$  and  $r_j$  on the super-hydrophobic surface

$$C(r_i, r_j; E) = \frac{\langle N_i N_j \rangle}{(\langle N_i^2 N_j^2 \rangle)^{1/2}} \quad (4)$$

where  $N_i$  is the instantaneous number of molecules inside the well at  $r_i$  and  $\delta N_i = N_i - \langle N_i(E) \rangle$  measures the fluctuations of the local population of water in a specified well and field strength. Fig. 7a shows the equilibrium correlation functions calculated for a set of adjacent field strengths  $E_z^{\text{eff}}$  including the threshold field strength for the formation of the Wenzel state in the three central grooves on the surface. In this calculation, we exclude the grooves at both surface edges from the averages to consider only wells at an essentially identical electric field. The averages include all well pairs separated by the specified distance  $r$ . The samples were taken from 14 ns trajectories for each of the selected field strength. Appreciable correlations among the neighboring wells support a cooperative transition as further illustrated in Fig. 7b, which shows equilibrium filling probabilities for the three central grooves at the identical set of electric fields. A tiny change in the strength of the applied field

is sufficient to revert the filling state of the wells on the entire area subjected to the specified field. As expected,<sup>58</sup> the correlation length increases with the *proximity* to the liquid/vapor coexistence in the grooves, which explains the initial increase of the range of correlations as the field approaches the threshold strength, followed by gradual reduction if the field strength continues to increase beyond the threshold value. While partial filling with a shallow bimodal distribution is indicated very close to the transition in the negative field, a much more abrupt transition involving only entirely vacant or completely wetted grooves was observed in the positive fields near the transition point precluding any sampling of intermediate situations.

### 3.2 Dynamics

**3.2.1 Fluctuation rate in equilibrium.** The characteristic response time for the changes of water content in the wells can be estimated by monitoring the temporal fluctuations of the number of molecules residing inside the surface wells under equilibrium conditions. For this purpose, we monitor the time correlation function

$$C(t; E) = \frac{\langle N(t)N(0) \rangle}{(\langle N(0)^2 \rangle)} \quad (5)$$

where  $N$  is the total number of molecules residing in surface wells and  $\delta N(t) = N(t) - \langle N(E) \rangle$  is the fluctuation from long time average at specified field strength. For the Wenzel states, the logarithmic plots of  $C(t)$  show approximately stretched exponential dependence of  $C(t)$  on time but the dependence is nearly mono-exponential in the vicinity of the Cassie-to-Wenzel transition. Fig. 8 shows the correlation function  $C(t)$  for the central grooves at the transition field,  $E_z^{\text{eff}} = -2.7 \pm 0.1 \text{ mV \AA}^{-1}$ . Under these conditions, the fluctuations decayed with a correlation time of  $\sim 0.39 \pm 0.02 \text{ ns}$ .

**3.2.2 Nonequilibrium transitions.** While relaxation times vary with the strength of the applied field, the order of magnitude,  $O(10^{-1}) \text{ ns}$ , appears preserved over a wide range of conditions including equilibration processes changing the

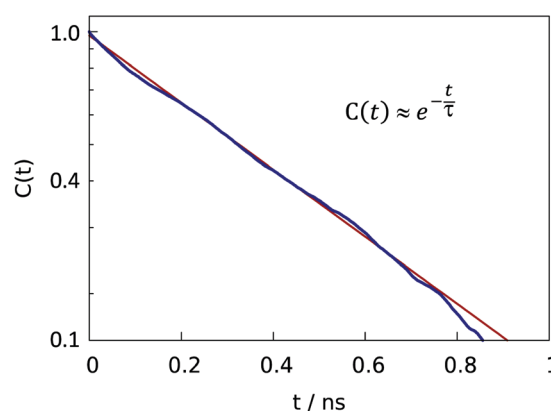


Fig. 8 Semilogarithmic plot of time correlation function describing fluctuations of water content (eqn (5)) in central grooves on the superhydrophobic surface at the Cassie-to-Wenzel transition field strength  $E_z^{\text{eff}} = -2.7 \pm 0.1 \text{ mV \AA}^{-1}$ . At given field strength, the decay of  $C(t)$  is approximately exponential with characteristic time  $\tau \sim 0.39 \text{ ns}$ .



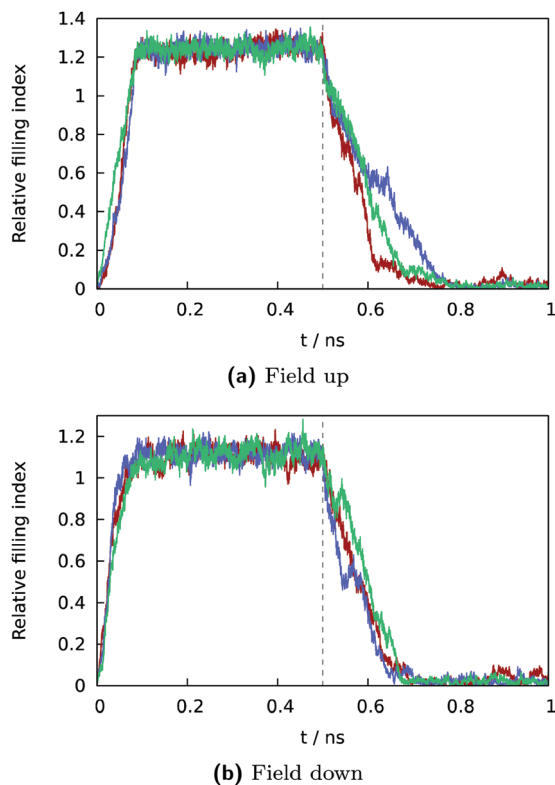


Fig. 9 Time dependence of relative groove filling following an abrupt imposition of field  $E_z^{\text{eff}} = 7 \text{ mV } \text{\AA}^{-1}$  (a) or  $-7 \text{ mV } \text{\AA}^{-1}$  (b) at time  $t = 0$  and cessation of the field at  $t = 0.5 \text{ ns}$  (vertical dashed line) from three distinct trajectories for each system. Different colors denote independent runs under identical conditions.

wetting state of the surface. Fig. 9 shows the results for the overall filling index as a function of time after an abrupt imposition, and subsequent cessation of the imposed field using the maximal field strength considered in the simulations illustrated in Fig. 6. The speed of response to the field change depends on the process (infiltration to or evacuation from the wells) and the direction of the field. When the field is imposed, the initially vacant wells fill with water in about 0.1 ns and the process is somewhat faster in the negative (downward) field. When the field is turned off, we first observe an instantaneous  $\sim 10\%$  reduction of the well occupancy due to the loss of electrostriction. On average, this stage corresponds to the expulsion of one water molecule from every well. Complete expulsion, delayed due to the kinetic barrier associated with the formation of a new liquid/vapor interface, follows in 0.2–0.3 ns and the process is slower (and less reproducible) in the system originally prepared under the positive (upward) field. The existence of different evacuation rates for opposite field polarities, observed even when the field is no longer present, is attributed to denser well filling by water achieved in the positive field *before* it was turned off. The observed trends appear consistent with the observations from Fig. 6. The correlation time of the spontaneous fluctuations of water content in the wells near 0.4 ns (Fig. 8) might suggest that smaller steps should be used to obtain full convergence of

cycles shown in Fig. 6 with respect to the increment size. However, multiple trial runs showed only an insignificant reduction of  $\sim 2 \times 10^{-4} \text{ V } \text{\AA}^{-1}$  for the intrusion fields (Fig. 6) when the averaging was performed using a ten times slower field increase rate and hence tenfold longer duration of the cycle.

### 3.3 Projections for macroscopic surfaces

While substantial computational costs precluded simulations for increased surface dimensions, the expected behavior of an extended superhydrophobic surface can be estimated from the simulated properties of the central grooves. Filling probabilities shown in Fig. 7b exclude the contributions from the grooves at the edges of the surface where the applied field (eqn (1)–(3)) is weaker than in the region above the central section. Comparison of the threshold fields for the formation of the Wenzel state in the central region (Fig. 7b) with the result for the entire surface (left panel of Fig. 6) shows the Wenzel state in the central region to occur at just about 5% weaker field than necessary to observe the transition over the entire model surface (Fig. 6). The results shown in Fig. 7 suggest that, for the corrugation topology used in this study, the negative (downward) field of strength of no more than  $E_z^{\text{eff}} \sim (2.7 \pm 0.1) \times 10^{-3} \text{ V } \text{\AA}^{-1}$  should suffice to trigger the Cassie-to-Wenzel state transition on experimentally relevant surfaces with macroscopic lateral dimensions. As long as the surface and applied field are uniform, essentially identical average transition rates should apply at any location on the entire surface. Increasing the size of the surface can slightly accelerate the overall dewetting transition as a bigger area provides more opportunities for initial vapor-nucleation events<sup>11,13</sup> that can stimulate the process in adjacent wells. In general, dynamic responses on a macroscopic surface should occur at timescales at least as fast as observed in finite-size model calculations.

## 4 Concluding remarks

Computational modeling of electrowetting on a textured surface manifests the possibility of reversible cycling between the Cassie and Wenzel states on a superhydrophobic surface with nanoscale corrugations. Nanosized wells capable of spontaneous expulsion of water in the absence of an external field can be brought to the Wenzel state by the application of experimentally achievable electric fields and the changes between the two states can occur below nanosecond timescales in both directions. The minimal field strength required to induce the Cassie-to-Wenzel state transition shows considerable dependence on field polarity. While the incoming field (pointing from the surface to water) produces more compact groove filling, the threshold field strength securing the transition is smaller in the field pointing toward the solid phase. The hysteresis of the wetting/expulsion cycle reflects a kinetic barrier to expulsion from surface wells and a shallower barrier is indicated to slow groove *wetting* primarily in the incoming field. The findings can assist the design of tunable



surfaces with large wettability amplitudes and essentially instantaneous response. Tunable superhydrophobic coating can also be used to control the permeability of nanochannels in nanofluidics,<sup>59,60</sup> e.g., in miniature lab-on-chip devices under electric control.

## Conflicts of interest

There are no conflicts to declare.

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