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Interactions in protein solutions close to liquid–liquid phase separation: ethanol reduces attractions *via* changes of the dielectric solution properties

Jan Hansen, ^a Rajeevann Uthayakumar,^a Jan Skov Pedersen, ^b
Stefan U. Egelhaaf ^a and Florian Platten ^{*ac}

Ethanol is a common protein crystallization agent, precipitant, and denaturant, but also alters the dielectric properties of solutions. While ethanol-induced unfolding is largely ascribed to its hydrophobic parts, its effect on protein phase separation and inter-protein interactions remains poorly understood. Here, the effects of ethanol and NaCl on the phase behavior and interactions of protein solutions are studied in terms of the metastable liquid–liquid phase separation (LLPS) and the second virial coefficient B_2 using lysozyme solutions. Determination of the phase diagrams shows that the cloud-point temperatures are reduced and raised by the addition of ethanol and salt, respectively. The observed trends can be explained using the extended law of corresponding states as changes of B_2 . The results for B_2 agree quantitatively with those of static light scattering and small-angle X-ray scattering experiments. Furthermore, B_2 values calculated based on inter-protein interactions described by the Derjaguin-Landau-Verwey-Overbeek (DLVO) potential and considering the dielectric solution properties and electrostatic screening due to the ethanol and salt content quantitatively agree with the experimentally observed B_2 values.

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1 Introduction

When the attractions between protein molecules are strong enough, protein solutions can undergo liquid–liquid phase separation (LLPS) into two coexisting phases, one enriched and one depleted in proteins. Such protein phase separation has severe implications in fundamental and applied fields of research, including cell biology, medicine, pharmaceutical industry, food processing, and protein crystallography. For example, LLPS is exploited *in vivo*: subcellular compartments, so-called membraneless organelles, are formed *via* LLPS in the cytosol, representing a way of intracellular organization and regulation of biochemical reactions.^{1,2} Furthermore, genetic mutations or altered physicochemical conditions inside a cell are likely to affect inter-protein interactions and thus to disturb LLPS.^{3,4} However, LLPS can also modulate the pathways and kinetics of pathological protein aggregation leading to severe

conditions for the patients.^{5,6} Protein solutions exhibit LLPS not only *in vivo*, but also *in vitro*.^{7,8} For example, antibodies, which are used as biopharmaceuticals in the treatment of various diseases,⁹ can undergo LLPS due to nonspecific antibody-antibody interactions.^{10–12} The dense-phase LLPS droplets might impair specific antibody-receptor interactions, enhance solution viscosity and cause immunogenicity, posing a major challenge to the formulation development.^{13,14} LLPS can also be employed for identifying conditions under which high-quality crystals grow, which are needed for crystallographic structure determination.¹⁵ Yet, attempts to crystallize proteins are still frequently based on trial and error. Close to the LLPS binodal enhanced protein crystal nucleation rates have been observed by simulations and experiments,^{16,17} and therefore the location of the LLPS boundary has been regarded as a predictor for optimized crystallization conditions,^{18,19} as neither too weak nor too strong attractions are considered to be well suited for crystallization.²⁰ Within the LLPS binodal, liquid-droplet nucleation or spinodal decomposition are typically faster than crystallization, thus leading to a two-step crystallization mechanism^{21,22} and altering crystallization kinetics.^{23,24}

Net attractions sufficient to induce LLPS can be achieved or avoided by dedicated changes of the physicochemical

^a Condensed Matter Physics Laboratory, Heinrich Heine University, Universitätsstraße 1, 40225 Düsseldorf, Germany. E-mail: florian.platten@hhu.de

^b iNANO Interdisciplinary Nanoscience Center and Department of Chemistry, Aarhus University, DK-8000 Aarhus C, Denmark

^c Institute of Biological Information Processing (IBI-4: Biomacromolecular Systems and Processes), Forschungszentrum Jülich, Wilhelm-Johnen-Straße, 52428 Jülich, Germany



properties of the solution, *e.g.*, by adding salts,^{25,26} excipients,²⁷ or non-aqueous solvents.^{28,29} Moreover, organic solvents, such as alcohols, can act as precipitants^{30,31} and as crystallization agents.^{32,33} For example, in blood plasma fractionation,^{34,35} moderate ethanol concentrations (up to 40 vol%) are used to obtain therapeutic protein products. If added at high concentrations or used at elevated temperatures, ethanol can destabilize and unfold proteins,^{36,37} which might even lead to amyloid fibril formation.^{38–40} Its effects on individual protein molecules^{41,42} are largely ascribed to its hydrophobic properties.⁴³ Ethanol is composed of a hydrophobic ethyl group and a hydrophilic hydroxyl group and can thus interact favorably with non-polar groups.³¹ However, far less (mechanistic) insight is established concerning the effects on inter-protein interactions, as relevant, *e.g.*, for LLPS.

The second virial coefficient B_2 represents an integral measure of the inter-protein interactions, which for a spherically symmetric potential $U(r)$ with center-to-center distance r reads

$$B_2 = 2\pi \int_0^\infty \left(1 - \exp\left[-\frac{U(r)}{k_B T}\right]\right) r^2 dr \quad (1)$$

with thermal energy $k_B T$. Upon addition of moderate alcohol concentrations, Liu *et al.*⁴⁴ observed an initial increase and then a plateau of B_2 , whereas Kundu *et al.*⁴⁵ reported a decrease for similar solution conditions. Direct and indirect mechanisms could be responsible for such effects: alcohol molecules might act as protein-binding ligands or induce nonlocal changes of the dielectric solvent properties. In view of the inconsistent results,^{44,45} both the effect and the underlying mechanism remain controversial.

Concepts developed in soft-matter physics^{46–48} have proven helpful to rationalize the inter-protein interactions and the related phase behavior. Experimental protein phase diagrams, including LLPS phase coexistence curves (binodals), are strikingly similar to those of colloids with short-ranged attractions,^{49,50} as encountered, *e.g.*, in square-well (SW) fluids^{49,51–53} or patchy particle systems.^{54–58} Furthermore, the structure factor of protein solutions close to phase separation has been described by Baxter's sticky particle model,^{19,59,60} for which an approximate analytical description is available.^{61,62} For colloids with short-ranged attractions, an extended law of corresponding states (ELCS) has been suggested by Noro and Frenkel,⁶³ according to which short-ranged attractive systems can be mapped onto an equivalent SW system, and the applicability of the ELCS to the binodals of protein solutions has been demonstrated.⁵³ The ELCS mapping thus reflects the insensitivity to the specific shape of the coarse-grained model potential, and in particular, it allows the estimation of B_2 based on cloud-point measurements.⁶⁴ In this context, the Derjaguin-Landau-Verwey-Overbeek (DLVO) theory has helped to rationalize the dependence of inter-protein interactions on simple salts, solvents or pH.^{65–69}

In the present work, the effects of moderate ethanol concentrations on protein molecules, inter-protein interactions as well as LLPS coexistence curves are studied using lysozyme in brine as a model system. Small-angle X-ray scattering (SAXS) was used for determining the form factor of protein molecules, thus confirming that the alcohol and salt have no influence on the structure of the individual molecules on the relevant length

scales. Cloud-point measurements are used to locate the LLPS binodal and to estimate B_2 exploiting the ELCS. SAXS is also used to study the structure factor of concentrated protein solutions close to phase separation. From the analysis of the SAXS data, B_2 is determined as a function of the ethanol content. The results confirm a universal temperature dependence of B_2 with respect to the critical LLPS temperature, as suggested by the ELCS. The dependence of B_2 on ethanol and salt content is quantitatively described by the DLVO theory taking only changes of the dielectric solution properties and the salt concentration into account. This work thus aims at a consistent picture of protein phase separation, a mechanistic explanation of solvent effects on inter-protein interactions and a resolution of controversial previous results.

2 Experimental methods

2.1 Sample preparation

Hen egg-white lysozyme was purchased from Sigma-Aldrich (prod. no. L6876) and used without further purification. For few SAXS experiments, lysozyme purchased from Roche Diagnostics (prod. no. 10837059001) was used, which led to consistent findings. Sodium chloride (NaCl), sodium acetate (NaAc) and ethanol (EtOH) were of reagent grade quality and used as received. Ultrapure water with a minimum resistivity of 18 M Ω cm was prepared using a water purification system.

Water-ethanol mixtures containing 50 mM NaAc were used as buffer solutions and adjusted to pH reading 4.5 by adding small amounts of hydrochlorid acid. At pH 4.5 each lysozyme molecule carries approximately 11.4 positive net charges.⁷⁰ Concentrated protein stock solutions were prepared by ultrafiltration, as described previously.²⁹ The protein, ethanol and salt content of the stock solutions was checked by refractometry. With respect to pH value (4.5) and NaCl concentrations (0.7 M and 0.9 M), solution conditions are chosen to resemble those of our previous studies^{71,72} to allow for a quantitative comparison. Concerning the ethanol content, low and moderate concentrations (up to 30 vol% in increments of 10 vol%) are considered, similar to those of Liu *et al.*⁴⁴ and Kundu *et al.*⁴⁵ At pH 2.2, where lysozyme is expected to be less stable than at pH 4.5, ethanol-induced (partial) unfolding of lysozyme was only observed for ethanol concentrations larger than 30 vol%.⁷³ Samples were prepared by mixing appropriate amounts of lysozyme, buffer and NaCl stock solutions. Protein concentrations c_p are related to the protein volume fraction $\phi = c_p/\rho_p$, where $\rho_p^{-1} = 0.740 \text{ cm}^3 \text{ g}^{-1}$ is the specific volume of lysozyme.²⁹ Mixing was performed at a temperature above the solution cloud-points to prevent immediate phase separation, typically at room temperature (21 ± 2) °C. Due to the high salt content, the samples were prone to crystallization²⁶ and hence investigated immediately after preparation. Cloud points were typically studied using three independently prepared samples for each condition in order to allow for a statistical analysis. For SAXS, some of the samples were measured more than once in order to check the reproducibility of our results.



2.2 Cloud-point temperature measurements

Metastable LLPS coexistence curves were determined by cloud-point temperature measurements. Samples with a typical volume of 0.1 mL were filled into thoroughly cleaned glass capillary tubes, sealed, and placed into a thermostated water bath at a temperature well above the cloud-point. A wire thermometer was mounted in a separate, but closely placed glass tube filled with 0.1 mL water. Then, the temperature of the water bath was gradually lowered and the sample solution visually observed. The cloud point was identified by the sample becoming turbid. Further details have been given previously.²⁹

2.3 Estimation of the second virial coefficient based on cloud-point measurements

The extended law of corresponding states (ELCS), suggested by Noro and Frenkel,⁶³ applies to colloidal system dominated by short-range attractions. It has been demonstrated⁵³ that it also applies to protein solutions, despite their complex interactions. According to the ELCS, these systems obey the same equation of state and hence their LLPS phase boundaries collapse onto one another, if expressed in suitable reduced quantities. The ELCS can be exploited to estimate the second virial coefficient.^{53,64} This is based on the critical temperature of the binodal and an effective hard-core diameter, which takes into account the repulsive inter-particle interactions and can be inferred from a one-parameter fit to the experimental gas branch of the binodal. Once these parameters are determined, the universal temperature dependence (with respect to the critical temperature) of the reduced second virial coefficient can be exploited to estimate the second virial coefficient at a given temperature. Details on this procedure have been given previously.⁵³

2.4 Small-angle X-ray scattering: instrumentation

Small-angle X-ray scattering (SAXS) was employed to determine the form factor of individual protein molecules to reveal possible shape or size changes as well as the structure factor characterizing the effective inter-protein interactions at temperatures close to, but above the solution cloud-points. SAXS experiments were performed using the laboratory-based facilities at the Interdisciplinary Nanoscience Center (iNANO) at Aarhus University, Denmark,⁷⁴ as well as at Center for Structural Studies at Heinrich Heine University Düsseldorf, Germany. In Aarhus, a NanoSTAR SAXS camera (Bruker AXS) optimized for solution scattering⁷⁵ with a home-built scatterless pinhole in front of the sample⁷⁶ was used to measure the scattered intensity of sample and buffer solutions. The solutions were filled in a thin flow-through glass capillary and thermostated using a Peltier element (Anton Paar). In Düsseldorf, SAXS measurements on sample and buffer solutions were performed on a XENOCS 2.0 device with a Pilatus 3 300 K detector. The solutions were injected into a thin flow-through capillary cell mounted on a thermal stage. Experiments were performed at 20.0 °C and 25.0 °C, respectively. Typical acquisition times of 10 and 5 min were used for dilute and

concentrated solutions (typically, 6 and 70 mg mL⁻¹), respectively. The data were background subtracted and converted to absolute scale using water in Aarhus⁷⁵ and glassy carbon in Düsseldorf as standards. The final intensity is displayed as a function of the magnitude of the scattering vector, $Q = (4\pi/\lambda_0) \sin(\theta)$, where the X-ray wavelength, λ_0 , is 1.54 Å and 2θ is the angle between the incident and scattered X-rays and calibration was performed using silver behenate.

2.5 Small-angle X-ray scattering: data analysis

Protein molecules tend to have anisotropic shapes; according to X-ray crystallography, lysozyme is approximately a prolate ellipsoid with an extension of $30 \times 30 \times 45$ Å.⁷⁷ For a monodisperse solution of particles with only a small anisotropy, the interactions can be assumed to be independent of the orientation. Then, the absolute scattered intensity $I(Q)$ can be described by the decoupling approximation:^{78–80}

$$I(Q) = K c_p M P(Q) S_{\text{eff}}(Q). \quad (2)$$

The Q dependence of the scattered intensity is due to intra-particle and inter-particle interference effects quantified by $P(Q)$ and $S(Q)$, respectively. The form factor $P(Q) = \langle A^2(Q) \rangle_{\Omega}$ is obtained from the form factor amplitude $A(Q)$ averaged (as denoted by brackets) over particle orientations Ω , and the effective structure factor reads

$$S_{\text{eff}}(Q) = 1 + \frac{\langle A(Q) \rangle_{\Omega}^2}{\langle A^2(Q) \rangle_{\Omega}} [S(Q) - 1], \quad (3)$$

where $S(Q)$ is the structure factor of an effective one-component system. The magnitude of the absolute scattered intensity depends on the particle (protein) mass concentration c_p , its molecular weight $M = 14\,320$ g mol⁻¹, and the contrast factor $K \sim (\Delta\rho)^2$ related to the electron density difference $\Delta\rho$ between particle and solvent, which can be computed.^{81,82}

For very dilute systems, $S(Q) \approx 1$ and the Q dependence of $I(Q)$ is determined by the size, shape and structure of the individual particles *via* $P(Q)$. In particular, the radius of gyration R_g , a measure of the particle size, can be inferred from the low- Q scattering. To describe the shape and structure of the lysozyme molecules, two different models for $P(Q)$ are considered here. On a coarse level,⁸⁰ the form factor of lysozyme can be modelled as a prolate ellipsoid of revolution with minor and major axes as parameters. Since the atomic coordinates of lysozyme are known (PDB file 1LYZ⁸³), the form factor can be calculated accurately using the programme CRY SOL,⁸⁴ which calculates the excess scattering and adds a 3 Å hydration shell with the shell electron density ρ_{sh} as a parameter.

In concentrated solutions, the structure factor $S(Q)$ contains information on the spatial arrangement of the particles and thus reflects inter-particle interactions. In a one-component system, the coexistence of two stable or metastable fluid phases is only possible if the particle interactions are net attractive. The square-well (SW) potential arguably represents the simplest model to describe the effective interactions of such a system.⁴⁹ It consists of a hard-core repulsion of range σ (the diameter of



the particle), which leads to excluded volume effects, and a constant attractive part, which has depth ε and extends to a distance $\lambda\sigma$ from the center. The adhesive hard-sphere (AHS) potential proposed by Baxter represents a specific limit of the SW potential:⁸⁵ the SW depth ε becomes infinite while the SW width $(\lambda - 1)\sigma$ becomes infinitesimal (*i.e.*, $\lambda \rightarrow 1$), such that the contribution to B_2 remains finite and nonzero:

$$\frac{U_{\text{AHS}}(r)}{k_{\text{B}}T} = \lim_{\lambda \rightarrow 1} \begin{cases} \infty & \text{for } 0 < r < \sigma, \\ \ln[12\tau(1 - 1/\lambda)] & \text{for } \sigma < r < \lambda\sigma, \\ 0 & \text{for } r > \lambda\sigma. \end{cases} \quad (4)$$

The corresponding Boltzmann factor reads

$$\exp[-U_{\text{AHS}}(r)/k_{\text{B}}T] = \Theta(r - \sigma) + \frac{\sigma}{12\tau}\delta(r - \sigma), \quad (5)$$

where the Heaviside step function Θ takes into account that overlap of the hard cores is not possible and the Dirac delta function favors contacts due to the stickiness parameter τ . The net interactions of the AHS potential, as quantified by B_2 (eqn (1)), are determined by only one parameter:

$$b_2 = 1 - \frac{1}{4\tau}, \quad (6)$$

where $b_2 = B_2/B_2^{\text{HS}}$ is the second virial coefficient of the system B_2 normalized by that of the corresponding hard-sphere system $B_2^{\text{HS}} = (2\pi/3)\sigma^3$. Approximate analytical descriptions of the structure factor of adhesive hard spheres in the Percus-Yevick closure are available^{61,62,86} and commonly used to model scattering data of short-range attractive systems.^{87,88} The AHS structure factor depends on the effective particle diameter σ , the stickiness τ and the particle volume fraction ϕ . The effective particle diameter σ is identified with the diameter of a sphere that has the same volume as the ellipsoid determined by form-factor modelling in a dilute solution. The volume fraction ϕ is related to the protein concentration c_{p} . Thus, only one fitting parameter, τ , has to be determined. To model the structure factor of proteins, inter-protein interactions are often described by the sum of an attractive and a repulsive hard-core Yukawa potential each with its own range and interaction strength parameter.^{89–92} However, close to LLPS, the interactions are dominated by net attractions and, hence, the simpler AHS description is favored here, allowing for a direct determination of b_2 .

The scattered intensity based on eqn (2) with a constant scattering background is fitted to the measured scattered intensity using a least-square routine. Since background subtraction is particularly delicate at very low Q , model fits are compared with experimental data for $Q \geq 0.015 \text{ \AA}^{-1}$. The contrast factor of lysozyme in the different water–ethanol mixtures is calculated using the MULCh software.⁸¹ To account for the experimental uncertainty in c_{p} , a deviation of up to 10% from its nominal value is allowed in fitting.

3 Results and discussion

First, the effect of moderate ethanol concentration on the size and shape of individual protein molecules is investigated by

SAXS. In a second step, LLPS coexistence curves are determined for various ethanol and salt compositions. Then, the structure factor of moderately concentrated systems close to LLPS is examined by SAXS measurements of concentrated samples. Both from the cloud-point measurements (by exploiting the ELCS) and from the SAXS data (by applying Baxter's AHS model), the normalized second virial coefficient b_2 is inferred. Finally, the dependence of b_2 on ethanol and salt content is rationalized based on DLVO theory.

3.1 Lysozyme molecular structure in water–ethanol mixtures

The scope of the present work is on the LLPS of folded, globular proteins,⁹³ whose interactions are tuned by the addition of ethanol and NaCl. However, ethanol can also denature and aggregate proteins.^{37,94,95} Therefore, the shape and size of individual lysozyme molecules in water–ethanol mixtures are determined.

Fig. 1 shows the scattered intensity $I(Q)$ of dilute protein solutions ($c_{\text{p}} \approx 6 \text{ mg mL}^{-1}$) under two particular conditions: (i) proteins in an aqueous solution with 0.9 M NaCl, which is used to screen electrostatic repulsions (squares), and (ii) proteins in a water–ethanol mixture with the highest ethanol concentration used in this work (30 vol% EtOH) with 0.9 M NaCl (diamonds). Experiments on intermediate ethanol concentrations show similar behavior. In Fig. 1(A), the experimental data for both conditions are shown with $I(Q)$ normalized by the ethanol-dependent contrast factor K , the molecular weight M and the protein concentration c_{p} . Since $S(Q) \approx 1$ in this case, eqn (2) implies that the data reflect the form factor $P(Q)$. The data obtained for the two different conditions do not show any significant difference in the covered Q range, indicating that the shape and size of the lysozyme molecules are not affected by 30 vol% ethanol. The Q dependence of the data exhibits a plateau with $I(Q)/Kc_{\text{p}}M \approx P(Q) \approx 1$ at low Q and a minimum at high Q which suggests a globular object. A Guinier analysis indicates radii of gyration $R_{\text{g}} = 15.5 \text{ \AA}$ (0 vol% EtOH) and $R_{\text{g}} = 14.9 \text{ \AA}$ (30 vol% EtOH). Radii of gyration determined in repeat measurements and experiments at intermediate ethanol concentrations range from approximately 15 to 17 \AA , indicating an experimental uncertainty of 1.1 \AA .

In Fig. 1(B), fits based on two different form factor models (lines) to the experimental data of the aqueous solution (symbols) are shown. The first form factor model is based on a prolate ellipsoid of revolution with a semi-minor axis 16.0 \AA and an axial ratio fixed at 1.5 (solid line), which describes the experimental data reasonably well. The second one is calculated *via* the CRY SOL programme⁸⁴ (dotted line) with ρ_{sh} in agreement with previous work.⁸⁴ It quantitatively reproduces the experimental data and thus agrees with the ellipsoid model except for minor differences at very high Q .

The experimental data and the analysis demonstrate that lysozyme molecules retain their compact native shape under all conditions studied. This is in line with a previous finding⁷³ that higher ethanol concentrations are required to induce unfolding, which might change protein size and shape.



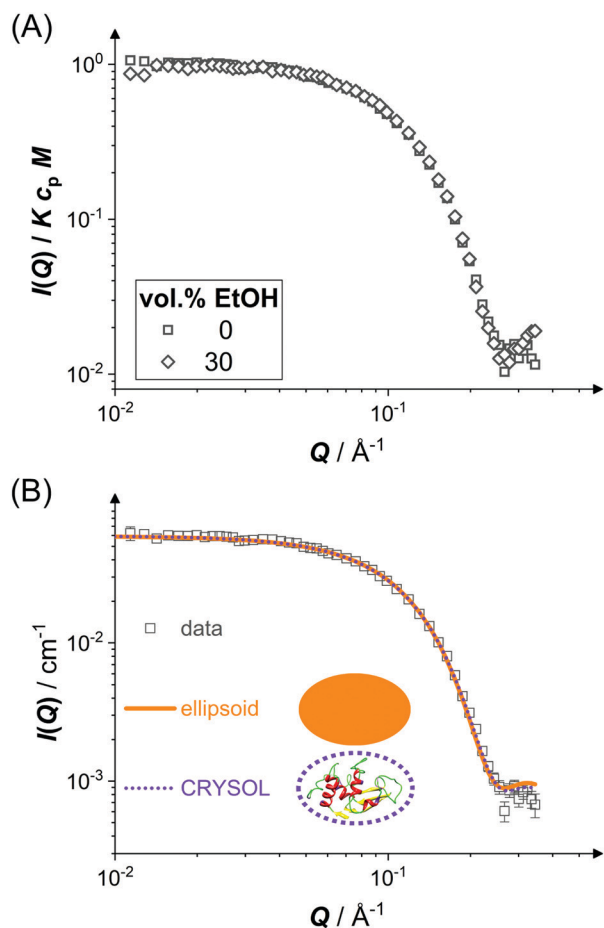


Fig. 1 Form factor of lysozyme molecules ($c_p \approx 6 \text{ mg mL}^{-1}$) in brine (0.9 M NaCl) without and with 30 vol% EtOH (squares and diamonds, respectively): (A) scattered intensity $I(Q)$ normalized by the contrast factor K , the molecular weight M , and the protein concentration c_p as a function of the magnitude of the scattering vector Q . (B) Scattered intensity $I(Q)$ as experimentally determined (squares as in (A)) and model fits (lines as indicated). Schematic drawings (not to scale) illustrate the two models. For the crystal structure, only the backbone is shown.

3.2 Liquid–liquid phase separation of lysozyme solutions in water–ethanol mixtures

Samples might show a macroscopic phase transition accompanied by a clouding of the system which indicates LLPS. The temperature at which the system becomes cloudy depends on the strength of the net attractions. Higher cloud-point temperatures indicate stronger net attractions. Cloud-point temperature measurements thus represent a simple way to characterize the inter-particle interactions.⁶⁴

Fig. 2(A) and (B) show the low-volume fraction branch of LLPS phase coexistence curves of lysozyme solutions in brine (0.9 and 0.7 M NaCl represented by open and closed large symbols, respectively) with and without ethanol being added. In the absence of ethanol, the data agree with literature results (small symbols).²⁸ With increasing protein concentration c_p , the cloud-point temperature T_{LLPS} first increases steeply,

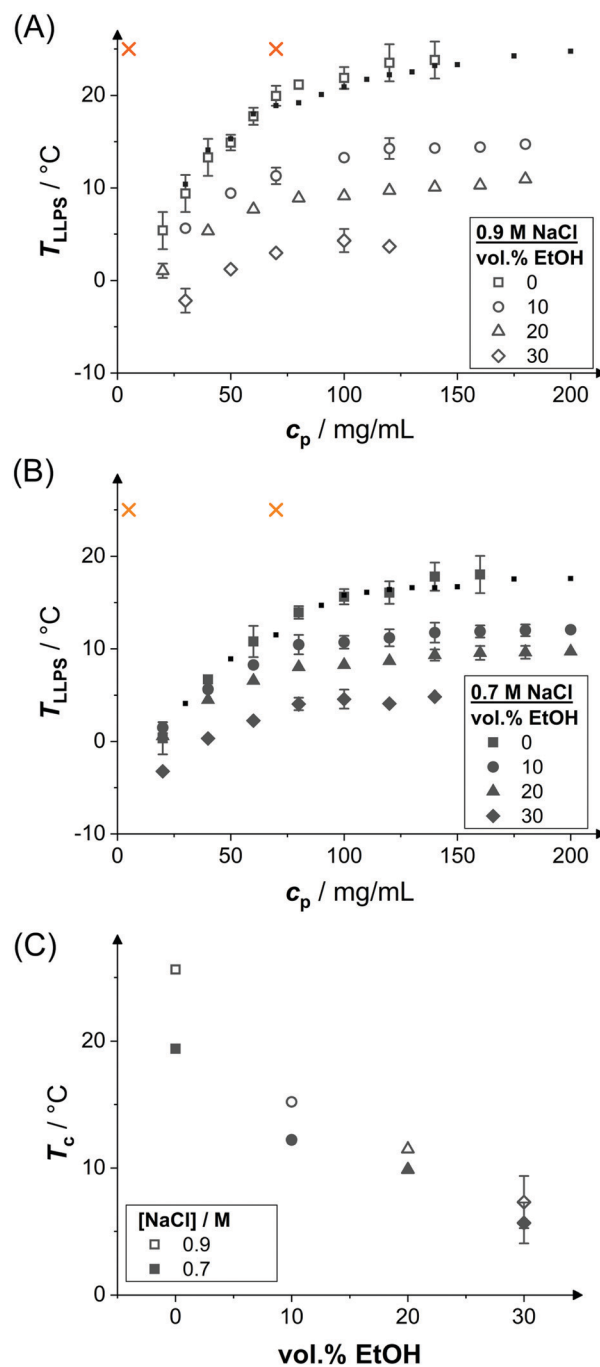


Fig. 2 Effect of ethanol on the LLPS. Cloud-point temperature T_{LLPS} as a function of protein concentration c_p representing the LLPS coexistence curves in the presence of (A) 0.9 M NaCl and (B) 0.7 M NaCl as well as various ethanol concentrations as indicated (large symbols). Literature data²⁸ in the absence of ethanol (small symbols). Typical solution conditions probed in SAXS experiments (crosses); at this temperature, b_2 is also estimated based on the cloud-points. (C) Estimated critical temperature T_c as a function of the ethanol content for the two NaCl concentrations as indicated.

reflecting an enhanced effect of inter-protein attractions. Then, T_{LLPS} saturates at high protein concentrations, indicating the proximity to the critical point.⁵³ In the latter case, critical



scalings can be used for describing the $T - c_p$ dependence:^{8,25,71,96}

$$\left| \frac{c_c - c_p}{c_c} \right| = a \left(\frac{T_c - T_{LLPS}}{T_c} \right)^\beta \quad (7)$$

with the critical temperature T_c , the critical concentration c_c , the critical exponent for binary demixing β and a fitting parameter a . By fitting eqn (7) to the data, T_c can be estimated. To minimize the number of free parameters, β is set to its renormalization group-theory value ($\beta = 0.325$) and, also in view of the limited c_p range, c_c is fixed to a previously determined value ($c_c = 270 \text{ mg mL}^{-1}$).⁵³ To avoid distortions due to the off-critical part of the binodal, cloud-points at $c_p < 70 \text{ mg mL}^{-1}$ have been excluded from the fit. The resulting T_c values are displayed in Fig. 2(C) as a function of the ethanol content for the two different NaCl concentrations. Upon addition of ethanol, T_c decreases as does T_{LLPS} in general (Fig. 2(A and B)). This indicates that ethanol reduces the net attractions between lysozyme molecules.

The attractions can be quantified by interaction parameters, such as the second virial coefficient b_2 . Based on cloud-point measurements, b_2 at a given temperature close to the binodal can be estimated by a comparison of the experimental binodal with those of short-ranged SW fluids,⁵³ as suggested by the extended law of corresponding states.⁶³ Following this approach, b_2 has been determined at the temperature indicated by crosses in Fig. 2(A and B) for the different solution compositions probed. The results will be discussed in Section 3.4.

3.3 The interactions in protein solutions close to phase separation

Pair interactions in protein solutions can be inferred from the concentration-dependence of the scattered intensity⁹⁷ or from the Q dependence of the scattering intensity through structure factor models.⁹⁸ However, close to the LLPS spinodal, critical or off-critical scattering contributions⁹⁹ are expected to occur and analytical mean-field models usually employed to analyze scattering data are expected to fail. Thus, to be able to determine the pair interaction parameters through structure factor modelling, we focus on moderately concentrated solutions at temperatures that are at least a few degrees above the expected LLPS spinodal temperatures.¹⁰⁰

Fig. 3(A) shows the normalized scattered intensity $I(Q)/Kc_pM$ of concentrated protein solutions ($c_p \approx 70 \text{ mg mL}^{-1}$ in the presence of ethanol and 50 mg mL^{-1} in the absence of ethanol) under conditions close to phase separation but far enough away from the LLPS spinodal, as indicated in Fig. 2(A and B). The experiments were performed at a fixed temperature. However, due to the different ethanol and NaCl concentrations (as indicated by the symbol type and filling, respectively) and hence different T/T_c , the distance to the LLPS boundary increases as T_c decreases with ethanol content (Fig. 2(C)) and decreases as T_c increases with NaCl concentration. In order to compare the different solution compositions with each other, all data are shown in a single graph.

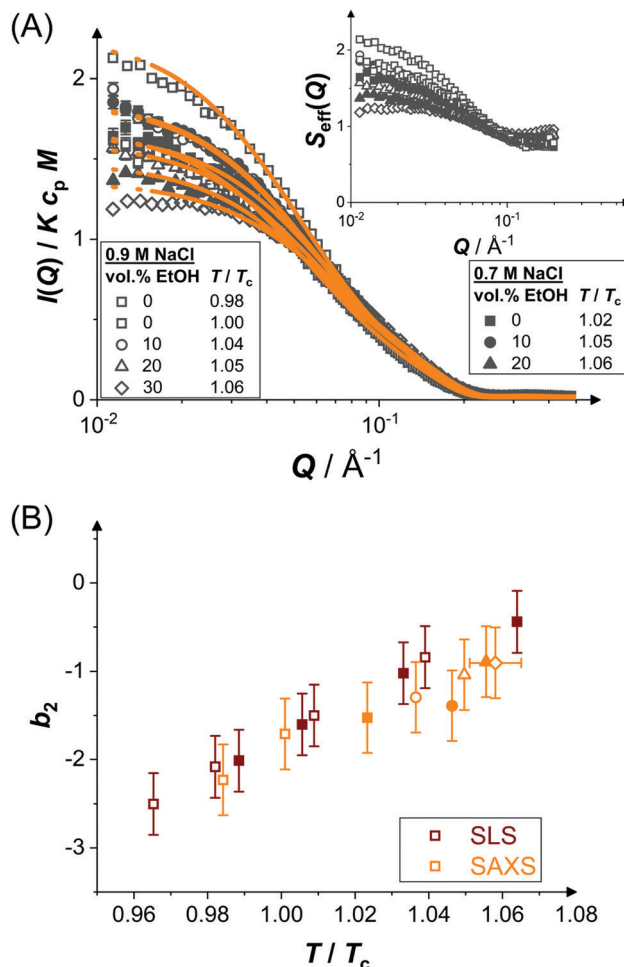


Fig. 3 (A) Scattering vector-dependent normalized scattered intensity, $I(Q)/Kc_pM$, of concentrated protein solutions ($c_p \approx 70 \text{ mg mL}^{-1}$) close to phase separation (temperature T relative to the respective critical temperature T_c , ethanol and salt content as indicated): experimental data (symbols) and model fits (lines). Inset: Effective structure factor $S_{\text{eff}}(Q)$ as inferred from the data, according to eqn (2). Only data with $Q \leq 0.2 \text{ \AA}^{-1}$ are shown, as they are very noisy beyond this value. (B) Normalized second virial coefficient b_2 as a function of temperature T normalized by the critical temperature T_c . Data based on SAXS (orange symbols) and static light scattering²⁸ (SLS, red symbols). Open and closed symbols correspond to 0.9 and 0.7 M NaCl, respectively. Ethanol content is reflected in the symbol shape as in (A).

According to eqn (2), the Q dependence of the scattering curves reflects both the form and structure factor. Since $P(Q)$ was found to be unaltered by the different solution conditions, the variations in $I(Q)$ are largely due to changes of $S(Q)$. At intermediate and high Q , the curves do not reveal marked differences. However, at low Q , the scattered intensity tends to increase as T/T_c decreases and hence the distance to the LLPS boundary also decreases. The effective structure factors $S_{\text{eff}}(Q)$ are shown as an inset. The low- Q increase with $S_{\text{eff}}(Q \rightarrow 0) > 1$ is due to enhanced inter-protein attractions upon approaching the LLPS (as well as minor changes of c_p). A qualitatively similar behavior has been observed for other protein systems.^{59,60,99}



The model of eqn (2) is fitted to the experimental data where the form factor is described by a prolate ellipsoid of revolution⁸⁰ with fixed parameters (*cf.* Section 3.1) and the analytical structure factor of adhesive hard-spheres in the Percus-Yevick approximation^{62,86} is implemented. As suggested by the ELCS, the specific shape of the interaction potential is not crucial. The experimental data are quantitatively reproduced by the model fits, in particular the low Q upturn upon approaching phase separation. For each scattering curve, the fit provides a refined value of the stickiness parameter τ , which can be converted to a normalized second virial coefficient b_2 via eqn (6). This determination of b_2 is based on an extended Q range and hence more reliable than a determination using $S(Q \rightarrow 0)$ only. The resulting b_2 values are displayed in Fig. 3(B) as a function of the reduced temperature T/T_c of the solution. The statistical uncertainty of b_2 is estimated to be ± 0.4 based on the analysis of several independently prepared samples at the same condition. In the temperature range investigated, b_2 increases monotonously with reduced temperature. The interaction parameter retrieved from fitting, τ , (and thus also b_2) as well as the quality of the fit are very similar if the form factor is modelled using the atomic coordinates implemented in a home-written programme that also takes the hydration layer into account.¹⁰¹

In addition to the b_2 data retrieved by the SAXS analysis, static light scattering (SLS) data²⁸ on the aqueous system are shown. Both data sets quantitatively agree with each other. Thus, despite the proximity to LLPS, SAXS yields reliable results for the interaction parameters. Due to the quantitative agreement with the SLS data, the SAXS data thus provide further support for a universal temperature dependence (with respect to T_c) of b_2 of protein solutions, as previously noted for lysozyme⁵³ and γ B-crystallin.⁹⁹

3.4 Ethanol effect on the second virial coefficient of lysozyme solutions: experiments and DLVO model

Upon addition of ethanol, the LLPS coexistence curve of lysozyme shifts to lower temperatures, as discussed in Section 3.2. Accordingly, for increasing ethanol content, T/T_c increases for a fixed temperature T , such as the temperature of the SAXS experiments (mainly 25 °C but also a few at 20 °C). The correspondingly reduced net attractions are reflected in the reduced low Q scattering. Hence, b_2 is expected to increase with ethanol content. To quantify this dependence, values of b_2 were determined by comparing the low-concentration branches of the binodals (Fig. 2(A and B)) with those of SW fluids and exploiting the ELCS.⁵³ The results reveal a weak, but systematic increase of b_2 with ethanol content (Fig. 4(A and B)). Moreover, the values quantitatively agree with b_2 values determined by SAXS model fits (Fig. 3 and 4(A,B)).

In order to rationalize the dependence of b_2 on ethanol and salt content, protein interactions are modelled by the DLVO potential:¹⁰²

$$U_{\text{DLVO}}(r) = U_{\text{HS}}(r) + U_{\text{SC}}(r) + U_{\text{VDW}}(r) \quad (8)$$

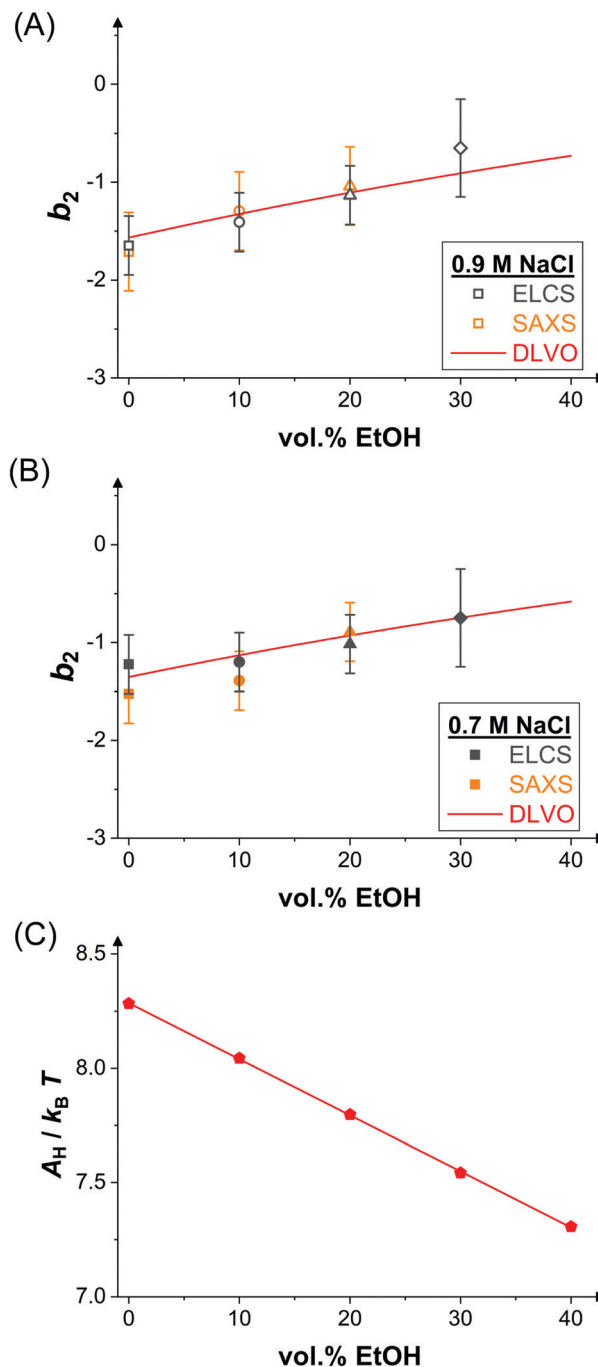


Fig. 4 Effect of ethanol on inter-protein interactions. (A) Normalized second virial coefficient b_2 as function of ethanol content at 25 °C and in the presence of 0.9 M NaCl. Data inferred from the cloud-point measurements (Fig. 2(A)) via the ELCS (grey symbols) and from the analysis of the SAXS data (Fig. 3(A)) (orange symbols) as well as calculated values based on the DLVO theory (line). (B) Data and theoretical predictions as in (A), but in the presence of 0.7 M NaCl. (C) Hamaker constant calculated based on eqn (12) (symbols) and linear fit (line).

with the hard-sphere contribution $U_{\text{HS}}(r)$, the screened Coulomb contribution $U_{\text{SC}}(r)$ and the van der Waals contribution $U_{\text{VDW}}(r)$. For $r > \sigma_p$ with particle diameter σ_p , $U_{\text{SC}}(r)$ is given by⁶⁶



$$U_{SC}(r) = \frac{(Ze)^2 \exp[-\kappa(r - \sigma_p)]}{4\pi\epsilon_0\epsilon_s (1 + \kappa\sigma_p/2)^2 r} \quad (9)$$

with the number of positive elementary charges $Z = 11.4$ at the present pH 4.5, the permittivity of the vacuum ϵ_0 and that of the solvent ϵ_s as well as the Debye screening length κ^{-1} :

$$\kappa^2 = \frac{e^2 N_A}{\epsilon_0 \epsilon_s k_B T} \sum_i z_i^2 c_i, \quad (10)$$

where N_A is Avogadro's number and z_i and c_i are the valence and molar concentration of the i -th ionic species, respectively. The van der Waals component of the potential reads⁶⁶

$$U_{VDW}(r) = -\frac{A}{12} \left(\frac{\sigma_p^2}{r^2 - \sigma_p^2} + \frac{\sigma_p^2}{r^2} + 2 \ln \left[1 - \frac{\sigma_p^2}{r^2} \right] \right) \quad (11)$$

with the Hamaker constant A , which for two identical particles in a medium can be approximated by¹⁰²

$$A = \frac{3}{4} k_B T \left(\frac{\epsilon_p - \epsilon_s}{\epsilon_p + \epsilon_s} \right)^2 + \frac{3h\nu}{16\sqrt{2}} \frac{(n_p^2 - n_s^2)^2}{(n_p^2 + n_s^2)^{3/2}} \quad (12)$$

with the permittivity of the protein ϵ_p , the refractive indices of the particle, n_p , and that of the solvent n_s , Planck's constant h , and a characteristic ultraviolet absorption frequency ν . Optical and dielectric constants are reported in the literature both for the solvents (water-ethanol mixtures)¹⁰³⁻¹⁰⁷ and the particles (proteins).^{108,109} For consistency with previous work,⁶⁷ we use $\sigma_p = 3.4$ nm, $\epsilon_p = 2$, $n_p = 1.69$ and $\nu = 3 \times 10^{15}$ s⁻¹. With these values, eqn (12) has been applied to compute the Hamaker constant as a function of the ethanol concentration. The result is shown in Fig. 4(C) as symbols. Without ethanol, $A = 8.3k_B T$ in agreement with previous studies.^{53,66,67} Upon addition of ethanol, A exhibits an apparently linear decrease (line), reflecting lowered net inter-particle attractions in water-ethanol mixtures. Similarly, a roughly linear decrease of A was observed for water-glycerol and water-dimethyl sulfoxide mixtures.^{28,64}

The normalized second virial coefficient, b_2 , can be computed based on the DLVO potential *via* eqn (1). To avoid divergence of the integral, a cut-off length δ related to the Stern layer is used as lower integration limit. Its value, $\delta \approx 0.16$ nm, has previously been adjusted to match SLS data.⁶⁴ Note that $\sigma_p + \delta \approx \sigma$; *i.e.*, the diameter of the adhesive hard sphere σ assumed in the structure factor modelling agrees with that of the hard sphere amended with a cut-off layer used in the DLVO model. This DLVO description might thus implicitly also account for non-DLVO effects, such as hydration, the hydrophobic effect and hydrogen bonding.¹¹⁰ The results of the DLVO model are shown in Fig. 4(A and B) as solid lines. The model b_2 monotonously increases with ethanol content and quantitatively agrees with the experimental data (symbols). Thus, the ethanol-dependent changes of the inter-protein interactions are fully accounted for by its effect on the dielectric solution properties and thus on the Hamaker constant and the screening length. Salt effects are contained in κ (eqn (10)).

Liu *et al.*⁴⁴ studied lysozyme pair interactions in water-ethanol mixtures at neutral pH. At three different NaCl

concentrations, an increase of b_2 at low and a plateau at moderate ethanol concentrations was observed by light scattering. To describe their data, they used a modified DLVO model. The Hamaker constant A was assumed to be constant irrespective of the ethanol content and the net charge Z was treated as an adjustable parameter in contrast to our approach (Fig. 4(C)). In addition, the DLVO potential was supplemented by an alcohol-dependent patchy SW potential and the interaction strength of the patch was allowed to vary with alcohol concentration. Compared with this more complex model, our DLVO calculation is simpler and does not require any free parameter. However, if applied to their solution conditions, our model (with $Z = 8.4$) predicts a monotonous weak increase of b_2 with ethanol content, similar to our experimental finding, and thus does not fully explain their observation. It is conceivable that the slightly different trends observed are due to differences in accounting for the peculiar physicochemical properties of water-ethanol mixtures, such as the interpretation of pH values.¹¹¹

Cosolvents can be preferentially bound to or excluded from the protein surface.¹¹² The composition of the surface layer can affect the inter-protein interactions¹¹³ and, as a consequence, the protein phase behaviour.⁷¹ Up to moderate ethanol concentrations, some preferential binding of ethanol to lysozyme has been reported,¹¹⁴ although significant excess binding was not observed in another study.¹¹⁵ This is consistent with our SAXS data (Fig. 1), which do not show a dependence on the ethanol content, and our DLVO model, which quantitatively agrees with the data without considering preferential binding. Moreover, the ELCS suggests that, as long as a system is governed by short-range attractions, the collective behaviour can be described by integral parameters, such as b_2 , whereas the details of the interaction potential are less relevant. Nevertheless, it cannot be excluded that preferential binding as well as patchiness and directionality,^{116,117} asymmetric shapes,¹¹⁸ charge patterns¹¹⁹ or other phenomena play some role. Their effects, however, are expected to be small or balance each other since our DLVO model is sufficient to quantitatively describe the data. Furthermore, also the effects of adding salt, glycerol or dimethyl sulfoxide can be rationalized by a DLVO model.^{28,64,66,67} This supports the view that at least the crucial effects are captured in a coarse-grained DLVO approach based on macroscopic solution properties despite the inherent complexity and molecular effects of inter-protein interactions.

4 Conclusion

The phase behavior and the interactions of proteins in water-ethanol mixtures were studied. The addition of moderate amounts of ethanol was found to decrease LLPS temperatures indicating reduced net attractions and, consistently, the low- Q SAXS intensity of concentrated protein solutions decreases and the b_2 values increase. The data suggest universal net interactions close to phase separation, supporting the extended law of corresponding states. The increase of b_2 with ethanol can be



quantitatively captured by a DLVO model taking into account the effect of ethanol on the dielectric solution properties. Thus, the DLVO theory can provide a mechanistic description of protein interactions also in complex solution environments.

Conflicts of interest

There are no conflicts to declare.

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