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Scouting for strong light-matter coupling signatures in Raman spectra†

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Strong coupling between vibrational transitions and a vacuum field of a cavity mode leads to the formation of vibrational polaritons. These hybrid light-matter states have been widely explored because of their potential to control chemical reactivity. However, the possibility of altering Raman scattering through the formation of vibrational polaritons has been rarely reported. Here, we present the Raman scattering properties of different molecules under vibrational strong coupling conditions. The polariton states are clearly observed in the IR transmission spectra of the coupled system for benzonitrile and methyl salicylate in liquid phase and for polyvinyl acetate in a solid polymer film. However, none of the studied systems exhibits a signature of the polariton states in the Raman spectra. For the solid polymer film, we have used cavities with different layer structures to investigate the influence of vibrational strong coupling on the Raman spectra. The only scenario where alterations of the Raman spectra are observed is for a thin Aq layer being in direct contact with the polymer film. This shows that, even though the system is in the vibrational strong coupling regime, changes in the Raman spectra do not necessarily result from the strong coupling, but are caused by the surface enhancement effects.

Introduction

Molecular vibrations (MVs) can be excited either through the absorption or the inelastic scattering of photons. The former has been used to detect vibrations associated with a change of the dipole moment, whereas the latter, which is the basis of Raman spectroscopy, has been employed to probe vibrations involving a change in polarizability. 1,2 Due to simple sample preparation, non-destructive nature and microscopy capabilities, Raman spectroscopy has become a valuable analytical tool.³⁻⁶ However, since MVs exhibit extremely small scattering crosssections, Raman scattering is a very inefficient process. As a result, Raman signals from low concentration samples are hard to detect and can, for resonance Raman, be overwhelmed by the molecular fluorescence signal.⁷⁻⁹ To circumvent this drawback, a

variety of enhancement strategies have been proposed over the years. The widely used method is surface-enhanced Raman spectroscopy (SERS) that increases Raman scattering by molecules adsorbed on, or located near metallic nanostructures or surfaces.8-11 Additionally, the fluorescence emission of the molecule is quenched due to the presence of the noble metal surface, which helps to detect the Raman scattering signal. 12 In tip-enhanced Raman spectroscopy, significant Raman signal enhancement and better resolution can be obtained by combining the sensitivity of SERS and the lateral resolution of scanning probe microscope. 13-15 The stimulating effect of vacuum fluctuations within a high-finesse microcavity (the Purcell Raman enhancement) has also been employed to improve Raman scattering from various kinds of materials, such as carbon nanotubes,16 a quantum well,17 atmospheric gases,18-21 and organic molecules.²² This approach has a potential for miniaturization, as it may be incorporated in a spectrometer. 18 Another route that has been explored to enhance Raman scattering efficiency is the strong light-matter coupling phenomenon. 23-28

Strong coupling occurs when the coherent energy exchange between molecules and a microcavity²⁹ or plasmon modes³⁰ becomes faster than any competing dissipation process. It leads to the formation of half-light/half-matter quasiparticles termed polaritons.31 So far, polariton states formed by the coupling between excitons and the cavity23-25 or surface plasmon²⁶⁻²⁸ modes have been widely investigated in terms of enhancing the Raman scattering process. In this polariton-mediated

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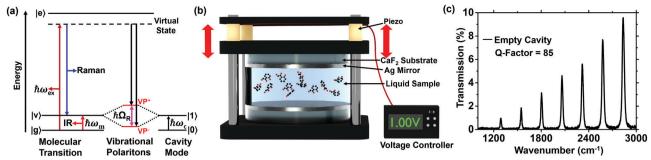


Fig. 1 (a) Simplified diagram illustrating the Raman scattering process and IR absorption of molecules under vibrational strong coupling. When the IR-vibrational frequency of the molecule (ω_m) coincides with the cavity mode (ω_c) , vibrational polaritons (VP⁺ and VP⁻) can be formed and the molecule in the virtual state may decay to either VP+ or VP- mode (black arrows). (b) Schematic illustration of the open IR-Fabry-Pérot type microcavity structure used to couple liquid phase samples. (c) Transmission spectrum of an empty microcavity with a Q-factor of 85.

enhancement mechanism, maximum intensity is observed when the Raman excitation energy becomes resonant with polariton states. 19,23 An alternative scheme proposed to increase the Raman scattering cross-section is vibrational strong coupling (VSC), 32-34 which is realized when dipole active MVs strongly couple with the vacuum electric field of a microcavity.35-43

VSC results in the formation of vibrational polaritons (VP+ and VP⁻), separated by the Rabi splitting energy ($\hbar\Omega_{\rm R}$, Fig. 1a). In 2015, Shalabney et al.35 and Long and Simpkins36 independently showed the formation of vibrational polaritons by coupling the C=O stretching modes of polyvinyl acetate and polymethyl methacrylate films with Fabry-Pérot cavity modes, respectively. Since then, VSC has been demonstrated for many systems such as neat liquids, 38,39 solutions, 40 ionic liquid crystals, 41 protein vibrational modes⁴² and multimode vibrational transitions of a polymer. 43 Experimentally, the VP and VP states can be observed in the transmission spectrum of the coupled system, as two new peaks with energies shifted from the original frequency by half the Rabi splitting.37,38 These hybrid light-matter states have attracted considerable attention because of their potential to control chemical reactivity, 44-49 vibrational energy transfer, 50 and nonlinear optical responses. 51-53 Since Raman spectra directly reflect vibrational modes of the molecule, it is only natural to expect VP and VP states to be observed in Raman spectra. Indeed, Shalabney et al.³² investigated the Raman scattering properties of vibrational polaritons obtained from a polymer film. In the experiment, the C=O IR-vibration of polyvinyl acetate (PVAc) was coupled with the optical mode of the cavity. The observed modifications in the Raman spectra were attributed to the strong coupling and to the coherent nature of the vibrational polaritonic states, which enhances the Raman cross-section.

In this work, we investigate the effects of VSC on the Raman scattering properties of three systems: two organic compounds in a liquid phase and a solid polymer film. For the liquid phase samples, benzonitrile (BN) and methyl salicylate (MS), the experiments were realized by coupling the C=O and C=N Raman vibrational mode with the vacuum cavity field of an open IR-microcavity.54 Additionally, we study the Raman scattering characteristics of a solid PVAc film under VSC. In order to obtain a complete picture of Raman VSC, we utilize different cavity geometries, which were prepared by varying the thickness and sequence of the cavity layers. Alterations in Raman spectra are observed only for cavities that support SERS effects. We did not find any signatures of VSC that would be consistent with the VSC observed in transmission spectra. Consequently, we find that it is crucial to not only consider VSC, but also other aspects, such as SERS, to understand lightmatter interaction in such systems. This observation is critical for a deeper understanding of the nature of strong light matter coupling and potential applications of Raman VSC in polaritonic chemistry to actively influence chemical reactivity.

Materials and methods

Methyl salicylate (99%), methylcyclohexane (99%), benzonitrile (99%), toluene (99%), and polyvinyl acetate (MW: 100 000) were purchased from Sigma-Aldrich and used without further purification. CaF2 windows (diameter: 25.0 mm, thickness: 5.0 mm) were purchased from Crystran LTD, while a mirror mount with a piezoelectric adjuster and a voltage controller were purchased from Thorlabs, Inc.

Open microcavity preparation^{54,55}

The Ag films, typically 10 nm thick (unless otherwise explicitly stated), were deposited on a CaF₂ substrate by a high vacuum sputter coater (Leica EM MED 020 coating system). The thickness of the metal film was controlled using a quartz microbalance film thickness monitoring system (EM QSG100) as a reference during sputtering. The microcavity was realized by bringing the Ag-coated CaF₂ windows in close proximity and by carefully controlling their parallelism with the kinematic mirror holders. Subsequently, the cavity was filled by adding a few droplets of an appropriate solution onto the edges of the CaF₂ windows using a micropipette. The solution flowed into the cavity by capillary action and remained stable between the mirrors during the entire experiment.

Polymer spaced microcavity and SERS sample preparation

Polyvinyl acetate (PVAc), 15% w/w, was dissolved in toluene and the solution was sonicated at 35 °C for 30 minutes. After cooling to room temperature, the solution was filtered using

a 0.22 µm Nylon filter. To prepare the PVAc spaced cavity, 10 nm or 30 nm Ag film (depending on the experiment) was deposited on a CaF2 window. Then the PVAc solution was spincoated (Chetmat Technology INC.) at a speed of 870 rpm for 60 s. These spinning conditions yielded a PVAc layer of approximately 5 µm thickness and ensured that one of the cavity resonances was ON resonance with the PVAc carbonyl stretch mode. Finally, an optical microcavity was realized when another 10 nm thick Ag film (or different when explicitly stated) was deposited on top of the PVAc film. The OFF resonance cavity was obtained by spin-coating the same PVAc solution at a speed of 1000 rpm for a duration of 60 s. Multiple ON and OFF resonance samples were made and the preparation procedure proved to be highly reproducible.

In order to prepare the SERS sample, a few droplets of a colloidal silver nanoparticle solution (spheres with a diameter of ~100 nm) were cast on a clean CaF2 window and left until dry. Finally, a PVAc solution was deposited on top of the SERS substrate using a micropipette and spin-coated at a speed of 870 rpm for a duration of 60 s.

Optical measurements

All transmission spectra were recorded using a Fourier transform infrared (FTIR) spectrometer (Bruker Vertex 70). The spectra were measured with a resolution of 0.5 cm⁻¹ and averaged from 50 scans. MS solutions (0.05, 0.5, 5, 15 and 25% v/v) were prepared by dissolving MS in methylcyclohexane. The transmission spectra of neat MS and neat BN were obtained by injecting the liquid between two uncoated CaF2 windows.

Prior to each vibrational strong coupling experiment, the quality of an empty cavity was verified by measuring its transmission spectrum. Then the cavity was filled with a solution and a voltage applied to the piezo element to tune the cavity mode towards the frequency of the molecular vibration under study. To measure FTIR spectra of the uncoupled, reference polymer sample, a PVAc film (5 μm thick) was spin-coated on a clean CaF₂ window. For all systems considered, the Rabi splitting, i.e., the separation between the upper and lower polaritonic peak, was determined when the cavity mode was isoenergetic with the molecular vibration of interest. Raman scattering and SERS measurements were performed using Renishaw inVia micro-Raman system. For all measurements, the laser excitation wavelength was set to 532 nm. For the MS and BN filled open microcavity, the excitation laser light was focused onto the sample surface using a long working distance Renishaw 15× objective. Raman spectra of the PVAc-spaced microcavities and the SERS sample were collected with a 50× Leica microscope objective (NA = 0.75). A movable stage was employed to move the sample and acquire 2D mapping. Data were collected in a raster scanning fashion, and the final spectra were obtained by averaging at least 140 spectra acquired from a large area of the microcavity.

Results

Fig. 1a illustrates the concept of the Raman scattering process under VSC. When a molecule is irradiated with monochromatic

light with a photon energy $\hbar\omega_{\rm exc}$, it will be transferred from the ground electronic state to an excited nonstationary virtual state. In the normal Stokes Raman scattering process, the molecule in the virtual state relaxes into the first excited vibrational state (blue arrow). However, if the first excited vibrational state is strongly coupled to the cavity mode, the molecule in the virtual state may decay to either the VP+ or VP- mode (black arrows in Fig. 1a). 32-34 In ref. 54, we have used a piezo-based tunable Fabry-Pérot type open microcavity to investigate infrared VSC of organic molecules and Fig. 1b shows the structure of the microcavity used in our experiments. The cavity consists of two CaF₂ windows coated with Ag metal film. The two mirrors were mounted into mirror holders and the optical path length (L_{op}) of the cavity was tuned by applying a voltage to the piezoelectric stacks integrated into one of the mirror mounts. An exemplary transmission spectrum of an empty IR-microcavity measured at normal incidence is shown in Fig. 1c. The long optical path length of the cavity ($L_{\rm op} \sim 20 \ \mu {\rm m}$) is reflected in a relatively small free spectral range (FSR = 260 cm⁻¹) and the multiple cavity resonances are present in the shown spectral range.⁵¹ The decrease of the cavity transmission towards lower wavenumbers is caused by the evolution of the dielectric constant of the Ag film in this spectral region.³⁸ The transmission spectra of an empty cavity as a function of the voltage applied to the piezo actuators are shown in the Fig. S1 (ESI†).

First, we studied the Raman scattering properties of benzonitrile (BN) under VSC. The C = N mode of BN is well separated from other vibrational modes and it is both IR and Raman active (blue curves in Fig. 2a and b, respectively). Vibrational polaritons were observed in the neat, liquid BN, when the $C \equiv N$ IR stretching frequency at 2229 cm⁻¹ was hybridized with one of the cavity modes (Fig. 2a, red curve). The separation between the VP⁺ and VP⁻ peaks - which, in resonant condition, is equivalent to the Rabi splitting – is found to be 50 cm⁻¹, and it is comparable to the Rabi splitting values of the $C \equiv N$ transition in BN (54 cm⁻¹)³⁸ and 4-butylbenzonitrile (46 cm⁻¹).^{56,57} The value of the Rabi splitting is much larger than the linewidth of the cavity mode (~ 22 cm⁻¹) and the molecular resonance ($\sim 12 \text{ cm}^{-1}$). This confirms that coupling between the cavity mode and the C≡N transition in BN satisfies the criterion of vibrational strong coupling.³⁸ In Fig. 2a (black curve) splitting into lower (VP-) and upper (VP⁺) vibrational polaritons were not clearly observed in the spectrum of BN filled microcavity, as the cavity resonance was strongly detuned from C=N stretching of BN. The minute dispersive line shape feature observed at about 2220 cm⁻¹ is associated with the weak highly detuned cavity-molecule interaction. This sample is considered as an OFF resonant cavity, due to the absence of the two polaritonic states in the coupled system.

The Raman spectra of BN inside the ON (red) and OFF (black) resonant microcavity are shown in Fig. 2b, together with a reference spectrum (blue curve) acquired in free space. Even though the Ag cavity mirrors decrease the intensity, new peaks due to the vibrational polaritons were not observed in the ON resonance case. Instead, the acquired Raman spectrum exhibits

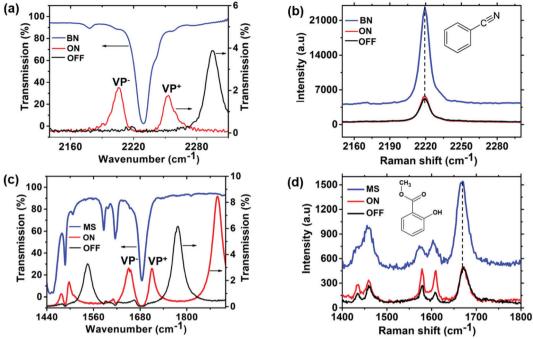


Fig. 2 (a) Transmission spectra of ON (red) and OFF (black) resonance microcavities filled with benzonitrile. The FTIR spectrum of uncoupled benzonitrile is shown in blue. (b) Raman spectra of BN obtained from the ON (red) and OFF (black) resonance cavities shown in panel (a). The Raman spectrum of BN from the reference sample is shown in blue, the inset shows the molecular structure of BN. (c) FTIR spectrum of 15% v/v MS dissolved in methylcyclohexane (blue). The red and black curves show the transmission spectrum of the solution placed inside ON and OFF resonance microcavity, respectively. (d) Raman spectrum of MS from the ON (red) and OFF (black) resonance cavities shown in panel c, the inset shows the molecular structure of MS.

a single vibrational band identical with that observed for the reference sample. This observation suggests that Raman scattering by the dominant fraction of the probed oscillators is insensitive to VSC and vibrational polariton peaks observed in the FTIR measurements cannot be probed using Raman scattering.

Fig. 2c and d show the results obtained for methyl salicylate (MS), which has richer vibrational spectrum, exhibiting several IR and Raman active vibrational peaks (blue lines). The infrared transmission spectra of the MS-filled cavity, set to be ON (red) resonance with the MS carbonyl stretch mode at 1685 cm⁻¹, are shown in Fig. 2c. When the cavity mode was tuned towards the carbonyl stretch resonance, new transitions at 1650 cm⁻¹ and 1710 cm⁻¹ could be observed in the transmission spectrum of the coupled system (red line), which has been described in detail by Takele et al.54 These are the signatures of the vibrational hybrid light-matter states (VP⁻ and VP⁺) in MS. The presence of VSC in MS is verified by the polariton anticrossing behaviour as a function of cavity tuning (see Fig. S2, ESI†). The transmission spectrum of another MS-filled cavity, in which the cavity mode was strongly detuned with respect to the C=O stretch vibration of MS is displayed in Fig. 2c (black curve). The weak dispersive line shape observed at about 1665 cm⁻¹ is caused by the weak interaction between the cavity mode at about 1780 cm⁻¹ and the C=O vibrational transition of MS. Due to the lack of the two polaritonic peaks, we consider this configuration as an OFF resonant sample.

The Raman spectrum of a reference MS sample, prepared by injecting the solution in-between two CaF2 windows without the Ag films, is depicted in Fig. 2d (blue line). The C=O vibration of MS is observed at 1670 cm⁻¹, which is in a full agreement with the value reported before. 58 Subsequently, Raman spectra were recorded from the MS-filled cavity under VSC conditions for a cavity resonance tuned to be ON or OFF resonant to C=O vibration (Fig. 2d, red and black lines, respectively). Apart from an overall decrease of the Raman signal intensity (due to lower transmission of the semitransparent cavity mirrors) no changes or formation of new spectral features can be observed for the three scenarios shown in Fig. 2d. In order to ensure that the cavity structure is not altered during the Raman experiment, the infrared transmission spectrum of the coupled system was acquired before and after the Raman measurement to confirm that the sample remains under strong coupling conditions (see Fig. S3, ESI†). Furthermore, the cavity assembly was scanned in the focal plane to verify that the measured spectra remain unchanged irrespectively of the position probed with the laser.

The experiments shown in Fig. 2 were all carried out in liquid phase and did not show any signature of Raman strong coupling. The third system investigated here is a PVAc film, which is used as a spacer between the cavity mirrors with a suitable thickness to support resonances in the IR spectral region. As depicted in Fig. 3a (black line), the PVAc layer has an intense IR peak at 1740 cm⁻¹ due to the stretching vibration of the C=O group. When the cavity transmission maximum was tuned toward the C=O transition of PVAc, the infrared transmission spectrum of the polymer loaded cavity showed two

distinct peaks at 1650 and 1803 cm⁻¹. These are lower (VP⁻) and upper (VP⁺) vibrational polaritons in PVAc (Fig. 3a, red line). The observed Rabi splitting (153 cm⁻¹) is much larger than the bandwidth of both the cavity mode (45 cm⁻¹) and the C=O vibration of PVAc (30 cm⁻¹). This confirms that the hybridized system fulfills the criterion of strong coupling, i.e., the coupling strength is larger than the bandwidths of the cavity mode and the molecular transition. 30 The green line in Fig. 3a shows the transmission spectrum of another PVAc loaded cavity, which was prepared by varying only the PVAc thickness during spin coating (for details, see Methods). This sample configuration was considered to be an OFF resonant cavity, as vibrational polariton signatures were not clearly observed. The small residual peak observed at 1707 cm⁻¹ is due to a weak interaction between the higher order cavity mode at 1940 cm⁻¹ and the C=O vibrational transition of PVAc film.

The Raman spectrum of a PVAc film on a bare CaF₂ substrate (configuration S1 in Fig. 3e) is presented by the black line in Fig. 3b and serves as reference. The Raman spectrum shown in red in Fig. 3b was acquired from an ON resonance cavity, where the mirrors are formed by two 10 nm Ag layers (MC1 in Fig. 3e). In this case, the spectral shape and intensity of the Raman spectrum is strongly altered compared to the reference spectrum of sample S1 and the largest differences

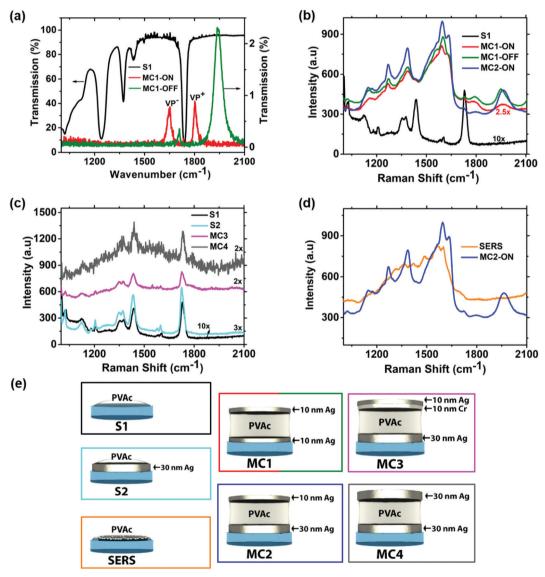


Fig. 3 (a) Infrared transmission of a reference PVAc film (S1 in panel (e)) deposited on a CaF₂ window (black line) and embedded in an optical microcavity (MC1 in panel (e)), which is ON (red line) or OFF (green line) to the C=O vibration of PVAc. (b) Corresponding Raman spectra of the configurations shown in (a). Additionally, the Raman spectrum of configuration MC2 is shown in blue. (c) Raman spectra of PVAc obtained with different sample configurations shown schematically in panel (e); for MC3 and MC4 the measurements were conducted under resonance condition. (d) Comparison of the SERS spectrum of PVA acquired using 100 nm spherical Ag nanoparticles as a substrate and the Raman spectrum obtained from configuration MC2. (e) Schematic illustration of different sample configurations; S1, S2, and SERS indicate a thin PVAc film deposited on a CaF2 window, a 30 nm Ag film, and a SERS substrate, respectively. MC1 to MC4 illustrate different PVAc spaced microcavity configurations.

can be observed in the spectral regions around 1600 cm⁻¹ and 1950 cm⁻¹. Similar spectral changes were reported by Shalabney et al. and were assigned to Raman VSC.32 Interestingly, we observed the same spectral features for an OFF resonant MC1 cavity with two 10 nm Ag layers (Fig. 3b, green spectrum), even though the infrared transmission spectrum clearly indicates the absence of strong coupling (Fig. 3a, green spectrum). The infrared transmission spectrum of the cavity configuration MC1, acquired before and after the Raman measurement, is shown in the ESI† (Fig. S4) and is not influenced by the Raman experiment. The appearance of similar spectral features for the ON and OFF resonant case indicates that they cannot be associated with the formation of polaritonic states. However, to reproduce the experimental conditions used by Shalabney et al., 32 we have replaced the bottom layer by a 30 nm thick Ag layer and kept the top layer constant at 10 nm (MC2 in Fig. 3e). The resulting Raman spectrum is presented in Fig. 3b (blue line) and the spectral shape is practically the same as already observed for MC1. This observation suggests that an increase of the bottom layer thickness has no significant impact on the overall spectral shape and the Raman spectra are strongly altered in the cavity configurations MC1 and MC2. However, the Raman spectra of the cavities MC1/MC2 are significantly more intense compared to the reference spectrum obtained from the reference sample S1, suggesting that surface enhancement effects may play a role. To verify whether surface effects have any influence on the intensity and spectral shape, we have acquired a series of Raman spectra using different sample configurations (S2, MC3, and MC4). The first configuration is a PVAc film directly spin-coated on a 30 nm Ag layer without a top mirror (S2 in Fig. 3e), which is shown in cyan in Fig. 3c. This Raman spectrum is similar to the reference spectrum of sample S1 and the spectral features observed for MC1/MC2 are not present. This suggests that a single 30 nm thick Ag layer does not induce the changes observed in Fig. 3b. The next step is to prevent direct contact between the top Ag layer and the PVAc film. This is achieved in the cavity configuration MC3 (Fig. 3e) by introducing a 10 nm thick Cr film to separate the polymer and the Ag layer. The infrared transmission spectrum (Fig. S5, ESI†) of this configuration confirms that the cavity and the C=O vibration are still strongly coupled. Interestingly, the shape of the PVAc Raman spectrum (Fig. 3c, purple) using the cavity MC3 is the same as the reference spectrum of sample S1 (Fig. 3c, black), indicating that the increased intensity and altered spectral shape in Fig. 3b is caused by direct contact between the Ag layer and the PVAc film. The last cavity configuration is MC4, where the thickness of both Ag layers is increased to 30 nm and the respective Raman spectrum is shown in Fig. 3c (grey line). Obviously, in this case, the Raman spectrum is more noisy, due to lower transmission of the cavity mirrors. Nevertheless, the main spectral features are still visible and closely resemble the reference spectrum of sample S1.

These results show that the PVAc Raman spectra of the configurations shown in Fig. 3c are identical to that of the reference sample S1 and the only ones differing from the reference are those with an unprotected 10 nm Ag layer. Evidently, a thin silver layer exhibits some degree of percolation and supports surface enhancement. The surface roughness and nanometer-scale structure of the cavity mirrors used in our study have been characterized by AFM (Fig. S6, ESI†) and show that their morphology is different, possibly leading to different SERS enhancements. However, if the spectral patterns of the MC1 and MC2 cavities indeed originate from surface enhancement effects, then acquiring Raman spectra from PVAc spin-coated on a typical SERS substrate should yield similar spectra. To this end, we acquired Raman spectra (or rather SERS spectra) of PVAc spincoated on a surface made of a layer of 100 nm Ag nanospheres (SERS in Fig. 3e). The measured PVAc SERS spectrum indeed closely resembles that of the MC1 (ON and OFF resonance) and MC2 samples – the comparison is presented in Fig. 3d.

PVAc exhibits Raman bands at 1023 cm⁻¹, 1375 cm⁻¹, 1440 cm⁻¹ and 1730 cm⁻¹, which are assigned to the CH₂ twisting, CH₃ asymmetric deformation, CH2 asymmetric deformation, and C=O stretching, respectively. 59,60 All these vibrations are clearly visible in the Raman spectrum of neat PVAc shown in Fig. 4a (black line), but none of these peaks is suitable to explain the appearance of the strong SERS peaks in Fig. 3b in the spectral region at approximately 1600 cm⁻¹. However, additional weak Raman peaks at 1580 cm⁻¹ and 1600 cm⁻¹ are present in the spectrum of the reference sample S1 (Fig. 4b, red line), which is prepared by spin coating PVAc dissolved in toluene. These peaks could be the origin of the spectral features observed in Fig. 3b and are most probably caused by residuals of toluene left in the PVA film after evaporation, since the peak positions are consistent with the Raman spectrum of liquid toluene (Fig. 4c, blue line).61,62 These peaks have been assigned to phenyl stretching modes of toluene 61-63 and can be strongly enhanced by SERS (Fig. 4d, pink line). 61 Interestingly, the SERS spectrum of toluene (Fig. 4d, pink line) and the Raman spectrum of PVAc film dissolved in toluene obtained using cavity configuration MC2 (Fig. 4e, green line) show a fair agreement between their spectral features. This suggests that

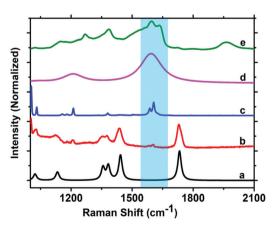


Fig. 4 Comparison of Raman spectra of PVAc and toluene: neat PVAc (black, a), PVAc film dissolved in toluene (red, b), liquid toluene (blue, c), SERS spectrum of liquid toluene (purple, d), and PVAc in MC2 cavity configuration shown in Fig. 3e (green, e). The Raman spectrum of the neat PVAc powder is from Taylor et al.,⁵⁹ whereas the SERS spectrum of liquid toluene is obtained from Qian et al.61

the strong, broad band observed at approximately 1600 cm⁻¹ for the cavities MC1/MC2 is likely caused by SERS enhancement of phenyl stretching vibrations of toluene.

Discussion and conclusions

Experimental and theoretical work where VSC has been employed to alter Raman scattering are rather scarce. To the best of our knowledge, only Shalabney et al.32 claimed enhancement of the Raman signal due to the formation of vibrational polaritons, particularly two to three orders of magnitude enhancement from the VP state. The authors explained their observation by an increase of the total Raman cross-section due to strong coupling of the C=O vibration of a PVAc polymer film with the cavity mode. On the other hand, Pino et al. 33 employed a series of complex theoretical models and showed that the total Raman cross-section is conserved during VSC, as long as ultrastrong VSC, the regime characterized by a Rabi splitting comparable to the vibrational frequency, 64 is not reached. They showed that the induced change in the ground state via ultrastrong VSC can lead to a modest enhancement of Raman scattering by less than a factor of two. Additionally, they found that the Stokes Raman and IR peaks in strongly coupled systems are located at the same energies, thus the same Rabi splitting energy should be observed in the Raman and in the infrared transmission spectra. This is in contrast to experimental results by Shalabney et al., 32 where the Rabi splitting energy obtained from the Raman data was about two times larger than the one obtained from the IR transmission spectrum. Strashko and Keeling³⁴ theoretically predicted significant enhancement of Raman scattering under ultrastrong VSC. On the other hand, it has been reported by many researchers that strong coupling of a material's electronic state with a microcavity or localized surface plasmon modes leads to modification of Raman scattering efficiency.^{23–28} For instance, Tartakovskii et al.23 showed a significant Raman signal enhancement from a microcavity containing cyanine dye J aggregates, when both the excitation energy and scattered photons are in resonance with the polaritonic states. Nagasawa et al.²⁷ demonstrated the influence of strong coupling between silver nanodimer plasmon modes and excitons of hexamethylindotricarbocyanine perchlorate molecules on the Raman scattering properties of the molecules. They obtained maximum Raman enhancement at the resonance energy between the polariton states and the Raman excitation. Minamimoto et al.28 also showed that electrochemically controlled strong coupling can be used to enhance Raman scattering spectra of molecules. In all of these and other works, 24-26 neither polaritonic signatures nor a shift in the Raman peak positions have been observed in the Raman spectra of the coupled systems.

Here, we studied the possible effects of VSC on the Raman scattering properties of molecules. For the two liquid systems of MS and BN, we find no evidence for strong coupling in the Raman spectra, even though the IR transmission spectra show

that the system is clearly strongly coupled. Additionally, the Raman spectra are the same regardless if the cavity is ON or OFF resonant to a Raman vibration. In contrast, the spectral shape and intensity of the Raman spectrum of a PVAc polymer film can be strongly altered by a microcavity. In some cases, new peaks can be observed and have been assigned to Raman VSC.³² However, these new peaks have different characteristics compared to the polaritonic peaks observed in the IR transmission spectrum. First, the full width at half maximum of the peaks in the Raman spectrum is larger compared to the VP⁺ and VP⁻ peaks in the infrared transmission spectrum. Second, the separation between these peaks is unexpectedly large, two times larger than the Rabi splitting obtained from infrared data. These different characteristics already indicate that the origin of these peaks is not Raman strong coupling, since both the peak position and FWHM should be same in the Raman and infrared spectra.33 Comparing the broad and strong peaks observed at about 1600 cm⁻¹ with literature values it is evident, that they do not emerge from the polaritonic states, but rather from the SERS enhancement of the phenyl vibrational peaks of toluene residuals. Nevertheless, coupling effects might still be present, but hidden by the strong SERS effect. However, the Raman spectrum obtained by separating the upper Ag mirror from the PVAc film by a thin Cr layer shows no observable difference compared with the reference spectrum of a pure PVAc film. This unequivocally proves that Raman scattering to the levels arising from vibrational strong coupling effect has not been detected. The hybrid molecule-cavity systems contain many uncoupled molecules, or the so-called "dark states", 65-67 which are molecular vibrations that are not interacting or interacting weakly with the cavity mode. This is mainly caused by a mismatch between the orientation of the transition dipole moment and the electric field in the cavity.⁵³ In contrast to the polaritonic states, these "dark states" are invisible in the infrared transmission measurements. However, in the Raman measurement, the entire bulk sample is probed. Consequently, the signal from the strongly coupled molecules can be overwhelmed by scattering of uncoupled molecules, making the detection of polaritonic states highly challenging. In the future, additional experimental and theoretical works should be performed in order to quantitatively disentangle coupled/ uncoupled molecules. For instance, the effect of ultrastrong vibrational coupling on Raman scattering could be investigated. In this coupling regime, the coupling rate is similar to the vibrational frequency, and it was theoretically predicted that Rabi splitting could be observed in the Raman spectra. 33,34

Conflicts of interest

There are no conflicts to declare.

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