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Constant-adiabaticity ultralow magnetic field manipulations of parahydrogen-induced polarization: application to an AA'X spin system

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The field of magnetic resonance imaging with hyperpolarized contrast agents is rapidly expanding, and parahydrogen-induced polarization (PHIP) is emerging as an inexpensive and easy-to-implement method for generating the required hyperpolarized biomolecules. Hydrogenative PHIP delivers hyperpolarized proton spin order to a substrate via chemical addition of H2 in the spin-singlet state, but it is typically necessary to transfer the proton polarization to a heteronucleus (usually ¹³C) which has a longer spin lifetime. Adiabatic ultralow magnetic field manipulations can be used to induce the polarization transfer, but this is necessarily a slow process, which is undesirable since the spins continually relax back to thermal equilibrium. Here we demonstrate two constant-adiabaticity field sweep methods, one in which the field passes through zero, and one in which the field is swept from zero, for optimal polarization transfer on a model AA'X spin system, $[1-^{13}C]$ fumarate. We introduce a method for calculating the constant-adiabaticity magnetic field sweeps, and demonstrate that they enable approximately one order of magnitude faster spin-order conversion compared to linear sweeps. The present method can thus be utilized to manipulate nonthermal order in heteronuclear spin systems.

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1 Introduction

Nuclear magnetic resonance (NMR) methods suffer from notoriously low sensitivity, which mostly limits the scope of magnetic resonance imaging (MRI) to observing water or fat molecules in the body. To overcome this limitation, hyperpolarization methods have been developed, allowing molecules to be produced with NMR signal enhancements on the order of 10⁵ to 10⁶ in a typical MRI scanner. 1-3 This enables the detection of chemical species in vivo at much lower concentrations than would otherwise be possible, and this has allowed for biochemical reactions in the body to be tracked in real time. 4-6 Fumarate is a metabolite that has been employed as a hyperpolarized biomarker; its rapid conversion to malate in vivo is indicative of cell necrosis.^{7–9}

Dissolution dynamic nuclear polarization (d-DNP) is currently the favored method to hyperpolarize biomolecules, 10,11 but this method is cumbersome and comes with high associated costs. An appealing alternative is parahydrogen induced polarization (PHIP)^{12,13} which is a chemical method renowned for its low cost

and accessibility. There are several molecules that have been hyperpolarized via PHIP and applied for in vivo studies. 14-19 The source of nonthermal spin order in PHIP experiments is the singlet order of parahydrogen²⁰ (pH₂, molecular hydrogen in the nuclear spin-singlet state). Although pH2 does not have a magnetic moment and is thus NMR-silent, upon symmetry breaking (i.e. by rendering the two protons chemically or magnetically inequivalent) the nonthermal singlet order can be converted into observable NMR signals, which are strongly enhanced compared to those under equilibrium conditions. The first step for hydrogenative PHIP is a catalytic hydrogenation reaction (addition of H₂ to a suitable substrate, usually one with an unsaturated C-C bond). When the two pH_2 -nascent protons occupy inequivalent positions in the reaction product the symmetry is broken, and NMR signal enhancements can be obtained. The magnetic interaction that induces symmetry breaking is typically a chemical shift difference, or inequivalent J-couplings to a third nucleus.

A common step in PHIP is transferring nonthermal spin order from the source spins - here the pH2-nascent protons - to target spins of choice, which are more suitable for NMR detection for various reasons (longer relaxation times, higher spectral resolution, lower background signals). A number of methods have been developed to transfer the pH2 spin order to various heteronuclei, via rf pulse methods at high field, 14,21-34 or through coherent spin mixing under zero- to ultralow-field (ZULF) NMR conditions. 35-42 In the ZULF regime, Larmor

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frequencies are small, and nuclear spins belonging to different isotopic species become "strongly coupled" - that is the difference in Larmor frequencies becomes comparable to the spin-spin couplings. Under these conditions, coherent exchange of polarization among the spins becomes possible.

A number of polarization-transfer techniques exploiting ultra-low magnetic field manipulations have been developed, for example one can:

- (1) Perform the reaction with pH_2 at ultralow magnetic field to induce spontaneous polarization transfer.⁴⁰
- (2) Perform the reaction with pH_2 at high field, nonadiabatically drop to ultralow or zero field, and adiabatically return to high field. 36-38 In this work we refer to this process as a field sweep from zero field (FS-f-Z). In previous literature this is commonly referred to as a magnetic field cycle.
- (3) Perform the reaction with pH_2 at high field, then adiabatically invert the magnetic field, passing through zero field. 41,43 In this work we refer to this process as a field sweep through zero field (FS-t-Z).

All NMR methods using adiabatic variation of the spin Hamiltonian are confronted with a common problem: adiabatic processes are by definition slow, and spin relaxation can be significant. Relaxation of hyperpolarized samples is generally detrimental as it gives rise to irreversible decay of the nonthermal spin order back to thermal equilibrium. It is therefore desirable to use the fastest possible adiabatic variation without disturbing the adiabatic nature of the process. 44-47 Solutions have been proposed such as "fast" adiabatic processes given by optimal control theory⁴⁸ or by varying the Hamiltonian $\hat{H}(t)$ such that the effective adiabaticity parameter is constant at all times.⁴⁹ The latter approach, constant-adiabaticity, is easy to implement and to adapt to specific molecular cases.

In this work we demonstrate constant-adiabaticity ultralow magnetic field manipulations to transfer proton singlet order into ¹³C magnetization in PHIP-polarized [1-¹³C]fumarate. We form hyperpolarized fumarate by chemical reaction of paraenriched hydrogen with an acetylene dicarboxylate precursor molecule⁵⁰ (see Fig. 1). The protons are initially in the singlet state, and are scalar-coupled to the ¹³C spin in the carboxylate position (we work at natural ¹³C abundance). In the case of [1-13C] furnarate, the *J*-coupling between the protons is significantly larger than the proton-carbon J-couplings; this is referred to as the "near-equivalence" regime. As a consequence, the proton singlet state is close to an eigenstate, and significant state mixing which allows for polarization transfer occurs only at well-defined magnetic fields, $\pm B_{\rm LAC}^{(i)}$, corresponding to the *i*-th level anti-crossings (LACs) of the spin system. 41 Here we specifically investigate two ZULF methods to perform polarization transfer: a field sweep from zero field, which uses a magnetic field variation from zero to B_{max} , and a field sweep through zero field, which uses a magnetic field variation from $-B_{\text{max}}$ to B_{max} . For the case of [1- 13 C]fumarate, B_{max} is a few μT , which is considerably higher than the LAC fields, $B_{LAC}^{(i)}$. For both FS-f-Z and FS-t-Z experiments we derive constant-adiabaticity magnetic field profiles, B(t), and compare the performance with linear (uniform) field variations.

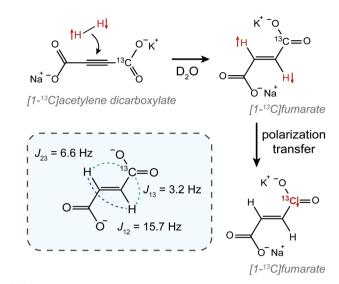


Fig. 1 The chemical reaction employed in this work to produce PHIPpolarized $[1-^{13}C]$ fumarate. In the inset the molecule is shown with the J-couplings labelled. The [1-13C] isotopomer is shown since it is the subject of this study, but all experiments were performed with material at natural ¹³C abundance.

2 Theory

Hamiltonian

The Hamiltonian of two protons, the I spins (I_1 and I_2), and a 13 C nucleus, the S spin (S_3) , in an external magnetic field B(t)(aligned along the z-axis) is written as:

$$\hat{H}(t) = \hat{H}_Z(t) + \hat{H}_I,\tag{1}$$

where

$$\hat{H}_{z}(t) = -B(t)\{\gamma_{t}(\hat{I}_{1z} + \hat{I}_{2z}) + \gamma_{s}\hat{S}_{3z}\},\tag{2}$$

$$\hat{H}_{I} = 2\pi J_{12}(\hat{\mathbf{l}}_{1} \cdot \hat{\mathbf{l}}_{2}) + 2\pi J_{13}(\hat{\mathbf{l}}_{1} \cdot \hat{\mathbf{S}}) + 2\pi J_{23}(\hat{\mathbf{l}}_{2} \cdot \hat{\mathbf{S}}), \tag{3}$$

and we set $\hbar = 1$ for simplicity. At high magnetic field, and given that $J_{12} > |J_{13} - J_{23}|$, the eigestates of the Hamiltonian (1) are approximately equal to those of the STZ (singlet-triplet-Zeeman) basis, which is defined as:

$$STZ = \{ |S^{12}\rangle, |T_{+}^{12}\rangle, |T_{0}^{12}\rangle, |T_{-}^{12}\rangle \} \otimes \{ |\alpha_{3}\rangle, |\beta_{3}\rangle \}. \tag{4}$$

The singlet and triplet states of the proton pair are defined

$$|S^{12}\rangle = (|\alpha_1\beta_2\rangle - |\beta_1\alpha_2\rangle) / \sqrt{2},$$

$$|T_{+1}^{12}\rangle = |\alpha_1\alpha_2\rangle,$$

$$|T_0^{12}\rangle = (|\alpha_1\beta_2\rangle + |\beta_1\alpha_2\rangle) / \sqrt{2},$$

$$|T_{-1}^{12}\rangle = |\beta_1\beta_2\rangle,$$
(5)

 $|\alpha\rangle$ and $|\beta\rangle$ denote the Zeeman spin states of an isolated spin-1/2 nucleus with z-projection of +1/2 and -1/2, respectively. The superscripts denoting the nucleus will be dropped henceforth. When the proton-carbon couplings are identical the **PCCP**

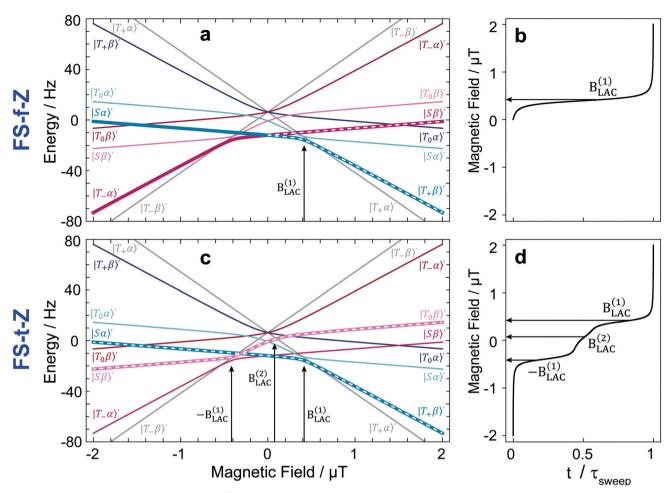


Fig. 2 Eigenvalue plots for the 3-spin system of [1-13C] furnarate with state labels shown. Top: In the eigenvalues plot in panel (a) the relevant energy levels for the field sweep from zero field (FS-f-Z) experiment are highlighted with white dashes, and the one relevant LAC is labelled. The constant-adiabaticity profile is shown in panel (b). Bottom: In the eigenvalues plot in panel (c) the relevant energy levels for the field sweep through zero field (FS-t-Z) experiment are highlighted, and the three relevant LACs are labelled. The constant-adiabaticity profile is shown in panel (d). The colours are used to distinguish between state manifolds with different angular momentum projection. The $m = \pm 3/2$ states are grey, while the m = 1/2 and m = -1/2 are in shades of blue and red, respectively. For the constant-adiabaticity profiles, only the relevant (labelled) LACs are taken into account. The LAC magnetic field values for fumarate are $\pm B_{\rm LAC}^{(1)} = \pm 0.416~\mu\text{T}$ and $\pm B_{\rm LAC}^{(2)} = \pm 0.076~\mu\text{T}$. In panes (b) and (d), t is time as a variable and $\tau_{\rm sweep}$ is the total field sweep duration

eigenbasis is given exactly by eqn (4). However, when $J_{13} \neq J_{23}$, the protons are magnetically inequivalent which mixes the states, and the eigenbasis is then denoted STZ'. This is discussed in detail elsewhere.41

By plotting the eigenvalues of STZ' as a function of magnetic field as shown in Fig. 2, it can be seen that there are a number of energy level-crossings. On close inspection, one can see that in four places the crossings are in fact avoided; the inequivalence in proton-carbon couplings acts as a small perturbation which lifts the degeneracy of the crossing states, and the level crossings are turned into LACs. The positions of the LACs have been determined previously:41

$$\pm B_{\text{LAC}}^{(1)} = \pm \frac{\pi (4J_{12} - (J_{13} + J_{23}))}{2(\gamma_{\text{I}} - \gamma_{\text{S}})},
\pm B_{\text{LAC}}^{(2)} = \pm \frac{\pi (J_{13} + J_{23})}{2(\gamma_{\text{I}} - \gamma_{\text{c}})}.$$
(6)

The value of the splittings at the centers of the LACs is:⁴¹

$$\Delta B_{\rm LAC}^{(1)} = 2\pi \left| J_{13} \cos \frac{\theta_{\rm G}}{2} - J_{23} \sin \frac{\theta_{\rm G}}{2} \right|$$

$$\Delta B_{\rm LAC}^{(2)} = 2\pi \left| J_{13} \cos \frac{\theta_{\rm G}}{2} + J_{23} \sin \frac{\theta_{\rm G}}{2} \right|$$
(7)

where $\theta_{\rm G}$ = arctan(2 $J_{12}/(J_{13}-J_{23})$) is the "Goldman angle".³⁷

At LACs, coherent spin mixing comes into play, which can be exploited in polarization-transfer experiments. For instance, adiabatic passage through a LAC gives rise to swapping of the populations of the unperturbed STZ' states (commonly termed diabatic states). The reason is that the populations follow the instantaneous eigenstates, i.e., the eigenstates of the full Hamiltonian (defined in the presence of the perturbation terms). Hereafter, by adiabatic variation of the Hamiltonian $\hat{H}(t)$ of a spin system under study we mean that its eigenstates $|\psi_i(t)\rangle$ vary with time so slowly that the state populations have sufficient time to adjust to such changes (populations "follow" the time-dependent states). The focus of this work is to optimize adiabatic passage through LACs through the use of constant-adiabaticity field profiles to minimize the passage time.

2.2 Density matrix

The nuclear spin state of pH_2 is given by the pure singlet-state wavefunction, since the two protons are magnetically equivalent. At magnetic fields far from $B_{\rm LAC}^{(1)}$ the proton singlet state is also close to an eigenstate in $[1^{-13}{\rm C}]$ fumarate. Hence, when the hydrogenation reaction takes place at a magnetic field far from $B_{\rm LAC}^{(1)}$ the singlet state remains close to an eigenstate. Note that the LACs at $\pm B_{\rm LAC}^{(2)}$ occur between the proton triplet states, so the hydrogenation could be performed at zero-field and the proton singlet population still substantially retained. The initial density matrix is approximately:

$$\rho_0 \approx \frac{1}{2} \left\{ \left| S\alpha \right\rangle' \left\langle S\alpha \right|' + \left| S\beta \right\rangle' \left\langle S\beta \right|' \right\},\tag{8}$$

where the primes indicate that the eigenstates are from the STZ' basis, not STZ. Only the two states close to singlet states of the two protons are populated; since $J_{12} \gg |J_{13} - J_{23}|$ the populations of other six spin states are negligibly small.

2.3 Constant adiabaticity profile

The general adiabaticity parameter is defined as:⁴⁹

$$\xi(t) = \sqrt{\sum_{i,j} \left| \xi_{ij} \right|^2},\tag{9}$$

where

$$\xi_{ij} = \frac{\langle i | \frac{\mathrm{d}}{\mathrm{d}t} | j \rangle}{\omega_{ii}} = \frac{\langle i | \frac{\mathrm{d}\hat{H}}{\mathrm{d}t} | j \rangle}{\omega_{ii}^2},$$

where i,j are the eigenstates of the Hamiltonian (1) and $\omega_{ij} = \omega_i - \omega_j$ is their energy difference (expressed in angular frequency units). Here the Haniltonian derivative is much easier to calculate then the eigenstate derivative. Hence, as dictated by eqn (9), for each pair of states we need to compute the parameter ξ_{ij} , which defines how fast the eigenstates change with time compared to the internal evolution frequency given by ω_{ij} . After that, we evaluate the general adiabaticity parameter ξ by averaging over ξ_{ij} defined for each pair of states. When $\xi \ll 1$, the process is adiabatic and the populations remain in the instantaneous eigenstates.

In order to determine optimized B(t) ramps, we impose the condition that the general adiabaticity parameter is equal to a constant value, $\xi(t) = \xi_0$, during the variation. Before proceeding, we introduce a few improvements for calculating constant-adiabaticity B(t) profiles.

First of all, to transfer populations between the diabatic states we use LACs, but there are also many level crossings in the system which occur between two states of degenerate energy when there are no perturbation terms to induce state mixing. Level crossings of a pair of levels occur when the Hamiltonian has a block-diagonal structure and the two states

belong to different blocks. In the case under study, the block-diagonal structure of the Hamiltonian is dictated by the fact that the z-projection of the total spin is conserved, since the commutator $[\hat{H}, \hat{I}_{1z} + \hat{I}_{2z} + \hat{S}_z]$ is zero. We exclude level crossings from consideration since, as follows from eqn (9), calculation of the $|i\rangle\xi_{ij}|j\rangle$ parameter meets certain difficulties (the numerator and denominator tend to zero). Although this uncertainty in calculating ξ_{ij} can be resolved analytically, numerical calculation of the adiabaticity parameter becomes problematic. Hence, we need to evaluate the ξ_{ij} parameters only for the states belonging to the same blocks and eqn (9) can be modified as follows:

$$\xi(t) = \sqrt{\sum_{i^{(p)},j^{(p)}} \left| \xi_{i^{(p)},j^{(p)}} \right|^2},\tag{10}$$

where $|i^{(p)}\rangle$, $|j^{(p)}\rangle$ are the eigenstates of the Hamiltonian (1) belonging to the block or subspace p. In our particular case, the index p refers to the angular momentum projection m which equals $m = \pm 3/2, \pm 1/2$.

Second, we take into account that in the case of $[1^{-13}C]$ furnarate prepared via PHIP, to a good approximation only the $|S\alpha\rangle'$ and $|S\beta\rangle'$ states are populated, which is only two states out of eight. To adiabatically manipulate the spin order, it is sufficient to consider only mixing of these states with other states belonging to the same blocks in the Hamiltonian. Specifically, the block of spin states characterized by the angular momentum projection on the field axis m=1/2 comprises three states $|T_0\alpha\rangle'$, $|S\alpha\rangle'$ and $|T_+\beta\rangle'$. If initially only the $|S\alpha\rangle'$ state is populated, spin mixing only in pairs of states $|S\alpha\rangle' \leftrightarrow |T_0\alpha\rangle'$ and $|S\alpha\rangle' \leftrightarrow |T_+\beta\rangle'$ is important. To take this into account, eqn (10) should be modified as follows:

$$\xi(t) = \sqrt{\sum_{i_0^{(p)}, j^{(p)}} \left| \xi_{i_0^{(p)}, j^{(p)}} \right|^2}, \tag{11}$$

where $|i_0^{(p)}\rangle$ are the spin states belonging to subspace p with non-zero initial population, due to the chosen method of preparing the system.

With these two considerations, we can calculate the optimized B(t) profile. The time derivative of the Hamiltonian (1) is:

$$\frac{\mathrm{d}\hat{H}}{\mathrm{d}t} = -\frac{\mathrm{d}B}{\mathrm{d}t} (\gamma_I (\hat{I}_{1z} + \hat{I}_{2z}) + \gamma_S \hat{S}_{3z}). \tag{12}$$

By substituting (12) into (11) and setting the general adiabaticity parameter to a constant value $\xi(t) = \xi_0$, we obtain:

$$\frac{\mathrm{d}B}{\mathrm{d}t} = \xi_0 / \sqrt{\sum_{i_0^{(m)},j^{(m)}} \frac{\left| \left\langle i_0^{(m)} \middle| \gamma_I \hat{I}_z + \gamma_S \hat{S}_{3z} \middle| j^{(m)} \right\rangle \right|^2}{2\omega_{i_0^{(m)},j^{(m)}}^4}},$$
(13)

here $\hat{I}_z = \hat{I}_{1z} + \hat{I}_{2z}$. The procedure used to calculate the optimized "constant-adiabaticity" B(t) ramp is described in the Materials and methods.

Polarization-transfer methods

The idea of the two methods considered here, FS-f-Z and FS-t-Z, is illustrated by the energy level diagrams shown in Fig. 2, which highlight the polarization-transfer pathways. In both experiments, the hydrogenation step is performed at +2 µT to produce $[1^{-13}C]$ furnarate with the $|S\alpha\rangle'$ and $|S\beta\rangle'$ states populated.

In the FS-f-Z experiment, the field is then rapidly (nonadiabatically) dropped to zero, which preserves the populations of $|S\alpha\rangle'$ and $|S\beta\rangle'$, and then abiabatically increased to exchange the populations of $|S\alpha\rangle'$ and $|T_+\beta\rangle'$, but leave the population of $|S\beta\rangle'$ unchanged. At the end of the process the $|T_+\beta\rangle'$ and $|S\beta\rangle'$ states are populated, and hence the ¹³C spin is hyperpolarized. In this experiment only one LAC is relevant: the LAC at $B_{LAC}^{(1)}$.

In the FS-t-Z experiment, after the hydrogenation step the field is reversed rapidly (nonadiabatically) to $-2 \mu T$ (although the hydrogenation could be done at $-2 \mu T$ and this step skipped) which preserves the populations of $|S\alpha\rangle'$ and $|S\beta\rangle'$, and then increased adiabatically through zero to +2 µT. The population in $|S\alpha\rangle'$ ends in $|T_+\beta\rangle'$, and the population in $|S\beta\rangle'$ ends in $|T_0\beta\rangle'$. At the end of the process, the $|T_+\beta\rangle'$ and $|T_0\beta\rangle'$ states are populated, and hence the ¹³C spin is hyperpolarized. In this experiment three LACs are relevant: LACs occurring at the fields $-B_{\rm LAC}^{(1)}$, $B_{\rm LAC}^{(1)}$ and $B_{\rm LAC}^{(2)}$. Note that because $-B_{\rm LAC}^{(2)}$ is not part of the adiabatic pathway, the resulting field profile is slightly asymmetric with respect the center point.

In Fig. 2, we also show the constant adiabaticity B(t) sweeps for both cases. One can see that the proposed algorithm dictates a slow increase of the field at the LACs, whereas away from the LACs field sweeping can be fast.

3 Materials and methods

The constant adiabaticity profiles were calculated using eqn (13). However, dB itself is a function of time and cannot be calculated by direct integration of the expression. Therefore, the profiles were calculated incrementally: the first point was set to an initial value (0 or $-2 \mu T$) in the considered cases) and ξ_0 was set to 1. The time increment, dt, should be small compared to 1/dB. For the considered cases $dt = 10^{-4}$ s was small enough, meaning that the obtained profiles were smooth and did not significantly change upon further decrease of dt. The derivative dB was calculated using eqn (13) for each point of the profile and is used to find the next point: $B(t + dt) = B(t) + dB(t) \times dt$. The number of points in the calculated profile depends on dt and the sweeping range, and was very large in the case of $dt = 10^{-4}$ s. To obtain a profile with a convenient number of points we performed polynomial interpolation of the calculated profile and used 1000 points to reconstruct the profile. The described procedure and all simulations were implemented using the MATLAB environment, and the code is available on GitHub (see ref. 51).

All chemicals were purchased from Sigma Aldrich. A solution of 50 mM monopotassium acetylene dicarboxylate, 100 mM sodium sulphite and 7 mM ruthenium catalyst [RuCp*(CH₃CN)₃]PF₆ in D2O was prepared by dissolving the solids by heating and

sonication. The sodium sulphite was added to increase the rate of reaction as discussed in ref. 52 and 53. The pH of the solution was adjusted to pH 10 with NaOD to further improve the rate of reaction. Oxygen was removed from the solution by bubbling nitrogen through for 5 min. 300 μL of this precursor solution was used for each experiment.

All experiments were performed at natural ¹³C abundance, but in experiments we specifically observe the [1-13C] isotopomer and generally refer to this molecule in the text.

The NMR experiments were performed in a 1.4 T ¹H-¹³C dual resonance SpinSolve NMR system (Magritek, Aachen).

Parahydrogen at >98% enrichment was generated by passing hydrogen gas (>99.999% purity) through an Advanced Research Systems (ARS, Macungie, USA) parahydrogen generator operating at 25 K.

For ultralow-field experiments, a magnetic shield (MS-1F, Twinleaf LLC, Princeton, USA) was used to provide a 10³ shielding factor from the laboratory field. Static internal magnetic fields for shimming were produced using built-in B_x , B_y , and B_z coils (on a flexible PCB), powered with computer-controlled DC calibrators (Krohn-Hite, model 523, Brockton, USA), providing three-axis field control to provide an additional order of magnitude in field reduction. The residual field in the shield was on the order of nanotesla, as verified with a fluxgate magnetometer. The timedependent applied magnetic fields were generated with a Helmholtz coil (70 mm diameter) with 10 turns on each side, wound with 0.5 mm diameter copper wire onto a 3D-printed former, with current supplied by a power amplifier (AE Techron 7224, Elkhart, USA). The magnetic-field profiles were generated using a data acquisition card (NI-9263, National Instruments, Austin, USA) with 10 µs time precision.

Low-pressure/vacuum J. Young NMR tubes held in the ZULF chamber and 1.4 T SpinSolve NMR spectrometer were connected with polytetrafluoroethylene (PTFE) tubing (1/16 in. O.D., 0.5 mm I.D.), as shown in Fig. 3. Gas and liquid flow were controlled by pneumatically actuated valves (Swagelok, Frankfurt, Germany). Sample hydrogenation was followed by shuttling into the Spin-Solve by reversing the gas flow. The sample transport was performed with nitrogen gas (any unreactive gas could be used) and took 2.5 s. In order to prevent the sample from passing through any fields that could lead to undesired state-mixing during sample transport, a penetrating solenoid was used to provide a guiding field during transit out of the magnetic shield. To avoid having bubbles in the detection region after sample transport, 100 μ L of acetone was placed in the SpinSolve tube at the start of each experiment. This mixed with the fumarate solution after shuttling, and served to reduce the surface tension and viscosity of the D₂O solvent. The experimental apparatus is shown in Fig. 3.

At the start of the experiment the sample was in the ZULF chamber in a 5 mm NMR tube, in a +2 µT (chosen as a relatively low field that is still high enough for the Hamiltonian eigenstates to be, to a good approximation, the STZ' basis states) field provided by the Helmholtz coils, and parahydrogen gas was bubbled in at 7 bar for 30 s. After a 1 s delay to allow the sample to settle, a field manipulation was applied using the Helmholtz

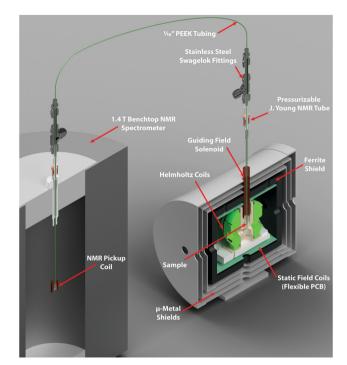


Fig. 3 The experimental apparatus used in this work.

coils. After the field sweep, the solenoid guiding field was switched on to provide a +20 µT field, and nitrogen gas at 7 bar was used to shuttle the sample into the SpinSolve NMR spectrometer. After a 1 s delay for the sample to settle, a 90 pulse was applied followed by data acquisition. A simplified event sequence is shown in Fig. 4.

After the hyperpolarization had fully relaxed, a thermal equilibrium ¹H NMR spectrum was acquired on each sample to quantify the concentration of fumarate formed. To calculate the polarization levels reported in Fig. 4(c and d), the hyperpolarized results were compared to a thermal equilibrium ¹³C NMR spectrum of an isotopically-enriched 500 mM [1-13C]fumarate standard in D2O.

4 Results and discussion

The results from experiments comparing linear and constantadiabaticity field sweeping are shown in Fig. 4, with both the FS-f-Z and FS-t-Z experiments examined. Each data point represents the signal from one experimental run. Simulations of the transfer efficiency as a function of sweep duration are shown by the lines (which ignore relaxation effects). In both cases, using the constant-adiabaticity profile allows one to achieve the maximal 13C polarization faster than when using a linear profile by approximately one order of magnitude. The faster spin-order conversion helps to minimize loss of polarization due to relaxation, although in these particular experiments the observed ¹³C polarization is similar between the constantadiabaticity and linear experiments. This is because the spin relaxation times are relatively long compared to the duration of the magnetic field manipulations, and significant polarization

loss is only observed for long sweep durations. The overall sweep times are shorter for the FS-f-Z experiment which requires passage through only one LAC. Note that the nonadiabatic field reversal at the start of the FS-t-Z experiment was used for convenience, but is not expected to have any effect on the spin dynamics; the hydrogenation could equally be performed at $B = -2 \mu T$ and the field adiabatically increased from there.

To perform the spin dynamics simulations, firstly the density matrix is projected onto the eigenbasis of the Hamiltonian (1) defined at $B = 2 \mu T$ and all off-diagonal elements (coherences) of the density matrix are removed, since they are averaged out upon continuous production of polarized molecule by the hydrogenation reaction. The resulting density matrix describes the spin system immediately following the hydrogenation step. Next, we numerically solve the Liouville-von Neumann equation with the time-dependent Hamiltonian (1), where B(t) corresponds to the magnetic field profile. Finally, we extract the expectation value of S-spin polarization from the final density matrix. Relaxation was not included in the simulations.

The experimental results are generally in good agreement with the simulations, but the ¹³C signals for the FS-t-Z experiments are notably lower than in the FS-f-Z experiments, with FS-f-Z showing \sim 15% higher transfer efficiency. This is not intrinsic to the methodology, since both methods can lead to >97\% ¹³C polarization in this molecular system. We believe the lower efficiency of the FS-t-Z is predominantly for two reasons. Firstly, in the FS-t-Z experiment, adiabatic passage through three LACs is necessary for polarization transfer, whereas for the FS-f-Z experiment only one LAC is used. Imperfections in the adiabatic passages will therefore compound, and be more detrimental in the FS-t-Z experiment. Secondly, and likely more importantly for most experimental cases, the requirement to pass through zero magnetic field for the FS-t-Z experiment can cause significant loss of polarization if there are residual magnetic fields along other axes. This introduces additional undesirable LACs which can lead to the populations being diverted from the desired transfer path. In Fig. 5 we show how the final 13C polarization for both FS-f-Z and FS-t-Z experiments with the sweep in the z-axis depends on the presence of a transverse field in the x/y-plane. We now use B_z to indicate a B field applied along the z-axis.

Despite shorter sweeping times when using a constantadiabaticity profile, these methods are more sensitive to magnetic field offset in the field sweep axis (z) than the linear profiles. This is because the constant-adiabaticity profiles are designed around the knowledge of LAC fields, and if there is a magnetic field offset or inhomogeneity across the sample, the slow part of the constantadiabaticity field ramp will not match the LAC field. The dependence of the constant-adiabaticity FS-f-Z and FS-t-Z conversion efficiencies on magnetic field offset is shown in Fig. 6. A Bz offset on the order of 100 nT is sufficient to reduce the transfer efficiency by >10%. The case is worse for the FS-t-Z experiment, which requires three LACs, compared to just one for the FS-f-Z experiment. We expect this situation can be improved by designing pseudo-constant-adiabaticity profiles to be close to constantadiabaticity, but made to be more robust with respect to B_2 field offset/inhomogeneity by broadening the LAC field condition.

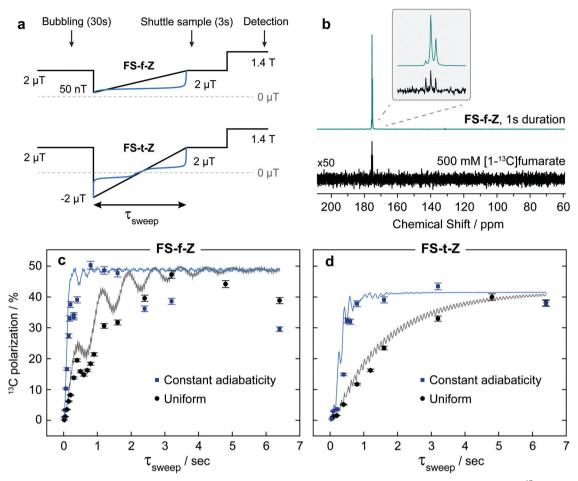


Fig. 4 (a) Experimental protocol for the datasets shown in panes (c and d). (b) A comparison between one of the hyperpolarized ¹³C NMR spectra, and a thermal equilibrium 13 C NMR spectrum acquired on a 500 mM sample of isotopically-enriched [1- 13 C]fumarate in D₂O. Both spectra were acquired at a field strength of 1.4 T with a single transient, and from this comparison it was possible to extract the polarizations shown for the results below. The asymmetry in the triplet structure in the hyperpolarized spectrum is due to the nonthermal proton spin polarization. (c and d) Results from the field sweep experiments, contrasting constant-adiabaticity and linear magnetic field profiles for field sweep from zero field (FS-f-Z) and field sweep through zero field (FS-t-Z) experiments. The error bars on the data points show one standard deviation, determined by repeating one experiment many times and measuring the standard deviation. Simulations are shown by the lines fitted to the data. A description of how the simulations were performed is given in the text. In theory and in simulations, both methods can lead to >97% 13 C polarization. The lower efficiency of the field sweep experiment is discussed in the text.

In these experiments the FS-f-Z experiment performs better than the FS-t-Z. However, there are certainly experimental cases in which the FS-t-Z might be preferred. One example is in a system in which the rapid (nonadiabatic) initial field drop of the FS-f-Z is inconvenient or not possible, such as when instead of varying the magnetic field applied to a static liquid, a static magnetic field spatial profile is constructed and the liquid flows through to achieve the desired polarization transfer. Another example of when the FS-t-Z experiment may be preferred is for molecular systems outside the near-equivalence regime (i.e. when $|J_{12}| < |\delta J|$, in our case J_{12} = 15.7 Hz and δJ = 3.4 Hz). In these cases, the proton singlet state is no longer close to an eigenstate at zero field, and the nonadiabatic field switch at the start of the FS-f-Z experiment can cause the population differences to be converted into coherences which rapidly dephase. This can be avoided by using the FSt-Z protocol which does not require nonadiabatic field changes.

For this work [1-13C]fumarate was chosen as a model system because it is a 3-spin system in the near-equivalence regime $(J_{12} \gg |J_{13} - J_{23}|)$. This is the relevant regime for many PHIPpolarized molecules for which this inequality is similar or even more pronounced, with some examples being ethyl propionate,³⁸ tetrafluoropropyl propionate,¹⁶ and allyl pyruvate.⁵⁴ The greater this inequality, the greater the difference in time required for a linear sweep profile over its constant adiabaticity analog. On the other hand, [1-13C]fumarate is not an ideal molecule for the demonstration since the proton singlet lifetime and the 13 C T_1 are both relatively long, 52 meaning there is little difference in the 13C polarization that can be reached whether using a constant adiabaticity or a linear sweep. This would certainly not be the result for molecules with more rapidly relaxing hyperpolarized spins, which is often the case when additional protons are present in the molecules.

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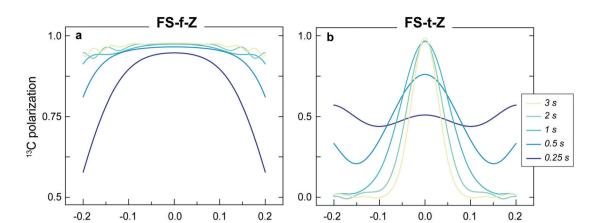


Fig. 5 The 13 C polarization generated by applying (a) a constant-adiabaticity field sweep from zero field (FS-f-Z), or (b) a constant-adiabaticity field sweep through zero field (FS-t-Z), to $[1^{-13}\text{C}]$ fumarate for different static transverse (i.e. in the x/y-plane) magnetic field strengths. In the simulated FS-f-Z B_z is swept from 50 nT to 2 μ T and in the simulated FS-t-Z B_z is swept from -2 to +2 μ T. The FS-f-Z is less sensitive to static transverse fields since the level anti-crossings introduced by the transverse field are centered at $B_z = 0$. Simulations were performed for five field sweep durations.

Transverse field / uT

Transverse field / µT

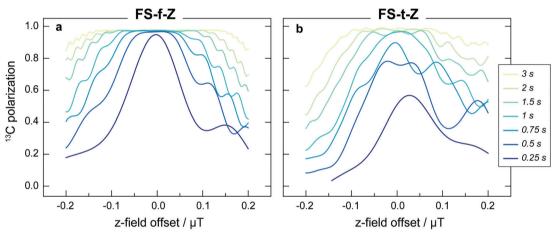


Fig. 6 The 13 C polarization generated by applying (a) a constant-adiabaticity field sweep from zero field (FS-f-Z), or (b) a constant-adiabaticity field sweep through zero field (FS-t-Z), to [1- 13 C]fumarate, as a function of B_z magnetic field offset. In the simulated FS-f-Z B_z is swept from 50 nT to 2 μ T and in the simulated FS-t-Z B_z is swept from -2 to +2 μ T. Simulations were performed for seven field sweep durations, and the lines are labelled correspondingly.

5 Conclusions

In this work we revisited the concept of using adiabatic variation of the spin Hamiltonian for manipulating nonthermal spin order. By exploiting the constraint of "constant adiabaticity" we are able to increase the rate of spin-order transformations in nuclear spin systems. In addition to the previously developed algorithm, here we propose a modification of the method, allowing one to limit the number of adiabatic levels to only those relevant for the desired spin-order transfer. The theoretical approaches discussed here are of a general scope, and they can be applied to a variety of NMR (and non-NMR) experiments. We illustrate the performance of constant-adiabaticity optimization on the specific example of polarization transfer from parahydrogenderived proton singlet order to a heteronuclear magnetization in an AA'X spin system in ZULF conditions. In such experiments the

external magnetic field is adiabatically varied in the μ T range; specifically, either the field is adiabatically increased from zero (FS-f-Z) or adiabatically inverted, passing through zero field (FS-t-Z). We demonstrate the methods on the molecule [1-¹³C]fumarate, and show that constant-adiabaticity B(t) ramps provide faster spin-order transfer than linear ramps, which is important when detrimental relaxation effects are considered. We expect that variation of the Hamiltonian using the constraint of constant adiabaticity will become a useful tool in NMR in general, and in ZULF NMR in particular.

Conflicts of interest

There are no conflicts to declare.

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