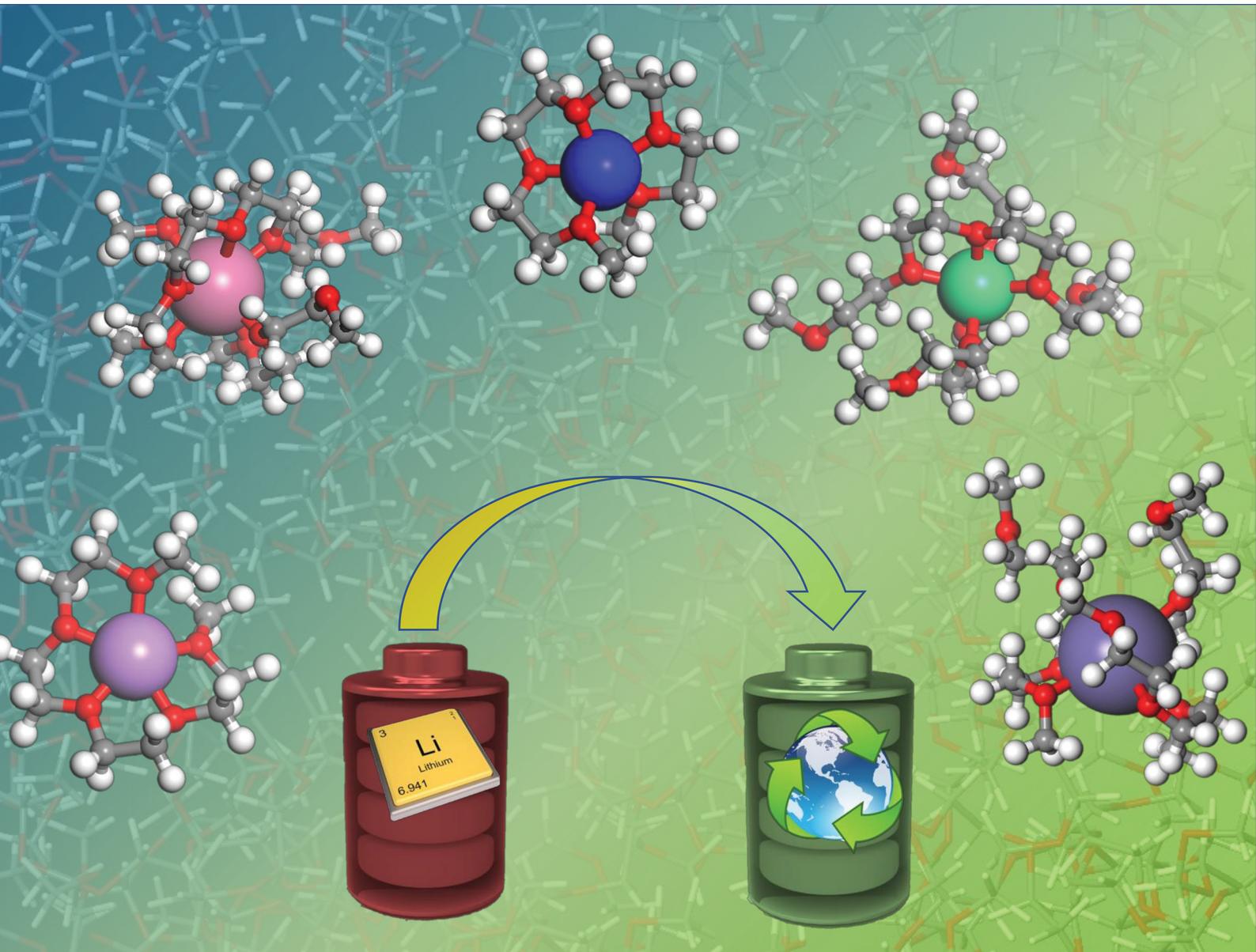


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## Investigation of alkali and alkaline earth solvation structures in tetraglyme solvent†

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This study compares molecular calculations performed with molecular and periodic codes through an investigation of the solvation structures of alkali and alkaline earth metal ions in tetraglyme solution. The two codes are able to produce equivalent structural and energetic information at the same level of theory, and in the presence of the implicit solvation model or not. This comparison reveals that molecular optimisations can be performed with periodic codes and used directly as input models for interface or electrochemistry calculations in order to preserve the solvent–solute interaction and the cavitation energy. By a rigorous comparison, we have demonstrated that equivalent energetic values can be obtained with the conventional PBE-D3 and the newly developed SCAN-rVV10 functionals. Nevertheless, as far as the vibrational features are concerned and when the molecule possesses a highly conjugated system, the SCAN-rVV10 functional is required to describe the vibrational modes properly. The computed IR/Raman spectra can thus be used as essential information to determine the first solvation shell of metal ions in glyme-based solutions. In tetraglyme solution, the alkali and alkaline earth metal ions exhibit a diverse solvation structure. Small ions like  $\text{Li}^+$  and  $\text{Mg}^{2+}$  tend to adopt a coordination number of five or six, while larger ions,  $\text{Na}^+$ ,  $\text{K}^+$ , and  $\text{Ca}^{2+}$ , prefer an eight-coordinated environment, and the metal–ligand interaction increases in the order  $\text{K}^+–\text{O} < \text{Na}^+–\text{O} < \text{Li}^+–\text{O} < \text{Ca}^{2+}–\text{O} < \text{Mg}^{2+}–\text{O}$ . The solvation spheres play a significant role in the stability and the reactivity of the solvated ions, and can thus be used as input models to construct the solvation structure in more sophisticated electrolytes, such as polyethylene oxide, or perform electrochemical calculations.

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## Introduction

Rechargeable lithium-ion batteries (LIBs) have long been the dominant energy storage system for portable devices due to their high operating voltage and high energy density value.<sup>1</sup> Nonetheless, the unequal distribution of Li resources in the Earth's crust and their increasing price have evoked the development of alternative systems, such as sodium-ion (SIBs),<sup>2–5</sup> potassium-ion (KIBs),<sup>6</sup> and multivalent ion batteries.<sup>7,8</sup> Among the multivalent ion technologies, magnesium-ion, and calcium-ion batteries are the most promising, thanks to the abundance of Mg and Ca resources, the low potential of the  $\text{Mg}^{2+}/\text{Mg}$  and  $\text{Ca}^{2+}/\text{Ca}$  redox pairs, and the high theoretical capacity associated with the exchange of two electrons. Even though practical uses of these multivalent ion technologies are still far from

reality due to the sluggish kinetics of  $\text{Mg}^{2+}$  and  $\text{Ca}^{2+}$  in solid phases and the lack of appropriate electrolytes, on-going research in these areas has led to significant discoveries in the field of chemistry and materials science.<sup>6,8</sup>

An essential component of all rechargeable batteries is the electrolyte, which acts as an electronic insulator between the two electrodes but still allows the ionic diffusion process to occur. Most rechargeable LIBs and SIBs employ liquid electrolytes consisting of Li- or Na-containing salts dissolved in a mixture of organic solvents, but polymer and solid-state electrolytes also exist.<sup>9–11</sup> There has been no report on the existence of an optimal electrolyte for multivalent ion batteries.<sup>12</sup> However, most on-going research shows great interest in organic carbonates and the glyme family.<sup>13,14</sup> The glyme family has the general chemical formula of  $\text{H}_3\text{CO}(\text{CH}_2\text{CH}_2\text{O})_n\text{CH}_3$ , with the main representatives being dimethoxylethane (DME) or monoglyme (G1), diglyme (G2), triglyme (G3), or tetraglyme (G4) when  $n = 1, 2, 3$ , or 4, respectively. These glyme molecules can be seen as oligomers and prototypes of a more complicated solid electrolyte, known as polyethylene oxide (PEO), which is becoming more and more popular in the scope of all-solid-state batteries. The glyme family exhibits great advantages in practical

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applications due to their high boiling point and high stability over a wide electrochemical window.<sup>15–19</sup>

Despite the great importance of glyme-based electrolytes in the field of batteries, little information can be found on the solvation structure of alkali and alkaline earth metal ions. The stability and reactivity of solvated metal ions strongly depend on the structure of the first coordination sphere, which cannot be ignored in theoretical models. Some attempts have been made to elucidate the solvation structures of these alkali and alkaline earth ions in glyme-based solvents. Among them, Saito *et al.* proposed a  $\text{Li}^+$  solvation structure in G4 solution determined by neutron total scattering. Fujii's group reported a thorough investigation of the solvation structures of  $\text{Mg}^{2+}$  in G2 and G3 solutions by combining infrared (IR)/Raman spectroscopy with Density Functional Theory (DFT) calculations. Nonetheless, all the structures proposed in these studies were modelled in the isolated gas phase, which completely ignores the solvent effect on the stability and the local structure of the solvated ions.<sup>20–22</sup> While progress has been achieved by employing an implicit solvent model in the calculation in conjunction with the explicit solvent or electrolyte molecules,<sup>23–26</sup> these studies are still performed at the molecular level, which assumes infinitely dilute solutions. In batteries, liquid electrolytes contain ions at considerable concentrations, and thus short- and long-range electrostatic interactions between the solvated species may be important. These interactions might lead to a significant deviation in the calculated and observed properties, especially in the energetic values. The ion–ion interaction energy that occurs in real solutions can be calculated from Debye–Hückel or extended theories and then added to energetic values obtained from molecular codes as a data post-processing treatment. Nonetheless, the reliability of these models stands only for high dielectric constants where long-range electrostatic interactions do not contribute extensively to the system energetics, which is not the case of glyme-based solutions. In the case of low dielectric constant electrolytes, a concentration-dependent computational model is required, which can be realised through the use of periodic calculations. To that end, a validation step is needed to ensure that both molecular and periodic codes can produce equivalent structural and energetic information under infinite dilution conditions.

This study aims at systematically comparing the structures and the physicochemical properties obtained from molecular modelling performed with the Q-Chem code and periodic modelling performed with the Vienna Ab initio Simulation Package (VASP) code through an investigation of the solvation structure of some important alkali and alkaline earth ions  $\text{M}^{n+}$  ( $\text{M} = \text{Li, Na, K, Mg, or Ca}$ ) in tetraglyme solutions. The Q-Chem code is chosen for this study as it offers many functionals that are equivalent to those available in the VASP code. The obtained results reveal that equivalent geometric and energetic information can be extracted from the molecular modelling performed in the two codes. As expected, van der Waals interactions have a significant contribution in these systems, and should be included in all calculations. Furthermore, we demonstrate the possibility of combining theoretical DFT calculations with experimental IR spectroscopy to determine ion solvation structures

in glyme-based solutions. Furthermore, our analysis shows that solvation energies can be decomposed into competing O–cation bonding and organic skeleton strain energies that present strong evolutions with the cation charge and size.  $\text{Li}^+$  in G4 has a coordination number of five, which is imposed by the tiny size of  $\text{Li}^+$  and the geometry constraint of the G4 ring.  $\text{Mg}^{2+}$  tends to reside in an octahedral site, while  $\text{Na}^+$ ,  $\text{K}^+$ , and  $\text{Ca}^{2+}$  prefer a coordination number of eight. The solvation structures in G4 represent those that can exist in more sophisticated glymes, and they can thus be used as starting models to construct the solvation sphere in polyethylene oxide.

## Results and discussion

### Validity of the calculation approach

The two computational codes, Q-Chem and VASP, employ many common exchange–correlation functionals, such as the Perdew–Burke–Ernzerhof (PBE) functional, hybrid functional PBE0, and the Strongly Constrained and Appropriately Normed (SCAN) semi-local density functional; nevertheless, Q-Chem utilises Gaussian-type orbitals while VASP uses plane waves as basis sets. In order to verify whether the difference in the choice of basis set may lead to a substantial discrepancy in the structural and energetic values we first compare the enthalpies of the reaction  $[\text{M}(\text{G4})]^{n+} + \text{G4} \rightarrow [\text{M}(\text{G4})_2]^{n+}$  ( $\text{M} = \text{Na, K, Mg, and Ca}$ ) calculated with the same functionals, *e.g.* PBE, PBE-D3, SCAN, and SCAN-rVV10. The calculations were performed in the isolated gas phase and in the presence of the implicit solvent model. Detailed information on the structure of  $[\text{M}(\text{G4})]^{n+}$  and  $[\text{M}(\text{G4})_2]^{n+}$  is discussed in the following parts. The obtained results show that the two computational codes produce similar structural and energetic information at the same level of theory, irrespective of the solvent conditions (Tables S1–S5, ESI<sup>†</sup>). The van der Waals interaction contributes significantly to the system energy with the dispersion corrected GGA (PBE-D3) or meta-GGA (SCAN-rVV10) functionals leading to similar solvation spheres. These results validate the performance of the periodic VASP code and its implicit solvent model to reproduce both the geometry and the energy of glyme-based solvation spheres, which can therefore be used as inputs in more complex calculations with a full transferability.

Apart from the energetics of the solvation energy, it is important to check how PBE-D3 and SCAN-rVV10 perform in terms of the vibrational properties, not only for the cations but also for the anions. At this stage, a direct comparison between the theoretical and experimental vibrational spectra of a cation solvated in G4 cannot give any clear conclusion, as the vibrations of G4 molecules in the free and in the complex states might overlap. Furthermore, one does not know whether the PBE-D3 and SCAN-rVV10 functionals can accurately reproduce the vibrational spectra or not. In order to facilitate the discussion, one should choose references whose vibrational spectra are well elucidated and are not interfered with by the solvent's vibrations. Among others,  $\text{TFSI}^-$  salts of alkali and alkaline earth metal ions are widely used in electrolytes for rechargeable batteries. When completely dissolved in G4,  $\text{TFSI}^-$  salts release



a considerable amount of solvated cations and free  $\text{TFSI}^-$  anions. In solutions,  $\text{TFSI}^-$  is experimentally found in the form of *cis*- and *trans*-isomers and these configurations are determined by the relative positions of the two  $-\text{CF}_3$  groups with respect to the S-N-S plane. The *trans*- $\text{TFSI}^-$  gives rise to a characteristic deformation mode  $\text{SO}_2$  at  $618\text{ cm}^{-1}$ , whereas the  $\text{SO}_2$  groups in *cis*- $\text{TFSI}^-$  have two characteristic vibrations at  $600$  and  $650\text{ cm}^{-1}$ .<sup>27</sup> These vibrations lie in the G4-transparent regions and have been the subject of several studies.<sup>27-29</sup> Modelling the  $\text{TFSI}^-$  anion within the DFT framework is not straightforward as it involves highly ionic C-F bonds and a strong conjugation through S=O bonds that can be difficult to capture by standard functionals. This anion is thus an excellent test case. The IR spectra of *cis*- and *trans*- $\text{TFSI}^-$  computed at the PBE-D3 level fail badly to reproduce the IR-active vibrations experimentally observed in the  $600$ – $675\text{ cm}^{-1}$  range (Fig. 1a). All the computed  $\text{SO}_2$  deformation modes are down shifted by  $40$ – $50\text{ cm}^{-1}$  compared to the experimental data recorded for a  $0.5\text{ M}$   $\text{Ca}(\text{TFSI})_2$ /G4 solution (Fig. 1a). On the other hand, the IR spectra computed with the SCAN-rVV10 functional match almost perfectly with the experimental data, with no need to apply any scaling factor (Fig. 1b).

The structures of the *cis*- and *trans*- $\text{TFSI}^-$  anions optimised with the PBE-D3 and SCAN-rVV10 functionals are mostly identical (Table S6, ESI<sup>†</sup>), showing that the molecular geometry is not the origin of the better description of the IR spectra with the SCAN-rVV10 functional. A charge density difference map is computed for the *trans*- $\text{TFSI}^-$ , based on the electron densities obtained with the SCAN-rVV10 and PBE-D3 functionals (Fig. 1c). It reveals that the SCAN-rVV10 functional enhances the charge transfer on the S=O and C-F bonds, which increases the bonds' ionicity and therefore the force constant. Consequently, the vibrational frequencies of S=O bonds, calculated with the SCAN-rVV10 functional, are shifted to higher wavenumbers, leading to a better agreement between the theoretical and experimental values.

In addition to those of  $\text{TFSI}^-$ , the IR spectra of  $[\text{Ca}(\text{G4})]^{2+}$  computed using the PBE-D3 and SCAN-rVV10 functionals are also compared (Fig. S1a, ESI<sup>†</sup>). The two spectra show slight differences in the relative intensity of some vibrations in the  $750$ – $1200\text{ cm}^{-1}$  range due to the difference in the functionals. Importantly, the wavenumbers computed using the PBE-D3 functional are underestimated by  $30$ – $40\text{ cm}^{-1}$  compared to SCAN-rVV10. The charge density difference map reveals that the SCAN-rVV10 functional increases the charge localisation on the O atom and on the C-C bonds while reducing the hyperconjugation contribution of the C-H bonds (Fig. S1b, ESI<sup>†</sup>). Like  $\text{TFSI}^-$ , the SCAN-rVV10 functional gives a better description of the nature of the chemical bonds in the solvated cations, and thus the chemical bonds' vibrational modes. The discrepancy in the wavenumber of the vibrations computed using the PBE-D3 and SCAN-rVV10 functionals seems to be more important in  $\text{TFSI}^-$  than in  $[\text{Ca}(\text{G4})]^{2+}$ , e.g.  $50$ – $70\text{ cm}^{-1}$  discrepancy vs.  $30$ – $40\text{ cm}^{-1}$ . This points out the tendency of the PBE-D3 functional to overdelocalise the electrons of the  $\text{TFSI}^-$  conjugated system, hence reducing the bond strength and the vibrations' wavenumber; this overestimation is weaker in  $[\text{Ca}(\text{G4})]^{2+}$ , in which the electrons are much more localised than in  $\text{TFSI}^-$ .

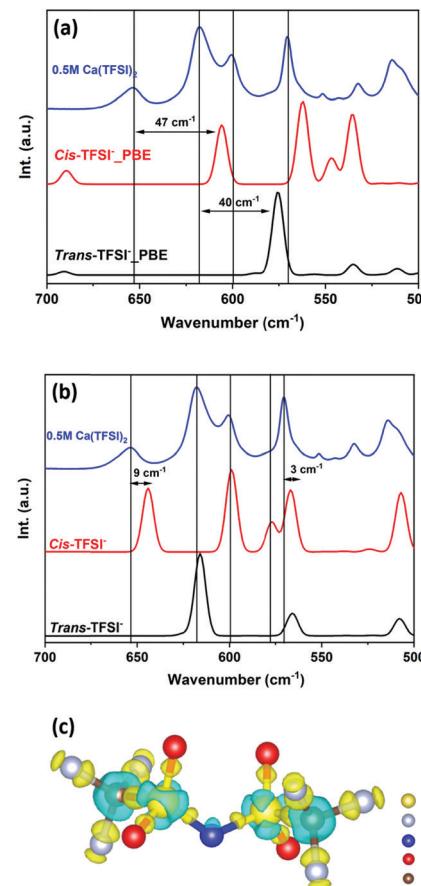


Fig. 1 IR spectra of *cis*- and *trans*- $\text{TFSI}^-$  computed using the (a) PBE-D3 and (b) SCAN-rVV10 functional in the VASP code with the presence of the implicit solvent model, compared to the experimental data recorded for a  $0.5\text{ M}$   $\text{Ca}(\text{TFSI})_2$ /G4 solution. Vertical lines are added for eye guidance. (c) Charge density difference at an iso-surface density of  $3.5 \times 10^{-3}$  electrons  $\text{\AA}^{-3}$  of *trans*- $\text{TFSI}^-$  calculated with the SCAN-rVV10 and PBE-D3 functionals in the VASP code with the presence of the implicit solvent model. The yellow and blue colours indicate the areas where the electron density is enhanced or depleted for the SCAN-rVV10 functional.

These comparisons show that, even though the PBE-D3 and SCAN-rVV10 functionals produce similar structural and energetic information, the SCAN-rVV10 functional is required to accurately describe the material's vibrational structure and the topology of its potential energy surface. In the following sections, all the structural, energetic, and vibrational properties of the solvated ions will be considered, especially for  $\text{Ca}^{2+}$ . Thus, only the results obtained from the SCAN-rVV10 functional in the VASP code will be given unless otherwise specified.

### $\text{Li}^+$ solvation structure

By using neutron total scattering, Saito *et al.* reported that  $\text{Li}^+$  in G4 solution is surrounded by five oxygens of a G4 molecule at  $\text{Li}-\text{O}$  distances of  $1.93$ ,  $2.06$ ,  $2.09$ ,  $2.13$ , and  $2.24\text{ \AA}$ . Nonetheless, the authors claimed that the  $\text{Li}^+$  site should be described as deficient five-coordination. The oxygen atom at  $2.24\text{ \AA}$  was not counted as a coordinating ligand since this distance was slightly greater than the sum of the Shannon radii of  $\text{Li}^+$  and

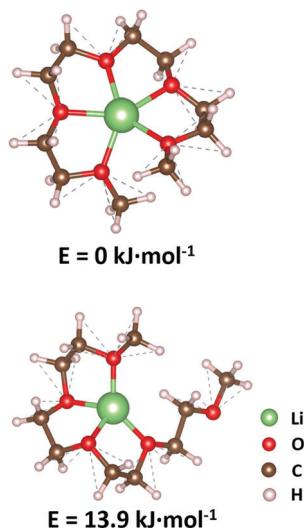


Fig. 2 Optimised structures and the relative energy of the pentadentate and tetradentate  $[\text{Li}(\text{G}4)]^+$  calculated with the SCAN-rVV10 functional.

$\text{O}^{2-}$ . The proposed structure was then modelled using an isolated  $[\text{Li}(\text{G}4)]^+$  in the gas phase at the MP2/6-311G(d,p)//HF/6-31G(d) level of theory.<sup>30</sup> Nevertheless, it is important to note that the Shannon radii were established from the solid-state database and the ionic radius for a certain ion varies with its coordination: a  $\text{Li}^+$  residing in an octahedral site has a larger ionic size than one in a tetrahedral site (0.76 Å vs. 0.59 Å). The Shannon radius of  $\text{Li}^+$  in a coordination of five is not tabulated, and it is not justifiable to exclude the oxygen at 2.24 Å from the  $\text{Li}^+$  solvation sphere by using the  $\text{Li}^+$  radius in a tetrahedral site. A  $[\text{Li}(\text{G}4)]^+$  structural optimisation performed using the SCAN-rVV10 functional in the presence of the implicit solvent model converges to a five-coordinated environment with corresponding Li–O distances of 2.08, 2.12 ( $\times 2$ ), 2.14, and 2.18 Å. An alternate model, with the fifth oxygen of the G4 molecule pointing away from  $\text{Li}^+$ , is less stable than the five-coordinated structure by 13.9 kJ mol<sup>-1</sup> (Fig. 2). This comparison shows that all the five oxygens of a G4 molecule coordinate to the  $\text{Li}^+$  in  $[\text{Li}(\text{G}4)]^+$ , which is in agreement with the theoretical study of Tsuzuki *et al.*, showing that pentadentate  $[\text{Li}(\text{G}4)]^+$  is more stable than the tetradentate one.<sup>31</sup> The reason for this behaviour is that the tetrahedral site formed by four oxygens of the G4 molecule is greatly distorted (*vide infra*), which leaves plenty of room for a supplementary bond.

### Mg<sup>2+</sup> solvation structure

The solvation structure of Mg<sup>2+</sup> in dilute G4 solution has not been reported to the best of our knowledge. Even though the solvation structure of Mg<sup>2+</sup> in G4 is unknown, it has been reported that Mg<sup>2+</sup> adopted distorted octahedral coordination and existed as  $[\text{Mg}(\text{G}2)_2]^{2+}$  and  $[\text{Mg}(\text{G}3)_2]^{2+}$  in G2 and G3 solutions, respectively.<sup>20,21</sup> By combining IR spectroscopy and DFT calculations, Fujii *et al.* proposed that the solvated  $[\text{Mg}(\text{G}2)_2]^{2+}$  ion would exist as a *fac*-isomer, where the three oxygens of the G2 molecules situate on three vertices of the

octahedron's face.<sup>21</sup> Nonetheless, G2 is a tridentate ligand, and the solvated  $[\text{Mg}(\text{G}2)_2]^{2+}$  can exist as a *fac*- or *mer*-isomer, which might exhibit different stability in solution. Structural models for the *fac*- and *mer*- $[\text{Mg}(\text{G}2)_2]^{2+}$  isomers were created and reconsidered in our study. The structural optimisation with the SCAN-rVV10 functional shows that *mer*- $[\text{Mg}(\text{G}2)_2]^{2+}$  is more stable than the *fac*-isomer by 37.7 kJ mol<sup>-1</sup> (Fig. S2, ESI†), which would be the favoured isomer to be found in solution. Due to its small size, Mg<sup>2+</sup> cannot adopt a coordination number greater than six in glyme-based electrolytes. The addition of the seventh oxygen to the coordination sphere of Mg<sup>2+</sup> would lead to repulsion between the organic chains and destabilize the structure. Consequently, the solvation structures of Mg<sup>2+</sup> in some of the higher-order glymes are just the derivatives of *mer*- $[\text{Mg}(\text{G}2)_2]^{2+}$ . In the triglyme molecule,  $\text{H}_3\text{CO}(\text{CH}_2\text{CH}_2\text{O})_3\text{CH}_3$ , there are four oxygens available for the complexation. Mg<sup>2+</sup> in a G3 solution can achieve octahedral coordination in the form of [3 + 3] by forming the *mer*- $[\text{Mg}(\text{G}3)_2]^{2+}$  isomer, where each G3 molecule donates three of its oxygens, as demonstrated in the work of Kimura *et al.*<sup>20</sup>

Tetraglyme,  $\text{H}_3\text{CO}(\text{CH}_2\text{CH}_2\text{O})_4\text{CH}_3$ , is a particular case that has a pronounced chelating effect on Mg<sup>2+</sup>. By using Raman spectroscopy, Watkins *et al.* demonstrated that a low-melting solvate ionic liquid with a G4/Mg(TFSI)<sub>2</sub> ratio of 1/1 had no signature of the Mg–TFSI interaction.<sup>32</sup> The absence of the Mg–TFSI vibration in the Raman spectrum implies that Mg<sup>2+</sup> can be completely solvated in the Mg<sup>2+</sup>/G4 ratio of 1/1; nonetheless, the structure of  $[\text{Mg}(\text{G}4)]^{2+}$  is unknown. The structural optimisation with the SCAN-rVV10 functional shows that Mg<sup>2+</sup> in  $[\text{Mg}(\text{G}4)]^{2+}$  resides in a distorted pyramidal site with five Mg–O distances of 1.99, 2.01, 2.03, and 2.04 ( $\times 2$ ) Å (Fig. 3). Furthermore, the addition reaction of G4 to  $[\text{Mg}(\text{G}4)]^{2+}$  is

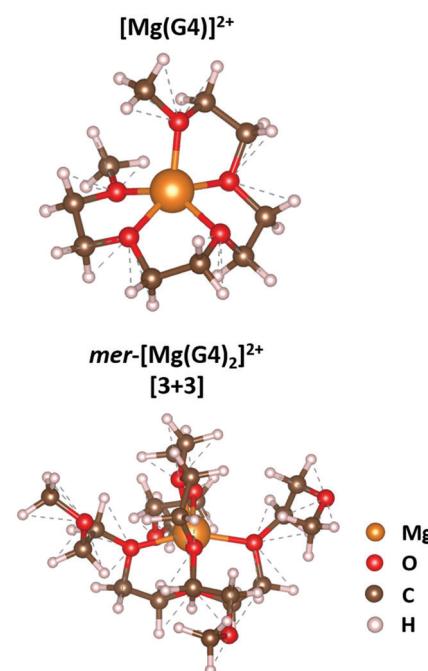


Fig. 3 Optimised structures of  $[\text{Mg}(\text{G}4)]^{2+}$  and *mer*- $[\text{Mg}(\text{G}4)_2]^{2+}$  calculated with the SCAN-rVV10 functional.

exothermic (Table S5, ESI<sup>†</sup>) so that the formation of  $[\text{Mg}(\text{G4})_2]^{2+}$  could occur easily in a dilute solution. The structural optimisation shows that  $[\text{Mg}(\text{G4})_2]^{2+}$  would adopt a structure similar to that of *mer*- $[\text{Mg}(\text{G4})_2]^{2+}$ , in which two G4 molecules run perpendicular to each other, and each G4 donates three oxygens to form a [3 + 3] coordination site (Fig. 3). By using Raman spectroscopy, Terada *et al.* suggested that in 0.5 M  $\text{Mg}(\text{TFSI})_2/\text{G4}$  solution  $\text{Mg}^{2+}$  ions would exist as  $[\text{Mg}(\text{G4})_y]^{2+}$  ( $y > 1$ ), but they did not provide any structural information on this solvation form.<sup>33</sup> Nevertheless, the form that they observed could be the *mer*- $[\text{Mg}(\text{G4})_2]^{2+}$  isomer as described here. In pentaglyme and higher-order glymes, the molecule would have a sufficient amount of oxygen to ensure octahedral coordination for  $\text{Mg}^{2+}$ , and only one molecule will be present in the first coordination sphere of  $\text{Mg}^{2+}$  (Fig. S3, ESI<sup>†</sup>). The computational results reveal that the Mg–O interaction and the ring deformation energy in  $[\text{Mg}(\text{G5})]^{2+}$  are completely comparable to those of *mer*- $[\text{Mg}(\text{G4})_2]^{2+}$  with  $-1659$  vs.  $-1691$  kJ mol<sup>-1</sup> for the former and  $113$  vs.  $130$  kJ mol<sup>-1</sup> for the latter (Fig. S3, ESI<sup>†</sup>), which promotes the formation of  $[\text{Mg}(\text{G5})]^{2+}$  in G5 solution.

### $\text{Ca}^{2+}$ solvation structure

As in the case of  $\text{Mg}^{2+}$ , the solvation structure of  $\text{Ca}^{2+}$  in G4 solution is unknown. Nonetheless, the G4-chelated structure of  $\text{Ca}^{2+}$  in the solid phase, such as  $[\text{Ca}(\text{G4})](\text{SCN})_2 \cdot \text{H}_2\text{O}$ , has been reported in the literature.<sup>34</sup>  $\text{Ca}^{2+}$  in  $[\text{Ca}(\text{G4})](\text{SCN})_2 \cdot \text{H}_2\text{O}$  has a coordination number of eight, and it resides in the centre of the G4 ring with five Ca–O distances of 2.46, 2.49 ( $\times 3$ ), and 2.50 Å. One  $\text{SCN}^-$  ion occupies the coordination site below the ring with a Ca–N distance of 2.49 Å. The other two coordination sites are occupied by one  $\text{SCN}^-$  ion and one  $\text{H}_2\text{O}$  molecule with Ca–N and Ca–O distances of 2.44 and 2.42 Å. By performing extended X-ray absorption fine structure (EXAFS) analysis at the Ca K-edge energy, Hahn *et al.* reported that solvated  $\text{Ca}^{2+}$  in G1, G2, and G3 solutions also has a coordination number of eight; nonetheless, there are no refined structures of these solvated ions.<sup>35</sup> Due to a lack of relevant information, the  $\text{Ca}^{2+}$  solvation structure in G4 solution is determined in this study by a combination of IR spectroscopy and DFT calculations.

Several solutions of  $\text{Ca}(\text{TFSI})_2$  in tetraglyme with a concentration of 0–0.5 M were prepared to determine the  $\text{Ca}^{2+}$  solvation structure. The IR spectrum of pure liquid G4 recorded at ambient temperature shows several broad signals (Fig. 4a). In reality, G4 molecules can exist in several conformations in the liquid state due to a small energy barrier for rotation around the C–C and C–O bonds. The computed IR spectra of four representative conformations of G4 (Fig. S4, ESI<sup>†</sup>) show distinct vibrations for each of them, especially in the range of 1000–1200 cm<sup>-1</sup>, corresponding to the C–H and C–O bonds' stretching modes. Nevertheless, the IR signals recorded for liquid G4 are broad due to different G4 conformations. The signal broadening is likely linked to the significant amount of conformations that cannot be resolved by IR spectroscopy and a rapid transformation between different conformations in the liquid state. By comparing the theoretical and experimental IR spectra, one can note that the linear conformation of G4 is not present in a large amount in solution while tilted conformations are the dominant ones. Upon adding  $\text{Ca}(\text{TFSI})_2$  in liquid G4,  $\text{Ca}^{2+}$ –G4 complexation

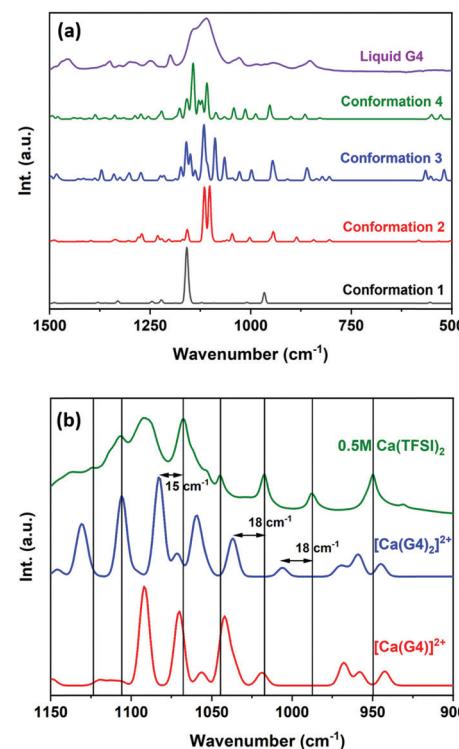


Fig. 4 (a) Computed IR spectra with the SCAN-rVV10 functional of the four representative conformations of the G4 molecule compared to the experimental spectrum recorded for liquid G4 at ambient temperature. (b) Computed IR spectra with the SCAN-rVV10 functional of  $[\text{Ca}(\text{G4})]^{2+}$  and *mer*- $[\text{Ca}(\text{G4})_2]^{2+}$  in [4 + 4] solvation coordination as compared to the experimental spectrum acquired for a 0.5 M  $\text{Ca}(\text{TFSI})_2$  solution in G4.

occurs together with an increase in the intensity of specific IR lines corresponding to the G4 conformation complexing to  $\text{Ca}^{2+}$ . The IR spectra of  $\text{Ca}(\text{TFSI})_2$  in G4 show the appearance of several distinct vibrations in the range of 1000–1200 cm<sup>-1</sup> (Fig. 4b), corresponding to the C–H and C–O stretching modes of the G4 conformation complexing to  $\text{Ca}^{2+}$ , thus providing valuable information for the determination of the  $\text{Ca}^{2+}$  solvation structure. Furthermore, the monotonic evolution in the vibrations' intensity (Fig. S5, ESI<sup>†</sup>) implies that the  $\text{Ca}^{2+}$  solvation structure in G4 is mostly unchanged in the 0.1–0.5 M concentration range.

The most simple solvation model that can exist is  $[\text{Ca}(\text{G4})]^{2+}$  as in the case of  $[\text{Ca}(\text{G4})](\text{SCN})_2 \cdot \text{H}_2\text{O}$ . The optimised structure of  $[\text{Ca}(\text{G4})]^{2+}$  reveals that the G4 molecule forms a nearly flat ring, where  $\text{Ca}^{2+}$  fits perfectly in the ring's centre with five Ca–O distances of 2.30, 2.32, 2.33, and 2.37 ( $\times 2$ ) Å (Fig. 5); nonetheless,  $\text{Ca}^{2+}$  in  $[\text{Ca}(\text{G4})]^{2+}$  is under coordinated.  $\text{Ca}^{2+}$  in  $[\text{Ca}(\text{G4})](\text{SCN})_2 \cdot \text{H}_2\text{O}$  attracts other ligands in the structure to coordination sites above and below the G4 ring to achieve a coordination of eight. Therefore,  $[\text{Ca}(\text{G4})]^{2+}$  might not be the optimum solvation for  $\text{Ca}^{2+}$  in a G4 solution where a surplus of G4 is available. Furthermore, the addition reaction of G4 to  $[\text{Ca}(\text{G4})]^{2+}$  is highly exothermic (by  $-209$  kJ mol<sup>-1</sup>) (Table S5, ESI<sup>†</sup>), which highly favours the formation of  $[\text{Ca}(\text{G4})_2]^{2+}$  in solution. Different  $[\text{Ca}(\text{G4})_2]^{2+}$  solvation models are generated with a coordination number of  $\text{Ca}^{2+}$  varying from six to eight. The stability of  $[\text{Ca}(\text{G4})_2]^{2+}$  increases with its coordination



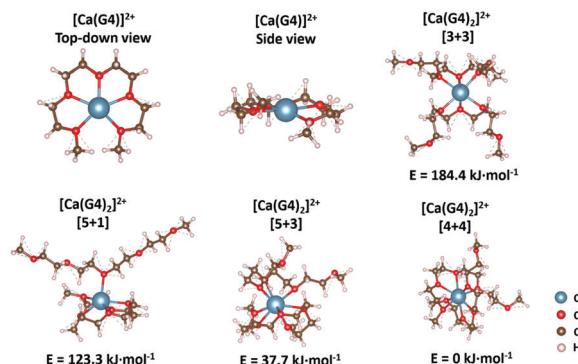


Fig. 5 Optimised structures of  $[\text{Ca}(\text{G4})]^{2+}$  and  $[\text{Ca}(\text{G4})]_2^{2+}$  with the SCAN-rVV10 functional. The relative energy between different forms of  $[\text{Ca}(\text{G4})]^{2+}$  is given for stability comparison.

number due to a higher number of Ca–O bonds surrounding a  $\text{Ca}^{2+}$  centre (Fig. 5). The models with more than eight oxygens participating in the  $\text{Ca}^{2+}$  complexation are unstable, and they converge to a structure with a coordination number of eight during the structural relaxation procedure. Two solvation structures satisfying a coordination number of eight are the  $[5 + 3]$  and  $[4 + 4]$  models, in which the latter is more stable (Fig. 5).

To confirm the existence of  $[\text{Ca}(\text{G4})]^{2+}$  in the form of  $[4 + 4]$  in solution, theoretical IR spectra of  $[\text{Ca}(\text{G4})]^{2+}$  and  $[\text{Ca}(\text{G4})]_2^{2+}$  are calculated and compared to the experimental spectrum acquired for a 0.5 M  $\text{Ca}(\text{TFSI})_2$  solution. The theoretical IR spectra of  $[\text{Ca}(\text{G4})]^{2+}$  and  $[\text{Ca}(\text{G4})]_2^{2+}$  show many similarities, except the vibrations at 1100 and 1150  $\text{cm}^{-1}$ , which only exist in  $[\text{Ca}(\text{G4})]_2^{2+}$  with  $[4 + 4]$  coordination (Fig. 4b). The computed IR spectrum of  $[\text{Ca}(\text{G4})]_2^{2+}$  fits well with the new vibrations observed in a 0.5 M  $\text{Ca}(\text{TFSI})_2$  solution (Fig. 4b) with a global shift of 15–18  $\text{cm}^{-1}$  compared to the experimental data. If a small scaling factor of 0.986 is applied, excellent agreement is obtained, which thus confirms the existence of  $[\text{Ca}(\text{G4})]_2^{2+}$  in the  $[4 + 4]$  form (Fig. S6, ESI†). The  $[\text{Ca}(\text{G4})]_2^{2+}$  structure is quite similar to the *mer*- $[\text{Mg}(\text{G2})_2]^{2+}$  isomer: two G4 chains, wrapping around the  $\text{Ca}^{2+}$  centre, orient along two perpendicular meridians, just like the Earth's Prime-Meridian and Equator. Only four oxygens of each G4 chain participate in the coordination with the  $\text{Ca}^{2+}$  centre in the  $[4 + 4]$  form. The fifth oxygen on each G4 chain does not participate in the complexation and points away from the  $\text{Ca}^{2+}$  centre (Fig. 5). This conformation minimises the repulsion between the two G4 chains and ensures the maximum Ca–O interaction. Note that the potential energy surface of the system was not exhaustively sampled because of its complexity, and there might be some undetermined structures that also contribute to the observable properties, though the ones computed therein reasonably reproduce experimental data.

### $\text{Na}^+$ solvation structure

The chemistry of  $\text{Na}^+$  with glymes is very diverse.  $\text{Na}^+$  can form several solvate ionic liquids with different kinds of glyme, such as  $[\text{Na}(\text{G1})_3][\text{TFSI}]$ ,  $[\text{Na}(\text{G2})_2][\text{TFSI}]$ ,  $[\text{Na}(\text{G3})][\text{TFSI}]$ , and  $[\text{Na}(\text{G3})_2][\text{TFSI}]$ . Furthermore, some of them can be used as stable electrolytes for SIBs.<sup>36,37</sup> Some liquid electrolytes can be crystallised at low temperatures, and their structures have been elucidated by the

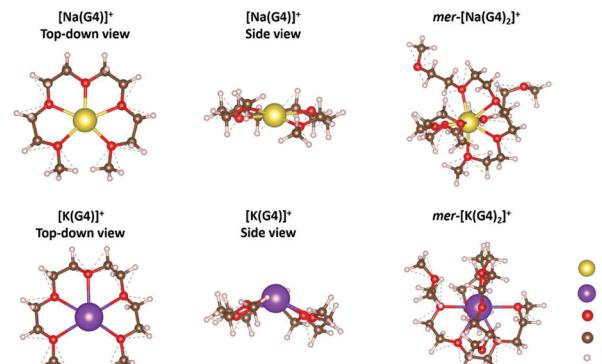


Fig. 6 Optimised structures of  $[\text{M}(\text{G4})]^+$  and  $[\text{M}(\text{G4})]_2^+$  ( $\text{M} = \text{Na}$  and  $\text{K}$ ) calculated with the SCAN-rVV10 functional.

single-crystal X-ray diffraction technique. When glyme/ $\text{Na}^+$  is 1/1, such as  $[\text{Na}(\text{G3})][\text{TFSI}]$ , the glyme molecule encircles  $\text{Na}^+$ , and the  $\text{TFSI}^-$  anions fill the coordination sites above and below the ring.<sup>36</sup> In  $[\text{Na}(\text{G3})][\text{TFSI}]$ ,  $\text{Na}^+$  has a coordination of  $[4 + 3]$  where the four  $\text{Na}–\text{O}$  bonds with the G3 ring are 2.46, 2.47, 2.50, and 2.56 Å, and the other three coordinated oxygens come from two different  $\text{TFSI}^-$  with  $\text{Na}–\text{O}$  distances of 2.33, 2.42, and 2.43 Å. In  $[\text{Na}(\text{G3})_2][\text{TFSI}]$ , two G3 chains wrap around the  $\text{Na}^+$  centre, and the  $\text{TFSI}^-$  anions exist in the crystal in the form of a “solvent-separated ion pair” without any direct interaction with  $\text{Na}^+$ .<sup>36</sup> It is interesting to note that two G3 chains wrap around  $\text{Na}^+$  in  $[\text{Na}(\text{G3})_2][\text{TFSI}]$ , oriented along two perpendicular meridians,<sup>36</sup> as in *mer*- $[\text{Ca}(\text{G4})]_2^{2+}$ . The actual coordination sphere of  $\text{Na}^+$  in G4 solution has not been determined experimentally. Nevertheless, the coordination number of  $\text{Na}^+$  is already saturated with two G3 molecules in the  $[4 + 4]$  form, and no more oxygen can enter the  $\text{Na}^+$  solvation structure. Therefore, it can be predicted that  $\text{Na}^+$  exists in G4 solution in the form of *mer*- $[\text{Na}(\text{G4})]_2^+$  (Fig. 6), whose structure is identical to *mer*- $[\text{Ca}(\text{G4})]_2^{2+}$ .

### $\text{K}^+$ solvation structure

It has long been known that G4 can dissolve K metal at ambient temperature to result in solvated  $\text{K}^+$  ions;<sup>38</sup> nevertheless, little information is known on the solvation structure of  $\text{K}^+$  in G4 or glyme-based solutions. The ionic radius of  $\text{K}^+$  is bigger than  $\text{Na}^+$  and  $\text{Ca}^{2+}$ ; hence, the  $\text{K}^+$  solvation structure cannot adopt coordination less than eight.  $\text{K}^+$  in  $[\text{K}(\text{G4})]^+$  cannot fit into the G4 cavity and puckers out of the ring, thus creating space for one more G4 molecule to enter its solvation sphere to form  $[\text{K}(\text{G4})]_2^+$  (Fig. 6). In  $[\text{K}(\text{G4})]_2^+$ , two G4 chains also run perpendicular to each other to form *mer*- $[\text{K}(\text{G4})]_2^+$  with  $[4 + 4]$  coordination (Fig. 6). The encapsulation of two G4 chains in the *mer*- $[\text{M}(\text{G4})]_2^{n+}$  isomer not only reduces the repulsion between the chains but also has great flexibility to adapt to the size of most ions.

### Relative stability of solvated $[\text{M}(\text{G4})_x]^{n+}$ complexes and their electrochemical activity

The energy of the M–O bonds involved in a particular solvated  $[\text{M}(\text{G4})_x]^{n+}$  complex can be evaluated by the relation  $E_{\text{M}–\text{O}} = \left( E_{[\text{M}(\text{G4})_x]^{n+}(\text{PCM})} - E_{\text{M}^{n+}(\text{gas})} - E_{\text{G4}(\text{PCM})} \right) / m$ ,  $m$  being

**Table 1** Energy of M–O bonds in solvated  $[M(G4)_x]^{n+}$  ( $x = 1$  or  $2$ ) and the energy required for the G4 deformation calculated with the SCAN-rVV10 functional in the VASP code. The coordination number of each central ion is indicated in square brackets

	Total M–O energy (kJ mol <sup>-1</sup> )	Energy per M–O bond (kJ mol <sup>-1</sup> )	Strain energy for G4 (kJ mol <sup>-1</sup> )	Percentage of G4 strain energy compared to M–O energy
$[Li(G4)]^+$ [5]	-542.8	-108.6	72.6	13.4
$[Na(G4)]^+$ [5]	-453.4	-90.7	55.6	12.3
$[Na(G4)_2]^{1+}$ [4 + 4]	-569.0	-71.1	55.7	9.8
$[K(G4)]^+$ [5]	-323.1	-64.6	18.1	5.6
$[K(G4)_2]^{1+}$ [4 + 4]	-434.0	-54.3	44.3	10.2
$[Mg(G4)]^{2+}$ [5]	-1529.1	-305.8	100.2	6.6
$[Mg(G4)_2]^{2+}$ [3 + 3]	-1691.3	-211.4	130.1	7.7
$[Ca(G4)]^{2+}$ [5]	-1189.9	-238.0	82.4	6.9
$[Ca(G4)_2]^{2+}$ [4 + 4]	-1463.0	-182.9	97.5	6.7

the number of M–O bonds and G4 (PCM) being the G4 in a PCM in the same geometry as in the  $[M(G4)_x]^{n+}$  complex to remove any strain effect. The strength of the M–O bonds in  $[M(G4)_x]^{n+}$  decreases in the order  $E_{Mg-O} > E_{Ca-O} > E_{Li-O} > E_{Na-O} > E_{K-O}$  (Table 1). In this series, the strength of the M–O bonds depends significantly on the charge of the ion. The M–O bonds of divalent ions, *e.g.*  $Mg^{2+}$  and  $Ca^{2+}$ , are much more stable than monovalent ions, which is expected from a purely electrostatic consideration. Among the ions bearing the same charge, the strength of the M–O bonds depends inversely on the ionic size of the central ion  $M^{n+}$ . The larger the size of the central ion, the softer the cation (the lower the charge density), and thus the interaction involved with the hard O-atom in the M–O bonds becomes weaker, as can be seen in the pairs Mg–O *vs.* Ca–O and Li–O *vs.* Na–O *vs.* K–O (Table 1). Compared to a free G4 molecule in the solution, the coordinating G4 molecules in the  $[M(G4)_x]^{n+}$  complexes have to undergo structural reorganization to orient their oxygen atoms to proper positions for the coordination to the central cation, and this structural reorganization induces strain that consumes energy. Nevertheless, the formation of M–O bonds can partially compensate for the energy loss in G4 deformation and favour complexation. The stress is greater on the G4 backbone in  $[Li(G4)]^+$  (Table 1) due to the tiny size of  $Li^+$ , while energy is gained by a fifth oxygen coordination to the central  $Li^+$ . The comparison between the  $[M(G4)]^{n+}$  ( $M = Na, K, Mg$ , and  $Ca$ ) ion and its  $[M(G4)_2]^{n+}$  counterpart shows that the gain in the total number of M–O interactions stabilizes the di-solvated system over the mono-solvated one (Table 1). In some particular cases, the proportion of the strain energy to the total M–O interaction is reduced in  $[M(G4)_2]^{n+}$ , and thus the enthalpy is the dominant factor that promotes the formation of  $[M(G4)_2]^{n+}$  in solution. Nevertheless, the entropy of the system decreases when the second G4 molecule participates in the solvation with  $[M(G4)]^{n+}$  because of the reduction of free molecules in the solvent and the reduction in the possible conformations of the complexing G4. For each  $[M(G4)]^{n+}/[M(G4)_2]^{n+}$  pair, a critical temperature should exist and beyond this point the entropy factor becomes dominant, and favours the mono-solvated  $[M(G4)]^{n+}$ .

In terms of electrochemistry, the solutions of  $Li^+$ ,  $Na^+$ , and  $K^+$  in G4 are commonly used as electrolytes for rechargeable batteries, and many of them employ TFSI<sup>-</sup> sources.<sup>39–43</sup> The facility in the plating and stripping reactions of these monovalent ions in G4

solutions could be linked to the low  $M^+–O$  interaction energy (Table 1). The electrochemical evaluation of  $Mg(TFSI)_2$  in G4 is also known, but it is pretty tricky to perform. The  $Mg(TFSI)_2$ /G4 electrolyte must be treated with activated molecular sieves, or additives such as  $Mg(BH_4)_2$  must be used; otherwise, electrode passivation occurs immediately.<sup>33,44</sup> The electrochemical behaviour of diluted  $Ca(TFSI)_2$  in G4 has not been reported; nevertheless, Hahn *et al.* have conducted a Ca plating and stripping experiment with a 0.5 M  $Ca(TFSI)_2$  solution in G1 and G3.<sup>35</sup> In the G1 solution, no reversible Ca electrodeposition and stripping were observed. The authors explained this observation by the fact that most  $Ca^{2+}$  ions in 0.5 M  $Ca(TFSI)_2$ /G1 exist in the form of a “contact ion pair” with  $TFSI^-$  and during reduction the coordinated  $TFSI^-$  ion in the “contact ion pair” becomes susceptible to degradation and then passivates the electrode. By replacing  $TFSI^-$  with a weaker coordinating anion, *e.g.* tetrakis(hexafluoroisopropoxy)borate  $[B(hfip)_4]^-$ , all  $Ca^{2+}$  ions exist as  $[Ca(G1)_4]^{2+}$  and thus the authors succeeded in performing reversible Ca plating and stripping in G1 solution. Nevertheless, the situation in G3 solution is even more complicated. No electrochemical activity is detected for 0.5 M  $Ca(TFSI)_2$  or  $Ca(BHFIP)_2$  in G3, while all the structural analyses show that all  $Ca^{2+}$  ions in these solutions only exist as solvated  $[Ca(G3)_2]^{2+}$ . The same authors speculated that the interaction in  $[Ca(G3)_2]^{2+}$  is so strong that desolvation could hardly occur, and the electrode reaction might suffer exceptionally sluggish desolvation kinetics.<sup>35</sup> The solvation structure of  $[Ca(G3)_2]^{2+}$  shows many similarities to  $[Ca(G4)_2]^{2+}$ , where  $Ca^{2+}$  has a coordination number of [4 + 4], and the *mer*-isomer is the more stable one. Therefore, one could expect that the electrochemical property of  $[Ca(G4)_2]^{2+}$  is similar to that of  $[Ca(G3)_2]^{2+}$ , which means that  $Ca^{2+}$  is strongly solvated in both cases with no reversible Ca plating and stripping reactions regardless of the nature of the anions. In order to promote desolvation and activate the electrochemical property of  $[Ca(G3)_2]^{2+}$  and  $[Ca(G4)_2]^{2+}$ , one should consider all the possibilities to weaken the Ca–O binding energy or reduce the number of solvent molecules present in the first coordination sphere. The following considerations can be taken into account:

- Employing perfluoro-G4 as a solvent or additive:  $Ca^{2+}$  in  $[Ca(G3)_2]^{2+}$  and  $[Ca(G4)_2]^{2+}$  is coordinated by eight oxygens coming from two different G3/G4 molecules, and during the electrode reaction these two molecules have to be desolvated concomitantly. As each G3/G4 chain anchors to  $Ca^{2+}$  by four



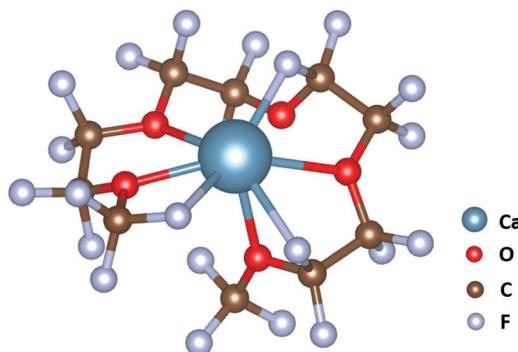


Fig. 7 The solvation structure of  $\text{Ca}^{2+}$  in perfluoro-G4.  $\text{Ca}^{2+}$  is solvated by five oxygens at  $\text{Ca}-\text{O}$  distances of 2.40–2.98 Å and three fluorines at  $\text{Ca}-\text{F}$  distances of 2.35–2.54 Å.

$\text{Ca}-\text{O}$  bonds and the two molecules wrap around the central ion in a perfect arrangement leaving little space for  $\text{Ca}^{2+}$  to escape (Fig. 5), the desolvation from  $[\text{Ca}(\text{G}3)_2]^{2+}$  and  $[\text{Ca}(\text{G}4)_2]^{2+}$  would require a high activation energy. In perfluoro-G4, all the hydrogens are replaced by fluorine, and these fluorine atoms possess lone pairs, which can also coordinate to the central ion, and thus a perfluoro-G4 molecule is sufficient to complete the solvation sphere of  $\text{Ca}^{2+}$  (Fig. 7). Consequently, the desolvation of  $\text{Ca}^{2+}$  from  $[\text{Ca}(\text{perfluoro\_G}4)]^{2+}$  would require the departure of one solvent molecule. Furthermore, the calculations performed at the same dielectric constant value ( $\epsilon_r = 7.5$ ) show that the  $\text{Ca}-\text{O}/\text{F}$  interaction energy in  $[\text{Ca}(\text{perfluoro\_G}4)]^{2+}$  is weaker than the  $\text{Ca}-\text{O}$  interaction energy in  $[\text{Ca}(\text{G}4)_2]^{2+}$  ( $-772 \text{ kJ mol}^{-1}$  vs.  $-1463 \text{ kJ mol}^{-1}$ ). This interaction energy might be strong enough to promote the dissolution of  $\text{Ca}(\text{TFSI})_2$  salt but does not impede the desolvation of  $[\text{Ca}(\text{perfluoro\_G}4)]^{2+}$  during the electrode reactions.

- Employing  $[\text{Ca}(\text{G}4)]^{2+}$  as an electroactive species. Up to now, we just consider the *mer*- $[\text{Ca}(\text{G}4)_2]^{2+}$  isomer, which is the most favourable solvation form of  $\text{Ca}^{2+}$  in dilute solutions in G4, in all discussions.  $\text{Ca}^{2+}$  can also exist as  $[\text{Ca}(\text{G}4)]^{2+}$  in G4-deficient conditions or perhaps in an equimolar mixture of  $\text{Ca}(\text{TFSI})_2$  and G4. When participating in an electrode reaction, the  $\text{Ca}^{2+}$  desolvation from  $[\text{Ca}(\text{G}4)]^{2+}$  only requires the rupture of five  $\text{Ca}-\text{O}$  bonds. Moreover, the total  $\text{Ca}-\text{O}$  interaction in  $[\text{Ca}(\text{G}4)]^{2+}$  is weaker than in  $[\text{Ca}(\text{G}4)_2]^{2+}$  (Table 1), which is a great advantage for the use of  $[\text{Ca}(\text{G}4)]^{2+}$ . Many studies have shown that when mixed in equimolar conditions at elevated temperature and then cooled down to ambient temperature, solvate structures of  $[\text{Li}(\text{G}4)](\text{TFSI})$ ,  $[\text{Na}(\text{G}4)](\text{TFSI})$  and  $[\text{Mg}(\text{G}4)](\text{TFSI})_2$  can be obtained. These compounds are solid at ambient temperature but become liquid at elevated temperature, and they can thus be used as solvents for reactions or electrolytes for batteries.<sup>33,37,45</sup> No such study has been explored for the  $\text{Ca}(\text{TFSI})_2$ -G4 binary system, which can be the goal for future investigations. Derivatives of G4, obtained by attaching different functional groups on the G4 chain, can also be used to stabilize solvate ionic liquids based on  $\text{Ca}(\text{TFSI})_2$ . The presence of functional groups might help to reduce the melting point of  $[\text{Ca}(\text{derivative-G}4)](\text{TFSI})_2$ , if existing, making it become liquid at ambient temperature, which is a necessity for a battery electrolyte. Furthermore, these functional

groups can also protect G4 from degradation in electrochemical reactions.

These mentioned considerations could be taken into account in the development of new glyme-based electrolytes, especially those for Ca-ion batteries. The solvation energy is an essential factor to the performance of the electrolyte, which should be strong enough to promote the formation of solvated ions but not impede ion desolvation in the electrode reactions.

## Conclusions

This study has demonstrated that equivalent conclusions can be extracted from molecular modelling performed with the Q-Chem and VASP codes. Furthermore, the results show that dispersion corrections are required to obtain better structural descriptions and reaction enthalpies. The structures and energetic values computed with the PBE-D3 and SCAN-rVV10 functionals are all equivalent; nevertheless, the SCAN-rVV10 functional is required to obtain accurate information on the topology of the potential energy surface and the phonons. We have also demonstrated the possibility of combining IR spectroscopy with theoretical modelling to identify the solvation structure of  $\text{Ca}^{2+}$  in G4 solution, which can further be applied to determine solvation structures in other glyme-based solutions. The solvation structures of some alkali and alkaline earth metals in G4 were also revised and compared systematically.  $\text{Li}^+$  has a small size, and  $[\text{Li}(\text{G}4)]^+$  exhibits an unusual structure where  $\text{Li}^+$  adopts a coordination number of five.  $\text{Mg}^{2+}$  exhibits structural flexibility in G4, where it can adopt a five-coordination site,  $[\text{Mg}(\text{G}4)]^{2+}$ , in G4-deficient conditions and a six-coordination site,  $[\text{Mg}(\text{G}4)_2]^{2+}$ , in dilute solution.  $\text{Na}^+$ ,  $\text{K}^+$ , and  $\text{Ca}^{2+}$  with large ionic radii tend to adopt eight-coordination sites, and their solvation structures in G4 can all be described by the *mer*- $[\text{M}(\text{G}4)]^{2+}$  isomer, where two G4 chains orient themselves on two perpendicular meridians. The solutions of  $\text{Li}(\text{TFSI})$ ,  $\text{Na}(\text{TFSI})$ ,  $\text{K}(\text{TFSI})$ , and  $\text{Mg}(\text{TFSI})_2$  in G4 can be used as electrolytes for rechargeable batteries. The electrochemical activity of  $\text{Ca}(\text{TFSI})_2$  in G4 has not been observed, which could be due to the strong  $\text{Ca}-\text{O}$  interaction and the participation of two G4 molecules in the first coordination sphere. Nevertheless, the functionalization of the G4 molecule and the investigation of solvate liquid electrolytes based on  $\text{Ca}(\text{TFSI})_2$  and G4 binary mixtures could be the solution to bypass current difficulties. Due to its medium chain length, the G4 molecule has a particular structural property, which is a transition between molecular and polymer glymes. Therefore, the solvation structures in G4 represent those that can exist in more sophisticated glymes, and they can also be used as starting models to construct the solvation sphere in polyethylene oxide. Furthermore, the electrochemical window and the decomposition mechanisms of these glyme-solvated ions can be investigated through interface potential-dependent DFT calculations in upcoming studies.

## Conflicts of interest

There are no conflicts to declare.



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