Journal of Materials Chemistry A

PAPER

Cite this: J. Mater. Chem. A, 2020, 8, 16405

Received 10th April 2020 Accepted 22nd July 2020

DOI: 10.1039/d0ta03945d

rsc.li/materials-a

1 Introduction

The growing global demand for renewable energy sources and the major environmental challenges posed by continued greenhouse gas emissions have made it vital to find new means to improve the efficiency of energy-intensive processes. Some 60% of global energy is wasted as heat, and thermoelectric power provides a means to recover this waste as useful electrical energy. Thermoelectrics can be used either for active cooling, consuming electrical energy to transport heat against a temperature gradient, or for power generation by extracting electrical energy from a temperature gradient.¹ At present, largescale thermoelectric power generation is not feasible due to the

α -Bi₂Sn₂O₇: a potential room temperature n-type oxide thermoelectric†

Warda Rahim, $\mathbf{D}^{\text{*ab}}$ Jo[n](http://orcid.org/0000-0001-9174-8601)athan M. Skelton \mathbf{D}^{c} and David O. Scanlon \mathbf{D}^{abd}

Interest in oxide thermoelectrics has been building due to their high thermal stability and earth-abundant constituent elements. However, the thermoelectric efficiency of flagship oxide materials remains comparatively low, and most materials only reach the maximum figure of merit, ZT , at very high temperatures, above those where the majority of low-grade industrial heat is emitted. It is important to identify thermoelectrics with high conversion efficiency closer to room temperature, particularly for lower-temperature applications such as in domestic heating, consumer electronics and electric vehicles. One of the main factors limiting the efficiency of oxide thermoelectrics is their large lattice thermal conductivities, which has inspired research into more structurally complex materials. In this study, we apply first-principles modelling to assess the low-temperature polymorph of $Bi_2Sn_2O_7$ (α -Bi₂Sn₂O₇) as a potential thermoelectric material, due to its complex crystal structure, which should suppress phonon transport, and the presence of Bi p and Sn s states in the conduction band, which should yield high electrical conductivity when donor (n) doped. Lattice-dynamics calculations using third-order perturbation theory predict an ultralow room-temperature lattice thermal conductivity of 0.4 W m⁻¹ K⁻¹, the lowest ever predicted for an oxide material, and suggest that nanostructuring to a grain size of 5 nm could further decrease this to 0.28 W m⁻¹ K⁻¹. The ultralow lattice thermal conductivity gives α -Bi₂Sn₂O₇ a maximum ZT of 0.36 at 385 K (0.46 with nanostructuring), which is the highest low-temperature value predicted for an oxide thermoelectric. Most importantly, our analysis highlights the relationship between the structural complexity, the chemical nature of the cation, and the short phonon lifetimes, and thus provides guidelines for identifying other novel high-performance oxide thermoelectrics. PAPER

(a) Check for undates
 $\frac{1}{2}$ Check for undates
 $\frac{1}{2}$ Check for undates
 $\frac{1}{2}$ Check for undates
 $\frac{1}{2}$ Check for the state of the **check form of the interpretation** (a) $\frac{1}{2}$ Check for the stat

scarcity of the constituent elements in flagship materials such as $Bi₂Te₃$ and the limited efficiency of more sustainable alternatives. Despite huge investment and research into the development of new thermoelectrics, the field has not made a large amount of progress in the last 50 years.²

The efficiency of a thermoelectric device is determined by the dimensionless figure of merit, ZT, defined as:

$$
ZT = \frac{S^2 \sigma T}{(\kappa_e + \kappa_1)}
$$
 (1)

where S is the Seebeck coefficient, σ is the electrical conductivity, κ_e is the electronic thermal conductivity and κ_1 is the lattice thermal conductivity.³ A low thermal conductivity acts to maintain the temperature gradient and thus the flow of charge carriers through the device, and the total thermal conductivity therefore appears in the denominator.

The properties in the ZT equation are intricately linked, which makes optimising ZT a difficult task. Maximising ZT requires the thermopower $S^2 \sigma$ to be maximised and the total thermal conductivity κ from both the charge carriers and the lattice vibrations (phonons) to be minimised. A high Seebeck coefficient S results from a high density of states effective mass, m^*_{DoS} , and low carrier concentration as shown in eqn (2).

a Department of Chemistry, University College London, 20 Gordon Street, London, WC1H 0AJ, UK. E-mail: warda.rahim.18@ucl.ac.uk; d.scanlon@ucl.ac.uk

b Thomas Young Centre, University College London, Gower Street, London, WC1E 6BT, UK

c Department of Chemistry, University of Manchester, Oxford Road, Manchester, M13 9PL, UK

^dDiamond Light Source Ltd., Diamond House, Harwell Science and Innovation Campus, Didcot, Oxfordshire, OX11 0DE, UK

[†] Electronic supplementary information (ESI) available. See DOI: 10.1039/d0ta03945d

$$
S = \frac{8\pi^2 k_B^2}{3eh^2} m_{\text{DoS}}^* T \left(\frac{\pi}{3n}\right)^{\frac{2}{3}}
$$
 (2)

where, k_B is the Boltzmann constant, e is the elementary charge, h is Planck's constant and n is the carrier concentration. However, the m^* are inversely related to the charge carrier mobilities μ , and high mobilities and carrier concentrations are required for high σ as shown in eqn (3):

$$
\sigma = ne\mu = \frac{ne^2\tau}{m^*}
$$
 (3)

where τ is the average scattering time. Furthermore, increasing σ also increases the electronic thermal conductivity κ_e , as a larger number of carriers facilitates a greater heat transport:⁴

$$
\kappa_{\rm e} = L\sigma T \tag{4}
$$

where L is the Lorenz number. The other contributor to κ is the lattice thermal conductivity κ_l , which encompasses heat transport through phonons, and various material features including structural complexity and intrinsic phonon anharmonicity are good indicators of low κ_1 .

Recently, SnSe rose to the forefront of thermoelectric research due to its ultralow high-temperature lattice thermal conductivity of <0.5 W m⁻¹ K⁻¹ along the layering direction,⁵ highlighting the importance of low lattice thermal conductivity in achieving high ZT values. There has thus been a surge in studying complex ternary and quaternary structures for thermoelectric applications. Mass contrast due to multiple constituent elements, as well as the inevitable higher structural complexity, favours increased phonon scattering and leads to lower lattice thermal conductivity. Building upon this, several ternary and quaternary compounds with complex structures and incorporating heavy elements have been identified that have lower κ_1 values compared to the industry standard Bi₂Te₃.⁶⁻¹⁰ Such complex structures often also have higher effective masses and thus high Seebeck coefficients.

For a material to be used in a thermoelectric module, where several TE materials are joined together in a couple, it is also important that the constituent elements are earth abundant and non-toxic. This provides another compelling reason to investigate oxide thermoelectrics, as they consist of chemically-inert and earth-abundant elements.¹¹ For a practical TE device, the thermoelectric materials should ideally meet a target *ZT* of >1. Although the ZT values of some of oxide thermoelectrics exceed this threshold at high temperature, figures of merit at room temperature (300 K) are often <0.1. Materials with layered structures comprising two different layers stacked along one crystallographic axis have emerged as the most promising candidates for p-type oxide thermoelectrics. Some of the best-performing examples include $Na_xCoO_{2-\delta}$, $Ca_3Co_4O_9$ and $Bi_2Sr_2Co_2O_y$, which have room-temperature ZT values of 0.036, 0.07, and 0.06 to 0.09, respectively.¹²–¹⁵ Among the n-type oxides, materials with the perovskite structure generally perform better than other structure types. This class includes $SrTiO₃$ and $CaMnO₃$, which upon doping have managed to attain maximum room temperature ZT values around 0.03 (ref. 16) and 0.05 (ref. 17–19) respectively. One

of the main contributors to the low ZT values of these structures is their high thermal conductivity,²⁰ which has also been established as a limiting factor in the thermoelectric performance of transparent conducting oxides.²¹ Various attempts at alloying, substitution and nanostructuring have been made to reduce κ within these structures,^{22,23} but have not been fruitful, with κ remaining larger than 1 W m^{-1} K⁻¹ at room temperature.

In addition to good electronic and thermal transport properties, the "dopability", refers to the carrier concentration limits which can be reached in a semiconductor, 24 also plays a significant role in predicting device performance. In this work, we study the thermoelectric properties of α -Bi₂Sn₂O₇, a complex ternary oxide with a pyrochlore-based structure, and a quantitative and accurate study of its dopability is important to fully gauge its potential as a good thermoelectric material. In principle, this can be achieved using first-principles defect calculations which may form part of future work.

 $Bi₂Sn₂O₇$ exists in three different polymorphic forms. The room temperature α form undergoes a first-order phase transition to a β structure at about 390 K, followed by a second-order phase transition to the γ polymorph above 900 K.²⁵ The structure of the high-temperature γ polymorph is undisputed and is the standard cubic $Fd\bar{3}m$ pyrochlore structure, but there has been debate around the structures of the intermediate and room-temperature polymorphs. Lewis et al. resolved this controversy using an exhaustive and automated symmetry mode analysis approach wherein they generated a complete set of candidate structures between the parent γ -Bi₂Sn₂O₇ and a lower symmetry P1 structure and refined each against combined neutron and high-resolution X-ray diffraction (XRD) data.²⁶ Based on this, they suggested the first reliable structural model for the β phase, belonging to the Aba2 space group (41) with 176 atoms per unit cell, and a simplified model for the α phase belonging to the Cc spacegroup (9) with 88 atoms in the **Journal of Materials Chemicary Access**
 $\frac{8\pi}{2}k_x^2$ $\frac{m_x}{2}k_y^2$ ($\frac{m_y}{2}$ ($\frac{m_z}{2}$) on the transit common and θ is limited controlled by "which has above restricted to the state of the state of the state

Fig. 1 Crystal structure of α -Bi₂Sn₂O₇. The view along the [010] plane is aligned along the $SnO₆$ octahedra and highlights the disorder in the Bi atomic chains along the b axis. The atoms are coloured as follows: Bi – orange, Sn – blue, O and O' – black. These images were generated using the VESTA software.²⁹

unit cell (Fig. 1). This is in contrast to the previous structural model of α -Bi₂Sn₂O₇, which was in the Pc spacegroup (7) and has 352 atoms in the unit cell.²⁷ Recently, using a theoreticallyrigorous phonon mode-mapping approach, we elucidated the lowest energy polymorph of $\mathrm{Bi}_2\mathrm{Sn}_2\mathrm{O}_7, ^{28}$ and found it to be the new structural model of α (Cc) suggested by Lewis et al.²⁶

The complex structure of α -Bi₂Sn₂O₇ results from distortions of the high-symmetry γ polymorph. The pyrochlore structure comprises two oxide sublattices consisting of corner-sharing $SnO₆$ octahedra and $Bi₄O'$ tetrahedra. The interpenetration of these two sublattices results in a hexagonal bipyramidal BiO $_6O_2{}^{\prime}$ coordination around the Bi atoms with six long equatorial Bi–O bonds and two short axial Bi-O' bonds. As the temperature is reduced, γ -Bi₂Sn₂O₇ changes progressively to the lower symmetry α structure, which involves minimal internal distortion of $SnO₆$ octahedra and large correlated displacements of the Bi atoms.^{26,30} The distortion is driven by the $6s²$ lone pair of electrons on Bi^{3+} ions and their tendency to prefer noncentrosymmetric coordination environments. In contrast to the eight-coordinate Bi atoms in the standard pyrochlore structure, this results in each Bi atom in α -Bi₂Sn₂O₇ coordinating to five oxygen atoms, with the lone pair occupying its own distinct position. The lone pair effect results in this polymorph being the most thermodynamically stable form of $Bi₂Sn₂O₇$ ³¹ **Paper**

During of Materials Chemistry Article control of the most article is the result of the control of the results of the control of the contr

The recent structural solution of the room-temperature polymorph of $Bi₂Sn₂O₇$ motivated us to study its thermoelectric properties. We anticipated, on the basis of its complex structure, the large number of atoms in the unit cell, and the presence of the stereochemically active lone pair, that it would likely have a low lattice thermal conductivity. The lone pair in SnSe was recently shown to introduce significant anharmonicity into the lattice dynamics,⁵ while the complex structure and large number of atoms should lead to a dense phonon dispersion and allow for multiple phonon scattering pathways, aided by the large mass contrast between the heavier Bi/Sn cations and lighter O anions. Furthermore, $Bi_2Sn_2O_7$ should possess conduction band minimum (CBM) features consistent with many excellent conducting oxides containing post transition metal cations in their highest oxidation state, including ZnO,³² SnO_2 ,³³⁻³⁶ In_2O_3 ,³⁷ CdO³⁸ and BaSnO₃.³⁹ In particular the presence of disperse Sn s states at the CBM is indicative of good carrier mobility, if effective donor doping can be achieved.

In this study, we show using first-principles calculations that the room temperature polymorph of $Bi_2Sn_2O_7$ has an ultralow lattice thermal conductivity due to the presence of heavy metal cations, a complex structure, and the active Bi^{3+} lone pair. With suitable n-type doping, we predict it to have a high roomtemperature ZT relative to other oxide thermoelectrics, highlighting how this strategy may serve as a new route to obtaining high ZT values in oxide materials.

2 Computational modelling

2.1 First-principles calculations

Calculations were performed using pseudopotential plane-wave density functional theory (DFT)⁴⁰ as implemented in the Vienna Ab initio Simulation Package (VASP).⁴¹⁻⁴⁴ The PBEsol functional,⁴⁵ a variation of the Perdew–Burke–Ernzerhof (PBE) generalised-gradient approximation (GGA) functional⁴⁶ revised for solids, was used, as this functional has consistently been shown to give structural properties and phonon frequencies in good agreement with experiment.⁴⁷⁻⁵¹ The projector augmentedwave (PAW) method⁵² was used to represent the core electrons, treating Bi $5d^{10}6s^26p^3$, Sn $4d^{10}5s^25p^2$ and O $2s^22p^4$ as valence states. Convergence testing using the primitive cell of a-Bi₂Sn₂O₇ (44 atoms) suggested that a *Γ*-centered 3 \times 3 \times 2 *k*point mesh and 500 eV plane-wave kinetic-energy cutoff were sufficient to converge the total energy to within 1 meV per atom and 3 meV per atom respectively (Fig. S1†). For the geometry optimisations the cutoff energy was increased to 650 eV to avoid Pulay stress,⁵³ and the optimisation was deemed converged when the residual Hellmann–Feynman forces acting on the atoms were less than 10^{-4} eV \AA^{-1} .

2.2 Electronic-structure and transport calculations

To calculate the electronic band structure and density of states, the screened Heyd–Scuseria–Ernzerhof hybrid functional $(HSE06)$ ⁵⁴ was employed, as HSE06 is known to give band gaps in better agreement with experiment compared to PBEsol.^{55,56} HSE06 splits the exchange interaction into short range (SR) and long range (LR) components, and 25% of the PBE exchange energy is replaced with the exact Hartree–Fock exchange at short-range. Relativistic effects were modelled by explicit treatment of spin-orbit coupling (SOC) effects.⁵⁷ The electronic band structure and density of states plots were produced using the open source Python package sumo.⁵⁸

Electronic transport properties were calculated using the semi-classical Boltzmann transport theory^{59,60} as implemented in the BoltzTraP code.⁶¹ BoltzTraP calculates transport coefficients using the constant relaxation time approximation (RTA), where the electron relaxation time τ is set to a single, isotropic value of 1×10^{-14} s. This method was chosen since calculating electronic relaxation times from first principles requires an explicit treatment of electron–phonon coupling; while this has been implemented in codes such as AMSET, it is computationally very demanding and thus not practical for lowsymmetry structures with large unit cells. The code has previously been tested on a variety of systems and found to give results in good agreement with experiment.⁶²–⁶⁴ It uses a smoothed Fourier expansion to obtain an analytical expression for the band energies, based on the charge carriers responsible for transport being present within a narrow energy range due to a delta function-like Fermi broadening. The interpolated bands pass exactly through the calculated band energies, but outside of these points the derivatives at band crossings cannot be evaluated accurately. These calculations therefore require a dense k -point mesh to keep such errors localised so as not to significantly impact the calculated transport properties, and because the predicted transport properties are obtained as a summation over many Fermi surfaces. We therefore used a denser k-point mesh with $12 \times 12 \times 7$ subdivisions, containing 285 k-points in the irreducible Brillouin zone, for these calculations. Using BoltzTraP, we obtain the electronic conductivity σ/τ , the Seebeck coefficient S, electronic thermal conductivity $\kappa_{\rm e}/\tau$, and the electronic power factor $S^2 \sigma/\tau$ as a function of temperature and carrier concentration. The ab *initio* predicted dimensionless figure of merit ZT is then predicted using these calculated electrical properties and calculated lattice thermal conductivity obtained as described below.

2.3 Lattice-dynamics calculations

Phonon dispersions, density-of-states (DoS) curves and other harmonic quantities were obtained from supercell finitedisplacement phonon calculations using the Phonopy package^{65,66} with VASP as the force calculator. These were combined with third-order force constants to calculate phonon lifetimes perturbatively within the single-mode relaxation time approximation (SM-RTA) using the Phono3py package.⁶⁷ The SM-RTA provides a closed-form solution to the linearised phonon Boltzmann transport equation (LBTE) which relates the macroscopic κ_1 to a sum of contributions from individual phonon modes λ (eqn (5)):

$$
\kappa_{\rm l} = \frac{1}{NV} \sum_{\lambda} C_{\lambda} \nu_{\lambda} \otimes \nu_{\lambda} \tau_{\lambda} \tag{5}
$$

where C_{λ} are the modal heat capacities, v_{λ} are the group velocities, τ_{λ} are the mode lifetimes and the summation is normalised by the unit cell volume V and the number of wave-vectors N used for the Brillouin zone (BZ) integration.

 C_{λ} and ν_{λ} are calculated within the harmonic approximation and assumed to be temperature independent. τ_{λ} are computed from the phonon linewidths Γ_{λ} as $\tau_{\lambda} = 1/(2\Gamma_{\lambda})$. Γ_{λ} are computed from the imaginary part of the phonon self-energy, which is computed perturbatively based on the strengths of energy- and momentum-conserving three-phonon scattering processes.⁶⁷

For the calculation of both the second- and third-order IFCs, we used the supercell finite-displacement method.^{68,69} To obtain the second-order IFCs, the 264 symmetry-inequivalent displacements were performed in a 264-atom cubic supercell expansion of the primitive cell, obtained using the supercell transformation matrix (M_s) shown below:

$$
M_{\rm s} = \begin{bmatrix} 2 & 1 & 0 \\ 0 & 1 & 2 \\ 1 & -1 & 0 \end{bmatrix} \tag{6}
$$

This was found to be sufficient to converge the computed phonon dispersion (see Fig. S3†). Evaluation of the third-order IFCs requires pairwise atomic displacements to be performed in a chosen supercell, the number of which scales with the supercell size. As a compromise between accuracy and computational cost, the IFCs were calculated in the 88-atom conventional cell of α -Bi₂Sn₂O₇, requiring a total of 69 828 single-point calculations.

PBEsol was used for force calculations, as it has been shown to give a good description of lattice dynamics in semiconductors.47,48 The 650 eV kinetic-energy cutoff used for the geometry optimisations was also used for the force calculations, but we did not include an explicit treatment of SOC effects as in the electronic-structure calculations, as these are unlikely to affect the calculated phonon frequencies but would significantly increase the computational cost.⁷⁰ The *F*-centred 3 \times 3 \times 2 k-point mesh used for the geometry optimisations was scaled appropriately for the supercell force calculations.

The phonon DoS was calculated by interpolating frequencies onto a uniform *Γ*-centered *q*-point mesh with $12 \times 12 \times 6$ subdivisions. The phonon dispersion was evaluated by interpolating the frequencies to strings of q -points on a set of paths between the high-symmetry wavevectors in the phonon Brillouin zone.

Modal properties were evaluated in the reciprocal space of the conventional unit cell on a Γ -centered q -point mesh with 6 \times 9 \times 6 subdivisions, chosen based on explicit convergence tests (Fig. S4†), and the Brillouin zone integration was performed using the linear tetrahedron method.⁷¹–⁷³

We also evaluated the pairwise contributions of other modes to the overall linewidths of each phonon mode. Due to the volume of data generated, this was performed using a smaller Γ centered q-point mesh with $4 \times 6 \times 4$ subdivisions, which yields κ_1 values within 5–7% of the denser mesh used in the evaluation of other modal properties (Fig. S4†). Finally, to further investigate the microscopic origin of the phonon lifetimes, we calculated the averaged three-phonon interaction strengths and the two-phonon joint DoS describing the density of energy- and momentum-conserving scattering events as a function of frequency. As the former are very expensive to compute, they were therefore evaluated on a smaller Γ -centered mesh with $2 \times 3 \times 2$ subdivisions, while the JDoS functions were evaluated using the same mesh used to calculate the other properties. Journal of Materials Chemicary A

one-wise cultural Paper access Content Content Content Content Content Content Content Content Content Content

of the case of the second of the second of the second of the second of the

3 Results and discussion

3.1 Equilibrium geometry and electronic structure

The calculated equilibrium lattice constants for the primitive cell are listed along with experimental values in Table 1. We obtain excellent agreement between the theoretical and experimental geometries, with typical deviations of <1%.

The calculated electronic density of states (EDoS) is shown together with an expanded view of valence and conduction band edges in Fig. 2. The valence band maximum (VBM) is dominated by O 2p and Bi 6s states, with small contributions from Bi 6p and Bi 5d states. Between -1 and -4 eV below the VBM, the DoS mainly comprises O 2p, Sn 4d, Sn 5p and Bi 6p states, while between -4 and -6 eV the valence band is dominated by O 2p,

Table 1 Calculated and experimental lattice parameters for the primitive cell of α -Bi₂Sn₂O₇ together with the percentage deviations between calculated and measured values

	a(A)	b(A)	c(A)	α	β	
PBEsol Expt. ²⁶	7.566 7.582	7.566 7.582	13.115 13.144	73.1° 72.7°	106.9° 107.3°	120.1° 120.4°
% Error		-0.2% -0.2% -0.2% $+0.6\%$			-0.4%	-0.2%

Bi 6p, Sn 5s and Sn 5p states. The feature from -6 to around -8 eV consists of O 2p and Sn 5s states, while the feature at lower energies around -10 eV is formed of O 2p and Bi 6s states. The Bi 6s states undergo a bonding interaction with O 2p states at the bottom of the VB and an antibonding interaction at the

Fig. 2 Electronic structure of α -Bi₂Sn₂O₇. (a) Calculated total and projected electronic density of states obtained using HSE06 + SOC with the valence band maximum (VBM) at $E = 0$ eV. (b)/(c) Expanded views of the VBM and conduction band minimum (CBM).

top. These antibonding states are filled and thus form the VBM. In the distorted polymorph of $Bi_2Sn_2O_7$, these states couple to Bi 6p and lead to the formation of an asymmetric electron density around the Bi atoms due to their stereochemically active $6s²$ lone pair. This is consistent with the presence of Bi 6p states in the VBM, and a similar phenomenon arises in other posttransition metal oxides from the interaction of the metal s and p states mediated by the anion p states.^{74,75} On the other hand, the conduction band edge predominantly consists of Bi 6p and O 2p states, while in the rest of the conduction band we observe dominant contributions from Bi 6p, O 2p and Sn 5s states. The conduction band minimum (CBM) also contains small amounts of Sn 5s states, which would mix with Bi 6p and O 2p states to yield low electron effective masses at the Γ -point.

To validate our calculated electronic structure against experiment, we compared against the experimental valence band (VB) X-ray photoemission spectrum (XPS spectrum).⁷⁵ The GALORE software package⁷⁶ was used to simulate a VB photoelectron spectrum from our calculated electronic density of states. The photoionization cross section depends on the probe radiation, the orbital shapes and their energies, and to account for this GALORE uses the Gelius method⁷⁷ to apply weightings to the atom-projected EDoS using the photoionization crosssections formulated by Yeh and Lindau.⁷⁸ For heavy elements, however, the valence s and p orbitals show relativistic effects, which are not taken into account in these calculated crosssections, and which is thus likely to result in some deviation in the simulated and measured spectra. Nevertheless, overlaying the calculated and measured spectra (Fig. 3) shows excellent correspondence between the positions of features in the EDoS obtained from our optimised structure using hybrid DFT and the measured VB XPS spectrum.

The electronic band structure of α -Bi₂Sn₂O₇ in Fig. 4 indicates an indirect fundamental band gap of 3.47 eV and a direct gap of 3.51 eV. The interaction with Bi 6p states at the top of VB

Fig. 3 Simulated valence band (VB) X-ray photoelectron spectrum (XPS spectrum) obtained from the electronic density of states calculated using the HSE06 hybrid functional with spin–orbit corrections. The green markers show the experimental VB XPS spectrum for comparison.⁷⁵

stabilises the s – p antibonding orbitals, resulting in an increased band gap compared to the high-temperature γ - $Bi₂Sn₂O₇$ polymorph.³¹

In our calculations, including explicit treatment of spin– orbit coupling (SOC) resulted in a band gap renormalisation of about 0.3 eV, which was mainly due to a lowering in energy of the CBM (Fig. S2†). This is due to the presence of Bi 6p states in the CBM and the scaling of the SOC correction as approximately $Z⁴$. Moreover, including SOC shifts the VBM from the highsymmetry point L to a point between L and V , and shifts the CBM from the zone centre Γ to a point between Γ and γ .

Within the parabolic band approximation, the effective masses m^* are proportional to the second derivative of the band energy with respect to the electron wave-vector:⁷⁹

$$
m^* = \frac{\hbar^2}{\left(\partial^2 E / \partial k^2\right)}\tag{7}
$$

where ħ is the reduced Planck's constant.

The band structure displays much larger dispersion around the CBM than the VBM, indicating low electron effective masses ($\sim 0.39m_e$ in the CBM-Y direction) and high hole effective masses (\sim 7.34 m_e in the VBM-V direction). Presuming the system is dopable, the low effective masses would result in greater electron mobility compared to hole mobility and therefore higher electrical conductivity for ntype doping. The low effective masses would, however, also lead to a reduced Seebeck coefficient, due to S being directly proportional to the density of states effective mass $m^{*}_{\rm{DoS}}$ (eqn (2)). **Journal of Materials Chemicary Axcelle.** Publis, resulting in an with request on the success Common on 22 July 2020. Downloaded on 22 July 2020. Downloaded on 22 July 2020. Downloaded on 22 July 2020. The success Common

3.2 Electronic transport properties

Materials with valence bands dominated by O 2p states are not normally p-type dopable. The O 2p states are deep in energy

Fig. 4 Electronic band structure of α -Bi₂Sn₂O₇ calculated using the HSE06 hybrid functional with spin–orbit coupling. The valence and conduction bands are coloured blue and orange, respectively, and the valence-band maximum (VBM) is set to $E = 0$ eV. The VBM between L and V and the conduction-band minimum (CBM) between Γ and Y are marked with green and red circles, respectively.

with respect to the vacuum level, with large ionisation potentials, and the formation of localised oxygen hole polarons is therefore highly favoured in such materials.⁸⁰ On the other hand, $Sn(w)$ compounds typically are n-type dopable.⁸¹⁻⁸³ We therefore modelled the electrical properties of n-type doped a- $Bi₂Sn₂O₇$, based on the HSE06 + SOC electronic structure, and up to the limit of 390 K at which the first phase transition takes place (Fig. 5).

The electrical conductivities for carrier concentrations in the range of 10^{17} to 10^{20} cm⁻³ vary from around 6 \times 10¹ to 6 \times 10^4 S m⁻¹. The values obtained with the larger carrier concentrations are comparable to polycrystalline $Na_xCoO_{2-\delta}$ $(\sigma = 5 \times 10^4 \text{ S m}^{-1}$ at 300 K), which possesses one of the highest conductivities among current oxide thermoelectrics.¹³ The high σ is consistent with the dispersive character of the CBM and the resultant low electron effective mass and high carrier mobility.

For n-type transport the Seebeck coefficient is negative, and at room temperature ranges from around 64 to 591 μ V K⁻¹ at carrier concentrations of 10^{20} cm⁻³ and 10^{17} cm⁻³ respectively. The room-temperature Seebeck coefficient of 203 μ V K⁻¹ predicted for a carrier concentration of 10^{19} cm⁻³ is comparable to dual-doped $\text{Zn}_{0.96}\text{Al}_{0.02}\text{Ga}_{0.02}\text{O}$ ($S \sim 176 \mu\text{V K}^{-1}$ at 300 K), which has the highest reported ZT of the known n-type bulk oxide thermoelectrics.⁸⁴

The combination of moderate electrical conductivity and high Seebeck coefficient results in power factors $S^2 \sigma$ ranging from 8–343 μ W m⁻¹ K⁻² at low temperatures/carrier concentrations and high temperatures/carrier concentrations respectively. Though the room temperature power factor of \sim 220–240 μ W m⁻¹ K⁻² at high carrier concentrations is lower than that of Na_xCoO₂ (2380 µW m⁻¹ K⁻² for single crystals and 500 µW m⁻¹ K^{-2} for polycrystalline samples),¹³ they are comparable to the room temperature PFs of most other oxide thermoelectrics including p-type Ca₃Co₄O₉ (\sim 150 μ W m⁻¹ K⁻²).⁸⁵
The electronic thermal conductivities μ range

The electronic thermal conductivities κ_e range from 5.4 \times 10^{-5} at low temperature and low carrier concentration to 4.3 \times 10^{-1} W m⁻¹ K⁻¹ at high temperature and high carrier concentration. For moderate carrier concentrations the electrons thus make a small contribution to the thermal conductivity, and heat transport through the lattice is likely to dominate the total thermal conductivity, as is typical in semiconductors.

3.3 Phonon dispersion and density of states

Fig. 6 shows the simulated phonon dispersion of α -Bi₂Sn₂O₇ together with the atom-projected phonon density of states (pDoS). The primitive cell contains 44 atoms, resulting in $3n_a =$ 132 phonon bands at each wave-vector $(q$ -point) and introducing a large amount of fine structure into the dispersion and DoS. The dispersion shows no imaginary frequencies, con firming that the low-temperature α polymorph of Bi₂Sn₂O₇ is dynamically stable.

The phonon spectrum spans a range of \sim 21.2 THz. As expected from the inverse relationship between the reduced mass and vibrational frequency, the pDoS shows that low-frequency phonon modes up to \sim 4 THz are primarily Bi vibrations with

Fig. 5 Predicted electronic transport properties of n-type doped α -Bi₂Sn₂O₇ over the temperature range of 50–390 K: electrical conductivity σ , Seebeck coefficient S, power factor S² σ (PF) and electronic thermal conductivity $\kappa_{\rm e}$. Values are calculated for carrier concentrations in the range of 10^{17} to 10^{20} cm⁻³ .

small contributions from Sn and O atoms. The intermediate 4– 10 THz range is composed primarily of Sn/O vibrations, while the high frequency modes above 10 THz are predominantly O vibrations.

The relatively flat dispersion implies small group velocities $v_{\rm g} = d\omega/dq$, indicative of a low intrinsic lattice thermal conductivity κ_1 . The low-frequency acoustic modes likely make larger contributions to κ_1 than the optic modes due both to their broader dispersion/larger group velocity and their larger occupation number, which is given by the Bose–Einstein distribution:

$$
n(\lambda, T) = \frac{1}{\exp(\hbar \omega(\lambda)/k_{\rm B}T) - 1}
$$
 (8)

where λ denotes a phonon mode with wavevector q and band index j, T is the temperature, ħ is the reduced Planck's constant, ω is the phonon frequency and k_B is the Boltzmann constant.

3.4 Lattice thermal conductivity

Fig. 7 shows the temperature dependence of the isotropicallyaveraged lattice thermal conductivity $\kappa_{\rm iso}$ together with the thermal conductivity along the three principal directions k_{xx} , k_{yy} and κ_{zz} . We calculate a room-temperature average κ_1 of 0.401 W $m^{-1} K^{-1}$, averaged over principal values of $\kappa_{xx} = 0.398$, $\kappa_{yy} = 0.461$ and $\kappa_{yy} = 0.344$ W m^{-1} K^{-1} . This is the lowest over 0.461 and $k_{zz} = 0.344 \text{ W m}^{-1} \text{ K}^{-1}$. This is the lowest ever calculated or measured for an oxide thermoelectric material near room temperature, and is lower than both SnSe (0.64/ 1.28 W m^{-1} K⁻¹ (ref. 48 and 86)) and the industry-standard PbTe (1.9–2.2 W m⁻¹ K⁻¹ (ref. 87–89)). The κ_1 values along the three lattice vectors differ only slightly, which is to be expected given that the low-temperature α phase of Bi₂Sn₂O₇ remains structurally similar to the high-temperature cubic phase.

Our calculated κ_1 value is likely to be an upper limit, as the RTA only accounts for scattering via three-phonon processes and does not account for the effect of e.g. structural defects and

Fig. 6 Simulated phonon dispersion and atom-projected density of states (pDoS) of α -Bi₂Sn₂O₇. Projections of the DoS onto Bi, Sn and O atoms are shown in orange, blue and black respectively.

Fig. 7 Lattice thermal conductivity of α -Bi₂Sn₂O₇ as a function of temperature calculated within the single-mode relaxation-time approximation and excluding isotope effects. The plot compares the principal xx (diamonds), yy (circles) and zz (triangles) components of the thermal-conductivity tensor with the diagonal average $\frac{1}{3}(\kappa_{xx} + \kappa_{yy} + \kappa_{zz})$ (green stars). The dotted black line marks the room temperature (300 K) average $\kappa_{\rm l}$ of 0.401 W m $^{-1}$ K $^{-1}$).

boundary scattering. The measured κ_1 would likely be further lowered by additional scattering from vacancies, substitutions and/or grain boundaries, if the sample is polycrystalline.

3.5 Modal contributions to the lattice thermal conductivity

To gain insight into the origin of the low room-temperature intrinsic κ_1 of α -Bi₂Sn₂O₇, we examined the modal thermal conductivities κ_{λ} , the group velocities norms $|\nu_{\lambda}|$, the phonon lifetimes τ_{λ} and the phonon mean free paths Λ_{λ} as a function of frequency at 300 K (Fig. 8).

The modes with the largest κ_{λ} are those with high group velocities and long lifetimes, and hence long mean free paths. As shown in Fig. 8(a) the acoustic modes make the largest contribution to κ_1 at 300 K, followed by an order of magnitude smaller contribution from optic modes in the range of 3–5 THz, and then a smaller contribution again from the remainder of the phonon spectrum, with a slight enhancement around 18–19 THz.

Due to the tensor product in eqn (5), the κ_{λ} are proportional to ν^2 . As shown in Fig. 8(b), for the bulk of the modes the $|\nu_\lambda|$ fall within a range if 10^1 to 10^3 ms⁻¹ and are relatively low due to the heavy atoms in the structure. The group velocities are largest around 1, 3 and 13 THz, which coincide with the peaks in the κ_{λ} spectrum. Inspection of the phonon dispersions in Fig. 6 shows regions around 0–1 and 12–13 THz where the modes have large dispersions, whereas over the remainder of the frequency spectrum the bands are relatively flat and indicative of smaller group velocities. The group velocities are comparable to the hybrid perovskite $(CH_3NH_3)PbI_3$ (MAPbI₃), for which an ultralow lattice thermal conductivity of 0.086 W m^{-1} K⁻¹ has been calculated.⁹⁰

The phonon lifetimes in Fig. 8(c) are those obtained by considering three-phonon scattering processes and, as noted above, are likely to be an upper limit due to the neglect of phenomena including higher-order phonon interactions, electron–phonon scattering, and defect and grain-boundary scattering. Across the phonon spectrum the lifetimes are <10 ps and are similar to those in highly-anharmonic compounds such as MAPbI₃.⁹¹ The lifetimes of the acoustic modes are an order of magnitude longer than the optic modes. Since the κ_{λ} are linearly proportional to τ_{λ} , these longer lifetimes are an important factor in the large contribution of the acoustic modes to the overall κ_1 .

The combination of short phonon lifetimes and small group velocities result in phonon mean free paths (Λ_{λ}) on the order of nanometers (Fig. 8(d)), with the majority being ≤ 10 nm. Whereas the spread in the mode group velocities is similar across the phonon spectrum, the strong frequency dependence of the phonon lifetimes results in the mean free paths of the acoustic modes being an order of magnitude longer than those of the optic modes. As expected from eqn (5) there is a strong correlation between Λ_{λ} and the modal κ_{λ} (Fig. S5†). However, the large number of atoms in the unit cell, and consequent small ratio of acoustic to optic modes, means the optic modes nonetheless make a substantial contribution to the overall κ ¹.

This is clearly evident in the cumulative 300 K lattice thermal conductivity as a function of frequency (Fig. 9), which shows that modes from across the entire phonon spectrum, i.e. acoustic as well as low- and high-frequency optic modes, contribute to the heat transport. From the phonon dispersion, the acoustic modes span a range of \sim 0 to 1.3 THz, and these modes contribute around 34% to the total κ_1 . A further \sim 41% of the total κ_1 (*i.e.* 75% in total) is due to low-frequency optic modes up to 5 THz, and thus 75% of the κ_1 arises from the 0–5 THz region of the phonon spectrum. Above 5 THz, the remaining 25% of the thermal conductivity is distributed almost evenly up to 21 THz. This differs markedly from SnSe⁹² and other conventional semiconductors such as GaAs and CdTe,⁹⁰ where

Fig. 8 Analysis of the modal contributions to the 300 K lattice thermal conductivity of α -Bi₂Sn₂O₇ defined in eqn (5): (a) isotropic modal thermal conductivities κ_{λ} , (b) group velocity norms $|v_{\lambda}|$, (c) lifetimes τ_{λ} and (d) mean free paths Λ_{λ} . The data points are coloured by band index. Note that a logarithmic scale is used for the y axis.

the majority of the heat is carried by the acoustic modes and is a consequence of the suppressed acoustic-mode transport, due to the low group velocities and short lifetimes, and the high proportion of optic modes compared to acoustic modes. (Of the $3n_a$ bands at each phonon wave-vector, 3 are acoustic modes and $3n_a - 3$ are optic modes.) This highlights how materials with complex structures can be conducive to obtaining a low lattice thermal conductivity and improving the thermoelectric performance.² A significant contribution of optic modes to the heat transport is also seen in $MAPbI₃$, where transport through the acoustic modes is similarly suppressed.⁹⁰

3.6 Microscopic origin of short phonon mode lifetimes

As noted above the phonon lifetimes are obtained from the phonon linewidths Γ_{λ} as:

$$
\tau_{\lambda} = \frac{1}{2\Gamma_{\lambda}} \tag{9}
$$

Fig. 9 Cumulative % lattice thermal conductivity of α -Bi₂Sn₂O₇ at 300 K as a function of frequency (green) overlaid against the phonon density of states projected onto the Bi (orange), Sn (blue) and O (black) atoms.

 Γ_{λ} are calculated as a sum of contributions from individual three-phonon scattering processes involving pairs of modes λ' and λ ^{*"*} according to:⁶⁷

$$
T_{\lambda} = \frac{18\pi}{\hbar^2} \sum_{\chi\chi''} |\Phi_{-\lambda\chi\chi''}|^2
$$

$$
\times \{ (n_{\chi'} + n_{\chi''} + 1) \delta(\omega_{\lambda} - \omega_{\chi'} - \omega_{\chi''}) + (n_{\chi'} - n_{\chi''})
$$

$$
[\delta(\omega_{\lambda} + \omega_{\chi'} - \omega_{\chi''}) - \delta(\omega_{\lambda} - \omega_{\chi'} + \omega_{\chi''})] \}
$$
 (10)

 $\Phi_{\lambda\lambda'\lambda''}$ are the anharmonic three-phonon interaction strengths,
which are calculated using the third order force constants and which are calculated using the third-order force constants and enforce the conservation of (crystal) momentum. Three-phonon processes can take one of two forms, viz. the decay of one mode into two lower-frequency modes such that $\omega_{\lambda} = \omega_{\lambda'} + \omega_{\lambda''}$, and the collision and coalescence of two modes such that $\omega_1 + \omega_2 =$ $\omega_{\lambda''}$ or $\omega_{\lambda} + \omega_{\lambda''} = \omega_{\lambda'}$. These requirements are enforced by the δ functions in eqn (10). The n_{λ} are the phonon occupation numbers defined in eqn (8) and produce the temperature dependence of the linewidths and lifetimes.

The 2D histogram in Fig. 10 shows the pairwise contributions of modes with frequency ν_{λ} and ν_{λ} to the linewidths of the modes from 0-5 THz identified in the previous section as being responsible for the majority of the heat transport in α - $Bi₂Sn₂O₇$.⁹¹ This analysis shows that strong interactions with acoustic and low-frequency optic modes are primarily responsible for the broadening of these modes. Scattering with modes up to 13 THz also makes a signicant contribution, while scattering processes involving the high-frequency optical modes have a relatively small impact.

The large dispersion of acoustic modes typically limits decay channels at low frequencies so that collisions are the dominant mechanism for acoustic-mode scattering. The large number of low-lying optic modes in α -Bi₂Sn₂O₇ would be significantly

populated at room temperature and provide means of "absorbing" acoustic phonons. A similar histogram analysis of the entire frequency spectrum (Fig. S7†) shows that the other modes in α -Bi₂Sn₂O₇ are also heavily broadened by scattering with modes in the low-frequency part of the spectrum. This region of the spectrum is dominated by Bi^{3+} vibrations, indicating that the heavy cations play a major role in the short mode lifetimes in α -Bi₂Sn₂O₇. The Bi atoms thus serve a dual function in suppressing the thermal transport in α -Bi₂Sn₂O₇: the large mass and weak Bi–O chemical bonding lowers the group velocities, while the resultant low-frequency vibrations enable a large number of decay pathways.

The requirement to conserve energy and (crystal) momentum in three-phonon scattering processes means that the shape of the phonon spectrum plays an important role in defining the number of available scattering pathways. The high density of low-frequency modes in the α -Bi₂Sn₂O₇ phonon spectrum would naturally provide a large number of energyconserving scattering channels. In addition to this, by analogy with SnSe, the presence of the active lone pairs of electrons around Bi may also facilitate stronger phonon–phonon interactions.⁸⁶ To investigate the relative importance of these two contributions, we followed the analysis proposed in ref. 67. The phonon linewidths Γ_{λ} can be approximated by the product of an averaged three-phonon interaction strength P_{λ} and a twophonon joint density of states N_{λ} (JDoS) which counts the number of energy- and momentum-conserving scattering channels available for a reference mode with frequency ω_{λ} : **Journal of Materials Chemicity A**
 $P_1 = \frac{18v}{18v^2}v^2$
 $\frac{1}{2}v^2v^2$
 $\frac{1}{2}v^2v^2$
 $\frac{1}{2}v^2v^2 + 4v^2 + 4v^$

$$
\tilde{\varGamma}_{\lambda} = \frac{18\pi}{\hbar^2} P_{\lambda} N_2(q_{\lambda}, \omega_{\lambda}) \tag{11}
$$

 P_1 is defined as:

$$
P_{\lambda} = \frac{1}{(3n_{\rm a})^2} \sum_{\lambda' \lambda''} \left| \Phi_{\lambda \lambda' \lambda''} \right|^2 \tag{12}
$$

where n_a is the number of atoms in the primitive cell, and thus $3n_a$ is the number of bands at each phonon wavevector. The twophonon JDoS $N_2(q,\omega)$ can be separated into two components for collision (Type 1) events, $N_2^{(1)}$, and decay (Type 2) events, $N_2^{(2)}$:

$$
N_2^{(1)}(q,\omega) = \frac{1}{N} \sum_{\chi \chi''} A(-q + q' + q'')(n_{\chi'} - n_{\chi''})
$$

$$
\times [\delta(\omega + \omega_{\chi'} - \omega_{\chi''}) - \delta(\omega - \omega_{\chi'} + \omega_{\chi''})]
$$

\n
$$
N_2^{(2)}(q,\omega) \frac{1}{N} = \sum A(-q + q' + q'')(n_{\chi'} + n_{\chi''} + 1)
$$
 (13)

$$
N_2^{(2)}(q,\omega)\frac{1}{N} = \sum_{\substack{\lambda'\lambda''}} \Delta(-q+q'+q'')(n_{\lambda'}+n_{\lambda''}+1) \times \delta(\omega-\omega_{\lambda'}-\omega_{\lambda''})
$$
(14)

where the function \varDelta enforces conservation of momentum. We further define a pair of averaged functions $\bar{N}_2(\omega_\lambda)$ which are averaged over the phonon wavevector q.

Fig. 11 compares the spectrum of phonon linewidths of α - $Bi₂Sn₂O₇$ at 300 K to this averaged two-phonon density of states and the spectrum of phonon interaction strengths. The Γ_{λ} show an inverse relationship to the lifetimes in Fig. 8, i.e. are narrow for the low-frequency modes and become broader at higher frequencies. Comparison of the Γ_{λ} with the JDoS $\bar{N}_2(\omega_{\lambda})$ shows

20 $5\frac{15}{5}$
10 15 5 \circ 5 15 Ω 10 20 v_{λ} (THz) Fig. 10 2D histogram showing the pairwise contribution of modes λ'

and λ'' , with frequencies $\nu_{\lambda'}$ and $\nu_{\lambda''}$, to the linewidth of the modes with ν $= 0-5$ THz in α -Bi₂Sn₂O₇. The colour scale is logarithmic and runs from black (zero contribution) to yellow (large contribution). The phonon density of states (green), and its projections onto Bi (orange), Sn (blue), and O atoms (black) is shown against both axes for

that the linewidths closely track the JDoS. This is particularly evident from 0 to 7.5 THz where the steep rise in the linewidth mirrors the sharp increase in the number of available scattering channels. The JDoS shows that Type 1 scattering events (collisions) are dominant at low frequency while Type 2 events (decay) become active around from around 5 THz and dominate at higher frequencies. Since spontaneous decay requires two modes with suitable energy and momentum to decay into, this pathway is only feasible for higher-energy modes. This confirms the main inference drawn from the 2D histogram analysis – that the low-frequency modes are predominantly scattered by interactions with other acoustic modes and low-lying optic modes.

The P_{λ} show a marked dip between 0–5 THz, which is reflected in the linewidths but counteracted by the steep increase in the JDoS over this frequency range. Across the entire spectrum, the linewidths are broadest at intermediate frequencies, which can be attributed to the large number of collision and decay channels available in this region. The averaged interaction strengths are stronger and show comparatively little variation at higher frequencies, which further explains the shorter lifetimes of these modes. Comparison with $MAPbI₃$ shows that the phonon–phonon interaction strengths are fairly weak and are more similar in magnitude to GaAs and CdTe.⁹⁰ We can therefore infer that the dominant factor in the short lifetimes and limited thermal transport in α -Bi₂Sn₂O₇ is the high density of scattering channels. This is a consequence of the shape of the spread of frequencies in the dispersion and DoS rather than strong interactions between modes. This can be attributed to the asymmetric bonding environment caused by the lone pair activity on the Bi cations inducing structural distortions from the high-temperature cubic phase.

3.7 Nanostructuring

The lattice thermal conductivity in thermoelectrics can be further reduced by employing a range of hierarchical approaches, of which nanostructuring is among the most popular.93,94 Analysis of modal contributions to lattice thermal conductivity shows that it is the Bi-dominant low-frequency modes that make the greatest contributions to κ_1 due to their longer mean free paths. Therefore, nanostructuring to suppress such modes is an obvious route to further reducing the thermal conductivity. One route to achieve this is to disperse nanoparticles into the material. Dispersal of ErAs nanoparticles into In_{0.53}Ga_{0.47}As alloys was used to successfully reduce the κ_1 ⁹⁵ while nanostructuring $\text{AgPb}_{18}\text{SbTe}_{20}$ to 20-30 nm drastically increased the thermoelectric figure of merit from 0.5 to 2.2 .^{96,97} However, the mean free paths in α -Bi₂Sn₂O₇ are close to typical grain sizes, with the majority being less than 10 nm (see Fig. 8), which means nanostructuring is unlikely to be quite so fruitful here. However, nanostructuring down to 5 nm has been demonstrated for $Ag_{1-x}Sb_{1+x}Te_{2+x}$ ($x = 0, 0.1$ and 0.2), resulting in a very low κ_1 of only 0.7 W m^{-1} K⁻¹.⁹⁸

We therefore modelled the effect of nanostructuring at two different length scales, viz. 10 nm and 5 nm, using a simple boundary scattering model which limits the contributions to κ_1

Fig. 11 Analysis of the phonon linewidths in α -Bi₂Sn₂O₇ using eqn (11– 14). (a) Mode linewidths Γ_λ as a function of frequency. (b) Two-phonon density of states $N_2(\omega_\lambda)$ showing the density of energy- and momentum-conserving three-phonon scattering channels as a function of frequency. Contributions from collisions (Type 1 events, $N_2^{(1)}$) and decay events (Type 2 events, $N_2^{(2)}$) are shown separately. (c) Averaged three-phonon interaction strength P_{λ} . The data points in (a) and (c) are coloured by band index. Note that the y -axis in (b) is on a linear scale while the axes in (a) and (c) are on a logarithmic scale.

from modes with mean free paths greater than the cutoff. As expected, imposing boundary scattering limits comparable to the acoustic mode mean free paths further reduces κ ₁, as shown in Fig. 12. The room temperature isotropically averaged κ_1 is reduced from 0.401 to 0.314 and 0.277 W m^{-1} K⁻¹ for grain sizes of 10 and 5 nm, respectively, indicating that if nanostructuring is possible down to these length scales it could significantly reduce κ_1 . Nanostructuring is also likely to decrease the electrical conductivity σ but would also therefore decrease κ_e which, along with the appreciable reduction in κ_l , may lead to an overall increase the ZT.

3.8 Maximum ZT and comparison with other oxide and low temperature thermoelectrics

Fig. 13 shows the predicted variation of the figure of merit ZT of n-type doped α -Bi₂Sn₂O₇ as a function of carrier concentration and temperature. The ZT value at each temperature and concentration is obtained by combining the predicted electrical properties and lattice thermal conductivity obtained in the previous sections. The maximum room temperature (300 K) ZT, where $\kappa_1 = 0.401 \text{ W m}^{-1} \text{ K}^{-1}$, is predicted to be 0.180 and occurs
at an electron certier concentration of $1.54 \times 10^{19} \text{ cm}^{-3}$. The at an electron carrier concentration of 1.54×10^{19} cm⁻³. The
movimum Z^T of 0.250 is predicted to equal at 225 K (μ maximum ZT of 0.359 is predicted to occur at 385 K (κ_1 = 0.322 W m⁻¹ K⁻¹) with a carrier concentration of 1.73×10^{19}
cm⁻³ and is the highest law temperature Z^T predicted for an cm^{-3} , and is the highest low temperature ZT predicted for an oxide thermoelectric at the time of writing.

With the reduction in κ_1 obtained by nanostructuring to 5 nm (Fig. 12), and under the assumption of a minimal effect on the electronic transport, we predict a room-temperature ZT of 0.246 $(k_1 = 0.277 \text{ W m}^{-1} \text{ K}^{-1})$; carrier concentration of $1.40 \times 10^{19} \text{ m}^{-3}$) and a maximum ZT of 0.459 at 295 K $(k_1 = 0.227 \text{ W m}^{-1}$ cm⁻³), and a maximum ZT of 0.458 at 385 K ($k_1 = 0.237$ W m⁻¹ K^{-1} , carrier concentration of 1.50 \times 10¹⁹ cm⁻³) (Fig. 13). Although nanostructuring to such a small size is challenging, it would substantially improve its TE performance, and given the very short phonon mean free paths predicted by the thermalconductivity calculations, nanostructuring at larger length scales would have comparatively little effect.

Fig. 12 Isotropically averaged lattice thermal conductivity κ_1 of α - $Bi₂Sn₂O₇$ as a function of temperature with a boundary scattering model used to mimic the effect of nanostructuring at different length scales. The plot compares κ_1 obtained without boundary scattering (pink circles) to values obtained with maximum phonon mean free paths of 10 nm (orange diamonds) and 5 nm (teal stars).

Fig. 13 Predicted thermoelectric figure of merit ZT of n-type doped α -Bi₂Sn₂O₇ as a function of temperature and carrier concentration. Plot (a) shows the predictions obtained based on the thermal conductivity calculated for the bulk material, while (b) shows the improved performance obtained by nanostructuring to 5 nm.

Since the structure undergoes a phase transition above 390 K, it may not be suitable for high-temperature industrial applications, but could be used to improve the efficiency of consumer devices that generate heat at or below 100 \degree C. Such applications might include for example recovering heat from exhaust gases in domestic boilers, recovering wasted energy from microprocessors, and battery conditioning in electric vehicles. The possibility of using a thermoelectric generator to improve the efficiency of domestic boilers is a particularly topical application given the large contribution of gas central heating to carbon emissions and the infrastructure challenges of replacing this with cleaner alternatives such as hydrogen.^{99,100}

A comparison of α -Bi₂Sn₂O₇ to other oxide thermoelectrics shows that it does not possess an exceptionally high or low power factor, but that its high predicted room temperature ZT results from its ultra-low intrinsic κ_1 , p-type NaCo₂O₄ is one of the earliest reported oxide thermoelectrics,¹² and single crystals of $\text{Na}_x\text{CoO}_{2-\delta}$ have high power factors comparable to the industry standard $Bi₂Te₃$. However, this material has a room temperature ZT of only 0.036 due to its high κ_1 of \sim 16.5 W m⁻¹ K^{-1} ,¹³ which is around 40 \times higher than our predicted 0.4 W
m⁻¹ K^{-1} for α -Bi Sp. Q. Similarly, p-type Ce Ce Q. only attains $m^{-1} K^{-1}$ for α -Bi₂Sn₂O₇. Similarly, p-type Ca₃Co₄O₉ only attains a ZT of around 0.07 at 300 K (${\sim}0.83$ at 973 K),¹⁴ again due to a large κ_1 of around 3 W m^{-1} K⁻¹. Finally, Bi₂Sr₂Co₂O_y, which has a layered structure similar to $NaCo₂O₄$ and $Ca₃Co₄O₉$, still has thermal conductivities ranging from 1.7 to 1.9 W m^{-1} $\mathrm{K}^{-1},$ up to 5 \times larger than Bi₂Sn₂O₇, and as a result gives a lowtemperature ZT of only 0.06 to 0.09, only rising to \sim 1.1 at a very high temperature of 973 K.¹⁵ The room-temperature polymorph of $Bi_2Sn_2O_7$ is thus predicted to perform significantly better than some of the best known p-type oxide thermoelectric materials at low temperature.

Comparison with n-type oxide semiconductors further highlights the potential thermoelectric performance of α - $Bi₂Sn₂O₇$. La- and Nb-doped single crystals of the cubic perovskite $SrTiO₃$ show very high electrical conductivity and power factors,¹⁶ but both have large room-temperature thermal conductivities, in the range of 9 to 12 W m^{-1} K $^{-1}$, resulting in a maximum 300 K ZT of only \sim 0.03, which is 6 \times smaller than that predicted for α -Bi₂Sn₂O₇. The n-type oxide semiconductor CaMnO₃ has a large κ_1 of 2–4 W m⁻¹ K⁻¹ at room temperature, resulting in $ZT < 0.05$ even after substitution.¹⁷⁻¹⁹ Dual-doped ZnO with Al and Ga has the highest reported ZT among the ntype oxides, with a power factor comparable to conventional thermoelectrics such as $Bi₂Te₃$, PbTe and Si-Ge.⁸⁴ Its roomtemperature thermal conductivity is, however, almost 30 times larger than $Bi_2Sn_2O_7$ (\sim 13 W m⁻¹ K⁻¹ for Zn_{0.96}Al_{0.02}Ga_{0.02}O), and it again only reaches a low ZT of only 0.14 at room temperature. **Paper**

Fundamy standard functions Are on Disparent and non-methods Article is liberations are completely the complete on the paper of the sixtense Article is likely the standard on 2019 and 2019 and 2019 and 2019 and 20

At present, the industry-standard materials for lowtemperature power generation are the $Bi₂Te₃$ alloys. Conventional $Bi₂Te₃$ -based materials attain a ZT of around 1 at room temperature,¹⁰¹ and further enhancements above unity have been achieved by tuning the composition, either by introducing ternary phases or by doping, and by optimising the fabrication methods.¹⁰²–¹⁰⁴ The lattice thermal conductivities range between 0.2–0.7 W m^{-1} K⁻¹ for compositionally-tuned and nanostructured samples,¹⁰²⁻¹⁰⁶ but it is mainly the outstanding power factors that are responsible for its higher ZT in comparison to α - $Bi_2Sn_2O_7$. α - $Bi_2Sn_2O_7$ is, however, composed of earth-abundant and cheap constituent elements, in contrast to the rare and expensive tellurium required to form $Bi₂Te₃$.

 $CsBi₄Te₆$ has also shown promise as a room-temperature thermoelectric, with very high power factors above 5000 μ W m^{-1} K⁻² in p-type doped samples producing high *ZT* values of around 0.82 at 225 K. However, this material has been predicted to have a κ_1 of 0.87 W m⁻¹ K⁻¹,¹⁰⁷ almost twice that of α -
Bi Sp Q, and even province term and even priva Te $Bi₂Sn₂O₇$, and again requires rare and expensive Te.

Recently, Mao et al. have demonstrated the potential of Mg_3Bi_2 -based alloys, which, unlike Bi_2Te_3 and $CsBi_4Te_6$, consist of earth-abundant elements.¹⁰⁸ Doping with small amounts of Te increases the power factor to 2000 μ W m⁻¹ K⁻², resulting in a ZT of 0.3 at 350 K, which is lower than the maximum ZT predicted for α -Bi₂Sn₂O₇. The low ZT was attributed to high κ_1 of between 2–3 W m^{-1} K⁻¹ at low temperatures, which can be

reduced by partial substitution of Bi with Sb, leading to a maximum ZT of 0.9 at 350 K for n-type $Mg_{3,2}Bi_{1,298}Sb_{0,7}Te_{0.002}$. It should be noted that although the maximum ZT obtained for α -Bi₂Sn₂O₇ is lower than the current best low-temperature thermoelectric materials, we have not investigated strategies such as alloying or band-structure engineering which may help to further improve the thermoelectric performance.

On the other hand, α -Bi₂Sn₂O₇ stands out among other oxide thermoelectrics as having a very low room-temperature lattice thermal conductivity. The strong chemical bonding in most oxide materials leads to large group velocities and, at best, moderate κ_1 values. The heavy metal cations in Bi₂Sn₂O₇ naturally impart weaker bonding and lower group velocities. Furthermore, the structural distortion induced by the active lone pair spreads out the phonon frequencies and results in a complex structure and a dense phonon dispersion, and this, together with the low-frequency vibrations associated with the Bi cations, produces a high density of energy-conserving scattering channels and leads to very short phonon lifetimes. These unusual lattice dynamics lead to the highest room-temperature ZT predicted so far for an oxide material.

4 Conclusions

We have used state-of-the-art quantum chemistry techniques to predict the thermoelectric properties of the room-temperature α polymorph of the heavy metal oxide Bi₂Sn₂O₇. Latticedynamics calculations suggest that α -Bi₂Sn₂O₇ possesses an ultralow lattice thermal conductivity of 0.4 W m^{-1} K⁻¹ at 300 K, the lowest ever predicted for an oxide at room temperature, due to a combination of low group velocities and extremely short phonon lifetimes. This low lattice thermal conductivity yields a room temperature n-type ZT of 0.18 and a maximum ZT of 0.36 at 385 K, which represent the highest low-temperature values yet predicted for an oxide thermoelectric. Despite having lower ZT than the industry-standard $Bi₂Te₃$, it offers the advantage of being composed of earth-abundant and cheap elements and therefore being suitable for widespread deployment. Our calculations suggest that its thermoelectric properties might be further improved by nanostructuring. A detailed analysis of the short phonon lifetimes shows that the structural distortions induced by the active lone pairs on the Bi cations produce a high density of phonon scattering pathways. This effect reinforces the naturally low group velocities arising from the weak chemical bonding associated with the heavy metals, and results in an ultra-low lattice thermal conductivity. The importance of its dopability for practical application as a thermoelectric material should not be underestimated. However, regardless of whether it can be doped or not this work provides a blueprint for improving the performance of oxide thermoelectrics by looking to complex multiternary systems with heavy cations, and thus paves the way for the guided discovery of other lowtemperature oxide thermoelectrics.

Conflicts of interest

The authors declare no competing financial interests.

Acknowledgements

Via our membership of the UKs HEC Materials Chemistry Consortium, which is funded by EPSRC (EP/L000202, EP/ R029431), this work used the ARCHER UK National Supercomputing Service (http://www.archer.ac.uk). We are also grateful to the UK Materials and Molecular Modelling Hub for computational resources, which is partially funded by EPSRC (EP/P020194/1), and to UCL for access to the Legion (Legion@UCL), Myriad (Myriad@UCL) and Grace (Grace@UCL) supercomputers. WR is grateful to University College London for awarding the PhD scholarship. JMS is grateful to the University of Manchester for the award of a Presidential Fellowship. **Journal of Materials Chemicary A⁴

¹⁹ 6. Xin, R. Fundhashi,** *P.* **P., Fundhashi,** *P.* **P. J. R. T. Fundhashi,** *P.* **P. J. R. T. T. R. T. C. C. Windown,** *Matterials* **Chemicary 2021** *Kin, S. P. R. T. C.* **C. Windown,** *Matt*

Notes and references

- 1 D. T. Morelli, Encyclopedia of Applied Physics, 1997, 21, 339.
- 2 F. J. Disalvo, Science, 1999, 285, 703.
- 3 T. M. Tritt, Annu. Rev. Mater. Res., 2011, 41, 433.
- 4 R. Franz and G. Wiedemann, Ann. Phys., 1853, 165, 497.
- 5 L.-D. Zhao, C. Chang, G. Tan and M. G. Kanatzidis, Energy Environ. Sci., 2016, 9, 3044.
- 6 Y. Pei, C. Chang, Z. Wang, M. Yin, M. Wu, G. Tan, H. Wu, Y. Chen, L. Zheng, S. Gong, T. Zhu, X. Zhao, L. Huang, J. He, M. G. Kanatzidis and L. D. Zhao, J. Am. Chem. Soc., 2016, 138, 16364.
- 7 T. J. Slade, J. A. Grovogui, S. Hao, T. P. Bailey, R. Ma, X. Hua, A. Gue, C. Uher, C. Wolverton, V. P. Dravid and M. G. Kanatzidis, J. Am. Chem. Soc., 2018, 140, 7021.
- 8 J. Li, Y. Zhou, S. Hao, T. Zhang, C. Wolverton, J. Zhao and L.-D. Zhao, Inorg. Chem., 2019, 58, 1339.
- 9 H. Xie, X. Su, X. Zhang, S. Hao, T. P. Bailey, C. C. Stoumpos, A. P. Douvalis, X. Hu, C. Wolverton, V. P. Dravid, C. Uher, X. Tang and M. G. Kanatzidis, J. Am. Chem. Soc., 2019, 141, 10905.
- 10 S. Pan, C. Wang, Q. Zhang, B. Yang, Y. Cao, L. Liu, Y. Jiang, L. You, K. Guo, J. Zhang, J. Yang, J. Luo and W. Zhang, ACS Appl. Energy Mater., 2019, 2, 8956.
- 11 Y. Feng, X. Jiang, E. Ghafari, B. Kucukgok, C. Zhang, I. Ferguson and N. Lu, Adv. Compos. Hybrid Mater., 2018, 1, 114.
- 12 I. Terasaki, Y. Sasago and K. Uchinokura, Phys. Rev. B: Condens. Matter Mater. Phys., 1997, 56, R12685.
- 13 K. Fujita, T. Mochida and K. Nakamura, Jpn. J. Appl. Phys., 2001, 40, 4644.
- 14 M. Shikano and R. Funahashi, Appl. Phys. Lett., 2003, 82, 1851.
- 15 R. Funahashi and M. Shikano, Appl. Phys. Lett., 2002, 81, 1459.
- 16 S. Ohta, T. Nomura, H. Ohta and K. Koumoto, J. Appl. Phys., 2005, 97, 34106.
- 17 M. Ohtaki, H. Koga, T. Tokunaga, K. Eguchi and H. Arai, J. Solid State Chem., 1995, 120, 105.
- 18 D. Flahaut, T. Mihara, R. Funahashi, N. Nabeshima, K. Lee, H. Ohta and K. Koumoto, J. Appl. Phys., 2006, 100, 084911.
- 19 G. Xu, R. Funahashi, Q. Pu, B. Liu, R. Tao, G. Wang and Z. Ding, Solid State Ionics, 2004, 171, 147.
- 20 J. W. Fergus, J. Eur. Ceram. Soc., 2012, 32, 525.
- 21 K. B. Spooner, A. M. Ganose and D. O. Scanlon, J. Mater. Chem. A, 2020, 8, 11948.
- 22 H. Muta, K. Kurosaki and S. Yamanaka, J. Alloys Compd., 2004, 368, 22.
- 23 L. M. Daniels, S. N. Savvin, M. J. Pitcher, M. S. Dyer, J. B. Claridge, S. Ling, B. Slater, F. Corà, J. Alaria and M. J. Rosseinsky, Energy Environ. Sci., 2017, 10, 1917.
- 24 A. Goyal, P. Gorai, E. S. Toberer and V. Stevanović, npj Comput. Mater., 2017, 3, 42.
- 25 R. D. Shannon, J. D. Berlein, J. L. Gillson, G. A. Jon and A. W. Sleight, J. Phys. Chem. Solids, 1980, 41, 117.
- 26 J. W. Lewis, J. L. Payne, I. R. Evans, H. T. Stokes, B. J. Campbell and J. S. O. Evans, J. Am. Chem. Soc., 2016, 138, 8031.
- 27 I. R. Evans, J. A. K. Howard and J. S. O. Evans, J. Mater. Chem., 2003, 13, 2098.
- 28 W. Rahim, J. M. Skelton, C. N. Savory, I. R. Evans, J. S. O. Evans, A. Walsh and D. O. Scanlon, Chem. Sci., 2020, DOI: 10.1039/D0SC02995E.
- 29 K. Momma and F. Izumi, J. Appl. Crystallogr., 2011, 44, 1272.
- 30 D. P. Shoemaker, R. Seshadri, M. Tachibana and A. L. Hector, Phys. Rev. B: Condens. Matter Mater. Phys., 2011, 84, 064117.
- 31 A. Walsh and G. W. Watson, Chem. Mater., 2007, 19, 5158.
- 32 S. C. Dixon, S. Sathasivam, B. A. D. Williamson, D. O. Scanlon, C. J. Carmalt and I. P. Parkin, J. Mater. Chem. C, 2017, 5, 7585.
- 33 M. J. Powell, B. A. D. Williamson, S. Y. Baek, J. Manzi, D. B. Potter, D. O. Scanlon and C. J. Carmalt, Chem. Sci., 2018, 9, 7968.
- 34 S. D. Ponja, B. A. D. Williamson, S. Sathasivam, D. O. Scanlon, I. P. Parkin and C. J. Carmalt, J. Mater. Chem. C, 2018, 6, 7257.
- 35 J. E. N. Swallow, B. A. D. Williamson, T. J. Whittles, M. Birkett, T. J. Featherstone, N. Peng, A. Abbott, M. Farnworth, K. J. Cheetham, P. Warren, D. O. Scanlon, V. R. Dhanak and T. D. Veal, Adv. Funct. Mater., 2018, 28, 1701900.
- 36 B. A. D. Williamson, T. J. Featherstone, S. S. Sathasivam, J. E. N. Swallow, H. Shiel, L. A. H. Jones, M. J. Smiles, A. Regoutz, T.-L. Lee, X. Xia, C. Blackman, P. K. Thakur, C. J. Carmalt, I. P. Parkin, T. D. Veal and D. O. Scanlon, Chem. Mater., 2020, 32, 1964.
- 37 J. E. N. Swallow, B. A. D. Williamson, S. Sathasivam, M. Birkett, T. J. Featherstone, P. A. E. Murgatroyd, H. J. Edwards, Z. W. Lebens-Higgins, D. A. Duncan, M. Farnworth, P. Warren, N. Peng, T. L. Lee, L. F. Piper, A. Regoutz, C. J. Carmalt, I. P. Parkin, V. R. Dhanak, D. O. Scanlon and T. D. Veal, Mater. Horiz., 2020, 7, 236.
- 38 M. Burbano, D. O. Scanlon and G. W. Watson, J. Am. Chem. Soc., 2011, 133, 15065.
- 39 Z. Lebens-Higgins, D. O. Scanlon, H. Paik, S. Sallis, Y. Nie, M. Uchida, N. F. Quackenbush, M. J. Wahila,

G. E. Sterbinsky, D. A. Arena, J. C. Woicik, D. G. Schlom and L. F. J. Piper, Phys. Rev. Lett., 2016, 116, 027602.

- 40 W. Kohn and L. J. Sham, Phys. Rev., 1965, 140, A1133.
- 41 G. Kresse and J. Hafner, Phys. Rev. B: Condens. Matter Mater. Phys., 1993, 47, 558.
- 42 G. Kresse and J. Hafner, Phys. Rev. B: Condens. Matter Mater. Phys., 1994, 49, 14251.
- 43 G. Kresse and J. Furthmuller, Comput. Mater. Sci., 1996, 6, 15.
- 44 G. Kresse and J. Furthmüller, *Phys. Rev. B: Condens. Matter* Mater. Phys., 1996, 54, 11169.
- 45 J. P. Perdew, A. Ruzsinszky, G. I. Csonka, O. A. Vydrov, G. E. Scuseria, L. A. Constantin, X. Zhou and K. Burke, Phys. Rev. Lett., 2007, 100, 136406.
- 46 J. P. Perdew, K. Burke and M. Ernzerhof, Phys. Rev. Lett., 1996, 77, 3866.
- 47 J. M. Skelton, D. Tiana, S. C. Parker, A. Togo, I. Tanaka and A. Walsh, J. Chem. Phys., 2015, 143, 64710.
- 48 J. M. Skelton, L. A. Burton, S. C. Parker, A. Walsh, C.-E. Kim, A. Soon, J. Buckeridge, A. A. Sokol, C. R. A. Catlow, A. Togo and I. Tanaka, Phys. Rev. Lett., 2016, 117, 075502.
- 49 A. M. Ganose, M. Cuff, K. T. Butler, A. Walsh and D. O. Scanlon, Chem. Mater., 2016, 28, 1980.
- 50 A. M. Ganose, K. T. Butler, A. Walsh and D. O. Scanlon, J. Mater. Chem. A, 2016, 4, 2060.
- 51 M. A. Tumelero, L. C. Benetti, E. Isoppo, R. Faccio, G. Zangari and A. A. Pasa, J. Phys. Chem. C, 2016, 120, 11797.
- 52 P. E. Blöchl, Phys. Rev. B: Condens. Matter Mater. Phys., 1994, 50, 17953.
- 53 P. Pulay, Mol. Phys., 1969, 17, 197.
- 54 A. V. Krukau, O. A. Vydrov, A. F. Izmaylov and G. E. Scuseria, J. Chem. Phys., 2006, 125, 6158.
- 55 C. N. Savory, A. M. Ganose, W. Travis, R. S. Atri, R. G. Palgrave and D. O. Scanlon, J. Mater. Chem., 2016, 4, 12648.
- 56 A. M. Ganose, C. N. Savory and D. O. Scanlon, J. Mater. Chem. A, 2017, 5, 7845.
- 57 D. Hobbs, G. Kresse and J. Hafner, Phys. Rev. B: Condens. Matter Mater. Phys., 2000, 62, 11556.
- 58 A. M. Ganose, A. J. Jackson and D. O. Scanlon, J. Open Source Softw., 2018, 3, 717.
- 59 J. R. Chelikowsky and S. G. Louie, Quantum Theory of Real Materials, Kluwer, Boston, 1996.
- 60 J. M. Ziman, Electrons and Phonons: The Theory of Transport Phenomena in Solids, Oxford Univ. Press, 2001.
- 61 G. K. H. Madsen and D. J. Singh, Comput. Phys. Commun., 2006, 175, 67.
- 62 D. Wang, L. Tang, M. Long and Z. Shuai, J. Chem. Phys., 2009, 131, 224704.
- 63 R. Chmielowski, D. Péré, C. Bera, I. Opahle, W. Xie, S. Jacob, F. Capet, P. Roussel, A. Weidenkaff, G. K. H. Madsen and G. Dennler, J. Appl. Phys., 2015, 117, 125103.
- 64 H. Shi, D. Parker, M.-H. Du and D. J. Singh, Phys. Rev. Appl., 2015, 3, 014004.
- 65 A. Togo, F. Oba and I. Tanaka, Phys. Rev. B: Condens. Matter Mater. Phys., 2008, 78, 134106.
- 66 A. Togo and I. Tanaka, Scr. Mater., 2015, 108, 1.
- 67 A. Togo, L. Chaput and I. Tanaka, Phys. Rev. B: Condens. Matter Mater. Phys., 2015, 91, 094306.
- 68 K. Parlinski, Z. Q. Li and Y. Kawazoe, Phys. Rev. Lett., 1997, 78, 4063.
- 69 G. Kresse, J. Furthmüller and J. Hafner, Europhys. Lett., 1995, 32, 729.
- 70 A. H. Romero, M. Cardona, R. K. Kremer, R. Lauck, G. Siegle, J. Serrano and X. C. Gonze, Phys. Rev. B: Condens. Matter Mater. Phys., 2008, 78, 224302. **Faper**

6. F. Sterlinds, P. A. Arrent, J.C. Wolch, D. C. Stellom and 67 A. Trgp., I. Chapter stoff. Published on 21 July 2020. No. 10 Creative SARTICLE. A Creative SARTICLE IS an access Article is licensed under a Creativ
	- 71 A. H. Macdonald, S. H. Voskot and P. T. Coleridges, J. Phys. C: Solid State Phys., 1979, 12, 2991.
	- 72 P. E. Blochl, O. Jepsen and O. K. Andersen, Phys. Rev. B: Condens. Matter Mater. Phys., 1994, 49, 16223.
	- 73 T. Tadano, Y. Gohda and S. Tsuneyuki, J. Phys.: Condens. Matter, 2014, 26, 225402.
	- 74 A. Walsh, D. J. Payne, R. G. Egdell and G. W. Watson, Chem. Soc. Rev., 2011, 40, 4455.
	- 75 A. Walsh, G. W. Watson, D. J. Payne, G. Atkinson and R. G. Egdell, J. Mater. Chem., 2006, 16, 3452.
	- 76 A. J. Jackson, A. M. Ganose, A. Regoutz, R. G. Egdell and D. O. Scanlon, *J. Open Source Softw.*, 2018, 3, 773.
	- 77 U. Gelius and K. Siegbahn, Faraday Discuss. Chem. Soc., 1972, 54, 257.
	- 78 J. J. Yeh and I. Lindau, At. Data Nucl. Data Tables, 1985, 32, 1.
	- 79 B. Van Zeghbroeck, Principles of Semiconductor Devices, University of Colorado, Boulder CO, 2004.
	- 80 D. O. Scanlon and G. W. Watson, J. Mater. Chem., 2012, 22, 25236.
	- 81 D. O. Scanlon, Phys. Rev. B: Condens. Matter Mater. Phys., 2013, 87, 161201.
	- 82 A. E. Maughan, A. M. Ganose, M. M. Bordelon, E. M. Miller, D. O. Scanlon and J. R. Neilson, J. Am. Chem. Soc., 2016, 138, 44.
	- 83 A. M. Ganose and D. O. Scanlon, J. Mater. Chem. C, 2016, 4, 1467.
	- 84 M. Ohtaki, K. Araki and K. Yamamoto, J. Electron. Mater., 2009, 38, 1234.
	- 85 R. Tian, R. Donelson, C. D. Ling, P. E. R. Blanchard, T. Zhang, D. Chu, T. Teck Tan and S. Li, J. Phys. Chem. C, 2013, 117, 13382.
	- 86 L.-D. Zhao, S.-H. Lo, Y. Zhang, H. Sun, G. Tan, C. Uher, C. Wolverton, V. P. Dravid and M. G. Kanatzidis, Nature, 2014, 508, 373.
	- 87 A. A. El-Sharkawy, A. M. Abou Ei-Azm, M. I. Kenawy, A. S. Hillal and H. M. Abu-Basha, Int. J. Thermophys., 1983, 4, 261.
	- 88 G. A. Akhmedova and D. S. Abdinov, Inorg. Mater., 2009, 45, 854.
	- 89 J. M. Skelton, S. C. Parker, A. Togo, I. Tanaka and A. Walsh, Phys. Rev. B: Condens. Matter Mater. Phys., 2014, 89, 205203.
	- 90 L. D. Whalley, J. M. Skelton, J. M. Frost and A. Walsh, Phys. Rev. B, 2016, 94, 220301.
	- 91 A. Gold-Parker, P. M. Gehring, J. M. Skelton, I. C. Smith, D. Parshall, J. M. Frost, H. I. Karunadasa, A. Walsh and M. F. Toney, Proc. Natl. Acad. Sci. U. S. A., 2018, 115, 11905.

- 92 J. Carrete, N. Mingo and S. Curtarolo, Appl. Phys. Lett., 2014, 105, 101907.
- 93 K. Biswas, J. He, I. D. Blum, C.-I. Wu, T. P. Hogan, D. N. Seidman, V. P. Dravid and M. G. Kanatzidis, Nature, 2012, 489, 414.
- 94 G. Tan, L.-D. Zhao and M. G. Kanatzidis, Chem. Rev., 2016, 116, 12123.
- 95 W. Kim, J. Zide, A. Gossard, D. Klenov, S. Stemmer, A. Shakouri and A. Majumdar, Phys. Rev. Lett., 2006, 96, 045901.
- 96 Y. L. Pei and Y. Liu, J. Alloys Compd., 2012, 514, 40.
- 97 K. F. Hsu, S. Loo, F. Guo, W. Chen, J. S. Dyck, C. Uher, T. Hogan, E. K. Polychroniadis and M. G. Kanatzidis, Science, 2004, 303, 818.
- 98 C. E. Carlton, R. De Armas, J. Ma, A. F. May, O. Delaire and Y. Shao-Horn, J. Appl. Phys., 2014, 115, 144903.
- 99 C. Hanmer and S. Abram, Energy Res. Soc. Sci., 2017, 34, 176.
- 100 Department for Energy and Climate Change (DECC), Emissions from Heat: Statistical Summary, 2012, https:// www.gov.uk/government/uploads/system/uploads/ attachment_data/file/140095/4093-emissions-heatstatistical-summary.pdf. **Journal of Materials Chemistry Article . Attribution Access Article 2020.** The Research on 22 Article is an an Access Article is article is an a Material Commons Article. Published under Access Article is licensed under A
	- 101 D. M. Rowe, CRC Handbook of Thermoelectrics, CRC Press, Boca Raton, 1995.
	- 102 B. Poudel, Q. Hao, Y. Ma, Y. Lan, A. Minnich, B. Yu, X. Yan, D. Wang, A. Muto, D. Vashaee, X. Chen, J. Liu, M. S. Dresselhaus, G. Chen and Z. Ren, Science, 2008, 320, 634.
	- 103 R. J. Mehta, Y. Zhang, C. Karthik, B. Singh, R. W. Siegel, T. Borca-Tasciuc and G. Ramanath, Nat. Mater., 2012, 11, 233.
	- 104 M. Hong, Z. G. Chen, L. Yang and J. Zou, Nano Energy, 2016, 20, 144.
	- 105 J.-L. Mi, N. Lock, T. Sun, M. Christensen, M. Søndergaard, P. Hald, H. H. Hng, J. Ma and B. B. Iversen, ACS Nano, 2010, 4, 2523.
	- 106 L. Yang, Z.-G. Chen, M. Hong, G. Han and J. Zou, ACS Appl. Mater. Interfaces, 2015, 7, 23694.
	- 107 D.-Y. Chung, T. P. Hogan, M. Rocci-Lane, P. Brazis, J. R. Ireland, C. R. Kannewurf, M. Bastea, C. Uher and M. G. Kanatzidis, J. Am. Chem. Soc., 2004, 126, 6414.
	- 108 J. Mao, H. Zhu, Z. Ding, Z. Liu, G. A. Gamage, G. Chen and Z. Ren, Science, 2019, 365, 495.