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Combined treatment of phonon scattering by electrons and point defects explains the thermal conductivity reduction in highly-doped Si

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The mechanisms causing the reduction in lattice thermal conductivity in highly P- and B-doped Si are looked into in detail. Scattering rates of phonons by point defects, as well as by electrons, are calculated from first principles. Lattice thermal conductivities are calculated considering these scattering mechanisms both individually and together. It is found that at low carrier concentrations and temperatures phonon scattering by electrons is dominant and can reproduce the experimental thermal conductivity reduction. However, at higher doping concentrations the scattering rates of phonons by point defects dominate the ones by electrons except for the lowest phonon frequencies. Consequently, phonon scattering by point defects contributes substantially to the thermal conductivity reduction in Si at defect concentrations above 10^{19} cm^{-3} even at room temperature. Only when, phonon scattering by both point defects and electrons are taken into account, excellent agreement is obtained with the experimental values at all temperatures.

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1 Introduction

With the characteristic lengths of nanoscale devices approaching the mean free paths of the heat-carrying phonons,¹ the need for a detailed and predictive understanding of thermal conductivity is more stark today than ever. In the last few decades, the usage of highly doped (10^{19} – 10^{21} cm^{-3}) semiconductor materials in electronics and energy devices has become prevalent, serving the purpose of achieving enhanced functional properties.² For these systems, predictive models are especially important because the increased phonon scattering due to point defects and additional charge carriers can result in a substantial drop in thermal conductivity.

Owing to its high abundance, non-toxicity, and ease of dopability, Si continues to be the linchpin of the semiconductor industry. Highly P- and B-doped Si are routinely used as source/drain materials in transistors to avoid unwanted Schottky junctions.³ Furthermore, highly-doped Si has also found usage in photovoltaics,⁴ microelectromechanical systems,⁵ and microelectronics,^{6,7} to cite a few applications. In thermoelectric applications the advantage of using highly-doped Si is twofold:^{8–10} the thermoelectric figure of merit is, on the one hand, proportional to the electronic power factor, which increases with increasing carrier concentration, and, on the

other, inversely proportional to the thermal conductivity. A recent advancement in the synthesis of such highly-doped systems was achieved by Rohani *et al.*,¹¹ who were able to dope Si nanoparticles with boron beyond its equilibrium solubility limit.

The lattice contribution to the thermal conductivity (κ_{ℓ}) dominates in Si. Phonon scattering by point defects (PDPS) and by electrons (EPS), were identified as the two main contributors to the κ_{ℓ} reduction in highly-doped Si.^{9,10,12,13} Zhu *et al.*¹⁰ reported a $\approx 36\%$ reduction in κ_{ℓ} in fine-grained, highly P-doped Si, and asserted that EPS is the major contributor to the κ_{ℓ} reduction. In contrast, Ohishi *et al.*⁹ attributed the κ_{ℓ} reduction in single-crystal, highly P- and B-doped Si solely to intrinsic anharmonic phonon–phonon scattering and PDPS.

The aforementioned disagreement highlights the problem in studying thermal transport when employing fitted models based on strongly-simplified assumptions about the underlying phonon band structures and scattering mechanisms. Important progress towards a more predictive treatment of κ_{ℓ} in doped Si was made recently by Liao *et al.*,¹³ who performed an *ab initio* study of n- and p-doped Si and showed that, EPS at a carrier concentration of $p \approx 10^{21} \text{ cm}^{-3}$ can result in a $\approx 45\%$ reduction in κ_{ℓ} at room temperature. The calculations reproduce how κ_{ℓ} is lower in p-doped samples than in n-doped ones, in agreement with the experiments.^{14,15} However, they do not capture the magnitude of the reduction observed in B-doped p-type single-crystal Si, which at a doping level of $5 \times 10^{20} \text{ cm}^{-3}$ amounts to more than 70%.¹⁴

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In the present work, we investigate the precise mechanisms responsible for the κ_ℓ reduction observed in highly-doped Si. We calculate κ_ℓ by employing the Boltzmann transport equation (BTE) for phonons, using only inputs in the form of interatomic force constants (IFCs) and electron-phonon coupling (EPC) matrix elements obtained from density functional theory. We extend the earlier work on EPS¹³ and include also the PDPS from first principles. At high defect concentrations, we find that the PDPS rates dominate the EPS rates at all frequencies except the lowest ones and contribute substantially to the κ_ℓ reduction at all temperatures. On the other hand, EPS dominates at low defect concentrations due to a fundamentally different frequency and concentration dependence. As a result, a correct quantitative prediction of the κ_ℓ dependence on defect concentration and temperature is obtained only when both EPS and PDPS are taken into account.

2 Methodology

Within the relaxation-time approximation, the lattice thermal conductivity tensor can be expressed as^{16,17}

$$\kappa_\ell^{\alpha\beta} = \frac{1}{k_B T^2 V_{uc}} \sum_{i\mathbf{q}} n_{i\mathbf{q}}^0 (n_{i\mathbf{q}}^0 + 1) (\hbar\omega_{i\mathbf{q}})^2 v_{i\mathbf{q}}^\alpha v_{i\mathbf{q}}^\beta \tau_{i\mathbf{q}}^0, \quad (1)$$

where α and β run over the Cartesian axes, k_B is the Boltzmann constant, V_{uc} is the unit cell volume, $n_{i\mathbf{q}}^0$, $v_{i\mathbf{q}}^\alpha$, and $\omega_{i\mathbf{q}}$ are the Bose-Einstein occupancy, the group velocity, and the angular frequency of a phonon mode with wave-vector \mathbf{q} and branch index i , respectively. $\tau_{i\mathbf{q}}^0$ represents the relaxation time of mode $i\mathbf{q}$ and is obtained as:

$$\frac{1}{\tau_{i\mathbf{q}}^0} = \frac{1}{\tau_{i\mathbf{q}}^{3ph}} + \frac{1}{\tau_{i\mathbf{q}}^{iso}} + \frac{1}{\tau_{i\mathbf{q}}^{pd}} + \frac{1}{\tau_{i\mathbf{q}}^{ep}}, \quad (2)$$

where the lifetime of a phonon of mode $i\mathbf{q}$ as limited by the scattering caused by: the three-phonon processes is given by $\tau_{i\mathbf{q}}^{3ph}$, the mass disorder due to isotopes by $\tau_{i\mathbf{q}}^{iso}$, the point defects by $\tau_{i\mathbf{q}}^{pd}$, and the electrons by $\tau_{i\mathbf{q}}^{ep}$. The expressions for the phonon scattering by three-phonon processes and isotopes can be found in ref. 16.

2.1 Point-defect phonon scattering

The phonon scattering rates by point defects, $1/\tau_{i\mathbf{q}}^{pd}$, can be calculated as:¹⁸

$$\frac{1}{\tau_{i\mathbf{q}}^{pd}} = -n_{def} V_{uc} \frac{1}{\omega_{i\mathbf{q}}} \text{Im} \{ \mathbf{e}_{i\mathbf{q}}^\dagger \mathbf{T} \mathbf{e}_{i\mathbf{q}} \}, \quad (3)$$

where n_{def} is the volumetric concentration of the point defects and $\mathbf{e}_{i\mathbf{q}}$ represents an incoming phonon mode. \mathbf{T} is the matrix that relates the Green's function of the perturbed lattice to that of the unperturbed lattice. It can be represented in terms of the retarded Green's functions of the unperturbed host lattice, \mathbf{g}^+ , and the perturbation \mathbf{V} as:¹⁹

$$\mathbf{T} = (\mathbf{1} - \mathbf{V} \mathbf{g}^+)^{-1} \mathbf{V}. \quad (4)$$

The matrix element of \mathbf{g}^+ projected on the atom pairs $l\eta$ and $l'\eta'$ is given as:¹⁹

$$\mathbf{g}^+_{l\eta, l'\eta'} = \lim_{\varepsilon \rightarrow 0^+} \sum_{i\mathbf{q}} \frac{\mathbf{e}_{i\mathbf{q}}(l\eta) \mathbf{e}_{i\mathbf{q}}^\dagger(l'\eta')}{\omega^2 + i\varepsilon - \omega_{i\mathbf{q}}^2}, \quad (5)$$

where, $\mathbf{e}_{i\mathbf{q}}(l\eta)$ is the eigenvector of mode $i\mathbf{q}$ projected on the η -th atom in the l -th unit cell. Moreover,

$$\mathbf{V} = \mathbf{V}_M + \mathbf{V}_K, \quad (6)$$

where \mathbf{V}_M and \mathbf{V}_K are the mass and IFC perturbation matrices, respectively. Their matrix elements are given by:

$$V_{M; l\eta, l'\eta'} = \frac{M_{l\eta, l'\eta'} - M_{0; l\eta, l'\eta'}}{M_{0; l\eta, l'\eta'}} \omega_{i\mathbf{q}}^2, \text{ and} \quad (7)$$

$$V_{K; l\eta, l'\eta'}^{\alpha\beta} = -\frac{\Phi_{l\eta, l'\eta'}^{\alpha\beta} - \Phi_{0; l\eta, l'\eta'}^{\alpha\beta}}{\sqrt{M_{l\eta} M_{l'\eta'}}},$$

where M is the mass of the defect atom which replaces a host atom of mass M_0 at site $l\eta$. Φ and Φ_0 are the IFC matrices of the defect-laden and host systems, respectively.

2.2 Electron-phonon scattering

The phonon scattering rates by electrons can be expressed as:^{13,20}

$$\frac{1}{\tau_{i\mathbf{q}}^{ep}} = \frac{2\pi}{\hbar} \sum_{mn, \mathbf{k}} |\phi_{mn}^i(\mathbf{k}, \mathbf{q})|^2 (f_{m\mathbf{k}+\mathbf{q}} - f_{n\mathbf{k}}) \times \delta(\varepsilon_{n\mathbf{k}} - \varepsilon_{m\mathbf{k}+\mathbf{q}} - \hbar\omega_{i\mathbf{q}}), \quad (8)$$

where $\phi_{mn}^i(\mathbf{k}, \mathbf{q})$ is the EPC matrix element of an interaction process involving a given phonon $i\mathbf{q}$ and two charge carriers with band indices m and n and wave-vectors \mathbf{k} and $\mathbf{k} + \mathbf{q}$, respectively. $f_{n\mathbf{k}}$ is the Fermi-Dirac distribution function and $\varepsilon_{n\mathbf{k}}$ is the eigenenergy of an electron state $n\mathbf{k}$. In non-spin-orbital-coupling or non-magnetic calculations, the formula above must be multiplied by a factor of two to take the electron spin degeneracy into account.

The EPC matrix element can be computed within density functional perturbation theory as:²¹

$$\phi_{mn}^i(\mathbf{k}, \mathbf{q}) = \sqrt{\frac{\hbar}{2\omega_{i\mathbf{q}}}} \sum_{\eta\alpha} \frac{\mathbf{e}_{i\mathbf{q}}^\alpha(0\eta)}{\sqrt{M_{0\eta}}} \left\langle m\mathbf{k} + \mathbf{q} \left| \frac{\partial V_{KS}(\mathbf{r})}{\partial u_{i\mathbf{q}}^\alpha(0\eta)} \right| n\mathbf{k} \right\rangle \quad (9)$$

where $M_{0\eta}$ is the atomic mass of the η -th atom in the unit cell, α is the Cartesian direction, and $\partial V_{KS}(\mathbf{r})/\partial u_{i\mathbf{q}}^\alpha(0\eta)$ is the perturbation of the Kohn-Sham potential with respect to the displacement $u_{i\mathbf{q}}^\alpha(0\eta)$.

3 Computational details

For calculating the PDPS rates, the total energy as well as the force calculations are carried out using the projector-augmented-wave method²² as implemented in the VASP code,^{23–25} within the local density approximation (LDA)^{26,27} to the exchange and correlation energy. For completeness and comparison to LDA we also calculate the PDPS rates with the Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional.²⁸ The volume of the unit cell is



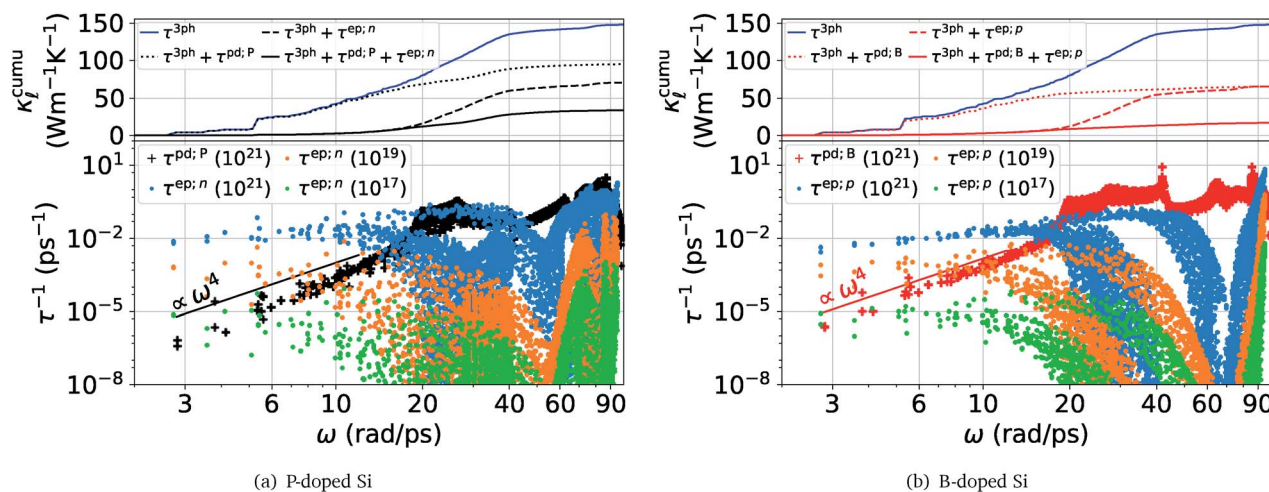


Fig. 1 The bottom panels in figures (a) and (b) show the EPS (dots) and PDPS (+signs) rates for P(n)- and B(p)-doped Si, respectively. PDPS rates are shown at a doping concentration of 10^{21} cm^{-3} and the EPS rates are shown for three different carrier concentrations at 300 K. The top panels in the figures show the cumulative κ_f at 300 K and at a defect concentration of 10^{21} cm^{-3} . In all the κ_f calculations reported in these and later figures, the phonon scattering caused by the mass disorder due to isotopes, τ^{iso} , is also considered by default.

relaxed until the energy is converged within 10^{-8} eV. The 2nd- and 3rd-order IFCs are extracted using $5 \times 5 \times 5$ supercell of the rhombohedral primitive cell containing 250 atoms using just the Γ -point. For the 2nd-order IFC calculations we use the Phonopy²⁹ software package and for the 3rd-order IFCs we use THIRDORDER.PY from the ShengBTE package.¹⁶ The same supercell size was used to calculate the IFCs for the defect-laden structures. To compute the PDPS rates, the Green's functions are calculated on a $38 \times 38 \times 38$ q -point mesh using the linear tetrahedron method³⁰ for integration over the Brillouin zone. The scattering rates are then calculated on $35 \times 35 \times 35$ q -point mesh.

For the calculation of EPS rates, the EPC matrix elements are first computed on coarse grids and then interpolated to dense grids with the Wannier function interpolation method.^{31,32} The interpolations are performed using Quantum Espresso³³ and the built-in EPW package³⁴ with norm-conserving pseudopotentials. Likewise, both the LDA and PBE exchange and correlation functionals are considered. The initial \mathbf{k} and \mathbf{q} grids are both $6 \times 6 \times 6$, which are interpolated to $35 \times 35 \times 35$ meshes needed for the thermal conductivity calculations. The energy conservation δ -function is treated by Gaussian function with self-adaptive broadening parameters.²¹

Finally, the bulk thermal conductivity is also calculated using the $35 \times 35 \times 35$ q -point mesh with the ALMABTE³⁵ package. Due to the dense \mathbf{q} -mesh the thermal conductivity is converged down to 40 K.

4 Results and discussion

Fig. 1 shows a comparison between the PDPS and EPS rates for both n- and p-doped Si, in the bottom panels. The PDPS depends on the actual defect type present in the system. We have studied the substitutional $\text{B}_{\text{Si}}^{(-1)}$ and $\text{P}_{\text{Si}}^{(+1)}$ defects, which are the most common doping elements and also those studied experimentally. The PDPS has a trivial dependence on the defect

concentration [eqn (3)] and is shown for only one defect concentration (10^{21} cm^{-3}). In a rigid band approximation, the EPS is dependent only on the carrier concentration through the distribution function in eqn (8). The EPS is shown for three different carrier concentrations in Fig. 1 and the corresponding chemical potentials are shown in Fig. 2 (inset). Our LDA EPS rates compare well with the PBE rates reported by Liao *et al.*¹³ The LDA rates are slightly higher than the PBE ones which results in a correspondingly higher κ_f reduction due to EPS in LDA as compared to PBE. However, this does not have any major effect on the interpretation of our results.

If we first consider the low frequency ($\omega < 12 \text{ rad ps}^{-1}$) behavior, the PDPS rates exhibit a simple Rayleigh ω^4 behavior and the EPS rates for a given carrier concentration are close to being independent of ω . Plotting the EPS rates as a function of

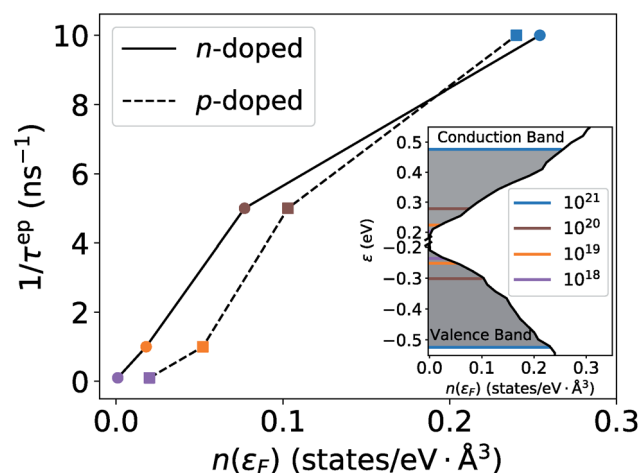


Fig. 2 The low-frequency EPS rates for different concentrations as a function of the electronic density of states. The marker colors correspond to the doping levels in the inset.



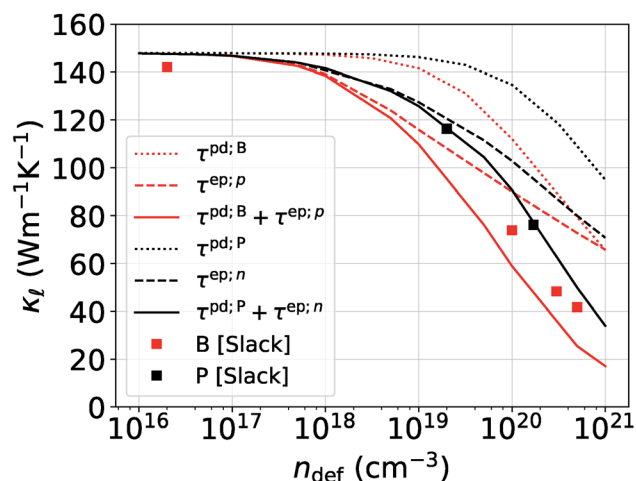


Fig. 3 Comparison of the reduction in κ_{ℓ} caused by EPS and PDPS individually and combined together vs. increasing doping concentration. The filled squares are from the experimental data in ref. 14.

the electronic density of states (DOS), obtained at the electron chemical potential corresponding to a given doping concentration, shows an almost linear dependence (Fig. 2). The EPS rates thus behave in accordance with a simple $\tau^{-1} \propto n(\epsilon)$ model³⁶ at low frequencies. With a $n(\epsilon) \propto \epsilon^{1/2}$ behavior of the electronic DOS, the low-frequency EPS rates will scale approximately as $n_{\text{def}}^{1/3}$ with the carrier/defect concentration as opposed to the linear scaling of the PDPS rates evident from eqn (3). These simple relations are in accordance with the expectation that EPS will dominate over PDPS at low temperatures and defect concentrations while PDPS will become increasingly important at high defect concentrations.

At the same time, it is clear from Fig. 1 that for $\omega > 12$ rad ps^{-1} the calculated rates deviate substantially from the aforementioned simple relations. The cumulative κ_{ℓ} plots in the

respective top panels in Fig. 1 (blue curves) illustrate that modes with $\omega > 12$ rad ps^{-1} carry about two-thirds of the heat at 300 K. Simply extrapolating the low frequency behavior would lead to a strong overestimation of the scattering. This is especially so for the EPS rates where a simple extrapolation would result in a strong overestimation of the predicted κ_{ℓ} suppression. The cumulative plots in the top panels of Fig. 1 also show for PDPS (dotted lines), at a large defect concentration, that the contribution to κ_{ℓ} for frequencies higher than 20 rad ps^{-1} is only $\approx 15\%$ in case of $\text{B}_{\text{Si}}^{(-1)}$ defect and $\approx 40\%$ in case of $\text{P}_{\text{Si}}^{(+1)}$. In contrast, the EPS causes a majority reduction in κ_{ℓ} by frequencies below 20 rad ps^{-1} , for both P- and B-doping.

Next, in Fig. 3, we look into the individual contributions from the EPS (dashed lines) and PDPS (dotted lines) to the room temperature thermal conductivity reduction for increasing doping concentrations and compare them to the experimental κ_{ℓ} data from Slack.¹⁴ In accordance with the analysis of the scattering rates, EPS dominates the reduction of κ_{ℓ} at low carrier concentrations. In the case of n-doped Si, EPS alone is almost enough to explain the experimental point at $2 \times 10^{19} \text{ cm}^{-3}$. However, at higher carrier concentrations, EPS alone clearly underestimates both the absolute reduction of κ_{ℓ} and the trend. Interestingly, PDPS captures the trend correctly for large defect concentrations, but also underestimates the absolute κ_{ℓ} reduction. At a doping concentration of 10^{21} cm^{-3} , the EPS and PDPS contribute almost equally in κ_{ℓ} reduction for B doping. Even though both EPS and PDPS contribute substantially to κ_{ℓ} reduction in Si, neither can explain the absolute reduction in κ_{ℓ} on its own. Only when both are taken into consideration in eqn (2) is the experimentally observed reduction of κ_{ℓ} reproduced. This is shown by the black and red solid lines in Fig. 3. Apart from a slight underestimation of κ_{ℓ} in case of B-doping, the calculated value of κ_{ℓ} considering both EPS and PDPS agree very well with the experimental values available for concentrations $\sim 10^{19}$ – 10^{21} cm^{-3} both in value and trend, Fig. 3.

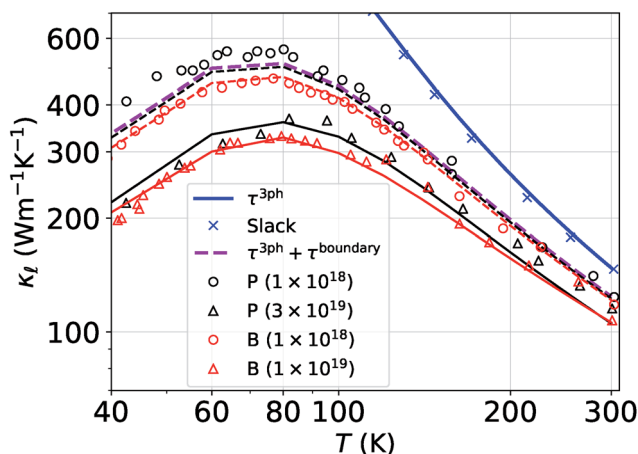


Fig. 4 κ_{ℓ} vs. temperature curves for the B(red)- and P(black)-doped Si considering the three-phonon, PDPS, EPS, and boundary scattering (at 10 μm). The open triangles and circles are the experimental data obtained from ref. 15. The solid and dashed (black and red) lines correspond to the calculations done at experimental carrier concentrations.

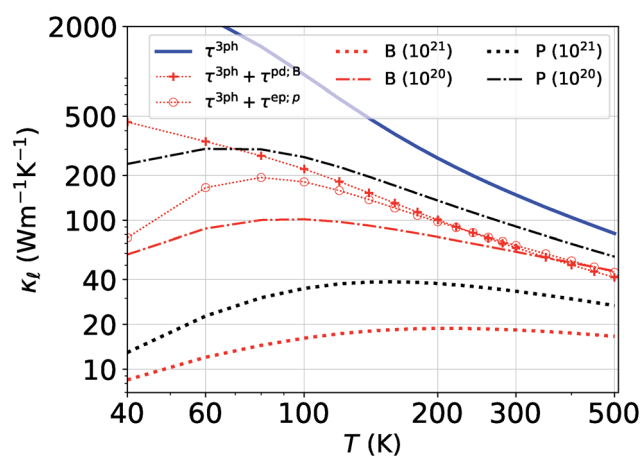


Fig. 5 Prediction of κ_{ℓ} for highly P- and B-doped Si. Also shown is the comparison of EPS and PDPS to κ_{ℓ} reduction considered at a concentration of 10^{21} cm^{-3} .



Besides the work of Slack *et al.*¹⁴ used for Fig. 3, there is a general lack of systematic experimental data on the thermal conductivity of single-crystal Si with varying doping concentrations. In order to gain further confidence in our results, we compare them to the more recent experimental data from ref. 15, which were measured on single-crystal Si films. Even at low defect concentrations, $n_{\text{def}} = 10^{17}\text{--}10^{18}\text{ cm}^{-3}$, these samples exhibit a substantially lower κ_{ℓ} than the bulk samples.¹⁵ However, a good agreement with the experimental curves can be obtained by adding a simple boundary scattering term, $1/\tau_{\text{iq}}^{\text{B}} = |\mathbf{v}_{\text{iq}}|/L$ with $L = 10\text{ }\mu\text{m}$, to eqn (2) to emulate the effect of a film, as seen in Fig. 4 (purple line). Adding now the effect of the PDPS and EPS, we calculate the variation of κ_{ℓ} as a function of temperature for both B- and P-doped Si films, shown in Fig. 4. For B-doping, when we include the PDPS and EPS along with the boundary scattering, we see that there is only a slight reduction from the purple line for the 10^{18} cm^{-3} doping level (dashed red lines). Nevertheless, this results in an excellent agreement with the experimental data at that concentration (red circles), throughout the temperature range. Keeping the boundary scattering constant, when the doping concentration is increased to 10^{19} cm^{-3} , a large reduction in κ_{ℓ} is observed (solid red line) which also agrees well with the experimental data (red circles). Similarly, for the P-doped calculations, we obtain an excellent agreement with the experiments except for a slight underestimation in κ_{ℓ} at temperatures below 80 K for 10^{18} cm^{-3} doped case. However, this is still under the uncertainties in experimental data.

We then make predictions for the highly-doped cases (10^{20} and 10^{21} cm^{-3}) as there is no experimental thermal conductivity data available for such high doping levels. These are shown in Fig. 5. At room temperature, we find more than 60% reduction as compared to the bulk value at 10^{20} cm^{-3} doping level and 90% at 10^{21} cm^{-3} for B doping, and 40% and 80% for P doping, respectively. Fig. 5 also shows the individual contributions to the κ_{ℓ} reduction by EPS and PDPS in the case of B doping at a doping concentration of 10^{21} cm^{-3} , revealing their characteristic effects on the thermal conductivity over the temperature range. The reduction in κ_{ℓ} caused by PDPS overtakes the one by EPS at $\approx 250\text{ K}$. This behavior highlights the importance of PDPS at high doping concentrations in Si and also emphasizes that, at temperatures higher than 300 K, PDPS is the most dominant scattering mechanism besides the intrinsic anharmonic scattering. We have also performed calculations including an $L = 10\text{ }\mu\text{m}$ boundary scattering term, however at such high doping concentrations the EPS and PDPS dominate the boundary scattering throughout the temperature range and only a small effect at very low temperatures was found on the calculated κ_{ℓ} . This observation is also in agreement with Fu *et al.*³⁷ who observed significant contribution of EPS towards room-temperature κ_{ℓ} reduction in highly-doped Si nanowires of 1 μm diameter.

It is important to note how the present case is very different from our previous work on SiC.^{38,39} In the present work, we observe a significant contribution of both EPS and PDPS to κ_{ℓ} of a highly-doped system; whereas in our previous work we observed that PDPS was sufficient on its own to correctly predict

the κ_{ℓ} of B-doped cubic SiC owing to the resonant phonon scattering that boron causes.^{38,39} The resonant scattering was at least one to two orders of magnitude higher than that caused by other defects and resulted in a drastic reduction (approximately two orders of magnitude at room temperature) in the thermal conductivity even at relatively modest defect concentrations ($\approx 10^{20}\text{ cm}^{-3}$). Boron does not cause resonant scattering in Si and therefore the contribution of both EPS and PDPS are comparable.

5 Conclusions

We have calculated the *ab initio* lattice thermal conductivity of highly P- and B-doped Si considering phonon scattering caused by three phonon processes, isotopes, point defects, and electrons. We illustrate that at low doping concentrations EPS causes a higher reduction in κ_{ℓ} as compared to PDPS owing to a near constant behavior of EPS rates at low frequencies. At low concentrations EPS alone is sufficient to reproduce the absolute reduction in κ_{ℓ} . However, at high doping concentrations it fails to reproduce the absolute values and the trend of κ_{ℓ} reduction. PDPS has a substantial contribution to κ_{ℓ} reduction at high doping concentrations and neither EPS nor PDPS is sufficient on its own to reproduce the experimental κ_{ℓ} values. Only when the effect of all the scattering mechanisms are considered together, we get a good agreement with the experimental values across the temperature range. At a doping concentration of 10^{21} cm^{-3} , we observe almost 90% reduction in the room temperature thermal conductivity of B-doped Si as compared to the bulk, whereas, 80% reduction in case of P doping is found. This is mainly because of the higher PDPS rates of the B defects than those of P defects. Neither EPS nor PDPS can be captured by conventional parameterized models. Together with our previous works on doping diamond, SiC, GaN and GaAs,^{38,40–42} we show that, at temperatures above 300 K, PDPS is the most dominant scattering mechanism in highly B- and P-doped Si and cannot be neglected.

Conflicts of interest

There are no conflicts of interest to declare.

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