



Cite this: *Sustainable Energy Fuels*, 2020, **4**, 2363

## Two-dimensional boron monochalcogenide monolayer for thermoelectric material†

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Monochalcogenide materials have outstanding potential for thermoelectric applications. In this paper, we have investigated the electronic structure, vibrational and transport properties of boron chalcogenide BX (X = S, Se, Te) materials. Electronic structure calculations show that each material has an indirect bandgap in the range of 2.92 eV to 1.53 eV. The presence of positive phonon frequencies shows the dynamic stability of the materials. We also calculated the mobility ( $m$ ) and relaxation time ( $t$ ) of all the materials. Additionally, as the 2D boron monochalcogenide BX (X = S, Se, Te) materials have superior carrier mobility, they have a small effective mass of electrons. The 1T and 2H phases of the BS monolayer have superior electron carrier mobilities of 11 903.07 and 11 651.61  $\text{cm}^2 \text{V}^{-1} \text{s}^{-1}$ . We also found that for the low and mid-temperature range (200–450 K), all the materials have a high electronic figure of merit  $ZT_e$  nearly equal to 1, with the exception of the BS 2H phase. The BSe 1T phase has high  $ZT_e = 1.022$ , which is the maximum across all the materials. These theoretical investigations suggest that boron monochalcogenide BX (X = S, Se, Te) materials have promise for applications in high-performance thermoelectrics.

Received 1st January 2020  
Accepted 25th February 2020

DOI: 10.1039/d0se00004c  
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## 1 Introduction

The conversion of waste heat into electricity could play a significant role in the recent challenge of developing alternative energy technologies to reduce the reliance on fossil fuels and emission of greenhouse gases.<sup>1</sup> However, the applicability of alternative energy technologies is limited by conditions such as the availability and durability of materials, cost and toxicity of components. It is possible to use thermoelectric materials to directly transform heat into electricity and *vice versa*. Thermoelectric (TE) materials have become increasingly important in the previous few decades because of their capability to overcome energy problems.<sup>2–4</sup> Some typical applications involving new thermoelectric materials include biothermal batteries to power cardiac pacemakers, and optoelectronics with increased efficiency combined with solid-state thermoelectric cooling to provide power to several spacecraft launched by NASA for deep-space missions.<sup>5</sup> Now thermoelectric materials are also actively utilized for a range of new applications such as the

transformation of automotive radiator heat to electricity, thermal powered night vision systems, electric refrigeration cages, coolers for diode lasers and some low voltage power generators.<sup>6</sup> The efficiency of thermoelectric materials is identified by the dimensionless figure of merit  $ZT$ .  $ZT = S^2 \sigma T / \kappa$ , where  $S$  represents the Seebeck coefficient,  $\sigma$  is the electric conductivity,  $T$  is the absolute temperature and  $\kappa$  is the thermal conductivity. The thermal conductivity  $\kappa$  contains both lattice and electronic parts, where  $\kappa = \kappa_l + \kappa_e$ .  $\kappa_l$  is the lattice thermal conductivity relative to lattice vibrations (phonons) and  $\kappa_e$  is the electronic thermal conductivity related to electronic structure. Over the last several years intensive work has been done to increase  $ZT$  for high thermoelectric performance.<sup>3,7,8</sup> To attain better thermoelectric efficiency, a high Seebeck coefficient ( $S$ ) and high electric conductivity ( $\sigma$ ) are needed. Yet electric conductivity ( $\sigma$ ) and the Seebeck coefficient ( $S$ ) are generally inversely related. Therefore, to increase the thermoelectric efficiency, a balance is required between these two opposing variables. It was proposed that in a low dimensional material the electronic density of states increases close to the Fermi level, hence transport of the carrier is confined, which could increase the Seebeck coefficient ( $S$ ) without reducing the electric conductivity ( $\sigma$ ). Many other methods have been adopted by researchers to enhance the thermoelectric performance of materials, such as doping or applying strain.<sup>9–13</sup> There are various crystal structures of different materials that provide good thermoelectric performance, such as Half-Heusler compounds,<sup>14</sup> clathrates,<sup>15</sup> skutterudites,<sup>16</sup> perovskites,<sup>17</sup> anti-perovskite,<sup>18</sup> some oxide materials<sup>19,20</sup> and chalcogenides.<sup>21,22</sup>

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† Electronic supplementary information (ESI) available. See DOI: [10.1039/d0se00004c](https://doi.org/10.1039/d0se00004c)



The elements of group 16 (O, S, Se, Te) are known as chalcogens. Materials that contain at least one chalcogen atom are known as chalcogenide materials.<sup>23</sup> Chalcogenide materials have a long tradition of well-known thermoelectric uses, for which lead telluride and bismuth telluride are very famous. Bismuth telluride ( $\text{Bi}_2\text{Te}_3$ ) is used commercially for low temperature thermoelectric devices, but for high temperatures lead telluride (PbTe) is a better candidate.<sup>24</sup> Many other chalcogenides, such as di-metal chalcogenides ( $\text{AgBiSe}_2$ ),<sup>25</sup> copper chalcogenide<sup>26</sup> and tin chalcogenide<sup>27</sup> have been identified as potential thermoelectric materials. In recent years, group IIIA monochalcogenides have also attracted significant interest from materials researchers. Previous studies reported that group IIIA monochalcogenides such as  $\text{AlX}$ ,  $\text{GaX}$  and  $\text{InX}$  ( $\text{X} = \text{S}, \text{Se}, \text{Te}$ ) have superior thermoelectric efficiency.<sup>28–30</sup>

Motivated by such fascinating thermoelectric properties of group IIIA chalcogenide materials, we have investigated the thermoelectric properties of boron monochalcogenide  $\text{BX}$  ( $\text{X} = \text{S}, \text{Se}, \text{Te}$ ). Boron monochalcogenides are recently proposed materials utilizing density functional theory (DFT) which contain two phases, 1T and 2H.<sup>31</sup> We have systematically investigated the thermoelectric properties of both the 1T and 2H phases of boron monochalcogenides. This present study includes the structural, vibrational, electronic and thermoelectric properties of boron chalcogenides.

## 2 Computational methods

In this work, we used the Vienna *ab initio* simulation package (VASP) code<sup>32–34</sup> to conduct first principle density functional theory (DFT) calculations. The electron exchange-correlations were defined by generalized gradient approximation (GGA) in the context of the Perdew–Burke–Ernzenhof (PBE) functional.<sup>35</sup> An energy cut-off of 500 eV was given for plane wave expansion. We chose convergence criteria of 0.005 eV  $\text{\AA}^{-1}$  and  $10^{-6}$  eV for force and energy. For system optimization, we used a conjugate gradient method with a Brillouin zone sampled by  $19 \times 19 \times 1$   $k$ -point mesh within the Monkhorst–Pack scheme.<sup>36</sup> A vacuum of 15  $\text{\AA}$  was introduced to prevent possible interactions between the layers in the vertical direction. In order to analyze the stability of boron monochalcogenides, a bigger supercell ( $2 \times 2 \times 1$ ) was produced for calculating force constants; this was then used by Phonopy software.<sup>37</sup>

To calculate electron transport properties we used semi-classical Boltzmann theory, taking into account the relaxation time approximation and rigid band approximation implemented by BoltzTrap code.<sup>38</sup> Transport properties such as the electric conductivity ( $\sigma$ ), the electronic part of thermal conductivity ( $\kappa$ ) and the Seebeck coefficient ( $S$ ) are explained in the ESI.<sup>†</sup> The simulation is carried out with the entire first Brillouin zone, which is divided into  $25 \times 25 \times 1$   $k$ -point mesh. In order to determine electrical and thermal conductivity, the electron relaxation time  $\tau$  is usually measured by experimentally observed data or theoretical calculations.<sup>39,40</sup> For the investigations of carrier mobility, we used deformation potential theory, which explains the transport of charge in 2D materials. In order to measure the thermoelectric properties we use the electronic

figure of merit,  $ZT_e = S^2 \sigma T / \kappa_e$ , which represents the features of electron transport and gives the upper limit of total  $ZT$ . Atomic structures are shown using the VESTA package.<sup>41</sup>

## 3 Results and discussion

### 3.1 Structural stability and electronic properties

To validate the computational methodology, we first examined the structural properties of the  $\text{BX}$  ( $\text{X} = \text{S}, \text{Se}, \text{Te}$ ) 1T and 2H phase monolayers, as presented in Fig. 1 (top view and side view of structure). Table 1 shows structural parameters such as lattice constants, bond lengths, bond angles, and cohesive energies. From our calculations, it is observed that our calculated parameters are in good agreement with previous work.<sup>31</sup> Cohesive energy was calculated by using the formula given below:

$$E_{\text{cohesive}} = \frac{E_{\text{unitcell}} - mE_B - nE_X}{m + n}, \quad (1)$$

where  $E_{\text{unitcell}}$  is the total energy of the  $\text{BX}$  monolayer with  $\text{X} = \text{S}, \text{Se}$  and  $\text{Te}$ ;  $E_B$  and  $E_X$  are the energies of isolated atom B and chalcogen atoms  $\text{X} = \text{S}, \text{Se}$  and  $\text{Te}$ ;  $m$  is the number of B atoms in the unit cell; and  $n$  is the number of X atoms in the unit cell.

In order to further investigate the stability of the  $\text{BX}$  ( $\text{S}, \text{Se}, \text{Te}$ ) monolayer, phonon calculations were performed along the  $\Gamma$ – $M$ – $K$ – $\Gamma$  high symmetry directions. Fig. S1 (ESI<sup>†</sup>) shows the obtained phonon dispersion curves, which show good agreement with previous investigations.<sup>31</sup> Most of the  $\text{BX}$  monolayers are free from imaginary frequencies, except  $\text{BTe}$  (2H).  $\text{BTe}$  (2H) can be considered dynamically stable and includes very low imaginary frequencies ( $-0.224$  THz) close to  $\Gamma$ , due to numerical anomalies that would be improved if a larger supercell or increased  $k$ -points were used for calculation. Since the B atom

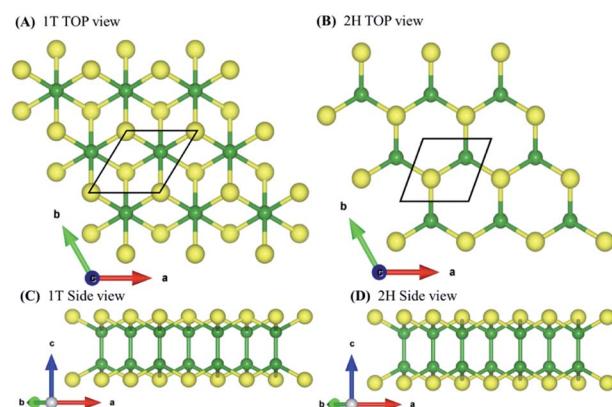


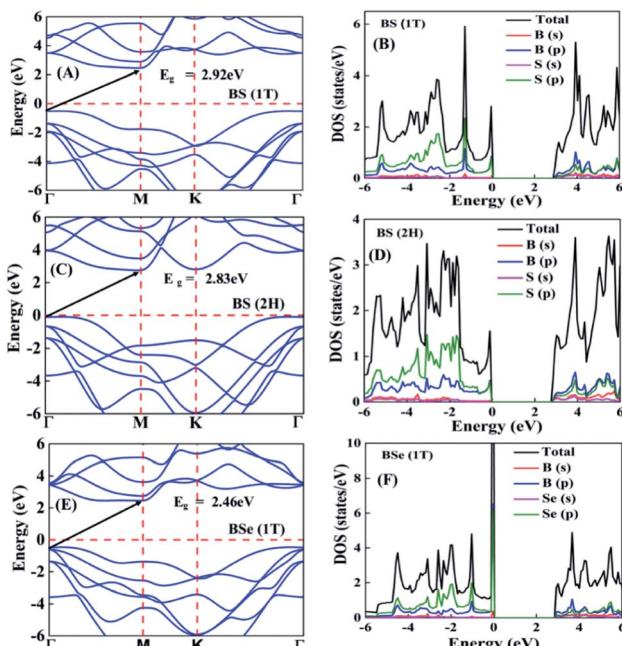
Fig. 1 (A) Top view of 1T, (B) side view of 1T phase, (C) top view of 2H, (D) side view of 2H phase. The structure shown has two buckled hexagonal layers arranged in such a way that, in the 2H configuration, boron atoms are located on boron atoms and chalcogen atoms are located at chalcogen atoms, but in the 1T configuration boron atoms are located on boron atoms and chalcogen atoms are placed at the hexagon centers. Green and yellow colors denote boron and chalcogen atoms, respectively. The black box indicates a unit cell containing four atoms.

**Table 1** The calculated lattice constant ( $a = b$ ); bond lengths  $d_{B-B}$  (Å) and  $d_{B-X}$  (Å); distance between X and X atoms  $d_{X-X}$  (Å), which is the distance between the top and bottom X atoms in the monolayer; different bond angles; and cohesive energy (eV per unit cell)

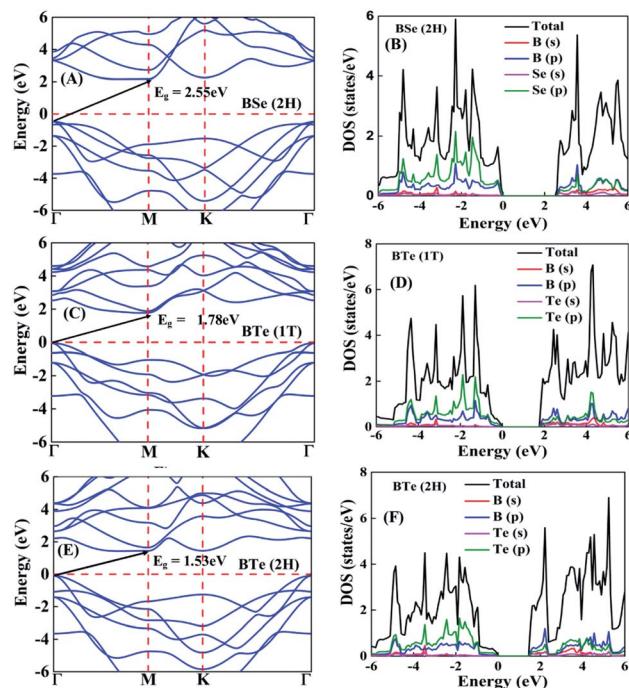
| System        | BS    |        | BSe    |        | BTe    |        |        |
|---------------|-------|--------|--------|--------|--------|--------|--------|
|               | Phase | 1T     | 2H     | 1T     | 2H     | 1T     | 2H     |
| $a$ (Å)       |       | 3.06   | 3.04   | 3.27   | 3.26   | 3.59   | 3.57   |
| $d_{B-B}$ (Å) |       | 1.70   | 1.73   | 1.69   | 1.71   | 1.68   | 1.71   |
| $d_{B-X}$ (Å) |       | 1.95   | 1.95   | 2.11   | 2.10   | 2.32   | 2.31   |
| $d_{X-X}$ (Å) |       | 3.81   | 3.43   | 4.02   | 3.61   | 4.28   | 3.83   |
| $\angle BBX$  |       | 115.45 | 115.83 | 116.22 | 116.71 | 116.51 | 117.21 |
| $\angle BXB$  |       | 102.89 | 102.44 | 101.94 | 101.34 | 101.61 | 100.74 |
| $E_{coh}$     |       | -5.79  | -5.78  | -5.24  | -5.23  | -4.72  | -4.69  |

has a lower mass, it appears to vibrate at high frequencies; hence the higher frequencies associated with optical phonons are contributed by B atoms. Chalcogen atoms contribute so much to vibrations at lower frequencies. There are two frequency gaps observed in the phonon dispersions for all the monolayers, which are due to mass differences between elements B and X (S, Se, Te) and the vibration modes. The calculated phonon dispersion curves also indicate that the 1T phase has slightly higher frequencies than the 2H phase.

The calculated electronic band structures and corresponding densities of states are shown in Fig. 2 and 3. The figures show that the considered materials, boron monochalcogenides BX ( $X = S, Se, Te$ ), are all broad indirect band gap semiconductors. In all the band structures the top of the valence band arises at



**Fig. 2** (A) Electronic band structure and (B) corresponding projected density of states of BS 1T phase. (C) Electronic band structure and (D) corresponding projected density of states of BS 2H phase. (E) Electronic band structure and (F) corresponding projected density of states of BSe 1T phase.



**Fig. 3** (A) Electronic band structure and (B) corresponding projected density of states of BSe 2H phase. (C) Electronic band structure and (D) corresponding projected density of states of BTe 1T phase. (E) Electronic band structure and (F) corresponding projected density of states of BTe 2H phase.

the high symmetry point  $\Gamma$  (0, 0, 0) and the minimum of the conduction band occurs very near to the  $M$  (0.5, 0, 0) point. The related band gap values of BS (1T), BSe (1T), and BTe (1T) are 2.92 eV, 2.46 eV, and 1.78 eV, respectively. For the 2H phase the band gaps of BS (2H), BSe (2H), and BTe (2H) are 2.83 eV, 2.55 eV, and 1.53 eV, respectively. We observed that the 2H phases have lower bandgap values in comparison with the 1T phases due to the different atomic arrangements. We also noticed that with the increasing size and weight of the chalcogen atoms, the band gap decreases, as shown in Fig. 4(a). We employed the hybrid functional HSE06 to find more accurate electronic band structures, as shown in Fig. S2 (ESI†). The electronic band gaps using HSE06 functional are BS (1T) = 4.03 eV, BS (2H) = 3.91 eV, BSe (1T) = 3.89 eV, BSe (2H) = 3.47 eV, BTe (1T) = 2.48 eV and BTe (2H) = 2.14 eV. Additionally, we calculated the electronic band structure and corresponding electronic density of states due to the presence of heavy atomic weight using PBE functional with spin-orbit coupling effect for both phases of the BTe monolayer, as depicted in Fig. S3 (ESI†). The electronic band gap is affected due to the presence of Te atoms in both the 1T and 2H phases. The computed electronic band gaps of the structure are BTe (1T):  $E_g = 1.54$  eV from 1.78 eV, and BTe (2H):  $E_g = 1.24$  eV from 1.53 eV.

To better understand the electronic structures of BX, we plot the total density of states (TDOS) and projected density of states (PDOS), which are also shown in Fig. 2 and 3. The PDOS provides detailed information about the contribution of different atomic orbitals in the valence band and conduction



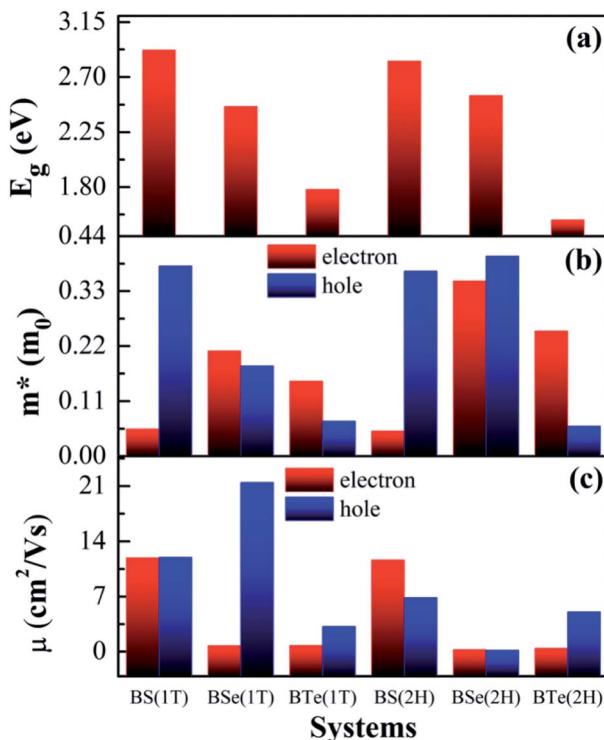


Fig. 4 Calculated electronic properties of boron monochalcogenide BX (X = S, Se, Te) monolayer showing (a) the electronic band gap, (b) effective mass of electrons and holes, and (c) carrier mobility ( $\times 10^3$ ) of electrons and holes.

band of BX (S, Se, Te). The s-orbitals of B and X atoms make a very small contribution to both the valence band and the conduction band. In the valence band away from the Fermi level, the p-orbital of the X atom is dominant over the p-orbital of B, but near the Fermi level the p-orbital of X is hybridized with the 2p-orbital of B atom. In the BS (1T), BS (2H) and BSe (1T) systems, we can see that very near to the Fermi level, the p-orbital of B has a slightly larger contribution than the p-orbitals of S and Se atoms. In the conduction band away from the Fermi level, the 2p-orbital of B is dominant over the p-orbital of X. Abrupt changes in the DOS indicate a high Seebeck coefficient.<sup>42,43</sup>

For calculating the relaxation time, we need the carrier mobility ( $\mu$ ). The carrier mobility can be determined by the use of deformation potential (DP) theory suggested by Bardeen and Shockley,<sup>44</sup> which is based on effective mass approximation. The carrier mobility is given by the following relation:<sup>45–48</sup>

$$\mu = \frac{2e\hbar^3 C}{3k_B T |m^*|^2 E_1^2}, \quad (2)$$

where  $e$  represents elementary charge;  $\hbar$  is the reduced Planck constant;  $C$  is the elastic modulus along the strain direction calculated by quadratic polynomial fitting of the energy-strain graph as shown in Fig. S4 (ESI†).  $k_B$  is the Boltzmann constant,  $T$  is temperature,  $m^*$  is the effective mass defined by  $m^* = \hbar^2 \left[ \frac{\partial^2 E(k)}{\partial k^2} \right]^{-1}$  and  $E_1$  is the deformation potential defined

as  $E_1 = \frac{\partial E_{\text{edge}}}{\partial \delta} = \frac{\Delta \text{CBM (eV)} \text{ or } \Delta \text{VBM (eV)}}{\Delta \text{strain} (\%)} \text{ where } E_{\text{edge}}$  for CBM (eV) = conduction band minimum for electrons and  $E_{\text{edge}}$  for VBM (eV) = valence band maxima for holes.  $\delta$  is the % uniaxial strain and is defined as strain (%):  $\delta = \left[ \frac{a - a_0}{a_0} \right] \times 100$ . Here,  $a_0$  = lattice constant without strain and  $a$  = lattice constant after applying strain. Additionally, we have calculated two  $E_1$ ; the first is for electrons and the second for holes.  $\Delta \text{CBM (eV)} = \partial E_{\text{edge}}$  is the shift in the conduction band minimum upon applying the strain (%).  $\Delta \text{VBM (eV)} = \partial E_{\text{edge}}$  is the shift in the valence band maximum upon applying the strain (%).  $E_1$  is determined by linear fitting of the CBM (eV) and VBM (eV) values of  $E_{\text{edge}}$  and uniaxial strain in %. In this work the range of strain % is taken as -1% to 1%, and at intervals of every 0.2%, we calculated the CBM (eV) and VBM (eV) values of  $E_{\text{edge}}$ . A graph was plotted between strain (%) and CBM (eV), as shown in Fig. S5 (ESI†). After linear fitting we measured the slope, that is the value of  $E_1$ , for further calculation of the mobility and relaxation time of electrons. Similarly, we plotted a graph between strain (%) and VBM (eV), as shown in Fig. S6 (ESI†). After linear fitting we measured the slope, that is the value of  $E_1$ , for further calculation of the mobility and relaxation time for holes. The electron/hole relaxation time can be determined by  $\tau = \mu m^* / e$ .

The calculated effective mass of the carriers (electrons and holes) is shown in Tables 2 and 3. The values of electron effective mass are significantly lower in the BS monolayer (both phases) as compared to the BSe and BTe monolayers, as shown in Fig. 4(b). The effective masses of carriers for electrons in the 1T and 2H phases of boron monochalcogenide BX (X = S, Se, Te) monolayers are comparable to the values for phosphorene,<sup>47</sup> CP<sup>45,49</sup> and hexagonal M<sub>2</sub>C<sub>3</sub> (M = As, Sb, and Bi) monolayers.<sup>50</sup> We also calculated the carrier mobility at room temperature ( $T = 300$  K) using eqn (2), as presented in Table 2. Due to the small effective mass, the BS monolayer has a high electron carrier mobility of  $1.19 \times 10^4 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  for the 1T phase and  $1.16 \times 10^4 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  for the 2H phase, which is significantly larger than monolayer MoS<sub>2</sub>.<sup>51</sup> The hole carrier mobilities of  $1.198 \times 10^4 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  for BS (1T phase) and  $2.14 \times 10^4 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  for BSe (1T phase) are slightly larger than the electron carrier mobilities. Additionally, the BSe and BTe monolayers with 1T and 2H phases have slightly lower electron mobilities in the

Table 2 Calculated deformation potential constant ( $E_1$ ), unidirectional elastic modulus ( $C$ ), effective mass of electron ( $m^*$ ), electron carrier mobility ( $\mu$ ) and relaxation time ( $\tau$ ) of electron for boron monochalcogenide BX (X = S, Se, Te) monolayer at  $T = 300$  K

| System   | $E_1$ (eV) | $C$ (N m <sup>-1</sup> ) | $m^*$ ( $m_0$ ) | $\mu$ ( $\text{cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ) | $\tau$ (fs) |
|----------|------------|--------------------------|-----------------|---|-------------|
| BS (1T)  | 11.24      | 205.078                  | 0.054           | 11 903.07   | 243.71      |
| BS (2H)  | 12.66      | 218.340                  | 0.050           | 11 651.61   | 220.89      |
| BSe (1T) | 10.36      | 166.857                  | 0.210           | 753.78  | 60.01       |
| BSe (2H) | 11.14      | 178.182                  | 0.350           | 250.62  | 33.26       |
| BTe (1T) | 10.23      | 129.395                  | 0.150           | 783.34  | 66.83       |
| BTe (2H) | 10.83      | 142.559                  | 0.250           | 415.83  | 39.41       |



**Table 3** Calculated deformation potential constant ( $E_1$ ), unidirectional elastic modulus ( $C$ ), effective mass of hole ( $m^*$ ), hole carrier mobility ( $\mu$ ) and relaxation time ( $\tau$ ) of hole for boron monochalcogenide BX (X = S, Se, Te) monolayer at  $T = 300$  K

| System   | $E_1$ (eV) | $C$ (N m $^{-1}$ ) | $m^*$ ( $m_0$ ) | $\mu$ (cm $^2$ V $^{-1}$ s $^{-1}$ ) | $\tau$ (fs) |
|----------|------------|--------------------|-----------------|--------------------------------------|-------------|
| BS (1T)  | 1.30       | 205.078            | 0.38            | 11 979.37                            | 2589.04     |
| BS (2H)  | 1.82       | 218.340            | 0.37            | 6863.66                              | 1444.93     |
| BSe (1T) | 1.85       | 166.857            | 0.18            | 21 449.88                            | 2195.93     |
| BSe (2H) | 9.70       | 178.182            | 0.40            | 168.72                               | 38.38       |
| BTe (1T) | 10.84      | 129.395            | 0.07            | 3197.65                              | 127.31      |
| BTe (2H) | 10.57      | 142.559            | 0.06            | 5052.56                              | 172.41      |

order of  $10^2$  cm $^2$  V $^{-1}$  s $^{-1}$  because they have a higher effective mass, as presented in Fig. 4. Fig. 4(c) depicts a comparison of the carrier mobilities for electrons and holes in boron monochalcogenide BX (X = S, Se, Te) monolayers. A higher carrier mobility enhances the electronic conductivity because both carrier mobility ( $\mu$ ) and electronic conductivity are directly proportional to relaxation time ( $\tau$ ). According to this, the thermoelectric figure of merit ( $ZT$ ) depends on carrier mobility and other parameters such as thermal conductivity and the Seebeck coefficient.

### 3.2 Thermoelectric properties

In this section, to analyze the thermoelectric properties of materials, we calculated the electronic thermal conductivity ( $\kappa_e/\tau$ ), electric conductivity ( $\sigma/\tau$ ), Seebeck coefficient ( $S$ ) and figure of merit ( $ZT$ ). Fig. 5(A) illustrates the relation between electronic thermal conductivity ( $\kappa_e/\tau$ ) and temperature. Lattice vibrations and electron motion are accountable for thermal conductivity. The part of thermal conductivity which arises due to the motion

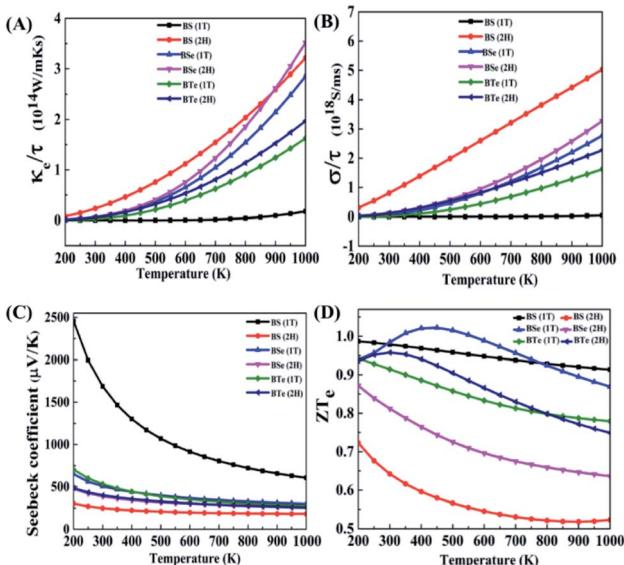
of electrons is considered electronic thermal conductivity. For BS (1T), the electronic thermal conductivity is much less at room temperature; it is  $4.99 \times 10^7$  W m $^{-1}$  K $^{-1}$  s $^{-1}$  at 300 K and increases with increasing temperature, reaching  $1.77 \times 10^{13}$  W m $^{-1}$  K $^{-1}$  s $^{-1}$  at 1000 K. The electronic thermal conductivity of all the other materials increases significantly with increasing temperature. The calculated data is given in Table 4.

From the above data we establish that the 2H phase has more electronic thermal conductivity as compared to the 1T phase, and in the 2H phase the electronic thermal conductivity increases more rapidly than in the 1T phase. BS (2H) phase has the highest value of electronic thermal conductivity,  $0.233 \times 10^{14}$  W m $^{-1}$  K $^{-1}$  s $^{-1}$  at 300 K. On the other hand, at 1000 K the BSe (2H) maximum value is  $3.51 \times 10^{14}$  W m $^{-1}$  K $^{-1}$  s $^{-1}$ , since BSe (2H) shows a larger temperature gradient near 900 K. At 900 K BS (2H) has  $2.59 \times 10^{14}$  W m $^{-1}$  K $^{-1}$  s $^{-1}$  electronic thermal conductivity, while BSe (2H) has  $2.61 \times 10^{14}$  W m $^{-1}$  K $^{-1}$  s $^{-1}$ . Low thermal conductivity materials are needed for high performance thermoelectric devices.

Fig. 5(B) shows the graph of electric conductivity ( $\sigma/\tau$ ) versus temperature. In the BS (1T) phase electric conductivity ( $\sigma/\tau$ ) is also very low, similar to the electronic thermal conductivity ( $\kappa_e/\tau$ ). At 300 K it is only  $5.72 \times 10^{10}$  S ms $^{-1}$ ; it increases with increasing temperature and reaches  $4.42 \times 10^{16}$  S ms $^{-1}$  at 1000 K. Beside this, all the other materials have more incremental electric conductivity, which is visible in the graph. The calculated data is presented in Table 5.

A similar trend is seen here; the 2H phases of all materials possess more electric conductivity than the 1T phases. The rate of increase of electric conductivity with temperature is greater in the 2H phase than in the 1T phase. In the case of BS (2H), electric conductivity increased approximately linearly with temperature and reached  $5.02 \times 10^{18}$  S ms $^{-1}$ . High electric conductivity is needed for good thermoelectric devices.

Fig. 5(C) shows the graph of Seebeck coefficient versus temperature. It is clear from the graph that the Seebeck coefficient decreases as the temperature increases. BS (1T) shows something amazing here – a very high Seebeck coefficient of  $2460 \mu\text{V K}^{-1}$  at 200 K, which is higher than that reported for cubic phase SnSe in an earlier study,<sup>52</sup> and  $1690 \mu\text{V K}^{-1}$  at room temperature (300 K). After 500 K it decreases rapidly to reach  $605.87 \mu\text{V K}^{-1}$  at 1000 K, while so much drastic change is not observed in the other materials. The positive Seebeck coefficient for BS (1T) shows that this is a p-type semiconductor. Therefore,



**Fig. 5** (A) Electronic thermal conductivity ( $\kappa_e/\tau$ ), (B) electric conductivity ( $\sigma_e/\tau$ ), (C) Seebeck coefficient ( $S$ ), and (D) figure of merit ( $ZT$ ) of the thermoelectric properties of 2D boron monochalcogenide BX (X = S, Se, Te) monolayer.

**Table 4** Calculated electronic thermal conductivity of boron monochalcogenide BX (X = S, Se, Te) monolayer at  $T = 300$  K and 1000 K

| Materials | Phase | $\kappa_e/\tau, 10^{14}$ W m $^{-1}$ K $^{-1}$ s $^{-1}$ |        |
|-----------|-------|--|--------|
|           |       | 300 K  | 1000 K |
| BS        | 1T    |  |        |
| BS        | 2H    | 0.233  | 3.21   |
| BSe       | 1T    | 0.050  | 2.85   |
| BSe       | 2H    | 0.064  | 3.51   |
| BTe       | 1T    | 0.025  | 1.62   |
| BTe       | 2H    | 0.063  | 1.96   |



**Table 5** Calculated electric conductivity of boron monochalcogenide BX (X = S, Se, Te) monolayer at  $T = 300$  K and 1000 K

| Materials | Phase | $\sigma/\tau, 10^{18} \text{ S ms}^{-1}$ |        |
|-----------|-------|--|--------|
|           |       | 300 K                                    | 1000 K |
| BS        | 1T    |  |        |
| BS        | 2H    | 0.808                                    | 5.02   |
| BSe       | 1T    | 0.064                                    | 2.77   |
| BSe       | 2H    | 0.158                                    | 3.27   |
| BTe       | 1T    | 0.027                                    | 1.62   |
| BTe       | 2H    | 0.124                                    | 2.27   |

**Table 6** Calculated Seebeck coefficient of boron monochalcogenide BX (X = S, Se, Te) monolayer at  $T = 300$  K and 1000 K

| Materials | Phase | $S, (\mu\text{V K}^{-1})$ |        |
|-----------|-------|---------------------------|--------|
|           |       | 300 K                     | 1000 K |
| BS        | 1T    |                           |        |
| BS        | 2H    | 248.87                    | 182.94 |
| BSe       | 1T    | 506.65                    | 299.05 |
| BSe       | 2H    | 387.77                    | 261.44 |
| BTe       | 1T    | 531.15                    | 279.29 |
| BTe       | 2H    | 401.02                    | 254.62 |

the upper part of the valence band has the greatest influence on the electric properties of the material. As shown in Fig. 2(A) in the dispersion of band structure near valence band maxima (VBM), along the  $\Gamma$ -M line, the curves are nearly flat, showing a high carrier (hole) effective mass around VBM. These bands are also known as heavy bands. Previous research has shown that heavy bands provide high Seebeck coefficients.<sup>42,53-55</sup>

The calculated data for the Seebeck coefficient is shown in Table 6. From the above data, we can see that BS (2H) has the smallest Seebeck coefficient among all the materials. The 1T phases of the materials provide larger Seebeck coefficients than the 2H phases. High Seebeck coefficients are needed for high performance thermoelectric devices.

Fig. 5(D) illustrates the variation in the electronic figure of merit ( $ZT_e$ ) with temperature. For some materials (BSe 1T and BTe 2H), the electronic figure of merit ( $ZT_e$ ) increases with an increase in temperature; after reaching a maximum value it starts to decrease, but for all the other materials it decreases

**Table 7** Calculated electronic figure of merit ( $ZT_e$ ) of boron monochalcogenide BX (X = S, Se, Te) monolayer at different temperatures

| System<br>$T$ | $ZT_e$ |       |       |       |       |       |        |
|---------------|--------|-------|-------|-------|-------|-------|--------|
|               | 200 K  | 250 K | 300 K | 350 K | 400 K | 450 K | 1000 K |
| BS (1T)       | 0.99   | 0.99  | 0.97  | 0.97  | 0.97  | 0.96  | 0.91   |
| BS (2H)       | 0.72   | 0.68  | 0.64  | 0.62  | 0.60  | 0.60  | 0.52   |
| BSe (1T)      | 0.94   | 0.96  | 0.98  | 1.01  | 1.02  | 1.02  | 0.87   |
| BSe (2H)      | 0.87   | 0.84  | 0.81  | 0.79  | 0.76  | 0.74  | 0.63   |
| BTe (1T)      | 0.94   | 0.93  | 0.91  | 0.90  | 0.89  | 0.87  | 0.78   |
| BTe (2H)      | 0.94   | 0.95  | 0.96  | 0.95  | 0.94  | 0.92  | 0.75   |

with increasing temperature. The calculated data for different temperatures is given in Table 7.

From the above data, at low temperature and near room temperature  $ZT_e$  is about 0.7 to 1.0 for all the materials except BS (2H). Therefore, the remaining five materials can be considered good thermoelectric materials at low temperature and near room temperature. Of all of them, BSe (1T) is the best thermoelectric material, having the highest  $ZT_e$  of 1.022 at 450 K temperature.

## 4 Conclusion

We have systematically investigated the electronic, vibrational and thermoelectric properties of boron monochalcogenide BX (X = S, Se, Te) materials using a density functional theory framework. The computed cohesive energy of each phase of boron monochalcogenides has a negative value, which shows the stability of the materials. From the phonon band structure calculations, the positive phonon frequencies show the dynamic stability of the materials. The electronic band structure shows that each material has an indirect bandgap varying from 2.92 eV to 1.53 eV. Due to the presence of the small effective mass of electrons, boron monochalcogenide BX (X = S, Se, Te) materials have superior carrier mobility. The 1T and 2H phases of the BS monolayer have carrier mobilities of  $1.19 \times 10^4$  and  $1.16 \times 10^4 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ . From the thermoelectric calculations, we found that for the low and mid-temperature range of 200 K to 450 K, each phase of the boron monochalcogenides shows a high electronic figure of merit  $ZT_e$  nearly equal to 1, with the exception of the BS 2H phase. The 1T phase of the BSe monolayer has the highest  $ZT_e = 1.022$ , which is the maximum across all the studied materials. These findings suggest that boron monochalcogenide monolayer materials have great potential applications in the field of high-performance thermoelectric devices.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

P. M. is thankful to SVNIT, Surat, for his Institute Research fellowship (FIR-DS17PH004). D. S. and R. A. thank Olle Engkvists Stiftelse, Carl Tryggers Stiftelse för Vetenskaplig Forskning (CTS) and Swedish Research Council (VR) for financial support. SNIC and HPC2N are acknowledged for providing the computing facilities. Y. A. S. is thankful to the Science and Engineering Research Board (SERB), India, for the financial support (grant number: EEQ/2016/000217).

## References

- 1 T. M. Tritt and M. Subramanian, *MRS Bull.*, 2006, **31**, 188–198.



2 K. Biswas, J. He, I. D. Blum, C.-I. Wu, T. P. Hogan, D. N. Seidman, V. P. Dravid and M. G. Kanatzidis, *Nature*, 2012, **489**, 414.

3 M. S. Dresselhaus, G. Chen, M. Y. Tang, R. Yang, H. Lee, D. Wang, Z. Ren, J.-P. Fleurial and P. Gogna, *Adv. Mater.*, 2007, **19**, 1043–1053.

4 G. J. Snyder and E. S. Toberer, *Materials for sustainable energy: a collection of peer-reviewed research and review articles from Nature Publishing Group*, World Scientific, 2011, pp. 101–110.

5 H. Wang, Y. Pei, A. D. LaLonde and G. J. Snyder, *Adv. Mater.*, 2011, **23**, 1366–1370.

6 L. E. Bell, *Science*, 2008, **321**, 1457–1461.

7 W. G. Zeier, J. Schmitt, G. Hautier, U. Aydemir, Z. M. Gibbs, C. Felser and G. J. Snyder, *Nat. Rev. Mater.*, 2016, **1**, 16032.

8 D. Singh, S. Kansara, S. K. Gupta and Y. Sonvane, *J. Mater. Sci.*, 2018, **53**, 8314–8327.

9 L. Hicks and M. S. Dresselhaus, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1993, **47**, 12727.

10 J. P. Heremans, V. Jovovic, E. S. Toberer, A. Saramat, K. Kurosaki, A. Charoenphakdee, S. Yamanaka and G. J. Snyder, *Science*, 2008, **321**, 554–557.

11 Y. Pei, X. Shi, A. LaLonde, H. Wang, L. Chen and G. J. Snyder, *Nature*, 2011, **473**, 66.

12 Y. Pei, A. LaLonde, H. Wang and G. J. Snyder, *Energy Environ. Sci.*, 2012, **5**, 7963.

13 D. Singh and R. Ahuja, *ACS Appl. Energy Mater.*, 2019, **2**, 6891–6903.

14 J. Yu, K. Xia, X. Zhao and T. Zhu, *J. Phys. D: Appl. Phys.*, 2018, **51**, 113001.

15 N. P. Blake, S. Lattner, J. D. Bryan, G. D. Stucky and H. Metiu, *J. Chem. Phys.*, 2001, **115**, 8060–8073.

16 H. R. Aliabad, M. Ghazanfari, I. Ahmad and M. Saeed, *Comput. Mater. Sci.*, 2012, **65**, 509–519.

17 A. Weidenkaff, M. Aguirre, L. Bocher, M. Trottmann, P. Tomes and R. Robert, *J. Korean Ceram. Soc.*, 2010, **47**, 47–53.

18 M. Bilal, B. Khan, H. R. Aliabad, M. Maqbool, S. J. Asadabadi and I. Ahmad, *Comput. Phys. Commun.*, 2014, **185**, 1394–1398.

19 I. Matsubara, R. Funahashi, T. Takeuchi, S. Sodeoka, T. Shimizu and K. Ueno, *Appl. Phys. Lett.*, 2001, **78**, 3627–3629.

20 W. Shin, N. Murayama, K. Ikeda and S. Sago, *J. Power Sources*, 2001, **103**, 80–85.

21 X. Wang, R. Yang, Y. Zhang, P. Zhang and Y. Xue, *Appl. Phys. Lett.*, 2011, **98**, 222110.

22 K. Pandey, P. Yadav, D. Singh, S. K. Gupta, Y. Sonvane, I. Lukac̆evic̆, J. Kim and M. Kumar, *Sci. Rep.*, 2016, **6**, 32690.

23 V. Sousa, *Microelectron. Eng.*, 2011, **88**, 807–813.

24 S. LeBlanc, *Sustainable Mater. Technol.*, 2014, **1–2**, 26–35.

25 C. Xiao, X. Qin, J. Zhang, R. An, J. Xu, K. Li, B. Cao, J. Yang, B. Ye and Y. Xie, *J. Am. Chem. Soc.*, 2012, **134**, 18460–18466.

26 T.-R. Wei, Y. Qin, T. Deng, Q. Song, B. Jiang, R. Liu, P. Qiu, X. Shi and L. Chen, *Sci. China Mater.*, 2019, **62**, 8–24.

27 S. Li, X. Li, Z. Ren and Q. Zhang, *J. Mater. Chem. A*, 2018, **6**, 2432–2448.

28 X. Chen, Y. Huang, J. Liu, H. Yuan and H. Chen, *ACS Omega*, 2019, **4**, 17773–17781.

29 M.-S. Li, K.-X. Chen, D.-C. Mo and S.-S. Lyu, *Phys. Chem. Chem. Phys.*, 2019, **21**, 24695–24701.

30 N. T. Hung, A. R. Nugraha and R. Saito, *Appl. Phys. Lett.*, 2017, **111**, 092107.

31 B. Mortazavi and T. Rabczuk, *Energies*, 2018, **11**, 1573.

32 G. Kresse and D. Joubert, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1999, **59**, 1758.

33 G. Kresse and J. Furthmüller, *Comput. Mater. Sci.*, 1996, **6**, 15–50.

34 G. Kresse and J. Furthmüller, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1996, **54**, 11169.

35 J. P. Perdew, K. Burke and M. Ernzerhof, *Phys. Rev. Lett.*, 1996, **77**, 3865.

36 H. J. Monkhorst and J. D. Pack, *Phys. Rev. B: Solid State*, 1976, **13**, 5188.

37 A. Togo and I. Tanaka, *Scr. Mater.*, 2015, **108**, 1–5.

38 G. K. Madsen and D. J. Singh, *Comput. Phys. Commun.*, 2006, **175**, 67–71.

39 B. Qiu, Z. Tian, A. Vallabhaneni, B. Liao, J. M. Mendoza, O. D. Restrepo, X. Ruan and G. Chen, *EPL*, 2015, **109**, 57006.

40 J. Sun and D. J. Singh, *Phys. Rev. Appl.*, 2016, **5**, 024006.

41 K. Momma and F. Izumi, *J. Appl. Crystallogr.*, 2011, **44**, 1272–1276.

42 D. Zou, S. Xie, Y. Liu, J. Lin and J. Li, *J. Mater. Chem. A*, 2013, **1**, 8888–8896.

43 M.-S. Lee, F. P. Poudeu and S. Mahanti, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2011, **83**, 085204.

44 J. Bardeen and W. Shockley, *Phys. Rev.*, 1950, **80**, 72.

45 G. Wang, R. Pandey and S. P. Karna, *Nanoscale*, 2016, **8**, 8819–8825.

46 D. Singh, S. K. Gupta, Y. Sonvane, T. Hussain and R. Ahuja, *Phys. Chem. Chem. Phys.*, 2018, **20**, 21716–21723.

47 R. Fei and L. Yang, *Nano Lett.*, 2014, **14**, 2884–2889.

48 S. Bruzzone and G. Fiori, *Appl. Phys. Lett.*, 2011, **99**, 222108.

49 D. Singh, V. Shukla, P. K. Panda, Y. K. Mishra, H.-G. Rubahn and R. Ahuja, *New J. Chem.*, 2020, **44**, 3777–3785.

50 P.-F. Liu, T. Bo, Z. Liu, O. Eriksson, F. Wang, J. Zhao and B.-T. Wang, *J. Mater. Chem. C*, 2018, **6**, 12689–12697.

51 B. Radisavljevic, A. Radenovic, J. Brivio, V. Giacometti and A. Kis, *Nat. Nanotechnol.*, 2011, **6**, 147.

52 F. K. Butt, B. U. Haq, S. ur Rehman, R. Ahmed, C. Cao and S. AlFaifi, *J. Alloys Compd.*, 2017, **715**, 438–444.

53 J. Ding, B. Xu, Y. Lin, C. Nan and W. Liu, *New J. Phys.*, 2015, **17**, 083012.

54 K. Kaur, *EPL*, 2017, **117**, 47002.

55 S.-D. Guo, *RSC Adv.*, 2016, **6**, 47953–47958.

