

**Showcasing research from Professor Takashi Morii's laboratory, Institute of Advanced Energy, Kyoto University, Uji, Kyoto, Japan.**

**Enhanced enzymatic activity exerted by a packed assembly of a single type of enzyme**

Enzymatic reactions were investigated under conditions that mimicked the densely packed conditions in the cell. A single type of monomeric enzyme carbonic anhydrase was located on a DNA scaffold in the packed or dispersed states. At the same concentration of enzyme, reaction proceeded faster in the packed than in the dispersed state. Acceleration of reaction in the packed assembly was more prominent for substrates with higher hydrophobicity. We propose that the entropic force of water increases local substrate concentration within the domain confined between enzyme surfaces, thus accelerating the reaction.

**As featured in:**




See Takashi Morii *et al.*,  
*Chem. Sci.*, 2020, 11, 9088.

Cite this: *Chem. Sci.*, 2020, **11**, 9088

All publication charges for this article have been paid for by the Royal Society of Chemistry

## Enhanced enzymatic activity exerted by a packed assembly of a single type of enzyme†

Huyen Dinh,  Eiji Nakata,  Kaori Mutsuda-Zapater, Masayuki Saimura, Masahiro Kinoshita  and Takashi Morii  \*

In contrast to the dilute conditions employed for *in vitro* biochemical studies, enzymes are spatially organized at high density in cellular micro-compartments. In spite of being crucial for cellular functions, enzymatic reactions in such highly packed states have not been fully addressed. Here, we applied a protein adaptor to assemble a single type of monomeric enzyme on a DNA scaffold in the packed or dispersed states for carbonic anhydrase. The enzymatic reactions proceeded faster in the packed than in the dispersed state. Acceleration of the reaction in the packed assembly was more prominent for substrates with higher hydrophobicity. In addition, carbonic anhydrase is more tolerant of inhibitors in the packed assembly. Such an acceleration of the reaction in the packed state over the dispersed state was also observed for xylose reductase. We propose that the entropic force of water increases local substrate or cofactor concentration within the domain confined between enzyme surfaces, thus accelerating the reaction. Our system provides a reasonable model of enzymes in a packed state; this would help in engineering artificial metabolic systems.

Received 24th June 2020  
Accepted 25th July 2020

DOI: 10.1039/d0sc03498c

rsc.li/chemical-science

## Introduction

Enzymes are often spatially organized within the cell, either in close proximity on the cell membrane or confined inside a micro-compartment. Such environments are believed to play key roles in enabling the extraordinary efficiency and specificity of sequential metabolic enzymatic reactions.<sup>1–3</sup> A typical example is the hetero oligomeric assembly of enzymes. Enzymes for sequential reactions are aligned in close proximity to prevent the loss of intermediate by random diffusion, thereby accelerating its transfer between enzyme subunits.<sup>4,5</sup> Compartmentalization also regulates the spatial organization of enzymes. Collaborating enzymes are often packed in bacterial micro-compartments (BMCs) to encapsulate the toxic intermediates or to overcome the intrinsic catalytic inefficiency.<sup>6–8</sup> Inside a proteinous shell, the enzyme concentration is in the millimolar range as was recently reported that enzyme aggregates inside a BMC carboxysome, form a dynamic liquid-like

matrix internally.<sup>9</sup> Autotrophic bacteria concentrate the central enzyme of the Calvin–Benson–Bassham cycle, ribulose-1,5-bisphosphate carboxylase/oxygenase (RubisCO), responsible for the final step of CO<sub>2</sub> fixation, in carboxysomes.<sup>10</sup> Around 2000 copies of RubisCO and 80 copies of carbonic anhydrase are encapsulated inside a proteinous shell with diameter of 100–200 nm.<sup>11,12</sup> The proteinous shell acts not only as a barrier for ligand diffusion but serves also as a container to confine the enzymes at high density.

While the factors controlling the efficiency of sequential reactions by two or three types of enzymes have been actively addressed,<sup>13,14</sup> the significance of such highly packed conditions for the reaction of a single type of enzyme remains to be determined. Reaction efficiency in a highly packed assembly could differ from that in a test tube, in which enzymes distribute freely in dilute conditions. To address this issue, protein assembly on a DNA scaffold offers an ideal system to study enzymatic reactions in spatially defined arrangements. DNA nanostructures have been applied as scaffolds for arranging functional molecules and nanomaterials.<sup>15–18</sup> In particular, DNA origami-based scaffolds enable the assembly of several different enzymes to address the effect of inter-enzyme distances on sequential reactions.<sup>19–24</sup>

Here we apply a protein adaptor<sup>25</sup> to assemble a single type of monomeric enzyme, carbonic anhydrase, on a DNA scaffold in a packed state with less than a few nanometers inter-enzyme distance or dispersed state and show that the esterase reaction proceeds faster in the packed than in the dispersed state. In the packed assembly, the reaction is accelerated more

Institute of Advanced Energy, Kyoto University, Uji, Kyoto 611-0011, Japan. E-mail: t-morii@iae.kyoto-u.ac.jp

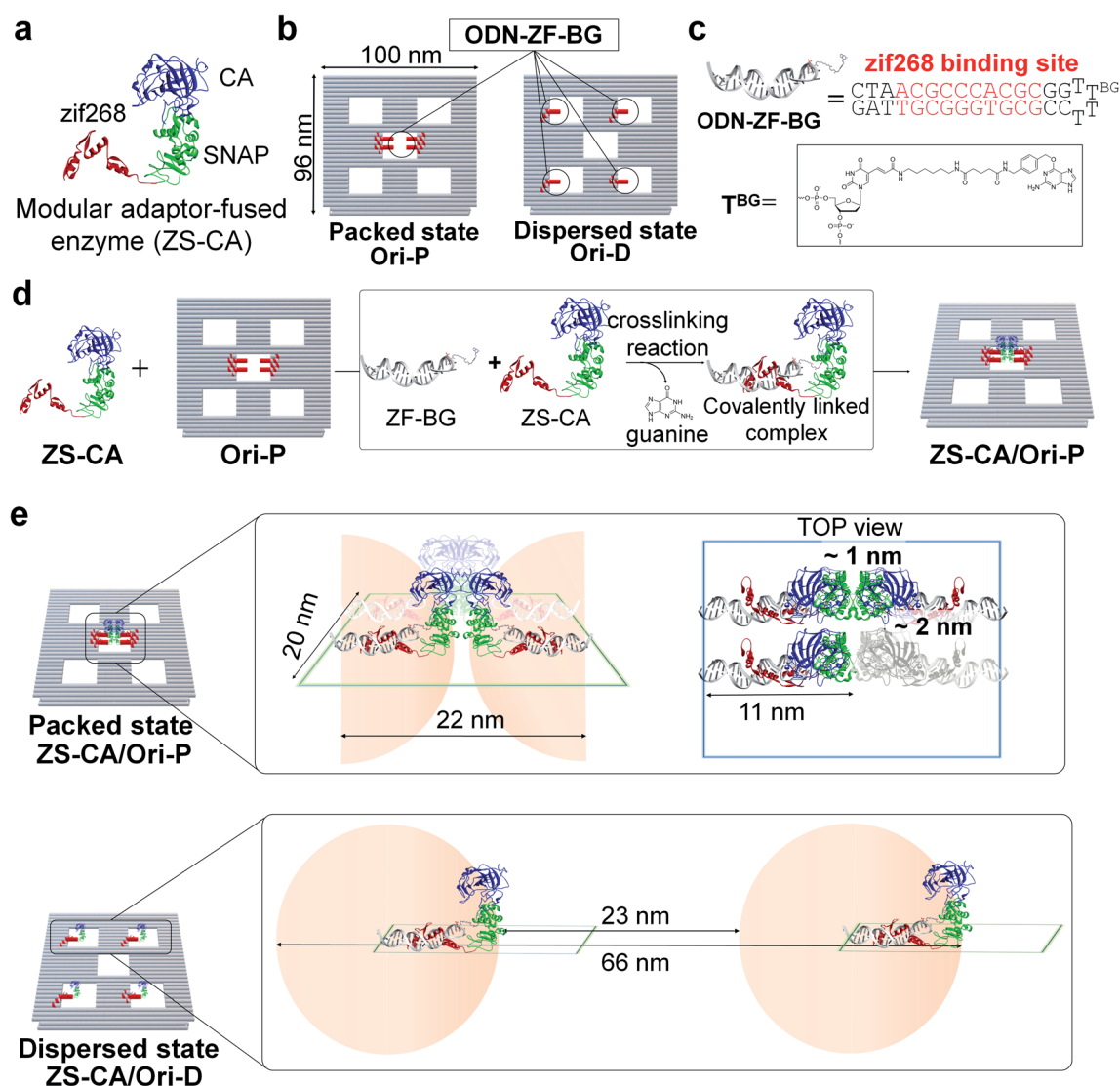
† Electronic supplementary information (ESI) available: Primer sequences for ZS-CA (Table S1), ZS-CA characterizations (Fig. S1–S3), illustrations of DNA scaffolds (Fig. S4), distance of ZS-CA in the packed state (Fig. S5), purification of DNA scaffolds (Fig. S6), ZS-CA volume analyses (Fig. S7 and S8), initial velocities of ZS-CA assembled on DNA scaffolds (Fig. S9), ZS-CA activity with PEG 6K (Fig. S10), ZS-CA activity with macromolecular crowding reagents (Fig. S11), thermal stability of ZS-CA on DNA scaffolds (Fig. S12), ZS-CA with *p*-NPA, *p*-NPB and *p*-NPV (Fig. S13), effect of bromide ion on the ZS-CA (Fig. S14), analyses of ZS-XR volumes on DNA scaffolds (Fig. S15), kinetic analyses of ZS-XR on DNA scaffolds (Fig. S16 and S17). See DOI: 10.1039/d0sc03498c

prominently for substrates with higher hydrophobicity and is more tolerant of inhibitors. When another enzyme xylose reductase was assembled in the packed state, a similar acceleration of the reaction in the packed state over the dispersed state was also observed. We propose that the entropic force of water increases local substrate concentration within the domain confined between enzyme surfaces, thus accelerating the reaction. Our finding offers a new insight on the efficiency of reaction by single type of enzyme in the packed state. The water-entropy effect increases as the enzyme structure becomes less flexible in the packed assembly. Therefore, a greater effect is expected within the spatially more constrained cellular compartments. Our system provides a reasonable model of enzymes in packed state; this would help in engineering artificial metabolic systems.

## Results

### Constructing the packed state of enzyme on DNA scaffold

A defined number of molecules of a single type of enzyme were located either in close proximity or far apart on a DNA scaffold (Fig. 1). Monomeric human carbonic anhydrase II (CA) was chosen as the target enzyme because its structure and enzymatic features have been extensively studied.<sup>26,27</sup> CA was genetically fused to a modular adaptor (ZS) consisting of a sequence-specific DNA-binding zinc finger protein (zif268) and a self-ligating SNAP-tag.<sup>28–30</sup> The resulting adaptor-conjugated enzyme, ZS-CA (Fig. 1 and S1†), showed almost the same enzymatic activity to the parent CA (Fig. S2†) and bound stably at the intended sites in high yields on the DNA scaffold through covalent linkage (Fig. S3†).<sup>30</sup>



**Fig. 1** Model of packed and dispersed states. (a) Model of modular adaptor-fused carbonic anhydrase (ZS-CA). (b) Illustration of DNA scaffolds containing five cavities to represent the packed (Ori-P) and the dispersed (Ori-D) states. (c) The ZS-CA binding site (ODN-ZF-BG) includes the specific binding sequence for zif268 and BG. (d) The cross-linking reaction between ZS-CA and ODN-ZF-BG on DNA scaffold. (e) Schematic representations of four ZS-CAs in the packed (upper) and dispersed (lower image) states. The shaded (half) circles indicate the possible area for movements of bound ZS-CA.





A rectangular DNA scaffold with five cavities<sup>30–33</sup> was prepared by the DNA origami method.<sup>15</sup> Four binding sites for ZS-CA (ODN-ZF-BG) containing the specific binding sequence and benzyl guanine (BG), the SNAP-tag substrate, were placed in the central cavity (Fig. 1b–d and S4†) to keep four ZS-CAs in the packed state (Ori-P). A scaffold mimicking the dispersed state of ZS-CA (Ori-D) contained four binding sites placed solely in the four outer cavities, allowing the four ZS-CAs to remain separated. Considering the flexibility of the connection between ODN-ZF-BG and the DNA scaffold, the distance from the connection to CA was calculated to be 11 nm. When four ZS-CAs were assembled in Ori-P, the inter-enzyme distance between CA regions was <1 nm (Fig. 1e and S5†). This corresponds to the average distance of free ZS-CA in a 18–38 mM solution (see Materials and methods). When four ZS-CA molecules were located in Ori-D, each CA region was completely separated by at least 23 nm (Fig. 1e). These enzyme assemblies on Ori-P and Ori-D allowed us to directly compare the reaction of CA in the packed and dispersed states without increasing its concentration.

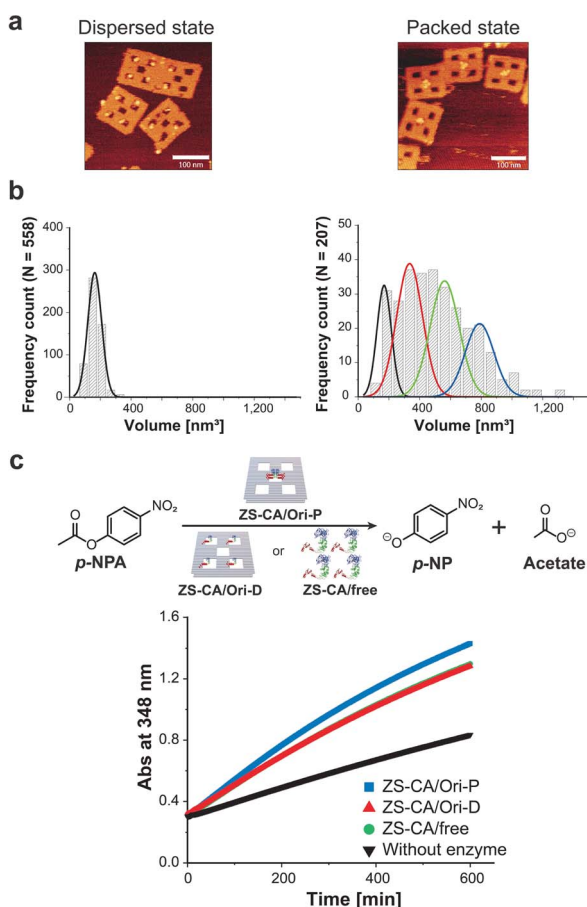


Fig. 2 Characterization of ZS-CA in the packed and the dispersed states. (a) AFM images of ZS-CA assembled on Ori-D (left) and Ori-P (right). (b) Analysis of the volumes of ZS-CA assembled on the DNA scaffold for single ZS-CA on Ori-D (left). The volume of ZS-CA on Ori-P corresponds to the volumes of one (black), two (red), three (green), and four (blue) ZS-CA molecules (right). (c) Time-course profiles of the esterase reactions of ZS-CA (4 nM) on DNA scaffold with *p*-NPA was monitored at 348 nm.

## Enzymatic activity of ZS-CA in the packed and dispersed states

To adjust the concentrations of CA in the packed and the dispersed states, actual numbers of ZS-CA molecules loaded on each scaffold were estimated from AFM images (Fig. 2a, b and S6–S8†).<sup>34</sup> In a typical experiment, the number of ZS-CA molecules bound to one Ori-D and Ori-P scaffold were deduced to be 3.1 and 2.6, respectively. The esterase activity of CA was assessed spectrophotometrically at 348 nm using *p*-nitrophenyl acetate (*p*-NPA) as a substrate (Fig. 2c), a widely applied ester to assess the activity of CA,<sup>27,35,36</sup> with the same concentrations of assembled ZS-CA on Ori-P and Ori-D. The concentrations of assembled ZS-CA on Ori-P and Ori-D were estimated from the concentration of DNA scaffold and the number of ZS-CA molecules bound to each scaffold deduced as described above (Fig. S8†). Time-course profiles for the formation of hydrolysed product, *p*-nitrophenolate (*p*-NP), by 4 nM ZS-CA assembled on Ori-P, Ori-D, and in bulk solution are shown in Fig. 2c. The reaction profile of ZS-CA on Ori-D was similar to that in bulk solution, indicating little or no effect of the DNA scaffold on ZS-CA activity. In contrast, the reaction of ZS-CA assembled on Ori-P was faster than that on Ori-D at substrate concentrations ranging from 0.1 to 1 mM (Fig. S9†).

## Characteristics of the enzymatic activity of ZS-CA in the packed state

An interface composed of two or more ZS-CA molecules is the distinct feature of the packed assembly on Ori-P. Unlike on Ori-P, free ZS-CA in solution or ZS-CA on Ori-D did not approach the inter-enzyme distance of 1 nm at nanomolar concentrations (see Materials and methods). We investigated whether specific interactions between the CA domains in certain orientation(s) in the packed state could enhance the esterase reaction. Accordingly, we devised three types of ZS-CA assemblies that allowed two CA regions to reside face-to-face, side-by-side, or diagonally at an inter-enzyme distance of 1 nm (Fig. 3). We expected that the cooperativity would be induced in certain orientation(s) of ZS-CA within the three assemblies by specific interaction between two CA regions, thus resulting in enhanced efficiency of esterase reactions. However, the reaction of *p*-NPA was enhanced in all three arrangements to the same extent as observed for the Ori-P assembly. Therefore, the proximal alignment of two ZS-CA molecules, regardless of orientation, was sufficient to increase the esterase reaction of ZS-CA.

It is well known that the presence of polyethylene glycol (PEG) stabilizes enzyme structure through the so-called macromolecular crowding effect.<sup>37,38</sup> Based on the findings so far, we assumed that enzyme activity improved with increasing structural stability and the structure of ZS-CA was more stable in Ori-P than in Ori-D. Consequently, addition of PEG could stabilize ZS-CA and enhance its reaction on Ori-D or free ZS-CA to the level seen on Ori-P. Thus, addition of PEG could amplify the differences between these two states in terms of stability and activity. Reactions of ZS-CA (4 nM) in bulk solution, on Ori-P, or Ori-D were carried out in the presence of PEG 6K (Fig. S10†). In all cases, the initial velocity of ZS-CA gradually decreased as PEG 6K concentration rose above 300 mg ml<sup>−1</sup>; moreover, the difference in



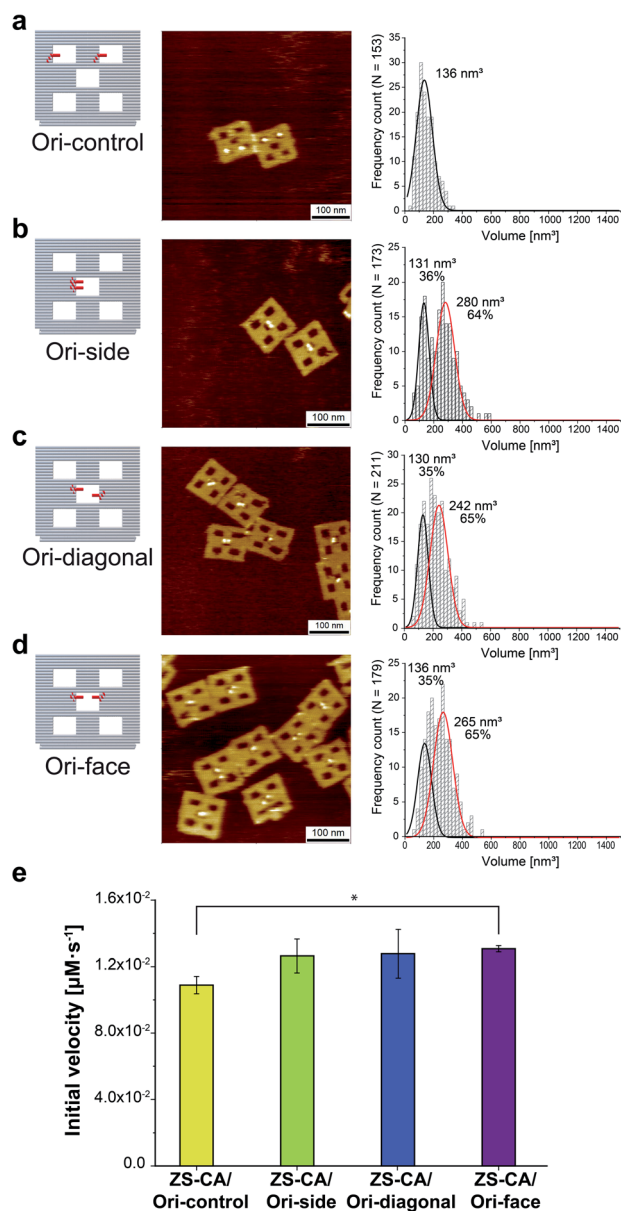


Fig. 3 (a–d) Illustration of DNA scaffolds (left) with AFM images (middle) and volume analysis (right) of ZS-CA on DNA scaffolds containing two binding sites per scaffold: in separated cavities (Ori-control, in a); in a center cavity with different orientations: side-by-side (Ori-side, in b), diagonally (Ori-diagonal, in c), or face-to-face (Ori-face, in d). The percentage of ZS-CA-loaded DNA cavities on Ori-control were determined from AFM images as 82% ( $n = 146$ ). Thus, the numbers of ZS-CA molecules bound to Ori-control were calculated as 1.6 with an average volume of 136 nm<sup>3</sup>. The volume of ZS-CA on Ori-side, diagonal, face with the respective volumes for one (black line), two (red line) molecules were estimated by fitting.<sup>30</sup> The percentages of ZS-CA-loaded DNA cavities on DNA scaffold were determined from AFM images as 99%, 98%, 98%, respectively. In average, numbers of ZS-CA bound to Ori-side, Ori-diagonal and Ori-face were calculated as 1.6 in three cases. (e) Initial velocities of the esterase reaction by each of the four ZS-CA assemblies. Reactions were carried out with 6 nM of DNA origami assembled with ZS-CA in a buffer (pH 7.6) containing 50 mM HEPES, 12.5 mM MgCl<sub>2</sub>, 1% acetonitrile, 1 μM ZnCl<sub>2</sub> and 0.001% Tween 20 with 1 mM *p*-NPA. Error bars represent the mean ± SD of three independent experiments (\* $p < 0.005$ ).

activity decreased as PEG concentration increased. Addition of other macromolecular crowding reagents, such as dextran (6K and 60K), PEG 8K, and ethylene glycol also slowed down the reaction of ZS-CA in all cases (Fig. S11†).

From these results, we conclude that acceleration of the ZS-CA esterase reaction in the packed state was not caused by the enhanced stability of proteins as reported for the effect of macromolecular crowding reagents. In addition, the activity of ZS-CA in free solution, on Ori-P or Ori-D, remained unchanged at 25 °C for 12 h (Fig. S12†), indicating that variations in the extent to which ZS-CA in each state retained its activity did not account for the enhanced activity in the packed state.

### Effect of sufficiently high concentration of Na<sub>2</sub>SO<sub>4</sub>

Steiner and Lindskog<sup>39</sup> reported activation of the CA-catalysed hydrolysis of *p*-NPA in the presence of high concentrations of sodium sulphate (Na<sub>2</sub>SO<sub>4</sub>) in the early 70's, and suggested that the effect of ionic strength on the chemical potential of the substrate caused an increase in apparent affinity of the substrate for the active site. In the presence of 0.5 M Na<sub>2</sub>SO<sub>4</sub>, the initial velocity of the esterase reaction of ZS-CA was increased by 2.0 times in all cases, *i.e.*, free solution, on Ori-D, and on Ori-P (Fig. 4a). Our interpretation on the effect of Na<sub>2</sub>SO<sub>4</sub> effect is different from that of Steiner and Lindskog as argued in "Effect of salt addition" of the Discussion.

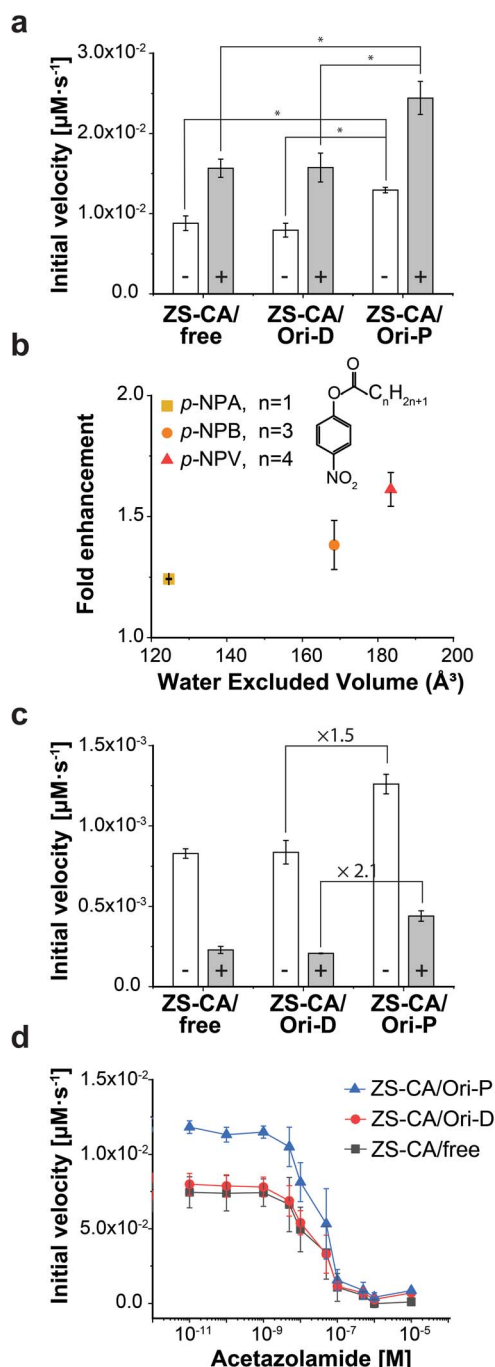
### Factors enhancing the enzymatic activity of ZS-CA in the packed state

The esterase reaction of ZS-CA in the packed state was further investigated with *p*-nitrophenyl butyrate (*p*-NPB) and *p*-nitrophenyl valerate (*p*-NPV), which bear larger, nonpolar acyl groups than *p*-NPA (Fig. 4b and S13†). With *p*-NPA as the substrate, the reaction was accelerated 1.3 times on Ori-P over Ori-D, but 1.5 and 1.6 times with *p*-NPB and *p*-NPV, respectively, showing the statistical significance of mean differences among experimental groups. As argued in the Discussion, a substrate generates a volume which is inaccessible to the centre of water molecules, which is referred to as the "excluded volume" (EV).<sup>40,41</sup> In general, a solute becomes more hydrophobic as its EV increases and its polarity or affinity for water decreases. These EV and affinity effects are entropic and energetic in origin, respectively. For substrates whose energetic affinity for water is not significantly high like *p*-NPA, *p*-NPB, and *p*-NPV, the entropic effect dominates with the result that the hydrophobicity can be discussed in terms of the EV. The esterase reaction of ZS-CA in the packed state was accelerated for substrates with the larger EV as shown in Fig. 4b where factors enhancing the initial velocity of ZS-CA on Ori-D over that on Ori-P for a given substrate (fold enhancement) were plotted against the EV of each substrate.

### Effects of inhibitors for ZS-CA in the packed and dispersed states

The esterase activity in the packed state was further enhanced for the larger, more hydrophobic substrates that resulted modulation in the substrate specificity of the parent enzyme. The result



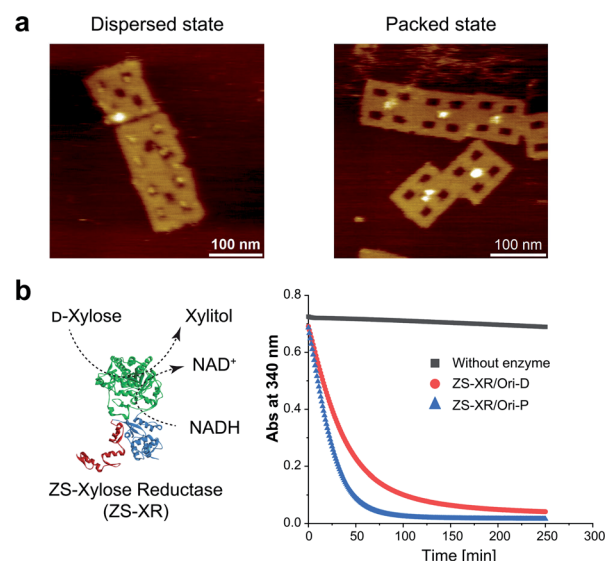


**Fig. 4** Kinetic properties of the enzymes in dispersed and packed assemblies. (a) The reaction rate of ZS-CA (5.5 nM) assembled on the DNA scaffold with 1 mM *p*-NPA in the absence (open bars) and presence (grey bars) of 0.5 M  $\text{Na}_2\text{SO}_4$  (\* $p < 0.005$ ). (b) The enhancement factors (initial velocity of CA on Ori-P over that of CA on Ori-D) for the esterase reaction of ZS-CA plotted against the water excluded volume (EV) of *p*-NPA (128  $\text{\AA}^3$ ), *p*-NPB (165  $\text{\AA}^3$ ), and *p*-NPV (183  $\text{\AA}^3$ ).<sup>39,40</sup> Reaction included 23 nM ZS-CA and 0.1 mM substrate. (c) Inhibition exerted by 1 M NaBr (grey bars) on the reaction rate of 5.5 nM ZS-CA with 0.1 mM *p*-NPA. (d) Initial reaction velocity of 5.5 nM ZS-CA assembled on the DNA scaffold (in 1 mM *p*-NPA) with an increasing concentration of acetazolamide (from 10 pM to 10  $\mu\text{M}$ ). Error bars represent the mean  $\pm$  SD of three independent experiments.

suggested that the sensitivity of the enzyme to inhibitory molecules or ions could be different depending on the assembly state of enzyme. Therefore, the effect of known CA inhibitors, such as weakly hydrated, large halide anions (*i.e.*,  $\text{Br}^-$  and  $\text{I}^-$ ) and sulfonamides,<sup>42,43</sup> were investigated in the packed state (Fig. 4c and S14<sup>†</sup>). In the presence of 1 M NaBr, the initial velocities of *p*-NPA hydrolysis reactions by ZS-CA on Ori-D and Ori-P were reduced in all cases. Interestingly, the initial velocity of ZS-CA on Ori-P was 2.1 times higher than that on Ori-D or in free solution in the presence of 1 M NaBr. Considering the 1.5 times enhancement for the reaction of ZS-CA on Ori-P in the absence of bromide ion, ZS-CA on Ori-P tolerated better the inhibitory effect of bromide than ZS-CA on Ori-D or in free solution. Inhibition of the esterase reactions by increasing concentrations of acetazolamide also revealed the lower sensitivity of ZS-CA on Ori-P to the inhibitor at up to 100 nM (Fig. 4d). Taken together, the sensitivity of the esterase reaction to inhibitory molecules or ions varies depending on the assembled state of ZS-CA.

### Enzymatic activity of xylose reductase in the packed and dispersed states

It is interesting to examine another enzymatic reaction in the packed and dispersed states. For this end, reactions in the packed and dispersed states of xylose reductase (XR), an enzyme from xylose metabolic pathway, were investigated. XR converts xylose into xylitol by consuming the cofactor NADH.<sup>44</sup> XR was fused to the ZS modular adaptor (ZS-XR)<sup>21</sup> to assemble in the packed and dispersed states on DNA scaffold (Fig. 5a). ZS-XR showed high binding yields to Ori-D and Ori-P as determined



**Fig. 5** Characterization of modular adaptor-fused xylose reductase (ZS-XR) in the packed and the dispersed states. (a) ZS-XR was assembled on Ori-D and Ori-P with the percentages of protein-loaded cavities were 82% and 99%, respectively, as observed by AFM images. (b) Time course profiles for the reaction of ZS-XR on DNA scaffold monitored by the oxidation of NADH at 340 nm. The reaction was initiated by an addition of ZS-XR/Ori-P or ZS-XR/Ori-D (14 nM) to the mixture of 200 mM D-xylose and 300  $\mu\text{M}$  NADH in a buffer (pH 6.8) containing 50 mM HEPES, 0.1 M NaCl, 12.5 mM  $\text{MgCl}_2$ , 1  $\mu\text{M}$   $\text{ZnCl}_2$ , 0.001% Tween 20.





from AFM images (the percentages of protein-loaded cavities were 82% and 99%, respectively). Volume analysis in each assembly indicated that the average numbers of ZS-XR on DNA scaffold were 2.7 molecules on one Ori-P and 3.2 molecules on Ori-D (Fig. S15†). The reaction of XR was assessed by measuring the oxidation of NADH spectrophotometrically at 340 nm. At the same concentration of enzyme (14 nM) on DNA scaffold, ZS-XR showed higher initial reaction rate in the packed state than in the dispersed state (Fig. 5b). Acceleration in the reaction rate of ZS-XR in packed state was also observed when the concentrations of both D-xylose and NADH were decreased to 5 mM D-xylose and 25  $\mu$ M NADH (Fig. S16†).

## Discussion

We suggest that the experimental results presented above can be interpreted by applying the entropic excluded-volume (EV) (water-entropy) effect<sup>45,46</sup> originating from the translational displacement of water molecules in the entire system. Substrates are enriched within such a domain by the water-entropy effect illustrated in Fig. 6.<sup>47</sup> A substrate or an enzyme generates a volume referred to as “excluded volume (EV)”, which is inaccessible to the center of water molecules (Fig. 6a, left panel). When the substrate comes in contact with the enzyme surface, the two EVs overlap (Fig. 6a, right panel). Consequently, the total volume available for the translational displacement of water molecules in the system increases by the overlapping volume, leading to a gain of configurational entropy of water. This entropic force causes enrichment of the substrate near the enzyme. When two enzymes are sufficiently close to each other (Fig. 6b), the substrate can contact both enzyme surfaces and a further increase in the overlapping volume follows. Hence, the local concentration of substrate becomes higher within the confined domain in the packed state than near the single

enzyme in the dispersed state or free in solution, leading to a higher initial reaction velocity by the nearest enzyme. The water-entropy effect described above is enhanced upon addition of a salt whose ions are strongly hydrated, such as sulfate ions ( $\text{SO}_4^{2-}$ ), through modification of the bulk water structure.

In what follows, we explain this effect and describe our physical interpretation of the experimental results.

### Basic concept based on entropic excluded-volume effect

We consider a simple model system where hard-sphere solutes with diameter  $d_U$  and a planar hard wall are immersed in small hard spheres with diameter  $d_S$  forming the solvent. In this hard-body model system where no soft (attractive or repulsive) interaction potentials are present, all of the accessible system configurations share the same energy, and the system behavior is purely entropic in its origin. We discuss the gain of solvent entropy occurring when a solute comes in contact with the wall. As depicted in Fig. 6a, the presence of a solute and a wall generates excluded volumes (EVs) which are inaccessible to the centers of solvent particles. Upon contact, the two EVs overlap (the overlapping volume  $\Delta V$  ( $\Delta V > 0$ ) is colored pink), and the total EV decreases by  $\Delta V$  and the total volume available for the translational displacement of solvent particles in the system,  $V$ , increases by  $\Delta V$  ( $\Delta V/V \ll 1$ ). Applying the expression for the ideal-gas entropy to the solvent entropy, we can formulate the gain of translational, configurational entropy of the solvent upon contact,  $\Delta S^\circ$ , as  $\Delta S^\circ = k_B N_S \Delta V/V$  ( $k_B$  and  $N_S$  denote the Boltzmann constant and the total number of solvent particles in the system, respectively).<sup>48</sup> Expressing  $\Delta V$  by  $d_U$  and  $d_S$ , we obtain

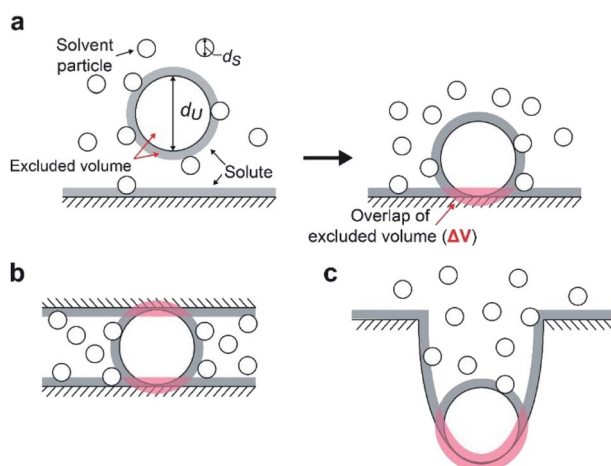
$$\Delta S^\circ = k_B N_S (\Delta V/V) = \{3(d_U/d_S) + 1\} \eta_S k_B, \quad \eta_S = \pi d_S^3 \rho_S/6, \quad \rho_S = N_S/V \quad (1)$$

where  $\eta_S$  is the packing fraction of solvent (the total volume occupied by  $N_S$  solvent particles divided by  $V$ ) which is a measure expressing how the solvent is dense. Importantly,  $\Delta S^\circ$  increases as  $d_U$  and  $\eta_S$  become larger and higher, respectively, and  $d_S$  becomes smaller. Upon contact, the free energy of solvent decreases by  $\Delta G^\circ = -T\Delta S^\circ$  ( $T$  is the absolute temperature). Due to this effect, the solute is entropically attracted to the wall (*i.e.*, an entropic force acts on the solute). Consequently, the solutes are enriched near the wall surface, and the number density of solutes at the surface divided by that in the bulk solvent,  $\chi$ , can be expressed as<sup>48</sup>

$$\chi = \exp\{-\Delta G^\circ/(k_B T)\}, \quad \Delta G^\circ < 0. \quad (2)$$

We emphasize that  $\Delta G^\circ$  is proportional to  $\Delta V$ . Due to the exponential dependence of  $\chi$  on  $|\Delta G^\circ|$ ,  $\chi$  can be much higher than unity.

The entropic force was referred to as the “depletion force” in a series of pioneering works.<sup>49–52</sup> The forces considered were those induced between colloidal particles<sup>49–51</sup> or a colloidal particle and a glass surface<sup>52</sup> suspended in solution of macromolecules. In these works, however, water was treated as inert background. We remark that this treatment is valid only under



**Fig. 6** Conceptual cartoon illustrating the contact of a substrate within a domain confined between two enzymes. An excluded volume (EV) is marked in grey. Upon contact, the total EV is reduced by the overlapping volume (in pink). (a) A hard-sphere solute with diameter  $d_U$  coming in contact with a planar hard wall. The solvent is formed by small hard spheres with diameter  $d_S$  ( $d_U > d_S$ ). (b) A hard-sphere solute in contact with two planar hard walls. (c) A hard-sphere solute in contact with a portion of a hard wall possessing concave surface.



a special solution condition in a colloidal system and usually inapplicable to a biological system.<sup>47</sup>

When a solute comes in contact with two walls as shown in Fig. 6b,  $\Delta V$  and  $|\Delta G^\circ|$  become twice larger than those in the contact shown in Fig. 6a, respectively. We note that  $\Delta V$  is largely dependent on the surface curvature of the wall. When a solute comes in contact with a portion of a wall possessing concave surface, for example,  $\Delta V$  can be even larger than that in Fig. 6b as illustrated in Fig. 6c.

### Application to enzyme–substrate–water system

In our system, the solvent, spherical solute, and wall in cartoons of Fig. 6 correspond to water, a substrate, and an enzyme, respectively. Water exists as dense liquid at ambient temperature and pressure due to hydrogen bonds despite its exceptionally small molecular size. For water,  $\eta_s$  is high though  $d_s$  is quite small, (refer to the section “Quantitative Analysis on Experimental Results Using Theoretical Model” below), leading to the largest EV effect among the ordinary liquids in nature. It has been shown that the water-entropy gain is a principal driving force of a variety of biological self-assembly processes.<sup>45–47,53</sup>

First, we consider Ori-D where only a single enzyme is present. Applying eqn (1) and (2) to the case where the solvent is water ( $d_s = 0.28$  nm and  $\eta_s = 0.383$ ) and the substrate is *p*-NPA ( $d_u \sim 0.8$  nm), we obtain  $\Delta S^\circ \sim 3.7$   $k_B$ ,  $\Delta G^\circ \sim -2.2$  kcal mol<sup>−1</sup>, and  $\chi \sim 40$  (refer to the section “Quantitative Analysis on Experimental Results Using Theoretical Model” below). An entropic force, which originates from the translational displacement of water molecules, acts on a substrate. This force drives the substrate to come in contact with the enzyme surface and enriches the substrates near it.

### Difference between Ori-D and Ori-P

We then consider Ori-P where two out of four enzymes are put close together. Here,  $\Delta V_1$  and  $\Delta V_2$  denote the increases in the total volume available for water molecules occurring when a substrate comes in contact with a single enzyme surface and with two enzyme surfaces, respectively. Hereafter, the subscripts “1” and “2” denote Ori-D and Ori-P, respectively. If Fig. 6 is applicable,  $\Delta V_2 = 2\Delta V_1$ . In the real system, however, the substrate and the enzyme possess polyatomic structures and the enzyme structure fluctuates to a large extent. Moreover, only small portions of the enzyme surfaces are close to each other. As a consequence, on an average,  $\Delta V_2$  is considerably smaller than  $2\Delta V_1$ . Nevertheless,  $\Delta V_2$  is larger than  $\Delta V_1$  as far as the surface separation between two enzymes is sufficiently small (*i.e.*, as small as the EV of the substrate) and we can write  $\Delta V_2 = \xi\Delta V_1$  ( $\xi > 1$ ) and  $\Delta G_1^\circ = \xi\Delta G_2^\circ$ . Applying eqn (2) to Ori-D and Ori-P yields

$$\chi_1 = \exp\{-\Delta G_1^\circ/(k_B T)\}, \quad (3a)$$

$$\chi_2 = \exp\{-\Delta G_2^\circ/(k_B T)\} = \exp\{-\xi\Delta G_1^\circ/(k_B T)\}, \quad (3b)$$

$$\chi_2/\chi_1 = \exp\{-\Delta G_1^\circ(\xi - 1)/(k_B T)\}. \quad (3c)$$

$\chi_2/\chi_1$ , the degree of substrate enrichment in Ori-P relative to that in Ori-D, is an increasing function of  $|\Delta G_1^\circ|$ . In the ideal case of Fig. 6,  $\xi = 2$  with the result of quite a large value of  $\chi_2/\chi_1$ . However, this is not realized in our system as mentioned above. Nevertheless, since  $\Delta G_1^\circ < 0$  and  $\xi > 1$ ,  $\chi_2/\chi_1$  is larger than unity. For a substrate concentration in the bulk aqueous solution given, it can be considered that the initial reaction velocity of esterase reaction increases in proportion to the degree of substrate enrichment near the enzyme surface. Thus,  $\chi_2/\chi_1 > 1$  leads to the acceleration of esterase reaction rate in Ori-P and the enhanced activity of ZS-CA as observed in our experiments. As argued in later sections, the increase of EV of the substrate or the addition of Na<sub>2</sub>SO<sub>4</sub> increases  $|\Delta G_1^\circ|$ , leading to larger  $\chi_2/\chi_1$  for  $\xi > 1$  ( $\xi$  can be considered almost unchanged for an enzyme species given. Refer to the section “Quantitative Analysis on Experimental Results Using Theoretical Model” below.)

We note that the substrate-active site binding corresponds to the event illustrated in Fig. 6c. Upon occurrence of the substrate enrichment near an enzyme surface or within the domain confined between two enzyme surfaces, a substrate, which can move along the enzyme surface, can reach the active site of the enzyme.<sup>54</sup> In Ori-P, the active site need not be within the domain confined between two enzyme surfaces. The essentially no differences among Ori-side, Ori-diagonal, and Ori-face in terms of the enhanced enzyme activity (Fig. 3e), which were observed in our experiments, is attributable to the large fluctuation of the enzyme structure.

### Effect of substrate species

Though the entropic EV (water-entropy) effect is highlighted in the above arguments, in the real system not only this entropic factor but also the energetic one comes into play. Therefore,  $\Delta G_1^\circ$  in eqn (3) is influenced by the energetic factor as well. The equation,  $\Delta G_1^\circ = -T\Delta S_1^\circ$ , does not hold but eqn (2) and (3) still hold. Entropically, a substrate is always attracted to an enzyme surface, promoting the substrate enrichment near the surface.<sup>55</sup> On the other hand, a substrate with high energetic affinity for water (*i.e.*, with high polarity) prefers to be hydrated in the bulk aqueous solution, opposing the substrate enrichment.<sup>56</sup> The opposite is true for a substrate with low affinity for water, cooperating with the entropic enrichment. In general, solutes are more enriched near the surface as the solute hydrophobicity becomes higher. With an increase in the solute EV or a decrease in the energetic affinity for water, the solute becomes more hydrophobic. The entropic factor usually dominates, but this is not true for a highly hydrophilic solute:  $\Delta G_1^\circ$  can take a small, positive value for the latter.

The three substrates, *p*-NPA, *p*-NPB, and *p*-NPV, are rather hydrophobic. Hence, the water-entropy effect dominates and becomes larger as the EV increases ( $d_u$  in eqn (1) corresponds to the substrate size, but for polyatomic substrates, the EV is physically more reasonable than the size in discussing the substrate hydrophobicity and the water-entropy effect). The EV follows the order, *p*-NPA < *p*-NPB < *p*-NPV (Fig. 4b). The enrichment of substrates described above becomes stronger in the same order.  $|\Delta G_1^\circ|$  ( $\Delta G_1^\circ$  is negative and considerably large





for the three substrates) and  $\chi_2/\chi_1$  in eqn (3) follow the order,  $p$ -NPA <  $p$ -NPB <  $p$ -NPV, which is in accord with our experimental observations.

The results obtained by reactions of ZS-XR assembled on Ori-D and Ori-P can be interpreted as follows (refer to “Summary of Interpretation of Experimental Results” for more details). ZS-XR showed higher initial reaction rate in the packed state than in the dispersed state (Fig. 5b). In water, the solubility of NADH is lower than that of D-xylose by a factor of  $\sim 1/50$ ,<sup>57,58</sup> manifesting the rather hydrophobic nature of NADH. This suggests that the acceleration of reaction in Ori-P over Ori-D is attributable to the enrichment of NADH within the domain confined between enzyme surfaces.

### Behaviour of reaction products

We comment on the behavior of products of the esterase reaction for  $p$ -NPA,  $p$ -NP and acetate.  $p$ -NP is less hydrophobic than  $p$ -NPA and acetate is hydrophilic. Hence,  $\Delta G_1^\circ$  for  $p$ -NP should be negative but smaller than that for  $p$ -NPA, and  $\Delta G_1^\circ$  for acetate can be very small (and possibly positive). Therefore, the enrichment of  $p$ -NP near the enzyme surface is less promoted than that of  $p$ -NPA, and that of acetate is not promoted.

In general, whether solutes come in contact with the surface or dissociate from the surface is dependent on not only  $\Delta G_1^\circ$  but also the solute concentration (or number density) in the bulk aqueous solution.  $\chi_1$  in eqn (3a) is the solute concentration at the surface ( $\rho_{\text{Surface}}$ ) divided by that in the bulk aqueous solution ( $\rho_{\text{Bulk}}$ ). Negative  $\Delta G_1^\circ$  implies that  $\rho_{\text{Bulk}}$  is lower than  $\rho_{\text{Surface}}$  (e.g.,  $\rho_{\text{Surface}}/\rho_{\text{Bulk}} \sim 40$  for  $\chi_1 \sim 40$ ). We note that  $\rho_{\text{Bulk}}$  of  $p$ -NP or acetate in the bulk aqueous solution is very low in our experiments. Therefore, upon production of  $p$ -NP and acetate by the reaction, they favorably dissociate from the enzyme surface. Thus, even the dissociation of hydrophobic reaction products is not hindered by the water-entropy effect as long as their concentrations in the bulk aqueous solution are sufficiently low.

### Effect of salt addition

Strongly hydrated ions with high charges and/or small sizes prefer to be present in the bulk water. They are not likely to come in contact with an oppositely charged portion of a solute immersed in water, because it is difficult to dehydrate the ions. For the activation of the CA-catalyzed hydrolysis of  $p$ -NPA in the presence of high concentrations of  $\text{Na}_2\text{SO}_4$ , it was suggested that the effect of ionic strength on the chemical potential of the substrate caused an increase in apparent affinity of the substrate for the active site.<sup>39</sup> The addition of  $\text{Na}_2\text{SO}_4$  produces strongly hydrated ions  $\text{SO}_4^{2-}$  and causes a volume reduction at a constant pressure and higher  $\eta_s$ , leading to an enhanced water-entropy effect.<sup>59,60</sup> Therefore, the addition of  $\text{Na}_2\text{SO}_4$  results in stronger enrichment of substrates for any portion of the enzyme surface and larger  $|\Delta G_1^\circ|$  followed by higher values of  $\chi_1$  and  $\chi_2$  (also by higher  $\chi_2/\chi_1$  for  $\xi > 1$ ). That is, the esterase reaction rate is accelerated upon  $\text{Na}_2\text{SO}_4$  addition not only in Ori-D but also in Ori-P, especially in the latter. These are also in accord with our experimental observations that the esterase

reaction rate becomes about 2.0 times higher in Ori-D and Ori-P when  $\text{Na}_2\text{SO}_4$  is added in a concentration of 0.5 M. The effect of  $\text{Na}_2\text{SO}_4$  addition can be explained even in a quantitative sense as described in the section “Quantitative Analysis on Experimental Results Using Theoretical Model”.

On the other hand, only weakly hydrated ions with low charges and/or large sizes can be dehydrated without difficulty and tend to come in contact with an oppositely charged portion of a solute immersed in water.  $\text{Br}^-$ , for example, preferentially contacts  $\text{Zn}^{2+}$  in the active site of CA (this is not the case for  $\text{SO}_4^{2-}$ ), thus acting as an inhibitor for CA. This is why the addition of  $\text{NaBr}$  decelerates the reaction rate as observed in our experiments.

### Quantitative analysis on experimental results using theoretical model

Our basic strategy of the quantitative analysis, which is performed for ZS-CA and  $p$ -NPA, is as follows:

- (1) Using the parameter values pertinent to our system ( $d_s = 0.28$  nm,  $d_U \sim 0.8$  nm,  $\eta_s = 0.383$ , and  $T = 298$  K), we calculate  $\Delta G_1^\circ$  ( $\Delta G^\circ$  in eqn (2)).
- (2) Using the experimental result,  $\chi_2/\chi_1 \sim 1.3$ , we estimate  $\xi$  in eqn (3c).
- (3) Upon addition of  $\text{Na}_2\text{SO}_4$  (0.5 M/L),  $\eta_s$  increases to 0.419.<sup>61</sup> From the resultant increase in  $\Delta G_1^\circ$ , we calculate  $\Delta G_1^{**}$ ,  $\chi_1^*/\chi_1$ , and  $\chi_2^*/\chi_2$  where the superscript “\*” denotes the value after the salt addition ( $\eta_s^* = 0.419$ ). It is assumed that  $\xi$  remains unchanged upon the salt addition. The calculated values are compared to our experimentally measured values.

We obtain  $\Delta G_1^\circ \sim -2.17$  kcal mol<sup>-1</sup> in (1) and  $\xi \sim 1.08$  in (2) (unfortunately,  $\xi$  is much smaller than the ideal value 2). According to eqn (1),  $|\Delta G^\circ|$  increases in proportion to  $\eta_s$ . However, our more rigorous theory based on statistical mechanics<sup>55</sup> suggests that  $|\Delta G^\circ|$  is more strongly dependent on  $\eta_s$ : when  $\eta_s$  increases further from the value pertinent to water, 0.383,  $|\Delta G^\circ|$  becomes larger in approximate proportion to  $\eta_s^2$ . Using this more rigorous dependence of  $|\Delta G^\circ|$  on  $\eta_s$ , we obtain  $\chi_1^*/\chi_1 \sim 2.1$  and  $\chi_2^*/\chi_2 \sim 2.2$  as the theoretical predictions. On the other hand, our experimentally measured values are  $\chi_1^*/\chi_1 \sim 2.0$  and  $\chi_2^*/\chi_2 \sim 2.0$ . We can conclude that the effects of addition of  $\text{Na}_2\text{SO}_4$  can well be explained by our theory even in a quantitative sense.

### Comments on dynamic aspect of system behaviour

We emphasize that all the water molecules in the system, i.e., not only the water molecules near the enzyme surface but also those in the bulk aqueous solution contribute to the water-entropy effect. The contribution from the latter is much larger.<sup>45</sup> It is experimentally and theoretically known that the water dynamics is extremely fast and the relaxation (e.g., the structure formation of water near a protein surface) occurs on a picosecond time scale at room temperature.<sup>62</sup> Water molecules are supplied in pico seconds upon their consumption by the reaction at the enzyme surface. Hence, neither the participation of water in the reaction nor the consumption of water influences the water-entropy effect.



The substrate dynamics should be somewhat slower than the water dynamics. The thermodynamic quantities,  $S^\circ$  and  $G^\circ$  are introduced to analyze the layer formed near the enzyme surface within which substrates are enriched (the above discussion is focused on the enrichment at the surface). A question then arises: How long will it take for the layer to be formed? Rather hydrophobic substrates are attracted to the enzyme surface through the force which becomes progressively stronger as the distance from the surface  $x$  decreases.<sup>58</sup> That is, the substrates are driven to move toward the surface by acceleration which increases with decreasing  $x$ . Even when the effect of the force is not taken into account, the time required for the substrates to reach the surface can be estimated to be only  $10^{-8}$  s as explained in what follows. The thickness of the layer  $l$  within which substrates are enriched is only several times of the substrate size. When the substrate is *p*-NPA with a size of  $\sim 0.8$  nm, for example,  $l \sim 4$  nm. The diffusion length ( $\sim$ the average distance by which substrates can move in  $t$  s)  $L$  is related to the diffusion coefficient of substrates  $D$  as  $L^2 = 2Dt$ . Substituting  $L = l = 4$  nm and  $D = 10^{-5}$  cm<sup>2</sup> s<sup>-1</sup> (this is the value for benzene<sup>63</sup>) in this equation yields  $t \sim 10^{-8}$  s. In reality, the substrates are strongly attracted to the enzyme surface as mentioned above. It follows that the substrates reach the surface in  $10^{-8}$  s or much faster (*i.e.*, almost instantaneously). Upon the consumption of substrates near the surface by the chemical reaction, the supply of substrates is also completed almost instantaneously. We can conclude the following: when a physical or chemical process occurring on a many orders of magnitude longer time scale such as the enzymatic reaction is considered, it is rationalized to assume that the equilibrium concentration profile of substrates is always formed near the surface.

### Summary of interpretation of experimental results

Strongly hydrated ions ( $\text{SO}_4^{2-}$  and  $\text{Mg}^{2+}$ ), somewhat strongly hydrated ions ( $\text{Na}^+$  and  $\text{Cl}^-$ ), and highly hydrophilic solutes such as HEPES are enriched neither near the enzyme surface nor within the domain confined between enzyme surfaces. Unless the substrate is highly hydrophilic, the local concentration of substrates becomes higher within the confined domain in Ori-P than near the single enzyme in Ori-D or free in solution, leading to a higher initial reaction velocity. The water-entropy effect is enhanced upon addition of a salt whose ions are strongly hydrated, such as sulfate ions ( $\text{SO}_4^{2-}$ ), through modification of the bulk water structure. In the presence of 0.5 M  $\text{Na}_2\text{SO}_4$ , the initial reaction velocity was increased in all cases, *i.e.*, free solution, on Ori-D, and on Ori-P as discussed in the section "Quantitative Analysis on Experimental Results Using Theoretical Model". Due to the water-entropy effect, the apparent affinity of the substrate increases for any portion of the enzyme surface, accelerating the esterase reaction in the presence of strongly hydrated  $\text{SO}_4^{2-}$ .

$\Delta V_1$ ,  $\Delta V_2 = \xi \Delta V_1$  ( $\xi > 0$ ),  $|\Delta G_1^\circ|$ , and  $\chi_2/\chi_1$  increase as the EV of substrate becomes larger. With *p*-NPA as the substrate, the reaction was accelerated only 1.3 times on Ori-P over Ori-D, but 1.5 and 1.6 times with *p*-NPB and *p*-NPV, respectively. The

substrate enrichment is strengthened for a more hydrophobic substrate, leading to larger  $\chi_2/\chi_1$ . This notion is corroborated in Fig. 4b where the fold enhancement of initial velocity of ZS-CA on Ori-D over that on Ori-P (acceleration factors corresponding to  $\chi_2/\chi_1$ ) for the three substrates are plotted against the EV (Fig. 4b).

The sensitivity of the enzyme to inhibitory molecules or ions such as weakly hydrated, large halide anions (*i.e.*,  $\text{Br}^-$  and  $\text{I}^-$ ) and sulfonamides should be different depending on its assembly state. In the presence of 1 M NaBr, the initial velocities of *p*-NPA hydrolysis reactions by ZS-CA on Ori-D and Ori-P were reduced in all cases. Interestingly, the initial velocity of ZS-CA on Ori-P was 2.1 times higher than that on Ori-D or in free solution in the presence of 1 M NaBr (Fig. 4c). Considering the 1.5 times enhancement for the reaction of ZS-CA on Ori-P in the absence of bromide ion, ZS-CA on Ori-P tolerated better the inhibitory effect of bromide than ZS-CA on Ori-D or in free solution. Inhibition of the esterase reactions by increasing concentrations of acetazolamide also indicated the lower sensitivity of ZS-CA on Ori-P to the inhibitor at up to 100 nM (Fig. 4d). Acetazolamide is a competitive inhibitor to carbonic anhydrase activity<sup>43</sup> and has lower hydrophobicity than the substrate *p*-NPA. By following our theory of the water-entropy effect, even in the presence of acetazolamide, enrichment of the more hydrophobic substrate *p*-NPA is favored over acetazolamide on the surface of packed state of enzyme. Taken together, the sensitivity of the esterase reaction to inhibitory molecules or ions varies depending on the assembled state of ZS-CA, which can reasonably be explained by the substrate enrichment near the enzyme surface driven by the entropic force.

The results obtained by reactions of ZS-XR assembled on Ori-D and Ori-P can be explained as follows. ZS-XR showed higher initial reaction rate in the packed state than in the dispersed state (Fig. 5b). Due to the rather hydrophobic nature of NADH over D-xylose, it can be suggested that the enrichment of NADH is responsible for the observed acceleration. Based on the hypothesis of substrate enrichment for the enzymes on Ori-P, the activity enhancement for the packed state of enzyme should be more prominent at low substrate concentrations. In fact, the activity enhancement is more prominent at low cofactor concentrations for XR as revealed by the reactions of ZS-XR/Ori-P and ZS-XR/Ori-D (Fig. S16†). Kinetic analyses by the Michaelis–Menten model (Fig. S17†) formally provided kinetic parameters for ZS-XR in the packed and the dispersed states. The  $K_m$  varied little between the packed and the dispersed states for both D-xylose and NADH, while the turn-over number ( $k_{\text{cat}}$ ) was higher in the packed state than in the dispersed state. However, we speculate that the general Michaelis–Menten kinetic equation is not applicable for evaluation of the kinetic data for packed state of enzyme. The increase in local substrate concentration could only increase the enzymatic activity when the substrate concentration is unsaturated. Such a reaction condition is not assumed for the general Michaelis–Menten kinetic analyses. Therefore, it would be irrelevant to have a preconceived idea for the Michaelis–Menten constants on this reaction system. Further analyses on various types of enzymatic reactions in the packed state would address this issue.



We emphasize that all the water molecules in the system, *i.e.*, not only the water molecules near the enzyme surface but also those in the bulk aqueous solution contribute to the water-entropy effect. The contribution from the latter is much larger.<sup>45</sup> Moreover, the water dynamics is extremely fast, and water molecules are supplied in pico seconds upon their consumption by the reaction at the enzyme surface. Hence, neither the participation of water in the reaction nor the consumption of water influences the water-entropy effect. As for the reaction products, they rapidly dissociate from the enzyme surface as explained above, and they are not likely to influence the water-entropy effect.

## Conclusion

In this study, the packed state of a single type of enzyme contributes to acceleration in the esterase reaction of CA or in the NADH dependent production of xylitol from xylose over those in the dispersed state. Moreover, in the packed state, the reaction proceeds faster for substrates with larger EVs and is more tolerant of inhibitors. We interpreted these results as follows: the reaction for the packed state of enzyme is accelerated by increasing the local concentration of substrate or cofactor within the domain confined between enzyme surfaces. The acceleration of an enzymatic reaction in the packed state over the dispersed one is ubiquitous as long as a component, either a substrate or a cofactor, participating in the reaction is rather hydrophobic and the distance between two enzyme surfaces in the packed state is comparable with the size of this component. Due to the entropic force, this component is enriched near an enzyme surface and even more enriched within the domain confined between enzyme surfaces, which is responsible for the acceleration. The entropic force originates from the translational displacement of water molecules in the entire system. Our finding offers a new insight on the efficiency of enzymatic reactions in the packed state. The water-entropy effect increases as the enzyme structure becomes less flexible in the packed assembly. Therefore, a greater effect is expected within the spatially constrained cellular compartments consisting of multiple types of enzymes, such as the possible internal packed assembly of proteins recently reported for the formation of liquid-like matrix of enzyme condensates inside the carboxysome.<sup>9</sup> The controlled packed assembly of enzymes could be used to determine which ones are impacted by the packed state, particularly with respect to acceleration of reactions and interactions with particular substrates. In addition, our designed system enables us to investigate the reaction of not only the same type of enzyme but also that of different types of enzymes, and the ligand binding of receptors in reasonably packed states.

## Materials and methods

### Materials

The single-stranded M13mp18, restriction enzymes (*NdeI* and *NotI*) and BG-GLA-NHS (S9151S) were purchased from New England Biolabs. Purified oligonucleotide as the staple strands

for DNA origami, oligonucleotide primers for gene construction and all other oligonucleotides were purchased from Sigma-Aldrich (St. Louis, MO), Thermo Fisher Scientific Inc. (Waltham, MA, USA), Japan Bio Services Co., LTD (Saitama, Japan) and Gene Design Inc. (Osaka, Japan). Human Kidney QUICK-Clone™ cDNA was purchased from TaKaRa Bio Inc. (Shiga, Japan). *E. coli* BL21 (DE3) competent cells were purchased from Invitrogen (Carlsbad, CA). Mini Elute Gel Extraction Kit was purchased from QIAGEN (Tokyo, Japan). HiTrap SP HP column (5 ml), HiTrap HP column (5 ml) and Sephacryl S-400 were purchased from GE Healthcare Japan Inc. (Tokyo, Japan). PrimeSTAR HS DNA polymerase, T4 DNA ligase, and *E. coli* DH5 $\alpha$  competent cells were purchased from TaKaRa Bio Inc. (Shiga, Japan). Ultrafree-MC-DV were purchased from Merck Millipore (Darmstadt, Germany). *p*-Nitrophenyl acetate (*p*-NPA), *p*-nitrophenyl butyrate (*p*-NPB) and *p*-nitrophenyl valerate (*p*-NPV) were purchased from Sigma Aldrich and used without further purification. Connolly solvent excluded volumes calculated by using Chem3D (ver.19, CambridgeSoft) were used as excluded volume (EV). Tetramethylammonium bromide, sodium bromide, and acetazolamide were purchased from Sigma Aldrich.

### Construction of a vector for ZS-CA

Human carbonic anhydrase II gene from Human Kidney QUICK-Clone™ cDNA and a modular adaptor ZS gene in pET-30a-ZF-SNAP vector<sup>30</sup> were amplified by PCR using the primer pairs provided in Table S1.† The PCR products were run on a 1% agarose gel in a buffer (pH 8.3) containing 40 mM Tris-HCl, 20 mM acetic acid and 1 mM EDTA and were purified by Mini Elute Gel Extraction Kit. The PCR products and pET-30a were digested with *NdeI* and *NotI* and were purified separately in the same manner. These products were incubated with T4 DNA ligase then transformed into *E. coli* DH5 $\alpha$  competent cells for amplification. The purity and sequence of vector encoding ZS-CA (termed as pET-30a-ZS-CA) were confirmed and transformed into *E. coli* BL21(DE3) competent cells. As a control, the gene of human carbonic anhydrase II with histidine tag at the N-terminus was also introduced into pET-30a vector digested with *NdeI* and *NotI* in the similar manner. Purified vector pET-30a-hCAII was transformed into *E. coli* BL21(DE3) for protein expression.

### Overexpression and purification of ZS-CA

The transformed cells were grown at 37 °C until OD<sub>600</sub> reached 0.5, and protein expression was induced with 1 mM IPTG for 24 h at 25 °C. The soluble fraction of the cell lysate containing ZS-CA was loaded to a HiTrap HP column in a buffer (pH 7.5) containing 100 mM Tris-HCl, 200 mM NaCl, 5 mM  $\beta$ -mercaptoethanol, 100  $\mu$ M ZnCl<sub>2</sub> and 20 mM imidazole, and eluted using gradient imidazole elution (concentrations from 20 to 500 mM). The main fractions containing ZS-CA were collected and loaded to a HiTrap SP HP column in a buffer (pH 7.2) containing 50 mM HEPES, 5 mM  $\beta$ -mercaptoethanol, and 100  $\mu$ M ZnCl<sub>2</sub>; these were then eluted by NaCl gradient. The purified ZS-CA was dialyzed by using a buffer (pH 7.2) containing 50 mM HEPES, 200 mM NaCl, 5 mM  $\beta$ -mercaptoethanol, 100  $\mu$ M ZnCl<sub>2</sub>,





and 50% glycerol and stored at  $-20\text{ }^{\circ}\text{C}$ . The purity of ZS-CA was checked by SDS-polyacrylamide gel electrophoresis (PAGE). The major band in SDS-PAGE (Fig. S1†) corresponded to the calculated molecular weight of ZS-CA (62 934 Dalton) with purity over 95% (calculated from ImageJ). Amino acid sequence of ZS-CA was shown in Fig. S1b.† Similarly, the parent carbonic anhydrase with histidine tag at the N-terminus (hCAII) in the vector pET-30a-hCAII was expressed and purified. Esterase activities of ZS-CA and hCAII were compared (Fig. S2†). The binding ability of ZS-CA to the specific binding DNA sequence and kinetic parameters were confirmed (Fig. S3†).

### Enzyme kinetics of ZS-CA

Assays for esterase activity of ZS-CA and substrates *p*-nitrophenyl acetate (*p*-NPA), *p*-nitrophenyl butyrate (*p*-NPB), *p*-nitrophenyl valerate (*p*-NPV) were carried out in 100  $\mu\text{L}$  volume of 96-well non-binding plate (corning), using a variety of enzyme and substrate concentrations. An acetonitrile solution of each substrate (100 mM) was freshly prepared for each experiment. Due to the low solubility of *p*-NPA in the buffer, the maximum concentration of *p*-NPA in reaction was set to 1 mM. Final concentration of acetonitrile in the reaction mixture was kept to 1% in all experiments unless otherwise noted. Reactions were monitored at 384 nm (isosbestic point of *p*-nitrophenol and *p*-nitrophenolate) with the extinction coefficients of  $5.0 \times 10^3\text{ M}^{-1}\text{ cm}^{-1}$  or at a maximum of absorbance at 400 nm (at pH 7.6) with the extinction coefficients of  $1.28 \times 10^4\text{ M}^{-1}\text{ cm}^{-1}$ .<sup>34</sup> The rate of spontaneous hydrolysis without enzyme was subtracted from the enzymatic initial rate. A buffer (pH 7.6) containing 50 mM HEPES was chosen for the high reaction rate and the low spontaneous hydrolysis rate. The reaction mixture was composed of a buffer (pH 7.6) containing 50 mM HEPES, 12.5 mM  $\text{MgCl}_2$ , 1% acetonitrile, 1  $\mu\text{M}$   $\text{ZnCl}_2$  and 0.001% Tween 20 with 1 mM *p*-NPA and 4 nM ZS-CA in assembly with DNA scaffold or in free solution (Fig. 2c) or 6 nM of DNA origami (with ZS-CA assembly) (Fig. 3e). ZS-CA (5.5 nM) and 1 mM *p*-NPA (Fig. 4a and d) or 0.1 mM *p*-NPA (Fig. 4c) were used in the reactions. In Fig. 4b, due to the even lower solubility of substrates *p*-NPB and *p*-NPV, all substrates (*p*-NPA, *p*-NPB and *p*-NPV) were prepared in 100% acetone and the reactions were carried out with 23 nM of ZS-CA and 0.1 mM substrates with 5% acetone instead of 1% acetonitrile.

### Preparation of the DNA scaffold

A solution (50  $\mu\text{L}$ ) containing M13mp18 single-stranded DNA (20 nM) and mixture of staple DNA strands (100 nM) of each staple strands, all of the staple strand sequences were shown in the previous report<sup>31</sup> in a buffer (pH 8.0) containing 40 mM Tris-HCl, 20 mM acetic acid, 12.5 mM  $\text{MgCl}_2$  was heated at  $95\text{ }^{\circ}\text{C}$  for 1 min, incubated at  $53\text{ }^{\circ}\text{C}$  for 30 min, and then cooled down to  $4\text{ }^{\circ}\text{C}$  by using a thermal cycler (C1000 Thermal Cycler, BioRad). The sample was purified to remove excess staple strands by gel filtration (500  $\mu\text{L}$  in volume of Sephacryl S-400) in Ultrafree-MC-DV column. The concentration of DNA scaffold was quantified by absorbance at 260 nm (the molar absorbance coefficient of DNA scaffold:  $\varepsilon_{\text{DNA scaffold}} = 1.27 \times 10^8\text{ M}^{-1}\text{ cm}^{-1}$ ).

### Preparation of DNA scaffold assembled with ZS-CA

A typical binding reaction of the purified DNA scaffold and ZS-CA was conducted with 16 nM DNA scaffold (64 nM binding site) and 200 nM ZS-CA in a buffer (pH 8.0) containing 40 mM Tris-HCl, 20 mM acetic acid, 12.5 mM  $\text{MgCl}_2$ , 1  $\mu\text{M}$   $\text{ZnCl}_2$ , 0.001% Tween 20, 5 mM  $\beta$ -mercaptoethanol and 125 nM of staple strands mixture for DNA scaffold (without the staple strands containing ZS-CA binding site). After 30 min incubation on ice, the mixtures were filtered through 500  $\mu\text{L}$  bed volume of Sephacryl S400 to remove all the non-bound ZS-CA and to exchange with a buffer (pH 7.6) containing 50 mM HEPES, 12.5 mM  $\text{MgCl}_2$  for enzymatic assay.

### Atomic force measurement (AFM) imaging and statistical analysis

The purified sample solution was deposited on a freshly cleaved mica (1.5 mm in diameter) surface, adsorbed for 5 min at ambient temperature, and then washed three times with a buffer (pH 8.0) containing 40 mM Tris-HCl, 20 mM acetic acid, 12.5 mM  $\text{MgCl}_2$ . The sample was scanned in solution with tapping mode using a fast-scanning AFM system (Nano Live Vision, RIBM Co. Ltd, Tsukuba, Japan) with a silicon nitride cantilever (Olympus BL-AC10DS-A2). At least three independent preparations of each sample were analysed by AFM, and several images were acquired from different regions of the mica surface. The total number of DNA scaffold corresponds to the number of expected rectangular shape possessing five cavities observed by AFM. The specific and non-specific binding of ZS-CA were counted only for the perfectly folded DNA scaffold.<sup>30</sup>

The yield of specific ZS-CA loaded DNA cavities ( $P_{\text{specific}}$ ) was calculated as the percentage of the number of cavity containing ZS-CA molecules at the expected positions ( $N_{\text{expected pos}}$ ), e.g., centre cavity in the case of Ori-P, over the total number of 'specific' cavities (bearing binding sites) from only well-formed DNA scaffolds ( $1 \times N_{\text{total}}$  for Ori-P with  $N_{\text{total}}$  is the number of well-formed DNA scaffolds):

$$P_{\text{specific}} = (N_{\text{expected pos}}/N_{\text{total}}) \times 100$$

The yield of ZS-CA-loaded DNA cavities at the unexpected positions ( $P_{\text{nonspecific}}$ ) was calculated as the percentage of cavity containing ZS-CA molecules resided non-specifically ( $N_{\text{unexpected pos}}$ ), e.g., other cavities beside the centre cavity in the case of Ori-P, over the total number of 'non-specific' cavities (without any binding sites) of well-formed DNA scaffold ( $4 \times N_{\text{total}}$  for Ori-P):

$$P_{\text{non-specific}} = (N_{\text{unexpected pos}}/4N_{\text{total}}) \times 100$$

### Volume analysis of AFM images

AFM images of ZS-CA bound on DNA scaffold were analysed by using SPIP™ software (ver. 6.2.8, Image Metrology). First, the image was flattened then the z-volume value (defined as the volume of all pixels inside the shape's contour with a Z value) of



particles correspond to ZS-CA on DNA scaffold was collected. The volume data were displayed as a histogram plot and each fraction was analysed by means of non-linear curve fit on a software (Origin Pro, ver. 9.1).<sup>30</sup>

### Calculating the inter-enzyme distance of ZS-CA in solution

The average distance separating molecules in solution was calculated as a function of molar concentration.<sup>64</sup> In a 1 M enzyme solution, there are  $6 \times 10^{23}$  molecules per litre ( $0.6$  molecules per  $\text{nm}^3$ ) or inverting, the volume per molecule is  $V = 1.66 \text{ nm}^3$  per molecule at 1 M. Therefore, for a concentration  $C$ , the volume per molecule is  $V = 1.66/C$ . By taking the cube root of the volume per molecule, the average distance ( $d$ ) is obtained from the equation:

$$d = V^{1/3} = 1.18/C^{1/3}$$

where  $C$  is in molar and  $d$  is in nanometre. In a solution containing 4 nM ZS-CA, the average distance between molecules is calculated to be 740 nm. When an enzyme solution has an average distance of enzyme molecules of 1 nm as in the case of ZS-CA in Ori-P, the concentration of enzyme in bulk condition is estimated to be 18 mM (the size of carbonic anhydrase with diameter of 3.5 nm was also considered).

### Estimating the concentration of DNA scaffold and DNA scaffold-protein complexes

To determine the molar absorbance coefficient of DNA scaffold, the recover yield of DNA scaffold after gel filtration was deduced by quantitation of DNA in the agarose gel electrophoresis band (Fig. S6†) by following this equation:

$$\text{Recovery yield (\%)} = \frac{\text{band intensity}_{(\text{after purification})}}{\text{band intensity}_{(\text{before purification})}}$$

The recovery yield of the first purification of DNA scaffold only was estimated to be 83% from the ratio of band intensities (lane 3/ lane 2). The recovery yield of the second purification after the binding reaction of DNA scaffold and ZS-CA was estimated to be 33% from the ratio of band intensities (lane 5/ lane 4). From the starting concentration of DNA scaffold (20 nM), the concentration of DNA scaffold after each purification process was calculated. In a typical case as shown in Fig. S6, ESI,† the concentration of DNA scaffold after the first purification was 17 nM and after second purification was 4 nM. The concentration of DNA scaffold was quantified by using a NanoDrop spectrophotometer (Thermo Fisher) at 260 nm. The molar absorbance coefficient of DNA scaffold after the first purification (lane 3) was  $\epsilon = 1.25 \times 10^8 \text{ M}^{-1} \text{ cm}^{-1}$ ; after the second purification (lane 5):  $\epsilon = 1.31 \times 10^8 \text{ M}^{-1} \text{ cm}^{-1}$ . The molar absorbance coefficient of ZS-CA was negligible to the value of DNA scaffold. The average of three experiments provided the molar absorbance coefficient of DNA scaffold ( $\epsilon = 1.27 \times 10^8 \text{ M}^{-1} \text{ cm}^{-1}$ ). The determined molar extinction coefficient is consistent with that of a fully double-stranded M13mp18 molecules (the calculated molar absorbance

coefficient is  $1.17 \times 10^8 \text{ M}^{-1} \text{ cm}^{-1}$  from website: <http://www.molbiotools.com/dnacalculator.html>).

The concentration of ZS-CA assembled on DNA scaffold was estimated as follow:

$$[\text{ZS-CA}] (\text{nM}) = n_{\text{ZS-CA}} \times \frac{\text{Abs}_{260 \text{ nm}}}{\epsilon_{\text{DNA scaffold}}} \times 10^9$$

where  $n_{\text{ZS-CA}}$  is the actual number of ZS-CA molecules bound to the specific binding sites on the DNA scaffold by volume analysis. In the case of Ori-D,  $n_{\text{ZS-CA}} = 3.1$ ; for Ori-P  $n_{\text{ZS-CA}} = 2.6$ .  $\text{Abs}_{260 \text{ nm}}$  is the absorbance at 260 nm of sample after purification.  $\epsilon_{\text{DNA scaffold}}$  is the molar absorbance coefficient of DNA scaffold ( $1.27 \times 10^8 \text{ M}^{-1} \text{ cm}^{-1}$ ).

### Enzyme Assay of ZS-XR

Catalytic activity of ZS-XR on DNA scaffold was analyzed by measuring the changes of absorbance at 340 nm (25 °C) derived from the oxidation of NADH with an Infinite 200 PRO microplate reader (TECAN Austria GmbH). The reaction was started with an addition of ZS-XR/Ori-D or ZS-XR/Ori-P to a mixture of 200 mM D-xylose, 300  $\mu\text{M}$  NADH in a buffer (pH 6.8) containing 50 mM HEPES, 12.5 mM  $\text{MgCl}_2$ , 100 mM NaCl, 1  $\mu\text{M}$   $\text{ZnCl}_2$ , and 0.001% Tween 20.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

This work was supported by JSPS KAKENHI Grant Numbers 17H01213 (T. M.) and 19H04653 (E. N.), and by JST CREST Grant Number JPMJCR18H5 (T. M.), Japan.

## References

- 1 C. A. Kerfeld, S. Heinhorst and G. C. Cannon, *Annu. Rev. Microbiol.*, 2010, **64**, 391–408.
- 2 K. Jørgensen, A. V. Rasmussen, M. Morant, A. H. Nielsen, N. Bjarnholt, M. Zagrobelny, S. Bak and B. L. Møller, *Curr. Opin. Plant Biol.*, 2005, **8**, 280–291.
- 3 A. H. Chen and P. A. Silver, *Trends Cell Biol.*, 2012, **22**, 662–670.
- 4 J. B. Thoden, H. M. Holden, G. Wesenberg, F. M. Raushel and I. Rayment, *Biochemistry*, 1997, **36**, 6305–6316.
- 5 D. R. Knighton, C. C. Kan, E. Howland, C. A. Janson, Z. Hostomska, K. M. Welsh and D. A. Matthews, *Nat. Struct. Biol.*, 1994, **1**, 186–194.
- 6 T. Gabaldón and A. A. Pittis, *Biochimie*, 2015, **119**, 262–268.
- 7 C. A. Kerfeld and O. Erbilgin, *Trends Microbiol.*, 2015, **23**, 22–34.
- 8 T. O. Yeates, C. A. Kerfeld, S. Heinhorst, G. C. Cannon and J. M. Shively, *Nat. Rev. Microbiol.*, 2008, **6**, 681–691.
- 9 H. Wang, X. Yan, H. Aigner, A. Bracher, N. D. Nguyen, W. Y. Hee, B. M. Long, G. D. Price, F. U. Hartl and M. Hayer-Hartl, *Nature*, 2019, **566**, 131–135.



- 10 J. M. Shively, F. Ball, D. H. Brown and R. E. Saunders, *Science*, 1973, **182**, 584–586.
- 11 C. V. Iancu, H. J. Ding, D. M. Morris, D. P. Dias, A. D. Gonzales, A. Martino and G. J. Jensen, *J. Mol. Biol.*, 2007, **372**, 764–773.
- 12 M. F. Schmid, A. M. Paredes, H. A. Khant, F. Soyer, H. C. Aldrich, W. Chiu and J. M. Shively, *J. Mol. Biol.*, 2006, **364**, 526–535.
- 13 A. Kuzmak, S. Carmali, E. von Lieres, A. J. Russell and S. Kondrat, *Sci. Rep.*, 2019, **9**, 1–7.
- 14 L. J. Sweetlove and A. R. Fernie, *Nat. Commun.*, 2018, **9**, 2136.
- 15 P. W. K. Rothmund, *Nature*, 2006, **440**, 297–302.
- 16 S. M. Douglas, H. Dietz, T. Liedl, B. Högberg, F. Graf and W. M. Shih, *Nature*, 2009, **459**, 414–418.
- 17 F. Zhang, J. Nangreave, Y. Liu and H. Yan, *J. Am. Chem. Soc.*, 2014, **136**, 11198–11211.
- 18 F. Hong, F. Zhang, Y. Liu and H. Yan, *Chem. Rev.*, 2017, **117**, 12584–12640.
- 19 J. Fu, M. Liu, Y. Liu, N. W. Woodbury and H. Yan, *J. Am. Chem. Soc.*, 2012, **134**, 5516–5519.
- 20 Z. Zhao, J. Fu, S. Dhakal, A. Johnson-Buck, M. Liu, T. Zhang, N. W. Woodbury, Y. Liu, N. G. Walter and H. Yan, *Nat. Commun.*, 2016, **7**, 10619.
- 21 T. A. Ngo, E. Nakata, M. Saimura and T. Morii, *J. Am. Chem. Soc.*, 2016, **138**, 3012–3021.
- 22 G. Ke, M. Liu, S. Jiang, X. Qi, Y. R. Yang, S. Wootten, F. Zhang, Z. Zhu, Y. Liu, C. J. Yang and H. Yan, *Angew. Chem., Int. Ed.*, 2016, **55**, 7483–7486.
- 23 T. M. Nguyen, E. Nakata, M. Saimura, H. Dinh and T. Morii, *J. Am. Chem. Soc.*, 2017, **139**, 8487–8496.
- 24 A. Rajendran, E. Nakata, S. Nakano and T. Morii, *ChemBioChem*, 2017, **18**, 696–716.
- 25 T. A. Ngo, H. Dinh, T. M. Nguyen, F. F. Liew, E. Nakata and T. Morii, *Chem. Commun.*, 2019, **55**, 12428–12446.
- 26 B. Sjöblom, M. Polentarutti, K. Djinoivic-Carugo, B. Sjöblom, M. Polentarutti and K. Djinoivic-Carugo, *Proc. Natl. Acad. Sci. U. S. A.*, 2009, **106**, 10609–10613.
- 27 V. M. Krishnamurthy, G. K. Kaufman, A. R. Urbach, I. Gitlin, K. L. Gudiksen, D. B. Weibel and G. M. Whitesides, *Chem. Rev.*, 2008, **108**, 946–1051.
- 28 N. P. Pavletich and C. O. Pabo, *Science*, 1991, **252**, 809–817.
- 29 A. Keppler, S. Gendreizig, T. Gronemeyer, H. Pick, H. Vogel and K. Johnsson, *Nat. Biotechnol.*, 2003, **21**, 86–89.
- 30 E. Nakata, H. Dinh, T. A. Ngo, M. Saimura and T. Morii, *Chem. Commun.*, 2015, **51**, 1016–1019.
- 31 E. Nakata, F. F. Liew, C. Uwatoko, S. Kiyonaka, Y. Mori, Y. Katsuda, M. Endo, H. Sugiyama and T. Morii, *Angew. Chem., Int. Ed.*, 2012, **51**, 2421–2424.
- 32 T. A. Ngo, E. Nakata, M. Saimura, T. Kodaki and T. Morii, *Methods*, 2014, **67**, 142–150.
- 33 H. Dinh, E. Nakata, P. Lin, M. Saimura, H. Ashida and T. Morii, *Bioorganic Med. Chem.*, 2019, **27**, 115120.
- 34 S. W. Schneider, J. Lärmer, R. M. Henderson and H. Oberleithner, *Pflugers Arch*, 1998, **435**, 362–367.
- 35 Y. Pocker and J. Stone, *J. Biochemistry*, 1967, **6**, 668–678.
- 36 J. a Verpoorte, S. Mehta and J. T. Edsall, *J. Biol. Chem.*, 1967, **242**, 4221–4229.
- 37 R. J. Ellis, *Trends Biochem. Sci.*, 2001, **26**, 597–604.
- 38 A. P. Minton, *J. Biol. Chem.*, 2001, **276**, 10577–10580.
- 39 H. Steiner and S. Lindskog, *FEBS Lett.*, 1972, **24**, 85–88.
- 40 M. L. Connolly, *J. Am. Chem. Soc.*, 1985, **107**, 1118–1124.
- 41 M. L. Connolly, *J. Mol. Graphics*, 1993, **11**, 139–141.
- 42 G. De Simone and C. T. Supuran, *J. Inorg. Biochem.*, 2012, **111**, 117–129.
- 43 G. Holló, in *Glaucoma*, Elsevier, 2nd edn, 2014, vol. 1, pp. 559–565.
- 44 S. Watanabe, A. A. Saleh, S. P. Pack, N. Annaluru, T. Kodaki and K. Makino, *Microbiology*, 2007, **153**, 3044–3054.
- 45 Y. Harano and M. Kinoshita, *Biophys. J.*, 2005, **89**, 2701–2710.
- 46 M. Kinoshita, *Biophys. Rev.*, 2013, **5**, 283–293.
- 47 M. Kinoshita, *Chem. Eng. Sci.*, 2006, **61**, 2150–2160.
- 48 M. Kinoshita and T. Hayashi, *J. Mol. Liq.*, 2017, **247**, 403–410.
- 49 S. Asakura and F. Oosawa, *J. Chem. Phys.*, 1954, **22**, 1255–1256.
- 50 S. Asakura and F. Oosawa, *J. Polym. Sci.*, 1958, **33**, 183–192.
- 51 B. Götzelmann, R. Evans and S. Dietrich, *Phys. Rev. E: Stat. Phys., Plasmas, Fluids, Relat. Interdiscip. Top.*, 1998, **57**, 6785–6800.
- 52 C. Bechinger, D. Rudhardt, P. Leiderer, R. Roth and S. Dietrich, *Phys. Rev. Lett.*, 1999, **83**, 3960–3963.
- 53 F. Kamo, R. Ishizuka and N. Matubayasi, *Protein Sci.*, 2016, **25**, 56–66.
- 54 M. Kinoshita, *J. Chem. Phys.*, 2002, **116**, 3493–3501.
- 55 T. Yoshidome, Y. Harano and M. Kinoshita, *Phys. Rev. E - Stat. Nonlinear Soft Matter Phys.*, 2009, **79**, 011912.
- 56 M. Kinoshita, *Condens. Matter Phys.*, 2007, **10**, 387–396.
- 57  $\beta$ -Nicotinamide adenine dinucleotide, reduced disodium salt hydrate; MSDS no. 43423; Sigma-Aldrich: CH-9471 Buchs/Schweiz, 27th Aug 2007.
- 58 X. Gong, C. Wang, L. Zhang and H. Qu, *J. Chem. Eng. Data*, 2012, **57**, 3264–3269.
- 59 M. Kinoshita, S. Y. Iba and M. Harada, *J. Chem. Phys.*, 1996, **105**, 2487–2499.
- 60 S. Murakami, T. Hayashi and M. Kinoshita, *J. Chem. Phys.*, 2017, **146**, 055102.
- 61 D. Zevin, T. Driesner and C. Sanchez-Valle, *J. Chem. Eng. Data*, 2015, **60**, 1181–1192.
- 62 M. Maroncelli, *J. Mol. Liq.*, 1993, **57**, 1–37.
- 63 D. R. Falcone, D. C. Douglass and D. W. McCall, *J. Phys. Chem.*, 1967, **71**, 2754–2755.
- 64 H. P. Erickson, *Biol. Proced. Online*, 2009, **11**, 32–51.

