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# Shape-adaptive single-molecule magnetism and hysteresis up to 14 K in oxide clusterfullerenes Dy<sub>2</sub>O@C<sub>72</sub> and Dy<sub>2</sub>O@C<sub>74</sub> with fused pentagon pairs and flexible Dy–(μ<sub>2</sub>-O)–Dy angle†

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Dysprosium oxide clusterfullerenes Dy<sub>2</sub>O@C<sub>s</sub>(10528)–C<sub>72</sub> and Dy<sub>2</sub>O@C<sub>2</sub>(13333)–C<sub>74</sub> are synthesized and characterized by single-crystal X-ray diffraction. Carbon cages of both molecules feature two adjacent pentagon pairs. These pentalene units determine positions of endohedral Dy ions hence the shape of the Dy<sub>2</sub>O cluster, which is bent in Dy<sub>2</sub>O@C<sub>72</sub> but linear in Dy<sub>2</sub>O@C<sub>74</sub>. Both compounds show slow relaxation of magnetization and magnetic hysteresis. Nearly complete cancelation of ferromagnetic dipolar and antiferromagnetic exchange Dy...Dy interactions leads to unusual magnetic properties. Dy<sub>2</sub>O@C<sub>74</sub> exhibits zero-field quantum tunneling of magnetization and magnetic hysteresis up to 14 K, the highest temperature among Dy-clusterfullerenes.

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## Introduction

Endohedral metallofullerenes (EMFs) comprising metal and non-metal atoms in their endohedral species are known as clusterfullerenes.<sup>1</sup> Enhanced electrostatic interactions between endohedral lanthanides (Ln) and non-metal ions (X<sup>q−</sup>), such as N<sup>3−</sup>, S<sup>2−</sup>, or O<sup>2−</sup>, reinforced by exceptionally short Ln–X bonds result in a strong magnetic anisotropy of Ln ions and lead to the single-molecule magnetism in many Ln-clusterfullerenes.<sup>2</sup> Especially Dy-clusterfullerenes are known as robust single molecule magnets (SMMs) with many favourable properties, including thermal and chemical stability, reasonably high blocking temperatures of magnetization, and magnetic hysteresis in bulk samples as well as in monolayers on different substrates.<sup>3</sup> Thus, with the improvement of EMF-SMMs, the tremendous progress achieved over the last two decades in the Ln-SMM field<sup>4</sup> has a good chance to further advance to the state of device-oriented functional molecular materials.

Oxide clusterfullerenes<sup>5</sup> with endohedral Ln<sub>2</sub>O clusters were predicted to have the largest ligand-field splitting in the whole EMF family<sup>3g,6</sup> and thus are viable synthetic targets as prospective SMM candidates. Indeed, our recent study of three isomers of Dy<sub>2</sub>O@C<sub>82</sub> revealed their unique magnetic properties.<sup>7</sup> The pronounced magnetic anisotropy is combined in these molecules with antiferromagnetic (AFM) exchange interactions, which are the strongest through all dinuclear Dy complexes with non-radical bridging ligands. In this Communication, we report that the encapsulation of the Dy<sub>2</sub>O cluster in smaller carbon cages has a profound influence on the magnetic properties and leads to the Dy<sub>2</sub>O@C<sub>74</sub> compound with the highest temperature of magnetic hysteresis among clusterfullerene-SMMs.

## Results and discussion

### Synthesis, molecular and electronic structure

New Dy-oxide clusterfullerenes Dy<sub>2</sub>O@C<sub>72</sub> and Dy<sub>2</sub>O@C<sub>74</sub> were synthesized by arc-discharge evaporation of Dy<sub>2</sub>O<sub>3</sub>-filled graphite rods in He/CO<sub>2</sub> atmosphere (200/20 Torr) and isolated by multi-step high-performance liquid chromatography (HPLC) as described in ESI.† Basic characterization of the purified Dy<sub>2</sub>O@C<sub>72</sub> and Dy<sub>2</sub>O@C<sub>74</sub>, including their HPLC profiles, high-resolution laser desorption ionization mass spectra with characteristic isotopic patterns, and UV-vis-NIR absorption spectra are surveyed in Fig. 1.

The molecular structures of Dy<sub>2</sub>O@C<sub>72</sub> and Dy<sub>2</sub>O@C<sub>74</sub> were elucidated by single-crystal X-ray diffraction of co-crystals with

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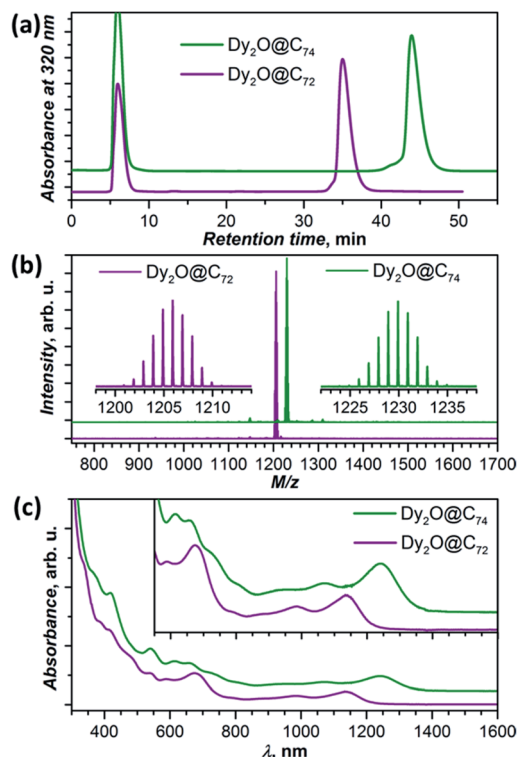


Fig. 1 Characterization of isolated  $\text{Dy}_2\text{O}@\text{C}_{72}$  and  $\text{Dy}_2\text{O}@\text{C}_{74}$ : (a) HPLC profiles (BuckyPrep column, toluene as eluent, flow rate  $4 \text{ mL min}^{-1}$ ; solvent peak appears at 6 min); (b) LDI mass-spectra in a positive-ion mode; (c) UV-Vis-NIR absorption spectra in toluene (the inset shows magnification of the low-energy range).

$\text{Ni}^{\text{II}}(\text{OEP})$  revealing  $\text{C}_s(10528)\text{-C}_{72}$  and  $\text{C}_2(13333)\text{-C}_{74}$  carbon cages (Fig. 2a and b). Both fullerenes violate the Isolated Pentagon Rule (IPR) and have two pairs of adjacent pentagons, which are stabilized by coordination with Dy ions (Fig. 2c,d). The  $\text{C}_s(10528)\text{-C}_{72}$  cage was found before in  $\text{Sc}_2\text{S}@\text{C}_{72}$ ,<sup>8</sup>  $\text{Sc}_2\text{C}_2@\text{C}_{72}$ ,<sup>9</sup> and presumably  $\text{Dy}_2\text{S}@\text{C}_{72}$ .<sup>3g</sup> The  $\text{C}_2(13333)\text{-C}_{74}$  cage was predicted theoretically as a plausible isomer of  $\text{Sc}_2\text{C}_2@\text{C}_{74}$ <sup>10</sup> and was found recently in  $\text{Ho}_2\text{O}@\text{C}_{74}$ .<sup>5c</sup>

Carbon cages and oxygen atoms are fully ordered in the crystals, but Dy atoms are less ordered with 2–3 sites for each metal atom (Fig. 2e and f). In  $\text{Dy}_2\text{O}@\text{C}_{72}$  the Dy–O–Dy angle is  $138.2(4)^\circ$  for the major Dy sites (occupancy 0.60 and 0.75), whereas in  $\text{Dy}_2\text{O}@\text{C}_{74}$  the  $\text{Dy}_2\text{O}$  cluster is close to the linear shape, similar to the  $\text{Ho}_2\text{O}$  cluster in  $\text{Ho}_2\text{O}@\text{C}_2(13333)\text{-C}_{74}$ .<sup>5c</sup> Dy–O bonds are very short,  $1.980(5)\text{--}2.059(5) \text{ \AA}$ , but the disorder in Dy positions does not allow detailed analysis. Optimization of the molecular structures performed at the PBE-D level (PAW 4f-in-core potentials, VASP 5.0 code<sup>11</sup>) resulted in the Dy–O distances and Dy–O–Dy angles of  $2.025 \text{ \AA}/138^\circ$  in  $\text{Dy}_2\text{O}@\text{C}_{72}$  and  $2.038 \text{ \AA}/180^\circ$  in  $\text{Dy}_2\text{O}@\text{C}_{74}$ .

Apparently, the variation of the  $\text{Dy}_2\text{O}$  cluster shape from bent to linear is dictated by the Dy⋯Dy distance, which changes from  $3.743(1) \text{ \AA}$  in  $\text{Dy}_2\text{O}@\text{C}_{72}$  to  $4.030(2) \text{ \AA}$  in  $\text{Dy}_2\text{O}@\text{C}_{74}$  (DFT values are  $3.784$  and  $4.076 \text{ \AA}$ , respectively). In due turn, the location of Dy atoms inside the fullerene is determined by the arrangement of pentalene units. The distance between

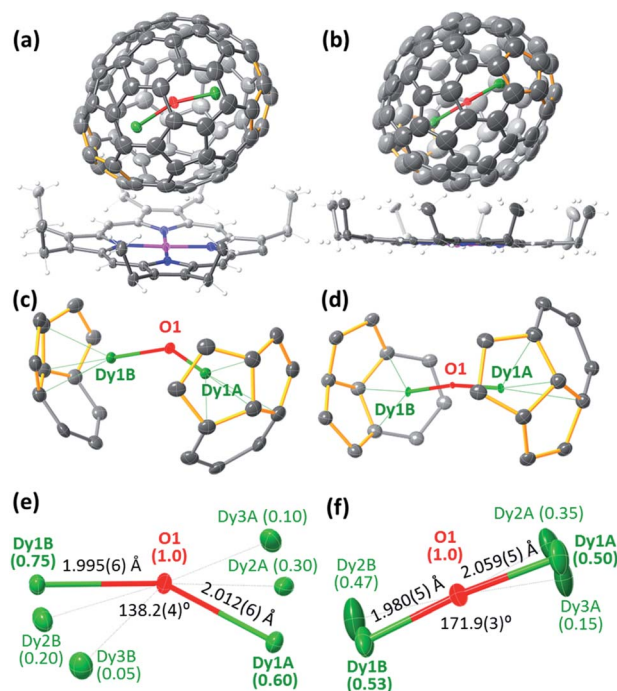


Fig. 2 (a and b) Thermal ellipsoids of  $\text{Dy}_2\text{O}@\text{C}_{2n}\cdot\text{Ni}^{\text{II}}(\text{OEP})$  crystals with 30% probability showing only the major dysprosium sites: (a)  $\text{Dy}_2\text{O}@\text{C}_s(10528)\text{-C}_{72}$ , (b)  $\text{Dy}_2\text{O}@\text{C}_2(13333)\text{-C}_{74}$ ; the solvent molecules and minor Dy sites are omitted, Dy is green, O is red, Ni is purple, N is blue, C is grey, adjacent-pentagon pairs are highlighted in orange. (c and d) Interaction of the major  $\text{Dy}_2\text{O}$  site with the closest cage motif in (c)  $\text{Dy}_2\text{O}@\text{C}_{72}$ , and (d)  $\text{Dy}_2\text{O}@\text{C}_{74}$ . (e and f) Endohedral  $\text{Dy}_2\text{O}$  units with disordered Dy sites and selected structural parameters in (e)  $\text{Dy}_2\text{O}@\text{C}_{72}$ , and (f)  $\text{Dy}_2\text{O}@\text{C}_{74}$ .

centroids of pentalenes in X-ray structures is  $8.151 \text{ \AA}$  in  $\text{Dy}_2\text{O}@\text{C}_{72}$  and  $8.597 \text{ \AA}$  in  $\text{Dy}_2\text{O}@\text{C}_{74}$ . Thus, the shape of the  $\text{Dy}_2\text{O}$  cluster is imposed by the fullerene cage form-factor.<sup>1c</sup> Note that in  $\text{Dy}_2\text{O}@\text{C}_{82}$  isomers the cluster is bent despite the larger cage size than in  $\text{Dy}_2\text{O}@\text{C}_{74}$ : in fact, Dy⋯Dy distances in all  $\text{Dy}_2\text{O}@\text{C}_{82}$  structures are shorter than in  $\text{Dy}_2\text{O}@\text{C}_{74}$ .<sup>7</sup> At the same time, the linear shape of the cluster was found in  $\text{Ho}_2\text{O}@\text{D}_{2d}(23)\text{-C}_{84}$ , which also has an elongated shape of the fullerene cage.<sup>5d</sup>

DFT-based molecular dynamics simulations showed that at 300 K on a timescale of 100 ps metal atoms oscillate near their optimized positions (Fig. S4†). IR spectra calculated from the Fourier transform of the time-dependent dipole moment resemble those computed for the static model and agree well with the experimental spectra (Fig. S5†). Antisymmetric Dy–O stretching vibration is found at  $680 \text{ cm}^{-1}$  in  $\text{Dy}_2\text{O}@\text{C}_{72}$  and  $700 \text{ cm}^{-1}$  in  $\text{Dy}_2\text{O}@\text{C}_{74}$ .

Electronic absorption spectra of both compounds extend to the near-IR region with the lowest-energy bands at  $1137 \text{ nm}$  ( $1.09 \text{ eV}$ ) in  $\text{Dy}_2\text{O}@\text{C}_{72}$  and  $1240 \text{ nm}$  ( $1.00 \text{ eV}$ ) in  $\text{Dy}_2\text{O}@\text{C}_{74}$  (Fig. 1c). The spectrum of  $\text{Dy}_2\text{O}@\text{C}_{72}$  exhibits a close similarity to the spectra of  $\text{Sc}_2\text{S}@\text{C}_{72}$ ,<sup>8</sup>  $\text{Sc}_2\text{C}_2@\text{C}_{72}$ ,<sup>9</sup> and  $\text{Dy}_2\text{S}@\text{C}_{72}$ ,<sup>3g</sup> featuring the same  $\text{C}_s(10528)\text{-C}_{72}$  cage. However, the cluster composition has a noticeable impact on the lowest energy excitation, found at  $1076 \text{ nm}$  ( $\text{Sc}_2\text{S}$ ),  $1082 \text{ nm}$  ( $\text{Sc}_2\text{C}_2$ ), or

**Table 1** Redox potentials<sup>a</sup> of Dy<sub>2</sub>O@C<sub>5</sub>(10528)–C<sub>72</sub> and Dy<sub>2</sub>O@C<sub>2</sub>(13333)–C<sub>74</sub>

EMF	O–II	O–I	R–I	R–II	R–III	R–IV	Gap <sub>EC</sub>
Dy <sub>2</sub> O@C <sub>72</sub>	0.87	0.33	–1.09	–1.56	–2.18	–2.55	1.42
Dy <sub>2</sub> O@C <sub>74</sub>	1.18	0.52	–0.81	–1.17	–2.16	–2.56	1.33

<sup>a</sup> Measured in TBAPF<sub>6</sub>/o-dichlorobenzene and referred *versus* Fe(Cp)<sub>2</sub><sup>+/0</sup>.

1115 nm (Dy<sub>2</sub>S). The absorption spectrum of Dy<sub>2</sub>O@C<sub>74</sub> is virtually identical to that of Ho<sub>2</sub>O@C<sub>2</sub>(13333)–C<sub>74</sub>.<sup>5c</sup>

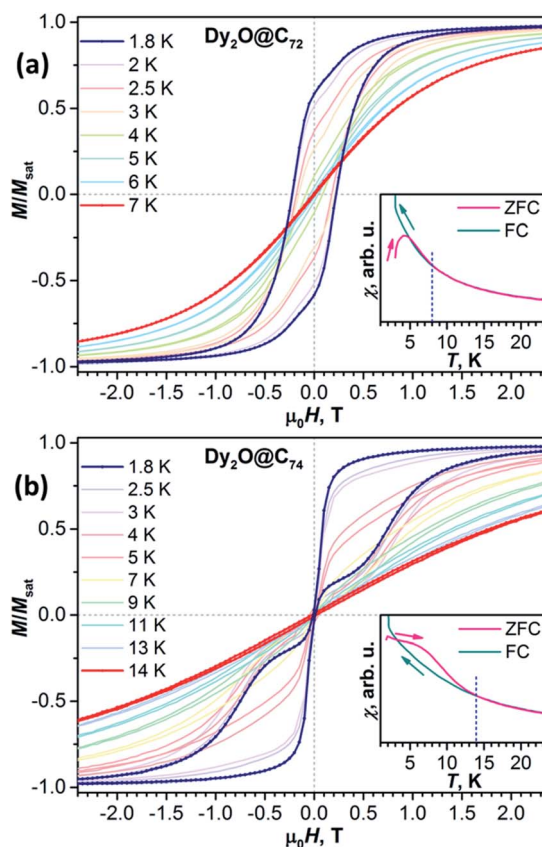
Further insight into the electronic structure of Dy<sub>2</sub>O clusterfullerenes is obtained from the electrochemical studies. Cyclic voltammograms are shown in Fig. S6† and redox potentials are listed in Table 1. Both Dy<sub>2</sub>O@C<sub>72</sub> and Dy<sub>2</sub>O@C<sub>74</sub> exhibit one reversible oxidation and three reversible reduction steps as well as poorly reversible fourth reduction and second oxidation steps. DFT calculations show that frontier molecular orbitals of both molecules are localized on their fullerene cages (Fig. S7†), which suggests that the redox processes do not affect the Dy<sub>2</sub>O cluster. Comparison of the redox potentials of Dy<sub>2</sub>O@C<sub>72</sub> to Sc<sub>2</sub>S@C<sub>72</sub><sup>8</sup> and Sc<sub>2</sub>C<sub>2</sub>@C<sub>72</sub><sup>9</sup> (Table S2†) reveals that the variation of the optical gap discussed above is also reflected in their electrochemical gaps despite the predominant localization of the frontier MOs on the carbon cage in all molecules.

## Magnetic properties

**SQUID magnetometry.** Magnetic properties of Dy<sub>2</sub>O@C<sub>72</sub> and Dy<sub>2</sub>O@C<sub>74</sub> powders were studied by SQUID magnetometry. Fig. 3a and b show low-temperature magnetization curves measured for two clusterfullerenes with a sweep rate of 2.9 mT s<sup>–1</sup>. Dy<sub>2</sub>O@C<sub>72</sub> shows open hysteresis up to 7 K (Fig. S8†). In the isostructural Dy<sub>2</sub>S@C<sub>72</sub>, the hysteresis is much narrower and is closing already at 3 K.<sup>3g</sup> Thus, once again Dy<sub>2</sub>O cluster is found to exhibit more robust single molecule magnetism than the Dy<sub>2</sub>S analog with the same fullerene cage. Earlier, superior SMM properties were found for Dy<sub>2</sub>O@C<sub>82</sub> when compared to the isostructural Dy<sub>2</sub>S@C<sub>82</sub>.<sup>7</sup> At the same time, the use of softer sulfur co-ligands was found to be beneficial to increase the axiality of other types of single-molecule magnets.<sup>12</sup>

Magnetic hysteresis in Dy<sub>2</sub>O@C<sub>74</sub> closes above 14 K (Fig. S8†). The shape of the hysteresis with the abrupt decay of magnetization near 0 T is different from that of Dy<sub>2</sub>O@C<sub>72</sub> and other dinuclear Dy-clusterfullerenes. Such a “waist-restricted” or “butterfly” hysteresis is characteristic for the quantum tunnelling of magnetization (QTM) in zero field and is common for single-ion magnets, but is not typical for dinuclear SMMs.

Blocking of magnetization is analysed by comparing magnetic susceptibility measured after cooling the sample in zero field ( $\chi_{ZFC}$ ) and during cooling the sample in field ( $\chi_{FC}$ ).<sup>13</sup> Blocking temperature  $T_B$  defined as the peak temperature of  $\chi_{ZFC}$  is near 4 K in Dy<sub>2</sub>O@C<sub>72</sub> and 6.7 K in Dy<sub>2</sub>O@C<sub>74</sub> (Fig. 3) when measured in a field of 0.2 T with the temperature sweep rate of 5 K min<sup>–1</sup>. However, both fullerenes show bifurcation of  $\chi_{ZFC}$  and  $\chi_{FC}$  curves (defined as  $T_{irrev}$ <sup>13</sup>) until noticeably higher



**Fig. 3** Magnetic hysteresis curves of Dy<sub>2</sub>O@C<sub>72</sub> (a) and Dy<sub>2</sub>O@C<sub>74</sub> (b) measured with the sweep rate 2.9 mT s<sup>–1</sup>. Insets show comparison of  $\chi_{FC}$  and  $\chi_{ZFC}$  curves ( $\mu_0 H = 0.2$  T, temperature sweep rate 5 K min<sup>–1</sup>); dashed blue lines denote  $T_{irrev}$  as the temperature, at which  $\chi_{FC}$  and  $\chi_{ZFC}$  curves bifurcate.

temperatures, reaching 8 K for Dy<sub>2</sub>O@C<sub>72</sub> and 14 K for Dy<sub>2</sub>O@C<sub>74</sub>. The uncommon shape of  $\chi_{ZFC}$ , being higher than  $\chi_{FC}$ , is caused in Dy<sub>2</sub>O@C<sub>74</sub> by the fast QTM at small fields. It should be also noted that  $T_B$  and  $T_{irrev}$  values are kinetic parameters and depend on the magnetic field, sweep rate, and some technical aspects of the measurements (see Fig. S9–S11† for further measurements and ref. 4d for a more detailed discussion). More universal parameter is the temperature  $T_{B100}$ , at which relaxation time of magnetization is 100 s. As determined from the relaxation time measurements described below,  $T_{B100}$  of Dy<sub>2</sub>O@C<sub>72</sub> is 3.4 K in zero field and 2.6 K at 0.2 T. For Dy<sub>2</sub>O@C<sub>74</sub>, the  $T_{B100}$  value in zero field is not defined because QTM limits the relaxation time, whereas in the field of 0.2 T the value is 5.0 K.

Relaxation times of magnetization  $\tau_M$  below  $T_{irrev}$  (Tables S3–S8 and Fig. S12†) were determined by the stretched exponential fitting of magnetization decay curves recorded after the fast sweep of the magnetic field from 5 T to a required value. Unfortunately, the isolable amounts of the clusterfullerenes are insufficient for the measurement of relaxation times at higher temperatures by AC magnetometry.

Fig. 4a shows the magnetic field dependence of  $\tau_M$  measured at a constant temperature. For Dy<sub>2</sub>O@C<sub>72</sub>,  $\tau_M$  decays fast with





the field from 523 s at zero field to 95 s at 0.4 T and then tends to level off. This  $\tau_M(H)$  dependence is a clear manifestation of the direct relaxation mechanism. For  $\text{Dy}_2\text{O}@\text{C}_{74}$ , relaxation rate in 0 T could not be measured because of the fast QTM, and the lowest field studied is 0.05 T. Field dependence at 2.5 K first shows a fast increase of  $\tau_M$  from 152 s at 0.05 T to 750–780 s at 0.2–0.35 T. This  $\tau_M(H)$  dependence corresponds to the gradual quenching of the QTM by increasing Zeeman splitting. With the further field increase beyond 0.35 T, relaxation accelerates due to the contribution of the direct mechanism as in  $\text{Dy}_2\text{O}@\text{C}_{72}$ .

The temperature dependence of  $\tau_M$  shown in Fig. 4b cannot be described by a direct process alone. Equally good fits are obtained either for a combination of the direct and Raman mechanisms:

$$\tau_M^{-1}(T) = C_{d,H}T^{n_d} + C_R T^{n_R} \quad (1)$$

or by a combination of the direct and Arrhenius process:

$$\tau_M^{-1}(T) = C_{d,H}T^{n_d} + \tau_0^{-1}\exp(-U^{\text{eff}}/T) \quad (2)$$

For the direct mechanism  $n_d$  should be 1, and  $C_{d,H}$  is field-dependent. For each fullerene, temperature dependence was measured in two different fields (Fig. 4b), and then two datasets were fitted jointly either with eqn (1) or with eqn (2) keeping field-independent parameters identical (Fig. S13 and S14†). Eqn (1) gives more physically sound interpretation of the relaxation of magnetization and will be discussed further. For  $\text{Dy}_2\text{O}@\text{C}_{72}$ , the procedure returned  $n_d = 1.43 \pm 0.13$ ,  $C_{d,0\text{ T}} = (5.2 \pm 0.1) \cdot 10^{-4} \text{ s}^{-1} \text{ K}^{-1.4}$ ,  $C_{d,0.2\text{ T}} = (1.8 \pm 0.2) \cdot 10^{-3} \text{ s}^{-1} \text{ K}^{-1.4}$ ,  $n_R = 3.7 \pm 0.4$ , and  $C_R = (8 \pm 4) \cdot 10^{-5} \text{ s}^{-1} \text{ K}^{-3.7}$ . The  $n_d$  value is higher than 1, which may be due to the phonon bottleneck effect (which increases  $n_d$  to 2). For  $\text{Dy}_2\text{O}@\text{C}_{74}$ , we obtained  $n_d = 1.23 \pm 0.14$ ,  $C_{d,0.2\text{ T}} = (1.3 \pm 0.3) \cdot 10^{-4} \text{ s}^{-1} \text{ K}^{-1.25}$ ,  $C_{d,0.8\text{ T}} = (4.9 \pm 0.5) \cdot 10^{-4} \text{ s}^{-1} \text{ K}^{-1.25}$ ,  $n_R = 3.28 \pm 0.14$ , and  $C_R = (4 \pm 1) \cdot 10^{-5} \text{ s}^{-1} \text{ K}^{-3.3}$ . For both molecules the direct mechanism dominates at lower temperature and at higher fields, whereas the field-independent Raman process with  $n_R$  of 3–4 takes over at higher temperatures.

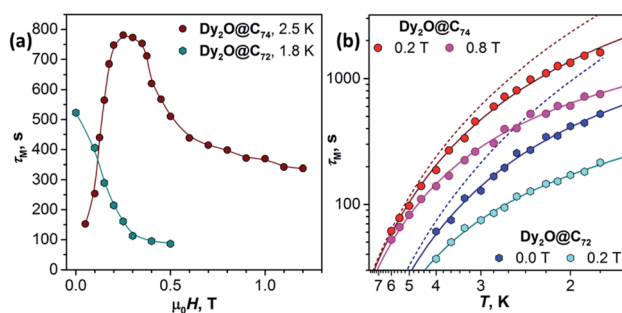


Fig. 4 Magnetization relaxation times of  $\text{Dy}_2\text{O}@\text{C}_{72}$  and  $\text{Dy}_2\text{O}@\text{C}_{74}$ : (a) Field dependence of  $\tau_M$  at 1.8 K ( $\text{Dy}_2\text{O}@\text{C}_{72}$ ) and 2.5 K ( $\text{Dy}_2\text{O}@\text{C}_{74}$ ). Note that the smallest field for  $\text{Dy}_2\text{O}@\text{C}_{74}$  is 0.05 T since the measurements in zero field are not possible because of the fast QTM process; (b) Temperature dependence of  $\tau_M$  in two different fields, dots are measured values, solid lines are fits by a combination of Raman and direct mechanisms (eqn (1)), dashed lines are contributions of Raman process for  $\text{Dy}_2\text{O}@\text{C}_{72}$  (blue) and  $\text{Dy}_2\text{O}@\text{C}_{74}$  (red).

These relatively small  $n_R$  values indicate that optical phonons contribute strongly to the relaxation of magnetization.<sup>14</sup> Contribution of the Raman mechanism is shown for each molecule in Fig. 4b. When eqn (2) was used for the fit, Arrhenius processes with effective barriers of 14–16 K were obtained (see ESI†). These values are much smaller than the ligand-field splitting of  $\text{Dy}^{3+}$  ions in  $\text{Dy}_2\text{O}@\text{C}_{2n}$  molecules, but are considerably larger than the energy difference between the states with ferromagnetic and antiferromagnetic coupling of magnetic moments (see below), and thus cannot match the spin energy levels of the system.

**Dy···Dy interactions and magnetic anisotropy.** To get better understanding of the Dy···Dy coupling, magnetization curves of  $\text{Dy}_2\text{O}@\text{C}_{72,74}$  molecules were simulated and fitted using powder averaging in the PHI code<sup>15</sup> with the following spin Hamiltonian:

$$\hat{H}_{\text{spin}} = \hat{H}_{\text{LF}_1} + \hat{H}_{\text{LF}_2} - 2j_{12}\hat{J}_1\hat{J}_2 + \hat{H}_{\text{ZEE}} \quad (3)$$

where  $\hat{H}_{\text{LF}_i}$  are single-ion ligand-field Hamiltonians of  $\text{Dy}^{3+}$  with *ab initio* computed parameters,  $j_{12}$  is the coupling constant between dysprosium moments, and  $\hat{H}_{\text{ZEE}}$  is Zeeman term.  $\text{Dy}^{3+}$  moments  $\hat{J}_i$  are treated in the  $|J, m_J\rangle$  basis sets ( $^6H_{15/2}$  multiplet). In this notation, the energy difference between FM and AFM-coupled states of the molecule is  $\Delta E_{\text{AFM-FM}} = 225j_{12}\cos(\alpha)$ , where  $\alpha$  is the angle between quantization axes of two  $\text{Dy}^{3+}$  ions.

The ligand-field parameters for Dy ions were computed *ab initio* at the CASSCF(9,7)/SO-RASSI<sup>16</sup> level for  $\text{DyYO}@\text{C}_{72}$  and  $\text{DyYO}@\text{C}_{74}$  molecules. Given the considerable disorder of experimental structures, DFT-optimized atomic coordinates were used. *Ab initio* calculations showed that  $\text{Dy}^{3+}$  ions in both clusterfullerenes have easy-axis magnetic anisotropy with the quantization axes aligned along the corresponding Dy–O bonds with a deviation of 2°. In  $|J, m_J\rangle$  representation, the four lowest energy Kramers doublets (KDs) are almost pure states with  $m_J$  of 15/2 (ground state), 13/2 (near 340  $\text{cm}^{-1}$ ), 11/2 (near 720  $\text{cm}^{-1}$ ), and 9/2 (near 1030  $\text{cm}^{-1}$ ) (Table S9†). Transition probabilities between these states are thus very low (Fig. 5). Further KDs have a more mixed nature, and at higher temperatures the relaxation of magnetization following the Orbach mechanism is expected to proceed *via* the fifth KD at 1180–1200  $\text{cm}^{-1}$ , which resembles the situation found experimentally in  $\text{Dy}_2\text{ScN}@\text{C}_{80}$  with the Orbach barrier of  $1206 \pm 15 \text{ cm}^{-1}$ .<sup>3e</sup> The overall LF splitting is 1337  $\text{cm}^{-1}$  in  $\text{Dy}_2\text{O}@\text{C}_{72}$  and 1329  $\text{cm}^{-1}$  in  $\text{Dy}_2\text{O}@\text{C}_{74}$ . In brief, both clusterfullerenes have strongly axial magnetic anisotropy with similar energies and state compositions, and their low-temperature magnetic properties are determined exclusively by the ground state KDs.

The coupling constants  $j_{12}$  defining the scale of Dy···Dy interactions are determined by fitting of the experimental magnetization curves to eqn (3) (Fig. S15 and S16†). For  $\text{Dy}_2\text{O}@\text{C}_{72}$ , the best fit is obtained for the ferromagnetic coupling with  $j_{12} = 0.009 \pm 0.002 \text{ cm}^{-1}$ , which gives  $\Delta E_{\text{AFM-FM}} = 1.5 \pm 0.3 \text{ cm}^{-1}$ . For  $\text{Dy}_2\text{O}@\text{C}_{74}$ , the optimal  $j_{12}$  is less than  $0.001 \text{ cm}^{-1}$  with the uncertainty of  $\pm 0.002 \text{ cm}^{-1}$ . The FM and AFM states in  $\text{Dy}_2\text{O}@\text{C}_{74}$  are thus degenerate within

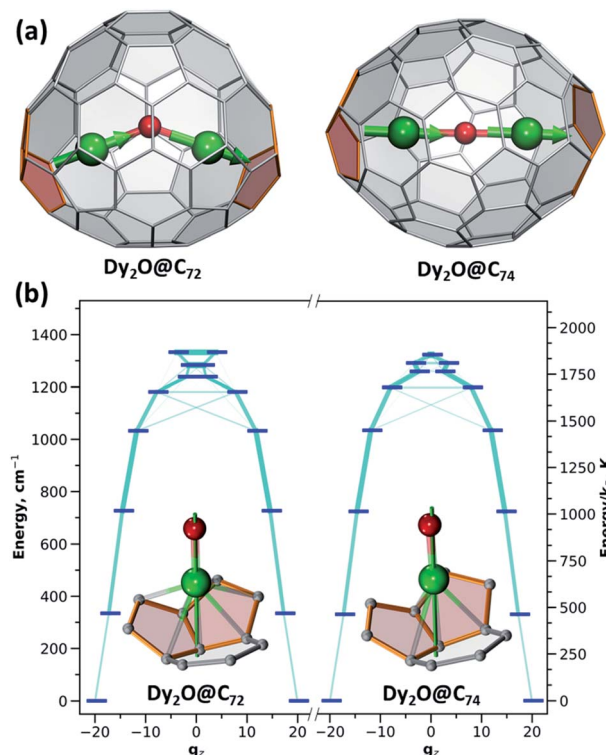


Fig. 5 (a) DFT-optimized molecular structures of Dy<sub>2</sub>O@C<sub>72</sub> and Dy<sub>2</sub>O@C<sub>74</sub> showing alignment of magnetic moment in ferromagnetically-coupled ground-state doublet (Dy is green, O is red, adjacent pentagon pairs are rose; magnetic moments of Dy ions are shown as green arrows). (b) CASSCF/RASSI-computed ligand-field splitting for Dy<sup>3+</sup> ions in Dy<sub>2</sub>O@C<sub>72</sub> and Dy<sub>2</sub>O@C<sub>74</sub>; the thickness of light blue lines corresponds to transition probability. The insets in (b) show Dy-coordinated fragments of the fullerene cage and quantization axis of Dy (green line); Dy–C distances shorter than 2.6 Å are shown as bonds. The scale on the left shows the energy in cm<sup>-1</sup>, on the right in K.

$|\Delta E_{\text{AFM-FM}}| < 0.4 \text{ cm}^{-1}$ , which means that Dy<sup>3+</sup> moments are essentially decoupled.

If a magnetic moment of one of the centers in a dinuclear FM-coupled system is flipped, the system arrives in the AFM-coupled state (and *vice versa*). As long as the FM and AFM states have a different energy, the  $\Delta E_{\text{AFM-FM}}$  difference acts as a barrier preventing the QTM, because the latter requires degeneracy of the energy levels. In all dinuclear Dy-clusterfullerenes studied to date the  $\Delta E_{\text{AFM-FM}}$  difference, either positive (FM) or negative (AFM), was large enough to prevent the QTM in zero field. Dy<sub>2</sub>O@C<sub>74</sub> is the first dinuclear Dy-clusterfullerene exhibiting efficient zero-field QTM, which can be explained by the vanishing Dy⋯Dy coupling. In Dy<sub>2</sub>O@C<sub>72</sub>, Dy⋯Dy coupling is also weak but still sufficient to quench the QTM in zero field.

The Dy⋯Dy coupling in the Dy<sub>2</sub>O clusters found in this work – weak FM in Dy<sub>2</sub>O@C<sub>72</sub> and negligible in Dy<sub>2</sub>O@C<sub>74</sub> – is in a sharp contrast with the situation in Dy<sub>2</sub>O@C<sub>82</sub> isomers, featuring strong AFM coupling with  $\Delta E_{\text{AFM-FM}}$  of (5.4–12.9) cm<sup>-1</sup>.<sup>7</sup> Such a large variation of the strength of magnetic interactions in seemingly very similar molecules requires

a closer look. The overall Dy⋯Dy coupling in dinuclear spin systems can be divided into exchange and dipolar contributions,  $\Delta E_{\text{AFM-FM}}^{\text{exch}}$  and  $\Delta E_{\text{AFM-FM}}^{\text{dip}}$ . The latter can be computed exactly when molecular structures and orientations of magnetic moments are known. Using DFT-optimized structures and orientation of quantization axes from *ab initio* calculations, we obtain  $\Delta E_{\text{AFM-FM}}^{\text{dip}}$  of 2.99 cm<sup>-1</sup> in Dy<sub>2</sub>O@C<sub>72</sub> and 2.56 cm<sup>-1</sup> in Dy<sub>2</sub>O@C<sub>74</sub>. Thus, dipolar interactions favour FM arrangement of Dy<sup>3+</sup> moments and are of the same size as in Dy<sub>2</sub>O@C<sub>82</sub> isomers with  $\Delta E_{\text{AFM-FM}}^{\text{dip}}$  of 2.5–3.0 cm<sup>-1</sup>. Apparently, small overall coupling in Dy<sub>2</sub>O@C<sub>72,74</sub> results from the cancellation of dipolar coupling by exchange interactions, which are therefore antiferromagnetic. To yield the experimentally determined  $\Delta E_{\text{AFM-FM}}$  energies,  $\Delta E_{\text{AFM-FM}}^{\text{exch}}$  values should be  $-1.5 \pm 0.3 \text{ cm}^{-1}$  in Dy<sub>2</sub>O@C<sub>72</sub> and  $-2.5 \pm 0.4 \text{ cm}^{-1}$  in Dy<sub>2</sub>O@C<sub>74</sub>. Thus, it is the antiferromagnetic exchange coupling in the Dy<sub>2</sub>O cluster that is changing strongly from one fullerene to another and is therefore responsible for the considerable variation of the magnetic properties in the series of Dy<sub>2</sub>O clusterfullerenes. The factors determining exchange interactions in Dy-clusterfullerenes are not very clear yet, and further studies of Dy-oxide clusterfullerenes with different fullerene cages are needed to establish structure–property correlations.

## Conclusions

In this work we isolated Dy<sub>2</sub>O@C<sub>s</sub>(10528)–C<sub>72</sub> and Dy<sub>2</sub>O@C<sub>2</sub>(13333)–C<sub>74</sub> clusterfullerenes violating the isolated pentagon rule and characterized their structural, electronic, and magnetic properties. The shape of the Dy<sub>2</sub>O cluster is determined by the form-factor of the carbon cage and location of pentalene units, leading to the bent cluster in Dy<sub>2</sub>O@C<sub>72</sub> but linear one in Dy<sub>2</sub>O@C<sub>74</sub>. Both fullerenes are single molecule magnets showing hysteresis up to 7 K in Dy<sub>2</sub>O@C<sub>72</sub> and 14 K in Dy<sub>2</sub>O@C<sub>74</sub>, the latter being the highest temperature among Dy-clusterfullerenes. The magnetic Dy⋯Dy interactions in Dy<sub>2</sub>O clusters are characterized by the ferromagnetic dipolar coupling counterbalanced by the antiferromagnetic exchange. In Dy<sub>2</sub>O@C<sub>74</sub>, these two contributions cancel each other completely leading to decoupled Dy moments and zero-field quantum tunnelling of magnetization. As a result, magnetization of Dy<sub>2</sub>O@C<sub>74</sub> relaxes fast in zero field, but the relaxation becomes slow once the tunnelling is quenched in a finite magnetic field. This study demonstrates that the shape flexibility of the Dy<sub>2</sub>O cluster and its conformity with the fullerene form-factor is reflected in the substantial variation of the Dy<sub>2</sub>O-clusterfullerene magnetic properties with the carbon cage. This cage-adaptive SMM behaviour suggests that even stronger variability of magnetic properties may be achieved in future exploration of lanthanide-oxide clusterfullerenes with different carbon cages.

## Conflicts of interest

There are no conflicts to declare.



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## Notes and references

§ Crystals were grown by layering the benzene solution of nickel octaethylporphyrin (Ni(OEP)) onto the CS<sub>2</sub> solution of the Dy<sub>2</sub>O@C<sub>2n</sub> (2n = 72, 74) isomers. The as-prepared crystals Dy<sub>2</sub>O@C<sub>8</sub>(10528)–C<sub>72</sub>·Ni(OEP)·2(C<sub>6</sub>H<sub>6</sub>) and Dy<sub>2</sub>O@C<sub>2</sub>(13333)–C<sub>74</sub>·Ni(OEP)·C<sub>6</sub>H<sub>6</sub>·CS<sub>2</sub> were measured with Bruker APEX II at 120 and 173 K, respectively. The structures were solved using direct methods<sup>17</sup> and refined on F<sub>2</sub> using full-matrix least-squares using the SHELXL2015 crystallographic software package.<sup>18</sup> Hydrogen atoms were inserted at calculated positions and constrained with isotropic thermal parameters. The crystal data are presented in Table S1.† The data can be obtained free of charge from the Cambridge Crystallographic Data Centre with CCDC no. 1974305 and 1974314,† respectively.

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