1 Introduction

Electrolysis of water to oxygen and hydrogen is a cornerstone in the transformation of our petrochemical based society toward a future based on sustainable chemicals and fuels.\(^1\)\(^2\) The energy produced from wind turbines, photovoltaics and other sustainable and renewable sources can be stored in the form of chemical bonds by utilising devices like Proton Exchange Membrane (PEM) water electrolyzers.\(^3\)\(^4\) Hydrogen produced from electrochemical water splitting can play the role of energy storage or as a reactant in chemical production.\(^5\)\(^6\) The overall reaction for water electrolysis is as follows:

\[
2\text{H}_2\text{O} \rightarrow 2\text{H}_2 + \text{O}_2
\]

At the cathode the Hydrogen Evolution Reaction (HER) takes place,

\[
2(\text{H}^+ + e^-) \rightarrow \text{H}_2
\]

The HER has minor losses\(^10\)\(^11\) compared to the complementary reaction at the anode, the Oxygen Evolution Reaction (OER). This is the bottleneck of the overall reaction of water splitting because of the high required driving force. Numerous experimental and theoretical studies have been conducted, trying to lower the overpotential needed for the reaction of water oxidation and thus increasing the efficiency of the overall reaction. The half-reaction describing the OER is as follows:

\[
2\text{H}_2\text{O} \rightarrow O_2 + 4(\text{H}^+ + e^-)
\]

The reaction consists of four consecutive electrochemical steps and the simplest way of conceiving that is by a reaction proceeding via three surface bound intermediates.

\[
\text{H}_2\text{O} + * \rightarrow \text{HO}^* + \text{H}^+ + e^- \tag{4}
\]

\[
\text{HO}^* \rightarrow O^* + \text{H}^+ + e^- \tag{5}
\]

\[
\text{H}_2\text{O} + O^* \rightarrow \text{HOO}^* + \text{H}^+ + e^- \tag{6}
\]

\[
\text{HOO}^* \rightarrow * + \text{O}_2 + \text{H}^+ + e^- \tag{7}
\]

In eqn (4)-(7), * represents an active surface site and HO^*, O^*, and HOO^* are the reaction intermediates adsorbed on the active sites of the catalyst. This reaction pathway is valid for acidic media; however from the thermodynamic perspective, changing to an alkaline medium does not change the analysis.\(^12\)\(^13\) The reactions above are naturally a strong simplification of the real OER; however, it illustrates one of the fundamental challenges for catalyzing the OER or any reaction involving more than one intermediate.\(^15\) Ideally the free energy of adsorption for the three intermediates should be so that all four steps could proceed close to the equilibrium potential. Up until now no such catalyst has
been discovered; in contrast several studies\cite{12-14,16-19} revealed that the overpotential seems to be an intrinsic property of the OER resulting from the constant energy difference between the HO* and HOO* intermediates, the so-called universal scaling relationship. The constant energy difference is a consequence of the similar way these particular intermediates are adsorbed on a surface, namely by creating a single bond between O and the active site. The energetic relationship for HO* and HOO* is ΔE_{HOO*} = ΔE_{HO*} + (3.2 ± 0.2) eV, while for the ideal situation it is ΔE_{HOO*} = ΔE_{HO*} + 2.46 eV. Thus, the constant difference between HOO* and HO* defines an upper limit for how efficient an OER catalyst can be, while fulfilling the scaling relationship. It seems that all OER catalysts are subject to this limitation. We have previously proposed special sites to overcome the limitation of the scaling relationship; however, the density of these sites is low, making the overall performance only marginally better.\cite{20} We speculate that it will be difficult or impossible to circumvent the limitation of the scaling relationship without imposing a similar limitation in terms of density of active sites or entropy. Assuming that the HO*/HOO* relationship has to be accepted as a precondition, the binding of O*, which is the intermediate in-between HO* and HOO*, has to be just right in order to reduce the overpotential as much as possible, and thus the energy difference between O* and HO* can be used as a descriptor for the energy efficiency of the OER catalyst and can be used as a first criterion for identifying promising catalysts.

The challenge for OER catalysis is to find materials which are active and stable. There are many oxides which are stable at high potentials; however, they are not active. Most of the stable oxides are semiconductors. One strategy is to dope or modify a stable material by adding metal atoms with a different valence than the host. This changes the electronic structure and thereby the binding and the conductivity of the catalyst material.

In the present work, we collected data from multiple studies involving DFT calculations for the OER in order to revise and understand the effect of metal oxide structures (doped and pristine) on the aforementioned reaction. The starting point of collecting data is the work of Man’s et al.,\cite{19} in which the universality of the constant energetic interdependence of HO* and HOO* intermediates on metal oxides was introduced. The only two criteria used for collecting the data are the calculations should include only metal oxides (doped and pristine) and involve DFT calculations for the binding energy of the intermediates on the surfaces. We extracted the data points from a total collection of 24 papers and when needed we subtracted the thermal corrections and the Zero Point Energy (ZPE) correction and obtained the DFT energy (ΔE). The data points comprise many different materials and structures, different functionals, approximations and so on. We are interested in the trends and conclusions which can be drawn regardless of all these differences. All the data are shown in the ESI in Table SI-2.†

2 Results and discussion

Doping metal oxides to improve the OER reactivity of a surface has been extensively investigated.\cite{19-42} The idea behind this strategy is that the dopant in a structure is able to provide the electrons needed in order to bind the first two intermediates more strongly on the surface of the electrode.

All the data gathered from the literature are depicted in Fig. 1 which provides some obvious observations.

**Observation number 1:** The scaling relationship between HO* and HOO* (the green points) is robust among all the collected data. There is a zoom-in on the relationship in Fig. 2. This observation is quite reliable given the very diverse origin and quantity of the data. This means that the simple picture for the limitation in OER efficiency described above holds no matter how the data are calculated. Previously it has been shown\cite{16,17,19} that the constant energetic interdependence is 3.20...
The relationship between O* and HO* is sensitive to the method and structure of the simulation, whereas the HOO*/HO* scaling relationship is not. The question is: what makes the O* trend line more sensitive than HOO* and is there still general information hidden in the blue scatter in Fig. 1?

**Observation number 3:** For most oxides the reaction step which requires the largest driving force is the oxidation of HO* to O*, reaction (5). This formation of a bond to the catalyst means that a stronger adsorption of oxygen would reduce the calculated overpotential. Thus, most structures end up located in the weak binding region on the volcano, see Fig. 3. Being stable, but not active pristine semiconducting oxides also belong to this category. This indicates that the doping has failed to reduce the overpotential of reaction (5) even if the doping has made the oxidation of water to HO* easier.

In order to understand why doped structures failed to reduce the potential of the HO* and O* step and why the trend line of O* is less steep and more scattered, we plot the same diagram as in Fig. 1, but this time only the data points corresponding to doped structures are included, see Fig. 4a. For comparison, the same diagram is created by using all the data for pristine surfaces. It can be seen in Fig. 4b.

The O* trend line for the doped structures becomes almost parallel to the HO* and HOO* trend lines in Fig. 4a. However, the O* line of the pristine structures in Fig. 4b shows a steeper slope. The values for the O* trend line slopes for all the diagrams are provided in Table SI-3.

We further distinguish the data, making a diagram with doped structures with U correction, see Fig. 5. The O* trend line of this particular diagram is more parallel compared to previously shown O* trend lines. The O* trend line seen in Fig. 5 is closest to being parallel with the HO* and HOO* trend lines and
is therefore the one that deviates the most from the expected picture.

In Fig. 5 we assume that the vast majority of the structures have a band gap, even though it is not clarified in most of the papers whether the structures used are semiconductors or not. We make this assumption because the $U$ correction is applied to obtain a better estimation\textsuperscript{36,39} for the magnitude of the band gaps (or even creating band gaps). It is well known that standard GGA – DFT severely underestimates band gaps.\textsuperscript{43}

### 2.1 Binding of $O^*$ on a surface

To explain the observations above we make a hypothesis for the nature of binding to semi-conductors based on the electronic structure. The Fermi level of a semiconductor is located in the band gap, and thus adding or removing electrons from the system by doping with atoms with a different valence than that of the host will shift the Fermi level towards the conduction or the valence band respectively. In contrast the Fermi level of a conductor will stay unaffected by a change of the number of electrons. Almost all simulations of doped oxides only include a single dopant.

One possible explanation for the slope of the $O^*$ trend line being close to 1 for doped structures is that including a single dopant results in a finite size effect that does not display the behavior of a real catalyst. A single dopant, most of the time, will provide only one electron available in the conduction band, which is used by the first bond created between the intermediate and the surface. When the double bond is formed, going from $HO^*$ to $O^*$, the second electron is not available at the same

### Table 1

<table>
<thead>
<tr>
<th>Intermediate energy dependence</th>
<th>0 dopants</th>
<th>1 dopant</th>
<th>2 dopants</th>
</tr>
</thead>
<tbody>
<tr>
<td>$HO^*$</td>
<td>$E_v$</td>
<td>$E_c$</td>
<td>$E_v$</td>
</tr>
<tr>
<td>$O^*$</td>
<td>$2E_v$</td>
<td>$E_c + E_v$</td>
<td>$2E_c$</td>
</tr>
<tr>
<td>$HOO^*$</td>
<td>$E_v$</td>
<td>$E_c$</td>
<td>$E_v$</td>
</tr>
</tbody>
</table>
chemical potential and therefore it has to be taken from the valence band, see Fig. 6b. In this case, O\(^{\ast}\) binding to the surface is not affected by the changes of doping twice as pronounced as HO\(^{\ast}\), since the two electrons participating in the bond to O\(^{\ast}\) come from two different chemical potentials.

As only the first electron in the oxygen bond comes from the conduction band and the second from the valence band, the oxygen bond has a dependence of \(E_{O^{\ast}} = E_{c} + E_{v}\), see Table 1. Since the position of the valence band of a given material does not change, when changing the type of dopant, \(E_{v}\) is kept constant and the oxygen bond, therefore, is affected by the changes in the dopant with the same strength as HO\(^{\ast}\) and HOO\(^{\ast}\), giving a scaling factor of 1. This finite size effect is therefore also partly responsible for the large scatter of the O\(^{\ast}\) binding in Fig. 1, as some of the data include both doped and non-doped structures.

The finite size effect does not occur if both electrons either come from the valence band when no dopants are included (Fig. 6a), or come from the conduction band in the presence of an n-type dopant (Fig. 6c).

Similar behaviors of the Fermi levels inside the band gap as in Fig. 6a–c were identified when adsorbing different fragments that behave as donors (e.g. H\(^{\ast}\) on an O site on a semiconductor oxide) and as acceptors (e.g. HO\(^{\ast}\) on a metal site of a semiconductor oxide) compared to the case when they are co-adsorbed.

In the case of conductors, the lack of bandgap leads to dopants not changing the Fermi level. For conductive oxides the scaling factor between HO\(^{\ast}\) and O\(^{\ast}\) is close to 2.

According to our hypothesis this effect creates an artifact which will not occur if more than one dopant is present in the simulation, since both electrons in the oxygen double bond will come from the same chemical potential, see Table 1 and Fig. 6c. In Fig. 7 data points for the few papers including more than one dopant and \(U\) correction are shown. As expected, the slope is much steeper.

Fig. 8 The difference between one and two dopants in the TiO\(_{2}\) structure. The blue trend line corresponding to a single dopant is almost parallel to HO\(^{\ast}\) and HOO\(^{\ast}\) trend lines, while the purple trend line corresponding to two dopants of the same elements has a slope of 2.

Fig. 9 (a) Starting from the top, the Fermi level is located in the conduction band due to the reason that V is providing an e\(^{-}\) to the unoccupied states of the conduction band. Then HO\(^{\ast}\) is bound with a single bond on the surface, by using the electron located in the conduction band, and thus the Fermi level is shifted to the middle of the band gap. Subsequently O\(^{\ast}\) is adsorbed with a double bond, by taking an extra electron from the valence band and thus the Fermi level is placed in the valence band and after the adsorption of HOO\(^{\ast}\) the Fermi level returns to the middle of the band gap since it has a single bond with the surface as in the case of HO\(^{\ast}\). (b) In contrast when we are using two dopants, the conduction band is populated with two electrons and when O\(^{\ast}\) is adsorbed the Fermi level is placed in the middle of the band gap, indication that both electrons are provided from the conduction band and thus eliminating the finite size effect.
We have only been able to find two papers studying O\(^*\) adsorption where two dopants are added to semiconductors. To supplement the evidence shown in Fig. 7, we performed DFT calculations of TiO\(_2\) structures doped with one or two atoms of the same element, iterating through different transition metal dopants. The results of our simulations are shown in Fig. 8. In addition, we can observe that the heavy metal doped structures are migrating towards the strong binding side. This can be seen in the volcano plot and also the free energy diagram in ESI Fig. SI-18(a and b).

Furthermore, the density of states (DOS) of TiO\(_2\) with one and two dopants, shown in Fig. 9a and b, shows the way the finite size effect occurs. As shown in Fig. 6b, with only one dopant present the finite size effect takes place. The effect is however eliminated when two dopants are present as shown in Fig. 6c.

The elimination of the finite size effect was also observed if a single dopant with an oxidation state carrying two charges higher than the host is used e.g. W or Mo in TiO\(_2\). W and Mo have an oxidation state of +6 while TiO\(_2\) has an oxidation state of +4, and thus two e\(^-\)'s are provided by one single dopant. This means that it is not the number of dopants that will eliminate the finite size effect but the number of electrons provided from the dopant or dopants, in the conduction band (Fig. 10). Mo, W, Ta and Nb density of states for one and two dopants can be found in Fig. SI3–SI6. Our findings are in agreement with the work of Xiang Huang et al.\(^{45}\) concerning the argument that the number of excess electrons (NEE) influences the binding energy of the OER intermediates strongly.

3 Computational methods

Density functional theory (DFT) calculations were conducted with the usage of the Grid-based Projector Augmented Wave (GPAW)\(^{46,47}\) with the Atomic Simulation Environment (ASE)\(^{48}\) interface. The generalized gradient approximation (GGA) was used by implementing the RPBE\(^{49}\) functional in order to express the exchange and correlation, with a grid spacing of \(h = 0.20\ \text{Å}\). The Brillouin zone was sampled with a \(k\)-point mesh of \((4, 4, 1)\) and the atomic positions were relaxed until the total forces were lower than 0.05 eV \(\text{Å}^{-1}\). The TiO\(_2\)(110) structure along with total energies will be available on Jan Rossmeisl’s group webpage: https://nano.ku.dk/english/research/theoretical-electrocatalysis/katladb/.

4 Conclusions

In the present work, we collected data from multiple studies referring to DFT calculations for the OER. We identify conclusions which can be made across all the data regardless of the exact nature of the simulations.

**Observation number 1:** The universal nature of the scaling relationship between the binding energy of HO\(^*\) and HOO\(^*\) is verified across all the different simulation methods and structures and it is therefore a very robust conclusion, which seems to be the origin of the large intrinsic overpotential for the OER. Furthermore, the collected data reveal that the scaling relationship between HO\(^*\) and O\(^*\) is much less well determined.

**Observations number 2 and 3:** Additionally, a lot of studies that calculate different structures with different methods end up overlapping their data, mostly in the region of the weak binding side of the volcano. Progressing our analysis on the gathered data, we found that structures with band gaps doped with only one dopant have an O\(^*\) trend line that tends to be parallel to HO\(^*\) and HOO\(^*\) trend lines. The interpretation of this observation is that the two electrons participating in O\(^*\)'s double bond to the surface bare different chemical potentials. The first electron is provided by the dopant and it is energetically located in the conduction band and the second e\(^-\) is provided from the valence band. From the total collection of 24 papers only two are using more than one dopant and as expected the slope for the O\(^*\) trend line is closer to two for those simulations. This is due to the fact that the electrons participating in the double bond to O\(^*\) are both provided from the conduction band.

Therefore, we conclude that for semiconductors at least two dopants or a single dopant with a sufficiently higher oxidation state compared to the host metal oxide should be used in order to avoid finite size problems in future studies. We note that we don’t judge which method or simulation will provide the most accurate binding energies, rather we conclude that if this finite size effect is not considered the results are wrong regardless of the methods. Furthermore, we conclude that there are findings which are robust regardless of the method. Our study also suggests that calculating accurate adsorption energies on semiconductors probably requires accurate absolute positions of the bands in the calculations which is not the case in most simulations today.

Conflicts of interest

There are no conflicts to declare.
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References


