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Theoretical investigation on the nature of 4-substituted Hantzsch esters as alkylation agents

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Recently, a variety of 4-substituted Hantzsch esters (XRH) with different structures have been widely researched as alkylation reagents in chemical reactions, and the key step of the chemical process is the elementary step of XRH$^{•+}$ releasing R$^•$. The purpose of this work is to investigate the essential factors which determine whether or not an XRH is a great alkylation reagent using density functional theory (DFT). This study shows that the ability of an XRH acting as an alkylation reagent can be reasonably estimated by its $\Delta G_{RD}^{\neq}$(XRH$^{•+}$) value, which can be conveniently obtained through DFT computations. Moreover, the data also show that $\Delta G_{RD}^{\neq}$(XRH$^{•+}$) has no simple correlation with the structural features of XRH, including the electronegativity of the R substituent group and the magnitude of steric resistance; therefore, it is difficult to judge whether an XRH can provide R$^•$ solely by experience. Thus, these results are helpful for chemists to design 4-substituted Hantzsch esters (XRH) with novel structures and to guide the application of XRH as a free radical precursor in organic synthesis.
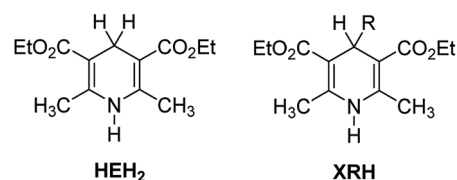
1 Introduction

It is well known that the Hantzsch ester (HEH$_2$, Scheme 1) was first synthesized by Hantzsch, a German chemist, in 1881.[1] Due to the simple synthesis method and excellent reduction performance, HEH$_2$ has long been used as an organic hydrogen molecular reductant to hydrogenate various types of unsaturated compounds.[2–4] HEH$_2$ releases two hydrogen atoms or hydrogen ions to unsaturated substrates while itself aromatizes into pyridine compounds, meanwhile the unsaturated bonds (C=C, C=N, C=O, *etc.*) in the substrates are reduced. Organic synthetic chemists have done excellent research work in designing novel catalysts, expanding new reaction substrate and improving product chirality and yield using HEH$_2$ as reducer. Since 2013, chemists found that 4-substituted Hantzsch esters (XRH, Scheme 1) can break C–C bond and release alkyl radical (R$^•$) under the condition of photocatalysis.[5] Then R$^•$ reacts with electron-activated substrate to produce alkyl substitution or alkyl addition products, and hundreds of literatures have reported the alkylation reaction between XRH with various substrates.[6–18]

There are two main mechanisms (Scheme 2) for the reactions of XRH as alkylating agents reacting with substrates. Under certain specific wavelength, the photocatalyst (PC) is activated into an excited state photocatalyst (PC*) with strong single

electron oxidation ability. PC* oxidizes XRH to XRH$^{•+}$ and transforms itself into PC$^{•-}$, a strong single electron reducer. XRH$^{•+}$ is an unstable and active key intermediate, which will release R$^•$ to substrate. The first mechanism[7–12] is that PC$^{•-}$ reduces the reaction substrate (R$_1$–G) to R$_1$–G$^{•-}$, subsequently, R$_1$–G$^{•-}$ releases stable G$^-$ group to generate R$_1$$^•$. Recombination of R$^•$ and R$_1$$^•$ radicals generates the desired product R$_1$–R. Since the concentrations of R$^•$ and R$_1$$^•$ are very low in solution, hydrogen-abstraction by the radicals may possibly occur as a side-reaction (Mechanism 1 in Scheme 2). Alkylation of haloalkanes is a typical reaction of this mechanism. The second mechanism[13–18] is that R$^•$ reacts with unsaturated substrate (such as R$_2$=R$_2$) to form active free radical intermediate RR$_2$–R$_2$$^•$ first, then RR$_2$–R$_2$$^•$ obtains electrons from PC$^{•-}$ and protons from XH$^+$ to form alkylation product RR$_2$–R$_2$H (Mechanism 2 in Scheme 2). After carefully analyzing the reaction mechanism of XRH acting as alkylating reagents, it is clear that the key step is the elementary step of XRH$^{•+}$ releasing R$^•$ (Scheme 3), but not all XRH with various R substituent groups in 4-position can give the alkyl radicals, for example, 4-Ph-HEH cannot provide Ph$^•$ in alkylation reaction.

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Scheme 1 Structures of HEH$_2$ and XRH investigated in this work.

Scheme 2 Two mechanisms of XRH being used as alkylation reagents in chemical reactions.
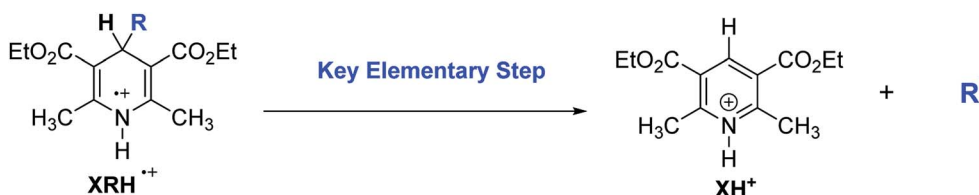

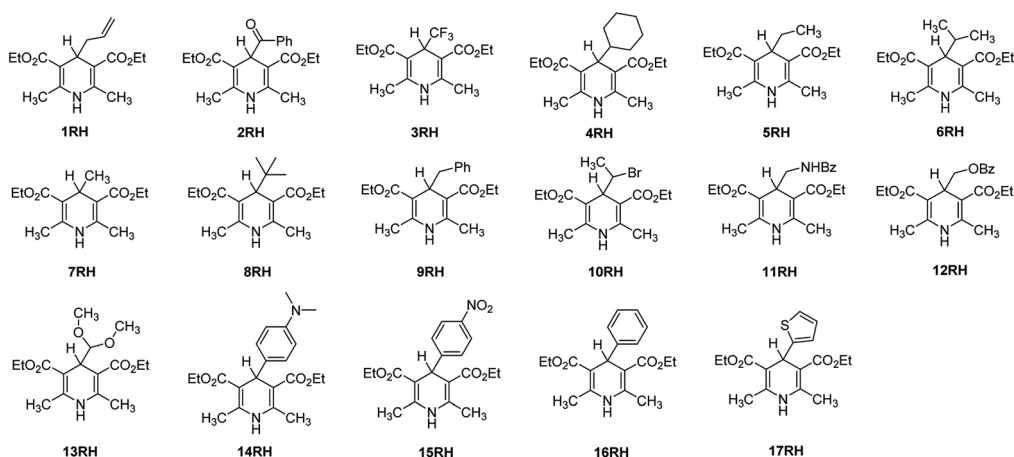**Scheme 3** Key elementary step of XRH being used as alkylation reagents in chemical reactions.

Then we begin to wonder: why some structures of XRH (R = Bn, *tert*-Bu, cyclohexyl, allyl, *etc.*) are excellent alkylation reagents, while some structures of XRH (R = Ph, thienyl, *etc.*) cannot be used as alkylation reagents, and what determines whether an XRH can be a good alkylation reagent? At present, the above question have not been well answered, and it is difficult to determine these important thermodynamic and kinetic data by experimental methods. Therefore, there is an urgent need for an accurate and reliable theoretical method to guide the experimental design in the field of organic synthesis. Further study on the thermodynamic and kinetic properties of the key intermediate XRH$^{\bullet+}$ releasing R$^{\bullet}$ can guide chemists to better design 4-substituted Hantzsch esters (XRH) as novel alkylation reagents and understand the alkylation mechanism in organic synthesis.

Owing to the rapid development of density functional theory (DFT)[19–23] in recent years and the large enhancement of

computational capability, the thermodynamic driving forces and activation energies of chemical reactions could be accurately computed by employing suitable density functionals. Based on the important structure of 4-substituted Hantzsch esters (XRH) reported in previous literatures, 17 XRH have been well-designed in this work (Scheme 4). The thermodynamic driving forces [free energy change, $\Delta G_{RD}^{o}(XRH^{\bullet+})$] and activation Gibbs free energies $[\Delta G_{RD}^{\neq}(XRH^{\bullet+})]$ of different structures of XRH$^{\bullet+}$ releasing R$^{\bullet}$ were computed using DFT, and the essential factors determining whether or not an XRH is alkylation reagent have been revealed in detail in this work.

2 Computational section
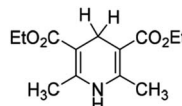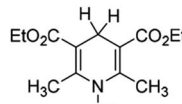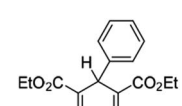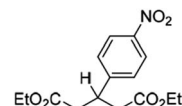
Molar free energy change of XRH$^{\bullet+}$ releasing R$^{\bullet}$ $[\Delta G_{RD}^{o}(XRH^{\bullet+})]$, molar enthalpy changes of XRH$^{\bullet+}$ releasing R$^{\bullet}$

Scheme 4 Chemical structures of 17 XRH examined in this work.

Table 1 Comparison between DFT calculation data and experimental data (kcal mol^{-1})

Compounds	$\Delta H_{HD}^{o}(XRH^{\bullet+})$ (DFT)^a	$\Delta H_{HD}^{o}(XRH^{\bullet+})$ (exp)^a	$\Delta\Delta H_{HD}^{o\ b}$
	30.27	31.40 (ref. 24a)	−1.13
	30.72	32.20 (ref. 24a)	−1.48
(16RH)	26.85	27.80 (ref. 24b)	−0.95
(15RH)	27.85	29.80 (ref. 24b)	−1.95

^{a} The unit is kcal mol^{-1}. ^{b} $\Delta\Delta H_{HD}^{o} = \Delta H_{HD}^{o}(XRH^{\bullet+})$ (DFT) − $\Delta H_{HD}^{o}(XRH^{\bullet+})$ (exp), the unit is kcal mol^{-1}.

[$\Delta H_{RD}^{o}(XRH^{\bullet+})$], and activation free energy of $XRH^{\bullet+}$ releasing $R^{\bullet}$ [$\Delta G_{RD}^{\neq}(XRH^{\bullet+})$] were computed in this work.

All quantum chemical calculations in this work were performed using Gaussian 09,[19a] and wave function analysis was performed using Multiwfn 3.7.[19b] First, find out the transition state of $XRH^{\bullet+}$ releasing $R^{\bullet}$, and calculate the Gibbs free energy and enthalpy of reactant, transition state and product of each elemental step. Through analyzing the difference between reactant and product, free energy changes and enthalpy changes of $XRH^{\bullet+}$ releasing $R^{\bullet}$ were obtained. The activation free energy and activation enthalpy could be obtained by comparing the reactant and the transition state in similar method.

First, the reactants, transition states and products of elemental step were geometrically optimized to convergence using the functional B3LYP[20] and the basis set 6-31G(d,p).[21] DFT-D3 empirical dispersion correction (BJ damping)[22] was applied, and SMD solvent model[23] (acetonitrile as the solvent) was used during the computation. After geometrical optimization, the vibration analysis was carried out using the same parameters. The results of vibration analysis showed that there is no imaginary frequency for all reactants and products; meanwhile, only one imaginary frequency was found for each transition state, and the direction of imaginary frequency was the same as that of C–C bond stretch, indicating that the transition states were correct. Intrinsic reaction coordinate (IRC) was then calculated for each transition state, and electron spin

density analysis of IRC-derived products showed that the cleavage products were alkyl radicals, not alkyl cations. Then, the thermodynamic correction was applied for each reactant, transition state and product at 298.15 K. The free energy was obtained by adding the single point energy to the Gibbs free

Table 2 Thermodynamic data and activation free energy data of $XRH^{\bullet+}$ releasing $R^{\bullet}$

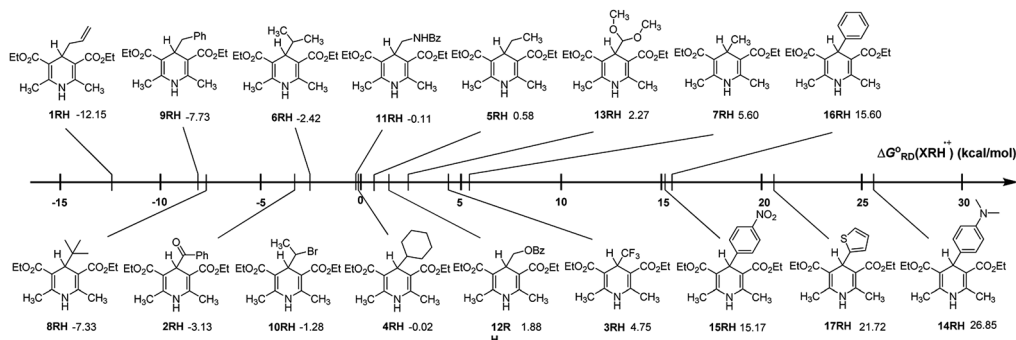| XRH	$\Delta H_{RD}^{o}(XRH^{\bullet+})^a$	$\Delta G_{RD}^{o}(XRH^{\bullet+})^a$	$\Delta H_{RD}^{\neq}(XRH^{\bullet+})^a$	$\Delta G_{RD}^{\neq}(XRH^{\bullet+})^a$
1RH	0.48	−12.15	3.29	3.47
2RH	9.43	−3.13	3.24	3.44
3RH	17.76	4.75	13.92	12.95
4RH	13.16	−0.02	5.68	5.38
5RH	13.71	0.58	9.64	8.66
6RH	11.49	−2.42	4.76	4.59
7RH	17.15	5.60	15.32	13.62
8RH	7.73	−7.33	1.44	1.17
9RH	5.37	−7.73	3.22	3.11
10RH	12.79	−1.28	7.77	7.45
11RH	13.47	−0.11	2.05	3.37
12RH	17.16	1.88	6.65	6.39
13RH	15.64	2.27	0.85	0.83
14RH	38.83	26.85	32.81	31.80
15RH	27.12	15.17	22.49	22.28
16RH	27.29	1.60	21.93	21.48
17RH	32.77	21.72	26.95	26.60

^{a} The unit is kcal mol^{-1}.

Fig. 1 Visual comparison of $\Delta G^o_{RD}(XRH^{\bullet+})$ among the 17 XRH in acetonitrile at 298.15 K.

energy correction value, and the enthalpy was obtained by adding the single point energy to the enthalpy correction value. Reaction rate constant (k_2) was obtained by Eyring equation [$k_2 = (k_B T/h)\exp(-\Delta G^{\neq}/RT)$].

In order to verify the applicability and accuracy of the calculation method in this work, first we calculated the molar enthalpy changes of four $XRH^{\bullet+}$ releasing H$^{\bullet}$ using the above method (termed "calculation values" in this work). The molar enthalpy changes of $XRH^{\bullet+}$ releasing H$^{\bullet}$ determined by the calorimetric titration method in previous literature were termed "experimental values".[24] The calculated value and the experimental value are listed in Table 1, and the data shows that the deviation between calculated values and the experimental values is less than 2.0 kcal mol^{-1}. Therefore, considering the experimental measurement error, it is appropriate to use the above calculation method to study the energy changes of $XRH^{\bullet+}$ releasing R$^{\bullet}$, and the results obtained are accurate and reliable.

3 Results and discussions

The calculation results, $\Delta H^o_{RD}(XRH^{\bullet+})$, $\Delta G^o_{RD}(XRH^{\bullet+})$ and $\Delta H^{\neq}_{RD}(XRH^{\bullet+})$, $\Delta G^{\neq}_{RD}(XRH^{\bullet+})$ are presented in Table 2.

3.1 $\Delta G^o_{RD}(XRH^{\bullet+})$

In order to discover the influence of structural factors on $\Delta G^o_{RD}(XRH^{\bullet+})$ values, the free energies changes of 17 $XRH^{\bullet+}$ releasing R$^{\bullet}$ are listed in Fig. 1 for comparison. From Fig. 1, it

is evident that the free energy changes of breaking C–C bond for $XRH^{\bullet+}$ releasing R$^{\bullet}$ varies greatly with the substituents, which ranges from -12.15 to 26.85 kcal mol^{-1}. Among 4-substituted Hantzsch ester structures investigated in this work, the Gibbs free energy of $XRH^{\bullet+}$ releasing R$^{\bullet}$ increased from $\Delta G^o \ll 0$ (-12.15 kcal mol^{-1}) to $\Delta G^o \gg 0$ (26.85 kcal mol^{-1}). $1RH^{\bullet+}$ (4-allyl-substituted Hantzsch ester) has the lowest $\Delta G^o_{RD}(XRH^{\bullet+})$ value as -12.15 kcal mol^{-1}, and $14RH^{\bullet+}$ (4-dimethylaminophenyl substituted Hantzsch ester) has the highest value of $\Delta G^o_{RD}(XRH^{\bullet+})$ as 26.85 kcal mol^{-1}, and the former is 39 kcal mol^{-1} lower than the latter. The thermodynamic data show that 1RH is the best alkylation reagents which spontaneously offers allyl radical in acetonitrile under the reaction condition of 298.15 K; in contrast, 14RH cannot give 4-dimethylaminophenyl group in chemical reactions. Such a large range of $\Delta G^o_{RD}(XRH^{\bullet+})$ values (-12.15–26.85 kcal mol^{-1}) indicates that the R group in the parent structure of XRH has a great influence on the value of $\Delta G^o_{RD}(XRH^{\bullet+})$, and the strength of C–C bond varies greatly in different structures of $XRH^{\bullet+}$.

Through comprehensive analysis and evaluation of $\Delta G^o_{RD}(XRH^{\bullet+})$, the results show that $XRH^{\bullet+}$ is possible (but not necessarily) to be an excellent R$^{\bullet}$ donors which are determined by the R substituents in 4-position. If R substituents in $XRH^{\bullet+}$ are not aromatic substituents, $XRH^{\bullet+}$ would be used as alkylation reagent; in contrast, if R substituents in $XRH^{\bullet+}$ are aromatic substituents, $XRH^{\bullet+}$ would not be used as R$^{\bullet}$ donors.
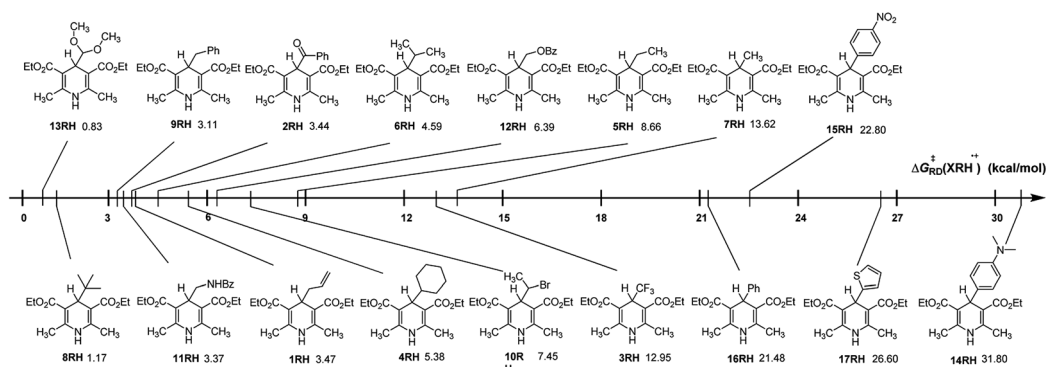

Fig. 2 Visual comparison of $\Delta G^{\neq}_{RD}(XRH^{\bullet+})$ among the 17 XRH in acetonitrile at 298.15 K.

3.2 $\Delta G_{RD}^{\neq}(XRH^{\bullet+})$

From columns 5 in Table 2, it is clear that the $\Delta G_{RD}^{\neq}(XRH^{\bullet+})$ values of $XRH^{\bullet+}$ releasing $R^{\bullet}$ range from 0.83 to 31.80 kcal mol^{-1}. As shown in Fig. 2, $\Delta G_{RD}^{\neq}(XRH^{\bullet+})$ value of $13RH^{\bullet+}$ releasing $R^{\bullet}$ is the smallest (0.83 kcal mol^{-1}); hence, the rate constant of $13RH^{\bullet+}$ releasing $R^{\bullet}$ (1.53×10^{12} M^{-1} s^{-1}) is greater than diffusion speed (10^{10} M^{-1} s^{-1}); while $\Delta G_{RD}^{\neq}(XRH^{\bullet+})$ value of $14RH^{\bullet+}$ releasing $R^{\bullet}$ is the largest (31.80 kcal mol^{-1}), so the rate constant of $14RH^{\bullet+}$ releasing $R^{\bullet}$ is lowest with 2.87×10^{-12} M^{-1} s^{-1} at 298.15 K in acetonitrile, which indicates that the reaction of $14RH^{\bullet+}$ releasing $R^{\bullet}$ is extremely slow, and therefore 14RH cannot be used as $R^{\bullet}$ donor in chemical reaction. The predicted rate constants of $XRH^{\bullet+}$ releasing $R^{\bullet}$ in this work range from 2.87×10^{-12} to 1.53×10^{12} (M^{-1} s^{-1}). Thus, it can be seen that there are many important chemical reactions *in vivo* or *in vitro* whose rates cannot be directly measured using experimental methods up to now. The reason is that some reactions are too fast, some are too slow and some have no detectable signals, *etc.* Because the accuracy of the calculation results is verified by experimental measured values, the rate constants of $XRH^{\bullet+}$ releasing $R^{\bullet}$ that cannot be measured experimentally can be estimated by the activation energy calculation method used in this work. Among the 17 XRH structures examined, $\Delta G_{RD}^{\neq}(XRH^{\bullet+})$ values of 13 XRH (1RH–13RH) are less than 16 kcal mol^{-1} ($k_2 = 6.29 \times 10^2$ M^{-1} s^{-1} at 298.15 K), $\Delta G_{RD}^{\neq}(XRH^{\bullet+})$ values of 4 XRH (14RH–17RH) span from 21.48 to 31.80 kcal mol^{-1} (1.07×10^{-3} to 1.07×10^{-11} M^{-1} s^{-1} at 298.15 K). The $\Delta G_{RD}^{\neq}(XRH^{\bullet+})$ values indicate that 1RH–13RH could be selected as $R^{\bullet}$ donor in chemical reactions, while 14RH–17RH cannot provide $R^{\bullet}$ as alkylation reagents. Further taking their structures into consideration, we find that R substituents in 14RH–17RH are aromatic substituents and the $\Delta G_{RD}^{\neq}(XRH^{\bullet+})$ of $XRH^{\bullet+}$ releasing $R^{\bullet}$ all larger than 21.4 kcal mol^{-1} which means 4-aromatic-group substituted Hantzsch esters cannot be used as $R^{\bullet}$ donors. If R substituents in $XRH^{\bullet+}$ are not aromatic substituents, $XRH^{\bullet+}$ (1RH–13RH) would be good $R^{\bullet}$ donors in radical reactions.

3.3 Entropy change and activation entropy change

Since Gibbs free energies $[\Delta G_{RD}^{o}(XRH^{\bullet+})]$, enthalpy changes $[\Delta H_{RD}^{o}(XRH^{\bullet+})]$, activation energies $[\Delta G_{RD}^{\neq}(XRH^{\bullet+})]$ and activation enthalpy changes $[\Delta H_{RD}^{\neq}(XRH^{\bullet+})]$ were obtained now, we calculated the entropy changes (ΔS_{RD}^{o}) and activation entropy changes ($\Delta S_{RD}^{\neq}$) of $XRH^{\bullet+}$ releasing $R^{\bullet}$ which are listed in Table 3.

From Table 3, it is found that the entropy changes of $XRH^{\bullet+}$ releasing $R^{\bullet}$, ΔS_{RD}^{o}, range from 38.75 to 51.26 cal mol^{-1} K^{-1}, and the activation entropy changes of $XRH^{\bullet+}$ releasing $R^{\bullet}$, $\Delta S_{RD}^{\neq}$, range from -4.42 to 5.69 cal mol^{-1} K^{-1}. ΔS_{RD}^{o} are positive values (cal mol^{-1} K^{-1}), which indicates that the chemical process of $XRH^{\bullet+}$ releasing $R^{\bullet}$ is the large entropy increase process. While the span of activation entropy changes of $XRH^{\bullet+}$ releasing $R^{\bullet}$, $\Delta S_{RD}^{\neq}$, is less than ± 5 cal mol^{-1} K^{-1}, which indicates that the chemical structures of $XRH^{\bullet+}$ do not change greatly in the transition state.

Table 3 Entropy changes and activation entropy changes of $XRH^{\bullet+}$ releasing $R^{\bullet}$

XRH	ΔS_{RD}^{o} ^{a}	$\Delta S_{RD}^{\neq}$ ^{b}
1RH	42.39	-0.60
2RH	42.13	-0.66
3RH	43.65	3.26
4RH	44.22	0.99
5RH	44.07	3.28
6RH	46.69	0.58
7RH	38.75	5.69
8RH	50.53	0.91
9RH	43.98	0.36
10RH	47.24	1.09
11RH	45.57	-4.42
12RH	51.26	0.87
13RH	44.85	0.08
14RH	40.21	3.37
15RH	40.12	0.72
16RH	39.24	1.50
17RH	37.09	1.18

^{a} From the equation, $\Delta S = (\Delta H - \Delta G)/T$, the unit is cal mol^{-1} K^{-1}.
^{b} From the equation, $\Delta S^{\neq} = (\Delta H^{\neq} - \Delta G^{\neq})/T$, the unit is cal mol^{-1} K^{-1}.

3.4 Main factors affecting free energy changes and activation free energy changes of $XRH^{\bullet+}$ releasing $R^{\bullet}$

3.4.1 Thermodynamic driving force and activation free energy. Because the XRH structure investigated in this work is 1,4-dihydropyridine compounds, only the R substituents in 4-position are different. In order to further explore the intrinsic relationship between the thermodynamic driving forces $[\Delta G_{RD}^{o}(XRH^{\bullet+})]$ and the activation energy $[\Delta G_{RD}^{\neq}(XRH^{\bullet+})]$, relationships between them are shown in Fig. 3. It can be seen from Fig. 3 that there is a certain correlation between the thermodynamic driving force and activation free energy changes of $XRH^{\bullet+}$ releasing $R^{\bullet}$, that is, $\Delta G_{RD}^{\neq}(XRH^{\bullet+})$ increases along with the increase of $\Delta G_{RD}^{o}(XRH^{\bullet+})$. But for all chemical reactions, there is no good linear correlation between $\Delta G^{\neq}$ and ΔG^{o}. This phenomenon shows that the thermodynamic driving force has an important influence on the activation energy, but it is not the only decisive factor.[25]
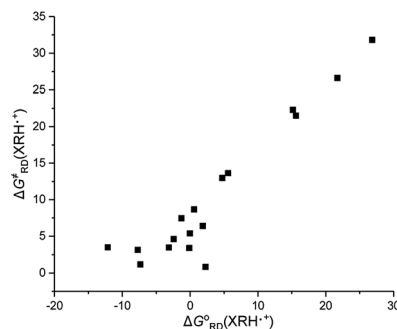

Fig. 3 Relationship between the activation free energies of 17 $XRH^{\bullet+}$ releasing $R^{\bullet}$ and the corresponding free energy changes of $XRH^{\bullet+}$ releasing $R^{\bullet}$ in acetonitrile at 298.15 K.
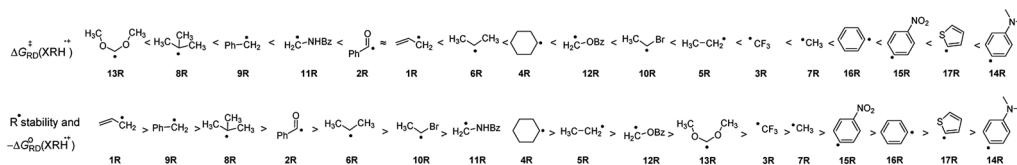
Fig. 4 The order of R[·] stability and activation free energies of 17 XRH[·+] releasing R[·].

3.4.2 The stability of R[·] and $\Delta G_{RD}^{\neq}$(XRH[·+]). It can be seen from the above discussion that many XRH with different structures can be used as R[·] donor. $\Delta G_{RD}^{\neq}$(XRH[·+]) values range from 0.83 to 13.62 kcal mol^{-1}, and the difference between the fastest and slowest rate constant is 10^{10}. Through the previous discussion, we have known that the thermodynamic driving force is an important factor affecting the activation energy of the reaction. Then, does it exist an internal relationship between the stability of R[·] and the reaction activity of XRH[·+] releasing R[·] $\Delta G_{RD}^{\neq}$(XRH[·+])? Considering the chemical process of XRH[·+] releasing R[·] with different structure, XRH[·+] → XH[+] + R[·], it is found that the values of molar free energy of XRH[·+] releasing R[·] [ΔG_{RD}^{o}(XRH[·+])] do reflect the relative stabilities of R[·]. The smaller ΔG_{RD}^{o}(XRH[·+]) is, the more stability R[·] is. On the basis of ΔG_{RD}^{o}(XRH[·+]) values computed in this work, the R[·] stability order in 1RH to 17RH molecules investigated in this work is 1R > 9R > 8R > 2R > 6R > 10R > 11R > 4R > 5R > 16R > 12R > 13R > 3R > 7R > 15R > 17R > 4R (Fig. 4). But according to the $\Delta G_{RD}^{\neq}$(XRH[·+]) values, the order of reactivity is 13R > 8R > 9R > 11R > 2R > 6R > 4R > 12R > 10R > 5R > 3R > 7R > 16R > 15R > 17R > 14R (Fig. 4). It is clear that there are significant differences between the order of stability of R[·] and the order of $\Delta G_{RD}^{\neq}$(XRH[·+]), and the stability of R[·] is not the decisive factor of $\Delta G_{RD}^{\neq}$(XRH[·+]). The results also show that the influence of structural factors on $\Delta G_{RD}^{\neq}$(XRH[·+]) is multifaceted and complicated.

3.4.3 Substituent effect. For 14RH, 16RH and 15RH, the R substituents at the 4-positions are *p*-dimethylaminophenyl, phenyl and *p*-nitrophenyl respectively, all of which are benzene ring structures with different *p*-substituents. Dimethylamino group ($\sigma_p = -0.83$) and nitro group ($\sigma_p = -0.78$) are relatively strong electron-donating and electron-withdrawing groups respectively. We designed these two groups in order to change the ability of XRH[·+] releasing R[·] to provide aromatic free radicals by tremendously changing the electronegativity of substituents. The relevant data are compared in Fig. 5. According to Fig. 5, the following conclusions can be made: (1) when the 4-position is a strong electron-donating group (dimethylamino group), free energy changes and activation energy changes of XRH[·+] releasing R[·] increased significantly (about 5–10 kcal mol^{-1}). (2) When the 4-position is a strong electron-withdrawing group (nitro group), free energy changes and activation energy changes of XRH[·+] releasing R[·] changed slightly (<1.5 kcal mol^{-1}). The above calculation results show that the change of electronegativity of benzene ring does not make XHR the donor of aromatic benzene free radicals. No matter it is electron-donating group or electron-withdrawing group, the abilities of XHR[·+] releasing R[·] are decreased, meanwhile the effect of electron-donating group on ability of XHR[·+] releasing R[·] is greater than that of electron-withdrawing group.[26]

3.4.4 Influence of steric hindrance and stability of R[·]. For 4-substituted Hantzsch esters 7RH, 5RH, 6RH and 8RH, R substituent groups are methyl, ethyl, isopropyl and *tert*-butyl (Fig. 6), respectively. The steric resistance of the substituents increases gradually with increasing of the stability of R[·]. From Fig. 6, it is found that ΔG_{RD}^{o}(XRH[·+]) of XRH[·+] releasing R[·] decrease from 5.60 to −7.33 kcal mol^{-1}, $\Delta G_{RD}^{\neq}$(XRH[·+]) of XRH[·+] releasing R[·] decrease from 13.62 to 1.17 kcal mol^{-1}, as gradually increasing of steric hindrance and stability of R[·] from 7RH[·+] to 8RH[·+] (Fig. 6).

	14RH	16RH	15RH
ΔG_{RD}^{o}(XRH[·+])	26.85	15.60	15.17
$\Delta G_{RD}^{\neq}$(XRH[·+])	31.80	21.48	22.28

Fig. 5 Effects of substituent groups on the activation free energy and free energy changes of XRH[·+] releasing R[·] (energy unit: kcal mol^{-1}).

Unit: kcal/mol	7RH	5RH	6RH	8RH
$\Delta G^{o}_{RD}(XRH^{\bullet+})$	5.60	0.58	-2.42	-7.33
$\Delta G^{\neq}_{RD}(XRH^{\bullet+})$	13.62	8.66	4.59	1.17

Fig. 6 Effects of size and stability of substituent groups on the activation free energy and free energy changes of $XRH^{\bullet+}$ releasing $R^{\bullet}$ (energy unit: kcal mol^{-1}).

Table 4 Diagnoses of reactivity of XRH using as radical agent according to $\Delta G^{\neq}_{RD}(XRH^{\bullet+})$

XRH	$\Delta G^{o}_{RD}(XRH^{\bullet+})^{a}$	$\Delta G^{\neq}_{RD}(XRH^{\bullet+})^{a}$	$k_{2}{}^{b}$	Diagnose
1RH	−12.15	3.47	1.76×10^{10}	Excellent $R^{\bullet}$ donor
2RH	−3.13	3.44	1.85×10^{10}	Excellent $R^{\bullet}$ donor
3RH	4.75	12.95	1.95×10^{3}	Medium $R^{\bullet}$ donor
4RH	−0.02	5.38	6.99×10^{8}	Excellent $R^{\bullet}$ donor
5RH	0.58	8.66	2.74×10^{6}	Excellent $R^{\bullet}$ donor
6RH	−2.42	4.59	2.66×10^{9}	Excellent $R^{\bullet}$ donor
7RH	5.60	13.62	6.29×10^{2}	Medium $R^{\bullet}$ donor
8RH	−7.33	1.17	8.59×10^{11}	Excellent $R^{\bullet}$ donor
9RH	−7.73	3.11	3.24×10^{10}	Excellent $R^{\bullet}$ donor
10RH	−1.28	7.45	2.12×10^{7}	Excellent $R^{\bullet}$ donor
11RH	−0.11	3.37	2.09×10^{10}	Excellent $R^{\bullet}$ donor
12RH	1.88	6.39	1.27×10^{8}	Excellent $R^{\bullet}$ donor
13RH	2.27	0.83	1.53×10^{12}	Excellent $R^{\bullet}$ donor
14RH	26.85	31.80	2.87×10^{-11}	Not $R^{\bullet}$ donor
15RH	15.17	22.28	2.78×10^{-4}	Not $R^{\bullet}$ donor
16RH	15.60	21.48	1.07×10^{-3}	Not $R^{\bullet}$ donor
17RH	21.72	26.60	1.88×10^{-7}	Not $R^{\bullet}$ donor

^{a} The energy unit is kcal mol^{-1}. ^{b} The unit is M^{-1} s^{-1}.

3.5 Judgment criteria of whether an XRH is a great alkylation reagent

Considering activation free energy of $XRH^{\bullet+}$ releasing $R^{\bullet}$ $[\Delta G^{\neq}_{RD}(XRH^{\bullet+})]$, the judgment criteria of XRH being a good $R^{\bullet}$ donor can be concluded reasonably (Table 4). Generally, in practice, an activation free energy ($\Delta G^{\neq}$) of 21 kcal mol^{-1} is usually used as a criteria in determining whether a reaction could easily occur at room temperature, according to the Transition State Theory (TST);[27] an activation free energy of 21 kcal mol^{-1} corresponds to a half-life of ~4.5 min and a 97% completion time of 22.3 min at room temperature, which indicate that the reaction can be completed within an acceptable time. Accordingly, the following predictions can be made: (1) if the value of $\Delta G^{\neq}_{RD}(XRH^{\bullet+})$ is larger than 21.0 kcal mol^{-1} ($k_{2} < 2.42 \times 10^{-3}$ M^{-1} s^{-1}), XRH could not be used as alkylation reagent, like 14RH–17RH. (2) If the value of $\Delta G^{\neq}_{RD}(XRH^{\bullet+})$ is larger than 17.5 kcal mol^{-1} ($k_{2} \leq 1$ M^{-1} s^{-1}), but smaller than 21.0 kcal mol^{-1} ($k_{2} \geq 2.42 \times 10^{-3}$ M^{-1} s^{-1}) XRH is a weak alkylation reagent. (3) If the value of $\Delta G^{\neq}_{RD}(XRH^{\bullet+})$ is larger than 12.0 kcal mol^{-1} ($k_{2} \leq 9.71 \times 10^{3}$ M^{-1} s^{-1}), but smaller than 17.5 kcal mol^{-1} ($k_{2} \geq 1$ M^{-1} s^{-1}) XRH is a medium alkylation

reagent, like 3RH and 7RH. (4) If the value of $\Delta G^{\neq}_{RD}(XRH^{\bullet+})$ is smaller than 12.0 kcal mol^{-1} ($k_{2} > 9.71 \times 10^{3}$ M^{-1} s^{-1}), XRH is an excellent alkylation reagent, like 8RH–13RH. Since $\Delta G^{\neq}_{RD}(XRH^{\bullet+})$ has no simple correlation with the XRH′ structure, the electronegativity and steric resistance, it is difficult to judge whether XRH can provide $R^{\bullet}$ in chemical reactions solely by experience. The calculation method and results provided in this work are helpful to guide the application of XRH as a free radical donor in organic synthesis.

4 Conclusions

In this work, 4 characteristic physical parameters, $\Delta H^{o}_{RD}(XRH^{\bullet+})$, $\Delta G^{o}_{RD}(XRH^{\bullet+})$, $\Delta H^{\neq}_{RD}(XRH^{\bullet+})$, $\Delta G^{\neq}_{RD}(XRH^{\bullet+})$ of 17 important XRH releasing $R^{\bullet}$ were calculated using DFT method. After careful discussion of the relevant thermodynamic and kinetic data, the following conclusions can be made: (1) through comprehensive analysis and evaluation of ΔG^{o} and $\Delta G^{\neq}$, it is found that $XRH^{\bullet+}$ is possible (but not necessarily) to be an excellent $R^{\bullet}$ donors which are determined by the R substituents in 4-position. (2) If R substituents in XRH are not aromatic groups, $XRH^{\bullet+}$ can release $R^{\bullet}$ as key intermediates,

therefore XRH could be used as alkylation reagents. In contrast, if R substituents in XRH are aromatic substituents, the key intermediates XRH$^{•+}$ could not release aromatic radical in chemical reactions, so XRH with aromatic substituents could not be used as alkylation reagents. (3) The thermodynamic driving force (Gibbs free energy) has an important influence on the activation energy, but it is not the only decisive factor. (4) There are significant differences between the order of R$^{•}$ stability and the order of $\Delta G_{RD}^{\neq}$(XRH$^{•+}$), and the stability of R$^{•}$ is not the decisive factor of $\Delta G_{RD}^{\neq}$(XRH$^{•+}$). In addition, the influence of structural factors on $\Delta G_{RD}^{\neq}$(XRH$^{•+}$) is multifaceted and complicated. (5) Change of electronegativity of benzene ring does not make XHR be an aromatic free radical donor. (6) According to $\Delta G_{RD}^{\neq}$(XRH$^{•+}$) values, the kinetic ability of XRH$^{•+}$ releasing R$^{•}$ can be predicted reasonably. ① If the value of $\Delta G_{RD}^{\neq}$(XRH$^{•+}$) is larger than 21.0 kcal mol^{-1}, XRH could not be used as an alkylation reagent. ② If the value of $\Delta G_{RD}^{\neq}$(XRH$^{•+}$) is larger than 17.5 kcal mol^{-1}, but smaller than 21.0 kcal mol^{-1}, XRH is a weak alkylation reagent. ③ If the value of $\Delta G_{RD}^{\neq}$(XRH$^{•+}$) is larger than 12.0 kcal mol^{-1}, but smaller than 21.0 kcal mol^{-1}, XRH is a medium alkylation reagent. ④ If the value of $\Delta G_{RD}^{\neq}$(XRH$^{•+}$) is smaller than 12.0 kcal mol^{-1}, XRH is an excellent alkylation reagent.

It is known that the reaction conditions of XRH using as alkylation reagents are quite complex, and this paper focuses on the intrinsic properties of key intermediate XRH$^{•+}$ releasing R$^{•}$. Since $\Delta G_{RD}^{\neq}$(XRH$^{•+}$) has no simple correlation with the XRH's structure, the electronegativity and steric resistance, it is difficult to judge whether XRH can be used as an alkylation reagent in chemical reactions solely by experience. The calculation method and results provided in this work are helpful to guide the application of XRH as a free radical donor in organic synthesis.

Conflicts of interest

The authors declare no competing financial interests.

Acknowledgements

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