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Instability and translocation through nanopores of DNA interacting with single-layer materials

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In this study, we use classical applied mathematical modelling to employ the 6–12 Lennard-Jones potential function along with the continuous approximation to investigate the interaction energies between a double-stranded deoxyribonucleic acid (dsDNA) molecule and two-dimensional nanomaterials, namely graphene (GRA), hexagonal boron nitride (h-BN), molybdenum disulphide (MoS₂), and tungsten disulphide (WS₂). Assuming that the dsDNA molecule has a perpendicular distance Δ above the nano-sheet surface, we calculated the molecular interaction energy and determined the relation between the location of the minimum energy and Δ . We also investigated the interaction of a dsDNA molecule with the surface of each nano-sheet in the presence of a circular hole simulating a nanopore. The radius of the nanopore that results in the minimum energy was determined. Our results show that the adsorption energies of the dsDNA molecule with GRA, h-BN, MoS₂, and WS₂ nano-sheets corresponding to the perpendicular distance $\Delta = 20$ Å are approximately 70, 82, 28, and 26 (kcal mol⁻¹), respectively, and we observed that the dsDNA molecule moves through nanopores of radii greater than 12.2 Å.

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1 Introduction

Owing to their small size and geometric and mechanical properties, nanomaterials have been used in many fields, including commercial applications, biomedicine, gene and drug delivery, clean energy, gas storage, gas separation, and materials science.^{1–7} Graphene (GRA) and graphene-like materials such as hexagonal boron nitride (h-BN), molybdenum disulphide (MoS₂), and tungsten disulphide (WS₂) have a two-dimensional (2D) atomic layer structure, as shown in Fig. 1. Such 2D nanomaterials have elicited increasing interest owing to their unique structures and exceptional properties, and they have been significantly promoted for many potential applications, including those in the fields of electronics, photonics, biomedical, and bioassays.^{9–12} 2D nanomaterials have essential features that remain unchanged upon adsorption of deoxyribonucleic acid (DNA); thus, they could prove to be promising for many applications such as self-assembly, therapeutic nucleic acids, and biosensors.^{14,35}

Although GRA, h-BN, MoS₂, and WS₂ sheets have structural similarities, the four nanomaterials have different properties that may lead them to behave differently from one another. For instance, the bond lengths in the B–N bonds in h-BN, C–C bonds in GRA, Mo–S bonds in MoS₂ and W–S bonds in WS₂ are 1.45 Å, 1.42 Å, 2.40 Å, and 2.43 Å, respectively.²⁰ In addition, h-

BN has a large ionicity, it is a good 2D insulator with a broad band gap, and its B–N bonds have an asymmetric distribution of charge. Moreover, h-BN has a smooth surface without any charge traps, and it also has a low dielectric constant and high temperature stability.¹³

Nanopores are very small gaps that biomolecules can use for transport through membranes, and could provide substantial opportunities to create the next generation of nanomaterial devices for various applications, especially in the nanomedical field and scanning microscopy.^{23,36,40} Numerous experiments and simulations have been conducted to explore the behaviour of DNA molecules interacting with nano-sheets, and the transfer mechanisms of DNA molecules through nanopores in such sheets.^{20,23–30,35,37–39}

Although previous studies have investigated interactions between DNA molecules and nano-sheets or nanopores, more research on the DNA sequencing by 2D materials is necessary. Mathematical modelling plays an important role in providing a description of experimental results and can help forecast new phenomena and new results. Additionally, mathematical

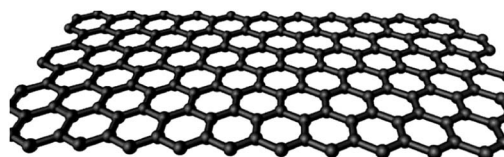


Fig. 1 Single layer structure of a two-dimensional material.

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modelling can be leveraged to accurately predict optimal configurations and physical parameters. In this study, we examine the interactions between a double-stranded DNA (dsDNA) molecule and monolayers of GRA, h-BN, MoS₂, and WS₂, and we determine the behaviour of a dsDNA molecule as it moves through a nanopore. We employ classical applied mathematical modelling using the basic principles of mechanics to exploit the continuous approximation with the 6–12 Lennard-Jones potential, which has been successfully used in several studies to determine the energy behaviours of nanostructures (for example, ref. 15–19). By minimising the binding energies, we determine the distance of the dsDNA molecule above the surface of each nano-sheet when the helix axis of the dsDNA molecule is perpendicular to the surface of the sheet. Additionally, we minimise the molecular interaction energy of the dsDNA molecules, which are assumed to move through a nanopore, to determine the radius b of the pore. Moreover, a comparison of the adsorption and the translocation of a dsDNA molecule through the nanopores of the four nano-materials is provided.

2 Modelling approach

The unit cell of B-DNA as shown in Fig. 2 is used in this study. This form of DNA is predominantly found in cells.⁸ Double-stranded DNA is assumed to contain 10.5 base-pairs, which gives an average of 792.75 atoms, in one complete helix rotation. Due to the large number of atoms in the dsDNA molecules and 2D-nanomaterials, they might be modelled using the continuous approximation, which assumes that the atoms are uniformly distributed over their entire surfaces, to formulate analytical expressions for their interactions. Thus, the interaction energy may be obtained as a double integral over the surface of each molecule, and it is given as

$$E = \eta_1 \eta_2 \int_{W_1} \int_{W_2} \Phi(\rho) dW_1 dW_2, \quad (1)$$

where η_1 and η_2 represent the mean surface densities of atoms on the two interacting molecules, and dW_1 and dW_2 are typical surface elements on the two non-bonded molecules. $\Phi(\rho_{ij})$ is the 6–12 Lennard-Jones potential function for atoms i and j located a distance ρ_{ij} apart on two distinct molecular structures, given by

$$\Phi(\rho) = -\frac{A}{\rho^6} + \frac{B}{\rho^{12}},$$

where $A = 4\epsilon\sigma^6$ and $B = 4\epsilon\sigma^{12}$ are the attractive and the repulsive constants, respectively. The attractive and the repulsive constants can be calculated using the empirical mixing laws $\epsilon_{12} = (\epsilon_1\epsilon_2)^{1/2}$, and $\sigma_{12} = (\sigma_1 + \sigma_2)/2$,^{31,32} where ϵ is the well depth and σ is the van der Waals diameter, which are taken from Rappi *et al.*²¹ The double integral and all the subsequent integrals in this study are surface integrals that are evaluated over the surfaces of molecules, and as shown in Kreyszig [ref. 33, pp. 443–452] and Kaplan [ref. 34, pp. 313–319], these surface integrals can be evaluated. Here, mathematical modelling is utilised to determine the molecular interaction energies between a dsDNA molecule and 2D-nanomaterials, by adopting the 6–12

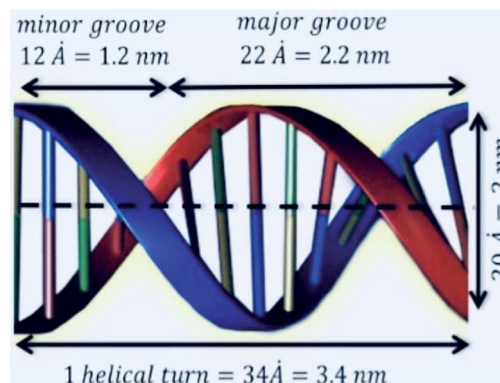


Fig. 2 Geometry of dsDNA molecule for one turn of helix (34 Å).

Lennard-Jones potential and the continuous approximation. Surface integration is utilised to calculate the total interaction energy of the nano-sheets with the dsDNA molecule due to the continuous approximation, which assumes that intermolecular interactions can be approximated by average atomic surface densities. The Cartesian coordinate system (x, y, z) is used as a reference to model the two interacting molecules - the nano-sheets and the dsDNA molecule. Thus, the coordinates of a typical point on the surface of a nano-sheet can be given by ($x, y, 0$), and the parametric equation of a typical point on the surface of the dsDNA may be given by

$$\left(\frac{R}{2} [\cos \Theta + \cos(\Theta - \phi) + t(\cos \Theta - \cos(\Theta - \phi))], \right. \\ \left. \frac{R}{2} [\sin \Theta + \sin(\Theta - \phi) + t(\sin \Theta - \sin(\Theta - \phi))], \frac{c\Theta}{2\pi} \right),$$

where ϕ is the helical phase angle parameter which can be either the special case $\phi = \pi$ or the physical value that leads to the measured locations of the major and minor grooves $\phi = 12\pi/17$. $R = 10 \text{ \AA}$ is the radius of the dsDNA helix, $c = 34 \text{ \AA}$ is the unit cell length of the dsDNA helix, and the parametric variables Θ and t are such that $-\pi < \Theta < \pi$ and $-1 < t < 1$. The adsorption onto nano-sheet surfaces and the translocation through nanopores by the dsDNA molecule are presented in the following sub-sections, respectively.

2.1 Interactions of dsDNA molecules and nano-sheets

2.1.1 Nano-sheet dsDNA adsorption. Here, we determine the binding energy of a dsDNA molecule to the surface of a nano-sheet. The binding energy is denoted as the potential energy between the bound DNA and the sheet surface and the sheet configuration is assumed to be infinite in extent. As illustrated in Fig. 3(a), the dsDNA is assumed to be situated above the sheet surface at distance Δ , which is the perpendicular spacing between the centre of the dsDNA and the sheet, and by defining a three-dimensional Cartesian coordinate system (x, y, z) with the centre point of the dsDNA molecule located at $(0, 0, P)$, where $P = \Delta + \frac{c\Theta}{2\pi}$. Now, by using eqn (1) we calculate the binding energy from the integral expression



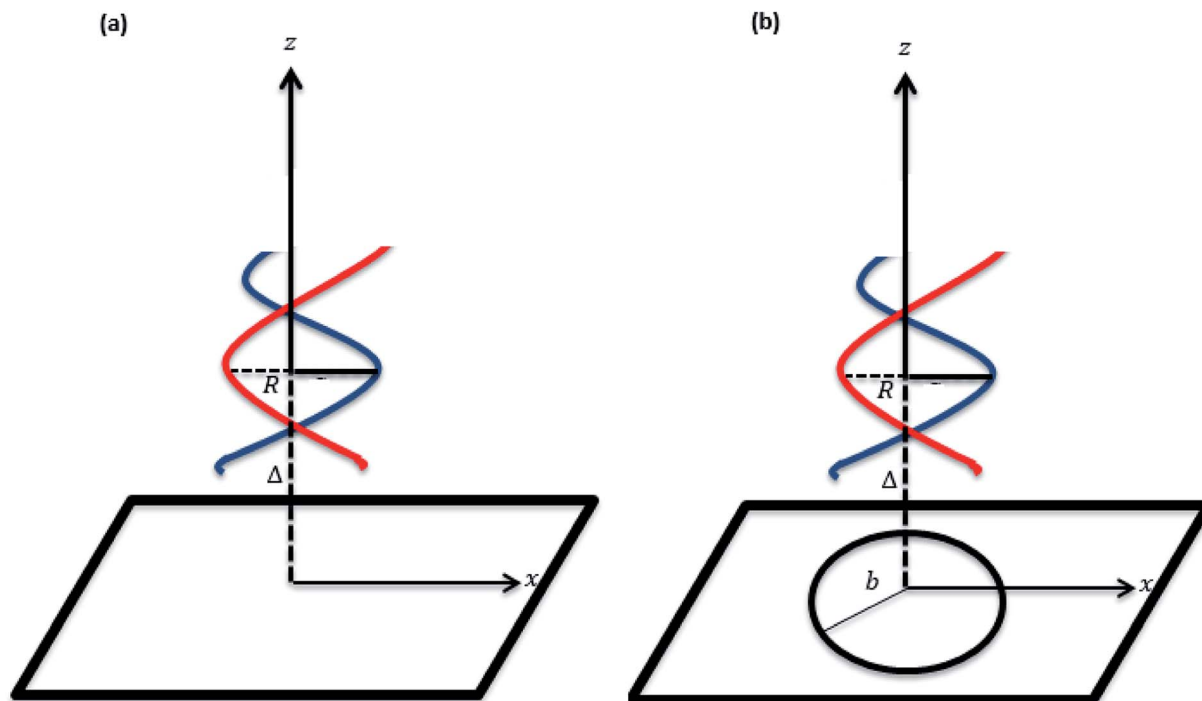


Fig. 3 Schematic for a dsDNA molecule (a) being adsorbed by the nanosheet and (b) penetrating a nanopore in the sheet.

$$E = \frac{Rc \sin(\phi/2) \eta_{D_i} \eta_j}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\pi}^{\pi} \int_{-1}^1 \left(\frac{-A}{\rho^6} + \frac{B}{\rho^{12}} \right) \times \left(1 + \frac{4R^2 \pi^2 \sin^2(\phi/2)}{c^2} t^2 \right)^{1/2} dt d\Theta dx dy, \quad (2)$$

where $\eta_{D_i} = \frac{\text{number of the atoms}}{\text{surface area of dsDNA}}$ ($i \in \{s, g\}$), is the atomic surface density of the dsDNA molecule, and

$\eta_j = \frac{\text{number of the atoms}}{\text{surface area of sheet}}$ ($j \in \{G, BN, M, W\}$) is the atomic surface density of the sheets, and they can be obtained

from $\eta_j = 4\sqrt{3}/9\iota$ where ι is the bonds length of the elements of the nano-sheets, they have listed in Table 1, and $\rho^2 = x^2 + y^2 + P^2$ denotes the distance between two typical points on the sheet and the dsDNA molecule. First, we find the interaction of a plane with point P , which is given by

$$E_{pp} = \eta_j \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \left(-\frac{A}{(x^2 + y^2 + P^2)^3} + \frac{B}{(x^2 + y^2 + P^2)^6} \right) dx dy, \quad (3)$$

introducing the integral E_n ($n = 3, 6$), where $E_{pp} = \eta_j(-AE_3 + BE_6)$, as

$$E_n = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} (x^2 + y^2 + P^2)^{-n} dx dy. \quad (4)$$

The details for the analytical evaluation of E_n are presented in the Appendix. Therefore, the total interaction E may be written as

$$E = \frac{Rc \sin(\phi/2) \eta_{D_i} \eta_j}{2} \int_{-\pi}^{\pi} \int_{-1}^1 E_{pp} (1 + \lambda t^2)^{1/2} dt d\Theta,$$

where $\lambda = \frac{4R^2 \pi^2 \sin^2(\phi/2)}{c^2}$. To evaluate the integral E over t , we introduce the integral J as follows

$$J = 2 \int_0^1 (1 + \lambda t^2)^{1/2} dt.$$

Making the substitution $t^2 = u$ yields the following

$$J = \int_0^1 (1 + \lambda u)^{1/2} u^{-1/2} du.$$

This integral can be written in a standard hypergeometric form as

Table 1 Numerical values for constants used in this paper

Constant	Value
Radius DNA, R	10 Å (ref. 8)
Length of DNA, c	34 Å (ref. 8)
Atomic density GRA, η_G	0.3818 Å ⁻²
Atomic density BN, η_{BN}	0.3661 Å ⁻²
Atomic density MoS ₂ , η_M	0.1336 Å ⁻²
Atomic density WS ₂ , η_W	0.1304 Å ⁻²
Atomic density dsDNA ($\phi = \pi$), $\eta_{D_s} = \frac{792.75}{943.75}$	0.84 Å ⁻²
Atomic density dsDNA ($\phi = 12\pi/17$), $\eta_{D_g} = \frac{792.75}{817.26}$	0.97 Å ⁻²



Table 2 Numerical values of the attractive and repulsive constants

Interaction	A (Å ⁶ kcal mol ⁻¹)	B (Å ¹² kcal mol ⁻¹)
GRA-DNA	791.8154556	2 424 599.652
h-BN-DNA	903.6818110	2 571 946.879
MoS ₂ -DNA	772.7401758	1 772 395.061
WS ₂ -DNA	739.1353066	1 690 802.161

$$J = 2F\left(\frac{-1}{2}, \frac{1}{2}; \frac{3}{2}; \frac{-4r^2\pi^2 \sin^2(\phi/2)}{c^2}\right).$$

Now we need only to evaluate the integral E over Θ , so we introduce the integral G_n

$$G_n = \int_{-\pi}^{\pi} \left(\frac{c\Theta}{2\pi} + \Delta\right)^{-2n} d\Theta$$

$$= (-2n + 1)^{-1} \left[(c/2 + \Delta)^{-2n+1} - (-c/2 + \Delta)^{-2n+1} \right].$$

Thus, the total binding energy between the dsDNA molecule and h-BN sheet surface is given by

$$E = 2R\pi \sin(\phi/2) \eta_{D_s} \eta_j F\left(\frac{-1}{2}, \frac{1}{2}; \frac{3}{2}; \frac{-4R^2\pi^2 \sin^2(\phi/2)}{c^2}\right)$$

$$\times \left(\frac{-A}{2}G_2 + \frac{B}{5}G_5\right). \quad (5)$$

2.1.2 Translocation of dsDNA through nanopores. In this section, the energy behaviour of the dsDNA molecule penetrating through a nanopore is investigated. The minimum energy is calculated to determine the preferred radius b of the nanopore for the dsDNA molecule to travel through. Here two cases of the helical phase angle ϕ are considered, a dsDNA molecule of radius R is assumed to be located above the sheet nanopore at distance Δ , as shown in Fig. 3(b). It is assumed that the sheet configuration is infinite in extent and remains planar, but has a single hole of radius b . A typical point on this plane has coordinates $(a \cos \vartheta, a \sin \vartheta, 0)$ and the hole in the surface of the plane is assumed to be located at $z = 0$ so that the coordinates of a typical point of the hole can be given by $(b \cos \vartheta, b \sin \vartheta, 0)$ where $b < a < \infty$. Without loss of generality, and owing to the symmetry of the sheet, the coordinates of a typical point on the dsDNA molecule may be given from $(\Omega, 0, \Delta + c\Theta/2\pi)$, where $\Omega^2 = R^2[\cos^2(\phi/2) + t^2 \sin^2(\phi/2)]$. The distance ρ from a typical point of the plane to a typical point of the dsDNA is given by

$$\rho^2 = a^2 + \Omega^2 - 2a\Omega \cos \vartheta + (\Delta + c\Theta/2\pi)^2$$

$$= (a - \Omega)^2 + 4a\Omega \sin^2(\vartheta/2) + (\Delta + c\Theta/2\pi)^2,$$

and the total potential energy of the dsDNA of general helical angle $\phi = 12\pi/17$ with respect to the nanopore is given by

$$E = \frac{Rc\eta_{D_s}\eta_j \sin(\phi/2)}{2\pi} \int_{-\pi}^{\pi} \int_{-\pi}^{\pi} \int_{-1}^1 \int_b^{\infty} a \left(-\frac{A}{\rho^6} + \frac{B}{\rho^{12}}\right)$$

$$\times \left(1 + \frac{4R^2\pi^2 \sin^2(\phi/2)}{c^2} t^2\right)^{1/2} da dt d\Theta d\vartheta. \quad (6)$$

Now, we consider a case where only the interaction energy for the special helical phase angle $\phi = \pi$ is considered. In this case, the formal analytical details are slightly simpler than for the general case. Thus, in this case we have $\Omega = Rt$ and the total energy E is given by

$$E = \frac{Rc\eta_{D_s}\eta_j}{2\pi} \int_{-\pi}^{\pi} \int_{-\pi}^{\pi} \int_{-1}^1 \int_b^{\infty} a \left(-\frac{A}{\rho^6} + \frac{B}{\rho^{12}}\right)$$

$$\times \left(1 + \frac{4R^2\pi^2}{c^2} t^2\right)^{1/2} da dt d\Theta d\vartheta, \quad (7)$$

where η_{D_s} represents the mean atomic surface density of the dsDNA molecule in this special case. We may therefore determine the total energy of the dsDNA molecule with the h-BN nanopore E from the following integral expression

$$E = \frac{Rc\eta_{D_s}\eta_j}{2\pi} (-AQ_3 + BQ_6), \quad (8)$$

where the integral Q_n can be written as

$$Q_n = \int_{-\pi}^{\pi} \int_{-\pi}^{\pi} \int_{-1}^1 \int_b^{\infty} a \left[(\Omega - a)^2 + 4a\Omega \sin^2(\vartheta/2) + (\Delta + c\Theta/2\pi)^2 \right]^{-n}$$

$$\times \left(1 + \frac{4R^2\pi^2}{c^2} t^2\right)^{1/2} da dt d\theta d\vartheta.$$

By letting $\xi = (\Omega - a)^2 + (\delta + c\theta/2\pi)^2$ and $\gamma = 4a\Omega$, we define the integral W_n as

$$W_n = \int_{-\pi}^{\pi} [\xi + \gamma \sin^2(\vartheta/2)]^{-n} d\vartheta.$$

Making the substitution $\sin^2(\vartheta/2) = u \Rightarrow d\vartheta = u^{-1/2}(1 - u)^{-1/2} du$, the integral W_n becomes

$$W_n = 2 \int_0^1 [\xi + \gamma u]^{-n} u^{-1/2} (1 - u)^{-1/2} du$$

$$= 2\xi^{-n} \int_0^1 [1 + (\gamma/\xi)u]^{-n} u^{-1/2} (1 - u)^{-1/2} du$$

$$= 2\pi \xi^{-n} F(n, 1/2; 1; -\gamma/\xi),$$

where $F(a^*, b^*; c^*; z^*)$ is the standard hypergeometric function. By using a Pfaff transformation,⁴¹ W_n becomes

$$W_n = 2\pi \xi^{-n} \left(\frac{\xi}{\xi + \gamma}\right)^{1/2} F\left(1 - n, 1/2; 1; \frac{\gamma}{\xi + \gamma}\right)$$

$$= 2\pi \xi^{-n} \left(\frac{\xi}{\xi + \gamma}\right)^{1/2} \sum_{k=0}^{n-1} \frac{(1 - n)_k (1/2)_k}{(k!)^2} \left(\frac{\gamma}{\xi + \gamma}\right)^k$$

$$= 2\pi \left[(Rta)^2 + (Z + c\Theta/2\pi)^2 \right]^{-n+1/2}$$

$$\times \sum_{k=0}^{n-1} \frac{(4aRt)^k (1 - n)_k (1/2)_k}{(k!)^2 \left[(Rt + a)^2 + (\Delta + c\Theta/2\pi)^2 \right]^k}.$$



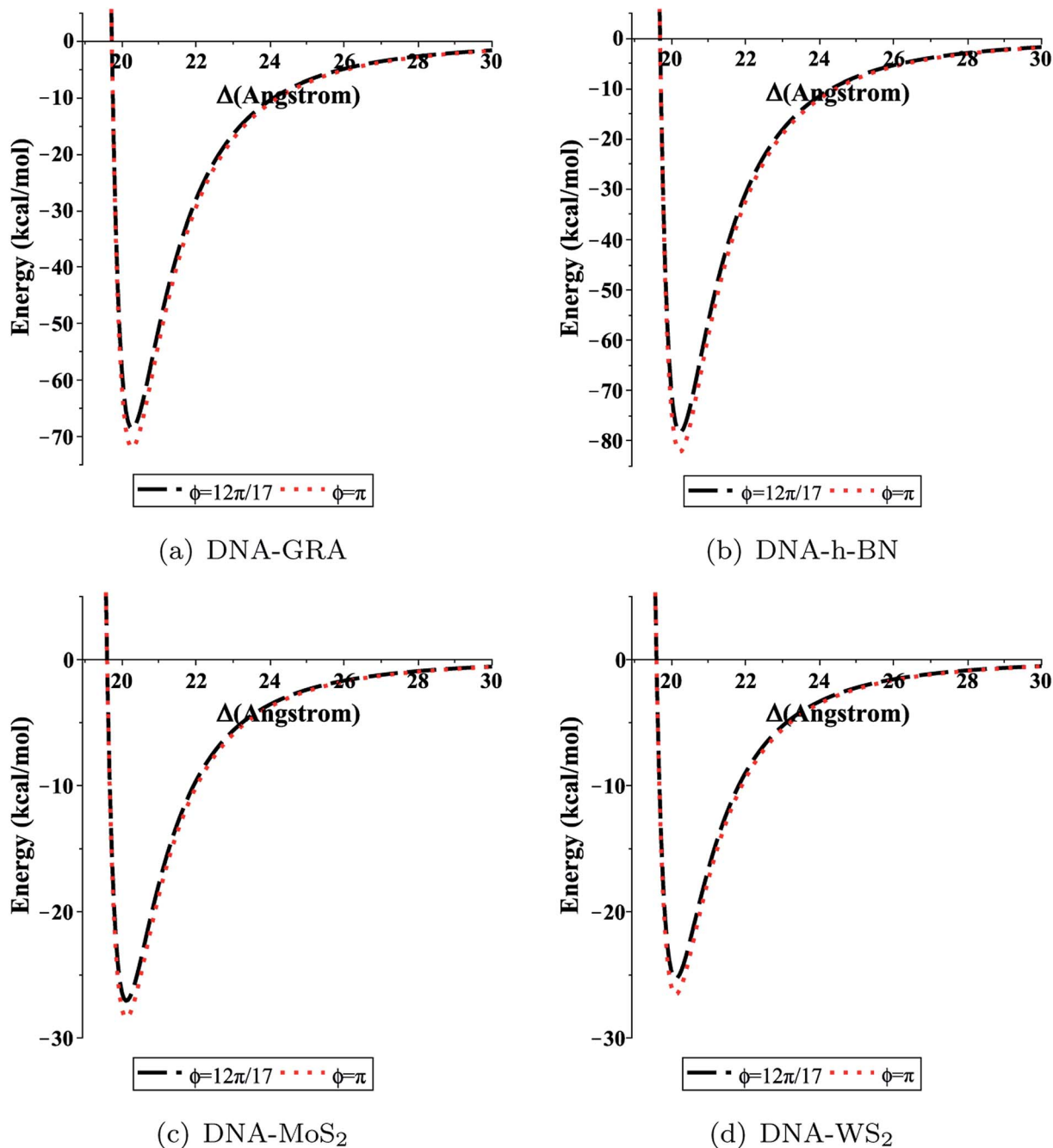


Fig. 4 Total interaction energy between dsDNA and the nano-sheets with respect to the perpendicular distance Δ for both cases $\phi = 12\pi/17$ (black dashed lines), and $\phi = \pi$ (red dotted lines).

Table 3 Main results of the interaction of dsDNA with nano-sheets

Interaction	Interaction energy, E (kcal mol ⁻¹)		Perpendicular distance, Δ (Å)	
	$\phi = 12\pi/17$	$\phi = \pi$	$\phi = 12\pi/17$	$\phi = \pi$
DNA-GRA	-68.56763	-71.97261	20.27102	20.27102
DNA-h-BN	-78.28127	-82.16862	20.23138	20.23139
DNA-MoS ₂	-27.05815	-28.40183	20.11723	20.11723
DNA-WS ₂	-25.29527	-26.55140	20.11584	20.11584

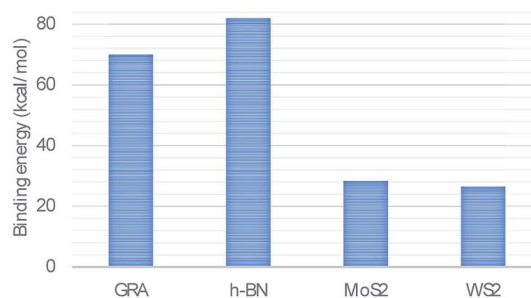


Fig. 5 Comparison of binding energies for a dsDNA molecule adsorbed on GRA, h-BN, MoS₂, and WS₂.



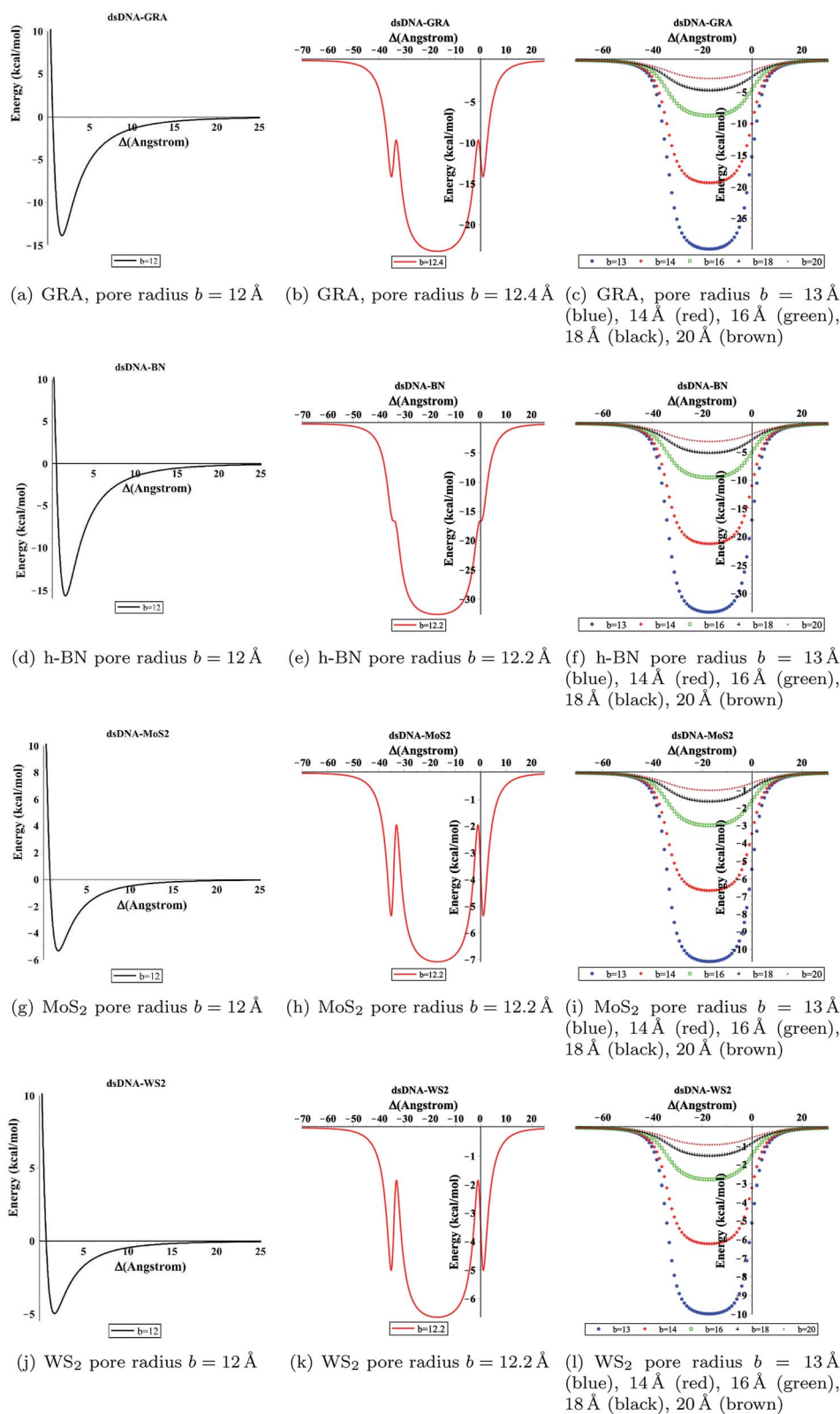


Fig. 6 Total energy associated with the interaction of dsDNA with pores showing different values of radius b with respect to the perpendicular distance Δ .



Thus, the integral Q_n has three remaining integrals over a , t and Θ as

$$Q_n = 2\pi \sum_{k=0}^{n-1} \frac{(4R)^k (1-n)_k (1/2)_k}{(k!)^2} \int_{-\pi}^{\pi} \int_{-1}^1 \int_b^{\infty} \frac{a^{k+1} t^k}{\left[(Rt-a)^2 + (\Delta + c\Theta/2\pi)^2 \right]^{n-1/2} \left[(Rt+a)^2 + (\Delta + c\Theta/2\pi)^2 \right]^{k+1/2}} \times \left(1 + \frac{4R^2\pi^2 t^2}{c^2} \right)^{1/2} da dt d\Theta,$$

which is becoming extremely complex, so we may use a standard integration package, such as MAPLE, to calculate the numerical results of these integrals.

3 Results and discussion

We evaluated eqn (5) and (8) using the algebraic computer package MAPLE together with the constant values in Tables 1 and 2. The relationship between the binding energy and the perpendicular distance Δ in the interactions between a dsDNA molecule and nano-sheets of the four 2D-nanomaterials GRA, h-BN, MoS₂, and WS₂, for two cases of the helical phase angle ϕ , are shown in Fig. 4 and Table 3. It is clear from Fig. 4 and Table 3 that the profile of the adsorption for the h-BN nano-sheet is significantly different from that for the other materials. The results show that the interaction between dsDNA and the h-BN nano-sheet is stronger than those between dsDNA and the other three materials, as the former reaches the lowest minimum energy. The comparison of binding energies of dsDNA with GRA, h-BN, MoS₂, and WS₂ is shown in Fig. 5, where the order of binding energy of the dsDNA molecule with the nano-sheets is h-BN > GRA > MoS₂ > WS₂. However, as shown in Table 3, the perpendicular distances Δ for these four materials to the centre of the dsDNA molecule is not significantly different, and the distance from the edge of the dsDNA to the surface of the sheets is given by $(\Delta - c/2 \approx 3.2 \text{ \AA})$, which is similar to that of GRA found in an earlier study.¹⁷ We note that the same equilibrium spacing profile is observed for the dsDNA molecule from the surface of each nano-sheet, and that only the magnitude of the energy differs. Our results for interaction energies with respect to the perpendicular distance of a dsDNA molecule from the nano-sheet surfaces are in good agreement with those given in the literature.^{20,22} We note from the difference of the results that

the binding energies are sensitive to the Lennard-Jones constants (A and B), which are obtained using the values of the well depth ϵ and the van der Waals diameter σ . Herein, we comment that although the structures of the four nano-sheets are similar, h-BN possesses different properties. For example, h-BN sheets may be more uniform with regard to electronic properties than other nano-sheets, which might affect the interactions with DNA molecules. In addition, Fig. 6 graphically shows the relation between the total potential energy and the perpendicular distance Δ for different values of the pore radius b . We observe that the dsDNA does not penetrate a nanopore in any nano-sheet type when the radius of the pore $b < 12.1 \text{ \AA}$, and the interaction energy tends to infinity, which corresponds to a positive value of Δ . These results are in good agreement with the results of other works, as shown in Table 4. Furthermore, we observe that the dsDNA molecule moves closer to the sheet surface as the hole radius increases, due to the lower repulsive force from the sheet surface, and the fact that the dsDNA molecule has more space to move through the gap. Once the gap radius is larger than 12.2 \AA , the dsDNA molecule can penetrate the surface of the sheet, which corresponds to negative values of Δ . These results are similar to those observed for GRA in an earlier study,¹⁸ and they are consistent with other experimental results, as shown in Table 4. Our results show that the optimal value of the gap radius b , where the minimum energy occurs, is $b \approx 12.8 \text{ \AA}$.

4 Conclusions

In summary, the molecular interaction energies of a dsDNA molecule with 2D monolayers of GRA, h-BN, MoS₂, and WS₂, as well as the translocation of the dsDNA through nanopores in these materials, have been investigated using applied mathematical modelling. Comparison of the calculated adsorption characteristics shows that the interaction between dsDNA and the h-BN nano-sheet is stronger than those between dsDNA and the other three materials, with the order of interactions being h-BN > GRA > MoS₂ > WS₂. By minimising the binding energies, we obtained the equilibrium distances of the dsDNA to the nano-sheets in the case where the helix axis of the dsDNA molecule is perpendicular to the sheet surface. We found that the minimum energies occur for distances $\Delta \approx 20 \text{ \AA}$. In addition, our results show that the dsDNA molecule passes through nanopores with radii b larger than 12.2 \AA in these materials. Moreover, the fundamental results in this study can provide promising guidance for designing new 2D nanomaterial-based

Table 4 Values of the nanopore radius at which a dsDNA molecule moves through the hole in the nano-sheet

Nanomaterial	Radius of pore (\AA)	
	This study	Other studies
GRA	>12.2	12.2 (ref. 23) 12 (ref. 25)
h-BN	>12.1	12.5 (ref. 26) ≈ 12.5 (ref. 27)
MoS ₂	>12	12.15 (ref. 28) 14 (ref. 29)
WS ₂	>12	>10 (ref. 30)



devices for several applications, particularly in biomedical and biological fields.

Appendix: analytical evaluation of (4)

In this appendix, we present the analytical details for the evaluation of eqn (4). We begin by defining the integral E_n ($n = 3, 6$), as

$$E_n = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} (x^2 + y^2 + P^2)^{-n} dx dy. \quad (9a)$$

We first integrate eqn (9a) with respect to y by making the substitution $y = \sqrt{x^2 + P^2} \tan \delta \Rightarrow dy = \sqrt{x^2 + P^2} \sec^2 \delta d\delta$, when $y = -\infty \Rightarrow \delta = -\pi/2$, and when $y = \infty \Rightarrow \delta = \pi/2$, thus integral E_n becomes

$$\begin{aligned} E_n &= \int_{-\pi/2}^{\pi/2} \int_{-\infty}^{\infty} [(x^2 + P^2) \tan^2 \delta + x^2 + P^2]^{-n} \sqrt{x^2 + P^2} \sec^2 \delta dx d\delta \\ &= \int_{-\pi/2}^{\pi/2} \int_{-\infty}^{\infty} [(x^2 + P^2)(1 + \tan^2 \delta)]^{-n} \sqrt{x^2 + P^2} \sec^2 \delta dx d\delta \\ &= \int_{-\pi/2}^{\pi/2} \int_{-\infty}^{\infty} (x^2 + P^2)^{-n} (1 + \tan^2 \delta)^{-n} (x^2 + P^2)^{1/2} \sec^2 \delta dx d\delta \\ &= \int_{-\pi/2}^{\pi/2} \int_{-\infty}^{\infty} (x^2 + P^2)^{1/2-n} (1 + \tan^2 \delta)^{-n} \sec^2 \delta dx d\delta. \end{aligned}$$

Using $\sec^2 \delta = 1 + \tan^2 \delta$, the integral E_n is given by

$$E_n = \int_{-\pi/2}^{\pi/2} \int_{-\infty}^{\infty} (x^2 + P^2)^{1/2-n} \sec^{-(2n-2)} \delta dx d\delta,$$

from $\sec^{-(2n-2)} \delta = \cos^{(2n-2)} \delta$, E_n becomes

$$E_n = \int_{-\pi/2}^{\pi/2} \cos^{2n-2} \delta d\delta \int_{-\infty}^{\infty} (x^2 + P^2)^{1/2-n} dx.$$

Since cosine is an even symmetric function, we can rewrite the integral as

$$E_n = 2 \int_0^{\pi/2} \cos^{2n-2} \delta d\delta \int_{-\infty}^{\infty} (x^2 + P^2)^{1/2-n} dx,$$

where the first integral can be evaluated using

$$\int_0^{\pi/2} \sin^\beta \theta \cos^\omega \theta d\theta = \frac{1}{2} \mathbf{B}\left(\frac{\beta+1}{2}, \frac{\omega+1}{2}\right),$$

where $\mathbf{B}(\chi, \kappa)$ is the beta function (in this case $\beta = 0$ and $\omega = 2n - 2$ and note that $\mathbf{B}(\chi, \kappa) = \mathbf{B}(\kappa, \chi)$). Thus, the integral E_n becomes

$$E_n = \mathbf{B}(n - 1/2, 1/2) \int_{-\infty}^{\infty} (x^2 + P^2)^{1/2-n} dx.$$

We make a further substitution of $x = P \tan \phi$ and proceed as in the previous integral, so the integral becomes

$$E_n = P^{2-2n} \mathbf{B}(n - 1/2, 1/2) \mathbf{B}(n - 1, 1/2).$$

We may evaluate the beta function given above using

$$\mathbf{B}(\chi, \kappa) = \frac{\Gamma(\chi)\Gamma(\kappa)}{\Gamma(\chi + \kappa)} = \frac{(\chi - 1)!(\kappa - 1)!}{(\chi + \kappa - 1)!},$$

to obtain

$$E_n = \frac{\pi}{(n - 1)P^{2n-2}}.$$

Thus, for ($n = 3, 6$) we have

$$E_3 = \frac{\pi}{2P^5}$$

$$E_6 = \frac{\pi}{5P^{10}}.$$

Conflicts of interest

The authors declare that there is no conflict of interest.

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