How does the Li-distribution in the 16d sites determine the stability of $A_3(Li,Ti_5)O_{12}$ ($A = Li$ and Na)?†

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Li$_3$(Li$_{1/3}$Ti$_{5}$)O$_{12}$ (LTO) is a stable and safe negative electrode material for Li-ion batteries, and its Na substitute Na$_3$(Li$_{1/3}$Ti$_{5}$)O$_{12}$ (NTO) is a counterpart for the Na-ion battery. In LTO and NTO, a sixth of the Ti-sites (16d) in the spinel framework are replaced by Li: Li mixing in the 16d sites. For conducting theoretical studies on these materials, e.g., density functional theory (DFT) calculations, one has to confront the astronomical number of combinations of Li distribution in 16d sites to construct model structures, of which the size is sufficiently large to represent the bulk material properties. Only a limited number of models, whose structures are a priori specified by “researcher intuition,” have been examined thus far, and how Li-mixing determines the material stability has yet to be clarified. Herein, we statistically analyzed the DFT total energy of more than 2 × 10$^6$ model structures of LTO and NTO that were extracted from the 4 × 10$^8$ possible combinations of Li-mixing with computer-aided symmetry analysis and an automated model building system. The local energy analysis further revealed the local stability/instability of each structure. We found that LTO and NTO stability can be well explained by the apparent coulombic repulsion between Li$^+$ in the 16d sites as if they were placed in a matrix of dielectric constants of 1.92 and 2.04 for LTO and NTO, respectively. That is, the sum of the inverse of the Li–Li distance (S) serves as a good descriptor in predicting the stability of these materials. The extent to which the O$^{2-}$ anions are displaced from the Wyckoff position (32e) is considered to differentiate NTO from LTO. However, the electronic structure of NTO does not significantly differ from that of LTO unless S exceeds a certain limit. These results suggest that the spinel framework tolerates the structural instability and variety to some extent, which is important in constructing a spinel structure with the mixing of other cations, thereby replacing the rare element Li.

1 Introduction

Secondary batteries are indispensable in daily life. Their recent widespread usage has necessitated further improvement in the safety of rechargeable Li-ion batteries.$^{1-3}$ Li$_i$Ti$_{5}$O$_{12}$ (LTO)$^{4-11}$ is a negative electrode material for Li-ion secondary batteries and, compared to conventional carbon electrodes, is safer for use in electric and plug-in hybrid electric vehicles. The Li ion is inserted in and extracted from the LTO according to

$$(Li_3)_{8a}(Li_{1/3},Ti_{5/3})_{16d}(O_{12})_{32e} + 3Li^+ + 3e^- \rightleftharpoons (Li_6)_{16c}(Li_{1/3},Ti_{5/3})_{16d}(O_{12})_{32e} \quad (1)$$

where superscripts 8a, 16d, 32e, and 16c, denote the Wycko positions of the $Fd\bar{3}m$ symmetry (spinel). During the reaction, the Ti–O framework maintains its spinel structure, which is stabilized by the Li$^+$ cations substituted for a sixth of Ti$^{4+}$ cations situated in the 16d sites (referred to as “Li-mixing”). The material functions as a negative electrode for Li-ion batteries when Li ions move between 8a and 16c sites. Li insertion only slightly expands the spinel lattice ([Li$_i$]$^{8a}$[Li$_{1/3}$, Ti$_{5/3}$]$_{16d}$[O$_{12}$]$_{32e}$: 8.36 Å, [Li$_6$]$_{16c}$[Li$_{1/3}$, Ti$_{5/3}$]$_{16d}$[O$_{12}$]$_{32e}$: 8.35 Å), so that the charge and discharge process is strain-free. This structural robustness yields good cycling properties (durability) and renders LTO suitable as a safe negative electrode material.

Our group has recently synthesized a Na substitute for LTO, Na$_3$Li$_{1/3}$Ti$_{5}$O$_{12}$ (NTO), in which all the Li$^+$ cations situated in the 8a sites are replaced by Na and, as in LTO, a sixth of the 16d sites are occupied by Li.$^{15-18}$ During the charge and discharge process with the Na counter electrode, NTO works as a negative electrode when Na ions in the 8a sites move to the 16c sites.
which, as in the LTO in eqn (1), proceeds with negligible strain in the lattice \((\text{Na}_3)_{8a}(\text{Li}_1,\text{Ti}_3)_{16d}(\text{O}_{12})_{32e}\) + \(3\text{Na}^+ + 3\text{e}^- \rightleftharpoons (\text{Na}_6)_{16c}(\text{Li}_1,-\text{Ti}_1)_{16d}(\text{O}_{12})_{32e},\)

(2)

structure than the regular composition \(\text{LiMn}_2\text{O}_4\).\cite{54} Thus, it is anticipated that the significant difference in cation mixing in the 16d sites should manifest itself in the stability of the spinel structure of LTO and NTO.

As NTO is synthesized by substituting Na for Li at the 8a sites of LTO, the states of the LTO precursor must be reflected in the 16d sites of the NTO product.\cite{15,37} Examination of the circumstances of the 16d sites provides the key to understanding why only NTO can retain its spinel structure among sodium titanates.

As mentioned above, previous theoretical studies have focused only on a limited number of stable structure configurations.\cite{16,18,21,23,31} Some studies attempted to predict the most stable structure of the LTO using systematic models.\cite{20,33} However, the models used were non-stoichiometric compositions, of which the results could contain computational errors, such as the dynamic and static correlations as well as the spin contamination, affecting the results of electrode materials.\cite{27,34} To precisely correct the errors, the multi-referenced calculations should be performed, which is often prohibited by the computational cost. Although the genetic algorithm,\cite{45,46} which seeks the most stable structure among those considered, may be applied to investigate the stable configuration of the dopant, it is beyond the scope of this technique to quantitatively relate the configuration to the stability (or instability). That is, we still do not know how Li-mixing determines the stability of the spinel framework of LTO and NTO, despite its importance in determining material performance.

Herein, we analyzed the DFT total energy of a number of randomly generated structural models to elucidate how the Li configuration influences the stability of LTO and NTO. The recent growth of super-computing systems has aided in the construction of a database that allows for statistical treatment of these randomly generated models. We used a super-computing system provided by Kyushu University and an in-house coded tool,\cite{25,47} which generates numerous model structures and analyzes data obtained by the DFT calculation. The statistical method can provide the descriptors for machine-learning, whereby one can determine the most stable structure from numerous candidates through the interpolative scheme. In addition, local energy analysis\cite{48,50} of the obtained stable structures allowed for the evaluation of the influence of local strain caused by Li-mixing. This analysis revealed the difference between LTO and NTO with respect to their stability.

2 Computational procedure

To represent the chemical composition of LTO (\(\text{Li} : \text{Ti} : \text{O} = 4 : 5 : 12\)) and NTO (\(\text{Na} : \text{Li} : \text{Ti} : \text{O} = 3 : 1 : 5 : 12\)), we adopted a \(1 \times 1 \times 3\) supercell model in which the number of sites was 24(8a), 48(16d), and 96(32e). All 32e sites were occupied by O\(^2^-\), and all 8a sites were occupied by Li\(^+\) in LTO or Na\(^+\) in NTO. The Li\(^+\) and Ti\(^{4+}\) cations are mixed in the 16d sites in such a way that Ti\(^{4+}\) occupy five-sixth of the sites (40 sites), and the remaining one-sixth (eight sites) is occupied by Li\(^+\). This results in \(48\text{C}_0\) = 377, 348, 994 possible configurations if the symmetry is not taken into account. We first randomly generated 15000
configurations, out of which 8444 were extracted by eliminating the combinations of equivalent symmetry. The set of energies calculated for all 8444 configurations by DFT, without optimization, was statistically analyzed for LTO and NTO. From the regression line, 58 models considered relevant were selected, and these models were optimized by DFT to obtain stable structure and energy. Further analysis of these selected data yielded more reliable regression results. The atomic positions were optimized whereas the lattice parameters were not. The purpose of the present work is to clarify the stability of the spinel framework by the Li-mixing. To preserve the spinel framework structure, we fixed the lattice parameter to the experimental values. Unstable structures would be unable to keep the framework, and hence takes a long time for the lattice parameters to be optimized. The optimization per se and the final structure with which the unstable state would end up are beyond the scope of the present study.

The energy and electronic states were obtained by DFT using the ab initio calculation package VASP on the ITO supercomputing system provided by Kyushu University. The structural models were generated, and the calculated data were managed using an in-house coded Python program.\(^\text{25-47}\) The structures were visualized using VESTA.\(^\text{42}\)

GGA-PBE\(^\text{45}\) was adopted as the exchange and correlation functional of DFT. The electrons in the core region were treated with the projector-augmented plane-wave (PAW) method\(^\text{44,45}\) with an energy cutoff of 450 eV. The number of valance electrons was one, one, ten, and six for Li, Na, Ti, and O, respectively. The \(k\)-points were sampled on the Monkhorst mesh\(^*\) of \(4 \times 4 \times 2\). The calculation conditions were optimized in our previous study,\(^\text{45}\) which confirmed that the corrections of the onsite Coulomb and dispersion forces hardly influence the electronic states and structures.

The formal valence in \(\text{X}_2\text{LiTi}_5\text{O}_{12}\) is \(X = +1, \text{Li} = +1, \text{Ti} = +4\) and \(O = -2\), respectively, suggesting that these ions are in the closed shell structure. The experimental EELS (Electron Energy Loss Spectrums) study indeed corroborates \(\text{Ti}^{(v)}\) in \(\text{X}_2\text{LiTi}_5\text{O}_{12}\). We hence consider that, as a first approximation, it should be reasonable to calculate under the spin-restriction with excluding the open shell structure. In the stable structures, the closed shell configuration is the electronic ground state and \(\text{Ti}^{(iii)}\) will occur in the high energy excited state; therefore, the spin-unrestricted calculation is not required. As for the unstable structures, \(\text{Ti}^{(iii)}\) could partially occur, for which the spin-restricted calculation would entail the error associated with the static electronic correlation. We made a brief consideration in Results and discussion regarding this issue.

By analyzing the local energy of the optimized structures using the QMAS program,\(^\text{48}\) we investigated how the structural strain caused by the Li-mixing depends on the configurations as well as how it differs in LTO and NTO. Local energy/stress analysis using the QMAS code has been adopted successfully in grain boundary systems and surface systems.\(^\text{49-55}\) The local energy discussed in this paper was obtained by integrating the energy density in the local region into which the calculated cell is divided into centered atoms.\(^\text{56,57}\) This method can clarify how much each atom contributes to the total energy obtained in the calculated cell. When the local energy is small, it is relatively unstable. Conversely, when the local energy is significant, it is stable. Therefore, by comparing the same atomic species, we are able to analyze the effect of structural distortion on the stability of the spinel framework in LTO and NTO.

3 Results and discussion

3.1 \(\text{Li}_x\text{Ti}_5\text{O}_{12}\) (LTO) system

Fig. 1 shows the total energy computation results of LTO. In Fig. 1(a), the y-axis is the total energy \(E\) before the structure optimization, indicating the structural stability (i.e., the more negative, the more stable), and \(S\) in the x-axis is the sum of the reciprocal distance between Li in the 16d sites; namely,

\[
S = \frac{1}{\sum_{ij} \frac{1}{r_{ij}}}
\]

which contains the combination of the distance between eight Li\(^+\) cations, i.e., \(8C_2 = 28\) terms. Energy \(E\) of 8444 structures in Fig. 1(a) obviously positively correlates with \(S\), from which we considered that LTO is in the relatively stable Li-mixing states when \(S\) is less than \(3.86\ \text{Å}^{-1}\). An additional 5000 structures were then generated using the same method as the initial 15 000 models, under the constraint \(S/\text{Å}^{-1} \leq 3.86\), and the result of the corresponding DFT calculation is indicated by the red cross in Fig. 1(b). The stability of LTO with respect to Li-mixing positively correlates with the sum of the reciprocal distance between Li in the 16d sites.
The results shown in Fig. 1 were obtained by fixing all the ions at the ideal Wyckoff positions. However, both theoretical and experimental studies suggest that the $O^{2-}$ anions in LTO are slightly displaced from the 32e sites, the ideal position for the spinel (rock-salt) structure because O would be too far from Ti to form a sufficient coordinate Ti–O bond.\textsuperscript{17,18} To discuss the stable structures, structural optimization is required to consider the stabilization brought by the coordinate Ti–O bond properly. We optimized the structures of 58 models that were selected from those in Fig. 1(a), indicated by orange squares, as (1) 18 structures from the most stable (the top 18), (2) ten structures from the least stable (the bottom ten), and (3) 30 structures from the entire range of $S$ with an equal interval. The result after the optimization is shown in Fig. 1(c), confirming the strong correlation between $E$ and $S$. The regression line is given by:

$$E/eV = a(S/A^{-1}) + b \quad (4)$$

where $a/\text{eV} = 7.49 \pm 0.36$ and $b/eV = -1350.4 \pm 1.8$ with $R^2 = 0.968$. It can be concluded that the stability of LTO is strongly correlated with the Li configuration measured by the sum of the reciprocal distance between Li. Namely, the greater the reciprocal distance, which implies that the Li$^+$ cations spatially aggregate, the less stable the structure. This result suggests that the apparent coulombic repulsion between Li$^+$ in the 16d sites dominates the stability of LTO. The orbital correlation, resulting from the coordinate Ti–O bond, is little correlated to the $S$–$E$ relation because the structural optimization did not affect it, as shown in Fig. 1(a) and (b). The energy density of states (DOS) corroborates this argument (Fig. 2). The coordinate Ti–O bond cleaves the band gap,\textsuperscript{17,24} of which the magnitude measures the orbital correlation. As shown in Fig. 2, when $S$ is less than 4.0–4.1 $A^{-1}$, the band gap is almost constant at ca. 2 eV wherever the structure is in the $E$–$S$ plot. The Li configuration hardly influences the coordinate Ti–O bond unless Li$^+$ extremely aggregates. In any Li configuration, the O$^{2-}$ anions in LTO can displace from the 32e sites in such a way that the electronic states converge to those observed in previous studies\textsuperscript{16–18,21–29} or in Fig. 2. Note that aggregated Li systems ($S/A^{-1} > 4.2$) may include static correlation errors because, as the DOS structures imply, Ti$^{4+}$ would be reduced to Ti$^{3+}$ by the surrounding Li$^+$. These errors, however, will hardly affect the results and discussion in the present study. In order for Ti(III) to occur, local structures resembling Li$_2$Ti$_2$O$_4$ should appear, which is caused by the localization of Li in the 16d sites. The apparent correlation with the sum of the inverse distance between Li (Fig. 1) exactly indicates that these Li-localized structures are unstable. This correlation is no more than apparent as it contains the above mentioned errors. The total energy of the structures with a high $S$ value may thus be slightly more negative (i.e., more stable) if these errors are corrected. However, specifying the ground state out of conceivable numerous spin-unrestricted solutions is intractable in reality. It would therefore barely deserve the laborious cost to specify the ground electronic states for these unstable structures. Previous studies had proposed the
most stable structures based on the models that should may contain the above-mentioned errors, which can be validated in the present study based on numerous models. Fig. S33 reveals that the most stable structures sorted out of the randomly built 13 444 models insignificantly differ from that in the previous studies, implying that the spin-unrestricted calculation is not necessary insofar as the electronic ground state of titanias has the closed shell configuration.

3.2 Na₃LiTi₅O₁₂ (NTO) system

Fig. 3 summarizes the results for NTO. As in LTO (Fig. 1(a)), the total energy of NTO, $E$ (NTO), is strongly correlated with the sum of the reciprocal distance between Li at the 16d sites, $S$ in Fig. 3(a), wherein the results of DFT calculations for 8444 configurations are without structural optimization. In real NTO, however, the O$^{−}$ anions are displaced from the ideal Wyckoff position $(32e)$, the extent of which has been experimentally and theoretically confirmed to be more significant than in LTO. For example, the results of high-intensity X-ray diffraction are better fitted by placing O in the 192i $(x,y,z)$ sites rather than in the $32e$ $(x,x,x)$ sites. Structural optimization would hence influence NTO more than LTO. As for LTO, we optimized a total of 58 structures, indicated by orange squares in Fig. 3(a) that are (1) the top 18 stable, (2) the bottom ten unstable, and (3) 30 models taken out of Fig. 3(a) with an equal interval in $S$. The O-displacement in the optimized structures is consistent with the experimental observation (Fig. S32†). The $E$ (NTO) versus $S$ relation after the optimization and the DOS are summarized in Fig. 3(b) and 4, respectively.

The coordinate Ti–O bonds, achieved by the optimization, create a band gap (Fig. 4) and significantly lower the total energy. The strong correlation between $E$ and $S$ is nevertheless persistent (Fig. 3(b)). The linear optimization with the analogous equation in eqn (4) yields $a/\AA\, eV = 7.07 \pm 0.36$ and $b/eV = -1318.7 \pm 1.7$ with $R^2 = 0.964$. The band gap of structures with $S$ less than 4.0–4.1 Å$^{-1}$ is nearly constant at ca. 2 eV. These observations are in line with those of LTO. We can, therefore, conclude that, as in LTO, the apparent coulombic repulsion between Li$^+$ in the 16d sites dominates the stability of the spinel framework of NTO with little orbital correlation between Ti and O. The analogous outcome drawn from LTO and NTO suggests that the 8a sites occupied by Li or Na are insignificant in determining the stability as far as the steady-state is concerned.

The present study implies that the stability of the (Ti, Li)–O spinel framework is dictated by the magnitude of the repulsion between Li, regardless of LTO or NTO. In effect, the models selected as the top 10 stable structures for LTO have identical Li configurations to those of NTO, and their order of stability is also identical for LTO and NTO (Fig. 5 and 6). A similar trend is observed for all selected (optimized) structures (see ES†). The relationship between LTO and NTO is clearly seen in the overlapping data. However, there is a slight difference in the slope in which the overlay is the energy difference ($\Delta E$) from the most stable structure versus $S$ for LTO and NTO (Fig. 3(c)). It can thus be concluded that, for either LTO or NTO, the stability of the spinel framework is determined by the distance between Li in the 16d sites, and their configuration hardly influences the electronic

![Fig. 3](image-url)  
Fig. 3 Perspective views of the optimized top ten stable structures and their $\Delta E$ values (the energy difference in the total energy from the most stable structure) for Li₅Ti₅O₁₂. In the left panels, spheres in green, blue, and red represent Li, Ti, and O atoms, respectively; spheres in dark and light green represent Li atoms at the 16d and 8a sites, respectively. In right panels, the Li atoms in the 16d sites are shown as the green spheres, and the other atoms are shown as the sticks.

![Fig. 4](image-url)  
Fig. 4 An example of the DOS of optimized structures of Na₃LiTi₅O₁₂ (others are shown in the ES†). $E_F$ represents the Fermi energy.
states from these results. This accompanies the fact that the optimized DOS is independent of the configuration if \( S \) is sufficiently small (Fig. 2 and 4) and is identical in LTO and NTO.\(^{17}\)

The strong ionicity of an alkali metal, as mentioned in a previous study,\(^{17}\) is attributed to the stability and is well supported by the coulombic repulsion between Li at the 16d sites. Spinel titanates can be viewed as ionic crystals comprised of alkali metals (Li\(^+\), Na\(^+\)) at the 8a sites and a complex spinel framework formed by the coordinate Ti–O bonds. The stability of the spinel framework is determined by the coulombic repulsion between cations (Li\(^+\)) in the 16d sites. In other words, the more homogeneous the Li-mixing, the more stable the framework. It can be expected from the present calculations that the spinel network is retained as a stable one as long as the substituting cation compensates the charge and has the ionic radius that the 16d sites can accommodate. Currently, only LTO and NTO are available as alkali spinel titanates, in which Li, a rare element, is used as the mixing cation. A further benefit is gained from the viewpoint of resource issues and industrial cost if we succeed in replacing Li with Na, an abundant element. The DFT calculation (Fig. S31\(^\dagger\)) suggests that a titanate, in which Na (ionic radius 102 pm) is mixed in the 16d sites, forms the spinel framework. Replacing Li\(^+\) in the 8a sites with Cu\(^+\) (60 pm) or Ag\(^+\) (100 pm) can also retain the spinel structure. On the other hand, inserting K\(^+\) (137 pm) in the 8a sites destroys the structure, indicating that the maximum ionic radius that can be accommodated in the 8a sites lies somewhere between the size of Ag\(^+\) and K\(^+\). Examining the stability of the spinel framework in this way, one can explore and design new functional materials.

The difference in the slope between LTO and NTO shown in Fig. 3(c) is explained as follows. The coulombic repulsion potential is expressed as:

\[
E_{\text{rep}} = \sum_{ij} \frac{Z_{ii}Z_{jj}}{r_{ij}}
\]

If we assume the valence of Li, \( Z_{Li} \), in the 16d sites is + 1.0, constant \( A \) is identical to the slope \( a \) in eqn (4), i.e., 7.49 and 7.07 Å eV for LTO and NTO, respectively, which translate into apparent specific permittivity of 1.92 and 2.04. Namely, the lithium ions in the 16d sites repel each other as if they were in the matrix of this apparent permittivity, which is not an observable property of matter. It is reasonable, nevertheless, that the apparent permittivity for NTO is greater than that for LTO. The high permittivity of barium titanates, which are strong dielectrics and represent substances with perovskite structures, stems from the displacement of oxide ions and titanium cations from the ideal Wycko positions.\(^{67–71}\) In addition, in LTO and NTO, the O\(^2–\) anions are displaced from the Wycko positions, the extent of which is proved from experimental and theoretical considerations.\(^{17,18}\) The difference in the apparent permittivity between LTO and NTO can be partly explained by the greater oxygen displacement in NTO. That is, the configuration of the anions in NTO is less regular than in LTO, resulting in a situation where the polarization vectors around Li\(^+\) hardly cancel out.

### 3.3 Local energies of LTO and NTO

The O\(^2–\) anions are more displaced from the 32e sites in NTO than in LTO, and the trend is independent of Li-mixing at the 16d sites. While the net stability of the spinel framework is discussed in Sections 3.1 and 3.2, we now deal with the local stability resulting from the oxygen position. The local energy of the structures belonging to the top ten (Fig. 5 and 6) was analyzed, and the results are shown in Fig. 7. The difference in the local energy between LTO and NTO is insignificant, which is surprising when considering the greater local distortion and the greater variance in the bond length in NTO caused by the oxygen displacement. However, as discussed in Section 3.2, the stability of the spinel structure is explicable in terms of the repulsion between Li\(^+\) in the 16d sites, and the coordinate Ti–O bonds are deemed identical in LTO and NTO. Although the structure (or symmetry) is more disrupted in NTO than LTO, the coordinate bonds nearly equally stabilize their structure, of which the total stability is determined by the inter-ionic interaction so that the energetics are insensitive to local disruption. The oxygen position in LTO and NTO has a high degree of freedom, serving as an absorber against structural distortion. The cycle stability of...
LTO as an active electrode material for the Li-ion batteries was described in the previous study. Our previous study examined the stability of NTO as an active material for the Na-ion batteries. This stability stems from the spinel structure of LTO and NTO. As for the stability of the spinel electrode materials other than LTO and NTO, the material Li[sub]8a(Li[sub]x−1Mn[sub]2−xMn[sub]3−1/2)16dO[sub]4, in which a part of the 16d sites was occupied by Li, more stably retains its spinel structure than the regular composition LiMn[sub]2O[sub]4. We have recently suggested the importance of the Li-substitution in the 16d sites for NTO to retain the spinel structure. The partial substitution of Li in the 16d sites in the spinel network thus plays an important role in maintaining the structural stability of the electrode during the charge and discharge cycles. The statistical analysis of the Li-substituted models in the present study is relevant to considering its stability as an active electrode material. In the present study, we examined the spinel Ti–O framework in the material to find that the difference in its stability between LTO and NTO is insignificant. Hence the difference in the redox potential of Li and Na, the former is lower than the latter, should be almost directly reflected in the electrode potential of LTO and NTO.

4 Conclusion

We investigated how Li configurations partially replacing Ti in the 16d sites of alkali titanates (LTO and NTO) influence the structural stability based on DFT calculations, statistical treatment, and local energy analysis. The stability (total energy) of alkali titanates is linearly well-correlated with the sum of the reciprocal distance between Li in the 16d sites with $R^2 > 0.96$. This suggests that the stability of the spinel titanate framework is described by the coulombic repulsion between the mixing Li; hence, the sum of the inverse of Li–Li distance is a good descriptor for predicting the stability of these materials. The distinction between LTO and NTO shows up in the apparent relative permittivity from the slope of the linear relationship and in the matrix where Li’ repels each other, as 1.92 and 2.04 for LTO and NTO, respectively, in which the greater displacement of O from the 32e sites in the latter is presumably reflected. The local energy analysis suggests, however, that there is no significant difference between LTO and NTO. Thus, it can be concluded that the spinel framework of alkali titanates tolerates a certain degree of destabilization, alluding to a diversity in stable spinel structures. In effect, a material in which Na, instead of Li, is partially substituted for Ti is calculated such that it should retain its structure. The present study proves that investigating the stability of the spinel framework is crucial for replacing the rare element Li with an abundant element.

Conflicts of interest

There are no conflicts to declare.

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