Bismuth subsalicylate, a low-toxicity catalyst for the ring-opening polymerization (ROP) of L-lactide (L-LA) with aliphatic diol initiators: synthesis, characterization, and mechanism of initiation†

Maria Guadalupe Ortíz-Aldaco, José E. Báez †* and J. Oscar C. Jiménez-Halla †

The ring-opening polymerization (ROP) of L-lactide (L-LA) was induced by the catalytic action of bismuth subsalicylate (BiSS) using linear aliphatic diols [HO(CH2)nOH, where n = 2, 3, 4, 5, 6, and 8] as initiators and chain transfer agents. The theoretical and experimental degree of polymerization (DP) in all samples of α,ω-hydroxy telechelic poly(L-lactide) (HOPLLAOH) had a good agreement in all samples, an effect attributed to the interaction of BiSS with HO(CH2)nOH inducing a transfer reaction. HOPLLAOH was synthesized and characterized by a range of analytical techniques, confirming the insertion of methylene groups from the initiator into the main chain of the polyester. The glass-transition temperature (Tg) of HOPLLAOH was found to be proportional to the number of methylene groups present in the diol. Various parameters regarding the ROP of L-LA were studied, such as temperature, time of reaction, amount of catalyst, and the nature of the diols. A kinetic study of the reaction allowed the determination of the rate constants (k) and activation energy (Ea). A mechanism of initiation is proposed based on a computational study using density functional theory (DFT), evidencing the role of the alkyl diol as an initiator, producing an alkoxide (Bi-OROH). This species then acts as a nucleophile, attacking the carbonyl group, inducing its insertion, and ultimately completing the ring-opening of L-LA.

Introduction

Aliphatic polyesters are some of the most versatile biodegradable polymers due to their moderate mechanical properties and good biodegradability and biocompatibility.1–4 Polylactide (PLA) and its derivatives, are frequently encountered aliphatic polyesters, having mechanical properties similar to those of poly(styrene), and are characterized by a high modulus and low elongation to break.7 PLA is a relatively brittle plastic but possesses good strength, and as such finds utility in biomedicine, including as a controlled drug delivery carrier, tissue engineering scaffold, surgical suture, and bone fixation material.7–10 PLA also has stereoisomers that are interesting materials in their own right, including poly(L-lactide) (PLLA), poly(D-lactide) (PDLA), and poly(D,L-lactide) (PDLLA). PLLA has gained attention because of its excellent biocompatibility, mechanical properties,11 and application as a precursor for a range of polymeric materials such as scaffolds for engineered tissue, films, macrodiols, polyurethanes, and others.12

The conventional method for the synthesis of high molecular-weight PLLA is ring-opening polymerization (ROP).11,12 The three most common mechanisms used in cyclic ester ROP are coordination–insertion, enzymatic, and anionic.14 Coordination–insertion ROP is initiated by an alcohol or initiator and catalyzed by metal complexes based on Lewis acidic metals such as tin, aluminum, and zinc.15 Studies on the ROP of cyclic esters such as L-lactide [L-LA] have been explored using different metal compounds, for example, (1) a series of binuclear zirconium salen-type complex was used as a catalyst in the ROP of L-LA and obtained a conversion >90% within 10 min, yielding high molecular weight PLLA with low dispersity, and the kinetic studies showed that the ROP of L-LA catalysed by this complex had a first-order dependency with respect to the [L-LA].16 (2) In another study of the ROP of L-LA, a series of Na complexes bearing ketiminate ligands used as catalyst was reported, the polymerization results revealed that all Na complexes had the highest catalytic activity at 0 °C in the presence of a high concentration of BN0H with a conversion of 99%.17 (3) On another side, a series of N-arylcyano-β-diketiminate zinc complexes with cyano groups in the ortho position of the aromatic ring was explored as a catalyst in the polymerization of L-LA, the zinc complexes with one cyano group showed good activity in the ROP of L-LA with a conversion of 95%.18 Currenty, tin(II) 2-ethyl hexanoate (stannous octoate or tin...
octoate, SnOct₂ is the most widely used catalyst to promote the ROP of cyclic esters despite an ongoing debate over its cytotoxicity.29,30

In this regard, the development of alternative, non-toxic catalytic systems is of considerable interest. The element bismuth, which is present in numerous pharmacology formulations, is considered to have very low toxicity; however, it has only been studied to a limited extent as a catalyst of ROP processes. Our interest in the use of bismuth-based catalysts is further motivated by the fact that Mexico produces the second most bismuth in the world (825 metric tonnes).21 A number of bismuth compounds have been reported to catalyze ROP processes, including inorganic derivatives such as BiX₃ (X = Cl, Br, I),32 the homoleptic acetate,33 2-ethyl hexanoate,34 hexanoate,35 triflate,36–38 alkoxides,29 the heteroleptic salicylate,39,40 (salen)bismuth alkoxides,32 and the diphenyl bismuth bromide.41,42 Bismuth(III) compounds have proven to be versatile catalysts for a variety of organic transformations.43–46 Bismuth subsalicylate (BiSS), an antiscorbutic and antigastritis drug commonly marketed in oral medications (e.g. Pepto Bismol®),39–41 has recently been demonstrated to be a less toxic catalyst for the ROP of cyclic esters.42–44 The ROP of cyclic esters was primarily, developed by Kricheldorf et al.,44 and the same group has reported the use of bismuth(III) complexes of carboxylic acids as useful catalysts in the ROP of ε-caprolactone (CL) and ε-lactide (ε-LA) to give poly(ε-caprolactones) (PCLs) and poly(ε-lactides) (PLLAs).45,46 Kricheldorf has also reported that bismuth alkanoates Bi(O₂CR)₃ may be used in the ROP of lactones.47

Other bismuth species have also been demonstrated to have interesting catalytic activity, exemplified by the polymerization of ε-LA at high temperatures without significant racemization initiated by bismuth(III) acetate [Bi(OAc)₃].47 These results demonstrate that Bi(OAc)₃ is a highly efficient initiator, allowing the syntheses of di-, tri- and tetrafunctional PLLAs. A comparison of the reactivity of Bi(OAc)₃ with that of SnOct₂ in the polymerization of ε-LA under the same reaction conditions, showed that good conversion was achieved (>90%) with both catalysts within a rather short time.47

Homoleptic Bi(III) alkoxides bearing sterically bulky alkoxide ligands (–OtBu or –OCMe₂iPr) have also been shown to be highly active catalyst for ε-LA ROP. Increasing the steric bulk of the alkoy ligand further from –OtBu to –OCMe₂iPr decreases the coordination ability of the monomer and lowers the activity of the catalyst. These Bi(III) alkoxides are considerably more active catalysts for ε-LA ROP than the commonly-used SnOct₂/butanol initiator combination. The simple formulation, low toxicity, and high activity of Bi(III) alkoxides make them very attractive catalyst candidates.48

BiSS (Scheme 1) has recently been demonstrated to be a less toxic catalyst for the ROP of cyclic esters,46–51 and as a catalyst/initiator for homo- and copolymerizations of lactones and lactides.52–55 An exciting result was the discovery that BiSS favored the presence of less blocky sequences than copolyesters prepared with SnOct₂ under identical conditions.55 However, neither the mechanism of the reaction nor the ROP of lactones using BiSS as a catalyst has been reported. The significant difference in toxicity between BiSS and SnOct₂ (Table 1),56 suggest the possibility of replacing tin-based catalyst with BiSS in the ROP of lactones. In this work, we reported the use of BiSS as a catalyst of the ROP of ε-LA in the presence of alkyl diols (HOROH) as initiators, aspects as synthesis, characterization, and mechanism of initiation are shown.

Experimental

Materials

All reagents, ε-lactide (ε-LA, purity 99%), bismuth subsalicylate (BiSS, purity 99.9%), ethylene glycol (purity 99.8%), 1,3-propanediol (purity 98%), 1,4-butanediol (purity 99%), 1,5-pentanediol (purity 96%), 1,6-hexanediol (purity 99%) and 1,8-octanediol (purity 98%) were purchased from Sigma-Aldrich and used as received.

Synthesis of α,ω-hydroxy telechelic poly(ε-lactide) (HO–PLLAₙ–OH)

The ring-opening polymerization (ROP) of ε-LA to synthesize poly(ε-lactide) macrodiols (HOPLLA(OH)) using linear aliphatic diols [HO–[CH₂]ₘ–OH, m = 2, 3, 4, 5, 6 and 8] as initiators and BiSS as catalyst, was carried out in a dried 20 mL vial. ε-Lactide (ε-LA, 20 mmol, 2.88 g), BiSS (0.03 mmol, 10.86 mg), and, 1,8-octanediol (2 mmol, 292 mg) were added to the flask and heated to reflux by stirring in an oil bath at 140 °C for 80 min (molar ratio ε-LA/BiSS = 667, ε-LA/1,8-octanediol = 10). The resulting PLLA was precipitated from chloroform/methanol, recovered by filtration, and dried under vacuum. The other PLLA oligo-esters were prepared and isolated using the same methodology as described for HOPLLA(OH). Number-average molecular weight (Mₙ) and conversion were monitored by ¹H NMR spectroscopy (Fig. 3): δ 5.16 (q, 1H, [–CH(CH₃)–O–], PLLA), 5.05 (q, 1H, [O–CH(CH₃)–O–], ε-LA), 4.35 (m, 1H, [–CH(CH₃)–OH], PLLA), 4.12 (m, 2H, [–CH₂–O–(C═O)–], Oct), 1.68 (d, 3H, [–CH(CH₃)–OCOCH₂–], PLLA), 1.58 (m, 3H, [–CH(CH₃)–O–], PLLA), 1.49 (d, 3H, [–CH(CH₃)–OH], PLLA), 1.31 (s, 2H, [–CH₂–],

Scheme 1 Structure of the bismuth subsalicylate (BiSS) in 2D (a) and 3D (b).


### Results and discussion

#### Synthesis and characterization

In the ring-opening polymerization (ROP) of lactones, such as $\alpha$-lactide ($\alpha$-LA), bulk polymerization is generally preferred as the solvent can be avoided, reducing solvent waste, complementary, in this work, only oligomers were synthesized. So, the viscosity attributed to the bulk polymerization during the polymerization reaction is not high enough due to the low $M_n$ (oligomers) and favoring the diffusion of the monomer. Additionally, alcohols (ROH) or diols (HOROH) have been used as initiators due to their ability to induce a transfer reaction in the presence of a catalyst, producing a new alkoxide in situ and controlling the degree of polymerization (DP). In our case, bismuth subsalicylate (BiSS) (Scheme 1) was tested as a catalyst for the ROP of $\alpha$-LA in bulk conditions and in the presence of 1,5-pentanediol [HO(CH$_2$)$_5$OH] as an initiator (Scheme 2). Previously, Kricheldorf et al. synthesized PLLA using BiSS as catalyst in the ROP of $\alpha$-LA in absent of alcohols or diols obtaining high $M_n$.  

![Scheme 2](image)

**Scheme 2** Synthesis of $\alpha$-ω-hydroxy telechelic poly($\alpha$-lactide) (HOPPLAOH) by ROP of $\alpha$-LA catalyzed by BiSS in the presence of an alkyl diol initiator.

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### Table 1  Comparison of the toxicity according to the globally harmonized system (GHS) for hazard communication$^{26}$

<table>
<thead>
<tr>
<th>Compound</th>
<th>CAS registry number</th>
<th>GHS</th>
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<tbody>
<tr>
<td>BiSS</td>
<td>14882-18-9</td>
<td>Non-dangerous substance</td>
</tr>
<tr>
<td>Sn(Oct)$_2$</td>
<td>301-10-0</td>
<td>Health hazard, corrosive, and exclamation mark (acute toxicity: oral, dermal, inhalation)</td>
</tr>
</tbody>
</table>
According to the previous descriptions, a different series of reaction parameters were tested, such as temperature, amount of catalyst, and reaction time. The factor used to quantify the optimal conditions of each parameter was the conversion, as detected by $^1$H NMR spectroscopy (Fig. 1).

The first parameter tested was the temperature, and variation of the temperature from 100 to 170 °C indicated an optimum value at 140 °C (Fig. 1a); testing of the second parameter, the amount of catalyst, is illustrated in the Fig. 1b, whereby the minimum amount of BiSS needed for full completion was 0.03 mmol. It is critical to minimize the concentration of the catalyst in the reaction medium for three reasons: (a) high catalyst concentration decreases the purity of the polyester, (b) high catalyst concentration can potentially induce side reactions, such as transesterification, and (c) low catalyst use leads to lower synthetic cost. The third parameter, reaction time, indicated that an excellent conversion was reached after 80 minutes (Fig. 1c). The optimal conditions of the ROP of L-LA in the presence of HO(CH$_2$)$_5$OH were ultimately found to be $T = 140$ °C, 0.03 mmol of BiSS, and 80 minutes.

To understand the kinetics of the ROP of L-LA catalyzed by BiSS and initiated by 1,5-pentanediol, three similar experiments were undertaken, varying the temperature from 100 to 140 °C. In Fig. 2a, the profile of the kinetics indicates an excellent agreement to a linear dependency, suggesting a first-order reaction with respect to monomer. Additionally, the temperature had a proportional relationship to the consumption of L-LA: the rate constant increased from 100 to 140 °C.

To calculate the constants, the activation energy ($E_a$) was also obtained (Fig. 2b). The $E_a$ of our reaction was found to be similar to previous reports of ROP of L-LA using stannous octoate [Sn(Oct)$_2$] as catalyst (Table 2), such as the work of Eenink, Witzke and Puaux. Therefore, the BiSS has similar suitability for use as a catalyst to the commonly-employed catalyst Sn(Oct)$_2$, but with the advantages of having low toxicity and environmental impact.

$a_{(t)}$-Hydroxy telechelic poly(L-lactide)s (HOPLLA-OH) (HOPLLA-(CH$_2$)$_m$-PLLA-OH) were prepared by ROP of L-LA catalyst by bismuth subsalicylate (BiSS) with a family of linear aliphatic diols as initiators. A gradual increase in the number of methylene groups in the diol (HO-CH$_2$)$_m$-OH, $m = 2, 3, 4, 5, 6$, and 8) was selected and after 80 min at 140 °C (Scheme 2) an excellent conversion was obtained for all samples (ca. 96%, Table 3, HOPLLA$_{2-8}$-OH), which indicates that the conversion is not
dependent on the number of methylene groups in the initiator. The conversion from l-LA to HOPLLAOH macrodiols in this work is comparable to the synthesis of \( \alpha,\omega \)-hydroxy telechelic PLLAs (HOPLLA\( _{\text{x}} \)-PLLA\( _{\text{OH}} \)) with \( x = \text{alkyl or ether groups} \) (yield: ca. 96%) previously reported using tin octoate (SnOct\(_2\)) as catalyst.

Fig. 3 shows the \(^1\)H NMR spectrum of HOPLLA\(_{\text{OH}}\). The signals at 4.25 and 4.12 ppm are attributed to a methine group (CHOH) attached to the terminal hydroxyl group and the methylene group adjacent to the ester group (CH\(_2\)OCO), evidence that the polymer is an \( \alpha,\omega \)-hydroxy telechelic polyester and that the aliphatic diol used as initiator had been inserted into the main chain. The rest of the signals are assigned to the repeat unit of the polyester and methylene groups of the initiator, the assignment of all peaks being consistent with those of reported \( \alpha,\omega \)-hydroxy telechelic PLLA samples.\(^{70-72}\) Additionally, the FT-IR spectrum (Fig. 4) evidenced a series of characteristic bands, such as the hydroxyl (O-H, 3510 cm\(^{-1}\)) and carbonyl groups (C=O, 1748 cm\(^{-1}\)), corroborating the chemical nature of the HOPLLAOH. However, the tacticity of HOPLLA\(_{\text{OH}}\) detected by \(^1\)C NMR (Fig. 5) showed a pattern of an atactic sample, this result is consistent with racemization of PLLA and PDLA previously reported by Asakura et al.\(^{73}\) So, during the polymerization to obtain PLLA oligomers the BiSS was not only a catalyst in the ROP of l-LA, but also induced the racemization of the polyester. The physical aspect of HOPLLA\(_{\text{OH}}\) is translucent; the tacticity of HOPLLA\(_{\text{OH}}\) was determined using \(^1\)H-NMR spectroscopy (Fig. 3) and analysis of the terminal groups, providing a range of \( D_{\text{PNMR}} \) values.

In the reactions summarized in Table 3, the feed l-LA/HOROH molar ratio applied was 10. However, as each lactone contains two ester groups, the theoretical ratio \((D_{\text{Ptheo}})\) is 20. The degree of polymerization \((D_{\text{PNMR}})\) was calculated experimentally using \(^1\)H-NMR spectroscopy (Fig. 3) and analysis of the terminal groups, providing a range of \( D_{\text{PNMR}} = 17.6-19.6 \) for our samples of HOPLLA\(_{\text{OH}}\). These values show excellent agreement with the theoretical ratio \((D_{\text{Ptheo}} = 20)\), an effect that can be attributed to the transfer reaction between the aliphatic diol (HOROH) as initiator and the BiSS as a catalyst, which ultimately generates a new alkoxide (Bi-O-R-OH) that is the active species in the initiation of the ROP of l-LA. Thus, the

![Fig. 3](image-url) **Fig. 3** \(^1\)H NMR spectrum at room temperature of HOPLLA\(_{\text{OH}}\) with \( D_{\text{PNMR}} = 18.8 \) (500 MHz, CDCl\(_3\)); asterisks indicate the residual monomer (l-LA).

![Fig. 4](image-url) **Fig. 4** FT-IR spectrum of HOPLLA\(_{\text{OH}}\).
content of HOROH (mmol) must be higher than BiSS in order to displace the equilibrium to favor a Bi–O–R–OH species, according to Le Chatelier’s principle. The insertion of the alkyl group and the formation of the α,ω hydroxyl telechelic terminal groups, previously evidenced by 1H NMR (Fig. 3) and 13C NMR (Fig. S22†) confirmed the operation of this transfer reaction.

The values of the number-average molecular weight (\(M_n\)) calculated by SEC are higher than the \(M_n\) values obtained by NMR analysis (Table 3). This effect is attributed to the differences in the hydrodynamic radius between the polystyrene standards and the HOPLLAOH samples. The dispersity (\(D_M\)) of HOPLLAOH samples was found to be narrow (1.06–1.12), with a unimodal distribution (Fig. S24†), suggesting that the initiation of the ROP is faster than the propagation. In line with this, experiments using a different monomer, such as D,L-lactide (racemate) (HOPDLLA\(_3\)/C\(_0\)8OH, Table 3), demonstrated similar behavior to the ROP of L-LA by BiSS. The synthesis of the HOPLLAOH with high \(M_n\) catalysed by BiSS will be explored in a future contribution.

Mechanism of initiation

The results presented herein have demonstrated the abilities of BiSS as a catalyst in the ROP of L-LA, and the insertion of an alkyl diol \([\text{HO(CH}_2\text{)}_n\text{OH}]\) into the main chain of the polyester (producing an ester group) demonstrated the role of these diols as initiators. The experimental evidence suggests that a bismuth alkoxide (Bi–OR) is formed in situ by a transfer reaction, and eventually, Bi–OR can act as an active species during the initiation step. In a previous report, Lahcini et al.29
used a series of bismuth(III) alkoxide catalysts for the ROP of lactones, and found that bulkier bismuth alkoxides showed high activity. In our case, the BiSS has three possibilities to produce the Bi–OR species by a transfer reaction (Scheme 3): (1) generally, a metallic hydroxy species (Scheme 3c) such as Bi–OH is insufficiently basic in an organic medium to deprotonate an alcohol (HOR) (or a diol HOROH) and generate Bi–OR (or Bi–OROH) and water, and (2) the bidentate ligand derived from 2-hydroxy-benzoic acid (salicylic acid) bound to the Bi center has two different types of Bi–O bonds, i.e. to phenoxy and benzoate groups.

The difference in pKₐ values between the phenoxy ion (0.4) and benzoate ion (11.03) is significant, thus it can be expected that the bond between the phenoxy group and the Bi center (PhO–Bi) can act as a Lewis base to deprotonate the alkyl diol and produce the Bi–OROH species plus a phenol group (Scheme 3a). To corroborate this idea, a series of computational calculations were conducted by DFT-based calculations at the PBE0/[LANL2DZ-6-31G(d)] level of theory (see Computational details). Table 4 lists the energy barriers to produce a transfer reaction, whereby the formation of a bismuth alkoxide and a phenol group is favored. Additionally, the effect of the numbers of methylenes (CH₂)n from

<table>
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<th>Alkoxides</th>
<th>Total energy barrier (kcal mol⁻¹)</th>
<th>Activation energy (Eₐ, kcal mol⁻¹)</th>
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<tr>
<td></td>
<td>13.57</td>
<td>6.85</td>
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<td>12.78</td>
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<tr>
<td></td>
<td>41.56</td>
<td>35.16</td>
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Fig. 7 Energy profile (gas phase, 140 °C) of the mechanism of initiation of l-lactide (l-LA) initiated with ethylene glycol \([\text{HO(CH₂)₂OH}]\) using bismuth subsalicylate (BiSS) as a catalyst.
ethylene glycol [HO(CH₂)₉OH] to 1,5-pentanediol [HO(CH₂)₉OH] on the transfer reaction [Scheme 3, Table S1] exhibited a gradual increase in the total barrier of the alkoxide, and also the product (a) (Scheme 3a) is mainly favored concerning (c) (Scheme 3c).

As can be seen in Fig. 7, the polymerization occurs through a ring-opening mechanism. Initially, the reaction is promoted by the formation of a metal alkoxide (Bi-OROH) product of the reaction between the BiSS catalyst and the ethylene glycol initiator. This induction step is the rate-determining step of the polymerization of α-LA, with an energy barrier of 13.57 kcal mol⁻¹. The reaction continues by coordination of the carbonyl group of α-LA with the Bi-O bond of the bismuth alkoxide, with an energy barrier of 9.38 kcal mol⁻¹. This followed by the insertion of the alkoxide group INT3, and then a rearrangement of the intermediate INT3, favoring the opening of the ring, which consists of a rotation of the substituents (alkoxy and ethoxy) of almost 90°.

The energy barrier of this rearrangement, which leads to the formation of the intermediate INT4, is 3.19 kcal mol⁻¹, and this shallow barrier suggests that both intermediates are likely in equilibrium. The next reaction step is the opening of the ring and occurs with a very small energy barrier of 1.43 kcal mol⁻¹. The last step proposed in this mechanism is a rearrangement toward zigzag conformation of INT5 to obtain P due to steric issues; these occur through a transition state similar to ET3.²⁵ The formation energy of P is −15.84 kcal mol⁻¹ making it an exergonic (spontaneous) reaction.

Conclusions

Bismuth subsalicylate (BiSS) acts as a catalyst in the ring-opening polymerization (ROP) of ω-lactide (ω-LA) in the presence of linear aliphatic diols [HO(CH₂)ₙOH, where n = 2, 3, 4, 5, 6, and 8] as initiators, obtaining α,ω-hydroxy telechelic polyω-lactide) (HOPPLAOH) in excellent conversion. A good agreement of the measured and theoretical degrees of polymerization (DP) in all HOPPLAOH samples was evidenced. This effect is attributed to the interaction of BiSS with HO(CH₂)₂OH, which induces a transfer reaction and, ultimately, generates an active bismuth alkoxide (Bi-OROH) species. The rate constant for the ROP of ω-LA catalyzed by BiSS was found to be proportional to the temperature, and the activation energies are comparable to those of the conventionally-used catalyst tin octoate [Sn(Oct)₂].

A computational study elucidated the behavior of the BiSS in the presence of an alkyl diol (HOROH), producing a Bi-OROH that acts as an active species and nucleophile in the ring-opening of ω-LA. These results indicate that BiSS is a very promising catalyst candidate for the ROP of ω-LA due to its low cost, low toxicity, and efficacy in the synthesis of macrodiols such as HOPPLAOH, which in turn are key precursors to triblock copolymers and poly(ester-urethanes).

Conflicts of interest

There are no conflicts to declare.

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Notes and references


