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The structure and vibrational spectroscopy of cryolite, Na_3AlF_6

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Cryolite, $\text{Na}_3[\text{AlF}_6]$, is essential to commercial aluminium production because alumina is readily soluble in molten cryolite. While the liquid state has been extensively investigated, the spectroscopy of the solid state has been largely ignored. In this paper, we show that the structure at 5 K is the same as that at room temperature. We use a combination of infrared and Raman spectroscopies together with inelastic neutron scattering (INS) spectroscopy. The use of INS enables access to all of the modes of $\text{Na}_3[\text{AlF}_6]$, including those that are forbidden to the optical spectroscopies. Our spectral assignments are supported by density functional theory calculations of the complete unit cell.

Introduction

Cryolite, $\text{Na}_3[\text{AlF}_6]$, occurs naturally as a rare mineral.¹ Historically, it was used as a source of aluminium but this has been superseded by bauxite (a mixture of the Al_2O_3 containing minerals boehmite, diasporite and gibbsite), largely because of the higher Al content of bauxite (~50%) vs. cryolite (13%) and the scarcity of the latter. However, cryolite remains essential to aluminium production because alumina is readily soluble in molten cryolite. This is crucial to the economics of aluminium production because cryolite melts at 1012 °C whereas alumina melts at 2072 °C. As the melt is ionic, it also conducts electricity efficiently making the electrolytic reduction of alumina feasible. This is the basis of the Hall–Héroult process, which was invented independently by Hall and Héroult in 1886 and it is still the method of production today.²

The liquid phase of cryolite has been extensively investigated by a variety of techniques including multinuclear (^{19}F , ^{23}Na , ^{27}Al) NMR,^{3–5} Raman spectroscopy^{6–8} and quasielastic neutron scattering.^{9,10} There are also a large number of molecular dynamics studies *e.g.*^{11–15}, some of which calculate the Raman spectra^{13,14} in the melt. Surprisingly, the solid state has been much less investigated, with only one paper on the infrared spectroscopy of $\text{Na}_3[\text{AlF}_6]$ ¹⁶ and one on that of the isostructural $\text{K}_3[\text{AlF}_6]$.¹⁷ Cryolite is the end member of the elpasolite family,¹⁸ the archetype is $\text{K}_2\text{Na}[\text{AlF}_6]$, and this is the most abundant prototype in the Inorganic Crystal Structure Database.¹⁹ The spectroscopy of elpasolite itself has been studied,²⁰ as has $\text{Cs}_2\text{Na}[\text{AlF}_6]$.²¹ Materials of the type $\text{Li}_3[\text{InX}_6]$ ($\text{X} = \text{Cl},^{22} \text{Br}^{23}$) are of current interest as lithium ion conductors.²⁴

In view of the technological importance of cryolite, we have carried out a comprehensive spectroscopic investigation and report new infrared and Raman spectra over extended temperature and spectral ranges and the inelastic neutron scattering (INS) spectrum. The last of these is observed for the first time and enables access to all of the modes of $\text{Na}_3[\text{AlF}_6]$. Our spectral assignments are supported by density functional theory calculations of the complete unit cell.

Results

Structure

At room temperature cryolite crystallizes in the monoclinic α -phase, space group $P2_1/n$ (no. 14) with two formula units in the primitive cell,^{25–27} Fig. 1. The non-standard setting is used because it highlights the relationship to the high temperature (above 823 K) face centered cubic β -phase, $Fm\bar{3}m$ (no. 225).^{27,28}

The structure in the α -phase is shown in Fig. 1 and it can be seen that there are two types of sodium ion: one (Na1 , orange) on the Wyckoff site 2c and two (Na2 , purple) on the Wyckoff site 4e. These are six- and eightfold coordinated by fluorine atoms, respectively. The $[\text{AlF}_6]^{3-}$ ion is on the Wyckoff site 2d and has C_i symmetry. Thus the compound is better formulated as: $(\text{Na}_2)(\text{Na})[\text{AlF}_6]$ and is an example of a double perovskite.²⁷

We are unaware of any structural studies below room temperature. Heat capacity measurements from 7–350 K,²⁹ do not show any evidence of a phase transition in that range, apart from the melting of a liquid inclusion at 268 K in the natural sample of cryolite that was used. However, the INS spectrometer used in this work, VISION,³⁰ also has a neutron diffraction capability. Fig. 2 shows a two-phase (cryolite plus the aluminium can) Rietveld fit of the neutron diffractogram measured at 5 K. Scale factors were refined for both phases in obtaining the fit to the data. Lattice parameters have been allowed to refine, to allow for cell contraction, but atomic

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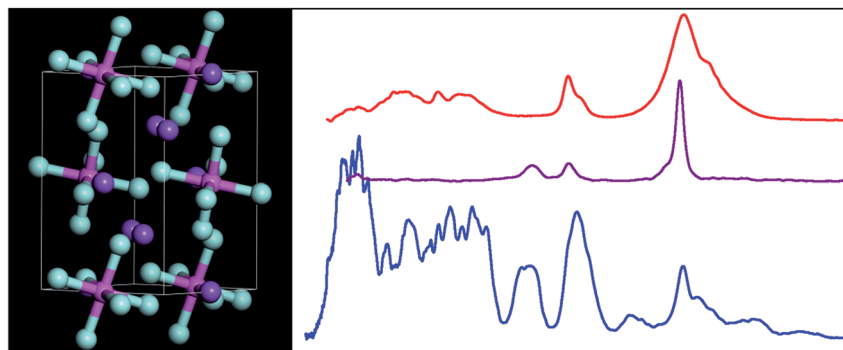


Fig. 1 The room temperature structure of cryolite in the monoclinic space group $P2_1/n$ (no. 14).²⁶ Key: Na1 = orange, Na2 = purple, Al = magenta, F = turquoise.

positions have been held at the room temperature values.²⁵ An excellent fit to the data is obtained, even though the atomic positions and temperatures factors of the cryolite have not been refined. Table 1 lists the lattice parameters determined here together with room temperature and estimated values. It is apparent that, apart from the expected lattice contraction on cooling, that the $P2_1/n$ structure is retained to at least 5 K.

Table 2 compares selected observed and calculated bond distances (all of the *cis* F–Al–F bond angles are $90 \pm 1^\circ$, all the *trans* angles are 180° by symmetry). As might be expected from the very small difference between the room temperature and 5 K lattice parameters there is little change in the interatomic distances. The calculation does slightly overestimate the Al–F distances. The Na–F distances are slightly shorter than found in NaF (2.318 Å (ref. 31)).

Vibrational spectroscopy

Fig. 3 shows the infrared, Raman and INS spectra of cryolite. The Raman spectrum at 13 K is seen in Fig. 3c, unfortunately, because of sample fluorescence, only the Al–F symmetric stretch mode at 554 cm^{-1} was observable. However, apart from a marked narrowing, there is no shift in transition energy or additional peaks apparent. The lattice mode region, shown in the lower part of Fig. 3, shows coincidences between the INS and the infrared and Raman data. Thus the vibrational spectroscopy suggests (but does not prove) that there is no phase change between room temperature and 5 K, consistent with the diffraction results.

An isolated octahedral, O_h , $[\text{AlF}_6]^{3-}$ ion has six Al–F stretch modes: ν_1 (A_{1g}), ν_2 (E_g), ν_3 (T_{1u}) and nine F–Al–F bend modes: ν_4 (T_{1u}), ν_5 (T_{2g}), ν_6 (T_{2u}). ν_1 , ν_2 and ν_5 are Raman active, ν_3 and ν_4 are infrared active and ν_6 is forbidden in both forms of spectroscopy.³² However, all of the modes are allowed in the INS spectrum. To go beyond this requires more detailed analysis and to this end we use the correlation method.³³ The results are shown in Table 3.

With two formula units in the primitive cell, there are 20 atoms present hence there are 60 modes, which are given by the sum of the last column in Table 3: $12 A_g + 12 B_g + 18 A_u + 18 B_u$. This includes the three acoustic translational modes, which have $A_u + 2 B_u$ representations and have zero energy at the

Brillouin zone Γ -point, where the infrared and Raman modes are observed. Modes that have A_u or B_u symmetry are infrared active, those with A_g or B_g are Raman active. Two deductions are immediately obvious: all of the degeneracies are formally lifted

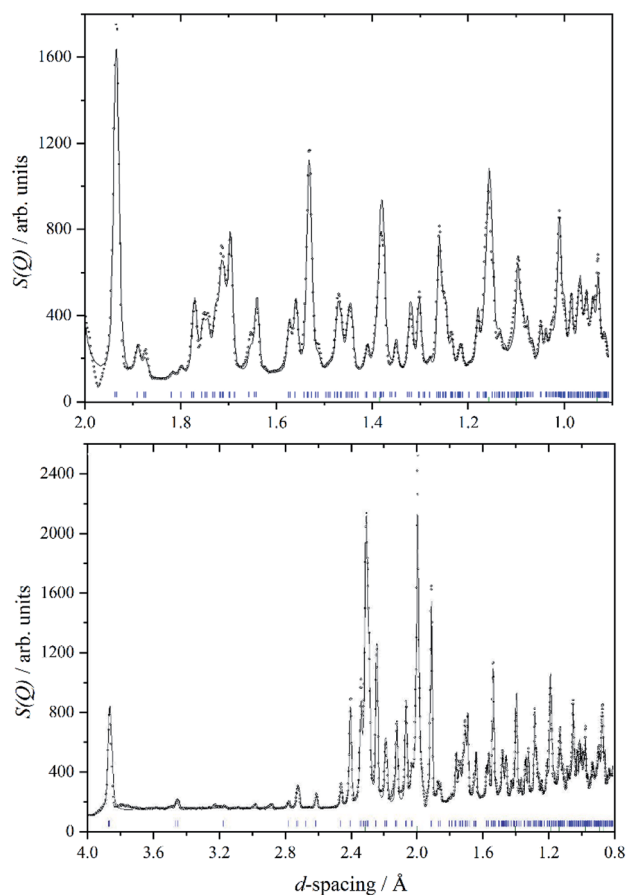


Fig. 2 A two-phase Rietveld fit (solid line) to the VISION neutron data (open circles) in the d -spacing range 2.0 to 0.8 Å (upper panel) and 4.0 to 0.8 Å (lower panel). Blue tick marks indicate the reflection positions for cryolite, whilst green tick marks indicate the reflections associated with the aluminium sample can. An excellent fit to data is obtained, even though the atomic positions and temperatures factors of the cryolite have not been refined.



Table 1 Lattice parameters of cryolite

	5 ^a K	0 ^b K	0 ^c K	295 ^d K	295 K ^e
<i>a</i> /Å	5.3917(5)	5.381	5.42	5.4139(7)	5.4054(1)
<i>b</i> /Å	5.6010(5)	5.581	5.63	5.6012(5)	5.5934(1)
<i>c</i> /Å	7.7556(8)	7.693	7.83	7.7769(8)	7.7672(1)
α /°	90.000	90.000	90.0	90.000	90.000
β /°	90.253(8)	90.285	90.2	90.183(3)	89.81(1)
γ /°	90.000	90.000	90.0	90.000	90.000
<i>V</i> /Å ³	234.21(4)	232.6	238.9	235.8	234.84

^a This work. ^b Extrapolated from ref. 25 by ref. 14. ^c Calculated by molecular dynamics.¹⁴ ^d From ref. 25. ^e From ref. 26.

and because the centre of symmetry is preserved, the free ion selection rules will still apply, except that ν_6 is now allowed in the infrared spectrum. As stated earlier, all modes are allowed in the INS spectrum.

The analysis in Table 3 enables some of the modes to be assigned. The intense, broad mode at 559 cm⁻¹ with shoulders at 596 and 608 cm⁻¹ in the infrared spectrum must be ν_3 . Previous work¹⁶ on the infrared spectrum of cryolite found ν_3 at 599 cm⁻¹ with shoulders at 580 and 630 cm⁻¹, the lower energy modes were not reported. We can only ascribe the difference in the transition energy of ν_3 to either a calibration error in the older (pre-FTIR) work or that the natural sample of cryolite used there was impure.

The strong mode at 554 cm⁻¹ in the Raman spectrum must be ν_1 and the two weaker modes at 396 and 344 cm⁻¹ in the Raman spectrum are ν_2 and ν_5 respectively. This is in excellent agreement with the previously reported Raman spectrum of cryolite.⁸ Cryolite melts^{6–8} show a strong band at ~550 cm⁻¹ assigned to ν_1 . In the infrared spectrum the mode at 396 cm⁻¹ is assigned as ν_4 . The coincidence with ν_2 is surprising because one is an Al–F stretch mode and the other an F–Al–F bending mode, but the selection rules are unambiguous. The assignment is supported by the INS spectrum, which shows a mode at 407 cm⁻¹, that is much stronger than ν_5 , consistent with it being the unresolved sum of the two modes. The optically silent mode ν_6 is not apparent, so it must occur below 300 cm⁻¹.

Table 2 Comparison of observed and calculated structure of cryolite

Distance/Å	295 ^a K	5 K initial ^b	5 K opt ^c
Al–F	2 × 1.799	2 × 1.812	2 × 1.825
	2 × 1.820	2 × 1.825	2 × 1.834
	2 × 1.830	2 × 1.836	2 × 1.836
Na1–F	2 × 2.211	2 × 2.205	2 × 2.219
	2 × 2.271	2 × 2.256	2 × 2.257
	2 × 2.272	2 × 2.264	2 × 2.274
Na2–F (min)	2.292	2.287	2.276
(max)	2.816	2.806	2.807
(ave)	2.498	2.494	2.564

^a From ref. 26. ^b Structure used for the fits in Fig. 2. ^c 5 K structure after geometry optimization.

It is only in the region <300 cm⁻¹ in the INS spectrum that the low symmetry of the system is readily apparent. In the infrared spectrum, there are three weak features, which Table 3 shows must be ν_6 and the translational modes of the ions, although there is no way to assign which is which. In the Raman spectrum there is a weak mode at 94 cm⁻¹, which is presumably the [AlF₆]³⁻ ion librational mode.

Computational studies

In order to assign the low energy region and to confirm the assignments for ν_1 to ν_5 we use periodic density functional theory (DFT) of the primitive cell and calculate the vibrational transition energies across the entire Brillouin zone (see: Materials and methods for details). The resulting dispersion curves are shown in Fig. 4 and the INS spectrum generated from the calculation is shown in Fig. 5.

It can be seen that the calculated INS spectrum is in almost quantitative agreement with the experimental data. The Al–F stretch modes are calculated slightly softer than is observed, this is probably because the bond lengths are calculated slightly too long: observed:^{25–27} 1.799, 1.820, 1.830 Å; calculated: 1.825, 1.834, 1.836 Å. However, the overall pattern of the experimental data is very well reproduced. In

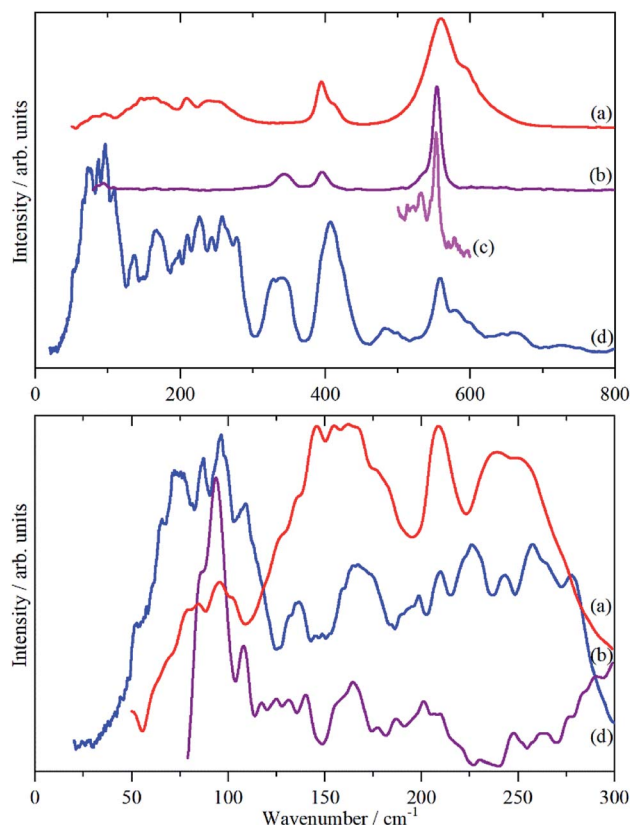


Fig. 3 Vibrational spectra of cryolite: (a) infrared at room temperature, (b) Raman at room temperature (1064 nm excitation), (c) Raman at 13 K (785 nm excitation) and (d) INS at 5 K recorded on VISION. The lower panel shows the lattice mode region on expanded scales. Relative to the top panel the spectra are ordinate expanded: (a) ×10, (b) ×40 and (d) ×1.5.



Table 3 Correlation table for cryolite

Ion	<i>n</i>	Crystal									
		Free ion		Translations		Librations		Intramolecular		Factor group	
		Sym. ^b	Rep.	Site ^c	Rep.	No.	Rep.	No.	Rep.	No.	Total ^a
Na1	2			C _i	A _u	3				(A _u + B _u)	3(A _u + B _u)
Na2	4			C ₁	A	3				(A _g + B _g + A _u + B _u)	3(A _g + B _g + A _u + B _u)
AlF ₆	2	O _h	T _{1u}	C _i	A _u	3	A _g	3		(A _u + B _u)	3(A _u + B _u)
	2	O _h	T _{1g}	C _i						(A _g + B _g)	3(A _g + B _g)
	2	O _h	A _{1g} (ν ₁)	C _i				1	A _g	(A _g + B _g)	(A _g + B _g)
	2	O _h	E _g (ν ₂)	C _i				2	A _g	(A _g + B _g)	2(A _g + B _g)
	2	O _h	T _{1u} (ν ₃)	C _i				3	A _u	(A _u + B _u)	3(A _u + B _u)
	2	O _h	T _{1u} (ν ₄)	C _i				3	A _u	(A _u + B _u)	3(A _u + B _u)
	2	O _h	T _{2g} (ν ₅)	C _i				3	A _g	(A _g + B _g)	3(A _g + B _g)
	2	O _h	T _{2u} (ν ₆)	C _i				3	A _u	(A _u + B _u)	3(A _u + B _u)

^a Total is the product of the column "No." and the factor group. ^b Sym. = symmetry, Rep. = irreducible representation of the point group, No. = number. ^c Symmetry of the site occupied by the ion in the crystal.

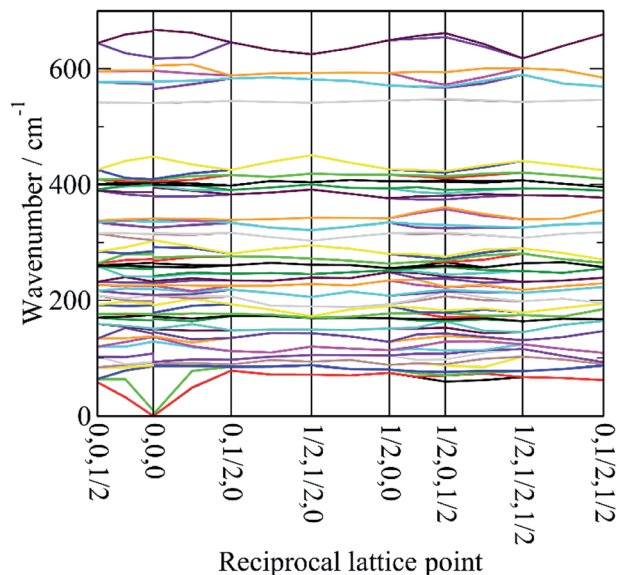


Fig. 4 Dispersion curves of cryolite in the monoclinic space group $P2_1/n$ (no. 14).

particular, the splitting of ν_3 is clearly seen and Fig. 4 shows that this is the result of the combination of the site group and factor group splitting combined with significant vibrational dispersion (variation with wavevector). The dense manifold of modes below 300 cm^{-1} occurs because the low symmetry removes all the degeneracies and results in the complex structure seen experimentally.

The transition energies at the Brillouin zone Γ -point, (0,0,0), are given in Table 4 with the assignments based on visualization of the modes. This confirms the assignments for ν_1 to ν_5 and in particular that ν_2 and ν_4 are coincident. The "missing" mode ν_6 is calculated at $254\text{--}288\text{ cm}^{-1}$ and is seen to occur weakly in the infrared spectrum at $239/253\text{ cm}^{-1}$. This is the first time that ν_6 has been observed experimentally.

Fig. 5 also includes the individual contributions to the INS spectrum from each element. As expected, the fluorine contribution accounts for most of the intensity and it confirms that the librational modes account for the peaks at $\sim 85\text{--}150\text{ cm}^{-1}$. However, the librations have the same symmetry, A_g and B_g , as some of the translational modes of Na2 which results in extensive mixing of the two vibrations. Thus the lower energy modes around 100 cm^{-1} are more librational in form while the higher energy ones around 210 cm^{-1} are more translational. Na2 has modes of both gerade and ungerade character, Table 3, and this results in the modes occurring in a broad band from $50\text{--}300\text{ cm}^{-1}$. In contrast, the Na1 modes are much more localized and largely occur in the narrower range of $200\text{--}300\text{ cm}^{-1}$. This is a consequence of the more regular coordination polyhedron of Na1: the Na–F distances vary by less than 0.06 \AA , by contrast those around Na2 vary by nearly ten times as much, 0.5 \AA (Table 2).

Discussion

This work provides the first complete assignment of the vibrational spectra of cryolite. In particular, the forbidden (in

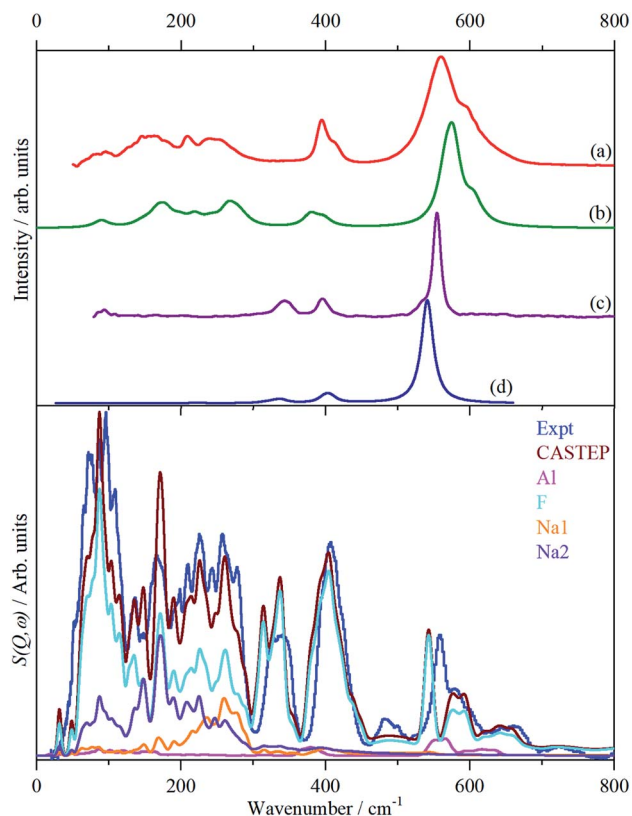


Fig. 5 Observed and calculated (CASTEP) spectra of cryolite. Top panel: infrared spectra (a) observed, (b) calculated. Raman spectra: (c) observed, (d) calculated. Lower panel: INS spectra. The individual element contributions to the calculated spectrum are also shown.

O_h symmetry) mode ν_6 has been observed. This is very rare:³² (pp. 216–218) lists the spectra of over 30 $[MF_6]^{x-}$ ions; for none of them is ν_6 given, although it is known for a few neutral MF_6 systems. Assignment of librational modes is equally rare. To our knowledge, the only examples for which this is known are for $K_2[MCl_6]$ ($M = Pt, Ir,$ ³⁴ Re ³⁵) where the librational transition energies are 55 cm^{-1} (Pt), 48 cm^{-1} (Ir) and 28 and 68 cm^{-1} (Re). Making the naive assumption that it is only the difference in the moment of inertia between the $[AlF_6]^{3-}$ and $[PtCl_6]^{2-}$ ions that accounts for the difference in transition energy would predict that $[AlF_6]^{3-}$ occurs at 87 cm^{-1} . This is on the lowest edge of the band of the librational modes (Table 4) and suggests that other factors are also relevant, the most likely being the difference in charge of the ions.

The only unassigned band in the spectra shown in Fig. 3 is the shoulder at 533 cm^{-1} on the low energy side of ν_1 that is clearly resolved at 13 K. We considered the possibility that it may be the B_g symmetric Al–F stretch mode that was miscalculated, however, there is no corresponding mode in the INS spectrum, which also argues against it being an overtone or combination. The calculated Raman intensity of this mode is almost zero which also militates against this assignment. Inspection of the Raman spectra of cryolite in the literature^{4,6,8} does not show the band in the solid or liquid phase. This suggests that it is an impurity, despite the stated purity being >99%, and the most likely candidate is chiolite, $Na_5Al_3F_{14}$. This mineral occurs naturally with cryolite³⁶ and consists of sheets of corner-sharing AlF_6 octahedra,³⁷ it has a very strong totally symmetric Al–F stretch mode at 530 cm^{-1} .³⁸

Table 4 Observed and calculated (at the Brillouin zone Γ -point) transition energies with assignments for cryolite

CASTEP/ cm^{-1}	Sym ^b	IR int/ $km\ mol^{-1}$	Raman int/ $\text{\AA}^4\ amu^{-1}$	Observed ^a			Description ^b
				INS/ cm^{-1}	Raman/ cm^{-1}	Infrared/ cm^{-1}	
0	B_u	0	0				Acoustic
0	A_u	0	0				Acoustic
0	B_u	0	0				Acoustic
86	A_g	0	0.02	75s			Lib + Na2 trans
87	A_u	13.62	0				AlF6 trans
90	B_u	103.00	0				AlF6 trans
92	A_g	0	0.02	87s	86sh		Lib + Na2 trans
93	B_g	0	0	96s	94w		Lib + Na2 trans
128	B_g	0	0	109s	109w		Lib + Na2 trans
137	A_g	0	0.02	136m			Lib + Na2 trans
138	B_g	0	0				Lib + Na2 trans
142	A_u	32.79	0				Na2 trans
149	A_u	9.73	0				AlF6 trans
150	B_u	36.73	0			146w	Na2 trans
165	A_u	55.50	0			154w	Na2 trans
167	B_u	163.52	0	164s		163w	Na2 trans
175	A_g	0	0.02				Na2 trans + Lib
175	B_g	0	0.01				Na2 trans + Lib
178	B_u	226.57	0			178w	Na2 trans
191	A_u	5.47	0			183w	Na1 trans
198	A_u	100.07	0				Na2 trans
209	B_g	0	0	198w			Na2 trans + Lib
209	A_g	0	0.02	210m			Na2 trans + Lib



Table 4 (Contd.)

CASTEP/cm ⁻¹	Sym ^b	IR int/km mol ⁻¹	Raman int/Å ⁴ amu ⁻¹	Observed ^a			Description ^b
				INS/cm ⁻¹	Raman/cm ⁻¹	Infrared/cm ⁻¹	
219	A _u	59.53	0	209m	209w		Na1 trans
219	B _u	96.45	0				Na1 trans
225	B _g	0	0.02	226m			Na2 trans + Lib
226	A _g	0	0.02				Na2 trans + Lib
232	A _u	1.86	0	243m			Na1 trans
240	B _u	37.39	0				Na1 trans
242	B _u	56.98	0			243w	Na1 trans
258	A _u	1.46	0	257m		252w	ν_6
264	B _u	199.11	0				ν_6
268	B _u	73.93	0	265sh			ν_6
271	A _u	71.91	0				ν_6
280	A _u	161.49	0	278sh			ν_6
292	B _u	38.42	0				ν_6
304	A _g	0	0.01	325s			ν_5
314	B _g	0	0.07				ν_5
326	A _g	0	0.18				ν_5
335	A _g	0	0.24				ν_5
341	B _g	0	0.16	336s,br	343m		ν_5
341	B _g	0	0.08				ν_5
379	B _u	108.53	0				ν_4
380	A _u	95.40	0				ν_4
397	B _u	129.31	0	396sh		395m	ν_4
398	A _g	0	0.62		395m		ν_2
400	B _u	0.62	0				ν_4
404	A _g	0	0.36				ν_2
405	A _u	0.24	0				ν_4
408	B _g	0	0.50	407s			ν_2
409	A _u	2.09	0			413sh	ν_4
448	B _g	0	0.05	425sh			ν_2
541	A _g	0	13.80				ν_1
541	B _g	0	0		554s		ν_1
565	B _u	562.08	0	559s		559s	ν_3
574	A _u	762.85	0				ν_3
578	B _u	657.32	0	580m			ν_3
597	A _u	21.77	0	601m			ν_3
605	B _u	336.80	0			596sh	ν_3
619	A _u	21.74	0			608sh	ν_3

^a s = strong, m = medium, w = weak, br = broad, sh = shoulder. ^b Lib = libration of [AlF₆]³⁻ ion, AlF₆ = translation of [AlF₆]³⁻ ion, Na1 trans = translational mode of Na1, Na2 trans = translational mode of Na2.

Materials and methods

Cryolite, Na₃[AlF₆] (>99%) was purchased from Sigma-Aldrich (Gillingham, Dorset, UK) and used as received.

INS spectra were recorded at 5 K using the VISION³⁰ spectrometer at the Spallation Neutron Source (SNS) (Oak Ridge, Tennessee, USA). An empty aluminium sample can has been subtracted from the measured INS data. Infrared spectra (50–4000 cm⁻¹, 4 cm⁻¹ resolution, 64 scans) were recorded at room temperature with a Bruker Vertex 70 Fourier transform infrared spectrometer using a Bruker Platinum single reflection attenuated total internal reflection accessory. The FT-Raman spectrum was recorded at room temperature a from the sample inside a quartz cuvette with a Bruker MultiRam spectrometer using 1064 nm excitation (500 mW laser power and 1024 scans at

4 cm⁻¹ resolution). Variable temperature (13–300 K) Raman spectra were recorded with a modified Renishaw InVia spectrometer using 785 nm excitation.³⁹

Dispersion corrected periodic density functional theory (DFT-D) calculations were carried out with CASTEP (version 17.21).⁴⁰ On-the-fly generated norm conserving pseudopotentials with a plane-wave cut-off of 870 eV were used with the PBE⁴¹ functional with the Tkatchenko–Scheffler (TS) dispersion correction scheme⁴² within the generalized gradient approximation (GGA). Brillouin zone sampling of electronic states was performed on a 10 × 8 × 9 Monkhorst–Pack grid (180 *k*-points). The starting structure was that determined here at 5 K. The equilibrium structure, an essential prerequisite for lattice dynamics calculations, was obtained by BFGS geometry optimization after which the residual forces were converged to



$|0.00097| \text{ eV } \text{\AA}^{-1}$. A second calculation that optimised both the lattice parameters and the geometry resulted in a 5.9% increase in the volume of the unit cell. Phonon frequencies were obtained by diagonalization of the dynamical matrix, computed using density-functional perturbation theory,⁴³ to compute the dielectric response and the Born effective charges, and, from these, the mode oscillator strength tensor and infrared absorptivity were calculated. Raman intensities were calculated by a finite displacement method.⁴⁴ In addition to the calculation of transition energies at zero wavevector, phonon dispersion was also calculated along high symmetry directions throughout the Brillouin zone. For this purpose, dynamical matrices were computed on a regular grid of wavevectors throughout the Brillouin zone, and Fourier interpolation was used to extend the computed grid to the desired fine set of points along the high-symmetry paths.⁴⁵ The atomic displacements in each mode, that are part of the CASTEP output, enable visualization of the modes in Materials Studio⁴⁶ to aid assignments and are also all that is required to generate the INS spectrum using the program ACLIMAX (version 6.0.0 LE).⁴⁷ It is emphasised that, for the calculated spectra and dispersion curves shown, the transition energies have not been scaled.

Conclusions

In this work we have shown that the structure of cryolite is the same at 5 K as previously determined at room temperature.^{25–27} We have used a combination of vibrational spectroscopies to observe all of the modes for the first time, including those that are infrared and Raman forbidden under octahedral symmetry.

This work also allows some assignments to be made for elpasolite²⁰ and $\text{Cs}_2\text{Na}[\text{AlF}_6]$.²¹ For the former, the Raman bands at 561, 330 and 138 cm^{-1} are ν_1 , ν_5 and the librational mode, the infrared bands at 590, 401 and 238 cm^{-1} are ν_3 , ν_4 and a Na^+ translation. For $\text{Cs}_2\text{Na}[\text{AlF}_6]$ the Raman bands at 520 and 364 cm^{-1} are ν_1 and ν_2 , those at 316, 310 and 307 cm^{-1} are from ν_5 .

Conflicts of interest

The authors declare no conflict of interest.

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