Cite this: *RSC Adv.*, 2020, 10, 22352

Transparent glass-ceramics for thermal management application: achievement of optical transparency and high thermal conductivity

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Oxide glass is an industrial material with advantages such as optical transparency and shaping ability of the melt, but at the same time, it is a bad conductor of heat due to its disordered structures. Therefore, heat dissipation in glass components often becomes a problem and its applications to the thermal management has been limited to use as a heat insulator. To break this mold and to apply it to fields, e.g., transparent sealing materials, for which low thermal conductive glasses and organic polymers have been conventionally used, we fabricated an MgO-dispersed glass-ceramics in our previous work. It comprises MgO crystal and glass matrix and their reflective indices are matched, leading to optical transparency and improvement in thermal conductivity. Here we investigate the atomic-scale structures in the MgO-dispersed glass-ceramics by nuclear magnetic resonance, etc. and attempt to further improve the thermal conductivity and the transparency. As a result, we show an MgO-dispersed glass-ceramic with a thermal conductivity of 3.3 W (m⁻¹ K⁻¹), corresponding to 300% of that of the glass matrix, high optical transparency, and glass transition. This report highlights that our strategies pave the way for development of novel transparent, functional glass-ceramics.

Received 3rd April 2020

Accepted 5th June 2020

DOI: 10.1039/d0ra03026k

rsc.li/rsc-advances

1. Introduction

Owing to its unique advantages, *i.e.*, high optical transparency and shaping ability of the melt, oxide glass has been used in vessels, windows, and ornaments since ancient times,¹ and moreover, in recent years, functional glasses such as optical fibers in telecommunication and the screen protector glass in mobile devices have been widespread.^{1,2} Here, its optical transparency and shaping ability of the melt originate from the intrinsic glass structure which are isotropic, boundaryless, and disordered.¹ Among them, the structural disorder inevitably disturbs propagation of atomic vibrations in the glass.³ Thus, in principle, the glass is a bad conductor of heat, and accordingly, heat dissipation in glass components often become a problem⁴ and it is not very useful for heat removal. In other words, glass application to the thermal management has been limited to use as a heat insulator.

However, if the glass attains high thermal conductivity, we can not only solve the problems on heat dissipation in the glass components but also pave the way for thermal management applications of the glass, *e.g.*, prevention of heat crack and malfunction in the glass components and application to sealing materials for high-power light-emitting devices requiring high thermal conductivity together with transparency and shaping

ability. Here, we emphasize that the glass has advantages of high chemical, light, and heat resistances,¹ compared to the conventional sealing materials such as organic polymers. In addition, from the viewpoint of affective engineering, we may be able to provide the glass with a high-class feeling, which can be improved with an increase in thermal conductivity (accurately, thermal effusivity) of materials.

To achieve that, we must leave the conventional, homogeneous glass, because it is impossible that the glass itself possesses high thermal conductivity, transparency, and shaping ability of the melt, at the same time. Instead, we have proposed a fabrication method of a transparent glass-ceramic comprising glass matrix and large amount of high thermal conductive crystal with a large size, where we take two strategies as follows:⁵

One is oversupply of a reagent which is expected to precipitate as the high thermal conductive crystal; generally, composition of glass batches is designed so that no crystal is precipitated during quenching. Conversely, we dare to oversupply the reagent so that its amount is out of a glass-forming range and the required crystal is precipitated. This concept corresponds to the Frozen sorbet method proposed by Nakanishi *et al.*⁶ in terms of the oversupply of reagents. The incorporation method⁷ and the crystallization method⁸⁻¹⁰ are well known as ones to provide functionality for glass by dispersing crystal; compared to the two conventional methods, the advantages of the oversupply method are as follows: one is that the process is as simple as the conventional melt-quenching

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method, meaning that the extra processes, *i.e.*, crystal-glass mixing process or heat treatment are not needed. The other is that precipitation of large-size crystals is anticipated, depending on preparation conditions, as shown in the present work.

The other strategy is refractive index matching between the precipitated crystal and the glass matrix through a batch composition design, enabling suppression of light scattering at interfaces between the two phases, *i.e.*, achievement of “optical stoichiometry”.^{5,8} Here, we select MgO as the oversupplied reagent, because MgO crystal yields a high thermal conductivity of $\sim 50 \text{ W (m}^{-1} \text{ K}^{-1})$ ¹¹ and high transparency in the region of UV-Vis-NIR,¹² and additionally the crystal exhibits optical isotropy as well as the glass due to belonging to cubic crystal system and a small refractive index of ~ 1.7 (ref. 13) compared with the other transparent, high thermal conductive crystals, both of which help the index matching with the glass matrix. We expect that the present method and concept are also expanded to development of other transparent oxide glasses having any functionalities such as high fracture toughness.

On the basis of these strategies, we fabricated a glass-ceramic comprising MgO crystal and $\text{La}_2\text{O}_3\text{-B}_2\text{O}_3\text{-SiO}_2\text{-MgO}$ glass matrix and demonstrated that it shows a thermal conductivity of $1.6 \text{ W (m}^{-1} \text{ K}^{-1})$, which is high for tentative multi-component oxide glasses, and a visible transparency of 60% for the sample with a thickness of 0.21 mm.⁵ However, its atomic-scale structure and mechanism of the MgO precipitation have been unclear and its properties are not high enough for practical use. Therefore, we investigate the structures by nuclear magnetic resonance, *etc.* and attempt to improve the thermal conductivity and the transparency. Finally, we present an MgO-dispersed glass-ceramic exhibiting a high thermal conductivity of $3.3 \text{ W (m}^{-1} \text{ K}^{-1})$, high optical transparency, and glass transition and discuss structural designs for higher thermal conductivity by prediction of the effective thermal conductivity based on an effective medium approximation model.

2. Experimental section

2.1 Sample preparation

The batch compositions of samples are listed in Table 1. Samples are hereinafter noted like A[53] with alphabetical names and MgO content as shown in Table 1. First, we used $\text{La}_2\text{O}_3\text{-B}_2\text{O}_3\text{-SiO}_2\text{-MgO}$ system. The process leading to this glass system is described in our previous work.⁵ In this study, we also used Nb_2O_5 , working as the index enhancer in glass,¹⁴ for increase in and precise control of the refractive index. The samples were synthesized as follows:⁵ reagents for these five contents, La_2O_3 (purity: 99.99%), Nb_2O_5 (99.99%), B_2O_3 (99.9%), SiO_2 (99.9%), and MgO (99.99%), purchased from Kojundo Chemical Laboratory Co., Ltd., were weighed and mixed to obtain the compositions of samples (A–D) in Table 1. Before weighing, the MgO reagent was dehydrated by heating at 700°C for 2 h in an electric furnace. The batches were placed in a platinum crucible and melted in air by using an electric furnace with a heating rate of $10^\circ\text{C min}^{-1}$. The melting temperature and time is shown in Table 1. The melts were

poured onto a steel plate maintained at 200°C and immediately quenched by covering with a metal plate, fixing the sample thicknesses at 2 mm with metal jigs.

2.2 Structural investigation

The structural and optical investigations of the samples at a temperature of $\sim 25^\circ\text{C}$ were conducted. For both the as-quenched and powdered samples, their X-ray diffraction (XRD) patterns were recorded with an apparatus (New D8 Advance, Bruker) using CuK_α radiation and θ - 2θ configuration to check the presence of MgO crystal and the glass matrix. The glass transition temperature T_g was determined using pieces with a size of a few mm in broken samples by differential thermal analysis (DTA; TG8120, Rigaku) at a heating rate of $10^\circ\text{C min}^{-1}$. For the pieces, the local coordination states of B and Si, whose oxides are expected to work as network former in glass, were determined from the ^{11}B and ^{29}Si magic angle spinning nuclear magnetic resonance (MAS NMR; ECA-600 and ECA-300 for ^{11}B and ^{29}Si , respectively, JEOL-Resonance). The frequency, the spin rate, the pulse delay, and the field intensity for ^{11}B (^{29}Si) were 192.56 (59.71) MHz, 15 (7.5) kHz, 30 (200) s, and 14.1 (7.0) T, respectively, unless otherwise noted. For the samples whose one side surfaces were mirror-polished by 0.5 mm, the refractive indices at wavelengths of 405, 633, and 829 nm were determined with a prism coupler (Model 2010, Metricon). For the samples with a thickness of 0.35 mm whose both surfaces were mirror-polished, the transmittance optical microscopy was performed and the optical transmittance was measured by means of a UV-Vis-NIR spectrophotometer (UV-3600, Shimadzu).

2.3 Thermal diffusivity and conductivity

The out-of-plane thermal diffusivity D ($\text{mm}^2 \text{ s}^{-1}$) of the 0.35 mm-thick samples was measured with a temperature wave analyzer (Mobile 1u, ai-Phase Co.). For a part of the samples, the out-of-plane thermal conductivity K ($\text{W (m}^{-1} \text{ K}^{-1})$) was calculated using the equation $K = \rho CD$,³ where the density ρ (g cm^{-3}) and the specific heat C ($\text{J (g}^{-1} \text{ K}^{-1})$) were determined by the Archimedes method and differential scanning calorimetry (DSC; 3500 Sirius, NETZSCH), respectively. The DSC measurements were carried out using the pieces.

3. Results and discussions

3.1 XRD and optical properties

Fig. 1a shows the XRD patterns of the as-quenched A[53, 60, 74]. A[53] shows a halo pattern with no sharp peaks, indicating that it is amorphous and/or has no crystals with enough amount and size. The same is true for A[0–43] (not shown). A[60, 74] show the halo patterns and two sharp peaks assigned to $\{111\}$ and $\{200\}$ planes of cubic MgO crystal, where the 111 peak intensity is enhanced and the 220 peak is negligible, compared to the powder pattern of cubic MgO crystal. On the other hand, the XRD patterns in powdered samples (Fig. 1b) has a different behavior from the as-quenched ones: we see the halo patterns in all the samples, but A[53], A[60], and A[74], respectively, show

Table 1 Batch compositions, melting conditions, and properties of samples (A–D). The content denotes a molar ratio, where the value for A[53], approximated to be the MgO-saturated glass, becomes 100 in total. Melting temperature T and time t , and glass transition temperature T_g are shown. Thermal diffusivity D , thermal conductivity K , refractive index for 633 nm light, and optical transmittance at a wavelength of 633 nm for ~ 0.35 mm-thick samples, at a temperature of ~ 25 °C, are also shown. The values of D , K , and n_{633} for MgO refer to a single crystal^{11,13}

Sample	La ₂ O ₃	Nb ₂ O ₅	B ₂ O ₃	SiO ₂	MgO	T (°C)	t (h)	T_g (°C)	D (mm ² s ⁻¹)	K (W (m ⁻¹ K ⁻¹))	n_{633}	T_{633} (%)
A	13	0	24	10	0–43	1400	1	653–675	—	—	—	—
					53			680	0.42	—	1.723	85
					60			681	0.46	—	—	60
					74			684	0.53	—	—	30
B	13	0	24	10	74	1650	4	—	0.70	—	—	54
					110			—	0.88	—	—	—
					140			—	1.6	—	—	20
C	8.2	5.0	24	10	90	1400	1	—	—	—	—	—
D	8.2	4.3	24	10	77	1400	1	—	—	—	1.740	—
					170			688	0.43	1.1	1.733	85
MgO	—	—	—	—	—	—	—	—	1.2	3.3	—	70
					—			—	15	50	1.735	—

no sharp peak, the small peaks due to MgO crystal, and the noticeable peaks corresponding to the powder pattern of MgO crystal. These results for both types of the samples can be interpreted as follows: MgO content is approximately saturated in A[53]. When the MgO content exceeds ~ 53 , the excess MgO prefers to precipitate as $\langle 111 \rangle$ -oriented MgO crystals at the surface, where the $\langle 111 \rangle$ -oriented nucleation may be involved. Such oriented nucleation has been reported¹⁵ in the surface crystallized glasses, but the origin of our result which provides

the enhancement of the 111 peak and the invisibility of the 220 peak has been unclear at present. Further addition of MgO promotes bulk nucleation and growth of MgO crystals below the oriented layer at the surface. This picture seems consistent with the results of optical microscopy in ~ 1 mm depth areas of the as-quenched A[0, 53, 60, 74] (Fig. 2), *i.e.*, we see optical homogeneity in A[0, 53]; on the other hand, in A[60, 74], we see heterogeneous structures wherein the polyhedral particles with a size of ~ 10 μm , which can be assigned to MgO crystal,⁵ are precipitated. Here, we emphasize that the particles are anything but undissolved reagent because we found that the particle size of the MgO reagent is of ~ 1 μm . Structural investigation by cross-sectional scanning/transmission electron microscopy to clarify orientation of the bulk nucleation and the mechanism of the surface (bulk) oriented nucleation will be a future work.

As shown in Table 1, A[53], approximated to the MgO-saturated glass, possesses a thermal diffusivity D of $0.42 \text{ mm}^2 \text{ s}^{-1}$, a refractive index n_{633} of 1.723, and an optical transmittance T_{633} of 85%. As for A[74], D is improved up to 0.53, which is clearly ascribed to the precipitation of MgO crystal (A[74] in Fig. 2), but T_{633} is reduced to 30%. This reduction is due to the light scattering at interfaces between the MgO crystals and the glass matrix, when the difference in n_{633} between the two phases is estimated to be ~ 0.012 (Table 1). This is consistent with the fact that we can clearly distinguish between the two phases in the optical microscopy.

3.2 MAS-NMR and glass transition

We first note that the as-quenched samples are used for the MAS-NMR and DTA measurements. This is not problematic at all, although the as-quenched samples show the different XRD patterns between the surface and the others (Fig. 1). This is because the thickness of the surface area was found to be thinner than ~ 1 μm by cross-sectional optical microscopy and by considering a spatial resolution for the microscopy and it is negligible compared with the total volume fraction, meaning

Fig. 1 XRD patterns of (a) as-quenched and (b) powdered A[53, 60, 74]. The powder pattern of MgO crystal is also shown.

Fig. 2 Optical microscopic images in ~ 1 mm depth areas of the ~ 0.35 mm-thick A[0, 53, 60, 74]. The white scale bars correspond to 100 μm and the photos of the samples are inset.

that NMR spectra and DTA curves dominantly yield information in the areas except for the surfaces.

Fig. 3a shows the ^{11}B MAS NMR spectra of A[0, 33, 53, 74]. We see two bands at chemical shifts of 10–20 and ~ 0 ppm, which are assigned to tri- and tetra-coordinate boron atoms, $^{[3]}\text{B}$ and $^{[4]}\text{B}$, respectively.^{16–18} By addition of MgO, the $^{[4]}\text{B}$ band intensity decreases, and the $^{[3]}\text{B}$ band seems to be moved to a higher chemical shift side together with broadening and deformation. This behavior is known to originate from a second-order quadrupole interaction,^{16–18} and particularly the chemical shift reflects degree of connectivity between trigonal BO_3 units (see Fig. 5 regarding schematics of the units per species), *i.e.*, number of bridging oxygen atoms and whether the units form boroxol ring or not.^{16,18} For A[0], the shoulder at ~ 16 ppm and the peak at ~ 13 ppm can originate from $T^{3(\text{ring})}$ and T^3 where T^n and $T^{n(\text{ring})}$ denote trigonal BO_3 units having n bridging oxygen atoms and ones forming the boroxol ring, respectively.^{16,18} In addition, A[53, 74] show the notable peak around 18 ppm, which are attributable to T^1 , $T^{2(\text{ring})}$, and T^2 . In short, the addition of MgO promotes decrease in connectivity, *i.e.*, formation of disconnected or isolated BO_3 units from tetrahedral BO_4 units, Q_B . Fig. 3b shows MgO content dependences of the fractions of $^{[3]}\text{B}$ and $^{[4]}\text{B}$. Here, we assume that the fractions are proportional to the integrated areas of the bands, which are obtained by fitting the spectra with Gaussian–Lorentzian mixed functions by means of the Dmfit program.¹⁹ The fractions of $^{[3]}\text{B}$ and $^{[4]}\text{B}$ decreases and increases, respectively, by the addition of MgO. At ~ 50 MgO, around which MgO crystal begins to precipitate, and over, the fraction of $^{[3]}\text{B}$ becomes dominant.

The ^{29}Si MAS NMR spectra are shown in Fig. 3c. The spectra can be decomposed with the three peaks at -75 , -78 , and -83 ppm. These peaks can be assigned to Q^0 , Q^1 , and Q^2 species,²⁰ where Q^n denotes tetrahedral SiO_4 units having n bridging oxygen atoms. Fig. 3d shows the fractions of the Q^n species ($n = 0, 1, 2$), obtained in the same way for those of $^{[3]}\text{B}$ and $^{[4]}\text{B}$, as a function of MgO content. Roughly, the average n decreases by the addition of MgO: at the regions lower than ~ 30 MgO and higher than ~ 50 MgO, the Q^2 and Q^0 species are dominant, respectively, and at the intermediate region, Q^1 species exists. Although there may be a little concern on the assignment of Q^n , the addition of MgO clearly causes a decrease in connectivity of tetrahedral SiO_4 units.

Fig. 4 shows the glass transition temperature as a function of MgO content. We see that the value slightly decreases by the addition of MgO in the range of 0–30 MgO and jumps up at 40–50 MgO, and become approximately invariant at >50 MgO. Roughly, the NMR and the DTA results mean that notable structural changes occur around the MgO-saturated composition.

3.3 Structural model

On the basis of these results, we propose a tentative structural model for samples A. Fig. 5a depicts a schematic illustration of A[0]. Here, A[0] has been found to form a transparent, homogeneous glass (Fig. 1 and 2). This fact is consistent with the result in a previous report,²¹ *i.e.*, the composition of $13\text{La}_2\text{O}_3\text{--}24\text{B}_2\text{O}_3\text{--}10\text{SiO}_2$ exists in the transparent glass forming region for the ternary system (Fig. 1 and 3 in ref. 21). The value of T_g for A[0] was ~ 660 $^\circ\text{C}$ in Fig. 4, which seems plausible compared to that of a sample with the similar composition, ~ 680 $^\circ\text{C}$ (sample A4 in ref. 21). The slight difference in T_g can be attributed to the difference in glass

Fig. 3 (a) ^{11}B MAS NMR spectra of A[0, 33, 53, 74] and (b) fractions of $^{[3]}\text{B}$ and $^{[4]}\text{B}$ as functions of MgO content. (c) ^{29}Si MAS NMR spectra of A[0, 33, 53, 74] and (d) fractions of Q^n species ($n = 0, 1, 2$) as functions of MgO content. The dash lines are guides for eyes. The spectrum of A[74] in (a) was obtained with a low spin rate of 6.5 kHz.

preparation conditions such as melting temperature. From the results of MAS-NMR, we infer that the species of T^3 , $T^{3(\text{ring})}$, Q_B , and Q^2 dominantly form the glass network and La^{3+} is uniformly distributed to compensate charge balance (Fig. 5a). The addition of MgO causes the formation of the disconnected or isolated T species

Fig. 4 MgO content dependence of glass transition temperature T_g in samples (A).

from the Q_B one and the disconnection of the bridging Q^2 ones, leading to a decrease in viscosity accompanied by the decrease in glass transition temperature (Fig. 4) in the range of 0–40 MgO. The steep increase in T_g around 40 MgO (Fig. 4), which has been reported in our previous study,⁵ may be attributable to suppression of structural relaxation of the glass network, *i.e.*, high content of MgO gives rise to an increase in viscosity. Fig. 5b corresponds to the structure for the MgO-saturated glass. The sample still forms the transparent glass, despite of high content of MgO (Fig. 2). Here, neglecting SiO_2 content, the composition of $13\text{La}_2\text{O}_3\text{--}24\text{B}_2\text{O}_3\text{--}53\text{MgO}$ seems to be out of the glass forming region for the ternary system,²² although we cannot discuss the details because the preparation conditions differ. However, we consider that the glass forming in the present samples can be due to the presence of SiO_2 , which is consistent with the picture that the added MgO has partially modified the bridging Q^2 species (Fig. 5b). At this composition, we should focus on the following atomic-scale structural changes: the disappearance of Q_B and Q^2 species and the appearance of Q_0 species (Fig. 3b and d). This means that the modification of Q_B and Q^2 species by the added MgO is completed, leading to the MgO-saturated glass. Considering that the fraction of Q_0 species still increases by the further addition of MgO exceeding ~ 50 MgO (Fig. 3d), it is plausible that partial fraction of the excess MgO

Fig. 5 Schematic illustrations of (a) A[0], (b) A[~50], and (c) A[≥50].

modifies the Q^1 species into Q^0 ones, and the majority of the excess MgO loses any species to modify and accordingly aggregated and precipitated as MgO crystal (Fig. 5c). The approximately invariant T_g at 50–80 MgO means that the structure of the glass matrix is uniquely determined in the range.

3.4 Effects of melting temperature and time

We investigate impacts of melting temperature T and time t on the MgO precipitation for improvement of T_{633} . As described above, the low optical transmittance T_{633} in A[74] (Table 1) is attributable to the presence of the small MgO crystals causing the large interfacial area and the light scattering therein. On the basis of our model, the atomic-scale structure of glass matrix above the MgO-saturated composition seems to be unique, indicating that the precipitation morphology of the excess MgO dominates the properties. Accordingly, we need large-size MgO crystals for improvement of T_{633} . To achieve that, high-temperature and long-time melting may be suitable, because we expect that a decrease in the quenching speed and uniform distribution of MgO in melt, induced by the high-temperature and long-time melting, respectively, causes an increase in the size of MgO crystal.

Thus, we set T and t for 1650 °C and 4 h, respectively, and we found that T_{633} is improved up to 54% (Table 1). The result of optical microscopy (B[74] in Fig. 6) clearly shows an increase in the size of the crystal compared with the sample for 1400 °C for 1 h (A[74] in Fig. 2), as anticipated, and accordingly a decrease in the interfacial area between MgO crystal and glass matrix depresses light scattering, leading to the improvement of optical transmittance. Coincidentally, D is found to be improved up to $0.70 \text{ mm}^2 \text{ s}^{-1}$, which can arise from a decrease in interfacial thermal resistance. For B[110], D improves to 0.88 (Table 1) and the optical transparency retained. For B[140], D drastically increases to 1.57, but T_{633} drops to 20%. The origins of the increase and the decrease are clearly due to high-content precipitation of MgO crystal and the existence of air bubbles, respectively (B[140] in Fig. 6). In short, the high-temperature and long-time melting provides the increase in the crystal

size, but the excessive addition of MgO gives rise to the appearance of bubbles, which may be due to an increase in viscosity and/or decomposition of the glass matrix.

3.5 Compositional design for high conductivity and transmittance

Taking A[53] as a standard sample, we optimize the composition for precise index matching with MgO crystal. First, we

Fig. 6 Optical microscopic images in $\sim 1 \text{ mm}$ depth areas of as-quenched D[74, 140]. The white scale bars correspond to 100 μm .

Fig. 7 (a) Refractive index dispersions of MgO crystal¹³ and D[77] and (b) optical transmittance spectra of D[77, 170] with a thickness of ~ 0.35 mm.

increased La_2O_3 content, which works as the index enhancer, but the sample exhibited an optical inhomogeneity, resulting in a decrease in optical transmittance. This result may be consistent with the previous report,²¹ *i.e.*, high content of La_2O_3 causes partial phase separation in the La_2O_3 – B_2O_3 – SiO_2 system.

Then, we added Nb_2O_5 , being also known to be the index enhancer,¹⁴ when the tentative contents of Nb_2O_5 and MgO are 5 and 90, respectively ($\text{C}[90]$ in Table 1). Thus, we found that $\text{C}[90]$ comprises homogeneous glass matrix and MgO crystal and $\text{C}[77]$, whose index is 1.740 (Table 1), approximately corresponds to the MgO -saturated glass. Note that the MgO content in the MgO -saturated composition increases from 53 to 77 by exchanging La_2O_3 for Nb_2O_5 . This may be because Nb_2O_5 partially works as a network former in the glass matrix²³ and consequently dissolution of MgO into the glass matrix is promoted. To decrease the excess index of 1.740, the Nb_2O_5 content is decreased and thus we found that the optimized composition for the glass matrix is that of D[77] with 4.3 Nb_2O_5 . Fig. 7a shows the refractive index dispersions in D[77], which is fitted by the Sellmeier equation,¹ and MgO crystal.¹³ The dispersions are in good agreement between the two samples, in which the difference is as small as 0.002 at a wavelength of 633 nm and we see approximately perfect matching around 500 nm. Finally, we increase the MgO with the condition of 1650 $^\circ\text{C}$ and 4 h for the large-size precipitation of MgO crystal.

As a result, D[170] shows the sharp peaks due to MgO crystal in the XRD pattern, and we hardly identify most of the MgO crystals (~ 50 μm in size) in optical microscopy (Fig. 8), which is consistent with the fact that the indices are successfully matched. In Fig. 7b, D[170] retains a high optical transmittance of $\sim 70\%$ in the visible region. The slight decrease at >700 nm and the significant decrease at <500 nm can be caused by the mismatch of the indices and the light scattering by density fluctuation, respectively.

D[170] is found to yield a high K of 3.3 $\text{W}(\text{m}^{-1}\text{K}^{-1})$. The value of K increases to $\sim 300\%$, $\sim 210\%$ and $\sim 240\%$ compared with those of D[77], our previous sample⁵ and SiO_2 glass,²⁴ respectively. Here, we used measured values of $C_{\text{D}[77]}$ and $C_{\text{D}[170]}$ at a temperature of 25 $^\circ\text{C}$, ~ 0.68 and ~ 0.75 $\text{J}(\text{g}^{-1}\text{K}^{-1})$, respectively. Moreover, the decline of T_{633} by the precipitation of MgO crystal is significantly suppressed to be -15% (Table 1). The result that T_g for D[77] and D[170] are matched (Table 1) is consistent with our structural model, *i.e.*, the glass matrix has a unique structure after the MgO saturation.

Regarding the shaping ability in D[170], we observed glass transition at ~ 688 $^\circ\text{C}$ (Table 1), but subsequent crystallization except for MgO at ~ 800 $^\circ\text{C}$. This point appears to be significantly lower than that of the softening point, so that, at the present, it is hard to provide the shaping ability for D[170] without any structural changes.

3.6 Prediction of effective thermal conductivity

It is worthwhile to theoretically predict the thermal conductivity of the MgO -dispersed glass-ceramic, D[170], on the compositional design for higher thermal conductivity. Many kinds of formula have been proposed to predict effective thermal conductivity of materials comprising matrix and high thermal conductive fillers.²⁵ Among them, we use a modified Bruggeman theory,^{25–27} classified as an effective medium theory, because it involves the validity for high volume fraction compared with the Maxwell–Garnet model and interfacial thermal resistance between the matrix and the fillers,^{25–27} as is the case in our material. Here, we consider that D[77] and MgO crystal correspond to the matrix and the filler, respectively. Then, the density $\rho_{\text{D}[170]}$ of D[170] is given as follows, using the volume fraction f of MgO crystal,

$$\rho_{\text{D}[170]} = (1 - f)\rho_m + f\rho_M, \quad (1)$$

where the subscript m and M denote matrix and MgO crystal, respectively. Then, eqn (1) yields,

$$f = \frac{\rho_m - \rho_{\text{D}[170]}}{\rho_m - \rho_M}. \quad (2)$$

Introducing the values of $\rho_{\text{D}[170]} \sim 3.65$, $\rho_m \sim 3.69$, and $\rho_M \sim 3.58$ g cm^{-3} (ref. 11 and 28) at a temperature of 25 $^\circ\text{C}$ to eqn (2), we obtain $f \sim 0.36$. According to the modified Bruggeman model, the effective thermal conductivity K_{eff} is approximated as follows,^{25–27}

$$(1 - f)^3 = \left(\frac{K_m}{K_{\text{eff}}} \right)^{(1+2\alpha)/(1-\alpha)} \left(\frac{K_{\text{eff}} - K_M(1 - \alpha)}{K_m - K_M(1 - \alpha)} \right)^{3/(1-\alpha)}. \quad (3)$$

Fig. 8 XRD patterns and optical microscopic images of D[77, 170]. The powder pattern of MgO crystal is also shown. The white scale bars correspond to 50 μm and the photos of the samples are inset.

Here, α is a non-dimensional parameter, defined as $\alpha = a_k/a$, where $a_k = R_{\text{int}}K_m$, called Kapitza radius,^{25,26} R_{int} is the interfacial thermal resistance between matrix and MgO crystal, and a ($\sim 25 \mu\text{m}$) is the radius of MgO crystal, here providing that it is sphere. Introducing the experimental values to eqn (3), we can estimate α and R_{int} to be 0.026 and $5.9 \times 10^{-7} \text{ m}^2 \text{ K W}^{-1}$, respectively. It is difficult to validate the value of R_{int} ; however, considering that R_{int} between a film ($\text{La}_{0.7}\text{Sr}_{0.7}\text{MnO}$) and MgO is estimated to $1\text{--}5 \times 10^{-7} \text{ m}^2 \text{ K W}^{-1}$ (ref. 29) and moreover, in this study, the amorphous matrix and defects such as structural ununiformity (dark areas in the image of Fig. 8) can effectively increase R_{int} , the value may be reasonable.

Fig. 9 shows f dependence of K_{eff} for $\alpha = 0, 0.026$. These lines clarify a guideline to obtain a higher thermal conductivity: not surprisingly, small α , *i.e.*, large a and small K_{int} , and high f

contribute to the increase in K_{eff} , but a decrease in α , even if $\alpha = 0$ was achieved, is not much effective for the increase in K_{eff} . On the other hand, an increase in f produces an approximately exponential increase in K_{eff} . However, we found that the MgO content in D[170] is almost equal to the upper limit value to obtain the transparent glass-ceramics, although the details are not shown. To overcome it, dispersion control of the MgO crystals, *e.g.*, formation of percolated MgO crystal network,²⁵ by controlling the melting and quenching conditions and the compositional design, can be promising.

4. Conclusion

For the thermal management applications of glass, we fabricated the MgO-dispersed glass-ceramics by means of the over-supply of the MgO reagent, on the basis of the concept of “optical stoichiometry”.^{5,8} First, we investigated the structures in the $\text{La}_2\text{O}_3\text{--B}_2\text{O}_3\text{--SiO}_2\text{--MgO}$ system (samples A) by XRD, ^{11}B and ^{29}Si MAS-NMR, and optical microscopy. As a result, we found the following structural change: the added MgO modifies the glass matrix network, causing the decrease in the connectivity of $\text{BO}_{3(4)}$ and SiO_4 units. The modification is completed in the MgO-saturated condition. By the further addition of MgO, the excess MgO loses the species to modify and accordingly it is aggregated and precipitated as MgO crystal.

Through the control of the melting temperature and time for the large-size precipitation of MgO crystal and the compositional design for the precise index matching, we reached the composition of $8.2\text{La}_2\text{O}_3\text{--}4.3\text{Nb}_2\text{O}_5\text{--}24\text{B}_2\text{O}_3\text{--}10\text{SiO}_2\text{--}170\text{MgO}$ (D [170]). The sample consisted of the glass matrix and MgO crystal with a volume fraction $f \sim 0.36$ and shows a high thermal conductivity K of $3.3 \text{ W (m}^{-1} \text{ K}^{-1})$, compared to the typical oxide glasses and organic polymers, corresponding to 300% of that of

Fig. 9 f dependence of K_{eff} for $\alpha = 0$ and 0.026 calculated from eqn (3).

the glass matrix (D[77]), and a high optical transmittance T_{633} of 70% for the 0.35 mm-thick sample. From the prediction of the effective thermal conductivity, we revealed that the dispersion control of MgO crystal can be effective for higher thermal conductivity. D[170] exhibits the glass transition at 688 °C, but is crystallized at ~800 °C, so that any further composition explorations are required for achievement of the shaping of the melt. In addition, investigation on difference in the thermal expansion coefficient between the two phases and on defect states such as compositional fluctuation and dangling bonds at the interface will be needed for the practical use. It is expected that the present method and concept are expanded to not only thermal management applications of glass but also development of transparent oxide glasses having any functionalities such as high fracture toughness.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

This work was partially supported by the Ministry of Education, Culture, Sports, Science and Technology of the Japanese government. We thank NETZSCH Japan K. K. for supporting the DSC measurement. We thank Ms Mariko Ando of the Department of Instrumental Analysis, School of Engineering, Tohoku University, and Mr Shingo Ebukuro of the Department of Applied Physics, Tohoku University, for the NMR and density measurements, respectively.

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