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Damage mechanism and electro-elastic stability of LiNbO_3 crystals irradiated with 6 MeV Xe^{23+}

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The trigonal lithium niobate crystal (LiNbO_3 , LN) is a multi-functional material that possesses excellent nonlinear optical, pyroelectric and piezoelectric properties. In this work, the irradiation damage mechanism and stability of the electro-elastic properties of LN crystals irradiated with different doses (10^{13} – 10^{16} ions per cm^2) of 6 MeV Xe^{23+} ions were evaluated for potential piezoelectric applications under irradiation conditions below 650 °C. The vacancy formation energies for Li, O, and Nb atoms are much lower than the irradiation energy of 6 MeV, with the lowest vacancy formation energy being obtained for Li, so that a high concentration of vacancies will be generated in LN upon irradiation. The vacancies narrow the band gap and decrease the electrical resistivity after irradiation. In contrast to the electrical resistivity, the relative dielectric permittivity of the LN crystal was found to increase with increasing irradiation dose, due to the weakened chemical bonds and distorted crystal structure, as confirmed by X-ray photoelectron spectroscopy. Despite the irradiation, the effective piezoelectric coefficients of bulk LN crystal remain nearly unchanged, indicating the favorable properties of LN for use under irradiation conditions at temperatures up to 650 °C.

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1. Introduction

High-temperature piezoelectric single crystals are required for sensors under critical conditions found in nuclear power plants, and in automotive, aeronautic and space applications. For example, the piezoelectric vibration sensors used in nuclear power plants usually endure irradiation and high temperatures above 400 °C. To satisfy the requirements of these applications, piezoelectric materials must show low dielectric loss and high resistivity as well as high piezoelectric performance with good temperature stability.^{1,2}

Trigonal lithium niobate crystals (LiNbO_3 , LN) have excellent optical and electrical properties such as the optical waveguiding, photo-refractivity, pyroelectricity, optical storage, and piezoelectric properties *etc.*^{3–9} The high ferroelectric-to-paraelectric phase transmission temperature of LN ($\sim 1195 \pm 15$ °C) enables the operation of LN-based devices at temperatures above 600 °C.^{7,10} Moreover, the effective piezoelectric coefficient d_{eff} of LN is on the order of 70 pC N⁻¹, thirty times higher than that of α -quartz (α -SiO₂) (~ 2 pC N⁻¹), favoring the use of LN crystal for piezoelectric sensing at high temperatures.^{11–14}

There are many reports on the irradiation damage for LN crystal such as the damage evolution in LN irradiated by Si ions,¹⁵ high-energy electron irradiation of stoichiometric LN,¹⁶ optical damage in LN induced by X-ray irradiation,¹⁷ *et al.* And

the extensive testing of different prototypes of piezoelectric sensors based on the LN crystal have been investigated.^{14,18–21} Irradiation is known to induce defects in crystals, affecting their electrical properties.^{22–25} However, there have been few reports on the stability of the electrical and piezoelectric properties of LN crystal as well as the relations between irradiation damage and variations of electro-elastic properties under the influence of intense ion irradiation. Therefore, in this work, the irradiation influencing mechanism and stabilities of the electro-elastic properties of an LN crystal irradiated by different doses (10^{13} , 10^{15} , and 10^{16} ions per cm^2) of 6 MeV Xe^{23+} ions were investigated to evaluate the potential use of LN piezoelectric crystal in irradiation conditions in nuclear power industry. Theoretical analysis, stopping and range of ions in matter (SRIM) simulations, and electron paramagnetic resonance (EPR) and X-ray photoelectron spectroscopy (XPS) measurements combined with first-principle calculations were used for this purpose in the present study.

2. Experimental

2.1 Sample preparation

The congruent composition of LN crystal was grown by the classical Czochralski method.^{26,27} The raw materials for single crystal growth were prepared with stoichiometric ratio. The pulling and rotation rates were 0.6–0.9 mm h⁻¹ and 6–8 rpm, respectively. The Li/Nb ratio of the grown LN crystal was 48.6/51.4.

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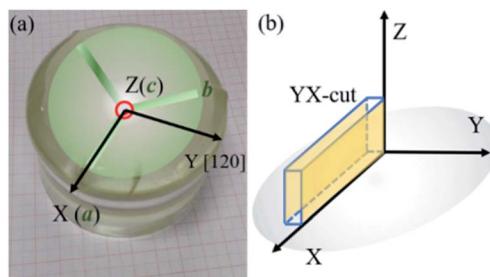


Fig. 1 The picture of LN crystal and the relationship between the crystallographic (a , b , c) and physical axes (X , Y , Z) (a), the orientations of YX-cut in physical coordinate (b).

Fig. 1(a) shows the picture of grown LN crystal and the schematic of the cross-section of LN crystal with the relationship between the crystallographic and physical axes determined referring to the IEEE standard on piezoelectricity.²⁸ The rectangular plate-shaped YX-cuts (Fig. 1(b)) with dimension of $12 \times 3 \times 1.2 \text{ mm}^3$ were orientated and prepared for tests.

2.2 The evaluation of electro-elastic constants

Rectangular YX-cut plate-shaped ($15 \times 3 \times 1.2 \text{ mm}^3$) samples were prepared and divided into four groups, with the first three bombarded by Xe^{23+} ions with the doses of 10^{13} , 10^{15} , and 10^{16} ions per cm^2 , respectively, while the last one was not irradiated and was used for comparison.

The electrical resistivities ρ_{22} were obtained by measuring the resistances of the samples using a source meter (Keithley 2410C). To study the electro-elastic properties in the temperature range from room temperature to 650°C , the capacitances (measured at 100 kHz), and the resonance (f_r) and anti-resonance (f_a) frequencies at different temperatures were measured using a multi-frequency LCR meter (Agilent 4263B, USA) and an impedance-phase gain analyser (Keysight E4990A) connected to a custom high-temperature furnace. The relative dielectric permittivity was evaluated according to eqn (1), where C , A , t and ϵ_0 are the capacitance, electrode area, thickness and dielectric permittivity in vacuum, respectively. The electromechanical coupling factor k_{21} and elastic compliance s_{11} as well as the piezoelectric coefficient d_{21} of the YX-cut samples were calculated by eqn (2)–(4) using the impedance method, where the l , ρ , f_r and f_a are the sample length, crystal density, and resonance and anti-resonance frequencies, respectively.

$$\epsilon_{22}/\epsilon_0 = \frac{Ct}{A\epsilon_0} \quad (1)$$

$$\frac{k_{21}^2}{1 - k_{21}^2} = \frac{\pi f_a}{2 f_r} \tan \frac{\pi}{2} \left(\frac{f_a - f_r}{f_r} \right) \quad (2)$$

$$s_{11} = \frac{1}{4\rho l^2 f_r^2} \quad (3)$$

$$d_{21} = k_{21} \sqrt{\epsilon_{22} s_{11}} \quad (4)$$

2.3 SRIM simulation

The nuclear and electronic energy loss profiles induced by the $6 \text{ MeV} \text{Xe}^{23+}$ ions in LN crystal were determined using SRIM 2013 with the full-cascade simulation code in which the density of 4.65 g cm^{-3} and threshold displacement energies of 25, 25, and 28 eV for Li, Nb, and O sublattices, respectively were used.²⁹

2.4 EPR analysis

The EPR spectra of the YX-cut LN crystal samples were recorded using a Bruker EMX plus EPR spectrometer (300 K, X band). The wavelength of the excitation laser beam was 532 nm, the central magnetic field intensity was on the order of 3500 G with sweep width being 150 G.

2.5 First-principles calculations

Density functional theory (DFT) calculations were performed using the Vienna *ab initio* Simulation Package^{29,30} with the Li $2s^1$, O $2s^2 2p^4$, and Nb $4d^4 5s^1$ states treated as the valence electrons. The electronic wave functions were expanded in a plane wave basis set up to the cutoff energy of 300 eV. The local-density approximation in the Ceperley–Alder and Perdew–Zunger form^{31,32} was used to describe the exchange–correlation potential, and to calculate the vacancy formation energies for atoms in LN.

The oxygen vacancy (V_O) model of LN crystal was constructed by removing one O atom from the unit cell. We could get the lithium vacancy (V_{Li}) and niobium vacancy (V_{Nb}) models following the same way. The vacancy formation energy could be evaluated using the following equation,³³

$$E_V = E_D + \mu_i - E_p \quad (5)$$

where E_p and E_D are the total energy of the supercell with and free of the corresponding vacancy, μ_i is the chemical potential of the corresponding atoms. The chemical potentials of Li and Nb atoms were calculated by using their corresponding elemental phases. Furthermore, a model structure of oxygen molecular with a dimension of $10 \times 10 \times 10 \text{ \AA}^3$ was utilized to calculate the chemical potential of oxygen atom being half of the O_2 total energy.

2.6 XPS analysis

The XPS spectra of the pristine and Xe^{23+} -irradiated LN crystals were obtained using an ESCALAB 250 X-ray photoelectron spectrometer (Thermo-Fisher, USA) with monochromatized Al $K\alpha$ X-ray radiation in ultrahigh vacuum ($< 10^{-7} \text{ Pa}$). The obtained binding energies were calibrated by the C 1s peak (284.6 eV) of carbon impurities as the reference, and the spectra were de-convoluted after subtracting the background with a mixed Gaussian–Lorentzian function. All the results were analyzed by using the Advantage software.



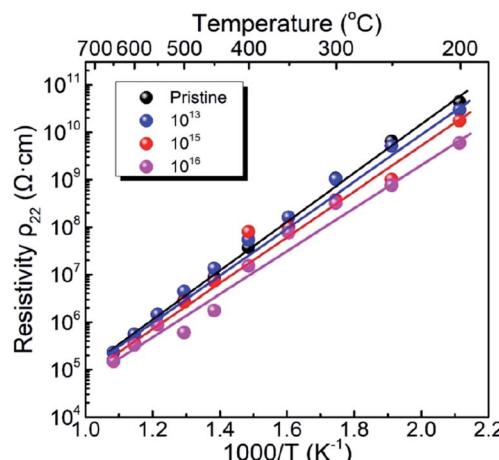


Fig. 2 Variation of electrical resistivity as a function of temperature for the pristine LN sample and the LN samples irradiated with the doses of 10^{13} , 10^{15} , and 10^{16} ions per cm^2 .

3. Results and discussion

3.1 Stabilities of electrical and electro-elastic properties after irradiation

Fig. 2 shows the electrical resistivity plotted as a function of inverse temperature for the pristine LN crystal and for the LN samples irradiated with different doses of Xe^{23+} (10^{13} , 10^{15} , and 10^{16} ions per cm^2) for the temperature range of $200\text{--}650\text{ }^\circ\text{C}$. The electrical resistivity of the LN crystal was $6 \times 10^9 \Omega \text{ cm}$ at $200\text{ }^\circ\text{C}$ after irradiation with a dose of 10^{16} ions per cm^2 , decreasing by approximately one order of magnitude compared to the pristine sample ($4.4 \times 10^{10} \Omega \text{ cm}$). It was also found that at $650\text{ }^\circ\text{C}$, the electrical resistivities of the LN samples both before and after irradiation were $\sim 1.5 \times 10^5 \Omega \text{ cm}$ since the electrical conduction at elevated temperature is attributed to the intrinsic band gap of crystal material rather than the defects induced by the irradiation,¹⁵ indicating that the Xe^{23+} irradiation has little influence on the high-temperature electrical resistivity of the LN crystal. Considering the main contribution of electrons to electrical conductivity, the activation energy for motivating the electrons to participant electrical conductivity was calculated using the Arrhenius law (eqn (6)),

$$\rho = A e^{-E_a/RT} \quad (6)$$

where E_a , A , T , and K are the activation energy, pre-exponential factor, absolute temperature, and the molar gas constant, respectively. The calculated activation energies of the pristine sample and the samples irradiated with the irradiation doses of 10^{13} , 10^{15} , and 10^{16} ions per cm^2 were 0.972, 0.968, 0.949, and 0.883 eV, respectively. It is clear the activation energy decreases with irradiation dose increasing. This phenomenon might be related to the variation of defect levels induced by the 6 MeV Xe^{23+} irradiation, which decreases the energy needed for the electron to be motivated into the conduction bands.²⁴

Fig. 3(a-d) show the relative dielectric permittivity (ϵ_{22}/ϵ_0), elastic compliance (s_{11}), electromechanical coupling factor (k_{21}), and piezoelectric coefficient (d_{21}) plotted as a function of temperature for the pristine sample and for the samples irradiated with different doses. It was observed that ϵ_{22}/ϵ_0 at room temperature shows a slight increase with increasing irradiation dose (Fig. 2(a)). The ϵ_{22}/ϵ_0 value of the pristine LN sample is ~ 84 at room temperature, and increases slightly to 86 after irradiation with the dose of 10^{16} ions per cm^2 , obtaining a change less than 5%. Furthermore, the s_{11} values of the irradiated samples were found to be the same as the pristine LN crystal (Fig. 2(b)). In contrast to ϵ_{22}/ϵ_0 , k_{21} was found to decrease slightly with increasing irradiation dose (Fig. 2(c)), contributing to the stability of the d_{21} value for the irradiated samples according to eqn (4), as shown in Fig. 2(d).

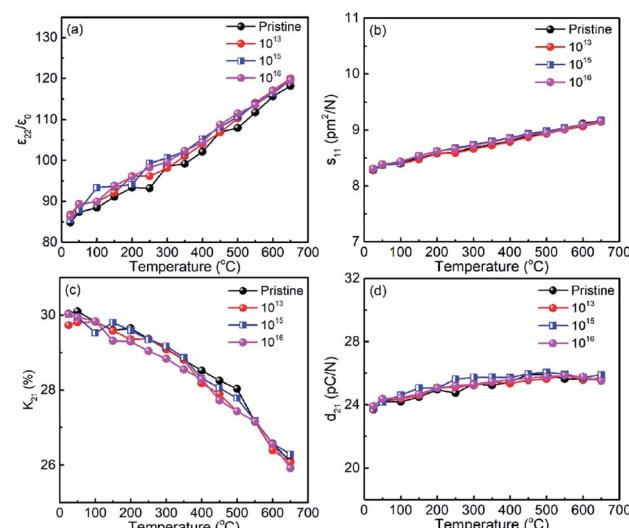


Fig. 3 Variations of electro-elastic constants of pristine and annealed LN samples as a function of temperature (a) relative dielectric permittivity ϵ_{22}/ϵ_0 , (b) elastic compliance s_{11} , (c) electromechanical coupling factor k_{21} , and (d) piezoelectric coefficient d_{21} .

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3.2 Irradiation damage analysis

The damage to the LN crystal as well as the nuclear and electronic energy losses induced by 6 MeV Xe^{23+} irradiation were evaluated. There are two types of stopping mechanisms for the bombardment by heavy ions, namely the nuclear stopping and the electron stopping. The stopping energies of the nuclear and the electronic states are described by eqn (7) and (8),³⁴ respectively,

$$s_n^0 = 2.8 \times 10^{-15} \frac{Z_1 Z_2}{(Z_1^{2/3} + Z_2^{2/3})} \frac{m_1}{m_1 + m_2} \quad (7)$$

$$S_e(E_1) = K E_1^{1/2} \quad (8)$$

where m_1 , Z_1 , and E_1 are the mass, atomic number, and energy of the bombarding ion, respectively, and m_2 and Z_2 are the mass and atomic number of the target material, respectively. K is a constant associated with the interaction between the bombarding ions and the target material. Nuclear plays an



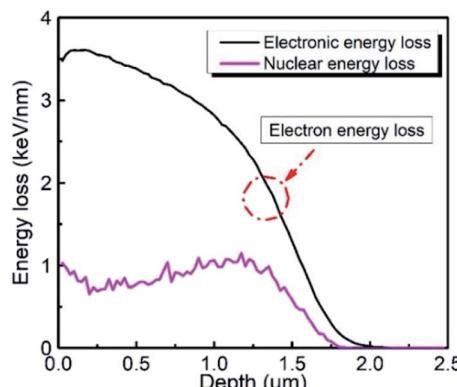


Fig. 4 Electron energy loss and nuclear energy loss as a function of depth of the LN sample.

important role in stopping bombardment by low-energy ions, while electron stopping is dominant for bombardment by high-energy ions. Hence, the critical threshold energy (E_c) of the bombarding ions was used to evaluate whether the nuclear or electron stopping is the dominant mechanism for preventing the bombardment damage. Here, E_c was calculated to be $\sim 2.76 \times 10^4$ eV based on eqn (7) and (8), which is much smaller than the 6 MeV energy of the ions used in this work, indicating that electronic stopping plays the dominant role in preventing the bombardment-induced damage. This was confirmed by the electron and nuclear energy loss simulation carried out by the SRIM simulation as can be seen in Fig. 4. It is clear the electronic energy loss is much higher than the nuclear energy loss (Fig. 4), indicating that electronic energy loss is dominant when LN is irradiated by the 6 MeV Xe^{23+} .

The irradiation depth for an LN crystal irradiated by the 6 MeV Xe^{23+} was evaluated according to eqn (9),

$$R = \frac{1}{N} \int_0^{E_1} \frac{dE_1}{S_e(E_1)} \approx \frac{1}{NK} \int_0^{E_1} E_1^{-1/2} dE_1 = \frac{2}{NK} E_1^{1/2} \quad (9)$$

where N is the number of atoms per cubic centimeter in the target material. The irradiation depth was calculated to be 3.7 μm for the LN crystal bombarded by 6 MeV Xe^{23+} and is similar to the irradiation depth of $\sim 2 \mu\text{m}$ obtained by SRIM simulations. According to both experiments and simulations, it is clear that the irradiation depth is much smaller than the thickness of the tested samples ($\sim 1 \text{ mm}$), indicating that 6 MeV Xe^{23+} ion bombardment has little influence on the electro-elastic properties of the LN crystal, which contributes to the stable piezoelectric properties of LN crystal when irradiated by the 6 MeV Xe^{23+} . And the Xe^{23+} irradiation condition only influences on the surface chemical structure of the bulk LN crystal samples.

3.3 EPR and the first principle calculation analysis

To evaluate the chemical stability of the different atoms in LN crystal, we used DFT calculations to determine the vacancy formation energies of Li, O, and Nb atoms. A higher vacancy formation energy corresponds to higher chemical stability of the atom. The vacancy formation energies of lithium, oxygen,

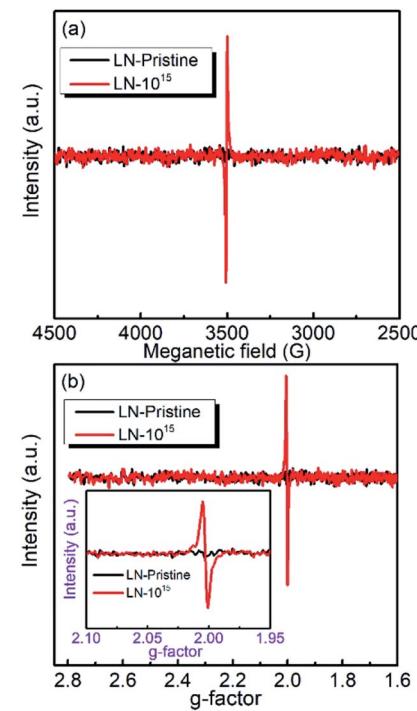


Fig. 5 (a) EPR spectra of the LN crystal; (b) calculated g -factor obtained at room temperature.

and niobium atoms were calculated to be 5.384, 6.780, and 18.426 eV, respectively. It indicates that under irradiation, a high density of vacancies of all three elements in the LN crystal will be generated because the irradiation energy (6 MeV)

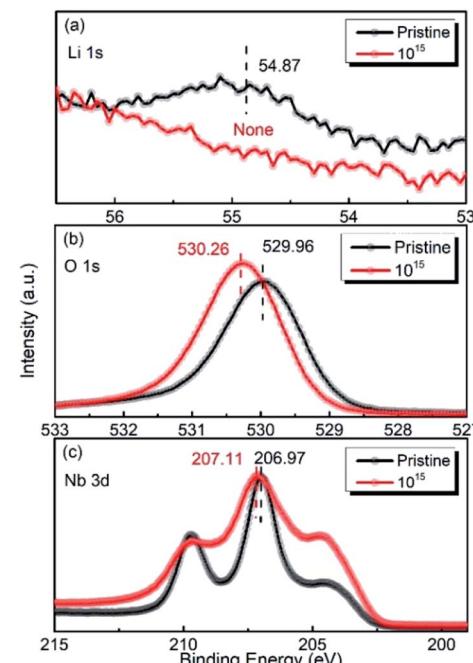


Fig. 6 XPS spectra of Li 1s (a), O 1s (b), and Nb 3d (c) before and after irradiation with the dose of 10^{15} ions per cm^2 .



Table 1 Binding energies and peak area fraction for lithium, oxygen, and niobium elements of the LN crystal before and after the irradiation

Elements	Binding energy		Contents ($\pm 5\%$)		Variations ($\pm 5\%$)
	Pristine	10^{15}	Pristine	10^{15}	
Li	54.87	—	19.10	0	-100%
O	529.96	530.26	67.74	82.52	21.82
Nb	206.97	207.11	13.16	17.48	32.83

is much larger than the vacancy formation energies and the threshold displacement energies being among 25–28 eV²⁰ for all of the atoms. The vacancies provide defect levels in the band gap, decrease the activation energies of carriers for electrical conduction, and reduce the electrical resistivity as well as the activation energy E_a , which is coincided with the electrical resistivity results. DFT calculations also showed that the vacancy formation energy was lowest (5.384 eV) for lithium, indicating that under 6 MeV Xe^{23+} irradiation, it is easier to remove the lithium atoms from the cell than niobium and oxygen atoms. In addition, the formation of oxygen vacancies by Xe^{23+} irradiation was confirmed by the comparison of the EPR spectra obtained before and after irradiation, for which the g-factor was calculated to be ~ 2.003 ,^{35–37} as shown in Fig. 5. Niobium was found to have the largest vacancy formation energy (18.426 eV), indicating that niobium is the most stable atom in LN crystal under irradiation condition.

3.4 Electronic structure analysis

The X-ray photoelectron spectroscopy is an effective method for the investigation of the variations in chemical bonding and composition in the crystals affected by different environmental conditions.^{38,39} When a metal–oxygen (M–O) bond formed (M: Li and Nb), valence electrons are transferred from the metal to oxygen. Therefore, it is difficult to eject an electron from a metal ion because the valence electron density of the metal is shifted towards oxygen, and the binding energy of the metal ion is shifted to a higher value.^{38,40} Consequently, for stronger M–O chemical bonding, the binding energy of metal M increases, while that of O 1s decreases. Conversely, a higher binding energy value of O 1s is associated with weaker M–O chemical bonding.

Fig. 6(a–c) show the XPS spectra of Li 1s, O 1s, and Nb 3d for the LN crystal irradiated by 6 MeV Xe^{23+} (10^{15} ions per cm^2) together with the corresponding spectra of the pristine LN crystal for comparison. It was observed that the binding energies of Li 1s, O 1s, and Nb 3d shows different values from the pristine LN crystal, indicating that the structure of the LN crystal became distorted after irradiation. In particularly, it was found that the signal for lithium is barely detected due to the small content induced by the irradiation (Fig. 6(a)), as can be seen in Table 1. Meanwhile, Fig. 6(b) shows that the binding energy of O 1s increases from 529.96 eV for the pristine LN crystal to 530.26 eV after irradiation, indicating the weakening

of the M–O bond, as discussed above. It is clear that the increased dielectric permittivity is associated with the distortion of the crystal structure and the weakened Li–O chemical bonding induced by irradiation as found by XPS.²⁴ So it is reasonable to conclude that despite the neglectable effect on the LN bulk crystals, it needs to point out that such an irradiation depth might affect the properties of thin-film devices. Unlike the Li 1s and O 1s peaks, it was found that the binding energy of Nb 3d hardly changes after irradiation (Fig. 6(c)). This indicates that the Nb atom is the most stable atom in LN crystal under irradiation by the 6 MeV Xe^{23+} , in agreement with the vacancy formation energies obtained by DFT calculations.

4. Conclusions

In this work, the irradiation damage and structural changes as well as the variations of electro-elastic properties for LN crystal induced by 6 MeV Xe^{23+} irradiation were studied. It was found that irradiation generates a high concentration of lithium, oxygen, and niobium vacancies in the LN crystal since the vacancy formation energies (5.384, 6.780, and 18.426 eV, respectively) and the threshold displacement energies are much lower than the irradiation energy 6 MeV. Such formation of vacancies is likely to be responsible for the observed slight decrease in the electrical resistivity of the crystal upon irradiation. The distortion of the structure and weakened chemical bonding, particularly for the Li–O bonds, were confirmed by XPS results, and contribute to the observed slight increase of ϵ_{22}/ϵ_0 from 84 to 86 at room temperature and the slight decrease in k_{21} . However, the small irradiation depth due to electronic stopping gives rise to stable d_{21} even after irradiation by 6 MeV Xe^{23+} with the dose of 10^{16} ions per cm^2 , demonstrating the favorable properties of the bulk piezoelectric LN crystal for use in high-temperature and irradiation conditions.

Conflicts of interest

There are no conflicts to declare.

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References

- 1 X. N. Jiang, K. Kim, S. J. Zhang, J. Johnson and G. Salazar, *Sensors*, 2014, **14**, 144–169.
- 2 S. J. Zhang, J. Luo, D. W. Snyder and T. R. Shroud, in *Handbook of Advanced Dielectric, Piezoelectric and Ferroelectric Materials-Synthesis, Characterization and Applications*, ed. Z. G. Ye, Woodhead Publishing Ltd., Cambridge, England, 2008, pp. 130–157.



3 D. Von der Linde, A. M. Glass and K. F. Rodgers, *Appl. Phys. Lett.*, 1974, **25**, 155–157.

4 I. P. Kaminow and J. R. Carruthers, *Appl. Phys. Lett.*, 1973, **22**, 326–328.

5 B. Rosenblum, P. Bräunlich and J. P. Carrico, *Appl. Phys. Lett.*, 1974, **25**, 17–19.

6 I. B. Barkan, A. V. Vorob'ev and S. I. Marenikov, *Sov. J. Quant. Electron.*, 1979, **9**, 492.

7 F. F. Chen, L. F. Kong, W. Song, C. Jiang, S. W. Tian, F. P. Yu, L. Qin, C. L. Wang and X. Zhao, *Journal of Materiomics*, 2019, **5**, 73–80.

8 Y. Wang and Y. J. Jiang, *Opt. Mater.*, 2003, **23**, 403–408.

9 L. Dai, Z. H. Yan, S. S. Jiao, C. Xu and Y. H. Xu, *J. Alloys Compd.*, 2015, **644**, 502–505.

10 R. C. Miller and A. Savage, *Appl. Phys. Lett.*, 1966, **9**, 169–171.

11 V. E. Bottom, *J. Appl. Phys.*, 1970, **41**, 3941–3944.

12 D. B. Fraser and A. W. Warner, *J. Appl. Phys.*, 1966, **37**, 3853–3854.

13 A. Randles, S. Tanaka, B. Pokines and M. Esashi, *The 13th International Conference on Solid-State Sensors, Actuators and Microsystems*, 2005, pp. 1380–1383.

14 M. H. Amini, A. N. Sinclair and T. W. Coyle, *IEEE Transactions on Ultrasonics, Ferroelectrics, and Frequency Control*, 2016, **63**, 448–455.

15 S. W. Tian, L. L. Li, X. Y. Lu, F. P. Yu, Y. L. Li, C. Jiang, X. Duan, Z. P. Wang, S. J. Zhang and X. Zhao, *Acta Mater.*, 2020, **183**, 165–171.

16 E. Hodgson and F. Agullo-Lopez, *J. Phys.: Condens. Matter*, 1989, **1**, 10015–10020.

17 Y. Ohmori, M. Yamaguchi, K. Yoshino and Y. Inuishi, *Jpn. J. Appl. Phys.*, 1977, **16**, 4302–4306.

18 K. Nakamura and Y. Adachi, *Electron. Commun. Jpn. Part III Fundam. Electron. Sci.*, 1998, **81**, 1–6.

19 A. M. Glass, D. v. d. Linde and T. J. Negran, in *Landmark Papers On Photorefractive Nonlinear Optics*, World Scientific, 1995, pp. 371–373.

20 F. Schremppel, T. Gischkat, H. Hartung, E. B. Kley, W. Wesch and A. Tünnermann, *MRS Online Proc. Libr.*, 2005, 908.

21 L. Arizmendi, J. M. Cabrera and F. Agullo-Lopez, *J. Phys. Solid State Phys.*, 1984, **17**, 515–529.

22 S. W. Tian, L. L. Li, F. P. Yu, Y. L. Li, F. F. Chen, X. L. Duan, X. F. Cheng, Z. P. Wang, S. J. Zhang and X. Zhao, *Appl. Phys. Lett.*, 2018, **113**, 122905.

23 A. Rivera, J. Olivares, G. García, J. M. Cabrera, F. Agulló-Rueda and F. Agulló-López, *Phys. Status Solidi A*, 2009, **206**, 1109–1116.

24 S. W. Tian, L. L. Li, F. F. Chen, C. Jiang, F. P. Yu, Y. L. Li, X. L. Duan, Z. P. Wang, S. J. Zhang and X. Zhao, *Journal of Materiomics*, 2019, **5**, 363–371.

25 E. R. Hodgson and F. Agullo-Lopez, *Solid State Commun.*, 1987, **64**, 965–968.

26 A. A. Ballman, *J. Am. Ceram. Soc.*, 1965, **48**, 112–113.

27 Y. Zhang, Y. Xu, M. Li and Y. Zhao, *J. Cryst. Growth*, 2001, **233**, 537–540.

28 A. H. Meitzler, D. Berlincourt, F. S. Welsh, H. F. Tiersten, G. A. Coquin and A. W. Warner, *IEEE Standard on piezoelectricity. An American National Standard*, IEEE, New York, 1987, vol. 14.

29 G. Kresse and J. Furthmüller, *Comput. Mater. Sci.*, 1996, **6**, 15–50.

30 G. Kresse and J. Furthmüller, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1996, **54**, 11169.

31 D. M. Ceperley and B. J. Alder, *Phys. Rev. Lett.*, 1980, **45**, 566.

32 J. P. Perdew and A. Zunger, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1981, **23**, 5048.

33 T. Mayeshiba and D. Morgan, *Solid State Ionics*, 2017, **311**, 105–117.

34 Y. H. Wang and Z. Q. Hu, *Ion Implantation and Analysis Basis*, Aviation Industry Press Beijing, 1992.

35 C. Canevali, N. Chiodini, P. Di Nola, F. Morazzoni, R. Scotti and C. L. Bianchi, *J. Mater. Chem.*, 1997, **7**, 997–1002.

36 M. Ivanovskaya, G. Branitskii, D. Orlik, S. Mal'chenko and A. Vrublevskii, *Russ. J. Inorg. Chem.*, 1992, **37**, 577–580.

37 M. Che and A. Tench, in *Advances in catalysis*, Elsevier, 1983, vol. 32, pp. 1–148.

38 J. Liu, X. L. Duan, Y. Zhang, Z. Q. Li, F. P. Yu and H. D. Jiang, *J. Alloys Compd.*, 2016, **660**, 356–360.

39 X. L. Duan, J. Liu, Y. Chen, Z. Q. Li, P. F. Zhu and H. D. Jiang, *Vacuum*, 2018, **147**, 38–44.

40 V. V. Atuchin, V. G. Kesler, G. Meng and Z. S. Lin, *J. Phys.: Condens. Matter*, 2012, **24**, 405503.

