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Investigating the effects of adding hybrid nanoparticles, graphene and boron nitride nanosheets, to octadecane on its thermal properties†

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Octadecane is an alkane that is used to store thermal energy at ambient temperature as a phase change material. A molecular dynamics study was conducted to investigate the effects of adding graphene and a boron nitride nanosheet on the thermal and structural properties of octadecane paraffin. The PCFF force field for paraffin, AIREBO potential for graphene, Tersoff potential for the boron nitride nanosheet, and Lennard-Jones potential for the van der Waals interaction between the nanoparticles and *n*-alkanes were used. Equilibrium and nonequilibrium molecular dynamics simulations were used to study the nano-enhanced phase change material properties. Results showed that the nanocomposite had a lower density change, more heat capacity (except at 300 K), more thermal conductivity, and a lower diffusion coefficient in comparison with pure paraffin. Additionally, the nanocomposite had a higher melting point, higher phonon density of state and radial distribution function peaks.

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1 Introduction

N-Paraffins (*n*-alkanes) are long chains of hydrocarbons with the chemical formula C_nH_{2n+2} .¹ These materials can be used for thermal energy storage (TES) applications and thermal management.² Different kinds of paraffins have many advantages such as high latent heat, low cost, and excellent melting temperature range, but an important disadvantage is their low thermal conductivity.³ Using high thermal conductive nanoparticles⁴ can ameliorate this defect.⁵ Qu *et al.*⁶ studied the effect of a hybrid of expanded graphite (EG) and multi-walled carbon nanotube (MWCNT) on the thermal conductivity enhancement of paraffin. The best result of their study was a 444% enhancement of the thermal conductivity for the hybrid nano-additives. The authors declared that using hybrid nano-additives was more effective than using a single one. A boron nitride nanosheet (BNNS) was used by Fang *et al.*⁷ to enhance the thermal energy storage properties of the paraffin-based phase change material (PCM). The result was that the presence of BNNS (up to 10 wt%) increased the thermal conductivity

of the nano-enhanced PCM (NEPCM) by up to 60%, while it decreased the latent heat of fusion by about 12%. A graphene nano-platelet (GNP) was used by Fang *et al.*⁸ to add to the *n*-eicosane paraffin. The results show that with the highest loading of 10 wt% of GNP, the thermal conductivity increased by about 400% at 10 °C. However, this addition led to a decrease of 16% in the latent heat capacity (for 10 wt% of GNP).

Molecular dynamics simulations have been demonstrated to be a useful tool for researchers to study the thermal properties of paraffin molecules. Every molecule is explicitly considered in this technique. The interaction of each atom with others is calculated using an atomic force field, which is the gradient of the potential energy function.⁹ Babaei *et al.*¹⁰ designed and simulated octadecane ($C_{18}H_{38}$) using carbon nanotubes and graphene. They demonstrated that adding carbon nanotubes and graphene improved the thermal conductivity, and decreased the thermal resistance as well. Indeed, by modifying the molecular alignment, these nano additives can increase the heat conductivity. They fixed the nano-additives to survey just the pure paraffin thermal properties. The findings of the non-equilibrium molecular dynamics (NEMD) simulations indicated that the thermal conductivity of paraffin-CNT at 270 K and 300 K was 0.499 and 0.243 W mK⁻¹, respectively. Moreover, this study showed that the thermal conductivity of paraffin-graphene was 0.560 and 0.249 W mK⁻¹ at 270 K and 320 K, respectively, while the pure paraffin thermal conductivity was 0.3 and 0.164 W mK⁻¹ at 270 K and 300 K, respectively. The eicosane system ($C_{20}H_{42}$) comprising boron nitride was carried

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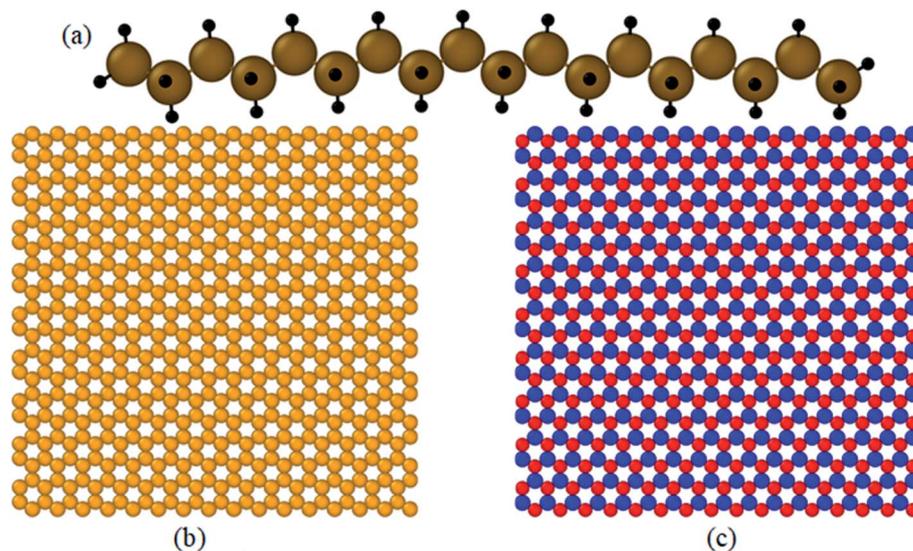


Fig. 1 Structure of: (a) an octadecane molecule ($C_{18}H_{38}$), (b) graphene, and (c) boron nitride nanosheet (BNNS).

out by Rao *et al.*¹¹ Using an equilibrium molecular dynamics simulation to study the thermal conductivity and other thermal properties, they chose *n*-eicosane alkane as the paraffin. Two paraffin mixtures, including the boron nitride nanosheet (BNNS) and boron nitride nanotube (BNNT), were simulated. Results revealed that the latent heat of the composites was reduced, in comparison to pure paraffin, after the addition of BN nanostructures. Conversely, the nano-additives significantly improved the thermal conductivity of pure paraffin. As will be shown in this paper, some discrepant results have been observed in these different studies. These differences arose from using different force fields and potentials, calculating several parameters in a wide range of temperatures, and incorporating different nanoparticles in one system, among others. By and large, fixing the nanoparticles and not allowing them to move is not a valid method to calculate the thermal properties of all nanocomposite systems. Additionally, using the equilibrium method for calculating thermal conductivity will produce much higher values for the nano-enhanced PCMs. Therefore, we think this method is not true for these systems. Accordingly, in this paper, we used the nonequilibrium method for the thermal conductivity calculation.

This paper studies the effects of adding nano-additives of graphene and BNNS to *n*-octadecane paraffin ($C_{18}H_{38}$). To the best of our knowledge, this has not been studied experimentally or numerically before. The essential contributions of this paper are as follows:

- (1) A novel nanocomposite containing graphene and a boron nitride nanosheet was introduced.
- (2) Several structural and thermal properties were studied to deeply investigate the PCM and NEPCM behaviors at different temperatures.
- (3) The proposed nanocomposite can be used as a NEPCM with better thermo-structural properties.

The rest of this paper is organized as follows: Section 2 explains the modeling structures, how they are built, simulation

trends and computational techniques. Section 3 presents the outcomes (including heat capacity, mean square displacement, diffusion coefficient, radial distribution function, phonon density of state, density, and thermal conductivity) and discussion, and finally, Section 4 presents the findings.

2 Materials and methods

2.1 Structures

All simulations were carried out with the package of the massively parallel atomic/molecular simulator (LAMMPS).¹² The velocity Verlet algorithm¹³ was used to numerically incorporate Newton's motion equation. The structures were visualized using Ovito software.¹⁴ The octadecane molecule ($C_{18}H_{38}$), single-layer graphene, and boron nitride nanosheet structures are shown in Fig. 1.

The box size for pure paraffin was $65 \times 65 \times 65 \text{ \AA}^3$ for 500 octadecane molecules. For the nanocomposite, the size of the box was $75 \times 75 \times 75 \text{ \AA}^3$. The graphene and BNNS weight proportions in the composite mixture were approximately 4.9% and 5.1%, respectively. Simulated graphene and BNNS were $38 \times 38 \text{ \AA}^2$. At the beginning of the simulations, the energy of the systems was minimized using the conjugate gradient algorithm.¹⁵ Fig. 2(a) indicates the structure of pure paraffin used in simulations after minimization. Fig. 2(b) illustrates the structure of the nano-enhanced PCM, which was used in simulations after minimization. Periodic boundary conditions were employed in all three directions. The number of atoms in each simulation system is reported in Table 1.

2.2 MD procedure

A PCFF[‡] force field^{16–19} with a cut-off radius of 10 \AA was used to simulate the octadecane molecules, and an AIREBO potential with a cut-off radius of 8.5 \AA was used to simulate graphene.²⁰ A

[‡] Polymer consistent force field.



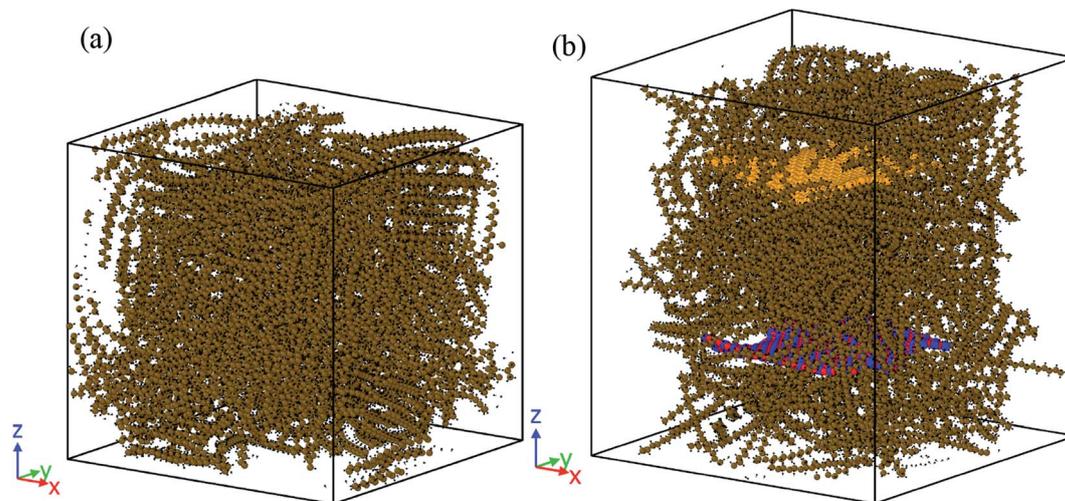


Fig. 2 Structures of: (a) the pure paraffin and (b) nano-enhanced PCM used in the simulations after minimization.

Table 1 Structural parameters of the simulation systems

System	# of atoms in paraffin	# of atoms in graphene	# of atoms in BNNS	# of all atoms
Pure octadecane	28 000	—	—	28 000
Nanocomposite	28 000	576	576	29 152

Tersoff potential^{21,22} developed by Sevik *et al.*^{23,24} was used to characterize the BNNS interactions. The 6–12 Lennard-Jones potential²⁵ was employed in conjunction with the Lorentz–Berthelot mixing rule²⁶ for the van der Waals interaction between the nano-additives and *n*-alkanes. The cut-off radius of LJ was assumed at 10 Å. The time step was set to 0.5 fs in all simulations. To simulate all structures, four steps were applied. The first step was the melting and crystallization cycle to optimize the structures. During 2×10^6 steps, the structures were heated from 260 K to 340 K under an NPT ensemble^{27,28} and atmospheric pressure to completely melt. Then, it was cooled down from 340 K to 260 K under an NPT ensemble for 2×10^6 steps to be solidified. Finally, the optimized structure of each system (pure paraffin or nanocomposite PCM) was extracted.

In the second step, all structures were simulated at 260, 270, 280, 290, 300, 310, 320, 330, and 340 K. The simulation process was such that under the NPT ensemble, all structures were equilibrated for 2×10^6 time steps of the corresponding temperature (at 1 atm). The output of this section led to various energy fluctuation plots and the final density of the system at the desired temperatures. Subsequently, simulations were followed at the desired temperature for 4×10^6 time steps under the NVT ensemble (the third step). The outputs of this step included the MSD (mean square displacement), D (diffusion coefficient), C_v (heat capacity at constant volume), RDF (radial distribution function), and PDOS (phonon density of state) at several temperatures for every two structures.

Lastly, the structures were simulated for 6×10^6 time steps (3 nanoseconds) under the NVE ensemble to account for their

thermal conductivity in the fourth step. The box was divided into several plates along the $X/Y/Z$ direction. Through the simulation box, the heat flux was introduced by adding heat to the molecules inside the heat source (a planar slab) in two regions of the box. The same amount of heat was then extracted from the molecules within another slab (thermal sink) in another region (in the middle of the box). The thermal conductivity of the material in the simulation box (subject to the periodic boundary condition) was calculated after achieving a steady state based on Fourier's law. These simulations were carried out at 280 K (solid-state), 300 K (octadecane melting point) and 320 K (fluid state).

3 Results and discussions

This chapter describes the thermal and structural characteristics of pure paraffin and the nanocomposite, including the heat capacity at constant volume (C_v), mean square displacement (MSD), diffusion coefficient (D), phonon density of state (PDOS), density (ρ), radial distribution function and thermal conductivity (κ). Fig. 3 displays the kinetic and potential energy fluctuations of pure paraffin and the nanocomposite at 300 K. According to Fig. 3, all systems were thoroughly equilibrated.

3.1 Validation

To validate the performed simulations, the density and thermal conductivity obtained for pure octadecane were compared with those of previous works. Since there is no similar study, comparing the outcomes of the current work for the nanocomposite was difficult. The results of this study, as shown in Table 2, aligned well with those outlined in prior works,^{10,29–33} and the simulations conducted in this work could be appropriately validated.

3.2 The latent heat capacity

For paraffin as a PCM, the latent heat is so important. The heat capacity is a very serious and substantial issue, especially at



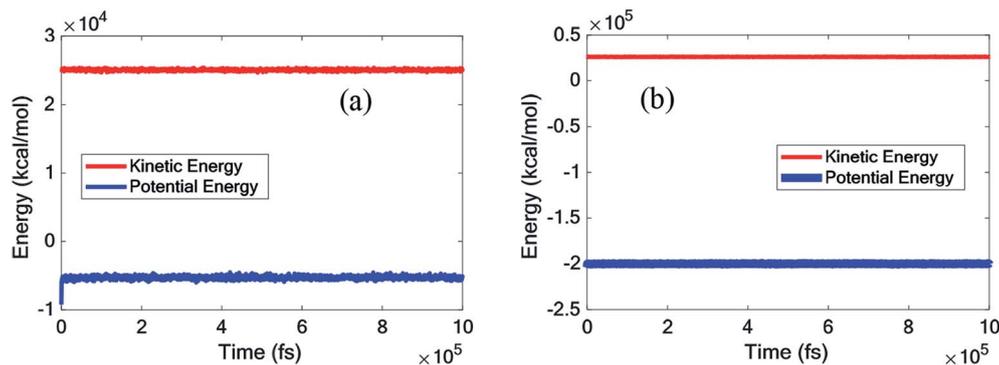


Fig. 3 Kinetic and potential energy fluctuations of (a) the pure octadecane, (b) octadecane–graphene–BNNS nanocomposite under NPT equilibrium at 300 K.

Table 2 Comparing density and thermal conductivity of pure paraffin (octadecane) obtained by the current study with those of previous experimental and computational works

Temperature (K)	Applied method	Density (g cm ⁻³)	Thermal conductivity (W mK ⁻¹)	Reference
280	MD (PCFF)	0.7356	0.1194	Current study
290	MD (PCFF)	0.7303	—	Current study
300	MD (PCFF)	0.7184	0.1227	Current study
310	MD (PCFF)	0.7130	—	Current study
320	MD (PCFF)	0.7024	0.1180	Current study
298.15	MD (COMPASS)	—	0.277–0.303	Liu <i>et al.</i> ²⁹
270	MD (NERD)	—	0.30	Babaei <i>et al.</i> ¹⁰
290	MD (NERD)	0.86	—	Babaei <i>et al.</i> ¹⁰
300	MD (NERD)	—	0.164	Babaei <i>et al.</i> ¹⁰
310	MD (NERD)	0.75	—	Babaei <i>et al.</i> ¹⁰
293–297 (solid phase)	Experimental	0.91	—	Gülseren <i>et al.</i> ³⁰
301–308 (liquid phase)	Experimental	0.778	—	Gülseren <i>et al.</i> ³⁰
300 (liquid phase)	Experimental	—	0.153	Powell <i>et al.</i> ³¹
275 (solid phase)	Experimental	—	0.33	Yarborough <i>et al.</i> ³²
294–300 (solid phase)	Experimental	—	0.1505	Xia <i>et al.</i> ³³

melting temperatures. The thermal capacity was calculated as follows under a constant volume (C_v):

$$C_v = \frac{\langle \delta E^2 \rangle}{k_B T^2} = \frac{\langle E^2 \rangle - \langle E \rangle^2}{k_B T^2} \quad (1)$$

where $\langle E^2 \rangle - \langle E \rangle^2$ is the energy fluctuation, k_B is the Boltzmann constant, and T is the temperature of the system. Fig. 4 illustrates the heat capacity (under constant volume) of pure paraffin and the nanocomposite at a temperature range between 260 K and 340 K. Results showed that the heat capacity decreased with increasing temperature, except in the melting range. It is notable that the nanocomposite with nano-fillers had a greater (or equal) thermal capacity than pure paraffin, except for at the melting point.

3.3 Mean square displacement

The mean square displacement (MSD), which implies a measure of all particles' average range through time, is generally used to define the system conduct during a phase change. eqn (2) was used to calculate the mean square displacement (MSD):

$$\text{MSD} = \frac{1}{N} \langle |r_i(t) - r_i(0)|^2 \rangle \quad (2)$$

where N is the number of atoms and r is the atomic position with angstrom unit. $r_i(t)$ is the i th atom's position at the time step of t . Fig. 5 shows the MSD graphs *versus* time for pure octadecane and the octadecane–graphene–BNNS mixture at temperatures of 260, 270, 280, 290, 300, 310, 320, 330, and 340 K.

Fig. 5(a) demonstrates that by increasing the octadecane temperature, the slope of the MSD diagram increased. It seemed that the slope of the MSD curve for octadecane grew considerably, becoming more steep at temperatures of 300 K and above. According to the experiments, the melting point was 300 K and this finding was quite close to it.³⁰ The curves in Fig. 5(b) describe how MSD changed in the octadecane–graphene–BNNS nanocomposite at different temperatures. The nanocomposite continued to be solid up to 300 K, and then was melted at 310 K. This result confirms that the nano-additives increased the paraffin melting point by approximately 10 K.



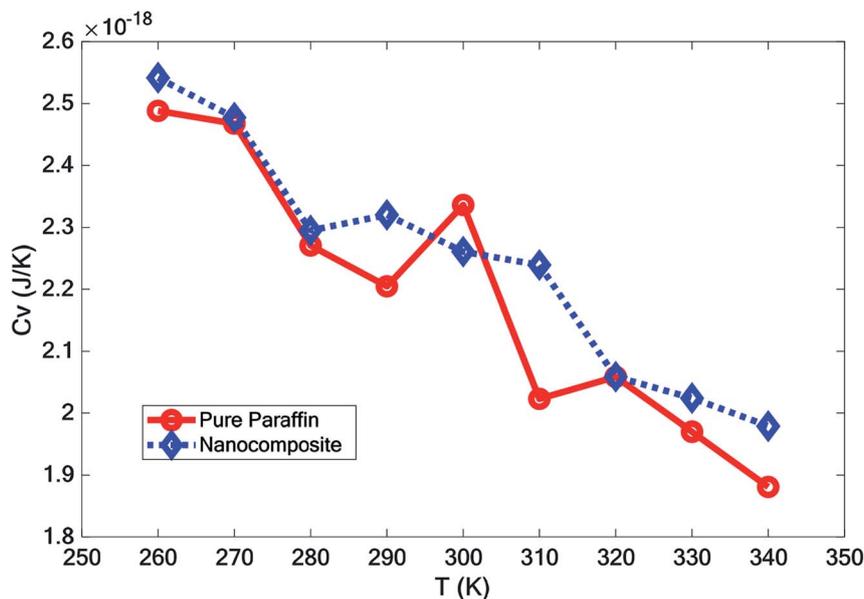


Fig. 4 Heat capacity of pure paraffin and the nanocomposite at different temperatures.

3.4 Diffusion coefficient

According to the Einstein equation,³⁴ the self-diffusion coefficient (D) was calculated as follows:

$$D = \frac{1}{6N} \lim_{t \rightarrow \infty} \frac{d}{dt} \sum_{i=1}^N \langle |r_i(t) - r_i(0)|^2 \rangle \quad (3)$$

where t indicates the simulation time, N is the number of atoms, r_i is the vector of the i th particle position, and the angular brackets are the ensemble's average. The self-diffusion coefficient value was calculated using the slope of the MSD curve. The temperature variation of the diffusion coefficient for two different simulated structures is illustrated in Fig. 6. The diffusion coefficient characterized the degree of mobility and atomic motion. This figure indicates that, with increasing temperature, pure paraffin atoms moved more quickly than the nanocomposite ones. Therefore, the addition of nano-additives caused a decrease in the diffusion coefficient and in the motion of the atoms.

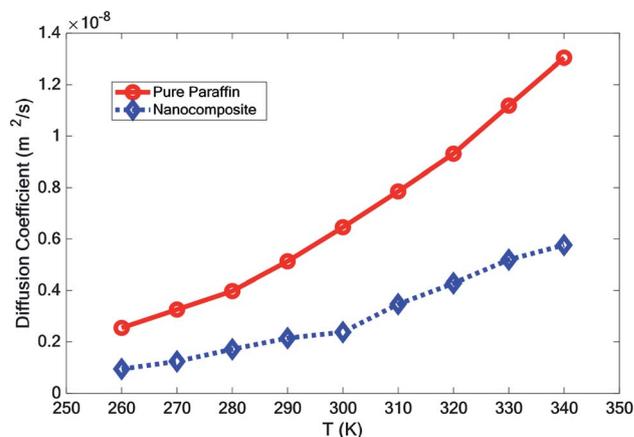


Fig. 6 The diffusion coefficient of simulated structures vs. temperature.

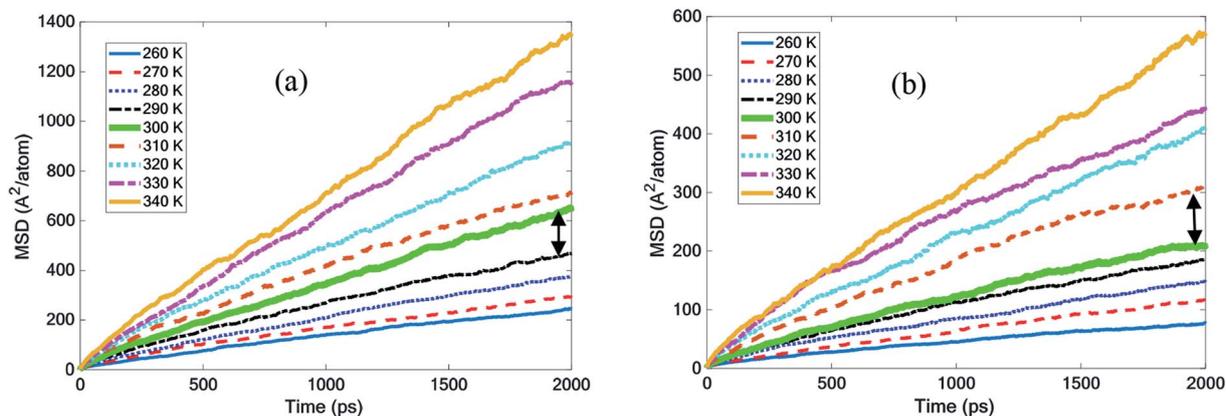


Fig. 5 Mean square displacement with temperature for (a) pure octadecane and (b) the octadecane-graphene-BNNS nanocomposite.



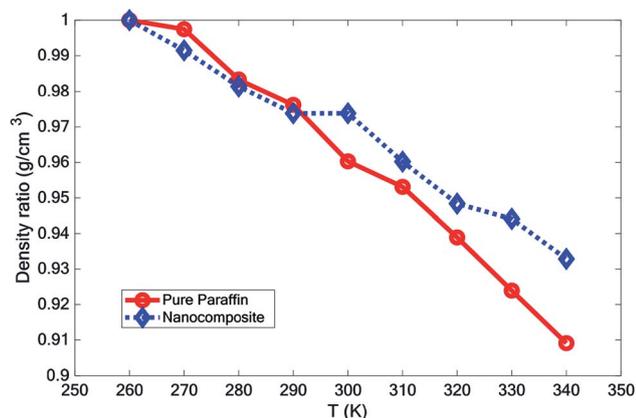


Fig. 7 Variation of the density of the simulated structures vs. temperature.

3.5 Density

The effect of adding nano-additives on the density of paraffin was investigated. Fig. 7 compares the density of the simulated structures at different temperatures. The density ratio was defined as $\frac{\rho}{\rho^*}$, where ρ is density and ρ^* is the density at $T = 260$ K. According to Fig. 7, the density of the systems decreased as the temperature increased. However, the slope of this reduction for the nanocomposite was less than that for pure paraffin. Also, the results showed that the addition of graphene and the boron nitride nanosheet caused an increase in the density of the nano-enhanced PCM.

3.6 Phonon density of state

The phonon density of state (PDOS) was obtained by calculating the Fourier transform of the velocity autocorrelation function (indicated by $\langle \cdot \rangle$) using the following equation:

$$P(\omega) = \sum_i \frac{m_i}{k_B T} \int_0^\infty e^{-i\omega t} \left\langle \vec{v}(0) \cdot \vec{v}(t) \right\rangle_i dt \quad (4)$$

where the summation and integration were run over all atom types i and the simulation time, respectively. Also, the

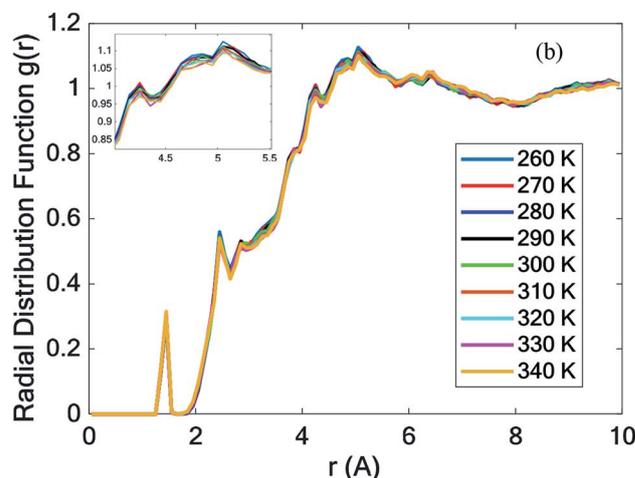
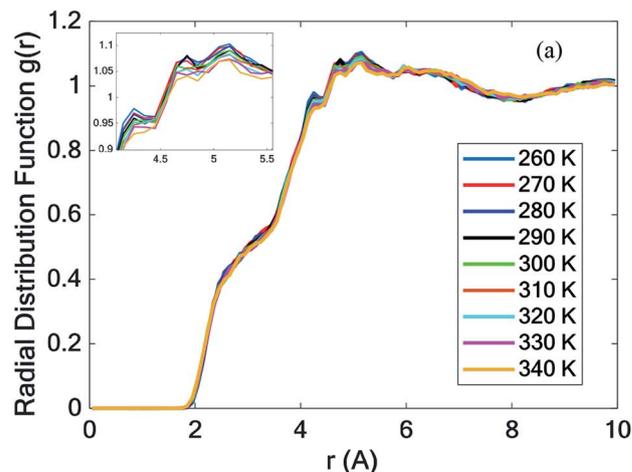
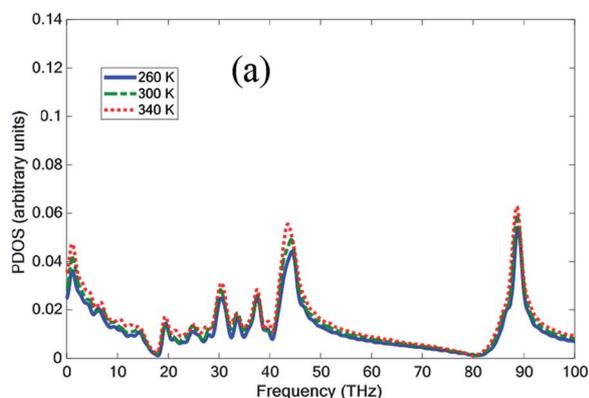


Fig. 9 Total radial distribution function (RDF) of (a) all pure octadecane atoms and (b) all octadecane-graphene-BNNS atoms.

quantities m , \vec{v} , and ω are the mass, velocity, and phonon angular frequency, respectively.

Fig. 8 shows the PDOS for pure paraffin, and the mixture at 260, 300, and 340 K. The PDOS of pure paraffin had some peaks between 20 to 45 THz and in 90 THz, which was inconsistent

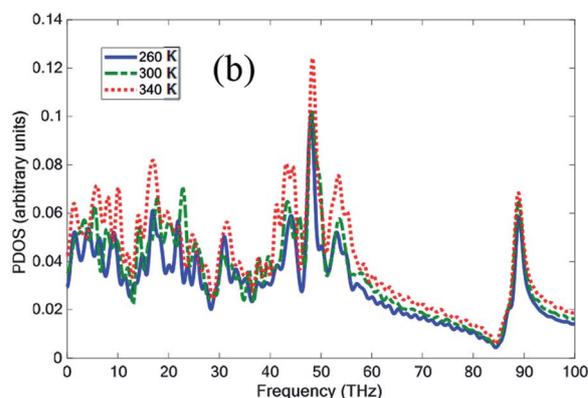


Fig. 8 Phonon density of state (PDOS) of (a) pure paraffin and (b) the nanocomposite at temperatures 260 K, 300 K, and 340 K.



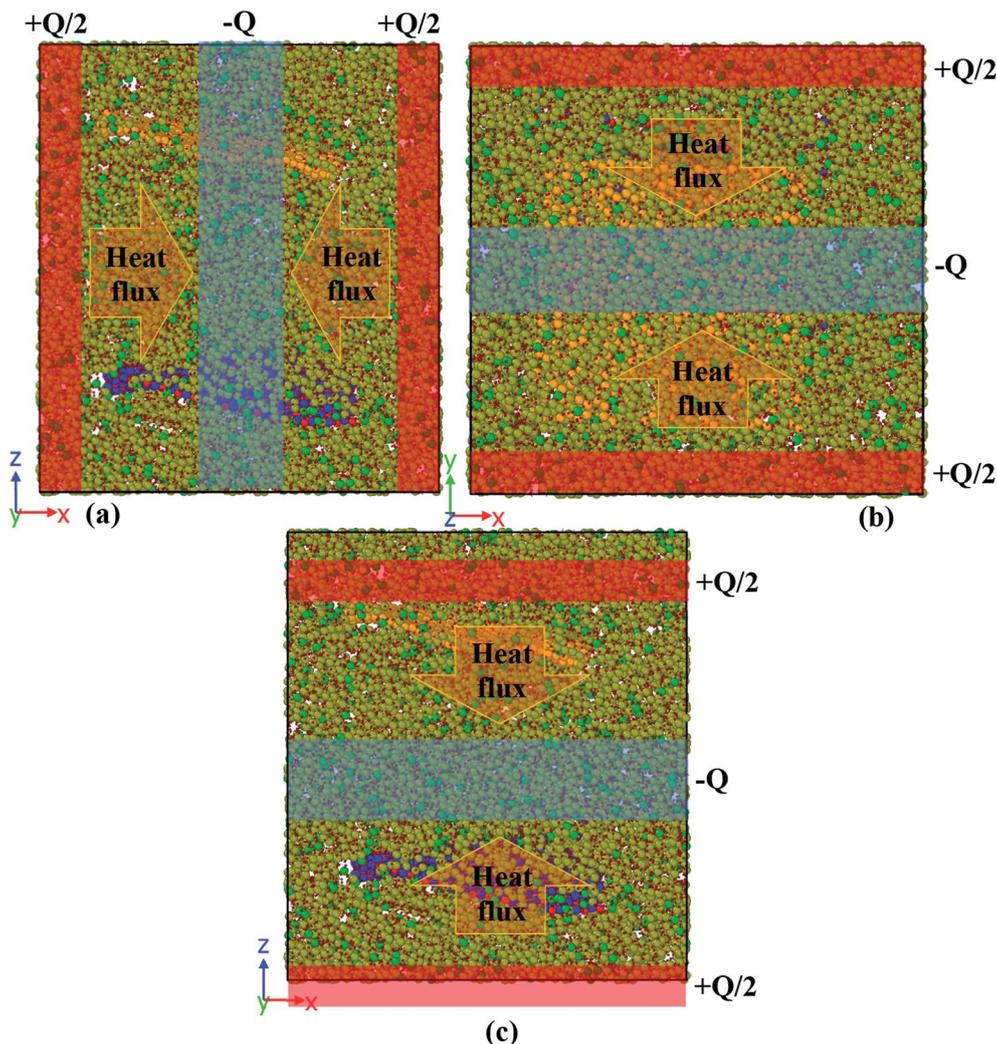


Fig. 10 A schematic diagram of the simulation box for calculating the thermal conductivity in the (a) x-direction, (b) y-direction, and (c) z-direction.

with ref. 35. Another peak for pure paraffin was between 0 to 5 THz. The existence of graphene and BNNS caused higher peaks and troughs, and also caused other new peaks between 0 to 55 THz. With increasing temperature in both pure paraffin and the nanocomposite, the peaks of PDOS also increased.

3.7 Radial distribution function

The radial distribution function is the probability of the presence of particles, which is calculated by assuming the spherical shells around a particle with different radii. RDF counts the

number of atoms around a specific particle in each of these shells. The RDF, represented by the symbol $g_{\alpha\beta}(r)$, as defined by Hansen and McDonald,³⁶ is calculated with eqn (3):

$$x_{\alpha}x_{\beta}\rho g_{\alpha\beta}(r) = \frac{1}{N} \left\langle \sum_{i=1}^{N_{\alpha}} \sum_{j=1}^{N_{\beta}} \delta(r - r_i + r_j) \right\rangle \quad (5)$$

It is a measure of the probability of finding a particle at a distance of r away from a given reference particle. The general algorithm involves determining how many particles are within

Table 3 The thermal conductivity of pure paraffin in the x-, y-, and z-directions at various temperatures

Temperature (K)	k_x (W mK ⁻¹)	k_y (W mK ⁻¹)	k_z (W mK ⁻¹)	k_{mean} (W mK ⁻¹)
280	0.11242	0.11921	0.12659	0.1194
300	0.12277	0.12246	0.12294	0.1227
320	0.11652	0.11681	0.12052	0.1180



Table 4 The thermal conductivity of the nanocomposite in the x -, y -, and z -directions at various temperatures

Temperature (K)	k_x (W mK ⁻¹)	k_y (W mK ⁻¹)	k_z (W mK ⁻¹)	k_{mean} (W mK ⁻¹)	Mean kappa changes compared to pure paraffin
280	0.16054	0.15231	0.12793	0.1469	+23.0%
300	0.16857	0.15731	0.13957	0.1552	+26.5%
320	0.16054	0.16124	0.13026	0.1507	+27.7%

a distance of r and $r + dr$ away from a particle (particle at each bin). N denotes the number of total atoms, N_i represents the number of atoms corresponding to the chemical type i (α and β subscriptions indicate the different types of chemicals), x is the mole fraction of chemical type α and β , and ρ is the density of the atoms.

Fig. 9 depicts the RDF curve of the two structures, pure PCM and nano-enhanced PCM (NEPCM) at different temperatures. This figure illustrates the radial distribution function for all atoms relative to each other. The RDFs displayed relatively isolated peaks at low temperatures. It implies that there were constant distances between the two atoms of interest that were characteristic of a solid-state. On the other hand, they became smoother for liquid materials. The RDF of NEPCM had more peaks than PCM.

3.8 Thermal conductivity

The simulation box was divided into several bins to measure the thermal conductivity in this study. The structure was heated *via* two heat sources at its left and right ends. A heat sink was assumed in the middle of the structure to dissipate the imposed heat and guarantee the equilibrium. Fig. 10 displays a corresponding schematic diagram for calculating the thermal conductivity in the x -, y -, and z -directions by the nonequilibrium molecular dynamics method.

The heat flux Q (0.01 kcal mol⁻¹ fs⁻¹ for pure paraffin and 0.03 kcal mol⁻¹ fs⁻¹ for the nanocomposite) was applied between the heat sources and sinks under the microcanonical ensemble. As the kinetic energy of the atoms of the hot slab increased and the kinetic energy of the atoms of the cold slab decreased, this energy transferred from warmer atoms to colder atoms. Simulations of the thermal conductivity under the microcanonical ensemble for 3 ns (6 million time steps) were performed. Using the temperature output for the atoms of each part of the box along the box length, the temperature-position profile was plotted, and the thermal conductivity was calculated using Fourier's law as follows:

$$k = \frac{\frac{dQ}{dt}}{A \left(\frac{dT}{dx_1} + \frac{dT}{dx_2} \right)} \quad (6)$$

In this equation, $\frac{dQ}{dt}$ is the rate of the heat addition to heat sources or the heat extraction from the heat sink. 'A' is the cross-sectional area of the simulation box perpendicular to the

direction of the imposed heat flux, whereas $\frac{dT}{dx_1}$ and $\frac{dT}{dx_2}$ are the temperature gradients on the linear section of the temperature-position curve for the left section and right section of the curve. This means that the temperature of the hot and cold sections was not included in calculating the temperature gradient. The heat sink was in the middle of the box with a thickness of 2 nm and the heat sources were in the two sides of the box, which were joined together as a union region, with 2 nm thickness. This means the thickness of each hot region was 1 nm.

Fig. S1† illustrates the temperature profiles of the pure octadecane in the x -, y -, and z -directions at 280 K (solid phase). Fig. S2 and S3† show the temperature-position profiles at 300 K (melting point) and 320 K (liquid phase), respectively, in different directions of pure octadecane paraffin. Thermal conductivities of paraffin at various temperatures in the x -, y -, and z -directions were calculated according to the corresponding graphs, and are presented in Table 3. The highest thermal conductivity of paraffin was obtained at the melting point.

Investigating the effects of adding graphene and the boron nitride nanosheet to paraffin and understanding the variation of thermal transport in different temperatures is the purpose of this section. Fig. S4–S6† display the temperature profiles of the octadecane-graphene-BNNS nanocomposite in the x -, y -, and z -directions at different temperatures. The thermal conductivity of the nanocomposite at various temperatures and directions is calculated according to the corresponding graphs, and are presented in Table 4. The nano-additives improve paraffin's thermal conductivity. With increasing temperature, the enhancement of the thermal conductivity increased. This may be because of the higher peaks of the phonon density of state at high temperatures.

According to the results, the maximum thermal conductivity was observed for the nanocomposite at 300 K. In both systems, the highest thermal conductivity occurred at 300 K.

4 Conclusion

In this paper, the effect of adding hybrid nanoparticles, graphene, and BNNS to octadecane and a consideration of its thermal conductivity were studied using molecular dynamics. The paraffin form studied was octadecane (C₁₈H₃₈), with a melting point of approximately 300 K. The effects of different temperatures on the density, melting point, diffusion coefficient, heat capacity, and thermal conductivity were investigated. The measurement of density showed that by adding nano-additives, the density increased. Furthermore, with increasing



temperature, the density decreased. However, the density reduction for the nanocomposite was lower than that for pure paraffin. The mean square displacement of different structures at various temperatures indicated that graphene and the BNNS nano-additives improved the melting point of octadecane by about 10 K.

It was observed that with increasing temperature, the diffusion coefficient also increased. However, the diffusion coefficient of the nanocomposite was lower than that for pure paraffin. Studying the thermal conductivity of different structures revealed that the addition of the nano-additives increased the thermal conductivity of paraffin by about 23.0%, 26.5% and 27.7% at 280 K, 300 K, and 320 K, respectively. By adding the nano-additives, the heat capacity of the phase change material was enhanced at all temperatures, except for at 300 K.

Conflicts of interest

There is no conflict of interest.

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