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Effect of surface oxidation on the electronic transport properties of phosphorene gas sensors: a computational study

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The potential for phosphorene-based devices has been compromised by the material's fast degradation under ambient conditions. Its tendency to fully oxidize under O₂-rich and humid environments, leads to the loss of its appealing semiconducting properties. However, partially-oxidized phosphorene (po-phosphorene), has been demonstrated to remain stable over significantly longer periods of time, thereby enabling its use in sensing applications. Here, we present a computational study of po-phosphorene-based gas sensors, using the Density-Functional-based Tight Binding (DFTB) method. We show that DFTB accurately predicts the bandgap for the pristine material and po-phosphorene, the electronic transport properties of po-phosphorene at different surface oxygen concentrations, and the appropriate trends in Density-of-States (DOS) contributions caused by adsorbed gas molecules, to demonstrate its potential application in the development of gas sensors. Results are compared against the more traditional and expensive Density Functional Theory (DFT) method using generalized gradient approximation (GGA) exchange–correlation functionals, which significantly underestimates the material's bandgap.

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1 Introduction

Sensor approaches based on two-dimensional (2D) hetero-structured materials, such as graphene, phosphorene, transition metal dichalcogenides (TMDs) and others,^{1–3} in conjunction with big data analytics, are expected to enable the real-time detection of adsorbates through differentiable electronic signatures. This is due to their usually high electronic mobility, mechanical rigidity and surface-to-volume ratio, which bring important benefits to the development of nanosensors. Measuring targeted biological markers (biomarkers), such as primary and secondary metabolites, volatile organic compounds (VOCs), and other biomolecules in nano-molar (nM) or pico-molar (pM) concentrations^{4,5} will enable fast, reliable and inexpensive diagnosis and tracking of health in human, animal and plant organisms. The potential for non- or minimally-invasive sensor coupled to mobile platforms for real-time measurements, also offers a unique opportunity within the Internet of Things (IoT) paradigm.

Here, we focus on phosphorene, as a two-dimensional material and allotrope of phosphorus made up of a single layer of black phosphorus. Black phosphorus is a layered material where P atoms covalently bond to 3 adjacent P atoms, forming a wrinkled honeycomb structure that stacks to other

individual layers through van der Waals forces.^{6–8} A single layer is known as phosphorene and has a direct bandgap of ~2 eV, that gradually decreases with increased stacking of layers down to ~0.3 eV in the bulk.^{9–12} Phosphorene is susceptible to mechanical deformation and stacking order,^{13,14} yet it has very high carrier mobility, up to >50 000 cm² V^{–1} s^{–1}.^{15,16}

Several authors have reported theoretical and experimental studies that show phosphorene's interaction with many small molecules, and their effect on its resistance and carrier density capabilities, enables the selective detection and measurement of such molecules.^{5,8,17–30} Recently published reviews associated to advances in the field of 2D materials for sensing applications, provide a clear picture of the opportunities and challenges offered by phosphorene.^{31–34} One of the main problems in its widespread use for sensing applications is its stability under ambient conditions. Phosphorene reacts with water vapor and oxygen assisted by visible light³⁵ to degrade within the scope of hours. One way to control this degradation, is to partially oxidize phosphorene (po-phosphorene). Po-phosphorene has been shown to remain stable in air and moisture, preserving its electronic properties at room temperatures and above,^{36,37} and enabling field-effect transistor (FET) devices with sub-nM concentration capabilities for different analytes (in particular nitrogenated species⁵).

Here, we report on a systematic study of the effects of surface oxidation on the electronic transport properties of phosphorene-based gas sensors. The paper is organized as follows: Section 2 introduces the first-principles based computational methods and procedures used in Section 3 to predict

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the electronic transport properties of pristine and po-phosphorene with different physically-adsorbed molecules, and the sensing capabilities of a po-phosphorene FET sensor device under various oxygen concentrations. Section 4 summarizes the importance and applicability of our results.

2 Methods and procedures

To determine the electronic transport properties of pristine and functionalized phosphorene, from first-principles, we solve the non-relativistic Schrödinger equation³⁸ $i\hbar \frac{\partial \Psi}{\partial t} = \hat{H}\Psi$. Particle wave functions in a periodic potential (Bloch waves) are used as solutions for band structure calculations, as $\Psi_{nk}(r) = e^{ikr}u_n(r)$, where $\psi(r)$ is an eigenfunction of the system and is defined as the product of a plane wave envelope and a periodic Bloch function $u(r)$; n is the band index and k the wave vector associated with the direction of motion of the electron in the crystal, which takes on values within the corresponding Brillouin zone (BZ). Consequently, the band structure is determined by the orbital energies ϵ_{nk} for each band n and momentum k , obtained with the Kohn–Sham approach to density functional theory (DFT).³⁹

Although GW calculations and DFT calculations with hybrid exchange–correlation functionals provide a very accurate band structure prediction of semiconductor materials, these are computationally very expensive or not available in electronic transport packages capable of solving the non-equilibrium Green's functions (NEGF) machinery^{40,41} on two/three-probe systems. Although exchange–correlation functionals within the generalized gradient approximation (GGA) usually underestimate the bandgap of semiconductor materials, we used Perdew–Burke–Ernzerhof (PBE) functionals⁴² as reference. Therefore, geometry optimization and electronic properties calculations were carried out using linear combination of atomic orbitals (LCAO) basis sets, as implemented in the QuantumATK package,^{43–45} where the Kohn–Sham (KS) Hamiltonian is represented in the basis of the PseudoDojo norm-conserving pseudopotentials⁴⁶ on all atoms and PBE parametrization with van der Waals correction,⁴⁷ using a 75 hartree density mesh cut-off, and a 5×10^{-5} self-consistent field (SCF) convergence criteria. A $1 \times 3 \times 3$ k -point mesh was used for the BZ sampling of a rectangular

unit cell consisting of 48 P atoms, and additional O, N, C and Na atoms, as discussed in the following Section. 2 nm of vacuum was added to the directions normal to the transport direction, z , to avoid unrealistic interactions between atoms in neighboring periodic cells. Atoms were allowed to relax until forces converged below $0.05 \text{ eV } \text{\AA}^{-1}$, using the Limited-memory Broyden–Fletcher–Goldfarb–Shanno (LBFGS) method.⁴⁸

To enable faster calculations on the relatively-large atomistic system models involved in this study, we used the Density-functional-based tight binding (DFTB) approximate methods. DFTB has been increasingly used in recent years, for predicting different phosphorene properties.^{30,49–54} Here, we use the third-order parameterization for organic and biological systems (3OB)^{55–57} Slater–Koster parameters to determine the electronic properties of interest, including band-structures and bandgaps. DFTB was coupled to the NEGF machinery, to determine the electronic transport characteristics for the different device configurations, involving pristine and po-phosphorene semiconducting channels in a three-probe, back-gated, field-effect configuration.

3 Results and discussion

3.1 Electronic transport properties of phosphorene with adsorbed molecules

We employed a 3×4 phosphorene surface unit cell as starting point, and characterized the effect on transport properties with different adsorbed organic molecules on it, including CH_4 , CO , CO_2 , HCN , HNC , NH_3 , NO , and NO_2 . Similar configurations have been reported in previous theoretical and experimental publications,^{19–23,29,30} to study the selective detection of such molecules. After minimizing each structure with DFT, we obtained the binding energy of each analyte to phosphorene from $E_b = E_c - (E_p + E_{\text{analyte}})$, where E_b is the binding energy, E_c the complex's total energy, E_p the pristine phosphorene energy, and E_{analyte} the single molecule energy. Then, we computed the system's fat bandstructure (FBS) and projected density of states (PDOS), to determine the contribution of each analyte on phosphorene's electronic properties. We also minimized the structure using the DFTB approximation, and performed FBS and PDOS calculations, to benchmark against DFT results.

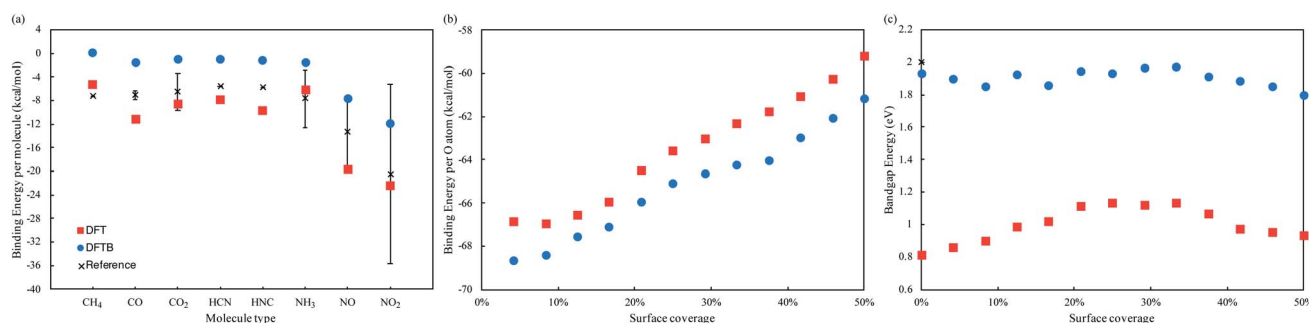


Fig. 1 (a) Binding energy of CH_4 , CO , CO_2 , HCN , HNC , NH_3 , NO , and NO_2 to phosphorene, using DFT and DFTB methods, compared to reference results in ref. 17, 21, 23, 25, 26, 29 and 30. (b) Binding energy per oxygen atom and (c) bandgap energy, as a function of adsorbed oxygen concentrations in the T1 position, using DFT and DFTB methods.

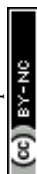


Fig. 1(a) compares the analyte's binding energy to phosphorene, using DFT, DFTB, and existing published data.^{17,21,23,25,26,29,30} As observed by Kou *et al.*,¹⁷ NO and NO₂ molecules consistently have the largest binding energy to pristine phosphorene, implying it is more sensitive to these

molecules. Fig. 2(a–i) depicts the changes in band structure as a function of analyte adsorption, and Fig. 3(a–i) shows the PDOS obtained for each system. NO and NO₂ are the only molecules among the tested gas phase molecules, that exhibit a significant contribution to the system's electronic properties around the

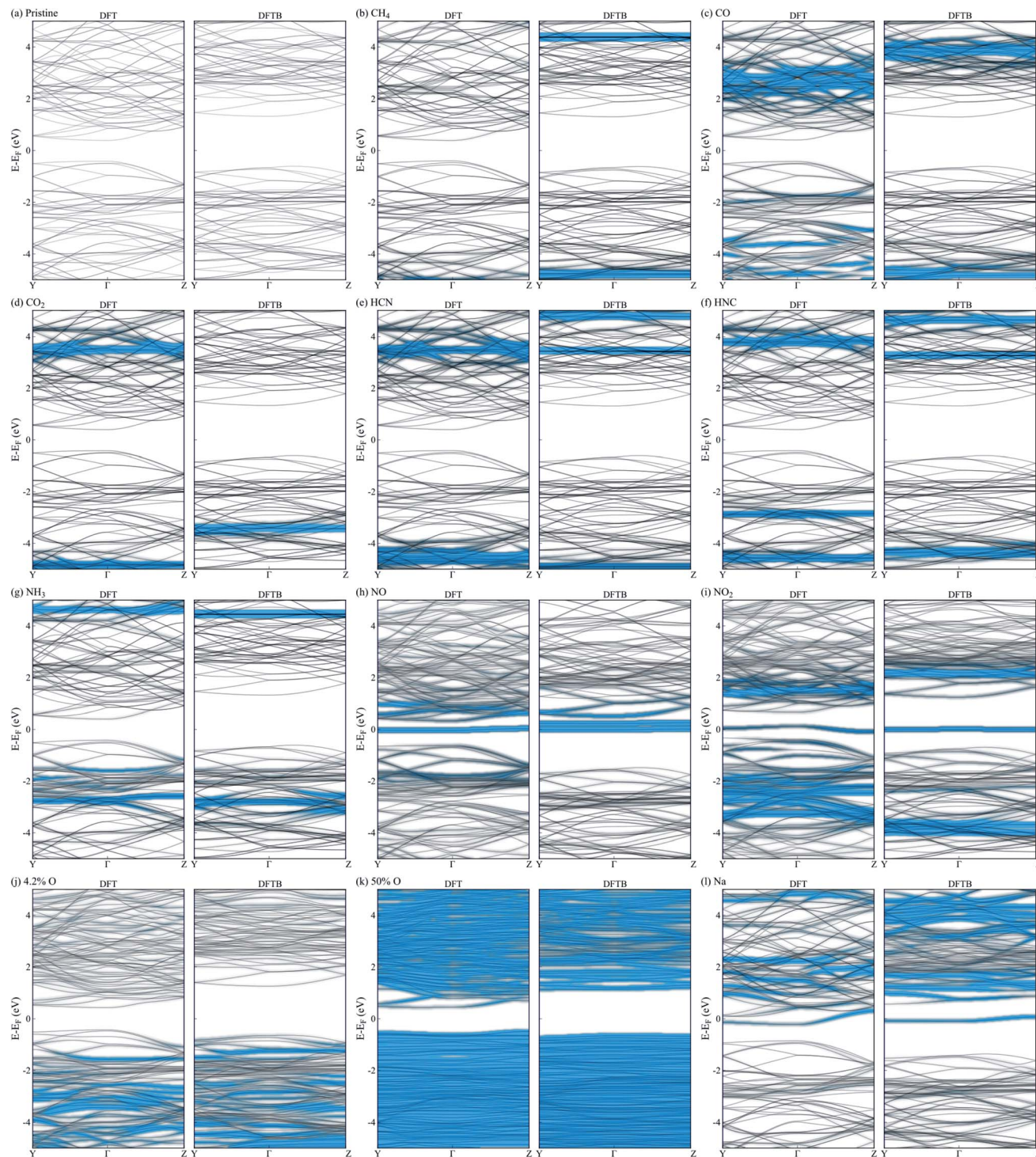


Fig. 2 Fat bandstructure of (a) pristine phosphorene, and phosphorene with adsorbed (b) CH₄, (c) CO, (d) CO₂, (e) HCN, (f) HNC, (g) NH₃, (h) NO, (i) NO₂, (j) 4.2% O, (k) 50% O and (l) Na. Fat bands in blue show the contribution of the adsorbed molecule to the electronic structure of phosphorene.

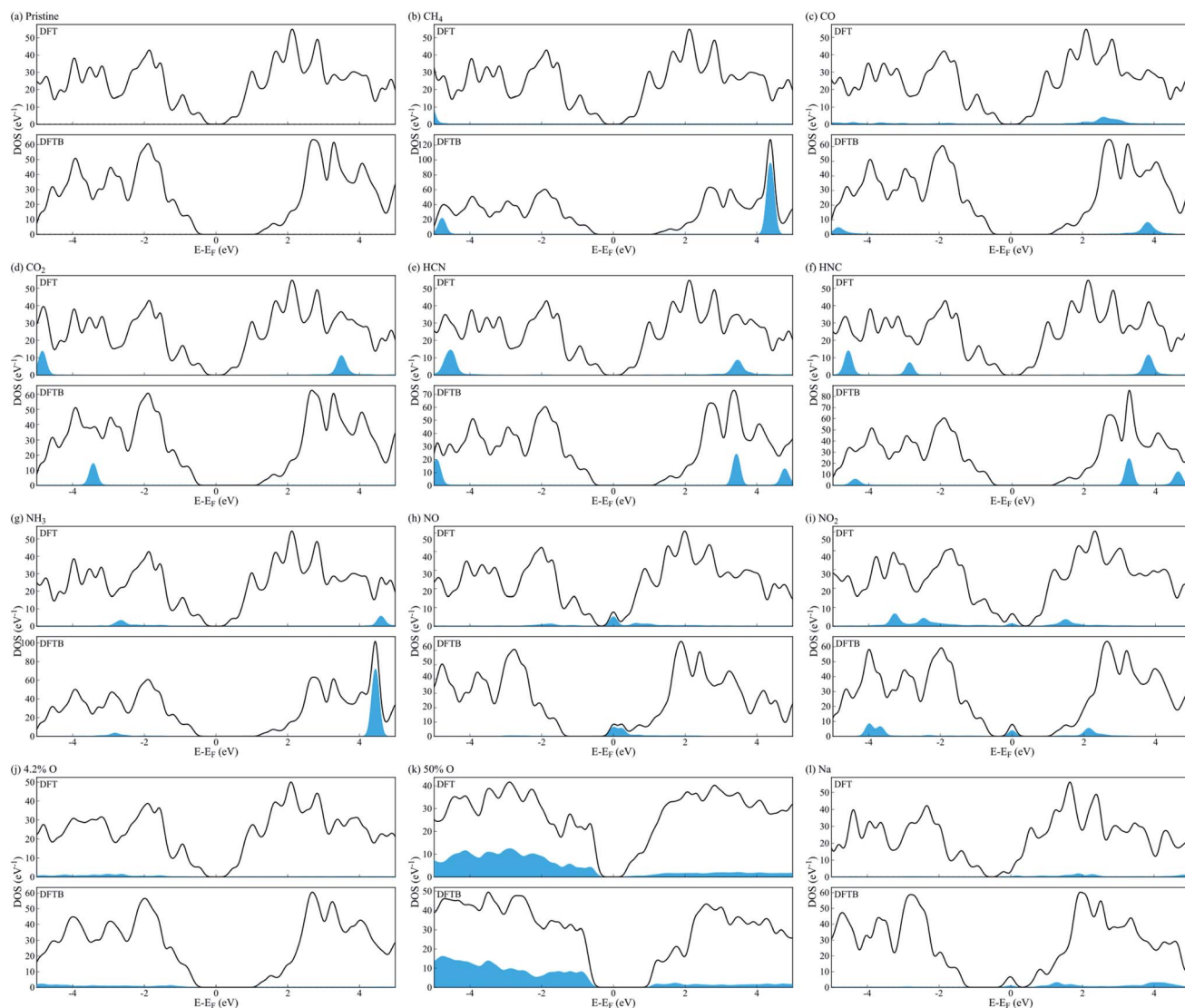


Fig. 3 Projected density of states of (a) pristine phosphorene, and phosphorene with adsorbed (b) CH_4 , (c) CO , (d) CO_2 , (e) HCN , (f) HNC , (g) NH_3 , (h) NO , (i) NO_2 , (j) 4.2% O, (k) 50% O and (l) Na. Blue areas correspond to the contribution of the adsorbed molecule to phosphorene's density of states.

Fermi level. Furthermore, DFT and DFTB results are qualitatively consistent, albeit the evident differences in bandgap values (~ 0.81 eV and ~ 1.93 eV, respectively). Contributions from CH_4 , CO , CO_2 , HCN , HNC and NH_3 molecules are a few eVs from the Fermi level, and have little effect on phosphorene's bandgap and semiconducting properties.

Similar to n-type doping of phosphorene with Cu adatoms,⁵⁸ other atomic dopants, such as Li, Na, Al and Cr, induce metallic behaviour on phosphorene,⁵⁹ and may be useful for avoiding Schottky barriers when contacting phosphorene with conventional metal electrodes.⁶⁰ This is observed in Fig. 2(l) and 3(l), where metalization of phosphorene is achieved *via* doping with Na atoms in the hollow position at a concentration of 5% (1 out of 20 available sites). We chose doping our electrodes with Na atoms in this study, because of the availability of Slater–Koster parameters to computationally characterize the electronic transport properties under a DFTB–NEGF formalism. Na-doping

effectively metalizes phosphorene electrodes without compromising the electronic transport characterization of the proposed device, albeit it is not practical to realize *via* experiments. Cu doping metallization is favored experimentally,⁵⁸ but Cu interaction parameters are not currently available for DFTB, hence our choice of Na.

3.2 Electronic transport properties of po-phosphorene as a function of oxygen concentration

We now consider po-phosphorene with moderate oxygen concentrations, to improve its stability under ambient conditions, and retain its sensing capabilities. As we had reported in ref. 5, oxygen adsorption in the dangling position (top T1 sites), corresponds to the most energetically favorable configuration for low oxygen concentrations. Hence, we started from the optimized pristine phosphorene surface and randomly added



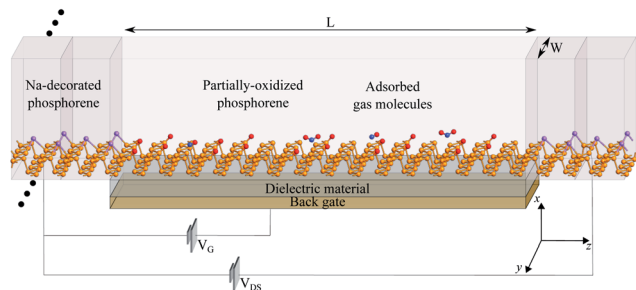


Fig. 4 Isometric view of the po-phosphorene FET sensor. We set $L = 6.5$ nm and $W = 1.345$ nm.

oxygen atoms on T1 sites, from 4.2% up to a 50% surface coverage.

Fig. 1(b) compares the binding energy per oxygen atom for different adsorbed concentrations on T1 positions, using DFT and DFTB. We observe a reduced rate of binding past 25% surface oxygen concentration, which picks up again past 37.5%. Fig. 2(j, k) and 3(j, k) show the calculated FBS and PDOS for the lower and upper limit cases (4.2% and 50% oxygen concentration), where contributions to the system's electronic properties are a few eVs away from the Fermi level; thus, only slight alterations to the bandgap are observed, and semiconducting properties are preserved in all cases. This is summarized in Fig. 1(c), where bandgap estimations are compared as a function of different adsorbed oxygen concentrations in the T1 position, for both DFT and DFTB. As also pointed out in ref. 5 and 61, DFT calculations result in higher bandgap energies at low oxygen concentrations, while indirect bandgap energies on the transport direction z . DFTB calculations, on the other hand, show indirect bandgap energies with very little variations across the range of oxygen concentrations studied here. A fully oxidized phosphorene structure, *i.e.* a phosphorus pentoxide (P_2O_5) monolayer, results in a 11.62 eV direct bandgap (7.45 eV using hybrid functionals⁶²).

We also calculated the binding energy of NO and NO_2 molecules to po-phosphorene, finding that surface adsorption is energetically favorable, at the different adsorbed oxygen

concentrations on T1 sites. Adsorption of NO/ NO_2 species on pristine phosphorene is energetically more favorable (by ~ 8 – 12 kcal mol⁻¹) when compared to adsorption onto available P sites of po-phosphorene, due to redistribution of surface charges caused by the oxygen population. In spite of this, we expect a po-phosphorene-based sensor is able of detecting NO, NO_2 and other gases whose electronic contributions are localized near the Fermi level.

3.3 Device geometry and electronic transport properties as a function of oxygen and adsorbed molecule concentrations

Fig. 4 shows a schematic illustration of the proposed sensor architecture, where Na-doped phosphorene is used for the electrodes (metal-like behavior), and pristine or po-phosphorene for the semiconducting channel. The y direction is assumed to be infinitely periodic, x is finite, and the z transport length (L) is set to 6.5 nm, for a total of 120 T1 surface sites available. The po-phosphorene surface is partially oxidized with 8.3% and 16.7% oxygen concentration on T1 sites, leaving 110 and 100 available sites for analyte adsorption, respectively. A metallic back-gate lays under the semiconducting junction, separated by a dielectric region with a relative dielectric constant set to 3.9 (*i.e.* equivalent to SiO_2).

Fig. 5(a) shows conductance as a function of gate voltage, V_G , with a maximum conductance in the order of tenths of μS . The proposed device is assumed to operate at room temperature 298 K \pm 50 K, hence we confirmed that it exhibits minimal changes in thermionic conductance over the range 250–350 K. Fig. 5(b) shows the IV characteristics for the bare device (*i.e.* no adsorbed gas molecules) with on-state currents of a few tenths of μA , which demonstrates a feasible operation for different V_G values. Fig. 5(c) shows the zero-bias projected (along the conduction direction) local device DOS (LDDOS), which corresponds to the number of allowed electron (or hole) states per volume at a given energy projected in real space, averaged over x and y , and plotted along z as a function of energy. A $V_G = -1.0$ V was chosen to guarantee a fast on-off device transition, as corroborated from the bare IV characteristics in Fig. 5(b). The available states in the semiconducting junction are shifted along the

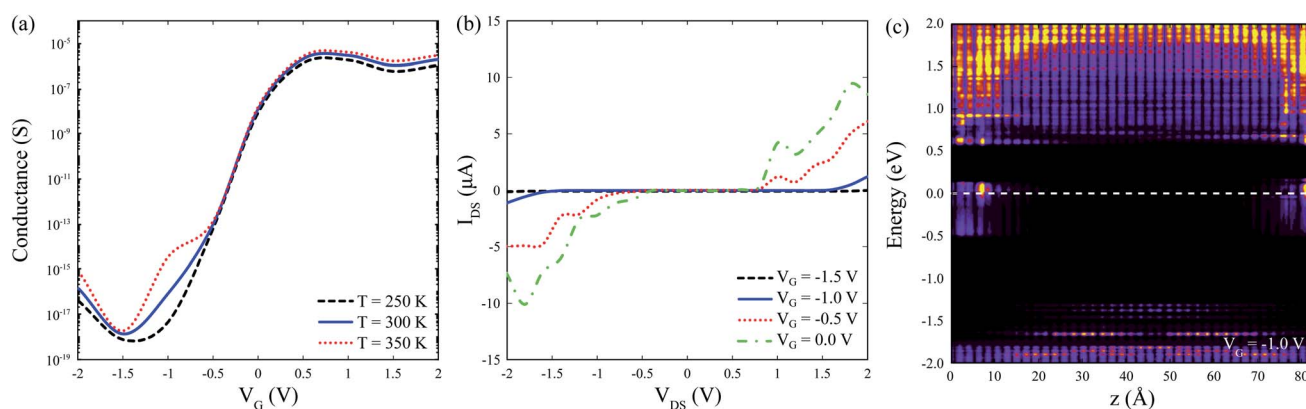


Fig. 5 Electronic transport characteristics for the bare system. (a) Zero-bias conductance as a function of gate voltage, V_G . (b) IV characteristics. (c) Zero-bias device density of states (DDOS) averaged over x and y , plotted along z as a function of energy at $V_G = -1.0$ V.



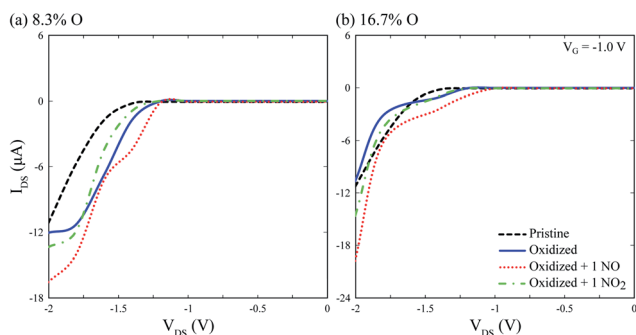


Fig. 6 Current vs. voltage (IV) characteristics for the device at $V_G = -1$ V with (a) 8.3% and (b) 16.7% surface oxidation, with and without physisorbed NO and NO₂ at 0.87% concentration. For comparison, IV characteristics for the bare device are included (black dashed line).

energy axis when applying a gate voltage V_G due to charge injection at the gate electrode.

IV calculations on Fig. 6 show the device is capable of detecting single physisorbed NO and NO₂ molecules on the channel, with differentiable electronic signatures at $V_G = -1$ V and $V_{DS} = -2$ V, disregarding surface oxidation. Although different peak current values are obtained for each oxidation level, NO and NO₂ signals differ by a few μ A, suggesting the need for a precise control of surface oxidation during device fabrication, and most likely a calibration step before usage. Notwithstanding, the device is capable of selectively detecting single NO and NO₂ molecules.

4 Conclusions

Our results demonstrate po-phosphorene can be practically used for gas sensing applications of nitrogen–oxygen moieties. Controlled oxidation of T1 sites on the phosphorene surface, up to 50% coverage, leads to preserved semiconducting properties, and sufficient binding sites for the potential detection of small organic molecules. Particularly, adsorbed molecules whose electronic contribution is located near the systems' Fermi level. We have shown that NO and NO₂ gas molecules bind to po-phosphorene's surface with favorable energy, and that they can be selectively detected by means of a field-effect sensor based on po-phosphorene. Notwithstanding, the high level of control over surface oxidation needed to achieve chemical stability of phosphorene, our IV calculations show that a po-phosphorene based sensor device is capable of single molecule detection with differentiable electronic signature for NO-adsorbed and NO₂-adsorbed molecules at minimum concentration for $V_G = -1$ V and negative V_{DS} . Then, we estimate a 19 nM L^{-1} limit of detection (LOD), assuming a capture gas chamber on top of the semiconducting channel with $8.775 \mu\text{m}^2$ surface area and 10 nm height.

Conflicts of interest

There are no conflicts to declare.

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