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# Tellurium–oxygen group enhanced birefringence in tellurium phosphates: a first-principles investigation†

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Phosphates possess a relatively large UV/DUV cutoff edge, but these compounds usually have very small birefringence. Recently the  $\text{Te}_2\text{P}_2\text{O}_9$  crystal was synthesized and its birefringence was reported to be as large as 0.106 at 1013.98 nm. Herein, we investigated the electronic structure and optical properties of  $\text{Te}_2\text{P}_2\text{O}_9$  using the first-principles method. The obtained results are in good agreement with the experimental values. The Born effective charges and SHG density of  $\text{Te}_2\text{P}_2\text{O}_9$  show that the contribution to the birefringence and SHG response mainly originates from the  $\text{TeO}_5$  group. The electronic structures and optical response of  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$  and  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$  were also investigated for comparison. The results show that these two tellurium phosphates also possess a large birefringence similar to  $\text{Te}_2\text{P}_2\text{O}_9$ . Also, the birefringence originates from the  $\text{TeO}_x$  polyhedrons, which was confirmed by the real-space atom-cutting results and distortion indices.

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## 1. Introduction

Nowadays, nonlinear optical (NLO) materials have attracted widespread attention because they can be used to obtain wide-band and tunable laser sources *via* the second order NLO effect.<sup>1–5</sup> During the past decades, numerous inorganic NLO materials have been obtained, including infrared, visible and ultraviolet (UV) materials.<sup>6–10</sup> Also, borates, phosphates and carbonates are thought to be good candidates for UV/deep-UV NLO compounds, such as BBO,<sup>11,12</sup>  $\text{LiB}_3\text{O}_5$  (LBO),<sup>13–15</sup>  $\text{CsLiB}_6\text{O}_{10}$  (CLBO),<sup>16–18</sup>  $\text{CsB}_3\text{O}_5$  (CBO),<sup>19,20</sup> and  $\text{KBe}_2\text{BO}_3\text{F}_2$  (KBBF).<sup>21–24</sup> It has been proven that the introduction of fluorine into borates is beneficial to obtain short UV cutoff edges and suitable birefringence and large NLO responses,<sup>25,26</sup> and new deep-UV fluoro-borates with good performances were obtained such as  $\text{Li}_2\text{B}_6\text{O}_9\text{F}_2$ ,<sup>25</sup>  $\text{AB}_4\text{O}_6\text{F}$  ( $\text{A} = \text{NH}_4$ , K, Rb, and Cs),<sup>27,28</sup> and  $\text{SrB}_5\text{O}_7\text{F}_3$ .<sup>29</sup>

Recently, phosphates have been reported to be good candidates as UV and deep-UV NLO crystal materials because of their short UV cut-off edge,<sup>30,31</sup> including  $\text{Rb}_2\text{Ba}_3(\text{P}_2\text{O}_7)_3$  (<200 nm),<sup>32</sup>

$\text{Ba}_5\text{P}_6\text{O}_{20}$  (about 167 nm),<sup>33</sup> and  $\text{KLa}(\text{PO}_3)_4$  (162 nm).<sup>34</sup> However, phosphates also have drawbacks. Most of the reported phosphates have a relatively small birefringence, which has relationship with the regular tetrahedron of the  $\text{PO}_4$  units. First principles investigations show that the anisotropic polarization of the regular  $\text{PO}_4$  unit is relatively small. Thus, to overcome this inherent drawback, different types of  $d^0$  transition metal cations ( $\text{Ti}^{4+}$ ,  $\text{Mo}^{6+}$ , *etc.*)<sup>35</sup> and lone pair electrons ( $\text{Bi}^{3+}$ ,  $\text{Te}^{4+}$ ,  $\text{Pb}^{2+}$ , *etc.*) are introduced to phosphates. Wang *et al.* at Shandong University<sup>36</sup> obtained large-size  $\text{Te}_2\text{P}_2\text{O}_9$  crystals *via* the Czochralski method. The crystals had the acentric polar space group  $Cc$ , and their basic building units were the  $\text{PO}_4$  tetrahedron and  $\text{TeO}_5$  square pyramid. Their linear and nonlinear optical properties were also investigated.<sup>36</sup> The SHG response and birefringence of  $\text{Te}_2\text{P}_2\text{O}_9$  are relatively large, which is  $1.3 \times \text{KDP}$ , and 0.13786–0.10615 at 404.66–1013.98 nm, respectively. Curiously, how can it possess such a large birefringence in comparison with other phosphates? Also, what is the origination of this large birefringence in phosphates?

Herein, we calculated the electronic structure and optical properties of  $\text{Te}_2\text{P}_2\text{O}_9$ . The obtained refractive indices, birefringence and SHG tensor agree well with the experimental values. Utilizing its electronic structures, Born effective charges, and the SHG density method, the atomic contribution to the birefringence and SHG tensors of  $\text{Te}_2\text{P}_2\text{O}_9$  are investigated. The results show that the  $\text{TeO}_5$  polyhedrons give the main contribution to the optical anisotropic birefringence and SHG response. Furthermore the optical response of the other tellurium phosphates  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$  (ref. 37) and  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$  (ref. 38) were also investigated for comparison. These two

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compounds possess similar basic building units as  $\text{Te}_2\text{P}_2\text{O}_9$ , which are an isolated  $\text{PO}_4$  tetrahedron and  $\text{TeO}_x$  polyhedrons (more details can be found in Table S1 in the ESI†). These two compounds also have very large birefringence like  $\text{Te}_2\text{P}_2\text{O}_9$ . The large birefringence in these tellurium phosphates originate from the  $\text{TeO}_x$  polyhedrons, which was further confirmed by the real-space atom-cutting results and the distortion indices.

## 2. Computational details

To better understand the relationship between the structure and optical properties, the electronic structure and Born effective charges were investigated using the first-principles method implemented in the CASTEP package.<sup>39,40</sup> During the calculation, the exchange-correlation functional with the Perdew–Burke–Ernzerhof (PBE)<sup>41,42</sup> functional and the norm-conserving pseudopotentials (NCP) was adopted. The kinetic energy cutoffs were set as 830 eV for  $\text{Te}_2\text{P}_2\text{O}_9$ , 830 eV for  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$ , and 830 eV for  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$ . The  $k$ -point mesh in the Monkhorst–Pack was set as  $5 \times 5 \times 3$  ( $\text{Te}_2\text{P}_2\text{O}_9$ ),  $2 \times 3 \times 3$  ( $\text{Te}_3\text{O}_3(\text{PO}_4)_2$ ), and  $4 \times 4 \times 3$  ( $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$ ). After the electronic structures were obtained, the refractive indices and the birefringence were further calculated *via* the OPTADOS code.<sup>43,44</sup> The nonlinear optical tensors of  $\text{Te}_2\text{P}_2\text{O}_9$  were further investigated using the method described in ref. 45–47. For comparison, the electronic structures and optical properties of  $\text{Te}_2\text{P}_2\text{O}_9$  were also investigated using the LDA(CA-PZ), GGA(PW91) and GGA(RPBE) functionals (shown in Table S2 in the ESI†). The results show that the GGA-PBE functional gives more reliable results in comparison with the experimental values. Hence, herein, we only discuss the GGA-PBE results.

## 3. Results and discussions

### 3.1 The electronic structures of $\text{Te}_2\text{P}_2\text{O}_9$

Using the method described above, the band structures and the projected density of states of  $\text{Te}_2\text{P}_2\text{O}_9$  were obtained. It can be seen clearly from Fig. 1 that  $\text{Te}_2\text{P}_2\text{O}_9$  is an indirect bandgap compound with the bandgap of 3.43 eV. The obtained bandgap is smaller than the experimental value (about 4.30 eV).<sup>36</sup> This underestimation of the bandgap may be related with the derivative discontinuity of the exchange-correlation energy.<sup>48</sup>

The projected density of states (PDOS) of  $\text{Te}_2\text{P}_2\text{O}_9$  is shown in Fig. 2. For the  $\text{Te}_2\text{P}_2\text{O}_9$  compound, the states of the valence bands (VB) from  $-10$  eV to the Fermi level are mainly the Te  $\text{sp}$ , P  $\text{sp}$  and O  $\text{sp}$  states. The states at the bottom of the conduction bands (CB) from 3 eV to 6.5 eV are dominated by the Te 5p and O 2p orbitals. From the states at the valence band and the conduction band, the hybrid states of the P–O and Te–O chemical bonds can be determined. According to the revised model,<sup>10,49–53</sup> the lone pair states from the Te–O chemical bond can be deduced. The optical properties of the material are closely related to the electronic transition between the top of the valence band and the bottom of the conduction band. Hence, we believe that the Te–O and P–O chemical bonds play an important role in determining the optical properties of  $\text{Te}_2\text{P}_2\text{O}_9$ .

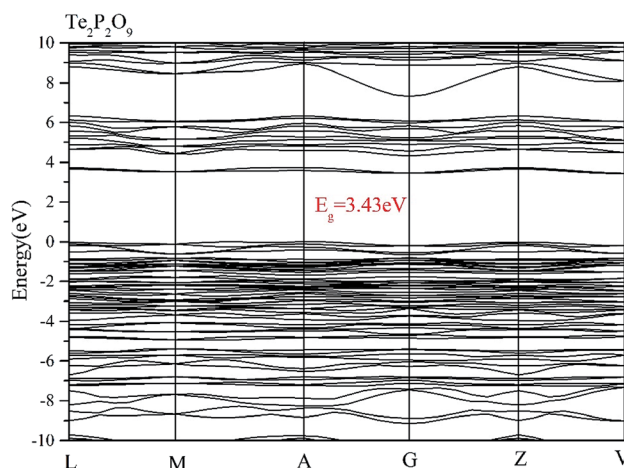


Fig. 1 Obtained band structures of  $\text{Te}_2\text{P}_2\text{O}_9$ .

### 3.2 The refractive indices and Born effective charges of $\text{Te}_2\text{P}_2\text{O}_9$

The obtained refractive indices and birefringence of  $\text{Te}_2\text{P}_2\text{O}_9$  are shown in Fig. 3. From the data shown in Fig. 3, it can be determined that the calculated refractive indices follow the order of  $n_x > n_y > n_z$ . The calculated birefringence is 0.12496–0.09236 in the wavelength range of 404.65–1013.61 nm. It is interesting to note that the reported experimental birefringence of  $\text{Te}_2\text{P}_2\text{O}_9$  is 0.13786–0.10615 in the wavelength range of 404.66–1013.98 nm. Thus, it is obvious that the calculated value matches well with the experimental value.

To better understand the atomic contribution to the optical anisotropic birefringence, the Born effective charges<sup>54–56</sup> were also investigated in this work. Because the optical anisotropic birefringence is closely related with the difference in the macroscopic polarizability along different optical axes, we focused on the anisotropic polarization.<sup>57–59</sup> The Born effective charges are defined as:

$$q_{ij}^{\text{Born}} = \left( \frac{\Omega}{e} \right) \frac{\delta p_i}{\delta d_j}$$

where  $\delta p_i$  is the change in polarization along the displacement direction  $\delta d_j$ . More details can be found elsewhere.<sup>60,61</sup> The obtained Born effective charges are shown in Table 1 and Table S3 in the ESI†. It is interesting to note that unlike  $\text{ABCO}_3\text{F}$  described in ref. 61, which has nondiagonal tensors of atomic Born effective charges of almost zero, nonzero nondiagonal tensors are found in  $\text{Te}_2\text{P}_2\text{O}_9$ . As described in ref. 61, the base unit of  $\text{ABCO}_3\text{F}$  compounds are  $\text{CO}_3$  groups, and the  $\text{CO}_3$  groups are all in a coplanar plane, which makes the nondiagonal tensors of the Born effective charges in these carbonates vanish. In contrast, for the  $\text{Te}_2\text{P}_2\text{O}_9$  compound described herein, it crystallizes in a 3D structure with  $\text{PO}_4$  tetrahedrons and a  $\text{TeO}_5$  square pyramid connected by Te–O and P–O chemical bonds. This complicated 3D structure makes it possess nonzero Born effective charges (shown in Table S3 in ESI†). Specifically, when the  $\text{Te}_2\text{P}_2\text{O}_9$  compound is exposed to an external electric field along the special direction, the electrons move everywhere, not



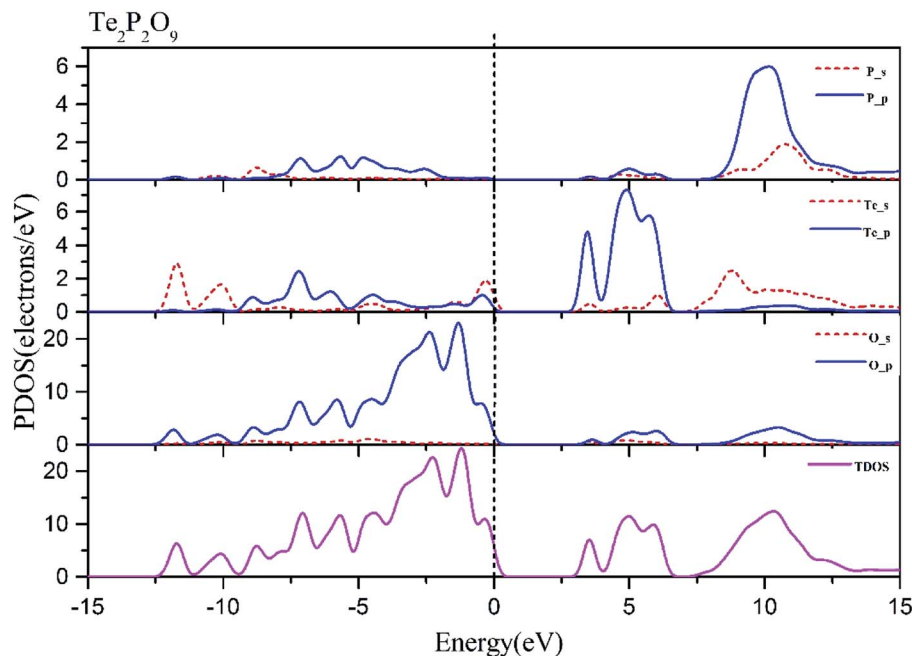


Fig. 2 Projected density of states (PDOS) of  $\text{Te}_2\text{P}_2\text{O}_9$ .

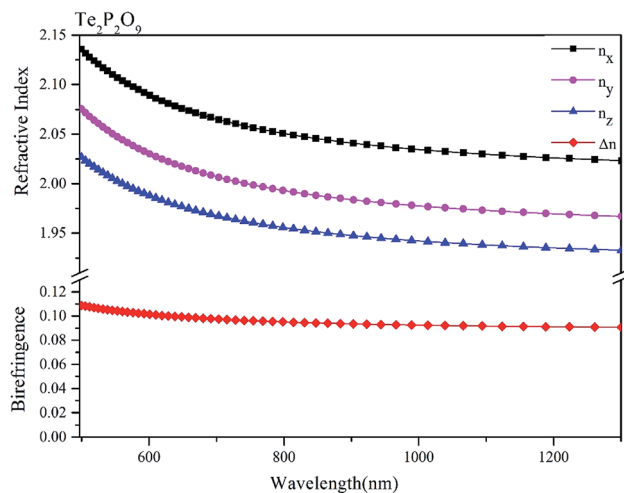


Fig. 3 Calculated refractive indices and birefringence of  $\text{Te}_2\text{P}_2\text{O}_9$ .

only in the direction of the external electric field, but also the vertical direction. Hence, nonzero nondiagonal Born effective charges can be found in  $\text{Te}_2\text{P}_2\text{O}_9$ . Furthermore, we also performed a detailed investigation into the diagonal Born effective charges along the optic principal axis and calculated the difference in the Born effective charges. As described above, the refractive indices follow the sequence of  $n_x > n_y > n_z$ , thus the difference in the Born effective charges was obtained by the  $q_{xx} - q_{zz}$ . The obtained diagonal tensor of the atomic Born effective charges of  $\text{Te}_2\text{P}_2\text{O}_9$ ,  $q_{ij}^{\text{Born}}$  is shown in Table 1. As shown in Table 1, a relatively large difference in the Born effective charge tensors was found in the Te and O atoms, while the P atoms

possess a relative small difference in comparison, implying that the Te and O atoms make a relatively large atomic contribution to the anisotropic birefringence. We believe that the contribution to the birefringence is provided mainly by the  $\text{TeO}_5$  group.

Table 1 Obtained diagonal tensor of the atomic Born effective charges of  $\text{Te}_2\text{P}_2\text{O}_9$

Compound	Atom	$q_{xx}$	$q_{yy}$	$q_{zz}$	$\Delta q^{\text{(Born)}}$
$\text{Te}_2\text{P}_2\text{O}_9$	Te1	4.34265	4.65936	6.63644	−2.29379
	Te2	6.4218	5.38842	3.37218	3.04962
	Te3	4.34265	4.65936	6.63644	−2.29379
	Te4	6.4218	5.38842	3.37218	3.04962
	P1	4.40285	3.49299	4.36297	0.03988
	P2	4.70919	4.86415	3.77507	0.93412
	P3	4.40285	3.49299	4.36297	0.03988
	P4	4.70919	4.86415	3.77507	0.93412
	O1	−1.78151	−1.84853	−2.74356	0.96205
	O2	−3.2844	−2.12701	−1.33367	−1.95073
	O3	−2.85789	−1.94646	−1.32288	−1.53501
	O4	−1.40561	−0.89945	−3.71391	2.3083
	O5	−1.30274	−2.25599	−1.88828	0.58554
	O6	−1.56074	−3.25254	−1.86712	0.30638
	O7	−1.54143	−1.92023	−2.76231	1.22088
	O8	−3.00828	−2.10674	−1.13507	−1.87321
	O9	−3.13389	−2.04796	−1.37986	−1.75403
	O10	−1.78151	−1.84853	−2.74356	0.96205
	O11	−3.2844	−2.12701	−1.33367	−1.95073
	O12	−2.85789	−1.94646	−1.32288	−1.53501
	O13	−1.40561	−0.89945	−3.71391	2.3083
	O14	−1.30274	−2.25599	−1.88828	0.58554
	O15	−1.56074	−3.25254	−1.86712	0.30638
	O16	−1.54143	−1.92023	−2.76231	1.22088
	O17	−3.00828	−2.10674	−1.13507	−1.87321
	O18	−3.13389	−2.04796	−1.37986	−1.75403

**Table 2** The obtained refractive indices and birefringence (at 1064 nm) of  $\text{Te}_2\text{P}_2\text{O}_9$ ,  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$ , and  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$  after real-space atom-cutting was performed

Crystal	Contribution	$n_x$	$n_y$	$n_z$	$\Delta n$
$\text{Te}_2\text{P}_2\text{O}_9$	Cut-PO	1.484	1.458	1.405	0.079
	Cut-TeO	1.232	1.226	1.203	0.029
	Origin	2.031	1.974	1.939	0.092
$\text{Ba}_2\text{TeO}(\text{PO}_4)_2$	Cut-BaO	1.408	1.332	1.323	0.085
	Cut-PO	1.555	1.486	1.475	0.080
	Cut-TeO	1.600	1.588	1.563	0.037
$\text{Te}_3\text{O}_3(\text{PO}_4)_2$	Origin	1.877	1.860	1.767	0.110
	Cut-PO	1.622	1.585	1.570	0.052
	Cut-TeO	1.243	1.229	1.211	0.032
	Origin	2.027	1.998	1.906	0.121

**Table 3** The obtained distortion indices of the different polyhedrons in  $\text{Te}_2\text{P}_2\text{O}_9$ ,  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$ , and  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$

	$\text{Te}_2\text{P}_2\text{O}_9$	$\text{Ba}_2\text{TeO}(\text{PO}_4)_2$	$\text{Te}_3\text{O}_3(\text{PO}_4)_2$
$\text{PO}_4$	0.005	0.020	0.013
$\text{TeO}_x$	0.034	0.039	0.051
$\text{BaO}_x$		0.034	

### 3.3 The contribution from $\text{TeO}_x$ polyhedrons in tellurium phosphate

To better understand the contribution from the  $\text{TeO}_x$  polyhedrons to the birefringence, the electronic structures and the optical response of the other tellurium phosphates  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$  and  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$  were also investigated. The obtained band structures and projected density of states (PDOS) of  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$  and  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$  are shown in Fig. S1–S4 in the ESI.† As shown in Fig. S1 and S3,† the obtained bandgap of  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$  and  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$  are 4.11 and 3.63 eV, respectively. To overcome the underestimation of the bandgap, HSE06 calculations<sup>62</sup> were performed using the PWmat code.<sup>63,64</sup> The obtained HSE06 bandgap of  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$  and  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$  is 4.47, and 4.18 eV, respectively. As shown in Fig. S2 and S4,† the states at the top of the valence band and at the bottom of the conduction band are mainly the Te-sp states, O-sp states, and P-sp states. Also, the chemical bonds of Te–O and P–O can also be found at the top of the valence band. Hence, it can be deduced that the  $\text{TeO}_x$  polyhedron and  $\text{PO}_4$  tetrahedron may play an important role in determining the optical response of these tellurite phosphates.

The refractive indices and birefringence of  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$  and  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$  were also obtained using the method described above, and the results are shown in Fig. S5 and S6,† respectively, and Table 2. As shown in Fig. S5 and S6,† the  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$  and

$\text{Te}_3\text{O}_3(\text{PO}_4)_2$  possess a relatively large birefringence of 0.110 and 0.121 (at 1064 nm), respectively. The birefringence of these compounds follow the sequence of  $\Delta n(\text{Te}_3\text{O}_3(\text{PO}_4)_2) > \Delta n(\text{Ba}_2\text{TeO}(\text{PO}_4)_2) > \Delta n(\text{Te}_2\text{P}_2\text{O}_9)$ .

The contribution from different polyhedrons was further investigated using the real-space atom-cutting method.<sup>45</sup> During the calculation, the atom-cutting radius of O, P, Te, and Ba was set as 1.10, 0.95, 0.96, and 1.74 Å, respectively. After the real-space atom-cutting method was performed, the refractive indices and birefringence of  $\text{Te}_2\text{P}_2\text{O}_9$ ,  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$ , and  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$  were obtained, which are shown in Table 2, and Fig. S7–S9 in the ESI,† respectively. As shown in Table 2, in comparison with the  $\text{PO}_4$  tetrahedron and  $\text{BaO}_x$  polyhedrons, the  $\text{TeO}_x$  polyhedrons give the main contribution to the total birefringence. Taking  $\text{Te}_2\text{P}_2\text{O}_9$  as example, the its birefringence is about 0.092 at 1064 nm. However, after the  $\text{TeO}_5$  polyhedron was removed, the obtained birefringence of the other part (marked as cut-TeO) is only about 0.029, implying that the  $\text{TeO}_5$  polyhedron may give a contribution of about  $(0.092 - 0.029 = 0.063)$  to the total birefringence of  $\text{Te}_2\text{P}_2\text{O}_9$ . Thus, in comparison with the  $\text{PO}_4$  tetrahedron, the  $\text{TeO}_5$  polyhedron gives main contribution to the total birefringence. A similar conclusion was also found for the other tellurium phosphates,  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$  and  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$  (as shown in Table 2). It is interesting to note that the conclusion obtained from the real-space atom-cutting is consistent with the results obtained from the Born-effective charges analysis (as described above).

The optical anisotropic birefringence is related with the anisotropic optical response from the different polyhedrons. The relatively small anisotropic polarization of the regular  $\text{PO}_4$  unit may be related with the relatively small distortion with the regular  $\text{PO}_4$  unit. Herein, the distortion indices of the different polyhedrons in these tellurium phosphates were also investigated. The distortion indices, defined by Baur as  $D = \frac{1}{n} \sum_{i=1}^n \frac{|l_i - l_{av}|}{l_{av}}$ ,<sup>65</sup> was calculated using the VESTA software.<sup>66</sup> The obtained distortion indices of the different polyhedrons in these tellurium phosphates are shown in Table 3. As described above, the  $\text{TeO}_x$  polyhedrons give the main contribution to the total birefringence, and hence was focused on the distortion indices of the  $\text{TeO}_x$  polyhedron. As shown in Table 3, the distortion indices of the  $\text{TeO}_x$  polyhedrons follow the sequence of  $D(\text{Te}_3\text{O}_3(\text{PO}_4)_2) > D(\text{Ba}_2\text{TeO}(\text{PO}_4)_2) > D(\text{Te}_2\text{P}_2\text{O}_9)$ , which is consistent with the sequence of the birefringence of  $\Delta n(\text{Te}_3\text{O}_3(\text{PO}_4)_2) > \Delta n(\text{Ba}_2\text{TeO}(\text{PO}_4)_2) > \Delta n(\text{Te}_2\text{P}_2\text{O}_9)$ .

### 3.4 The atomic contribution to the SHG response of $\text{Te}_2\text{P}_2\text{O}_9$

The SHG tensors of  $\text{Te}_2\text{P}_2\text{O}_9$  were also obtained (shown in Table 4). For that crystallized in the  $Cc$  space group, there are six independent nonzero SHG tensors,  $d_{11}$ ,  $d_{12}$ ,  $d_{13}$ ,  $d_{15}$ ,  $d_{24}$  and  $d_{33}$ .

**Table 4** The calculated SHG tensors and experimental powder SHG (PSHG) intensity

Crystal	Space group	Calculated SHG tensors ( $\text{pm V}^{-1}$ )	PSHG intensity
$\text{Te}_2\text{P}_2\text{O}_9$	$Cc$	$d_{11} = -0.17$ , $d_{15} = -0.53$ , $d_{12} = 0.59$ , $d_{13} = -0.56$ , $d_{24} = -0.95$ , $d_{33} = 1.01$	$1.3 \times \text{KDP}$





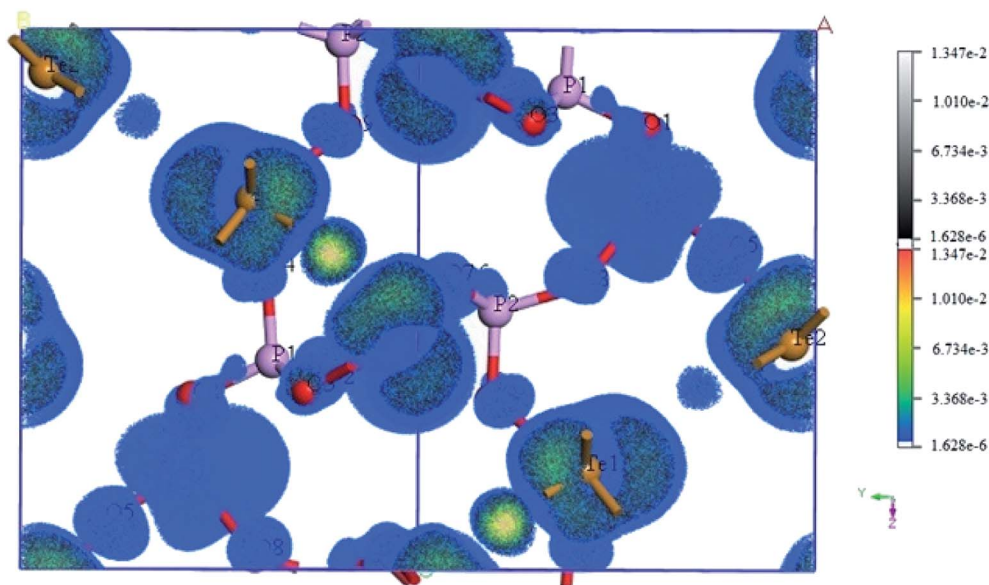


Fig. 4 The obtained SHG density of  $\text{Te}_2\text{P}_2\text{O}_9$ . Note that the brown, pink, and red atoms are Te, P, and O atoms; and the color and black–white clouds are the veocc and vhnocc SHG densities, respectively.

As shown in Table 4, for  $\text{Te}_2\text{P}_2\text{O}_9$ , the maximum is  $d_{33} = 1.01 \text{ pm V}^{-1}$ , which is about 2.6 times that of  $d_{36}(\text{KDP})$ . The obtained SHG tensors are comparable with the experimental powder second-harmonic generation (PSHG) intensity (about  $1.3 \times \text{KDP}$ ). The experimental values agree well with the calculated values, indicating that the method selected in this work is appropriate. To deeply investigate the atomic contribution to the SHG tensors, the spatial distribution of the atomic SHG density was also calculated. The SHG density method is a normalized weighting coefficient *via* the use of the effective SHG response of each occupied and unoccupied band.<sup>59,60</sup> Using this method, the states irrelevant to the SHG response will not be shown, and the distribution of the SHG density represents the origin of the SHG response. Herein, we only show the SHG density obtained from the virtual electron process (labeled as veocc) and the virtual hole process (labeled as vhnocc). The obtained SHG density of  $\text{Te}_2\text{P}_2\text{O}_9$  is shown in Fig. 4, where the color part and white–black part represent the SHG density of the veocc and vhnocc process, respectively. As shown in Fig. 4, there is no SHG distribution around the P atoms, implying that the P atoms give a relatively small contribution to the total SHG response. It is shown that the SHG density is distributed mainly on the Te and O atoms, indicating that the  $\text{TeO}_5$  polyhedrons give the main contribution to the total SHG response.

## 4. Conclusions

In this work, the refractive indices, birefringence, and the SHG coefficient of  $\text{Te}_2\text{P}_2\text{O}_9$  were obtained using the first-principles method. The obtained results are in good agreement with the experimental values. The calculated birefringence of  $\text{Te}_2\text{P}_2\text{O}_9$  is 0.12496–0.09236 in the wavelength range of 404.65–1013.61 nm. The maximum SHG tensor  $d_{33}$  is  $1.01 \text{ pm V}^{-1}$ , which is about

2.6 times that of  $d_{36}(\text{KDP})$ . The atomic contribution to the birefringence and SHG response was also investigated using the projected density of states, Born effective charges, and real-space SHG density method. The results show that the  $\text{TeO}_5$  groups play an important role in determining the birefringence and SHG response of  $\text{Te}_2\text{P}_2\text{O}_9$ . The electronic structures and optical response of  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$  and  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$  were also investigated for comparison. The results show these two tellurium phosphates also possess a large birefringence like  $\text{Te}_2\text{P}_2\text{O}_9$ . Also, the birefringence originates from the  $\text{TeO}_x$  polyhedrons, which was confirmed by the real-space atom-cutting results and distortion indices.

## Conflicts of interest

There are no conflicts to declare.

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## References

- 1 C. T. Chen, G. L. Wang, X. Y. Wang and Z. Y. Xu, Deep-UV nonlinear optical crystal  $\text{KBe}_2\text{BO}_3\text{F}_2$  – discovery, growth,



- optical properties and applications, *Appl. Phys. B*, 2009, **97**, 9–25.
- 2 Y. Ning, C. Tu, X. Long and M. Hong, Recent Advances in Crystal Growth in China: Laser, Nonlinear Optical, and Ferroelectric Crystals, *Cryst. Growth Des.*, 2010, **10**, 4672–4681.
  - 3 W. Zhang, H. Yu, H. Wu and P. S. Halasyamani, Phase-Matching in Nonlinear Optical Compounds: A Materials Perspective, *Chem. Mater.*, 2017, **29**, 2655–2668.
  - 4 Z. Hu, T. Higashiyama, M. Yoshimura, Y. Yap, Y. Mori and T. Sasaki, A New Nonlinear Optical Borate Crystal  $K_2Al_2B_2O_7$  (KAB), *Jpn. J. Appl. Phys.*, 1998, **37**, L1093–L1094.
  - 5 H. P. Wu, H. W. Yu, Z. H. Yang, X. L. Hou, S. L. Pan, X. Su, K. R. Poeppelmeier and J. M. Rondinelli, Designing a deep ultraviolet nonlinear optical material with large second harmonic generation response, *J. Am. Chem. Soc.*, 2013, **135**, 4215–4219.
  - 6 X. L. Chen, B. B. Zhang, F. F. Zhang, Y. Wang, M. Zhang, Z. H. Yang, K. R. Poeppelmeier and S. L. Pan, Designing an excellent deep-ultraviolet birefringent material for light polarization, *J. Am. Chem. Soc.*, 2018, **140**, 16311–16319.
  - 7 Y. Wang, B. Zhang, Z. Yang and S. Pan, Cation-Tuned Synthesis of Fluorooxoborates: Approaching the Optimal Deep-Ultraviolet Nonlinear Optical Materials, *Angew. Chem., Int. Ed.*, 2018, **57**, 2150–2154.
  - 8 G. Q. Shi, Y. Wang, F. F. Zhan, B. B. Zhang, R. H. Yang, X. L. Hou, S. L. Pan and K. R. Poeppelmeier, Finding the Next Deep-Ultraviolet Nonlinear Optical Material:  $NH_4B_4O_6F$ , *J. Am. Chem. Soc.*, 2017, **139**, 10645–10648.
  - 9 B. H. Lei, Z. Yang and S. Pan, Enhancing optical anisotropy of crystals by optimizing bonding electron distribution in anionic groups, *Chem. Commun.*, 2017, **53**, 2818–2821.
  - 10 X. Dong, Q. Jing, Y. Shi, Z. Yang, S. Pan, K. R. Poeppelmeier, J. Young and J. M. Rondinelli,  $Pb_2Ba_3(BO_3)_3Cl$ : A Material with Large SHG Enhancement Activated by Pb-Chelated  $BO_3$  Groups, *J. Am. Chem. Soc.*, 2015, **137**, 9417–9422.
  - 11 G. Qu, Z. Hu, Y. Wang, Q. Yang and L. Tong, Synthesis of Optical-Quality Single-Crystal  $\beta$ - $BaB_2O_4$  Microwires and Nanowires, *Adv. Funct. Mater.*, 2013, **23**, 1232–1237.
  - 12 Y. Xu, W. Y. Ching and R. H. French, Electronic structure and interatomic bonding of crystalline  $\beta$ - $BaB_2O_4$  with comparison to  $LiB_3O_5$ , *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1993, **48**, 17695–17702.
  - 13 C. Chen, Y. Wu, A. Jiang, B. Wu, G. You, R. Li and S. Lin, New nonlinear-optical crystal:  $LiB_3O_5$ , *J. Opt. Soc. Am. B*, 1989, **6**, 616–621.
  - 14 A. Borsutzky, R. Brünner, C. Huang and R. Wallenstein, Harmonic and sum-frequency generation of pulsed laser radiation in BBO, LBO, and KD\*P, *Appl. Phys. B: Photophys. Laser Chem.*, 1991, **52**, 55–62.
  - 15 Q. H. Xue, Q. Zheng, Y. K. Bu, F. Q. Jia and L. S. Qian, High-power efficient diode-pumped Nd :  $YVO_4/LiB_3O_5$  457 nm blue laser with 4.6 W of output power, *Opt. Lett.*, 2006, **31**, 1070–1072.
  - 16 J. Sakuma, Y. Asakawa and M. Obara, Generation of 5-W deep-UV continuous-wave radiation at 266 nm by an external cavity with a  $CsLiB_6O_{10}$  crystal, *Opt. Lett.*, 2004, **29**, 92–94.
  - 17 N. Umemura and K. Kato, Ultraviolet generation tunable to 0.185 microm in  $CsLiB_6O_{10}$ , *Appl. Opt.*, 1997, **36**, 6794–6796.
  - 18 D. Xue, K. Betzler and H. Hesse, Chemical-bond analysis of the nonlinear optical properties of the borate crystals  $LiB_3O_5$ ,  $CsLiB_6O_{10}$ , and  $CsB_3O_5$ , *Appl. Phys. A: Mater. Sci. Process.*, 2002, **74**, 779–782.
  - 19 Y. Wu, *et al.*,  $CsB_3O_5$ : A new nonlinear optical crystal, *Appl. Phys. Lett.*, 1993, **62**, 2614–2615.
  - 20 H. Kitano, *et al.*, Efficient 355-nm generation in  $CsB_3O_5$  crystal, *Opt. Lett.*, 2003, **28**, 263–265.
  - 21 C. Chen, Z. Xu, D. Deng, J. Zhang, G. Wong, B. Wu, N. Ye and D. Tang, The vacuum ultraviolet phase matching characteristics of nonlinear optical  $KBe_2BO_3F_2$  crystal, *Appl. Phys. Lett.*, 1998, **68**, 2930–2932.
  - 22 C. Chen, J. Lu, G. Wang, Z. Xu, J. Wang, C. Zhang and Y. Liu, Deep Ultraviolet Harmonic Generation with  $KBe_2BO_3F_2$  Crystal, *Chin. Phys. Lett.*, 2001, **18**, 1081.
  - 23 C. Chen, J. Lu, T. Togashi, T. Suganuma, T. Sekikawa, S. Watanabe, Z. Y. Xu and J. Wang, Second-harmonic generation from a  $KBe_2BO_3F_2$  crystal in the deep ultraviolet, *Opt. Lett.*, 2002, **27**, 637–639.
  - 24 T. Togashi, T. Kanai, T. Sekikawa, S. Watanabe, C. Chen, C. Zhang, Z. Xu and J. Wang, Generation of vacuum-ultraviolet light by an optically contacted, prism-coupled  $KBe_2BO_3F_2$  crystal, *Opt. Lett.*, 2003, **28**, 254.
  - 25 B. B. Zhang, G. Q. Shi, Z. H. Yang, F. F. Zhang and S. L. Pan, Fluorooxoborates: Beryllium-Free Deep-Ultraviolet Nonlinear Optical Materials without Layered Growth, *Angew. Chem., Int. Ed.*, 2017, **56**, 3916–3919.
  - 26 Z. Yang, B.-H. Lei, W. Zhang and S. Pan, Module-Analysis-Assisted Design of Deep Ultraviolet Fluorooxoborates with Extremely Large Gap and High Structural Stability, *Chem. Mater.*, 2019, **31**, 2807–2813.
  - 27 X. Wang, Y. Wang, B. Zhang, F. Zhang, Z. Yang and S. Pan,  $CsB_4O_6F$ : A Congruent-Melting Deep-Ultraviolet Nonlinear Optical Material by Combining Superior Functional Units, *Angew. Chem., Int. Ed.*, 2017, **56**, 14119–14123.
  - 28 Z. Zhang, Y. Wang, B. Zhang, Z. Yang and S. Pan, Polar Fluorooxoborate,  $NaB_4O_6F$ : A Promising Material for Ionic Conduction and Nonlinear Optics, *Angew. Chem., Int. Ed.*, 2018, **57**, 6577–6581.
  - 29 M. Mutailipu, M. Zhang, B. Zhang, L. Wang, Z. Yang, X. Zhou and S. Pan,  $SrB_5O_7F_3$  Functionalized with  $[B_5O_9F_3]^{6-}$  Chromophores: Accelerating the Rational Design of Deep-ultraviolet Nonlinear Optical Materials, *Angew. Chem., Int. Ed.*, 2018, **57**, 6095–6099.
  - 30 Y. Shen, S. Zhao, B. Zhao, C. Ji, L. Li, Z. Sun, M. Hong and J. Luo, Strong Nonlinear-Optical Response in the Pyrophosphate  $CsLiCdP_2O_7$  with a Short Cutoff Edge, *Inorg. Chem.*, 2016, **55**, 11626–11629.
  - 31 M. Abudourehman, S. Han, B. Lei, Z. Yang, X. Long and S. Pan,  $KPb_2(PO_3)_5$ : a novel nonlinear optical lead polyphosphate with a short deep-UV cutoff edge, *J. Mater. Chem. C*, 2016, **4**, 10630–10637.



- 32 S. Zhao, P. Gong, S. Luo, L. Bai, Z. Lin, C. Ji, T. Chen, M. Hong and J. Luo, Deep-Ultraviolet Transparent Phosphates  $\text{RbBa}_2(\text{PO}_3)_5$  and  $\text{Rb}_2\text{Ba}_3(\text{P}_2\text{O}_7)_2$  Show Nonlinear Optical Activity from Condensation of  $[\text{PO}_4]^{3-}$  Units, *J. Am. Chem. Soc.*, 2014, **136**, 8560–8563.
- 33 S. Zhao, P. Gong, S. Luo, L. Bai, Z. Lin, Y. Tang, Y. Zhou, M. Hong and J. Luo, Tailored Synthesis of a Nonlinear Optical Phosphate with a Short Absorption Edge, *Angew. Chem., Int. Ed. Engl.*, 2015, **127**, 4291–4295.
- 34 P. Shan, T. Sun, H. Chen, H. Liu, S. Chen, X. Liu, Y. Kong and J. Xu, Crystal growth and optical characteristics of beryllium-free polyphosphate,  $\text{KLa}(\text{PO}_3)_4$ , a possible deep-ultraviolet nonlinear optical crystal, *Sci. Rep.*, 2016, **6**, 25201.
- 35 V. G. Dmitriev, G. G. Gurzadyan and D. N. Nikogosyan, Properties of Nonlinear Optical Crystals, in *Handbook of Nonlinear Optical Crystals. Springer Series in Optical Sciences*, Springer, Berlin, Heidelberg, 1997, vol. 64.
- 36 W. Dong, Q. Yao, J. Zhang, L. Liu, J. Li and J. Wang, Czochralski Growth and Characterization of a Novel Nonlinear Optical Crystal  $\text{Te}_2\text{P}_2\text{O}_9$ , *Cryst. Growth Des.*, 2018, **18**, 5919–5926.
- 37 K. Min Ok and P. S. Halasyamani, Synthesis, structure, and characterization of a new one-dimensional tellurite phosphate,  $\text{Ba}_2\text{TeO}(\text{PO}_4)_2$ , *ChemInform*, 2006, **179**(5), 1345–1350.
- 38 H. Mayer and M. Weil, Synthesis and crystal structure of  $\text{Te}_3\text{O}_3(\text{PO}_4)_2$ , a compound with 5-fold coordinate tellurium(IV), *ChemInform*, 2003, **629**(6), 1068–1072.
- 39 M. Segall, P. Lindan, M. Probert, C. Pickard, P. Hasnip, S. Clark and M. Payne, First-principles simulation: ideas, illustrations and the CASTEP code, *J. Phys.: Condens. Matter*, 2002, **14**, 2717–2744.
- 40 S. Clark, M. Segall, C. Pickard, P. Hasnip, M. Probert, K. Refson and M. Payne, First principles methods using CASTEP, *Z. Kristallogr.*, 2005, **220**, 567–570.
- 41 M. Ernzerhof and G. E. Scuseria, Assessment of the Perdew–Burke–Ernzerhof exchange–correlation functional, *J. Chem. Phys.*, 1999, **110**, 5029–5036.
- 42 B. Hammer, L. Hansen and J. Nørskov, Improved adsorption energetics within density-functional theory using revised Perdew–Burke–Ernzerhof functionals, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1999, **59**, 7413–7421.
- 43 R. J. Nicholls, A. J. Morris, C. J. Pickard and J. R. Yates, OptaDOS - a new tool for EELS calculations, *J. Phys.: Conf. Ser.*, 2012, **371**, 012062.
- 44 A. J. Morris, R. J. Nicholls, C. J. Pickard and J. R. Yates, OptaDOS: A tool for obtaining density of states, core-level and optical spectra from electronic structure codes, *Comput. Phys. Commun.*, 2014, **185**, 1477–1485.
- 45 Z. Lin, Z. Wang, C. Chen, S. Chen and M. Lee, Mechanism for linear and nonlinear optical effects in crystals of the  $\text{Sr}_2\text{Be}_2\text{B}_2\text{O}_7$  family, *J. Appl. Phys.*, 2003, **93**, 9717–9723.
- 46 B. Zhang, M. Lee, Z. Yang, Q. Jing, S. Pan, M. Zhang, H. Wu, X. Su and C. Li, Simulated pressure-induced blue-shift of phase-matching region and nonlinear optical mechanism for  $\text{K}_3\text{B}_6\text{O}_{10}\text{X}$  ( $\text{X} = \text{Cl}, \text{Br}$ ), *Appl. Phys. Lett.*, 2015, **106**, 992.
- 47 Q. Jing, X. Dong, X. Chen, Z. Yang, S. Pan and C. Lei, The lone-pairs enhanced birefringence and SHG response: A DFT investigation on  $\text{M}_2\text{B}_5\text{O}_9\text{Cl}$  ( $\text{M} = \text{Sr}, \text{Ba}$ , and  $\text{Pb}$ ), *Chem. Phys.*, 2015, **453–454**, 42–46.
- 48 J. Perdew and M. Levy, Physical Content of the Exact Kohn–Sham Orbital Energies: Band Gap and Derivative Discontinuities, *Phys. Rev. Lett.*, 1983, **51**, 1884–1887.
- 49 A. Walsh, D. J. Payne, R. G. Egdell and G. W. Watson, Stereochemistry of post-transition metal oxides: revision of the classical lone pair model, *Chem. Soc. Rev.*, 2011, **40**, 4455–4463.
- 50 A. Walsh and G. Watson, The origin of the stereochemically active  $\text{Pb}(\text{II})$  lone pair : DFT calculations on  $\text{PbO}$  and  $\text{PbS}$ , *J. Solid State Chem.*, 2005, **178**, 1422–1428.
- 51 A. Walsh and G. W. Watson, Influence of the anion on lone pair formation in  $\text{Sn}(\text{II})$  monochalcogenides: a DFT study, *J. Phys. Chem. B*, 2005, **109**, 18868–18875.
- 52 J. Raulot, G. Baldinozzi, R. Seshadri and P. Cortona, An ab-initio Study of the Role of Lone Pairs in the Structure and Insulator–Metal Transition in  $\text{SnO}$  and  $\text{PbO}$ , *Solid State Sci.*, 2002, **4**, 467–474.
- 53 D. J. Payne, R. G. Egdell, A. Walsh, G. W. Watson, J. Guo, P. A. Glans, T. Learmonth and K. E. Smith, Electronic Origins of Structural Distortions in Post-Transition Metal Oxides: Experimental and Theoretical Evidence for a Revision of the Lone Pair Model, *Phys. Rev. Lett.*, 2006, **96**, 157403.
- 54 P. Hohenberg and W. Kohn, Inhomogeneous Electron Gas, *Phys. Rev.*, 1964, **136**, B864.
- 55 A. Filippetti and N. A. Spaldin, Strong-correlation effects in Born effective charges, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2003, **68**, 045111.
- 56 A. Roy, R. Prasad, S. Auluck and A. Garg, First-Principles Calculation of Born Effective Charges and Spontaneous Polarization of Ferroelectric Bismuth Titanate, *J. Phys.: Condens. Matter*, 2010, **22**, 165902.
- 57 R. Resta and D. Vanderbilt, Theory of Polarization: A Modern Approach, *Top. Appl. Phys.*, 2007, **105**, 31–68.
- 58 R. Resta, Modern theory of polarization in ferroelectrics, *Ferroelectrics*, 1994, **151**, 49–58.
- 59 Q. Zhang, Q. Jing, H. Duan and H. Cao, The relationship between covalent bonds and the optical response in a nonpolar family  $\text{ATeMoO}_6$  ( $\text{A} = \text{Mg}, \text{Zn}, \text{Cd}$ ): A Berry-Phase investigation, *J. Solid State Chem.*, 2018, **264**, 22–28.
- 60 N. A. Spaldin, A beginner's guide to the modern theory of polarization, *J. Solid State Chem.*, 2012, **195**, 2–10.
- 61 Q. Jing, G. Yang, J. Hou, M. Sun and H. Cao, Positive and negative contribution to birefringence in a family of carbonates: A Born effective charges analysis, *J. Solid State Chem.*, 2016, **244**, 69–74.
- 62 A. V. Krukau, O. A. Vydrov, A. F. Izmaylov and G. E. Scuseria, Influence of the Exchange Screening Parameter on the Performance of Screened Hybrid Functionals, *J. Chem. Phys.*, 2006, **125**, 224106.
- 63 W. Jia, J. Fu, Z. Cao, *et al.*, Fast plane wave density functional theory molecular dynamics calculations on multi-GPU machines, *J. Comput. Phys.*, 2013, **251**, 102–115.



- 64 W. Jia, Z. Cao, L. Wang, *et al.*, The analysis of a plane wave pseudopotential density functional theory code on a GPU machine, *Comput. Phys. Commun.*, 2013, **184**, 9–18.
- 65 W. H. J. A. C. Baur, The geometry of polyhedral distortions. Predictive relationships for the phosphate group, *Acta Crystallogr., Sect. B: Struct. Crystallogr. Cryst. Chem.*, 1974, **30**(5), 1195–1215.
- 66 K. Momma and F. Izumi, VESTA 3 for three-dimensional visualization of crystal, volumetric and morphology data, *J. Appl. Crystallogr.*, 2011, **44**, 1272–1276.

