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# Tuning exciton diffusion, mobility and emission line width in CdSe nanoplatelets via lateral size†

Alexander W. Achtstein, \*\* \* Sabrine Ayari, \* \* Sophia Helmrich, \* Michael T. Quick, \* Nina Owschimikow, \* Sihem Jaziri<sup>b,c</sup> and Ulrike Woggon\*\*

We investigate the lateral size tunability of the exciton diffusion coefficient and mobility in colloidal quantum wells by means of line width analysis and theoretical modeling. We show that the exciton diffusion coefficient and mobility in laterally finite 2D systems like CdSe nanoplatelets can be tuned via the lateral size and aspect ratio. The coupling to acoustic and optical phonons can be altered via the lateral size and aspect ratio of the platelets. Subsequently the exciton diffusion and mobility become tunable since these phonon scattering processes determine and limit the mobility. At 4 K the exciton mobility increases from  $\sim 4 \times 10^3$  cm<sup>2</sup>  $V^{-1}$  s<sup>-1</sup> to more than 1.4 × 10<sup>4</sup> cm<sup>2</sup>  $V^{-1}$  s<sup>-1</sup> for large platelets, while there are weaker changes with size and the mobility is around 8 × 10<sup>1</sup> cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup> for large platelets at room temperature. In turn at 4 K the exciton diffusion coefficient increases with the lateral size from  $\sim 1.3 \text{ cm}^2 \text{ s}^{-1}$  to  $\sim 5 \text{ cm}^2 \text{ s}^{-1}$ , while it is around half the value for large platelets at room temperature. Our experimental results are in good agreement with theoretical modeling, showing a lateral size and aspect ratio dependence. The findings open up the possibility for materials with tunable exciton mobility, diffusion or emission line width, but quasi constant transition energy. High exciton mobility is desirable e.g. for solar cells and allows efficient excitation harvesting and extraction.

# Introduction

CdSe nanoplatelets<sup>1,2</sup> (NPLs) are colloidal analogues to both conventional 2D quantum wells, produced *via* molecular beam

epitaxy (MBE), and monolayers of van der Waals semiconductors like transition metal dichalcogenides (TMDCs). While graphene exhibits high (carrier) mobilities<sup>3,4</sup> and diffusion coefficients, it is a gap less material, which makes its application in optoelectronics more complicated. Novel ultrathin 2D semiconductor materials combine high mobility, strong light matter interaction and short radiative lifetimes resulting in high quantum efficiencies. 2,5-11 CdSe NPLs are set apart from laterally infinite quantum wells as they exhibit a finite lateral size and weak lateral confinement 12,13 resulting in size tunable exciton-phonon interaction<sup>12</sup> or giant two photon absorption.<sup>7,14-17</sup> Furthermore, their directed emission<sup>18</sup> and emission polarization<sup>19</sup> as well as their high, wellwidth dependent dark-bright splitting<sup>20,21</sup> of 3-6 meV are of great interest. Robust excitons even at room temperature with high exciton binding energies (of ~200 meV) have been found.<sup>2,22-24</sup> The low temperature double peak emission of CdSe NPLs has been attributed to exciton and additional trion states, 21,25,26 where the latter exhibit a fine structure due to shakeup lines<sup>27</sup> that originate from the quantized nature of electron states in the laterally weakly confined system.

Inspired by a phenomenological correlation between the exciton mobility and emission line width in ref. 28, we investigate in this paper the exciton (quasiparticle) diffusion constant, exciton mobility and scattering rate using temperature dependent photoluminescence (PL) spectroscopy and theoretical modeling for CdSe nanoplatelets, a model system for 2D semiconductors of finite lateral size. Unlike charge carrier mobility determination by classical transport measurements with contact or contact-less THz and microwave conductivity measurements, 29,30 we determine the diffusion coefficient and mobility of neutral excitons by connecting the temperature dependent emission line width of the considered colloidal CdSe quantum wells to the microscopic scattering rates and subsequently to the (exciton) diffusivity. We demonstrate that our method shows good agreement with theoretical modeling and other methods, e.g. with dephasing data. The exciton diffusion and emission line width are linked, as scattering

<sup>&</sup>lt;sup>a</sup>Institute of Optics and Atomic Physics, Technische Universität Berlin, Strasse des 17. Juni 135, 10623 Berlin, Germany. E-mail: achtstein@tu-berlin.de

<sup>&</sup>lt;sup>b</sup>Laboratoire de Physique des Materiaux, Faculte des Sciences de Bizerte, Universite de Carthage, Jarzouna 7021, Tunisia

<sup>&</sup>lt;sup>c</sup>Laboratoire de Physique de la Matiere Condensee, Departement de Physique, Faculte des Sciences de Tunis, Campus Universitaire, 1060 Tunis, Tunisia

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<sup>‡</sup>These authors contributed equally.

events (with e.g. phonons) do not only result in diffusion, but also randomize the PL emitter phase of the excitons, causing dephasing and line width broadening. We show in the following that the acoustic and optical phonon limited scattering rates, exciton mobility and diffusion in CdSe nanoplatelets can be tuned by their lateral size and aspect ratio.

#### 2. Results and discussion

4.5 monolayer (ML) zinc blende (ZB) CdSe nanoplatelets with different lateral sizes of  $17 \times 6 \text{ nm}^2$  to  $41 \times 13 \text{ nm}^2$  ( $17 \times 6 \text{ nm}^2$ ,  $19 \times 7 \text{ nm}^2$ ,  $17 \times 11 \text{ nm}^2$ ,  $29 \times 8 \text{ nm}^2$ ,  $30 \times 15 \text{ nm}^2$ ,  $41 \times 10^{-2}$ 13 nm<sup>2</sup>) and corresponding platelet areas (rounded) of 102, 134, 187, 232, 450 and 533 nm<sup>2</sup> were synthesized according to ref.1 and 31, analyzed by transmission electron microscopy (TEM) and embedded into a polymer layer (see the Methods section). Fig. 1 shows temperature dependent PL emission spectra of exemplary sizes at 4 and 200 K under off-resonant 2.95 eV (420 nm) excitation. Clearly a double emission is observed, which has been attributed to trion (lower energy emission T<sup>-</sup>) and exciton (upper energy emission X)<sup>21,25-27</sup> PL. We remark that due to the low coupling to LO-phonons in the CdSe platelets, e.g. confirmed by Raman<sup>32,33</sup> or pump-probe spectroscopy,<sup>34</sup> no relevant LO-phonon replicas of the exciton emission are present in the PL spectra.<sup>35</sup>

The lateral size tunable trion binding energy and oscillator strength in CdSe nanoplatelets have been studied systematically in ref. 26. We focus in this paper on the exciton emission line and exciton-phonon coupling. Therefore we fit the double emission by two Voigt functions accounting for the homogeneous (Lorentzian) and inhomogeneous (Gaussian) contributions to each emission peak (see also the Methods section). They are related to the natural line width (the former) and lateral size dispersion altering the weak lateral confinement<sup>12</sup>

of the nanoplatelets (the latter). The inhomogeneous contribution is temperature independent, and hence kept as a constant parameter for each platelet size for all temperatures in the fit, see also the Methods section for a discussion. In line with ref. 12 we obtain the temperature dependent homogeneous line width, which can be fitted according to:

$$\Delta(T) = \Delta_0 + \tilde{\Delta}_{AC}T + \tilde{\Delta}_{Opt}/\left(e^{E_{LO}/k_BT} - 1\right)$$
 (1)

 $\Delta_0$  is the zero temperature homogeneous line width, while  $\tilde{\Delta}_{AC}$  and  $\tilde{\Delta}_{Opt}$  describe the line width broadening due to scattering with acoustic phonons or optical-phonons of energy  $E_{IO}$ . We use  $E_{LO} = 25.6$  meV from Raman results in ref. 32. Exemplary fits to this equation are shown in Fig. 1(c) for our nanoplatelets of different sizes, resulting in the coupling coefficients displayed in Fig. 2 (orange points).

In Fig. 2(a) we observe a decrease of the coupling to acoustic modes with increasing platelet size, 12 while by trend the coupling strength of excitons to optical-phonons in (b) increases. Since both  $\tilde{\Delta}_{AC}$  and  $\tilde{\Delta}_{Opt}$  can be tuned by the size of the platelets, the exciton-phonon interaction becomes size dependent, so that also the associated microscopic scattering rates  $\Gamma_{AC,Opt}$  become tunable. The larger data scatter for the optical-phonons among the samples may be related to the fact that optical-phonon scattering is more susceptible to alterations by (charged) defects as well as strain fields in the NPLs, which can be a result of NPL quality distribution.

To analyze the underlying trends in detail, Fig. 2 contains the results of theoretical modeling of the exciton-phonon interaction in these 2D quantum wells, which depends on the NPL area and lateral aspect ratio. The lateral aspect ratio R = $L_x/L_y$ , defined as the ratio of the platelet extent in the long and short in-plane directions, is varied from 1:1 to 4:1. In our theoretical calculation, we take into account all relevant couplings to acoustic (AC) and optical (Opt) phonons in CdSe nano-

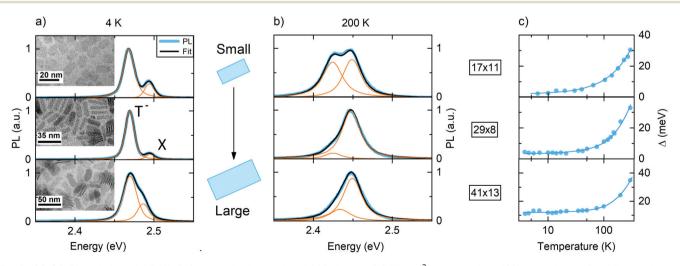


Fig. 1 (a), (b): PL emission of 4.5 ML CdSe nanoplatelets at 4 and 200 K under 0.2 W cm<sup>-2</sup> cw-equivalent 420 nm excitation for different platelet sizes in the three rows. Fits to the double emission of exciton (X) and trion (T<sup>-</sup>) are carried out using Voigt functions. Insets: Representative TEM images of the nanoplatelets. The temperature dependent exciton line width, obtained from fits like in (a) and (b), for a temperature variation between 4 and 200 K is shown in (c) along with the platelet size in nm x nm.

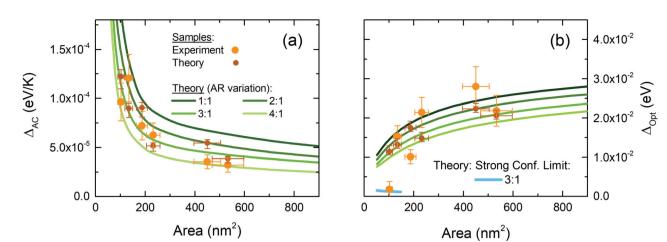


Fig. 2 (a) Experimental coupling to acoustic phonons *versus* lateral platelet area (orange dots) and theoretical simulation results for the considered NPLs (brown dots) as well as theory predictions for different lateral aspect ratios *R* (continuous lines). (b) Coupling to optical phonons. The simulations are both in the weak lateral confinement limit. For very small NPLs the strong confinement limit is indicated in (b).

platelets. This includes (i) scattering by acoustic phonons (AC) via deformation potential (DA) and piezoelectric interaction (PA) and (ii) scattering by optical phonons (Opt) via the Fröhlich interaction (LO, Fr) and nonpolar (optical) deformation-potential (NP, Def). For the acoustic phonon, while the deformation potential primarily yields interactions with longitudinal acoustics phonons, the piezoelectric scattering couples the electronic system to both longitudinal LA and transversal TA acoustics phonons<sup>36,37</sup> (for more details, see the Methods section). To build up our theory, we at first relate the microscopic scattering rates with phonons ( $\Gamma_{\lambda=AC,Opt}$ ) to the coupling parameters  $\tilde{\Delta}_{\lambda=AC,Opt}$  in Fig. 2. Acoustic phonon scattering results in an emission linewidth contribution of

$$\Delta_{\rm AC}(T) = \hbar \Gamma_{\rm AC}(T) = \tilde{\Delta}_{\rm AC} T, \tag{2}$$

while for the optical phonon scattering 38,39

$$\Delta_{\mathrm{Opt}}(T) = \hbar\Gamma_{\mathrm{Opt}}(T) = \tilde{\Delta}_{\mathrm{Opt}} / \left(e^{E_{\mathrm{LO}}/k_{\mathrm{B}}T} - 1\right)$$
 (3)

is valid, with  $n_{\rm B}(T)=1/(\exp(E_{\rm LO}/k_{\rm B}T)-1)$ , the Bose statistics factor. Hence, the observed coupling constants in Fig. 2 can be connected to the associated microscopic scattering rates. We model the mentioned acoustic and optical exciton–phonon scattering rates in first-order perturbation theory using Fermi's golden rule, taking into account phonon emission and absorption,

$$\begin{split} \varGamma_{\lambda} &= \frac{2\pi}{\hbar} \sum_{\mathbf{f},q} |\mathbb{G}_{\lambda,\mathbf{f}}(q)|^{2} \cdot \\ &\left\{ (N_{\lambda}(q) + 1) \delta \big( E_{\mathbf{X}}^{\mathbf{f}} - E_{\mathbf{X}}^{\mathbf{i}} + E_{\lambda}(q) \big) + N_{\lambda}(q) \delta \big( E_{\mathbf{X}}^{\mathbf{f}} - E_{\mathbf{X}}^{\mathbf{i}} - E_{\lambda}(q) \big) \right\} \end{split} \tag{4}$$

where  $\lambda = AC$ , Opt is the acoustic (including deformation potential (DA) and piezoelectric (PA) coupling) and optical coupling (including polar (LO, Fr) and nonpolar (NP, Def) coupling) of excitons to phonon modes.  $E_X^{i(f)}$  are the energies of the exciton initial and final states.  $E_\lambda(q)$  is the energy of the phonon with wave vector q.  $q = (Q, q_z)$  is composed of in-plane

Q and perpendicular  $q_z$  components of the phonon wave vector. Notably, in our calculation while for the acoustic phonons we use continuum phonon modes in the z-direction, for optical phonons in the thin platelets (thickness d=4.5 ML), we consider quantized modes in the z-direction, i.e.  $q_z=q_n$ , see eqn (15) in the Methods section. The occupation number  $N_\lambda(q,T)=\left[\exp\left(\frac{E_\lambda(q)}{k_{\rm B}T}\right)-1\right]^{-1}$  is given by a Bose distribution. The sum in eqn (4) extends over all possible phonon wave vectors q and final exciton states f. The matrix element of the exciton–phonon interaction involved in the transition is given by

$$\mathbb{G}_{\lambda,f}(q) = \langle \Psi_{X}^{f} | \mathbb{H}_{X-ph}^{\lambda} | \Psi_{X}^{i} \rangle \tag{5}$$

with  $\Psi_{\rm X}^{i({\rm f})}$  the exciton wave function,  $\mathbb{H}_{{\rm X-ph}}=(V_{\rm e}{}^{\lambda}(q)e^{-iq\cdot r_{\rm e}}-V_{\rm h}{}^{\lambda}(q)e^{-iq\cdot r_{\rm h}})$  + c.c is the exciton–phonon interaction Hamiltonian, with  $r_e(\rho_e,z_e)$  and  $r_h(\rho_h,z_h)$  the electron and hole spatial coordinates. c.c. stands for the complex conjugate.  $V_{e(h)}^{\lambda}$ (q) is the electron (hole) coupling element. (See also the Methods section with a detailed description of the theory and a list of all used material constants.) The modeling results for the acoustic and the optical coupling are depicted in Fig. 2 for varying lateral aspect ratios as well as for the exact sizes and lateral aspect ratios of the platelets (see the Methods section) used in experiments. In the ESI† the contributions of different coupling mechanisms (via DA, PA, LO-Fr and NP-Def couplings) to optical and acoustic phonon scattering are shown. Overall, we find that the acoustic deformation potential interaction and the Fröhlich interaction dominate the coupling to acoustic and optical phonon, respectively. The piezoelectric interaction and the nonpolar (optical) deformation-potential coupling are weak and their role is negligible in the coupling to acoustic and optical phonons; however it is taken into account in our calculations.

Our theory in Fig. 2 shows – in line with the experimental results – that the coupling to acoustic phonons decreases with

the platelet area and lateral aspect ratio, while the coupling to optical-phonons increases with the platelet area and decreasing aspect ratio. The demonstrated area and lateral aspect ratio dependence of the acoustic and optical phonon scattering rates and subsequently the coupling constants (Fig. 2) arises from the effects of lateral confinement on the exciton-phonon wave function overlap as well as from the q dependence of the coupling matrix elements. Inserting the expression for the optical and acoustic matrix element in exciton basis, converting the sum over q into an integral and evaluating the  $\delta$ -function, leads to the following dependency: for the acoustic scattering rate we obtain the scaling

 $\Gamma_{\rm AC} \simeq \frac{C_{\rm DA}{}^2 \mathbb{F}_{\rm DA} \left(q_x,q_y,q_z\right)}{A}$ , while for optical phonon scattering  $\Gamma_{\rm Opt} \simeq C_{\rm LO,Fr}{}^2 \mathbb{F}_{\rm LO,Fr} (q_x,q_y,q_z) A$  (see the ESI† and Methods section). This explains the observed trend of a decrease of acoustic and an increase of the optical phonon coupling with the lateral platelet area. Here,  $C_{\rm LO,Fr}$  and  $C_{\rm DA}$  are material constants and A the platelet area. The matrix element  $\mathbb{F}_{\lambda}(q_x,q_y,q_z)$  imposes an additional alteration, depending on lateral size  $L_{\rm X}$  and  $L_{\rm Y}$ . Therefore the coupling constants (Fig. 2(a) and (b)) are a function of the lateral aspect ratio  $R = \frac{L_{\rm X}}{L_{\rm Y}}$  for fixed area A.

Hence the phonon coupling in CdSe NPLs can be tuned by the platelet area and lateral aspect ratio. This directly impacts the emitter line width, as reflected in eqn (1)–(3), so that it becomes tunable too.

We compare the results for optical phonon coupling with published Raman data yielding a Huang-Rhys factor of S = 0.08 for 156 nm<sup>2</sup> NPLs with a lateral aspect ratio of 4.3.<sup>33</sup> Using  $S = (\Delta_{\text{Opt}}/E_{\text{LO}})^2/2$  (ref. 41) we calculate a 10 meV coupling strength. This is in agreement with the trend of the R = 4theory line in Fig. 2(b) and the general trend of a reduction of the coupling strength with reduced size. Comparing the acoustic coupling in Fig. 2(a) with the literature is less straight forward. Dong et al.34 reported dimensionless displacements  $\hat{\Delta}$  for in-plane and out-of-plane direction for acoustic phonons in CdSe NPLs by pump-probe spectroscopy. They relate via  $S = \hat{\Delta}^2/2$  to the Huang-Rhys factor S. It is related to the exciton-phonon coupling strength  $a_{AC}$  via  $S = (1/2)(a_{AC}/E_{AC})^2$ , with  $E_{AC}$  the acoustic phonon energy. The acoustic line width contribution in eqn (1) relates to the coupling strength via  $\Delta_{\rm AC}T = k_{\rm B}a_{\rm AC}/E_{\rm AC}$ , so that  $\Delta_{\rm AC} = k_{\rm B}\sqrt{2S}$ . Summing this over the in- and out of plane results of ref. 34 results in  $4.2 \times 10^{-5}$  eV K<sup>-1</sup>. The platelet area used here is 203 nm<sup>2</sup> and the lateral aspect ratio R = 4.1. The obtained value is in good agreement with the R = 4 line of our simulations in Fig. 2(a), substantiating our results.

An increasing deviation of our experimental results from the theory for the polar LO-phonon coupling is observed in Fig. 2(b) for the smallest considered platelet ( $17 \times 6 \text{ nm}^2$ ), which is already in an intermediate to strong (lateral) confinement, as the short direction approaches the bulk exciton Bohr radius of CdSe. We therefore indicate in the figure also the strong confinement theory limit of the phonon coupling, which agrees well with the experimental result. In general, a

continuous theory ranging from strong to weak lateral confinement regimes is very difficult, as the confinement in the unequal lateral x and y dimensions can be in different regimes for (lateral) aspect ratios R bigger than one. Nevertheless we can conclude that our theory reproduces the observed trends in the phonon couplings well.

The mentioned scattering events with phonons (eqn (1)–(3)) do not only result in line broadening, but also impact the exciton mobility and diffusion constant. According to the relaxation time approximation the scattering time  $\tau = 1/\Gamma$ , with  $\Gamma$ , the scattering rate, is related to the diffusion coefficient D  $via^{42,43}$ 

$$D(T) = \frac{k_{\rm B}T}{M}\tau(T) = \frac{k_{\rm B}T}{M}\frac{1}{\Gamma(T)} \tag{6}$$

with  $M=0.63m_0$ , <sup>23</sup> the exciton mass. We remark that this equation is analogous to the case of charged particles, <sup>39,42</sup> but in our case formulated for neutral species, the excitons. According to Einstein and Smoluchowski<sup>44</sup>

$$D = \mu k_{\rm B} T \tag{7}$$

is valid for neutral gas molecules or particles, like the considered excitons here, with  $\mu$  the particle mobility, while for charged particles the more familiar equation  $D_{\lambda} = \mu_{\lambda}k_{\rm B}T/q_{\rm e}$  applies. ( $\lambda$  is here an index representing an e or h charge of  $q_{\rm e}$ .) This allows relating particle mobility  $\mu$ , the diffusion constant D and the scattering time  $\tau$  via  $\mu = \tau/M$  and eqn (7) for neutral particles. <sup>44</sup> As the scattering rates and line width obey a linear dependence (eqn (2) and (3)), eqn (6) and (7) result in an inverse dependence of the exciton mobility and line width. Indications for such a behavior have been reported in ref. 28 and support our framework. Using eqn (2) and (3), we obtain the diffusion coefficients

$$D_{\rm AC}(T) = \frac{\hbar k_{\rm B}}{M\tilde{\Delta}_{\rm AC}} \tag{8}$$

$$D_{\text{Opt}}(T) = \frac{\hbar k_{\text{B}} T}{M \tilde{\Delta}_{\text{Opt}} n_{\text{B}}} = \frac{\hbar k_{\text{B}} T}{M \tilde{\Delta}_{\text{Opt}}} \left( e^{E_{\text{LO}}/k_{\text{B}} T} - 1 \right)$$
(9)

for acoustic and optical phonon scattering. We use two exemplary platelet sizes (a small and a large one) of 134 nm $^2$  (19  $\times$ 7 nm<sup>2</sup>) and 533 nm<sup>2</sup> (41  $\times$  13 nm<sup>2</sup>) to investigate the total phonon scattering limited mobility and diffusion constant using Matthiessen's rule for independent scattering processes. From the original  $1/\mu = 1/\mu_{AC} + 1/\mu_{Opt}$  equation follows  $1/D = 1/\mu_{AC}$  $D_{\rm AC}$  + 1/ $D_{\rm Opt}$  via eqn (7). Fig. 3(a) shows the resultant temperature dependence of  $\mu$ , while (b) shows the related diffusion coefficient D and (c) the course of the associated total scattering rate as well as the associated PL line width. We observe an increase of the scattering rate with temperature, which is related to the increasing probability for phonon emission or absorption due to the increasing occupation probability of both acoustic and optical phonon modes with increased thermal energy. This results in a decrease of the exciton mobility (a) and diffusion coefficient (b) with temperature. We remark that the exciton mobility in (a) is scaled with the elementary charge  $q_{\rm e}$  to obtain a reduced unit, which

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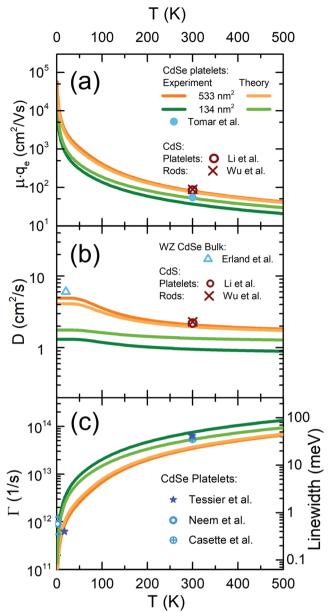


Fig. 3 Temperature dependent (scaled) CdSe platelet exciton mobility  $(\mu q_{\rm e})$  (a) and diffusion coefficient (b) as well as scattering rate and line width (c), as obtained from the experimental results in Fig. 2, for two exemplary platelet sizes.(two darker lines) Corresponding theory results for weak lateral confinement (pale lines) for the same sizes. Additional reference data points from the literature (including methods) of Tomar et al. (ref. 29, area = 326 nm<sup>2</sup> CdSe NPLs, THz time-domain spectroscopy), Li et al. (ref. 45, CdS NPLs, pump-probe spectroscopy (PP)), Wu et al. (ref. 46, CdS rods, PP), Erland et al. (ref. 43, wurtzite CdSe in c-direction, four wave mixing (FWM)). CdSe NPLs: Cassette et al. (ref. 47, 380 nm<sup>2</sup> NPLs, FWM), Tessier et al. (ref. 35, 280 nm<sup>2</sup> NPLs, single particle PL), and Naeem et al. (ref. 8, range of values for NPLs of different sizes, from 100 to 350 nm<sup>2</sup>, FWM).

resembles the rather more familiar units of an electron mobility than that for a neutral particle (in  $cm^2/(V s A s)^{-1}$ ), giving values in the range of  $\sim 10^{20}$  to  $10^{24}$  cm<sup>2</sup> V<sup>-1</sup> A<sup>-1</sup> s<sup>-2</sup>. (See also comments below eqn (7)). We also plot, based on our simulations in Fig. 2, the theory results for the four parameters on

display and obtain good agreement, substantiating our results. The slight overestimation of the diffusion constant for the smaller platelet is the result of the increasing strong confinement nature for small platelets, resulting in a slight overestimation of the optical-phonon coupling, discussed in the framework of Fig. 2.

As a general trend, Fig. 3 shows that larger platelets have lower coupling to acoustic phonons, so that the 533 nm<sup>2</sup> platelets exhibit higher mobilities (diffusion coefficients), especially at low temperatures, as compared to the smaller samples. This also results in a lower emission line width (Fig. 3(c)). At low temperature, the exciton mobility in CdSe nanoplatelets can reach more than  $10^4$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup>, a considerably high value. At room temperature, the (experimental) mobilities are with 36 cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup> and 82 cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup> lower due to the increasing contribution of optical phonon scattering. Fig. 3 also shows reference values from other methods, namely THz pumpprobe spectroscopy, four wave mixing dephasing and linewidth measurements, which nicely agree with our results, as reflected in the shown values for the mobility, diffusion constant and scattering rate. Our measured exciton mobilities are also comparable in order of magnitude with electron mobilities for TMDC materials like MoS<sub>2</sub>, which has 400 cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup> at 300 K and  $\sim 10^4$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup> at low temperature.<sup>48,49</sup> The abovementioned exciton mobility values for CdSe nanoplatelets translate via eqn (7) into exciton diffusion constants of  $1.3 \text{ cm}^2 \text{ s}^{-1} (134 \text{ nm}^2) \text{ and } 4.9 \text{ cm}^2 \text{ s}^{-1} (533 \text{ nm}^2) \text{ at } 4 \text{ K, as well}$ as 1.0 cm $^2$  s $^{-1}$  and 2.1 cm $^2$  s $^{-1}$  at 300 K (see also later Fig. 4). These values are comparable to measured exciton diffusion constants of 2.2 cm<sup>2</sup> s<sup>-1</sup> in CdS platelets<sup>45</sup> or 2.3 cm<sup>2</sup> s<sup>-1</sup> in CdS rods. 46 Further reference values are indicated in Fig. 3(b) for comparison and show good agreement with our results. The mentioned diffusion constant values, shown in (b), are slightly lower than typical values for bulk wurtzite CdSe in ref. 43, reflecting the known decrease in phonon coupling strength with a reduced quantum well width. 38,39

A comparison of subfigure (a) and (b) together with eqn (7) shows that the main part of the temperature dependence of the exciton mobility is related to the  $1/k_BT$  prefactor of the mobility in  $\mu = D/k_BT$ , while the direct temperature dependence of D is smaller. Furthermore, we can state from the data in Fig. 3(c) that exciton diffusion is the dominant transport mechanism in 2D nanoplatelets, so that the exciton movement is not radiatively (or lifetime) limited by population decay or trapping. This can be seen from the fact that the scattering rates in Fig. 3(c) exceed the radiative rates (inverse lifetimes) in CdSe nanoplatelets well. The latter are of the order of  $\sim$ 1 – 5 ×  $10^{10} \text{ s}^{-1}$  at 4 K (ref. 6 and 50) and even lower at elevated temperatures, due to the increase of exciton lifetime with temperature caused by the giant oscillator strength effect<sup>51,52</sup> in 2D. A further important feature is that the exciton mobility and exciton-phonon scattering rate in CdSe NPLs can be tuned by the lateral size at low temperatures, as seen in Fig. 3(a) and (c).

Fig. 4 shows the nanoplatelet lateral size (area) dependence of the exciton diffusion constant and mobility at 4 K and 300 K, as obtained from the experiment and theory displayed

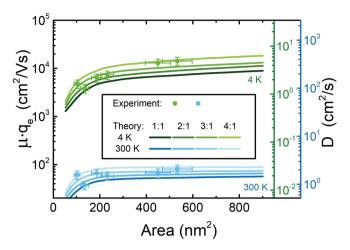


Fig. 4 Dots: Experimental, lateral size (area) dependent exciton diffusion constant D and mobility  $\mu \cdot q_e$  at 4 K (green) and 300 K (blue) for the six considered platelet sizes obtained from Fig. 2 using eqn. (8) and (9). Continuous lines result from our weak lateral confinement theory for different lateral aspect ratios from 1:1 to 4:1. Two axes are drawn for D on the right side due to the temperature dependent scaling factor  $k_B T$  between  $\mu$  and D in eqn (7).

in Fig. 2 and using eqn (7)-(9). Again, both quantities are higher at low temperature, with a larger variation at low temperature (see double ordinate) and an overall increase with the lateral size and aspect ratio. The first perception is due to the temperature dependence of the scattering rates, while the latter two are related to the size-dependent coupling coefficients (Fig. 2). For 300 K Fig. 4 shows a weaker (lateral) size dependence as compared to 4 K, as the (lateral size) trends of acoustic and optical phonon contributions (Fig. 2) partially compensate each other at higher temperatures, where not only acoustic phonons contribute like at 4 K. As a general trend the coupling to acoustic phonons and with it the scattering rate increases with decreasing well thickness39 (from bulk to a narrow 2D system), which is in principle an effect of the increasing (exciton) wave function amplitude (or normalization pre-factor) upon stronger z-confinement. Hence, the mobility and diffusion coefficient for (ZB) CdSe NPLs (Fig. 4), e.g. at 4 K, is a bit lower than that for bulk (WZ) CdSe, 43 having 14 cm<sup>2</sup> s<sup>-1</sup>. Data on ZB bulk do not exist, as it is not a stable bulk modification. Since optical-phonon scattering dominates at elevated temperatures (e.g. at 300 K) and adds to the acoustic scattering rate, eqn (6) and (7) translate this to a reduced mobility. This results in lower exciton diffusion constants and mobility at 300 K, as seen in Fig. 4. Increasing the lateral platelet area results in an increase of the mobility and diffusion constant for small platelets, while a saturation behavior is observed for large NPLs, which is the result of the saturation behaviors of the coupling constants observed in Fig. 2. With increasing lateral size  $(L_x, L_y)$ , the lateral confinement becomes weaker and the exciton is increasingly delocalized; i.e. the exciton center of mass (CM) motion is (quasi) free and can be described by the plane wave function  $\Psi_{\rm CM}(R_{\rm X}) = \frac{1}{\sqrt{A}} e^{iK_{\rm X}R_{\rm X}}$ .

Hence the CM matrix element reduces to the conservation of the crystal momentum  $\delta_{K_X^{i}-K_X^{f}}$ , Q in the free directions. This case is analogous to ideal 2D quantum wells and TMDC materials. There, (i) the scattering rate and subsequently the mobility  $\mu$  and the diffusion coefficient D are independent of the area. Furthermore, (ii) the deformation-potential interaction weakens due to the decreasing phonon wave vector q and becomes constant for large wells. Additionally, (iii) the Fröhlich interaction saturates and becomes sensitive to the dielectric environment. For (iii) screening will be relevant in the phonon-momentum dependency of the polar-optical coupling.  $^{53,54}$  Due to (i)–(iii) it is not surprising that e.g. the room temperature mobility remains at a constant, area independent value for large platelets. This corresponds to a bulk like limit for the two weakly confined lateral dimensions.

A brief note relates to the contributions of the nonpolar (optical) deformation-potential coupling and piezoelectric (acoustic) interaction on the total diffusion coefficient and mobility. They are considerably weaker than the Fröhlich and the acoustic deformation potential interaction and have a very minor effect on the total mobility. We demonstrate and discuss this in section S1A and B of the ESI† by further calculations. Additionally Table S1† shows a comparison of their impact on the total mobility. The acoustic deformation potential and the Fröhlich interaction dominate the total mobility, while the piezoelectric interaction results in only a slight reduction of the total mobility. The optical deformation potential has a vanishing contribution with respect to the other interactions as Matthiessens' rule for the total mobility is applied.

Summing up, our results in Fig. 3 and 4 show that there is an opportunity to tune the exciton mobility and diffusion constant in our CdSe nanoplatelets *via* lateral platelet size and aspect ratio as well as the sample temperature, especially for smaller NPLs. This is based on the lateral size and aspect ratio dependencies of the acoustic and Fröhlich coupling.

Finally we remark that a similar analysis of the trion diffusion coefficient and mobility, based on the T<sup>-</sup> peak in Fig. 1, like performed for the excitons in this paper, is not possible. This is due to the fact that the trion line width does not only depend on the mentioned scattering processes, but is also influenced by the energy, density of states and occupation probability of final states for the residual electron transferred to a continuum state upon radiative trion decay. This energy and momentum transfer to the electron alters the trion emission line width, both with the platelet size and temperature, and is beyond the scope of this investigation.

# 3. Conclusions

In summary we have shown that the exciton diffusion coefficient and mobility in CdSe nanoplatelets can be tuned *via* the lateral extent and aspect ratio. The coupling to acoustic and optical phonons can be engineered *via* the lateral size of the platelets. As these phonon scattering processes determine and limit the exciton diffusion and mobility, both can be tuned *via* 

the lateral size and aspect ratio. At 4 K the exciton mobility increases with the lateral size from  $\sim \! \! 4 \times 10^3 \; \mathrm{cm^2 \; V^{-1} \; s^{-1}}$  to more than  $1.4 \times 10^4 \; \mathrm{cm^2 \; V^{-1} \; s^{-1}}$ , while it is about  $8 \times 10^1 \; \mathrm{cm^2 \; V^{-1} \; s^{-1}}$  for large platelets at room temperature. In turn, at 4 K the exciton diffusion coefficient increases with the lateral size from  $\sim \! \! 1.3 \; \mathrm{cm^2 \; s^{-1}}$  to  $\sim \! \! \! 5 \; \mathrm{cm^2 \; s^{-1}}$ , while it is around half the value for large platelets at room temperature. We have shown good agreement between our theory predictions and experimental results as well as with other experimental methods like four wave mixing, THz conductivity and mobility measurements. Our theoretical modeling shows that the exciton diffusion coefficient and mobility in the 2D nanoplatelets are tunable by the platelet area and lateral aspect ratio as well as the sample temperature.

Our findings open up the possibility for materials with e.g. engineerable (exciton) diffusion, mobility and PL line width. Especially important is that this tuneability via lateral size and aspect ratio is quasi independent from the optical transition energy, which is given by the strong, but constant z-confinement in our colloidal quantum wells and only minorly by the weak lateral confinement (Scott et al. 12) in NPLs, which is of the order of <30 meV. The presented findings will strongly impact further studies, as the demonstrated lateral size tuneability of the exciton mobility can improve e.g. excitation or charge extraction efficiencies of solar cells, solar hydrogen generation, or conversely light emission efficiencies of LEDs or lasers. Tuning e.g. exciton diffusion might be interesting for instance for investigations about biexciton formation upon exciton fusion, as it determines the encounter probability of the two particles. Our results provide a toolbox for the design of photonic materials with engineered properties, that is directly transferable to other 2D materials of current interest, like Perovskite (Weidman et al. 55) and TMDC materials, which can be grown also with finite lateral size.

## Methods

### 4.1. Samples and setup

4.5 monolayer (ML) zinc blende (ZB) CdSe nanoplatelet samples with the first exciton absorption band around 512 nm and different average lateral sizes of  $17 \times 6 \text{ nm}^2$  to  $41 \times 13 \text{ nm}^2$  were synthesized according to ref.1 and 31 and characterized by transmission electron microscopy (TEM). The corresponding lateral aspect ratios R are: 2.8 ( $17 \times 6 \text{ nm}^2$ ), 2.7 ( $19 \times 7 \text{ nm}^2$ ), 1.5 ( $17 \times 11 \text{ nm}^2$ ), 3.6 ( $29 \times 8 \text{ nm}^2$ ), 2.0 ( $30 \times 15 \text{ nm}^2$ ) and 3.2 ( $41 \times 13 \text{ nm}^2$ ).

The samples were embedded in PMAO polymer on fused silica substrates. The volume fraction in the polymer was kept below 1% to avoid any aggregation or FRET effects. <sup>56</sup> We remark that the TEM images in Fig. 1 are made by a different coating process for the TEM grids without any (host) polymer. The samples were mounted in a CryoVac Micro cryostat. The second harmonic of a 150 fs, 75.4 MHz repetition rate Ti:Sa laser (Coherent Mira 900HP) at 420 nm was used for confocal excitation with an 0.4 NA objective ( $\approx$ 0.2 W cm<sup>-2</sup> CW equi-

valent excitation density). The moderate excitation density leads to <0.1 percent of the platelets being excited within one laser pulse (average number of excitons per platelet per pulse below  $10^{-3}$ , estimated *via* ref. 57 and the measured continuum absorption). This low density excludes multiexcitonic processes. Time integrated PL detection was realized using a Horiba IHR550 spectrometer with an attached LN<sub>2</sub> cooled CCD (Roper Spec 10).

The emission line width fits in Fig. 1 result in the following Gaussian inhomogeneous contributions, which depend on the platelet size and lateral aspect ratio (17  $\times$  6 nm<sup>2</sup>, 7.5 meV; 19  $\times$  $7 \text{ nm}^2$ , 12.9 meV;  $17 \times 11 \text{ nm}^2$ , 10 meV;  $29 \times 8 \text{ nm}^2$ , 10.1 meV;  $30 \times 15 \text{ nm}^2$ , 15 meV;  $41 \times 13 \text{ nm}^2$ , 10.4 meV). They are temperature independent and reflect the lateral size dispersion of CdSe NPLs. The inhomogeneous contribution is not relevant for the determination of  $\tilde{\Delta}_{AC}$  and  $\tilde{\Delta}_{LO}$  as the quantities do not relate to any offset in Fig. 2. We remark that the order of magnitude of the inhomogeneous lateral center of mass confinement (inhomogeneous Gaussian component of the fits mentioned above) can be reasoned by simply considering the lateral confinement energy of the exciton center of mass motion and relating it to the lateral size dispersion of the samples. Adapting the infinitely deep well expression for a quantum box and its confinement energies  $\Delta E = (1/2\mu)(n_z\pi\hbar/$  $(L_z)^2 + (\pi^2 \hbar^2 / 2M) (n_x^2 / L_x^2 + n_y^2 + L_y^2)^{12}$  for our NPLs, the first term reflects the strong z-confinement in the well, while the second term the weak center of mass confinement in x and ydirection.  $\mu$  is the reduced exciton mass and M is the total exciton mass, and  $n_i$  is the quantized state quantum numbers in i = x,y,z direction. We consider the lowest states  $n_i = 1$ . A fluctuation propagation calculation is analogous to conventional error propagation to the following expression for the inhomogeneous broadening of the emission energies due to lateral (and transversal) size distribution:  $\Delta_{00} = (\pi^2 \hbar^2 / M_{x,y}) (\delta L_x)$ +  $L_x^3$  +  $\delta L_v/L_v^3$ ) +  $(\pi^2\hbar^2/\mu_z)(\delta L_z/L_z^3)$ , with  $\delta L_i$  the standard deviation of an approximately Gaussian size distribution from TEM characterization in direction i.

Since nanoplatelets are atomically smooth quantum wells, we neglect at first the last contribution in z and assume a  $\sim$ 20% size dispersion in x- and y-directions, as obtained from TEM for the  $17 \times 6 \text{ nm}^2$  sample. Using effective masses from ref. 23 we obtain an ~7 meV predicted inhomogeneous contribution, in good agreement with our experimental result (7.5 meV) above, substantiating our findings and the magnitude of the inhomogeneous contribution. For increasingly larger platelets additional effects occur, which impact the transverse confinement. It is known that extended NPLs tend to bend, which causes inhomogeneous strain in the platelet due to the distortion of the zinc blende lattice.<sup>58</sup> This translates to small well width variations from platelet to platelet and within the platelet. The effect increases by trend for larger platelets as there is stronger bending, which could explain an additional and increasing contribution to the inhomogeneous broadening for larger platelets. The bending directly impacts the third contribution in the equation above by altering the z-confinement.

# 4.2. Theoretical formulation of the exciton-phonon coupling matrix element

The exciton phonon matrix element reads:

$$\mathbb{G}_{\lambda,f}(q) = \langle \Psi_{X}^{f} | V_{e}^{\lambda}(q) e^{-iq \cdot r_{e}} - V_{h}^{\lambda}(q) e^{-iq \cdot r_{h}} ) | \Psi_{X}^{i} \rangle$$
 (10)

For a zinc blende crystal structure, the coupling to acoustic phonons is a sum of deformation potential (DA) and piezoelectric (PA) interactions. In such a structure, only the longitudinal acoustic-phonon modes (LA) are connected with the deformation potential while the piezoelectric scattering couples the electronic system to both  $\lambda$  = LA and TA phonons. <sup>36,37</sup> The coupling of electrons (holes) to longitudinal-acoustic (LA) phonons by means of a deformation potential D is described by: <sup>36,48,59,60</sup>

$$V_{\rm e(h)}^{\rm DA}(q) = \frac{D_{c(v)}}{\sqrt{2\rho_{\rm d}c_{\rm LA}^2V}} \sqrt{E_{\rm LA}(q)},$$
 (11)

where  $E_{\lambda}(q) = \hbar c_{\lambda} q$  is the phonon energy, V is the quantization volume,  $\rho_{\rm d}$  is the mass density,  $c_{\lambda}$  is the velocity of sound and  $D_{c(v)}$  is the electron (hole) deformation potential.

In non-centrosymmetric crystals such as II–VI polar semiconductors, a strain associated with acoustic phonons can induce a macroscopic electric polarization in the crystal, which is known as the piezoelectric effect. The piezoelectric interaction is given by:<sup>36,37,61</sup>

$$V_{\rm e}^{\rm PA}(q) = V_{\rm h}^{\rm PA}(q) = i \frac{4\pi e}{q^2 \varepsilon_0 \varepsilon_{\rm s}}$$

$$\sum_{\lambda = {\rm LA, TA}} \sum_{l,j,k} \sqrt{\frac{\hbar}{2\rho_{\rm d} V c_{\lambda} q}} q_k e_{k,lj} \xi_l(\lambda, q) q_j$$
(12)

The piezoelectric constant  $e_{kij}$  is a third rank tensor, and the subscripts  $l_{ij}$  or k are for (x,y,z). In a zinc blende structure semiconductor such as CdSe, there is only one nonzero independent piezoelectric constant  $e_{14} = e_{25} = e_{36}$ .  $\xi_{\rm l}(\lambda,q)$  is the unit polarisation vector,  $\varepsilon_{\rm s}$  is the static dielectric constant,  $\varepsilon_{\rm 0}$  denotes the vacuum susceptibility, while e represents the elementary charge. Notably, the piezoelectric coupling would lead to an anisotropy that is, however, usually neglected. Instead, an effective isotropic model is constructed that is obtained by averaging over the angles.  $^{36,37}$  In the calculation of the acoustic scattering rate, we have assumed that  $E_{\lambda}(q) \ll K_{\rm B}T$ , so that we have  $N_{\lambda}(E_{\lambda},T) \sim \frac{K_{\rm b}T}{E_{\lambda}(q)} \gg 1$ .

The coupling to optical phonons has contributions from both the longitudinal optical (LO) polar-Fröhlich interaction and the nonpolar optical interaction through a zero order optical deformation potential. The contribution of polar transverse optical (TO) phonons in polar crystals (e.g. II–VI semiconductors) to the Fröhlich interaction can in general be ignored, because TO phonons produce negligible electric fields, whereas longitudinal optical (LO) phonons produce sizeable electric fields along the direction of phonon propagation. <sup>36,37</sup> The interaction with the polar LO phonon, which originates from the macroscopic electric field set up by

its lattice vibration, is described by the Fröhlich interaction. For bulk three-dimensional systems, the amplitude of the long-range 3D Fröhlich interaction is given by (the same for electrons and holes):<sup>36,48</sup>

$$V_{\rm e}^{\rm LO,Fr}(q) = V_{\rm h}^{\rm LO,Fr}(q) = i \frac{1}{q} \sqrt{\frac{e^2 E_{\rm LO}(q)}{2V \varepsilon_0} \times \left(\frac{1}{\varepsilon_{\infty}} - \frac{1}{\varepsilon_{\rm s}}\right)}$$
(13)

where  $\varepsilon_{\infty}$  is the high-frequency and  $\varepsilon_{\rm s}$  is the static dielectric constant of CdSe. The polar-optical coupling with longitudinal optical phonons, or Fröhlich interaction, is fundamentally affected by the dimensionality of the system. <sup>48,62,63</sup> In quasi 2D materials, based on atomic Born effective charges, the Fröhlich interaction is given by: <sup>48,62,63</sup>

$$\begin{split} &V_{\rm e}^{\rm LO,Fr}(q) = V_{\rm h}^{\rm LO,Fr}(q) \\ &= i \frac{1}{Q} \sqrt{\frac{e^2 E_{n,\rm LO}(q)}{2 V \varepsilon_0} \times \left(\frac{1}{\varepsilon_\infty} - \frac{1}{\varepsilon_{\rm s}}\right)} \cdot {\rm erfc} \left[\frac{Q \sigma}{2}\right] \end{split} \tag{14}$$

The inclusion of the complementary error function  $\operatorname{erfc}\left[\frac{Q\sigma}{2}\right]$ , where  $\sigma$  is the effective width of the electronic Bloch states (see the ESI†), reflects the constrained interaction of LO phonons with charge carriers in two-dimensional materials. Since Fermi's Golden Rule requires an energy continuum, the LO phonon energy is approximated by<sup>13,40</sup>

$$E_{n,\text{LO}}(q) = \sqrt{\hbar^2 \omega_{\text{Bulk},\text{LO}}^2 - \beta_{\text{LO}}^2 \hbar^2 q_n^2}.$$
 (15)

In the narrow thickness platelets, and due to the fact that there is no common frequency domain for optical modes with the vibration modes of the organic ligands and host polymer, in which the platelets are embedded, we assume that  $q_z=q_n=\frac{n\pi}{d}$ , where d=4.5 ML. This is not the case for the acoustic phonon for which we take into account propagating phonon modes in the z-direction (thickness direction). Here  $\beta_{\rm LO}$  is the LO-phonon dispersion parameter and  $\hbar\omega_{\rm Bulk,LO}$  is given by:<sup>13,40</sup>

$$\hbar\omega_{\rm Bulk,LO} = \alpha + \gamma \, \cos\left(\frac{\pi q}{q^{\rm X}}\right) \tag{16}$$

Here  $\alpha=\frac{\hbar\omega_{\mathrm{LO}}^{\Gamma}+\hbar\omega_{\mathrm{LO}}^{\mathrm{X}}}{2}$  and  $\gamma=\frac{\hbar\omega_{\mathrm{LO}}^{\Gamma}-\hbar\omega_{\mathrm{LO}}^{\mathrm{X}}}{2}$  and hence  $E_{\mathrm{n,LO}}(q)$  can be rewritten as:

$$E_{n,\text{LO}}(q) = \sqrt{\left(\alpha + \gamma \cos\left(\frac{\pi q}{q^{X}}\right)\right)^{2} - \hbar^{2} \beta_{\text{LO}}^{2} q_{n}^{2}}$$
 (17)

In a semiconductor in principle phonon scattering can also occur by a zero-order optical deformation potential  $D_{\rm opt}$ . The interaction of the exciton with nonpolar optical phonons (LO and TO) can be described by<sup>48,61</sup>

$$V_{\rm e}^{\rm NP}(q) = V_{\rm h}^{\rm NP}(q) = \sum_{\lambda = {
m LO, TO}} \sqrt{\frac{\hbar}{2MN\omega_{\lambda}}} D_{
m opt},$$
 (18)

where M is the total atomic mass within the unit cell and N is the number of unit cells.  $D_{\mathrm{opt}}$  is the zero-order optical defor-

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Table 1 Material parameters used in our theoretical modeling

$\beta_{LO} = 2.97 \times 10^3 \text{ ms}^{-1} \text{ (ref. 40)}$	$\omega_{LO}^{\Gamma} = 0.038 \text{ fs}^{-1} \text{ (ref. 72)}$
$\omega_{LO}^{X} = 0.0396 \text{ fs}^{-1} \text{ (ref. 72)}$	$m_{\rm e} = 0.22 m_0  ({\rm ref.}  23)$
$C_{LA} = 3.63 \text{ km s}^{-1} \text{ (ref. 73)}$	$C_{\rm TA} = 1.56 \; {\rm km \; s^{-1}} \; ({\rm ref. \; 37})$
$m_{\rm h} = 0.41 m_0  ({\rm ref.}  23)$	$D_{\rm c} = -6 \text{ eV (ref. 74 and 75)}$
$\rho_{\rm d} = 5.82 \ {\rm g \ cm}^{-3} \ ({\rm ref.} \ 13)$	$D_{\rm v} = -3 \text{ eV (ref. 74 and 75)}$
$\varepsilon_{\infty} = 7.9 \text{ (ref. 6)}$	$\varepsilon_{\rm s}$ = 9.4 (ref. 6)
$D_{\text{opt}} = 1 \times 10^9 \text{ eV cm}^{-1} \text{ (ref. 64 and 65)}$	$\sigma = 4.45 \text{ Å (ref. 13)}$
$e_{14} = 0.16 \text{ C m}^{-2} \text{ (ref. 76)}$	

mation potential constant. Notably a value for wurtzite CdSe (see Table 1) is used in our calculations, since there are no values available for ZB CdSe in literature. 64,65 Regarding the importance of nonpolar TO modes in optical deformation potential interaction: as e.g. done in ref. 66 and 67 we ignore the transverse-longitudinal optical mode splitting in zinc blende, as long as short range interaction is considered, e.g. for the optical deformation potential interaction. Hence we include in our calculation the LO/TO Mode. Since the above assumption is made, all optical modes have the same LO energy and are summed up in our calculation to an effective number, labeled LO.

For phonon scattering processes, the matrix elements are evaluated with the corresponding wave functions. In the expressions of the scattering rate (eqn (4)+(5)), the exciton wavefunctions  $\Psi_{\rm X}^{\rm i(f)}$  and the energies  $E_{\rm X}^{\rm i(f)}$  are the solutions of the following Schrödinger equation:

$$\left(\sum_{j=e,h} H_j(z_j) + \frac{p_j^2}{2m_j} + V_j(\rho_j) + \widehat{V}_c(\rho_e - \rho_h)\right)$$

$$\Psi_X(r_e, r_h) = E_X \Psi_X(r_e, r_h)$$
(19)

Here  $H_i(z_i)$  is the single electron (hole) Hamiltonian in the zdirection (perpendicular to the layers of the NPLs),  $p_i = -i\hbar \nabla_{p_i}$ are the in plane momentum operators,  $m_i$  is the in-plane mass of carrier j, and  $V_i(\rho_i)$  are the confinement potentials of the electron and hole.  $\hat{V}_{c}(\rho_{e}-\rho_{h})$  is the nonlocally screened electron-hole interaction originating from the change in the dielectric environment, given by a Rytova-Keldysh potential. 13,68-71 For the calculation of the matrix element, we factorize the wave function of the exciton into an in-plane part  $\xi_{\rm p}(\rho_{\rm e}, \rho_{\rm h})$  and z-confinement related functions  $\chi_{\rm e}(z_{\rm e})$  and  $\chi_{\rm h}(z_{\rm h})$ , the solutions of the single electron (hole) Hamiltonian for the lowest electron and heavy-hole sublevel. The solutions of the single electron (hole) Hamiltonian in the z-direction are:

$$\Psi_{\rm X}(r_{\rm e},r_{\rm h}) = \chi_{\rm e}(z_{\rm e})\chi_{\rm h}(z_{\rm h})\xi_{\rm p}(\rho_{\rm e},\rho_{\rm h})$$

Furthermore, using the relative  $\rho = \rho_e - \rho_h$  and center of mass coordinates  $R_{\rm X} = \frac{m_{\rm e}\rho_{\rm e} + m_{\rm h}\rho_{\rm h}}{M_{\rm X}}$  we separate the center of mass and the relative motion of the exciton (weak confinement limit), i.e. assuming that the NPLs are more quantum well like, as this paper aims for larger platelets (for more details see ref. 13 and 68). Hence the in-plane exciton wave function can be written as the product of the exciton center of mass and the relative wave function  $\xi_{\mathrm{p}}(\rho_{\mathrm{e}},\rho_{\mathrm{h}})=\phi_{\hat{n}l}^{\mathrm{rel}}(\rho,\theta)\psi_{n_{\mathrm{x}},n_{\mathrm{y}}}^{\mathrm{CM}}(X,Y)$ . Here, the relative wave function  $\phi^{\rm rel}_{\tilde{n}l}(\rho,\theta)=\sum\limits_{n,l}C(n,l)\varphi_{n,l}(\rho,\theta)$  is the solution of the relative Hamiltonian and can be expanded in terms of 2D hydrogenic states  $\varphi_{n,l}(\rho, \theta)$ .  $\tilde{n}, l \ (n \in \mathbb{N}^*)$  represents the quasi hydrogenic series obtained for the exciton using a Rytova-Keldysh potential. Using the exciton wave function above and expressing the in-plane position vectors of the electrons and holes as a function of the center of mass  $R_x$  and relative coordinates  $\rho$ , the resulting matrix element in eqn (10) can be rewritten as

$$\mathbb{G}_{\lambda,\mathrm{f}}(q) = \mathbb{I}(q_z) \mathbb{M}^{\mathrm{CM}}\big(q_x,q_y\big) \big(V_\mathrm{e}^\lambda(q) \mathbb{M}_\mathrm{e}^{\mathrm{rel}}(Q_\mathrm{e}) - V_\mathrm{h}^\lambda(q) \mathbb{M}_\mathrm{h}^{\mathrm{rel}}(Q_\mathrm{h})\big), \ \ (20)$$

where the Fourier transformed projection of the relative wave function overlap integral on the electron/hole coordinate - calculated numerically - is defined as:

$$\begin{split} \mathbb{M}_{\mathrm{e}(\mathrm{h})}^{\mathrm{rel}}\left(Q_{\mathrm{e}(\mathrm{h})}\right) &= \langle \phi_{\tilde{n}l}(\rho)|e^{\mp iQ_{\mathrm{e}(\mathrm{h})}\rho}|\phi_{\tilde{n}'\tilde{l}'}(\rho)\rangle = \\ &\sum_{n,l}\sum_{n',l'}C(n,l)C(n',l')2\pi i^{l'-l}\int_{0}^{\infty}\varphi_{n,l}\varphi_{n',l'}J_{l'-l}\left(\frac{m_{\mathrm{h}}(e)}{M_{\mathrm{X}}}Q\rho\right)\rho\mathrm{d}\rho \end{split} \tag{21}$$

$$\text{Here, } Q_{\mathrm{e}(\mathrm{h})} &= \frac{m_{\mathrm{h}(\mathrm{e})}}{M_{x}}Q = \frac{m_{\mathrm{h}(\mathrm{e})}}{M_{x}}\sqrt{q_{x}^{2}+q_{y}^{2}},$$

$$\mathbb{I}_{\mathrm{e}}(q_{z}) &= \mathbb{I}_{h}(q_{z}) = \mathbb{I}(q_{z}) = \left\langle \chi_{\mathrm{e}(\mathrm{h})}\left(z_{\mathrm{e}(\mathrm{h})}\right)\Big|e^{iq_{z}z_{\mathrm{e}(\mathrm{h})}}\Big|\chi_{\mathrm{e}(\mathrm{h})}\left(z_{\mathrm{e}(\mathrm{h})}\right)\right\rangle \\ &= \frac{\pi^{2}\sin\left(\frac{q_{z}L_{z}}{2}\right)}{\frac{q_{z}L_{z}}{2}\left[\pi^{2}-\left(\frac{q_{z}L_{z}}{2}\right)^{2}\right]}, \tag{22}$$

This expression shows that the squared matrix element decreases strongly for  $q_z>rac{2\pi}{L_{\scriptscriptstyle 7}}.$  This reflects a general feature of electron (hole)-phonon interaction: the coupling is weak when along a given direction the phonon wavelength is small compared to the spatial variation of the electron (hole)wave function. The center of the mass matrix element is given by:

$$\mathbb{M}^{\mathrm{CM}}(q_x, q_y) = \left\langle \psi_{n_x, n_y}^{\mathrm{CM}}(X, Y) \middle| e^{i(q_x x + q_y y)} \middle| \psi_{n_x, n_y}^{\mathrm{CM}}(X, Y) \right\rangle. \tag{23}$$

In the case of infinite confinement potential, the center of the mass matrix element is given by  $\mathbb{M}^{CM}(q_x,q_y) =$  $\mathbb{M}^{CM}(q_x)\mathbb{M}^{CM}(q_y)$ , where  $\mathbb{M}^{CM}(q_{x(y)})$  is defined by the following expression:

$$\begin{split} \mathbb{M}^{\text{CM}}(q_{x(y)}) &= \frac{\sin\left(\frac{n_{x(y)}\pi + n'_{x(y)}\pi + q_{x(y)}L_{x(y)}}{2}\right)}{n_{x(y)}\pi + n'_{x(y)}\pi + q_{x(y)}L_{x(y)}} \\ &+ \frac{\sin\left(\frac{n'_{x(y)}\pi + q_{x(y)}L_{x(y)} - n_{x(y)}\pi}{2}\right)}{n'_{x(y)}\pi + q_{x(y)}L_{x(y)} - n_{x(y)}\pi} \\ &+ \frac{\sin\left(\frac{n_{x(y)}\pi - n'_{x(y)}\pi + q_{x(y)}L_{x(y)}}{2}\right)}{n_{x(y)}\pi - n'_{x(y)}\pi + q_{x(y)}L_{x(y)}} \\ &+ \frac{\sin\left(\frac{n_{x(y)}\pi + n'_{x(y)}\pi - q_{x(y)}L_{x(y)}}{2}\right)}{n_{x(y)}\pi + n'_{x(y)}\pi - q_{x(y)}L_{x(y)}}. \end{split} \tag{24}$$

For the case of laterally unconfined wells (for example laterally infinite TMDCs), the center of the mass matrix element reduces to the conservation of the crystal

momentum  $\mathbb{M}^{\text{CM}}(q_x,q_y)=2\pi A\delta_{K_X^i-K_X^f,Q}$ , where  $K_X^{i(f)}$  is the initial (final) in-plane free center of the mass wave vector.

Finally, Table 1 shows the material parameters used in the calculations.

# **Author contributions**

A.W.A. designed and performed measurements, analyzed data, and carried out calculations. A.W.A and S.A. wrote the paper. S.A. and S.J. did theoretical modeling. A.W.A. contributed to modeling. S.H., M.T.Q., N.O., and U.W. contributed to discussion and interpretation of results.

# Conflicts of interest

There are no conflicts to declare.

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