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Ab initio nanofluidics: disentangling the role of the energy landscape and of density correlations on liquid/solid friction†

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Despite relevance to water purification and renewable energy conversion membranes, the molecular mechanisms underlying water slip are poorly understood. We disentangle the static and dynamical origin of water slippage on graphene, hBN and MoS₂ by means of large-scale *ab initio* molecular dynamics. Accounting for the role of the electronic structure of the interface is essential to determine that water slips five and eleven times faster on graphene compared to hBN and to MoS₂, respectively. Intricate changes in the water energy landscape as well as in the density correlations of the fluid provide, respectively, the main static and dynamical origin of water slippage. Surprisingly, the timescales of the density correlations are the same on graphene and hBN, whereas they are longer on MoS₂ and yield a 100% slowdown in the flow of water on this material. Our results pave the way for an *in silico* first principles design of materials with enhanced water slip, through the modification of properties connected not only to the structure, but also to the dynamics of the interface.

Nanofluidics has attracted increasing attention over the years for its potential to remedy future shortages of clean water and for the generation of renewable energy.^{1–3} The miniaturization of devices and the accurate characterization of nanoscale transport have led to the development of extremely efficient nanotube and Å-scale slits membranes for water desalination, purification and osmotic energy conversion membranes.^{4–7} At the nanoscale specific materials properties, pore chemistry and confinement geometry may all have a strong impact on nanofluidic transport, and therefore on the performance of desalination and osmotic energy conversion membranes. In

the case of water transport through nanotubes, there is mounting evidence that slippage is qualitatively different between carbon and boron nitride materials,⁸ a result that hints at the role of the electronic structure on flow.⁹ Despite fundamental insights provided by transport experiments across single pores, connecting the electronic structure of materials to water slippage under confinement remains an open challenge. Computer simulations, and in particular molecular dynamics based on empirical force fields (FFMD) are instrumental to provide insights into the atomistic mechanisms underlying transport in nanofluidics.^{6,10–17} Yet, the role of the electronic structure is not accounted for in these studies and FFMD results are often sensitive to the choice of the interaction parameters. Additionally, the lack of transferability of force-field parameters between different interfaces poses a problem when comparing slippage on different materials. The development of force fields capable of accurately describing the structure and energetics of water interacting on two-dimensional materials is an active area of research, where recently machine learning is playing a prominent role.^{18,19} Nevertheless, to be able to compare water slippage between different nanofluidic interfaces on equal footing, it is essential to resort to *ab initio* molecular dynamics (AIMD), where the electronic structure is accounted for with density functional theory (DFT). Due to the formidable challenges associated with carrying out AIMD simulations of nanofluidic transport, these types of studies have been scarce.^{20–22}

Here, we tackle this challenge in full strength by using AIMD to investigate the slippage of water confined between two-dimensional materials. We concentrate our efforts on connecting the atomistic features and electronic structure of the interface to the friction of water on graphene, hBN and MoS₂ sheets, motivated by a number of experimental works on nanofluidic transport at such interfaces.^{8,23–25} We find that the friction on graphene is about five and eleven times smaller than on hBN and MoS₂, respectively. The structure of water in the direction perpendicular to the sheets is very similar across the three materials. Yet, slight changes in the corrugation of the

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water energy landscape of at most a few $k_B T$ in the direction parallel to the sheets impact the friction dramatically. Interestingly, slippage is also controlled by the density correlations of the contact layer, and their time relaxation provides the main dynamical origin of the friction. These results illustrate how a delicate interplay of interfacial forces, which are governed by the electronic structure of materials, can have a tremendous impact on nanofluidic transport. Additionally, favourable comparison with experimental slip lengths on carbon nanotubes with small curvature and with BN nanotubes illustrates the relevance of the electronic structure on nanofluidic transport.

We performed a series of extensive AIMD simulations of water confined between graphene, hBN and MoS₂ sheets for different confinement widths, as well as with water films supported on the three types of sheets for systems containing up to 2000 atoms. AIMD simulations were carried out in the Born–Oppenheimer approximation with the electronic structure computed at the DFT level using the optB88-vdW exchange–correlation functional^{26,27} and the dynamics was propagated in the canonical ensemble for about 100 ps at 330 K. Snapshots of the simulated systems for MoS₂ with different confinements are shown in Fig. 1.

We start our discussion on the structural properties of water under confinement. A key property of confined fluids is their density profile as a function of the distance from the

sheets,²⁸ which is shown in Fig. 1. The water density profiles were computed with respect to the instantaneous height between each fluid molecule and the nearest sheet's atom, in the spirit of ref. 29 (ESI†). There is a strong similarity in the layering of water between the three materials for each confinement height. The properties of the first water layer, so-called contact layer, are most relevant to understand nanofluidic water slip.³⁰ Therefore, particular emphasis is placed on the understanding of its structure. Except for the smallest confinement width, the contact layer density peaks at approximately 3.5 g cm^{-3} , regardless of the type of material. For confinement heights between 1.2 and 1.5 nm (Fig. 1f–h) two additional smaller peaks appear beyond the contact layer. Gradually less pronounced density oscillations are also visible beyond the first two layers for confinement widths between 2.0 and 3.0 nm (Fig. 1j–p). A bulk liquid region is almost recovered in systems whose confinement width reaches about 3.0 nm (Fig. 1n–p). The differences observed in the first density peaks seen in Fig. 1(b)–(d) and in the second peaks in Fig. 1(f)–(h) result from commensurability between the size of the water molecules and the confinement width of each system,³¹ along with differences in the magnitude of the water/sheet interactions.§

We now turn to water slip, as the most relevant contribution of this work. At liquid–solid interfaces where the major contribution to the water/surface interaction comes from dispersion forces – such as those considered here – the tangential velocity of the fluid in contact with the solid, so-called slip velocity v_{slip} , is non-zero and the friction force parallel to the flow is proportional to the slip velocity *via* the so-called friction coefficient λ , following the relation $F = (\mathcal{A}\lambda) \times v_{\text{slip}}$,^{32,33} with \mathcal{A} the surface area. Whereas the relation of proportionality between the total force acting on the liquid and the slip velocity can be used to calculate λ from nonequilibrium molecular dynamics simulations,³⁴ here we apply the following Green–Kubo relation and compute the friction coefficient from the equilibrium fluctuations of the force acting on the liquid extracted from our equilibrium AIMD trajectories:^{33,35}

$$\lambda = \frac{1}{\mathcal{A}k_B T} \int_0^\infty \langle F(t)F(0) \rangle dt, \quad (1)$$

where $F(t)$ is the total force acting on the liquid along the x or y direction parallel to the sheets at time t , \mathcal{A} is the surface area of the sheets. For finite size systems, the integral in eqn (1) decays to zero as $t \rightarrow \infty$, but the equilibrium value of the friction coefficient can be obtained when the integral reaches a plateau value at intermediate times^{22,36} (ESI†). Fig. 2 shows the friction coefficient for different confinement widths and also for the liquid film configurations on graphene, hBN and MoS₂.

It can be seen that water flow is fastest on graphene, as λ on graphene is about 5 times smaller compared to hBN and about 11 times smaller than MoS₂. Additionally, there is no apparent effect of confinement on friction, as λ is approxi-

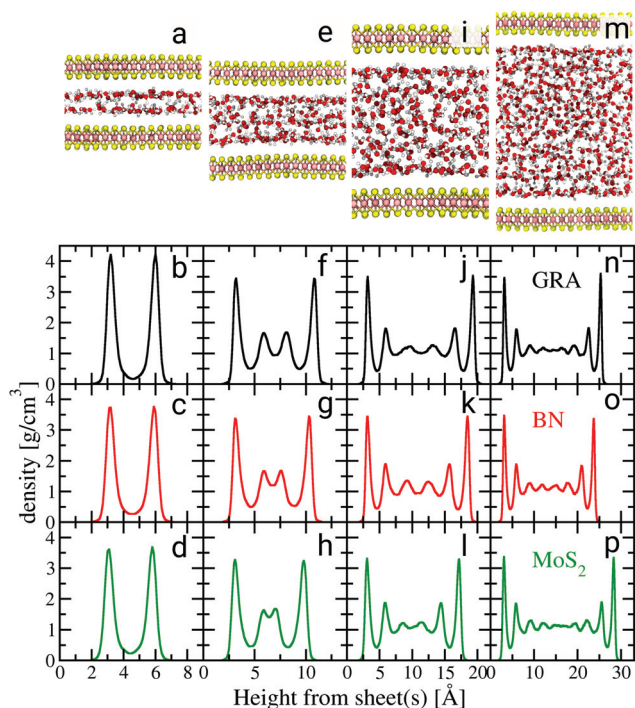


Fig. 1 Water density profiles for different confinement heights. Black, red and green graphs are density profiles for graphene (GRA), hBN and MoS₂, respectively. The snapshots in (a), (e), (i) and (m) illustrate the configurations of water confined between MoS₂ sheets for different confinements. The density profiles for the supported water films are shown in the ESI†.



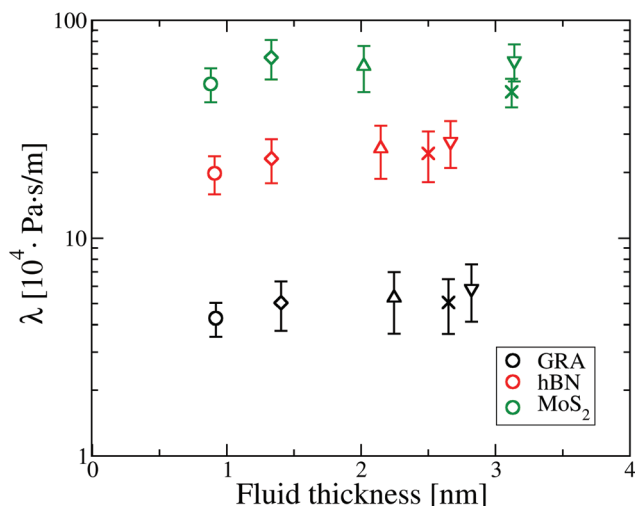


Fig. 2 Friction coefficient λ for different fluid thicknesses. \circ refers to a fluid thickness of 0.9 nm, \diamond is for 1.5 nm, \triangle for 2 nm, ∇ for a confinement between 2.5 and 3.0 nm and \times is for the water film configurations which have a thickness between 2.5 and 3.2 nm. In this and subsequent plots the error bars correspond to the statistical error within a 95% confidence level, computed over about 20 blocks of data along the armchair and zigzag axis, for a total of 40 blocks.

mately constant as a function of the fluid thickness for all materials.

To provide mechanistic insights into the observed trends of the friction coefficient, eqn (1) is formulated in terms of the second moment of the force $\langle F^2 \rangle$ and the force correlation time τ_F :

$$\lambda = \frac{1}{Ak_B T} \langle F^2 \rangle \times \tau_F, \quad (2)$$

where

$$\tau_F = \int_0^\infty \frac{\langle F(0)F(t) \rangle}{\langle F^2 \rangle} dt. \quad (3)$$

From eqn (2) it is possible to disentangle the dependence of the friction coefficient on static and dynamical properties of the interface, where $\langle F^2 \rangle$ and τ_F entail a static and dynamical contribution, respectively. We first illustrate the dependence of λ on $\langle F^2 \rangle$ as shown in Fig. 3 for the systems considered. A clear correlation between the friction and the mean squared force is observed: upon going from graphene to hBN to MoS₂ $\langle F^2 \rangle/A$ increases, and so too does λ , for all confinement widths. Based on dimensional grounds, the dependence of λ on $\langle F^2 \rangle/A$ can be further expressed as $\langle \Delta V^2 \rangle/a_0^4$, where $\langle \Delta V^2 \rangle$ is a measure of the corrugation of the potential energy of the fluid in the contact layer and a_0 is the lattice constant of the sheets.^{11,30} The corrugation of the water energy landscape can be estimated from the calculation of the free energy profile defined as $\Delta G(x,y) = -k_B T \log[P_O(x,y)/P_O(x_{\max},y_{\max})]$, where $P_O(x,y)$ is the two-dimensional probability distribution of an oxygen atom in a water molecule in the contact layer and the subscript “max” indicates the point where the probability is at the maximum. The free energy profile thus computed is shown in Fig. 3(b)–(d).

The level of corrugation can be extracted from the free energy barrier, obtained as the maximum in ΔG , which is of about 0.01 eV, 0.02 eV and 0.05 eV for graphene, hBN and MoS₂, respectively. Whereas the free energy barriers in graphene and hBN are smaller than the thermal energy at room temperature (about 0.025 eV), the free energy barrier on MoS₂ is about 0.05 eV, and therefore larger than $k_B T$, indicating definitely a more corrugated overlayer. The increased level in the corrugation of the free energy explains the observed relation between λ and $\langle F^2 \rangle/A$ and it provides a static and structural origin for the observed behaviour of the friction coefficient. Looking closely at Fig. 3, some changes in the dynamics can be anticipated by noting that, while λ and $\langle F^2 \rangle$ appear to be proportional for graphene and hBN, the friction of water on MoS₂ is too large or it to be explained simply based on its dependence on $\langle F^2 \rangle$.

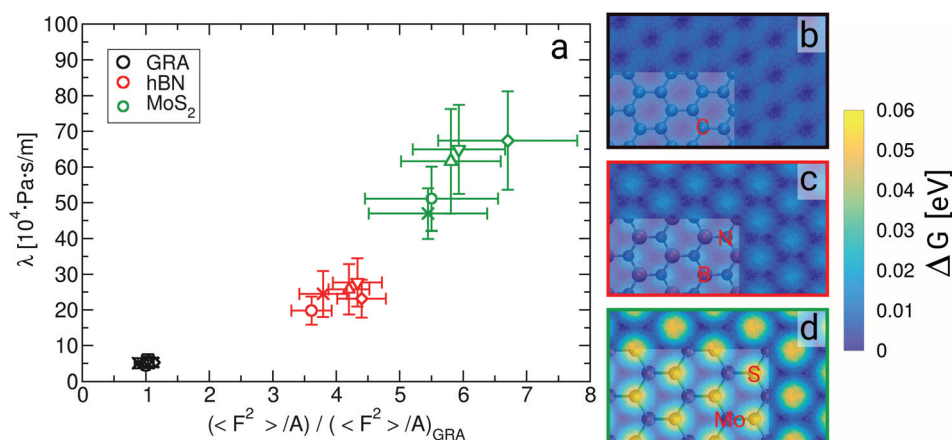


Fig. 3 Friction coefficient λ as a function of $\langle F^2 \rangle/A$ (a), and free energy landscape of water in the contact layer for (b) graphene, (c) hBN and (d) MoS₂, where snapshots of the sheets are superimposed on part of the graphs. In (a) $\langle F^2 \rangle/A$ is normalized by its value on graphene at a confinement width of about 0.9 nm, and the different symbols refer to systems with different fluid thicknesses, as per Fig. 2.



Indeed, we provide evidence of an intriguing mechanism underlying friction, inherent to the dynamics of the water contact layer. To this end we plot λ as a function of the force correlation time τ_F for the systems discussed so far, see Fig. 4. The most apparent feature is that τ_F is approximately 50 fs for graphene and hBN, considering all fluid thicknesses, whereas it is about 100 fs for MoS₂. The larger value of τ_F indicates a slower relaxation of the lateral force acting on the fluid at the water–MoS₂ interface compared to the other two interfaces. The dependence of friction on τ_F can be tuned by changing the amplitude of the bond length oscillations of the sheets,¹⁵ and by modifying the magnitude of the electrostatic and dispersion interactions (see ESI†). Because depositing two-dimensional materials on different substrates may lead to a change in the electrostatic and/or van der Waals interactions at the interface, it is possible to test experimentally this dependence.^{25,37,38}

In order to provide further insights into the molecular origin of this phenomenon, eqn (1) is approximated in terms of the structure and dynamics of the liquid contact layer (ESI†):^{30,39}

$$\lambda \approx \frac{N_1}{Ak_B T} f_{q_{\parallel}}^2 \times S(q_{\parallel}) \times \tau_{\rho}, \quad (4)$$

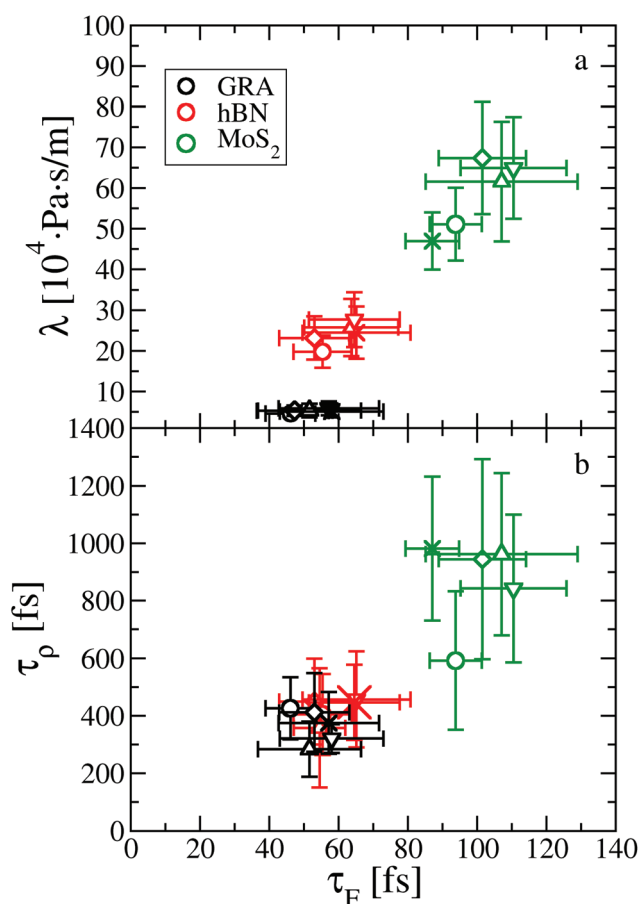


Fig. 4 Dynamical origin of water slip on two-dimensional materials, as shown by the dependence (a) of the friction coefficient λ on the force correlation time τ_F , and (b) of the density correlation time τ_{ρ} on τ_F . The same symbols are used as in Fig. 2.

with

$$\tau_{\rho} = \int_0^{\infty} dt \frac{\langle \rho_{q_{\parallel}}(t) \rho_{-q_{\parallel}}(0) \rangle}{\langle \rho_{q_{\parallel}}(0) \rho_{-q_{\parallel}}(0) \rangle}, \quad (5)$$

where N_1 is the number of molecules in the contact layer, q_{\parallel} the wave-vector characterizing the wall corrugation with a magnitude $q = 2\pi/a_0$, where $f_{q_{\parallel}}$ is the first Fourier component of the force between a water molecule and the underlying sheet, $S(q_{\parallel}) = \frac{1}{N_1} \langle \rho_{q_{\parallel}} \rho_{-q_{\parallel}} \rangle$ the static structure factor, and τ_{ρ} the density correlation time, both defined in terms of the Fourier component of the fluid density $\rho_{q_{\parallel}}(t) = \sum \exp(iq_{\parallel} \cdot r_j(t))$.

Altogether, eqn (2) and (4) imply a correlation between the force correlation time and the density correlation time, *i.e.* $\tau_F \sim \tau_{\rho}$. As it can be seen in Fig. 4(b), both τ_F and τ_{ρ} are approximately twice as small in graphene and hBN compared to MoS₂. The apparent correlation between τ_F and τ_{ρ} provides the main explanation for the different dynamical contribution to the friction. The density correlation time on graphene and hBN is smaller than on MoS₂ because (i) the density modes on the former materials are associated with a smaller lattice constant a_0 and therefore decay more rapidly⁴⁰ and (ii) the collective diffusion of the fluid probed at a specific wave-vector ($D_{q_{\parallel}}$) is larger on graphene and hBN compared to MoS₂. This can be seen by expressing τ_{ρ} in terms of the wave-vector and of $D_{q_{\parallel}}$ as $\tau_{\rho} = 1/(D_{q_{\parallel}} q^2)$.³⁰ By taking τ_{ρ} for graphene (or hBN) and MoS₂ to be about 400 fs and 1000 fs, respectively, we can extract $D_{q_{\parallel}}$ to be about $0.38 \text{ \AA}^2 \text{ ps}^{-1}$ for graphene and hBN and $0.25 \text{ \AA}^2 \text{ ps}^{-1}$ for MoS₂. As a result, we find that the differences in the lattice constant (*i.e.* the q^{-2} term), and in the collective diffusion coefficient ($D_{q_{\parallel}}$ term) equally contribute to the observed behaviour of τ_{ρ} . In the ESI (see Fig. S13†) we also show that stretching and compressing the underlying lattice has a strong effect on τ_{ρ} , but the larger MoS₂ lattice constant is not sufficient to explain alone the larger value of τ_{ρ} on MoS₂. Instead, there is a remaining contribution to τ_{ρ} on MoS₂ beyond the obvious q^{-2} dependence, which arises from the slower collective diffusion of water on MoS₂ compared to the other two materials, as it can be seen by compressing MoS₂ to approximately the same lattice constant of hBN and graphene. Despite the evident correlation between τ_F and τ_{ρ} , the latter is smaller by almost a factor of 10. A possible reason for the discrepancy is that the density correlation time results from an average over the density modes for the whole contact layer, whereas the force correlation time is more sensitive to those modes closer to the contact layer.³⁰ Note also that the derivation of eqn (4) is based on truncating the Fourier expansion of the potential energy landscape of the wall, but higher order modes could contribute.

Our results can be used in practice to test experimentally a possible dependence of the viscosity on confinement, which remains still an open question.^{31,41–44} Indeed, liquid–solid slip is most often characterized experimentally through the slip length b , defined as the ratio between the slip velocity v_{slip} and



the shear rate $\dot{\gamma}$ at the interface: $b = v_{\text{slip}}/\dot{\gamma}$. Because at the interface the viscous shear stress $\eta\dot{\gamma}$ (with η the shear viscosity) is equal to the wall shear stress λv_{slip} , the slip length can be expressed as the ratio between the viscosity and the friction coefficient:⁴⁵ $b = \eta/\lambda$. Using the experimental viscosity of bulk water ($\eta = 10^{-3}$ Pa s), we obtain on average a slip length of 19.6 ± 1.9 nm, 4.0 ± 0.4 nm and 1.8 ± 0.2 nm for graphene, hBN and MoS₂, respectively. As we report little to no effect of friction on confinement in all three materials, any dramatic change in the slip length measured in experiments can be ascribed to a change in the viscosity, *via* the expression $b = \eta/\lambda$. The surface force apparatus, atomic force microscopy as well as scanning tunneling microscopy are some of the most promising techniques to investigate changes in the slip length and in the viscosity under confinement.^{25,46}

Additionally, measurements of the slip length in nanotubes using optical microscopy have shown that water essentially does not slip inside BN nanotubes, whereas it does slip inside carbon nanotubes, the slip length being larger in nanotubes with smaller radii.⁸ In the carbon nanotubes with the lowest curvature (100 nm in diameter), the reported slip length of about 23 nm compares favorably with our predicted value for graphene, 19.6 ± 1.9 nm. For BN nanotubes, no slip is detected above the detection limit of 5 nm, consistent with our prediction of 4.0 ± 0.4 nm. This comparison indicates that the difference in the slip length between carbon and BN nanomaterials may originate to a large extent from the different underlying corrugation of the energy landscapes of these materials. Nevertheless, the proclivity for adsorption of hydroxide ions may provide an additional reason for the smaller slip length on BN nanotubes.^{8,22,47–49} Carrying out experiments at different levels of pH would likely provide a definitive answer to this question.

It has been pointed out before that there is a large uncertainty over the simulated slip length of water on graphene or graphite, with values between 1 and 80 nm.⁵⁰ In this work we have contributed to reduce this uncertainty, also given the good agreement with recent experiments for large carbon nanotubes, stressing the relevance of *ab initio* methods for studies of liquid/solid friction. Instead, using previously reported water/sheet interaction potentials, the slip length on the three materials obtained with FFMD may be up to five times larger compared to obtained AIMD (ESI†). Moreover, the mechanisms involved in water slippage may critically depend on the particular choice of the force field, as seen in the strong dependence of τ_F and λ on the values of the Lennard-Jones interaction and in the values of the partial charges (ESI†). This indicates that empirical interaction potentials, usually developed to describe bulk systems and sometimes combined with *ad hoc* mixing rules to describe interfaces, may be unreliable for the comparison of slippage mechanisms across different systems.

Overall, in this work we have unraveled the dependence of water slippage on the energy landscape corrugation and on the correlation time of the density fluctuations of water on three prototypical two-dimensional materials. Obtaining such funda-

mental mechanistic insights from 100 ps-long AIMDs through a systematic investigation of water slippage under different confinement regimes on different materials was not possible just a few years ago, when a first AIMD study of liquid/solid friction appeared,²¹ and has been made possible thanks to recent advances in computational power and algorithm developments.⁵¹ With the aim of designing materials with faster water slip one can envision different mechanisms to further reduce the friction, not only by decreasing the corrugation of the energy landscape but also by reducing the force correlation time. The recent discovery of a few thousands “exfoliatable” two-dimensional materials and the rise of van der Waals layered heterostructures may present a number of additional routes to further improve water slip.^{52–55} So far graphene is the two-dimensional material which exhibits the lowest friction to water. It remains to be seen whether water slip on newly proposed two-dimensional materials or van der Waals heterostructures can be faster than on graphene. Furthermore, inclusion of non-additive many-body effects may reveal new routes to enhance slip, as a result of repulsive dispersion forces arising from confinement.^{56,57} It will be interesting to extend AIMD studies to other domains of nanofluidics including problems in osmotic energy conversion, in a time where also ionic transport is accessible experimentally under extreme confinement regimes.

Materials and methods

Electronic structure and *ab initio* molecular dynamics

The electronic structure problem was solved using DFT with the CP2K code⁵⁸ with the optB88-vdW density functional. The optB88-vdW functional has been shown to predict accurate interlayer binding and interlayer distances in graphite and bulk hBN,⁵⁹ to give a sufficiently good description of the structure of bulk liquid water^{60,61} and also to accurately capture the relative stability of a water monomer on graphene and hBN on different adsorption sites compared to reference diffusion monte carlo data.^{62,63} Further details on the electronic structure are reported in the ESI.†

AIMD simulations within the Born–Oppenheimer approximation were performed in the canonical ensemble for about 100 ps at 330 K to partly compensate for the overstructuring of water with the optB88-vdW functional.^{60,61} The initial atomic configurations for each system were obtained from pre-equilibrated FFMD trajectories. Additional AIMD and FFMD simulations ensured that our results were not affected by the finite size and time-scales accessible to AIMD and by the type of ensemble chosen (ESI†).

Structural details of the water/sheet interface

The graphene/water and hBN/water interfaces have been modeled using 10×6 orthorhombic cells about 2.5×2.5 nm² large and the MoS₂/water interface has been modelled using 8×4 orthorhombic cells approximately 2.5×2.2 nm² large. The graphene, hBN and MoS₂ lattice constants are about 2.46,



2.50 and 3.15 Å, respectively. The number of confined water molecules was varied between 100 and 500, and the systems spontaneously equilibrated at a given confinement width, between about 0.9 nm and 3 nm, as all atoms were allowed to move. Additionally, simulations on up to *ca.* 3 nm-thick supported water films were carried out, where water is at the interface with the sheets on one side and with vacuum on the other side. Further details on the structure of supported water films and of water under confinement, as well as tests on the size of our simulations are included in the ESI.† These tests also include a comparison on the friction coefficient computed for thinner supported water films, as reported in ref. 21. Overall, they confirm that the results presented so far on water slippage are not altered by changing the lateral cell dimensions and the number of water molecules present in our simulations.

Conflicts of interest

There are no conflicts to declare.

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† k_B being Boltzmann constant and T room temperature.

§ The magnitude of the peaks for the smallest confinement widths (Fig. 1b–d) and the presence of one or two additional peaks beyond the contact layer (Fig. 1f–h) may be marginally affected by the number of water molecules present in our simulations, and as such care must be taken while interpreting these differences in the density profiles.

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