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Frequency dependent multiphase flows on centrifugal microfluidics†

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The simultaneous flow of gas and liquids in large scale conduits is an established approach to enhance the performance of different working systems under critical conditions. On the microscale, the use of gas–liquid flows is challenging due to the dominance of surface tension forces. Here, we present a technique to generate common gas–liquid flows on a centrifugal microfluidic platform. It consists of a spiral microchannel and specific micro features that allow for temporal and local control of stratified and slug flow regimes. We investigate several critical parameters that induce different gas–liquid flows and cause the transition between stratified and slug flows. We have analytically derived formulations that are compared with our experimental results to deliver a general guideline for designing specific gas–liquid flows. As an application of the gas–liquid flows in enhancing microfluidic systems' performance, we show the acceleration of the cell growth of *E. coli* bacteria in comparison to traditional culturing methods.

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Introduction

Flow regimes are mainly determined by the relationship between inertia, viscous, gravitational, and surface related forces. In large dimension fluid channels (*i.e.*, hydraulic diameter >1 mm), gas–liquid flows are mainly classified into slug (*i.e.*, liquid plugs separated by gas pockets), stratified (*i.e.*, gas primarily flows above the liquid), annular (*i.e.*, liquid films flowing on the walls of the conduit), and bubbly flows.¹ Currently, these flows are mostly used to enhance the efficiency of industrial and environmental devices such as increasing the rate of mass and heat transfer² and limiting liquid dispersion.³ The application of the stratified flow is mainly environmental while the slug and annular flows are commonly used in heat exchangers and air pollution control systems *e.g.*, detecting airborne toxic biological and non-biological particles.^{4,5} In these systems establishing gas–liquid flows requires bulky, expensive and often multiple mechanical parts. In micro-scale systems, gas–liquid flows can be employed to enhance chemical reactions occurring in diagnostic devices and drug discovery applications,^{6–10} and enhance the mixing of miscible liquid streams *e.g.*, in micro-reactors for synthesizing nanoparticles.^{7,11}

Micro-scale devices that are developed to perform diagnostics are commonly known as lab-on-a-chip devices. These devices use a lower volume of expensive reagents, perform clinical assays in a shorter time and by the use of liquid storage techniques may be able to automate and integrate diagnostic processes. But, despite significant advances in lab-on-a-chip devices, especially in on-chip storage liquid handling,¹² generating some gas–liquid flows without using bulky equipment has been challenging.^{1,3} This is due to the decrease of gravitational force to surface tension force (*i.e.*, low Bond number). Also, the specific conditions inducing different gas liquid flows in large fluid channels are not necessarily the same in microfluidics.³ Nevertheless, researchers have employed various methods for forming different gas–liquid flows. These techniques are mainly inspired by conventional systems *i.e.*, using external compressors to blow air. For instance, researchers have achieved a stratified flow by using side stream gas to squeeze the liquid streaming in a microchannel.^{13,14} This technique has been used for focusing liquid streams, containing particles and cells in flow cytometry.^{13,15,16} Using a similar approach, an inertial microfluidic system has been introduced to generate stratified flow in order to transfer aerosol particles from air into the liquid phase.¹⁷ The device consists of two separate inlets for pumping liquid and gas into a curved microchannel that was used for migrating particles and allowing for real-time detection. They blew compressed air containing the particles (0.6–2.1 μm) into a liquid channel to form a stratified flow and load the particles. Similar techniques have been used to produce a

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slug flow often in pressure-driven microfluidic systems.^{6–10} In these platforms, liquid and gas have been introduced in microfluidic networks by syringe pumps and an air compressor. A significant application of the slug flow is mixing different reagents in microfluidic systems.¹⁸ The mixing by this technique is tunable and more efficient since the residence time distribution of the liquid is shorter in a slug flow in comparison to a single-phase flow.¹⁹ The residence time distribution is a criterion for measuring the distribution of residence times of different particles in a microchannel. Improving the performance of thermally dependent applications, *e.g.*, PCR and material synthesis, is achievable using slug flow. Due to higher thermal coefficients arising from the convection heat transfer in liquid plugs, the temperature change rate of a segmented flow is always more than that of a continuous flow in the same fluid flow rate.²⁰ The gas–liquid segmented flow circumvents the destabilization of the flow in flow-through PCR in continuous flow systems which occurs due to the generation of the bubbles when the liquid reaches the high-temperature zones. The generated bubbles are pushed into the gas segments due to internal circulation inside the liquid plug which make the slug flow a good choice when rapid thermal processing is required.^{21,22}

In addition to pressure driven microfluidics, centrifugal microfluidic platforms have been recently employed for generating slug flows.^{23,24} In these systems, the air phase is injected into a liquid stream through a sequentially-driven internal pump which is actuated by external magnets during the rotation of the lab-disc.²⁴

Overall, due to high surface tension forces compared to gravitational force in microfluidics the use of bulky accessories has been considered inevitable for generating gas–liquid flows. Here, we report on the exclusive use of artificial gravity available on centrifugal microfluidic platforms to generate and switch between the slug and stratified flows. We experimentally show that both slug and stratified flows can be achieved using centrifugal microfluidic platforms at relatively low rotational speeds. We thoroughly investigate the effects of centrifugal forces on generating different flow regimes and provided an analytical formulation for the prediction of the flow regimes. The analytical formulation is validated by experimental results and can be used as a guideline for designing gas–liquid centrifugal microfluidic systems. Our experiments show that different thicknesses of a stratified flow can be generated by tuning the rotational speed.

Results

Analytical model

Stratification of the liquid streams in different microchannel geometries brings new capabilities in fields that require lamination of the particles along with a superficial mass transfer between the phases. Different results combined generally show that using a simple micro-structure on a

centrifugal microfluidic platform is an effective alternative for producing a wide range of stratified flows. This is useful in applications that require adjustment of the residence time such as thermally dependent reactions, *e.g.*, PCR for DNA amplification by implementing the presented heating methods for centrifugal microfluidics.²⁵ An adjacent stream of the gas phase to the liquid phase can be used for removing the bubbles generated in the liquid passing the high-temperature zones.

We have developed an analytical model that can be used as a tool for designing and developing gas–liquid centrifugal

Fig. 1 The effects of different functional parameters on the stratified flow thickness. a) The theoretical and experimental results for the effect of the liquid flow rate (Q) on the stratified flow thickness, b) the effect of rotational velocity (ω) of the lab-disc in four different hydraulic diameters of the liquid inlet microchannel ($D_{h1} = 200 \mu\text{m}$, $D_{h2} = 266 \mu\text{m}$, $D_{h3} = 300 \mu\text{m}$, $D_{h4} = 342 \mu\text{m}$) and the theoretical graph for D_{h4} , and c) the effect of the liquid kinematic viscosity (ν) in two different spiral angles ($\alpha_1 = 80^\circ$, $\alpha_2 = 70^\circ$) and the theoretical graph for α_1 .

microfluidics for biomedical applications, *e.g.*, cell culture. Fig. 1 shows the effects of the liquid flow rate (Q), rotational velocity (ω), and kinematic viscosity (ν) on the stratified flow thickness (t). The increase of the liquid flow thickness in a defined channel dimension will induce a transition to a slug flow from an initially stratified flow. In order to prevent such a transition, the height of microchannels must be considered wide enough to maintain the dominance of centrifugal forces over surface tension forces. We apply the Navier–Stokes equations for calculating the stratified flow thickness, see ESI,† part A. The centrifugal force appears as a body force similar to the gravitational force in fluid dynamics of a large channel and we use a geometry coefficient to take into account the effect of shear stress.²⁶ Eqn (1) defines the flow thickness:

$$\frac{wt^4}{(2t + w)} = \frac{3\mu Q}{\cos(\alpha)F_\omega} \quad (1)$$

The channel dimension appears in the left part of eqn (1); where w is the channel width. The right side of the equilibrium includes the rotational speed, the liquid properties, and the spiral microchannel azimuth angle. The azimuth angle α is kept constant by designing a logarithmic path along the entire spiral channel. This assists in maintaining the thickness of the stratified flow constant throughout the operation. Our theoretical calculation predicts that the angle α is required to be less than 90° to establish a stratified flow, see ESI,† part A. Our experimental results validate this prediction. We evaluate our analytical model by experimentally measuring the flow thickness for four different flow rates. To increase the flow rate, we increased the hydraulic diameter of the liquid inlet channel and kept the rotational velocity and the geometrical parameters constant. Fig. 1a compares the experimentally measured liquid flow thickness with that obtained from eqn (1). The results show excellent agreement between the experimental and analytical data (less than 5% of standard error at a high flow rate higher than $40 \mu\text{L s}^{-1}$). Here, the centrifugal force is constant, and the thickness is increased due to the elevated volume of the liquid entering the spiral microchannel. At high flow rates, higher than $25 \mu\text{L s}^{-1}$, a nearly linear relationship between this parameter and the flow thickness helps to evaluate the established flow. As a result, the optimal microchannel height can be defined which ensures that the stability of the stratified flow regime is always achieved.

Fig. 1b shows the effect of rotational speed and different inlet hydraulic diameters on the flow thickness by using 4 different lab-disc samples. Our results show that the thickness of the stratified flow generated is rather independent of the rotational speed. This is due to the simultaneous increase of propelling force and the flow rate that compensates the effect of each other. For each case, four different rotational speeds, from 500 rpm to

2500 rpm, are evaluated. According to eqn (1), both the liquid flow rate and centrifugal force are a function of rotational speed. Also, the flow rate in centrifugal microfluidics is calculated as:²⁷

$$Q = \frac{\pi\rho\omega^2 d_h^4 (\bar{r}\Delta r)}{128\mu l} \quad (2)$$

where r is the radial position from the center of the disc, $\bar{r}$ is the average distance of the liquid in the channels and Δr is the radial distance of the liquid subjected to centrifugal force. We combine this equation with eqn (1) to derive an equation for flow thickness that is independent of rotational velocity:

$$\frac{t^4}{(2t + w)} = \frac{3\pi d_h^4 (\bar{r}\Delta r)}{128l r w \cos(\alpha)} \quad (3)$$

By implementing this equation, the stratified flow thickness for similar geometries and material properties of the conducted experiments was calculated. For $D_{h4} = 342 \mu\text{m}$, the calculated value was approximately $268 \mu\text{m}$. As it is shown in Fig. 1b, the equation can be used for approximation of the stratified flow. Due to the independence of the stratified flow thickness to rotational velocity in eqn (3), the theoretical graph is in the form of a horizontal line. Although the thickness of the stratified flow is independent of the rotational velocity, the residence time of the liquid in a given length of the spiral channel is reduced by increasing the rotational velocity. Consequently, the residence time of the liquid segment in a given length of the spiral microchannel can be calculated by having the liquid flow rate.

Fig. 1c shows the effects of azimuth angle α on the flow thickness for four different liquids having different viscosities and densities. As is shown in the theoretical graph, the experimental results are in excellent agreement with eqn (3), confirming that the viscosity and density have a negligible effect on the flow thickness. Due to the independency of the stratified flow thickness to the kinematic viscosity in eqn (3), the theoretical graph is in the form of a horizontal line. However, our results also show that the flow thickness increases when the angle α decreases from 80° to 70° . This implies that for a constant flow rate, applying different spiral angles causes different magnitudes of propelling centrifugal forces which generate different stratified flow thicknesses. The stratified flow will convert to other flow regimes when the surface tension forces are dominant due to wall effects.

Fig. 2 shows the transition between stratified, slug and single-phase flow regimes in the spiral microchannel. In large channels, the stratified flow is formed in low superficial velocities at large Bond numbers, *i.e.*, $Bo > 4.7$. In linear microfluidics, this dimensionless number is often lower than 1 due to the importance of surface tension forces with respect to gravitational force.² We apply the same criterion but replace the gravitational force with the perpendicular component of the centrifugal force acting on the

Fig. 2 Still-frame images of generating different flow regimes in a microchannel on a rotating lab-disc in different applied centrifugal forces, a) the microchannel is completely filled by the liquid to form a single-phase flow (applied centrifugal force = 18g), b) a stratified flow formation in the spiral microchannel by applying a relatively high centrifugal force (82g), and c) a slug flow that is formed through a transition from the stratified flow (applied centrifugal force = 36g).

microchannel to calculate the centrifugal-based Bond number:

$$Bo_c = \frac{F_\omega \sin \alpha d_h^2}{\sigma} \quad (4)$$

where d_h is the hydraulic diameter of the spiral channel and σ is the surface tension coefficient of the liquid and gas. In small rotational velocities *i.e.*, relatively low centrifugal Bond numbers, the liquid fills the microchannel due to the relatively high capillary forces. At larger values of the centrifugal Bo number (Bo_c), a stratified flow of a certain thickness is generated. Fig. 2a shows the formation of a single-phase flow in the microchannel as a result of increasing the rotational speed. As described in the previous section, if this thickness becomes wider than or as wide as the channel height, air cannot enter the spiral channel and a single-phase flow is formed. Fig. 2b shows a stratified flow in the spiral channel due to increasing of Bo_c number. Fig. 2c shows that for a critical flow thickness (t_{cr}), the slug flow is developed by trapping air bubbles among the liquid stream which is due to a formation of a liquid bridge between the two edges of the microchannel, see ESI† part B. Due to its lower density, the flow rate of the gas is negligible compared to the liquid flow rate.

Characterization

Fig. 3 summarizes the conditions required to produce stratified, slug and single-phase flows in microchannels on the centrifugal microfluidic platforms. They include the rotational speed, geometrical parameters, and liquid properties including density and viscosity. Liquid properties influence the magnitudes of the liquid flow rate and applied centrifugal force while the geometrical parameters mainly contribute to maintaining the stability of the flows. By using eqn (3) and knowing the critical thickness, the preferred flow regime can be formed by using different spiral channel heights. For the generated flows, the residence time and volume fractions of the different phases can be adjusted by varying the operational parameters, *e.g.*, geometries and rotational speed. As we showed in Fig. 1b, the thickness of the stratified flow was changed by using different hydraulic diameters of the inlet channel. The effects of the operational parameters on the slug flow patterns will be shown in the following sections.

For different fluid velocities in macro dimensions, the Kelvin-Helmholtz instability theory is used as the criterion of the transition.^{28–30} In microchannels, the predominance of the surface tension forces is responsible for this

Fig. 3 The flowchart for prediction of the generated flow regime on the spiral microchannel in the presented platform based on the effective parameters. Different parameters including kinematic (rotational velocity), geometrical (inlet and spiral region), and material-based properties (liquid properties and surface wettability) affect the thickness of the flow in the microchannel. The flow regime can be adjusted by using the presented flowchart comparing the flow thickness with the microchannel height (h) and the critical thickness (t_{cr}).

transition.^{30,31} Our experimental results confirm that when centrifugal force is well coordinated with other contributing parameters, such a transition can be achieved on centrifugal microfluidic platforms. Fig. 4a shows the measured critical

thicknesses of the liquid flow in a 400 μm wide microchannel for four different liquids each experiencing a different centrifugal force. Based on these results, in higher rotational speeds, the transitions take place in wider thicknesses of the liquid. For a more precise evaluation, the results are analyzed based on the dimensionless critical number (Cr) that describes the ratio of the critical thickness to the height of the microchannel (t_{cr}/h). The Bo_C number is used instead of the rotational speed in order to evaluate the effects of centrifugal force as well as the surface tension coefficients of different materials. Fig. 4b shows that by increasing the centrifugal force, relatively thicker stratified flows are required for the transition to occur. In Bo_C numbers close to 6, the liquid flow is in a stratified form even when more than $\sim 70\%$ of the microchannel is filled by the liquid. In the dimensionless analysis, a nonlinear curve with $r^2 = 0.85$ can be fitted for estimating the behavior of the system.

Fig. 5 shows the flow pattern in terms of dimensionless numbers for detailed characterization of flow transition on the centrifugal microfluidic platforms. The centrifugal Bond number and the Reynolds number are used as variables to present a holistic view over different parameters *i.e.*, the viscous, inertia, surface tension and centrifugal forces. The hydraulic diameter is used as the length scale that is different for stratified and slug flows because of different wetted perimeters.³ The Reynolds number for the laminar gas-liquid flow is calculated for the liquid only due to the extremely large difference between the densities of the two phases. In order to investigate the flow rates, hydraulic diameter of the spiral channel and applied centrifugal force, ten different lab-discs were used. For Reynolds numbers less than 10, the stratified flow is formed because the flow thickness cannot elevate to the associated critical thicknesses. For Bo_C of 1 to 8 corresponding to the increase of the Re from 10 to 100, respectively, the transition to slug flow begins. The transition boundary in corresponding regions is in agreement with those of the effects of Bo_C on the critical thickness (Fig. 4b) predicted by our analysis. For $Bo_C > 8$, the applied centrifugal force is large enough to prevent the transition even for $Re \sim 1000$. Note that we

Fig. 4 Illustration of the effect of liquid properties, microchannel properties, and kinematic conditions on the critical thickness causing the transition of a stratified flow to a slug flow. a) The relationship between the critical thicknesses of the liquid flow *versus* the rotational velocity, b) the relationship between the dimensionless critical thickness *versus* the centrifugal Bond number of the flow for four different liquids with a nonlinear regression fitting.

Fig. 5 Gas-liquid flow pattern map for the presented platform based on the different Reynolds values (logarithmic scaling) and centrifugal Bond numbers. In $Bo_c < 8$ both stratified and slug flows are generated on the spiral microchannel based on the Re . In $Bo_c > 10$ the stratified flow can be formed due to high centrifugal forces applied on the flow. Different slug flow patterns for the liquid plugs and gas bubbles are shown based on different operational conditions with a hydraulic diameter of $400\ \mu\text{m}$.

conducted our experiments on the PMMA substrates and using different materials will probably change the results shown in Fig. 5.

Different lengths and size fractions of liquid plugs and gas bubbles can be achieved by adjusting the operational parameters of the system. Four different patterns of the slug flow in different regions of the flow pattern map are shown in the Fig. 5. In the higher Re numbers, corresponding to higher rotational velocities of the disc, the lengths of the generated bubbles are more than twice the length of the liquid plugs. As the Re is reduced, the length of the bubbles is decreased. Consequently, there are several kinematic and

geometrical parameters (mainly the rotational velocity of the disc and the radial distance of the spiral channel) that can be manipulated to control the sizes of the liquid and gas segments in a given hydraulic diameter of the spiral channel. This can be implemented for the intended application, *e.g.*, mixing of miscible liquids, as well as addressing some technical problems in multiphase microfluidics. For instance, reduction of the uniformity of segmented flows is a major challenge in thermally dependent applications due to gas expansion and changing liquid viscosity. This causes the change in the flowrate and lengths of the liquid plugs.³² The main reported solution is to adjust the backflow to neutralize

Fig. 6 a) Schematic view of various parts of the presented model for generation of a constant liquid flow rate in centrifugal microfluidics and different possible conditions of the liquid in the buffering structure based on the inflow and outflow rates of the liquid: (b) most of the liquid is overflowed into the waste chamber due to the relatively higher inflow rate; (c) an equilibrium state due to a balance between inflow and outflow rates; (d) the buffering structure is not completely filled due to the relatively higher rate of the outflow. e) Distribution of the liquid plugs remaining in the spiral microchannel after stopping the rotating disc in $\omega_0 = 1200\ \text{rpm}$ ($\sim 52\ g$) through an abrupt deceleration ($\alpha = 1000\ \text{rpm s}^{-1}$). A close view of the liquid plugs shows the uniform-sized and asymmetric bubbles surrounded with a very thin liquid film at the walls (approximately $15\ \mu\text{m}$).

the vapor pressure during thermocycling. Due to the influence of multiple parameters on the patterns of the centrifugally-induced slug flow in the presented platform, the flow can be stabilized by designing the particular geometries of the main microchannel and or varying the cross-sections to achieve stable slug flow conditions in different temperature zones.

Durability

We studied the stability of the gas–liquid flows both on rotating and stationary platforms (*i.e.*, platform brought to a halt). On the rotating platform, both the liquid plugs and the gas bubbles maintain their initial sizes. But a small deviation occurs when the last group of bubbles was generated which was due to the decrease of the liquid level in the reservoir. The gradual change in the liquid level in the reservoir consequently affects the total propulsive force and the liquid flow rate in the connected microchannel.²⁷ In order to alleviate the effects of this on the quality of generated slug and stratified flows, we designed a flow regulator mechanism. Fig. 6a shows the liquid handling features that allow for producing a constant flow rate. It consists of an inlet chamber, a buffering structure, and a waste chamber. The buffering structure assists in generating constant pressure by overflowing the excess into the waste chamber. In order to employ this technique, the lengths and hydraulic diameters of the inlet and outlet microchannels must be adjusted in a way that the inflow and outflow rates of the liquid are balanced. Fig. 6b shows that the liquid level is maintained at a high flow rate and the excess liquid overflows into the waste chamber. Fig. 6c and d show the operation of the pressure regulator mechanism at lower flow rates.

We also studied the gas–liquid state by stopping the platform with different deceleration rates. For the initially stratified flow on a rotating disc the flow eventually turns into a single-phase for the investigated deceleration rates. For the same experimental conditions, the slug flow shows some level of sustainability. At the stationary state it turns into a two-phase liquid–air plug at a deceleration rate of 1000 rpm s^{−1}. Fig. 6e shows the liquid–air plug after the platform is brought to halt. In comparison with the slug flow in the rotating state the sizes of the air bubbles are slightly different which may be due to the larger effect of wall induced forces. The ability of stilling the slug flow is useful for incubation steps in clinical and chemical applications. We show that hundreds of thousands of bubbles and liquid plugs can be generated on a centrifugal microfluidics of a compact disc size, see ESI,† part C.

Applications

The slug flow is principally used for its ability to mix immiscible liquids due to the formation of secondary flows inside the liquid plugs. To show this capability in centrifugally-induced slug flows, we designed a model

comprising two inlet chambers connected to a radial microchannel. After the disc rotation, the solution of the liquids with different colors was introduced into a slug flow regime by implementing the presented technique. A color-changing analysis showed that the mixing of the liquids can be enhanced by taking advantage of the recirculation motion inside the liquid plugs (see ESI,† part D). Simple design, no requirement to external devices and simple separation of the gas phase from the mixture (after the mixing process) are the main advantages of this continuous mixing method. In addition, multiple samples and reagents can be introduced into the slug flow by connecting multiple inlet chambers to the main channel *via* microchannels. For delivering the reagents in precise timing, the release of the reagents from different reservoirs can be controlled using different kinds of valves.³³

Microfluidic devices have shown capabilities for serving as cell culturing devices due to the reduction of the total processing time and reagent consumption.³⁴ In centrifugal microfluidics, cell culturing is typically conducted in liquid chambers that are continuously stirred for enhancing the homogeneity of the solution.³⁵ In this study, the capability of the presented platform for the production of liquid slugs is evaluated for bacterial cell culture. Segmentation of the mixture in the form of slugs may facilitate the single cells to access the nutrients and air supply. To assess the effects of converting the accommodated culture mixture into a segmented form, *Escherichia coli* bacteria (*E. coli*) samples were cultured in either the cell culture tubes or the liquid slugs under the same incubation conditions. The monitoring of the bacterial growth level during the incubation process was necessary. There are several methods for measuring cell concentration.³⁶ Fluorescence-based cell counting and colony forming are the common techniques that were not suitable for this case because they require extraction of the samples from the containers. Furthermore, the optical density measurement was not applicable due to the small sample volume in the microchannel (less than 0.2 μL for each liquid plug). Consequently, we used an image analysis technique for immediate measurement of the color change of the mixture for the *in situ* estimation of the bacterial growth in the liquid plugs and culture tubes. To this end, phenol red was added to the samples as a pH indicator material for indirect monitoring of the bulk metabolic activity of the cell population.^{37,38} The color of this material is initially red and gradually turns to yellow when the pH of the mixture is changed due to the increase of the metabolic activity of the bacteria. It should be noted that the pH change of the solution may be due to other reasons, *e.g.*, toxicity of the medium environment, rather than increasing the level of bacteria concentrations.

After segmentation of the mixture in form of liquid plugs, a microscopic observation showed that the bacteria are successfully located inside the liquid plug, see Fig. 7a. The prepared disc and a 0.5 ml Eppendorf tube containing 100 μL of the sample were incubated at 37 °C for 12 hours. For

Fig. 7 Illustration of the culturing results of the *E. coli* bacteria in tube and liquid slug. a) Microscopic illustration of the suspended bacterial cells in a liquid plug adjacent to an air bubble, and b) comparison of the growth of the bacteria in the liquid plugs and the Eppendorf tube in terms of the color change of the mixture.

image analysis, the samples were captured (every 1 hour) using a high-resolution benchtop scanner. Fig. 7b shows the changes in the color of the samples in the tube and slugs in a normalized range of the color intensities. The color intensities were measured through a histogram analysis using the image analysis software ImageJ (National Institutes of Health, Bethesda, MD, USA). The graphs show that the samples in the liquid slug have rapidly started to grow after 1 hour while this time is 3–4 hours for the samples in the tube. In addition, the growth rate in the slug case is considerably higher than that in the tube. The stability of the liquid slugs after 12 hours shows the ability of the presented centrifugally-induced slugs to be used in processes with longer duration. We considered the growth level at $t = 12$ h as the ultimate level. Note that due to different depths of the liquids in the slug (400 μm) and tubes (~ 2 mm), the slug samples were collected after the test in a 0.5 ml Eppendorf tube for measuring the ultimate colors under equal conditions. This makes it possible to compare the results of the plugs and tubes in a normalized range of the color changes. The higher value of the ultimate growth level in slugs in comparison to the tube samples (11% approximately) might be due to the facilitation of the bacterial cell growth in the segmented volumes.

As the color change of the solution containing phenol red can be due to several reasons, it is essential to control the viability of the bacteria after the culturing process. To determine the viability of bacterial cells, we used the same

solution (without phenol red) as the control sample. The sample was collected from the microfluidic system after 12 hours and cultured in eosin methylene blue agar (EMB) medium and then kept at a temperature of 37 $^{\circ}\text{C}$ for 24 hours. *Escherichia coli* growth colonies exhibited a greenish metallic sheen by reflected light. Also, we used the Live/Dead BacLight kit (Thermo Fisher Scientific, USA) for a viability assay. In this regard, 100 μL of bacteria solution was mixed with dye (1 μL). For 15 min, the mixture was kept in the dark at room temperature for the bacteria to be stained. The stained bacteria were observed with fluorescence microscopy to determine their viability. The results confirm high viability of bacteria in the sample, see ESI,† part E.

Conclusion

Although gas–liquid flows are established and well applied in various industries, they have been rarely used in microfluidics technology especially on lab-on-a-chip platforms. In lab-on-a-chip devices, gas–liquid flows can be used as highly efficient mixing techniques, accelerating chemical reaction and cell growth rate. The main reason for scarcity of gas–liquid systems in microfluidics platforms has been the high surface to volume ratio of the microchannels that creates a substantial challenge to generate these flows. Here, we have reported on generating two of the common gas–liquid flows using a centrifugal microfluidics platform

Fig. 8 Illustration of a) different regions of the designed model on the lab-disc and b) details of the inlet region parts and geometrical parameters including the hydraulic diameter of the liquid inlet microchannel (D_h), spiral angle (α), and hydraulic diameter of the spiral microchannel (d_h).

only. The gas–liquid flows are interchangeable by alternating the rotational speed and/or changing the channel dimension. We have derived and experimentally verified an analytical expression that can be used as a primary guideline for designing gas–liquid flows of specific specifications. We used the generated gas–liquid regime for culturing *E. coli* and our results show significant enhancement of the growth rate in comparison to traditional methods.

Methods

Disc fabrication and experimental setup

The discs are made of 2 layers of 1 mm-thick PMMA which are bonded with a pressure sensitive adhesive (PSA) layer. The details of manufacturing of a lab-disc can be found in the literature including our previous publications.^{39–41} Briefly, the PMMA and PSA layers were cut using a Roland MDA-40 and a Graphtec CE-6000 cutter plotter machine, respectively. The layers were aligned and placed in a custom-made screw-press to complete the bonding. A still-frame imaging system was used in this study for capturing images of the rotating lab-disc in different rotational velocities. The system specifications are reported in our previously published articles.^{12,42,43}

Design of the disc

The design of the lab-disc used for the experiments is shown in Fig. 8. It consists of three main features: the inlet region

for liquid and air, the spiral microchannel for generating gas–liquid flows and the collecting chamber (Fig. 8a). Various parts of the inlet region are shown in detail in Fig. 8b. The liquid is pipetted into the liquid chamber through the liquid loading hole. During the rotation of the platform, the liquid and air enter the spiral microchannel through a radially vented channel. Based on the different operational conditions, a flow pattern is shaped in the initial region of the connected spiral microchannel and transferred to the collecting chamber.

Image processing

Commercial image processing software ImageJ (National Institutes of Health, Bethesda, MD, USA) was used for measuring the stratified flow thickness in various experiments.⁴⁴ The captured images were analyzed in a specific region of the spiral channel to diminish the effect of the variation of the centrifugal force on the flow thickness along the channel. The experiments were repeated 5 times for each condition to ensure adequate precision (see ESI,† part F).

Bacterial cell culture

For sterilization of the manufactured lab-disc, it was first washed with 70% ethanol and phosphate buffered saline and subsequently UV irradiation was used for 30 min in a laminar flow hood.

The culture media were prepared by adding 25 mg L^{−1} phenol red (Sigma-Aldrich, Steinheim, Germany) to the Mueller Hinton broth (Sigma-Aldrich, Steinheim, Germany). The concentration of the *Escherichia coli* bacteria (*E. coli*, JM109) was controlled to be 10⁶ cells per mL.

For introducing the culture mixture into the slug form, 100 µL of the solution was introduced to the inlet chamber of the lab-disc. The disc was accelerated up to 1200 rpm and after 5 seconds it was stopped with 1000 rpm s^{−1} for

Table 1 The properties of different liquids utilized in the experiments

Water volume %	Glycerol volume %	Mixture ρ [kg m ^{−3}]	Mixture μ [Ns m ^{−2}]	Mixture ν [m ² s ^{−1}]
100	0	997	9×10^{-4}	9×10^{-7}
75	25	1070	2×10^{-3}	2×10^{-6}
42	58	1117	4.5×10^{-3}	4×10^{-6}
40	60	1165	1.3×10^{-2}	1×10^{-5}

generation of the liquid plugs in the microchannel. Based on the size distribution analysis, the kinematics ($\omega = 1200$ rpm, $\alpha = 200$ rpm s^{-1}) and the geometries ($r = 32$ mm, $D_h = 200$ μ L) were selected in a way to have equal sizes (~ 1 mm) of the liquid plugs and air bubbles in a microchannel with a hydraulic diameter of 400 μ m.

Material preparation

Diluted water was used as the liquid for most of the experiments. For visibility of the liquid during the experiments and precise image analysis, food colors were added to the liquid. For the preparation of the liquids for evaluating the effect of kinematic viscosity, different portions of glycerol (G5516, Sigma-Aldrich, Germany) were mixed with specific volumes of diluted water at the temperature of 25 °C based on Table 1.⁴⁵

Conflicts of interest

There are no conflicts to declare.

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