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Multiorbital bond formation for stable oxygenredox reaction in battery electrodes†

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High-energy-density batteries have been a long-standing target toward sustainability, but the energy density of state-of-the-art lithium-ion batteries is limited in part by the small capacity of the positive electrode materials. Although employing the additional oxygen-redox reaction of Li-excess transitionmetal oxides is an attractive approach to increase the capacity, an atomic-level understanding of the reaction mechanism has not been established so far. Here, using bulk-sensitive resonant inelastic X-ray scattering spectroscopy combined with ab initio computations, we demonstrate the presence of a localized oxygen 2p orbital weakly hybridized with transition metal t_{2a} orbitals that was theoretically predicted to play a key role in oxygen-redox reactions. After oxygen oxidation, the hole in the oxygen 2p orbital is stabilized by the generation of either a $(\sigma + \pi)$ multiorbital bond through strong π backdonation or peroxide O_2^{2-} through oxygen dimerization. The multiorbital bond formation with σ -accepting and π -donating transition metals can thus lead to reversible oxygen-redox reaction.

Broader context

Increasing the energy density of lithium-ion batteries is an urgent task toward achieving a sustainable society. However, the limited capacities of cathodes render lithium-ion batteries unsuitable for electric transport or grid-scale applications. As an effective way to increase the capacity of cathodes, additional oxygen-redox reactions have attracted much attention. Although the presence of "orphaned" oxygen 2p orbitals that are responsible for additional oxygen-redox reactions was theoretically proposed in 2016, no experimental verification has been reported to date. In this work, we experimentally verify the presence of a localized oxygen 2p orbital weakly hybridized with transition metal t2g orbitals in oxygen-redox battery cathodes using resonant inelastic X-ray scattering. We also clarify the stabilization mechanism of the oxidized phase through multiorbital bond formation of oxidized oxygen 2p orbitals.

Introduction

The development of advanced electrochemical energy storage devices has been a topic of intensive research because it offers prospects of sustainability, for instance, reduction of fossil fuel reliance by realizing an electric vehicle range of 500 km per charge or integrating renewable energy sources to an electrical grid. 1-3 Market-leading lithium-ion batteries (LIBs) efficiently store energy by lithium-ion (de)intercalation associated with redox reactions. 4,5 However, their energy density has approached the theoretical limit, in part owing to the small capacity of the positive electrode materials, which severely hinders the wide deployment of LIBs.6 Therefore, it is important to find an alternative battery chemistry that can exceed the existing positive-electrode capacity limits.

The use of redox reactions of oxygen in addition to conventional transition-metal redox reactions is an attractive way to increase the capacity of transition-metal oxides. In general, most oxygen 2p orbitals in conventional electrode materials LiMO₂ (M: transition metal) form σ -type bonds with axial M 3d orbitals (eg orbitals in an Oh symmetry). As the atomic energy

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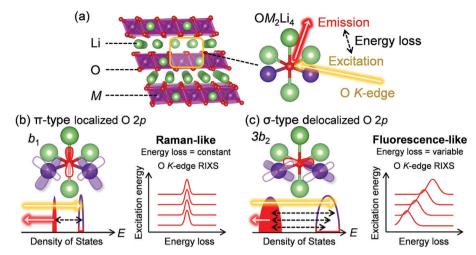


Fig. 1 Resonant inelastic X-ray scattering (RIXS) spectra for delocalized and localized oxygen 2p orbitals. (a) Crystal structure of Li-excess layered transition-metal oxides Li[Li_x M_{1-x} IO₂ (M: transition metal). (b) π -type localized occupied/unoccupied states consisting of oxygen 2p and M $t_{2\alpha}$ orbitals (b_1/b_1^*) bands in a C_{2v} -symmetry OM_2Li_4 cluster) give a Raman-like RIXS peak with constant energy loss regardless of the excitation energy. (c) σ -type delocalized occupied/unoccupied states consisting of oxygen 2p and M e_q orbitals $(3a_1/3a_1^*)$ and $3b_2/3b_2^*$ bands in a C_{2v} -symmetry OM₂Li₄ cluster) give a fluorescence-like RIXS peak with variable energy loss depending on the excitation energy.

level of oxygen 2p orbitals is usually lower than that of M e_g orbitals, the σ -type bonding orbitals are predominantly from oxygen 2p orbitals.8,9 Therefore, it is difficult to oxidize oxygen 2p orbitals that have a σ-type bonding character. 10 However, research groups led by Bruce and Ceder postulated that oxygen in Li-excess transition-metal oxides Li_{1+x}M_{1-x}O₂ (Fig. 1a) intrinsically have localized ("orphaned") 2p orbital along the Li-O-Li axis without σ -type bonding characteristics, which can contribute to an additional oxygen-redox capacity. 10,11 Indeed, large capacities exceeding the capacity limit of M redox reactions have been reported for many Li-excess transition-metal oxides including Li₂MnO₃-LiMO₂ solid solutions, ^{12,13} layered honeycomb Li₂IrO₃, ¹⁴ random rock salt Li_{1.2}Ti_{0.4}Mn_{0.4}O₂, ¹⁵ three-dimensional β -Li₂IrO₃, ¹⁶ and anti-fluorite Li₅FeO₄. ¹⁷ In addition, the electronic states of various oxygen-redox electrode materials have been intensively investigated using analytical methods such as X-ray photoelectron spectroscopy, X-ray absorption spectroscopy, X-ray emission spectroscopy (or resonant inelastic X-ray scattering (RIXS)), or density functional theory (DFT) calculations. 18-22

However, despite the theoretical adequacy of the proposed "orphaned" oxygen 2p orbital hypothesis, the presence of the localized oxygen 2p orbitals in Li-excess transition-metal oxides has not been verified experimentally. Furthermore, although localized, the oxygen 2p orbital along the Li-O-Li axis still exhibits π -type interactions with the M t_{2g} orbital, which should play an essential role in oxygen-redox reactions.²³ It is important to emphasize that the rigid-band model, which has been frequently used for consideration of oxygen-redox electrodes, 15,24 cannot qualitatively discuss M-O interaction (e.g., covalency), because it only considers a bandwidth and the band-center energy of each band. Therefore, for a thorough understanding of the reversible oxygen-redox reactions occurring in Li-excess transition-metal oxides, it is necessary to clarify the nature of the M-O bonds during the oxygen-redox reactions.25

In this work, we used oxygen K-edge resonant inelastic X-ray scattering (RIXS) spectroscopy combined with ab initio computations to demonstrate a criterion for stable oxygen-redox reactions.

Results and discussion

RIXS to detect localized orbitals

Oxygen K-edge RIXS spectroscopy was used to examine the existence of π -type localized oxygen 2p orbitals in Li₂MnO₃, a standard Li-excess layered transition-metal oxide. Li2MnO3 was synthesized by a conventional solid-state method, and the powder X-ray diffraction pattern and Rietveld refinement confirmed its successful synthesis (Fig. S1 and Table S1, ESI†). Li₂MnO₃ that contains only Mn⁴⁺ enables obtaining a simple RIXS spectrum, allowing for direct comparison with DFT calculations. Oxygen K-edge RIXS spectroscopy records the inelastic scattering during core excitation-relaxation (1s \rightarrow 2p \rightarrow 1s), in which the energy loss corresponds to valence excitation between occupied and unoccupied 2p bands.²⁶ RIXS spectroscopy has a probing depth of approximately 100 nm (bulk-sensitive). Importantly, when occupied/unoccupied oxygen 2p bands show a localized character with weak orbital hybridization, the inelastic scattering becomes Raman-like and leads to constant energy loss regardless of the incident photon energy (Fig. 1b and Fig. S2a, ESI†).27 Conversely, delocalized occupied/unoccupied oxygen 2p bands with a large orbital hybridization give fluorescencelike inelastic scattering with variable energy loss depending on the incident photon energy (Fig. 1c and Fig. S2b, ESI†).27 Therefore, oxygen K-edge RIXS spectroscopy allows us to diagnose localized or delocalized oxygen 2p bands.

Before obtaining the RIXS spectra, we conducted ab initio calculations using the HSE06 hybrid functional²⁸ for Li₂MnO₃. Fig. 2a shows that a localized oxygen 2p orbital exists along the Li–O–Li axis with an orbital energy of approximately -0.9 to

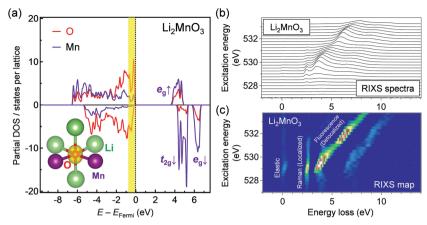


Fig. 2 Direct observation of a localized oxygen 2p orbital hybridized with Mn t_{2g} orbitals in Li_2MnO_3 . (a) Calculated partial density of states for oxygen and manganese in Li₂MnO₃. The inset shows the spatial electron density at the energy range from -0.9 to 0 eV versus the Fermi energy. (b) Oxygen K-edge RIXS spectra, and (c) second differential RIXS map for Li₂MnO₃ with excitation photon energy from 527 to 533.75 eV. The Raman-like RIXS peak with constant energy loss of approximately 2.5 eV indicates the existence of a localized oxygen 2p orbital that is weakly hybridized with Mn t₂₀ orbitals.

0.0 eV against the Fermi energy. The RIXS spectra and the corresponding second differential RIXS map (Fig. 2b and c) exhibit two broad fluorescence-like peaks (the energy loss ranging from 3.5 to 8.0 eV), which could be related to the valence excitation between the σ -type wide oxygen 2p bands strongly hybridized with axial Mn eg orbitals (Fig. 1c). Based on the C_{2v} symmetry of an OMn₂Li₄ cluster, these bands are labelled as 3a₁/3b₂ bands.^{8,23} More importantly, the RIXS spectra show an intense Raman-like peak with constant energy loss of approximately 2.5 eV. This Raman-like peak clearly indicates the existence of the π -type narrow oxygen 2p bands weakly hybridized with Mn t_{2g} orbitals (b_1/b_1^*) bands based on the C_{2v} -symmetry labelling, Fig. 1b). It is important to note that the Raman-like feature is not the simple projection of the d-d excitation of Mn L-edge, because O K-edge XAS and RIXS always involve charge-transfer processes through O-Mn interactions (Fig. S3, ESI†). Therefore, whether Raman- or fluorescence-like RIXS is observed depends primarily on the strength of the O-Mn interactions.

In contrast, for a non-Li-excess layered oxide LiNi_{1/3}-Co_{1/3}Mn_{1/3}O₂, the RIXS spectra show only fluorescence-like peaks with variable energy loss depending on the incident photon energy (Fig. S4, ESI†) because most oxygen 2p orbitals form σ-type wide bands with axial M 3d orbitals. Therefore, this is the first experimental verification of the localized oxygen 2p orbital weakly hybridized with M t2g orbitals in Li-excess transition-metal oxides, and oxygen K-edge RIXS spectroscopy can, thus, be considered as an effective diagnostic tool to detect electrochemically active oxygen states.

Oxidation of localized oxygen 2p orbital

Having experimentally confirmed the existence of the π -type narrow oxygen 2p bands, the contribution of the localized states to the oxygen-redox reactions was examined using ex situ oxygen K-edge RIXS spectroscopy. As a target Li-excess layered transition metal oxide, Li_{1,2}Ni_{0,13}Co_{0,13}Mn_{0,54}O₂ was used as an oxygen-redox electrode material. Li_{1.2}Ni_{0.13}Co_{0.13}Mn_{0.54}O₂ was synthesized by a conventional solid-state method, and the

powder X-ray diffraction pattern and Rietveld refinement confirmed its successful synthesis (Fig. S5 and Table S2, ESI†). Before acquiring the RIXS spectra, ab initio calculations using the HSE06 hybrid functional were carried out for $\text{Li}_{1,2-x}\text{Ni}_{0,13}\text{Co}_{0,13}\text{Mn}_{0,54}\text{O}_2$ (Fig. 3a). The structural configuration of Li_{1.2}Ni_{0.13}Co_{0.13}Mn_{0.54}O₂ was determined by a genetic algorithm (GA) approach that optimizes Li/Ni/Co/Mn arrangement (Fig. S6a and b, ESI†). For the delithiated states, Li and the vacancy configuration in Li_{1,2-x}Ni_{0,13}Co_{0,13}Mn_{0,54}O₂ was also determined by the GA approach (Fig. S6c, ESI†). The optimized structures for x = 0 and 1.2 are shown in the inset of Fig. 3b. The analysis of partial density of states (pDOS) for pristine Li_{1,2}Ni_{0,13}Co_{0,13}Mn_{0,54}O₂ shows that Co and Ni 3d bands dominate the top of the valence band ($-1 \text{ eV} < E - E_F < 0 \text{ eV}$), accompanied by a localized oxide band due to Li-O-Li at a slightly lower energy region ($-2 \text{ eV} < E - E_F < 1 \text{ eV}$) (Fig. S7, ESI†). The averaged Bader charges of Ni and Co decrease only during the early stage of Li^+ extraction (x < 0.4), whereas that of oxygen decreases continuously during the entire delithiation process, suggesting the occurrence of additional oxygen-redox reactions for x > 0.4 (Fig. 3a). This trend is also confirmed by the spin integration (SI) analysis, where the change of spin density of O (O oxidation) occurs at the delithiation process of x > 0.4(Fig. S8, ESI†).29 Ni2+ and Co3+ ions are oxidized to Ni4+ and Co^{4+} respectively in the early stage of delithiation (x < 0.4), followed by oxidation of oxide ions (x > 0.4). The oxidation state of Mn⁴⁺ ions remains unchanged in the entire compositional range. Indeed, using the predicted oxygen-redox reactions, Li_{1,2}Ni_{0,13}Co_{0,13}Mn_{0,54}O₂ delivers a large reversible capacity of approximately 250 mA h g-1, which exceeds the theoretical capacity (123 mA h g⁻¹) of the Ni⁴⁺/Ni²⁺ and Co⁴⁺/Co³⁺ redox reactions (Fig. 3b). 11,30

The oxygen K-edge X-ray absorption spectrum (XAS) obtained in the bulk-sensitive partial fluorescence yield mode for the pristine Li_{1,2}Ni_{0,13}Co_{0,13}Mn_{0,54}O₂ (Fig. 3c) shows two absorption peaks (528.5 and 531 eV) for the 1s core-electron excitation to unoccupied σ -type bands (oxygen 2p-Mn $e_g^{\downarrow}/e_g^{\uparrow}$)

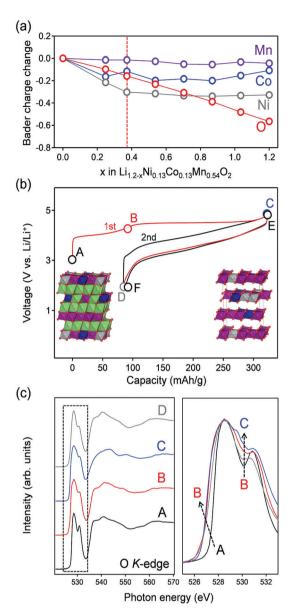


Fig. 3 Oxygen-redox reaction in $Li_{1.2-x}Ni_{0.13}Co_{0.13}Mn_{0.54}O_2$. (a) The average Bader charge changes of Mn, Co, Ni, and O in Li_{1.2-x}Ni_{0.13}Co_{0.13}Mn_{0.54}O₂. (b) Charge-discharge curves for $Li_{1.2}Ni_{0.13}Co_{0.13}Mn_{0.54}O_2$. The inset shows optimized Li/Ni/Co/Mn arrangements for Li_{1.20}Ni_{0.13}Co_{0.13}Mn_{0.54}O₂, and Li₀Ni_{0.13}Co_{0.13}Mn_{0.54}O₂. Green, grey, deep blue, and purple-colored octahedra correspond to LiO₆, NiO₆, CoO₆, and MnO₆ octahedra, respectively. (c) Oxygen K-edge X-ray absorption spectra in a bulk sensitive partial fluorescence yield mode for $Li_{1.2-x}Ni_{0.13}Co_{0.13}Mn_{0.54}O_2$ during the first cycle. The pre-edge region is enlarged for comparison.

and an unoccupied π -type band (oxygen 2p-Mn t_{2g}^{\downarrow}). Upon charging to 4.4 V vs. Li/Li^+ (A \rightarrow B in Fig. 3b), a new XAS shoulder emerged at 527 eV owing to hole generation in σ -type (oxygen 2p-Ni e_g) and π -type (oxygen 2p-Co t_{2g}) bands. After further charging to 4.8 V vs. Li/Li⁺ (B → C in Fig. 3b), a new absorption peak emerged at a relatively high absorption-energy region of approximately 530.5 eV. Similar spectral changes were also observed during the second cycle (Fig. S9, ESI†). The XAS signal at 530.5 eV can be ascribed to a 1s core electron

excitation to an unoccupied π -type band (oxygen 2p-Mn t_{2g}^{\uparrow}). Emergence of the absorption peak at a relatively high energy region is reasonable because oxygen oxidation increases the effective nuclear charge, which lowers the initial energy level of an oxygen 1s core electron and hence raises the excitation energy.²³ Similar changes in the XAS signals by oxidation (the emergence of new absorption peaks at a high energy region) are often observed in transition-metal K-edge absorption spectra. 11,15,31 Another explanation for this new absorption is a 1s core electron excitation to an unoccupied σ^* molecular orbital of peroxide O_2^{2-} resulting from the dimerization of oxidized oxide ions, which will be discussed later. In either case, the emergence of the XAS signal at 530.5 eV is an experimental indicator for the occurrence of oxygen oxidation.

The RIXS spectra of pristine Li_{1.2}Ni_{0.13}Co_{0.13}Mn_{0.54}O₂ (Fig. 4a) exhibit a Raman-like peak with constant energy loss corresponding to a π -type narrow oxygen 2p band ($\pi \to \pi^*$), in addition to the fluorescence-like peaks ($\sigma \to \sigma^*$). The *ab initio* calculations for pristine Li_{1,2}Ni_{0,13}Co_{0,13}Mn_{0,54}O₂ supports the existence of localized oxygen 2p orbitals along the Li-O-Li axes with an orbital energy near the Fermi level (Fig. S7, ESI†). The $\pi \to \pi^*$ RIXS peak intensified after charging to 4.4 V vs. Li/Li⁺ (transition-metal oxidation, Fig. 4b), which indicates accumulation of the localized oxygen 2p states to the Fermi level. The initial Li⁺ extraction associated with Co and Ni oxidation gives an oxygen coordination environment with a \square -O-Li⁺ or \Box -O- \Box axis (\Box : Li⁺ vacancy), which electrostatically raises the energy level of the localized oxygen 2p orbitals. Indeed, the fact that the energy loss of the Raman-like RIXS peak decreased from 2.5 to 2.0 eV supports a rise in the energy level of the localized oxygen 2p orbitals. We presume that accumulation of the localized oxygen 2p states to the Fermi level should be an essential preceding process that triggers oxygen-redox reactions. For example, it is well known that the electrochemical activity of Li₂MnO₃ is poor³² even though oxygen has a Li⁺-O-Li⁺ axis and hence a localized oxygen 2p orbital (Fig. 2a). Most likely, as Li₂MnO₃ cannot exhibit initial Li⁺ extraction owing to the electrochemically inactive Mn4+, it is difficult to generate the \square -O-Li⁺ and \square -O- \square axes, and the energy level of the localized oxygen 2p orbital remains too low to undergo oxidation within the liquid electrolyte stability window. Indeed, Li₂MnO₃ delivers large reversible capacities when cycled with a solid electrolyte that possesses a large electrochemical stability window.³³ Conversely, when redox-active transition metals are present, such as in Li₂MnO₃-LiMO₂ solid solution, \Box -O-Li⁺ and \Box -O- \Box axes are easily formed by the initial Li⁺ extraction to raise the energy level of the localized oxygen 2p orbital, unlocking the redox activity of oxygen. Once the oxygenredox reaction is triggered, the \Box -O-Li⁺ and \Box -O- \Box axes are continuously generated to achieve a large oxygen-redox capacity.

After charging to 4.8 V vs. Li/Li⁺ (oxygen oxidation, Fig. 4c), the Raman-like $\pi \to \pi^*$ RIXS peaks disappear, and all the RIXS peaks become fluorescence-like. Importantly, a new intense fluorescence-like peak emerges at an energy loss of approximately 7.5 eV with an incident photon energy of 530.5 eV. Assuming an incident photon of 530.5 eV excites a 1s core

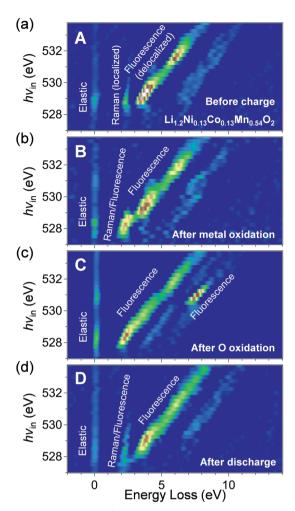


Fig. 4 Monitoring oxygen 2p orbitals during oxygen-redox reaction of $\text{Li}_{1.2}\text{Ni}_{0.13}\text{Co}_{0.13}\text{Mn}_{0.54}\text{O}_2$. Oxygen K-edge second differential RIXS map for the samples (a) before charge (sample A in Fig. 3b), (b) after transition-metal oxidation (sample B in Fig. 3b), (c) after oxygen oxidation (sample C in Fig. 3b), and (d) after discharge (sample D in Fig. 3b), with excitation photon energy from 527 to 533.75 eV. The corresponding RIXS spectra are shown in Fig. S10 (ESI†).

electron to an unoccupied π -type band (oxygen 2p-Mn $t_{2g}^{\mathbb{T}}$), resonant inelastic scattering with the 530.5 eV incident photon includes valence excitation between the π -type bands ($\pi \to \pi^*$). Therefore, a large energy loss of approximately 7.5 eV for this RIXS peak should correspond to π -type splitting. This large π -type splitting should be induced by hole generation in the antibonding π -type band which makes the Mn–O bonds more bonding (more delocalization/larger orbital hybridization). Therefore, the RIXS peak is observed as fluorescence-like. The enhanced π -type interaction stabilizes the oxidized oxygen, leading to reversible oxygen-redox reactions.

It is also important to note that the Raman-like RIXS peak of the localized oxygen 2p orbitals was not fully recovered after full discharge (Fig. 4d). The emission at the energy loss region of approximately 2 eV becomes weakly fluorescence-like after the 1st cycle. Presumably, structural degradation such as cation migration during the 1st charge modulates the coordination environment of oxide ions, making the RIXS peak weakly fluorescence-like. The irreversible structural change during the 1st charge could explain the experimental observation that the potential profile of the 2nd charge differs from that of the 1st charge (Fig. 3b). Nevertheless, in the 2nd cycle, the spectral shape change is reversible (Fig. S11, ESI†), suggesting stable occurrence of the oxygen-redox reactions.

Possible O-O bond formation in oxygen redox electrodes

Gent and Hong et al. also observed similar intense RIXS peaks for Li_{1.17-x}Ni_{0.21}Co_{0.08}Mn_{0.54}O₂ and Li₂Ir_{0.75}Sn_{0.25}O₃ after oxygen oxidation,34,35 and transition-metal migration and subsequent O-O bond formation were proposed to explain the emergence of the new XAS and RIXS peaks after oxygen oxidation. To examine this hypothesis, we acquired O K-edge XAS and RIXS spectra for WO₂(O₂)(H₂O), which contains peroxide O₂²⁻ coordinated to W⁶⁺.36 Based on the DFT calculations (Fig. 5a and b), $WO_2(O_2)(H_2O)$ possesses (i) a strong π -type LUMO band consisting of O 2p and large W 5d (t_{2g}) (3.5 < $E-E_{\rm F}$ < 4.3 eV) and (ii) an unoccupied σ^* band of peroxide (6.1 < $E-E_{\rm F}$ < 7.1 eV). The XAS spectrum shows a broad absorption arising from coreelectron excitations to these unoccupied π -type and σ -type bands of W-O and peroxide (Fig. 5c). Importantly, two intense fluorescence-like emissions were observed in the RIXS map (Fig. 5d), which can be ascribed to valence excitations between the π -type bands of W-O and between the σ -type bands of O-O, respectively. The fluorescence-like feature of the emission from the π -type bands of W–O is explained by electron delocalization through strong π-type W t_{2g}-O 2p interactions. The fluorescencelike emission between the σ -type bands of O-O takes place approximately with an energy loss of 6 eV at hv_{in} = 530 eV, which differs slightly from that observed for fully charged $Li_{1.2}Ni_{0.13}Co_{0.13}Mn_{0.54}O_2$ (the energy loss of 7.5 eV at hv_{in} = 530.5 eV). Furthermore, the transition-metal migration and peroxide formation are one of possible explanations for the RIXS spectral changes for lithium-rich layered oxides, but cannot explain the almost identical RIXS spectral changes during the oxygen-redox reactions of many other sodium-based layered oxides (e.g., $Na_{2/3}[Mg_{0.28}Mn_{0.72}]O_2$)³⁷ and $Na_2Mn_3O_7$, ³⁸ where the transition-metal migration is known to be negligible due to large Na⁺ slabs. In fact, neither a short O-O distance below 2.2 Å nor significant MO6 distortion was found in the relaxed structures of delithiated phases (Fig. S12, ESI†). Although the possibility of the O-O bond formation cannot be excluded, another possible but less argued mechanism of hole generation in the antibonding π -type band will be discussed below.

Multiorbital bond formation in oxygen redox electrodes

Crystal orbital overlap population (COOP) diagrams for selected Mn–O bonds from *ab initio* calculations for Li_{1.2}Ni_{0.13}-Co_{0.13}Mn_{0.54}O₂ (Fig. 6) quantify the reversible transformation of an oxygen 2p orbital characteristics during the oxygen-redox reaction. The COOP is an overlap-population-weighted density of states that serves as a bonding descriptor.³⁹ The sign of COOP indicates bonding (positive), non-bonding (zero), or antibonding (negative) contributions between two selected atoms.

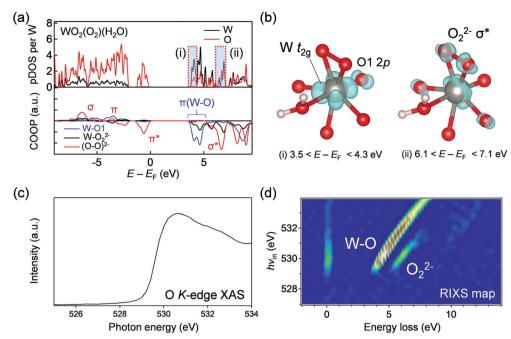


Fig. 5 Electronic structure and XAS/RIXS spectra for WO₂(O₂)(H₂O). (a) Partial density of states (pDOS) for W and O, and crystal orbital overlap population (COOP) diagrams for W-O and O-O bonds. (b) Spatial hole densities with the selected orbital energies (i) from 3.5 to 4.3 eV, and (ii) from 6.1 to 7.1 eV against the Fermi energy (dotted areas in pDOS). (c) O K-edge X-ray absorption (XAS) spectrum. (d) O K-edge differential RIXS map. While the RIXS peak for O_2^{2-} can be referred to explain a mechanism of O redox cathodes, a care should be taken that the similar signal is also induced by M-O multi-orbital bond formation (see text).

Before charging, the spatial distribution of the electron at the energy range of -2.0 to -1.0 eV against the Fermi energy (Fig. 6a)

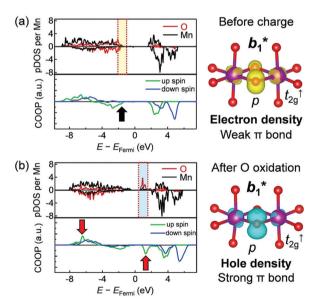


Fig. 6 Enhancement of π -type interaction after oxygen oxidation. Partial density of states (pDOS) for oxygen and manganese, and crystal orbital overlap population (COOP) diagrams for Mn-O bonds in Li_{1.2-x}Ni_{0.13-} $Co_{0.13}Mn_{0.54}O_2$ (a) before charge (x = 0) and (b) after oxygen oxidation (x = 1.2). The dotted areas denote states mainly consisting of oxygen 2p orbitals responsible for oxygen-redox reactions. The spatial electron or hole density with the selected orbital energy (dotted areas in pDOS) is depicted.

takes up a π -type orbital shape consisting of oxygen 2p and Mn t_{2g} orbitals (b_1^* in C_{2v}). However, the oxygen 2p orbitals have no significant COOP with Mn t2g orbitals (black arrow, Fig. 6a), indicating a localized nature of the oxygen 2p orbitals. After oxygen oxidation, the spatial distribution of a hole at the energy range from +1.0 to +2.0 eV versus the Fermi energy also has a π -type orbital shape (Fig. 6b). On increasing the number of holes in the antibonding π -type orbital, Mn-O bonds show more bonding characteristics with a considerable COOP between the oxygen 2p and Mn t_{2g}^{\uparrow} orbitals (Fig. S13, ESI†). The COOP diagram also indicates that the bonding states reside at the energy range of -7.0 to -6.0 eV against the Fermi energy (red arrows, Fig. 6b), which may correspond to the occupied π -type bonding b_1 orbital. The calculated b_1/b_1^* splitting (ca. 7.0 eV) agrees well with the energy loss of the intense fluorescence-like peak observed in the RIXS spectra (Fig. 4c).

To summarize the reaction mechanism, the Li⁺-O-Li⁺ coordination in the pristine state forms localized oxygen 2p orbital weakly hybridized with the Mn t_{2g} orbital. When the initial Li⁺ extraction occurs in association with M redox reactions, the \square -O-Li $^+$ and □-O-□ coordination axes are generated, which raises the energy level of the localized oxygen 2p states to the Fermi level. After this accumulation, exclusive oxygen oxidation occurs; a hole is generated in the antibonding π -type orbital and orbital hybridization is enhanced to delocalize the hole within a Mn-O-Mn bond. Alternatively, or in parallel, unstable oxidized oxide ions dimerize to form peroxide O_2^{2-} . The resulting either b_1/b_1^* splitting of the Mn-O-Mn bond or σ/σ^* splitting of the O-O bond stabilizes the oxidized oxygen, enabling a reversible oxygen-redox reaction.

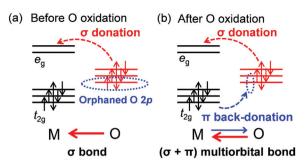


Fig. 7 Multiorbital bond formation upon oxygen oxidation. (a) σ bond in conventional metal oxides. (b) $(\sigma + \pi)$ multiorbital bond in oxygen-oxidized states.

From a conventional viewpoint of an electronic structure in transition-metal oxides, an M-O bond is formed mainly by σ donation from oxygen (σ bond), as the 2p orbitals of O²⁻ are filled completely (Fig. 7a).9 However, hole generation on the outer sphere 2p orbital of oxygen is intrinsically unstable, and π back-donation from M occurs to stabilize the oxygen hole, giving rise to $(\sigma + \pi)$ multiorbital bonds (Fig. 7b). Therefore, the reversible oxygen-redox reaction requires M to possess both σ -accepting and π -donating abilities for oxidized oxygen. For example, Ti^{4+} with a vacant t_{2g} configuration has no π -donating ability whereas Sn^{4+} with a filled $e_{\rm g}$ configuration has no σ-accepting ability. Therefore, Li₂TiO₃ and Li₂SnO₃ are not oxygen-redox active, 40,41 and replacing transition metals with Ti⁴⁺ or Sn⁴⁺ could promote stabilizing oxidized oxygen, for instance, by peroxide formation.³⁵ Conversely, Mn⁴⁺, Co⁴⁺, and Ni⁴⁺ with (partially) filled t_{2g} and vacant e_g configurations satisfy the requirement for $(\sigma + \pi)$ multiorbital bond formation, leading to the high oxygen-redox activity of the Li₂MnO₃-LiMO₂ solid solution such as Li_{1.2}Ni_{0.13}Co_{0.13}Mn_{0.54}O₂. Large overlap between O 2p and M 4d/5d orbitals should give more stable $(\sigma + \pi)$ multiorbital bonds. Indeed, a short Ru(v)-O distance of 1.85 Å (relative to the conventional Ru(v)-O distance of 2.0 Å) was observed for Li₂Ru_{0.75}Sn_{0.25}O₃ after oxygen oxidation. 42 Owing to the enhanced multiorbital bonding, Li-excess 4d/5d transitionmetal oxides exhibit highly reversible oxygen-redox reactions without oxygen gas release or surface side reactions.

Conclusions

In this work, using oxygen K-edge RIXS spectroscopy, we investigated oxygen-redox battery electrodes, demonstrating the importance of the combined control of the $(\sigma + \pi)$ interaction between transition metals and oxygen. In addition to the previously reported criteria, 10,11,15 we have discussed a novel and crucial criterion related to the electronic configuration: transition metal ions with simultaneous σ -accepting and π -donating abilities can realize stable oxygen redox reaction toward higher-capacity, higher-energy-density cathode materials. Typical transition metals that satisfy these requirements are Mn⁴⁺ $(t_{2g}^{\uparrow} t_{2g}^{\downarrow} e_{g}^{\uparrow} e_{g}^{\downarrow})^{\circ}$; π -donating t_{2g}^{\uparrow} and σ -accepting e_{g}^{\uparrow} to O 2p) and Ru⁵⁺ $(t_{2g}^{\uparrow} t_{2g}^{\downarrow} e_{g}^{\uparrow} e_{g}^{\downarrow})^{\circ}$; significantly π -donating t_{2g}^{\uparrow} and σ -accepting

 $e_{\rm g}^{\uparrow}$ to O 2p). The exploration of Li-excess oxides including transition metals that satisfy these criteria could help surpass the existing LIB performance limits.

Methods

Synthesis

Li₂MnO₃, LiNi_{1/3}Co_{1/3}Mn_{1/3}O₂, and Li_{1.2}Ni_{0.13}Co_{0.13}Mn_{0.54}O₂ were prepared using stoichiometric amounts of Li₂CO₃ (Wako, 99%), NiO (Wako, 99%), Co₃O₄ (Kanto chemicals, 99%) and MnO₂ (Wako, 99.5%). The precursors were ball-milled at 400 rpm for 6 h (cycles of 5 min ball milling followed by 5 min of resting) using a FRITSCH P-7. After recovery, the powders were pelletized and fired at 900 °C (heating rate of 5 °C min⁻¹) for 12 h under an O₂ atmosphere (ASAHI RIKA, ARF-MC). WO₂(O₂)(H₂O) was synthesized by a procedure reported in literature.³⁰ The resulting powder compounds were characterized by X-ray diffraction recorded using a Rigaku RINT TTR-III (Cu Kα radiation), and Rietveld refinements were performed using Jana 2006 software.⁴³ The crystal structures were drawn using VESTA.⁴⁴

Electrochemistry

Electrochemical measurements were carried out in Li/LiPF₆ in PC (1 mol L⁻¹, Kishida Chemical)/positive electrode batteries assembled in 2032-type coin cells. The positive electrodes were prepared by mixing 80 wt% active material with 10 wt% acetylene black (Denka) and 10 wt% polyvinylidene difluoride (Sigma-Aldrich) in *N*-methyl pyrrolidone (Kanto Chemical) to form a slurry, which was then coated onto Al foil (mass loading of *ca.* 1 mg cm⁻²). The obtained films were dried at 70 °C for several hours before punching the electrodes (diameter: 16 mm), which were then further dried under vacuum at 120 °C overnight before placing them into a glovebox. The positive and negative electrodes (Li foils) were separated by a glass fiber separator soaked with the electrolyte. All electrochemical measurements were controlled and recorded using a TOSCAT-3100 battery tester.

Sample preparation for X-ray absorption/emission spectroscopy

Samples for the X-ray absorption and emission spectroscopy experiments were prepared in 2032-type coin cells. The batteries were galvanostatically charged/discharged until a given voltage, and then the voltage was maintained until the residual current dropped to 0 mA. The batteries were recovered and disassembled in an Ar-filled glovebox and the electrodes were washed three to five times with anhydrous dimethyl carbonate and dried before being stored in air-tight containers. The samples were then transported to the synchrotron facility without exposure to air.

X-ray absorption/emission spectroscopy

The XAS and RIXS experiments were performed at BL07LSU, SPring-8.⁴⁵ For the oxygen K-edge XAS, the bulk-sensitive partial-fluorescence-yield (PFY) detection mode was employed. Flat-field type grazing incidence spectrometers were used for

the oxygen K-edge RIXS. All the measurements were performed at room temperature. The samples were taken out from the cell in the glove box filled with Ar gas, and then they were transferred into a vacuum chamber without exposure to air using a transfer vessel.

Ab initio calculations

Ab initio calculations were performed using the Vienna ab initio simulation package (VASP)46 using the projector-augmentedwave (PAW) method. 47,48 For Li₂MnO₃, the range-separated hybrid functional introduced by Heyd, Scuseria, and Ernzerhof (HSE) was used throughout the calculations. 28 The exact exchange fraction in the Hartree-Fock/density functional theory (DFT) hybrid functional and range-separation parameter are set at 0.25 and 0.2, respectively (HSE06). The DFT part of HSE06 employed a modified version of the Perdew-Burke-Ernzerhof functional (PBEsol)⁴⁹ according to literature. The kinetic energy cutoff was set to 520 eV and the k-point was sampled on a $(5 \times 3 \times 5)$ grid. The lattice parameters and atomic positions were relaxed until the forces on each atomic site were less than 0.01 eV \mathring{A}^{-1} . To model $\text{Li}_{1.2}\text{Ni}_{0.13}\text{Co}_{0.13}\text{Mn}_{0.54}\text{O}_2$, $\text{Li}_{29/24}\text{Ni}_{3/24}\text{Co}_{3/24}\text{Mn}_{13/24}\text{O}_2$ was considered and the structural configurations were determined by the genetic algorithm (GA) approach that optimizes the Li/Ni/Co/ Mn arrangement. The on-site Coulomb correction (GGA+U) was included for localized electronic states, and the U value was chosen to be 6.0, 3.4 and 3.9 eV for the 3d states of Ni, Co and Mn, respectively, according to literature. 50 During the GA procedure, we obtained the total energies using modified Perdew-Burke-Ernzerhof generalized gradient approximation (PBEsol-GGA)⁴⁹ by reducing the energy cutoff and the number of k points in the reciprocal cell to 360 eV and unity (Γ point sampling), respectively. After the GA cycles, the obtained five lowest energy configurations were recalculated with a sufficient energy cutoff (500 eV) and k point mesh (2 \times 2 \times 2 k-point meshes) using the HSE06 hybrid functional. U was not employed in the HSE calculations. The lowest energy configuration among the five configurations was chosen for Li_{29/24}Ni_{3/24}Co_{3/24}Mn_{13/24}O₂. Similarly, the Li and vacancy configurations for delithiated $Li_{29/24(1-x)}Ni_{3/24}Co_{3/24}Mn_{13/24}O_2$ were also determined by optimizing the Li/vacancy arrangement using the GA approach, and recalculated using the HSE06 functional for selected configurations. The calculated formation energies correspond to zero-Kelvin conditions. The GA approach was detailed in the ESI.† For WO₂(O₂)(H₂O), HSE06 hybrid functional was employed with the Grimme dispersion correction (DFT-D3)⁵¹ for hydrogen bonds. The energy cutoff was set to 520 eV with the k-point of $4 \times 6 \times 4$. The COOP was calculated by LOBSTER software.⁵²

Author contribution

M. O. and A. Y. conceived and directed the project. K. U. and B. M. B. synthesized and characterized Li₂MnO₃, $\text{Li}_{1,2}\text{Ni}_{0,13}\text{Co}_{0,13}\text{Mn}_{0.54}\text{O}_2$ and $\text{Na}_2\text{Ru}_{0.5}\text{Sn}_{0.5}\text{O}_3$. A. T. synthesized WO₂(O₂)(H₂O). T. S., K. U., A. T., D. A., T. S., Y. H. and M. O. measured and analysed the XAS, XES, and RIXS spectra.

T. M., X. M. S., T. S., E. W., and M. N. conducted the ab initio calculation. All authors wrote the manuscript.

Conflicts of interest

There are no conflicts to declare.

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