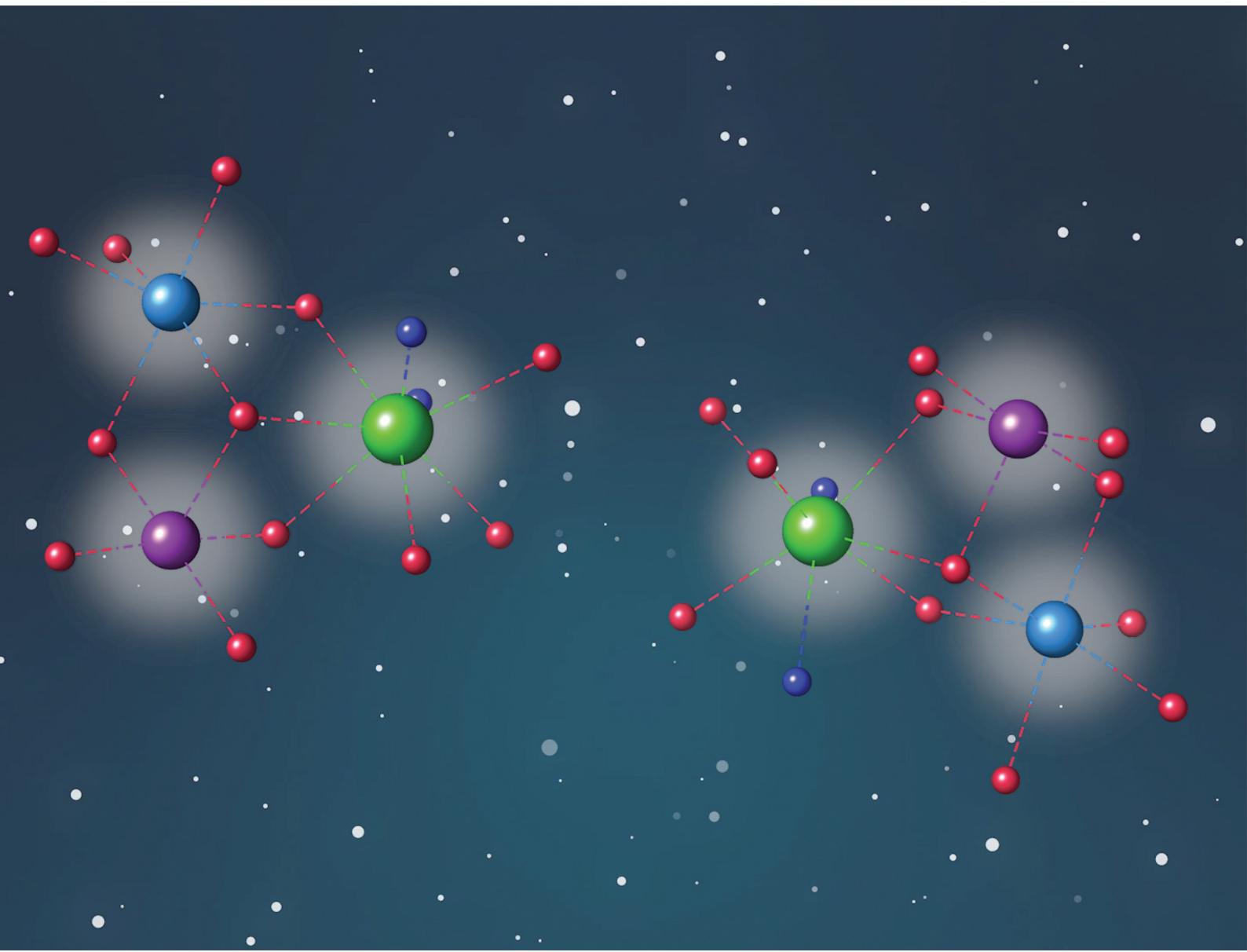


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## Magneto-structural studies of an unusual $[\text{Mn}^{\text{III}}\text{Mn}^{\text{II}}\text{Gd}^{\text{III}}(\text{OR})_4]^{4-}$ partial cubane from 2,2'-bis-*p*-<sup>t</sup>Bu-calix[4]arene<sup>†‡</sup>

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Reaction of 2,2'-bis-*p*-<sup>t</sup>Bu-calix[4]arene ( $\text{H}_8\text{L}$ ) with  $\text{MnCl}_2 \cdot 4\text{H}_2\text{O}$ ,  $\text{GdCl}_3 \cdot 6\text{H}_2\text{O}$  and 2,6-pyridinedimethanol ( $\text{H}_{2\text{pdm}}$ ) affords  $[\text{Mn}^{\text{III}}\text{Mn}^{\text{II}}\text{Gd}^{\text{III}}(\text{H}_3\text{L})(\text{pdm})(\text{MeOH})_2(\text{dmf})] \cdot 3\text{MeCN} \cdot \text{dmf}$  (**3**·3MeCN·dmf) upon vapour diffusion of MeCN into the basic dmf/MeOH mother liquor. **3** crystallises in the tetragonal space group  $P4_12_12$  with the asymmetric unit comprising the entire cluster. The highly unusual core contains a triangular arrangement of  $\text{Mn}^{\text{III}}\text{Mn}^{\text{II}}\text{Gd}^{\text{III}}$  ions housed within a  $[\text{Mn}^{\text{III}}\text{Mn}^{\text{II}}\text{Gd}^{\text{III}}(\text{OR})_4]^{4-}$  partial cubane. Magnetic susceptibility and magnetisation data reveal best fit parameters  $J_{\text{Mn}(\text{II})-\text{Mn}(\text{III})} = +0.415 \text{ cm}^{-1}$ ,  $J_{\text{Mn}(\text{III})-\text{Gd}(\text{III})} = +0.221 \text{ cm}^{-1}$ ,  $J_{\text{Mn}(\text{II})-\text{Gd}(\text{III})} = -0.258 \text{ cm}^{-1}$  and  $D_{\text{Mn}(\text{III})} = -4.139 \text{ cm}^{-1}$ . Theoretically derived magnetic exchange interactions, anisotropy parameters, and magneto-structural correlations for **3** are in excellent agreement with the experimental data.

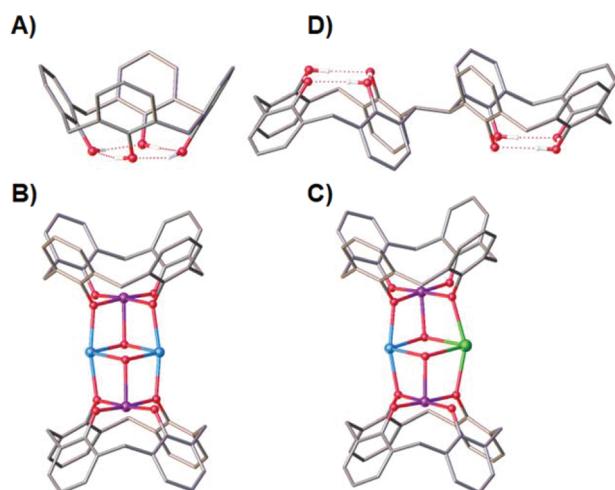
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## Introduction

Ligand design has always been central to the evolution of molecular magnetism, whether that be in order to manipulate exchange interactions,<sup>1</sup> direct magnetic anisotropy,<sup>2</sup> enhance magnetocalorics,<sup>3</sup> develop quantitative magneto-structural correlations,<sup>4</sup> construct specific topologies,<sup>5</sup> or self-assemble aesthetically pleasing structures – sometimes of enormous nuclearity.<sup>6</sup> Combined with ever-improving technical capabilities and theory, progress in this diverse field continues apace.<sup>7</sup>

*p*-<sup>t</sup>Bu-calix[4]arene (TBC[4], molecular framework minus <sup>t</sup>Bu groups shown in Fig. 1A) has proven to be a highly versatile ligand for the synthesis of a breadth of polymetallic transition metal (TM), lanthanide metal (LnM) and 3d-4f complexes, in which TM/LnM-TBC[4] moieties act as capping vertices.<sup>8</sup> The TBC[4] polyphenolato pocket is particularly suited to binding

the Jahn-Teller (JT) distorted  $\text{Mn}^{\text{III}}$  ion, because it can happily accommodate four short equatorial bonds and two long axial bonds. A good illustration of this comes in the complexes  $[\text{Mn}_2^{\text{III}}\text{Mn}_2^{\text{II}}(\text{OH})_2(\text{TBC}[4])_2(\text{dmf})_6]$  (**1**, Fig. 1B) and  $[\text{Mn}_2^{\text{III}}\text{Mn}^{\text{II}}\text{Gd}^{\text{III}}(\text{OH})_2(\text{TBC}[4])_2(\text{NO}_3)_6(\text{solvent})_6$  (**2**, Fig. 1C) whose structures can be considered as two  $[\text{Mn}^{\text{III}}(\text{TBC}[4])(\text{OH})$



**Fig. 1** Single crystal X-ray structures of TBC[4] (A), **1** (B), **2** (C),  $\text{H}_8\text{L}$  (D). Colour code C – grey, O – red,  $\text{Mn}^{\text{II}}$  – pale blue,  $\text{Mn}^{\text{III}}$  – purple,  $\text{Gd}^{\text{III}}$  – green, H – white. Hydrogen atoms (except those involved in lower-rim H-bonding in A and D), <sup>t</sup>Bu groups, ligated solvent molecules and co-crystallised anions omitted for clarity.

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†Dedicated to Prof. Alan Welch on the occasion of his retirement from Heriot-Watt University.

‡ Electronic supplementary information (ESI) available: Bond valence sum calculations, experimental/theoretical figures and tables to support discussion. CCDC 2020261. For ESI and crystallographic data in CIF or other electronic format see DOI: 10.1039/d0dt02731f



(DMF)] metalloligands encapsulating two  $Mn^{II}$  ions (**1**) or one  $Mn^{II}$  ion and one  $Gd^{III}$  ion (**2**).<sup>9</sup>

This general bonding motif has been exploited in the construction of a library of coordination compounds, allowing for the development of detailed empirical metal ion binding rules for TBC[4].<sup>10</sup> Under ambient reaction conditions, TBC[4] preferentially binds  $TM^{III}$  ions, will bind  $TM^{II}$  ions in the absence of  $TM^{III}$  ions, and will bind  $LnM^{III}$  ions in the absence of  $TM^{II}$  or  $TM^{III}$  ions.<sup>11</sup>

One might expect that a systematic move to *p*-*t*-Bu-calix[8]arene would result in ready binding of two  $Mn^{III}$  ions, however the nature of the ligand (*e.g.* pleated-loop) means that the polyphenolato pockets do not behave exactly as two TBC[4] equivalents. Instead, this ligand prefers to bind  $Ln^{III}$  ions under the standard conditions we employ, though forcing conditions can be used to form Mn-based clusters.<sup>12</sup> Although that is the case, the recent synthesis of TBC[4] molecules modified at one methylene bridge position allows this chemistry to be systematically expanded to include bis-TBC[4] molecules, an important example of which with respect to this paper is 2,2'-bis-*p*-*t*-Bu-calix[4]arene ( $H_8L$ , Fig. 1D).<sup>13</sup> This synthetic move to  $H_8L$  presents a molecule that truly represents two TBC[4]s as opposed to TBC[8], and a perfect opportunity to translate the aforementioned empirical metal ion binding rules.

The conformational flexibility (ring inversion) of TBC[4] in solution is well known,<sup>14</sup> and in the case of  $H_8L$ , presents the possibility of having a ligand with eight phenolic O-atoms in close proximity and, importantly, all converging/oriented in the same direction. This is very attractive from the perspective of polymetallic cluster growth with paramagnetic ions. We have recently begun exploring 3d, 4f and 3d-4f cluster formation with  $H_8L$ , and in doing so have reported a range of new clusters with varied nuclearity:  $[Mn_8]$ ,  $[Mn_{10}]$ ,  $[Mn_{20}]$ ,  $[Mn_6Gd_2]$ ,  $[Mn_8Gd_2]$ ,  $[Mn_4Gd_4]$ ,  $[Fe_5Gd_4]$ ,  $[Cu_{13}]$  and  $[Cu_4Tb_5]$ .<sup>15</sup> All of these cases show clear, systematic extension of the empirical metal ion binding rules established for TBC[4].  $H_8L$  has therefore already provided a wealth of new structural chemistry, and shows much promise for the discovery of fascinating new complexes (particularly when one considers the possibility of co-ligand addition, a common approach employed in cluster synthesis). Herein, we outline the synthesis, structure and magnetic behaviour of a new bis-TBC[4]-supported complex,  $[Mn^{III}Mn^{II}Gd^{III}(H_3L)(pdmH)(pdm)(MeOH)_2(dmf)]\cdot 3\text{MeCN}\cdot \text{dmf}$  (3-3MeCN·dmf; pdmH<sub>2</sub> = 2,6-pyridinedimethanol), together with theoretical magneto-structural studies examining the exchange interactions. The presence of the co-ligand in the resulting assembly breaks our empirical metal ion binding rules, and in doing so affords this new triangular cluster that is of interest from various perspectives.

## Results and discussion

Reaction of  $H_8L$  with  $MnCl_2\cdot 4H_2O$ ,  $GdCl_3\cdot 6H_2O$  and  $H_2pdm$  (in the presence of base,  $Et_3N$ ) affords single crystals of  $[Mn^{III}Mn^{II}Gd^{III}(H_3L)(pdmH)(pdm)(MeOH)_2(dmf)]\cdot 3\text{MeCN}\cdot \text{dmf}$

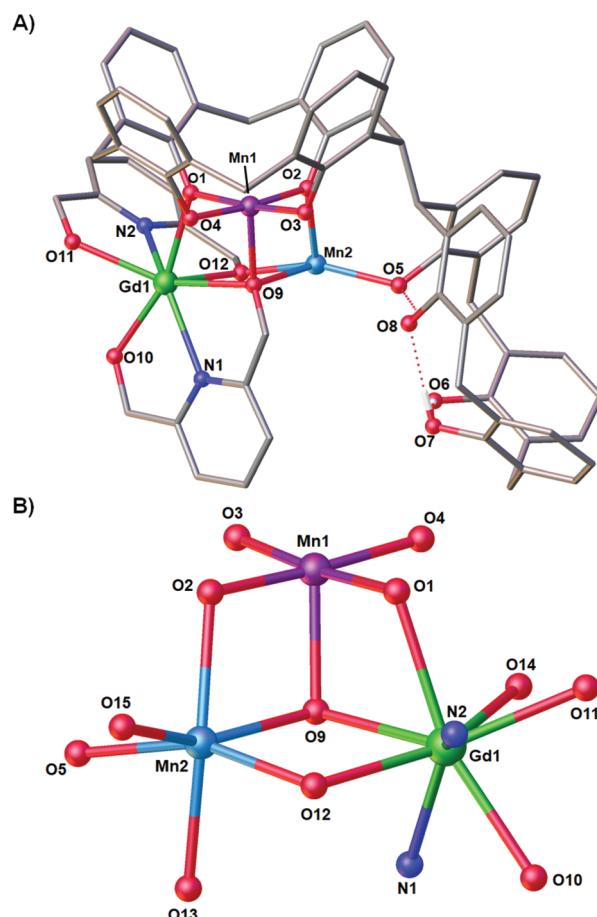


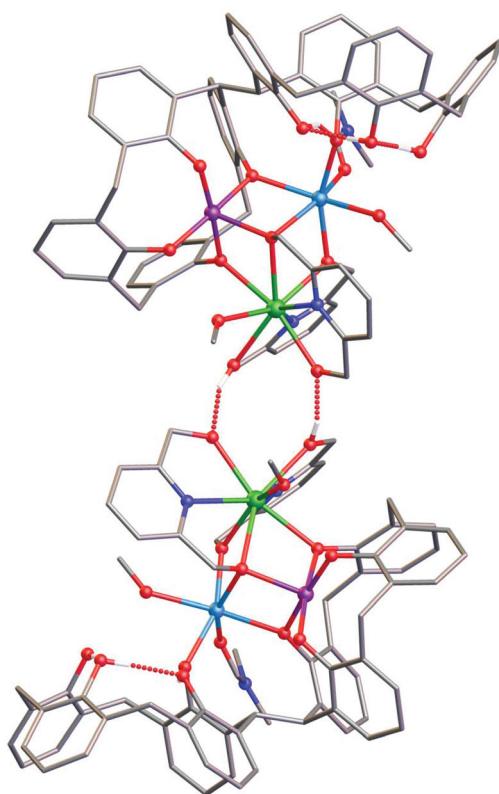
Fig. 2 (A) Single crystal X-ray structure of 3-3MeCN-dmf and (B) Metallic skeleton of 3-3MeCN-dmf highlighting the partial cubane arrangement. Selected labels have been added according to discussion. Colour code C – grey, O – red, N – royal blue,  $Mn^{II}$  – pale blue,  $Mn^{III}$  – purple,  $Gd^{III}$  – green, H – white. Hydrogen atoms (except those involved in lower-rim H-bonding), *t*-Bu groups, ligated solvent molecules and co-crystallised solvent/anions omitted for clarity.

(3-3MeCN·dmf, Fig. 2), upon vapour diffusion of MeCN into the basic dmf/MeOH mother liquor. The crystals were found to be in a tetragonal cell and structure solution was carried out in the space group  $P4_12_12$ . The ASU comprises the entire cluster, which has a triangular arrangement of  $Mn^{III}Mn^{II}Gd^{III}$  ions housed in a  $[Mn^{III}Mn^{II}Gd^{III}(OR)_4]^{4-}$  partial cubane. The bis-TBC[4] ligand has undergone conformational change although one of the calixarene binding sites remains unoccupied. This contravenes our established binding rules for this relatively new ligand, and we hypothesise that this is due to the steric constraints enforced by the pdm/pdmH co-ligands that play an important role in directing the prevailing structure.

$Mn1$  is in the trivalent state (Table S1‡) and is bound in a TBC[4] lower-rim tetraphenolato pocket ( $Mn1\text{--}O1\text{--}4$ , 1.873(8)–1.974(9) Å). Its coordination sphere is completed by a  $\mu_3\text{-}O$  atom belonging to the pdm molecule ( $Mn1\text{--}O9$ , 2.091(8) Å), which is also bonding  $Mn2$  and  $Gd1$  ( $Mn2\text{--}O9$ , 2.278(8) Å and  $Gd1\text{--}O9$ , 2.477(8) Å). There is a sixth, longer contact to a MeCN



molecule sitting in the calixarene cavity (Mn1–C020,  $\sim 4$  Å) and thus one can consider Mn1 as being either square pyramidal or pseudo-octahedral in geometry. Mn2 is in the bivalent state, adopting a distorted octahedral geometry and is located between the two TBC[4] moieties generated through inversion of the ligand. It is bonded to two  $\mu$ -phenoxides belonging to separate TBC[4] moieties (Mn2–O2, 2.224(8) Å and Mn2–O5, 2.150(8) Å), a  $\mu$ -O atom of the pdmH molecule (Mn2–O12, 2.097(10) Å), a ligated dmf molecule (Mn2–O15, 2.187(11) Å) and a ligated methanol molecule (Mn2–O13, 2.225(10) Å). Gd1 is octacoordinate, is in a square antiprismatic geometry and is bonded to a phenolic oxygen (Gd1–O1, 2.393(9) Å), a ligated methanol molecule (Gd1–O14, 2.457(10) Å) and the two pdm/H ligands (Gd1–N1, 2.519(12) Å; Gd1–O10, 2.331(9) Å; Gd1–O11, 2.404(9); Gd1–N2, 2.520(12) Å and Gd1–O12, 2.296(10) Å). Structure expansion reveals that the clusters pack *via* H-bonding interactions along the *c* axis, occurring between the protonated and deprotonated OH/O groups of neighbouring H-pdm/pdm molecules (O10…O11',  $\sim 2.47$  Å). The shortest metal–metal inter-cluster distance ( $\sim 5.9$  Å) also occurs along the *c* axis, between two neighbouring Gd ions (Fig. 3).

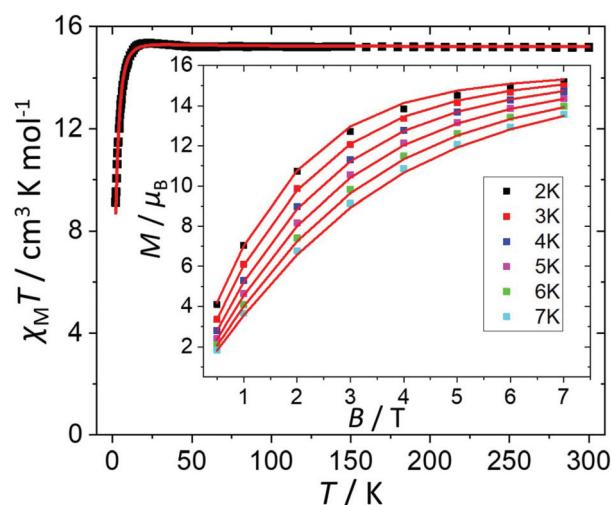


**Fig. 3** View orthogonal to the *c* axis in the extended structure of **3** showing the intermolecular hydrogen bonding interaction (dashed red lines). Colour code C – grey, O – red, N – royal blue, Mn<sup>II</sup> – pale blue, Mn<sup>III</sup> – purple, Gd<sup>III</sup> – green, H – white. Hydrogen atoms not involved in H-bonding, <sup>t</sup>Bu groups, co-crystallised solvent/anions omitted for clarity.

There are several points of interest to this seemingly rather simple structure. Complex **3** is in fact the first reported example of a heterometallic [Mn<sub>2</sub>Gd] triangle containing Mn in the trivalent and bivalent states (Table S1‡). The only other such triangle in the CSD has both Mn ions in the III<sup>+</sup> oxidation state.<sup>16</sup> There is also a single [MnGd<sub>2</sub>] species known, with Mn in the tetravalent state.<sup>17</sup> The triangular [Mn<sup>III</sup>Mn<sup>II</sup>Gd<sup>III</sup>] unit in compound **3** is also found in compound **2** and as a moiety in [Mn<sub>8</sub>Gd<sub>2</sub>].<sup>9</sup> Notably this is the first time that a TBC[4] polyphenolato pocket has ever been found to be unoccupied in our studies on 3d/4f coordination chemistry, and it is also the first example in which the bis-TBC[4] ligand is not fully deprotonated, acting here as a penta- (H<sub>5</sub>L) rather than octa-anion (L). As with all our other studies on TBC[4] and bis-TBC[4], the Mn<sup>III</sup> ion preferentially sits in the polyphenolic pocket and acts as a [Mn<sup>III</sup>(TBC[4])]<sup>–</sup> capping fragment/metalloligand.

### Magnetic behaviour

The direct current (dc) molar magnetic susceptibility,  $\chi$ , of a freshly prepared polycrystalline sample of **3** was measured in an applied field, *B*, of 0.5 T, over the 2–300 K temperature, *T*, range. The experimental results are showed in Fig. 4, in the form of the  $\chi_M T$  product, where  $\chi = M/B$ , and *M* is the magnetisation of the sample. At room temperature the  $\chi_M T$  product of **3** has a value of 15.0 cm<sup>3</sup> K mol<sup>–1</sup>, in good agreement with the sum of the Curie constants for non-interacting Mn<sup>III</sup> (*s* = 2), Mn<sup>II</sup> (*s* = 5/2) and Gd<sup>III</sup> (*s* = 7/2) ions, assuming *g* = 2.00 (15.25 cm<sup>3</sup> k mol<sup>–1</sup>). As temperature decreases, the  $\chi_M T$  product remains essentially invariant to  $\sim 50$  K before increasing slightly to reach a value of  $\sim 15.2$  cm<sup>3</sup> K mol<sup>–1</sup> at *T* = 20 K, before abruptly decreasing to a value of  $\sim 9.0$  cm<sup>3</sup> K mol<sup>–1</sup> at *T*



**Fig. 4** Plot of  $\chi_M T$  vs. *T* in the range *T* = 2–300 K and *B* = 0.5 T. Inset: field dependence of the magnetization (*M*) measured in the *T* = 2–7 K and *B* = 0.5–7.0 T temperature and field ranges. The (□) symbols represent the experimental data and the solid red lines the fit of the experimental data to spin-Hamiltonian (1). See text for details.



= 2.0 K. This is clearly indicative of the presence of very weak magnetic exchange interactions. In order to gain more insight into the low temperature energy spectrum of 3, low temperature variable-temperature-and-variable-field (VTVB) magnetisation data were measured in the temperature range 2–7 K, in magnetic fields from 0.5 to 7.0 T (Fig. 4 inset). At the lowest temperature and highest field,  $M$  reaches a value of  $\sim 15.2 \mu_B$ . To quantitatively interpret the magnetic properties of 3, we use the following general spin-Hamiltonian (1):

$$\hat{H} = \sum_i D_i (\hat{S}_{z,i}^2 - S_i(S_i + 1)/3) + \mu_B B \sum_i g_i \hat{S}_i - 2 \sum_{i,j < 1} J_{ij} \hat{S}_i \cdot \hat{S}_j \quad (1)$$

where the summation indices  $i, j$  run through the constitutive metal centres,  $D$  is the uniaxial single-ion anisotropy parameter of  $\text{Mn}^{\text{III}}$ ,  $\hat{S}$  is a spin operator,  $S$  is the total spin and  $J$  is the isotropic exchange interaction parameter.

The  $\chi_M T$  and VTVB magnetisation data were simultaneously fitted to spin-Hamiltonian (1) using the program PHI assuming three different exchange interactions in the  $[\text{Mn}^{\text{III}}\text{Mn}^{\text{II}}\text{Gd}^{\text{III}}]$  triangle.<sup>18</sup> This results in the following best fit (error) parameters:  $J_{\text{Mn}^{\text{II}}-\text{Mn}^{\text{III}}} = +0.415 (1.4 \times 10^{-2}) \text{ cm}^{-1}$ ,  $J_{\text{Mn}^{\text{III}}-\text{Gd}^{\text{III}}} = +0.221 (5.7 \times 10^{-3}) \text{ cm}^{-1}$ ,  $J_{\text{Mn}^{\text{II}}-\text{Gd}^{\text{III}}} = -0.258 (3.8 \times 10^{-3}) \text{ cm}^{-1}$  and  $D_{\text{Mn}^{\text{III}}} = -4.139 (4.8 \times 10^{-2}) \text{ cm}^{-1}$ , with the  $g$ -factors fixed at  $g = 2.00$  for  $\text{Mn}^{\text{II}}$  and  $\text{Gd}^{\text{III}}$  and  $g = 1.98$  for  $\text{Mn}^{\text{III}}$ . Therefore, the  $\text{Mn}^{\text{III}}-\text{Mn}^{\text{II}}$  interaction and the  $\text{Mn}^{\text{III}}-\text{Gd}^{\text{III}}$  interaction are very weakly ferromagnetic and the  $\text{Mn}^{\text{II}}-\text{Gd}^{\text{III}}$  interaction is very weakly antiferromagnetic. These parameters are similar to those found for complex 2.<sup>9</sup> With these parameters the ground spin-state of 3, when only the isotropic part of spin-Hamiltonian (1) is taken into account, is an  $S = 4$  spin-state, lying very close to several excited spin states (Fig. 5).

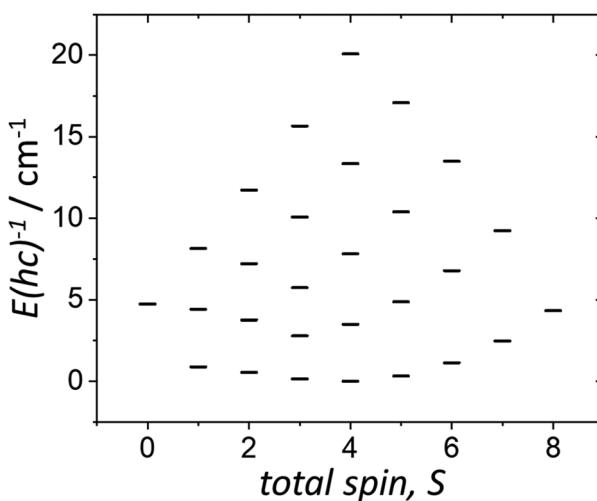


Fig. 5 Energy spectrum of 3 at zero magnetic field, for the isotropic part of spin-Hamiltonian (1), with the determined best-fit parameters, as described in the text.

## Theoretical studies

To understand the origin of the magnetic exchange interactions in more detail we have performed *ab initio* calculations on a model complex, 3A (Fig. S1‡), using the MOLCAS 8.0 suite.<sup>19</sup> Model 3A has the same structure as 3, but with the terminal  $^t\text{Bu}$  groups on the calixarene ligand replaced with Me groups to reduce computational cost.

We have first performed *ab initio* CASSCF<sup>20</sup>/RASSI-SO<sup>21</sup>/SINGLE\_ANISO<sup>22</sup> calculations on the individual paramagnetic ions. The  $\text{Mn}^{\text{III}}$  centre shows moderate easy-axis anisotropy ( $D = -3.3 \text{ cm}^{-1}$ ,  $E = 0.1 \text{ cm}^{-1}$ ,  $g_{xx}/g_{yy}/g_{zz} = 1.99/1.99/1.96$ ), whereas the other two paramagnetic centres,  $\text{Gd}^{\text{III}}$  and  $\text{Mn}^{\text{II}}$ , are found to be isotropic ( $g_{xx} = g_{yy} = g_{zz} = 2.00$ ). These values are as expected, and in accordance with the experimental values. Next, we have performed POLY\_ANISO calculations, which includes the Lines model, to estimate the magnetic coupling constants.<sup>23</sup> The so-obtained exchange interactions are given in Table 1 and are in good agreement with the experimental values and simulate the susceptibility data well (Fig. 6a). The  $J_{\text{Mn}^{\text{II}}-\text{Mn}^{\text{III}}}$  and  $J_{\text{Mn}^{\text{III}}-\text{Gd}^{\text{III}}}$  interactions are found to be weakly ferromagnetic, whereas  $J_{\text{Mn}^{\text{II}}-\text{Gd}^{\text{III}}}$  is found to be weakly antiferromagnetic. It is worth noting that for both  $J_{\text{Mn}^{\text{II}}-\text{Gd}^{\text{III}}}$  and  $J_{\text{Mn}^{\text{III}}-\text{Gd}^{\text{III}}}$  the dipolar contribution is calculated to be dominant, as seen previously for other 3d-4f complexes.<sup>24</sup>

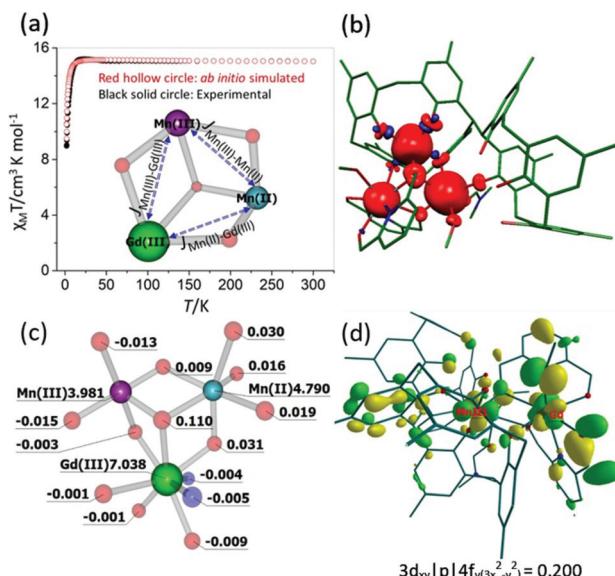
To further confirm the magnetic exchange values, we have performed density functional theory (DFT) calculations in the G09 suite using two different methods (see computational details section for more information).<sup>25</sup> In the first method, we have performed calculations on model 3A. In the second method, we have performed pairwise exchange interaction calculations on model complexes containing only two paramagnetic centres, replacing the third paramagnetic centre with a diamagnetic element, *i.e.*  $\text{Gd}^{\text{III}}/\text{Mn}^{\text{III}}/\text{Mn}^{\text{II}}$  with  $\text{Y}^{\text{III}}/\text{Ga}^{\text{III}}/\text{Zn}^{\text{II}}$ , respectively (Fig. S1(b)–(d)).‡ The computed magnetic exchange values from both methods are in good agreement with the *ab initio* calculated values (Table 1).

The spin densities for model 3A (Fig. 6(b) and (c), Fig. S2‡) reveal that while dominant spin delocalisation is observed for both the  $\text{Mn}^{\text{III}}$  (3.981) and  $\text{Mn}^{\text{II}}$  (4.790) ions, spin polarisation is detected for  $\text{Gd}^{\text{III}}$  (7.038). The  $\mu_3$ -bridging O-atom (O9, Fig. 2) has a spin density of 0.110, more than three times higher than any other bridging atoms in the molecule, and is therefore expected to play a dominant role in the magnetic

Table 1 *Ab initio* POLY\_ANISO derived magnetic exchange interaction parameters in 3. The values in parentheses are calculated from DFT. The bold values are calculations performed on model complex 3A shown in Fig. S1(a).‡ The italicised values are the pairwise exchange interactions calculated on the model complexes shown in Fig. S1(b)–(d) in which the  $\text{Mn}^{\text{III}}$ ,  $\text{Mn}^{\text{II}}$  and  $\text{Gd}^{\text{III}}$  ions are, in turn, replaced with the diamagnetic  $\text{Ga}^{\text{III}}$ ,  $\text{Zn}^{\text{II}}$  and  $\text{Y}^{\text{III}}$  ions

	$J^{\text{total}}/\text{cm}^{-1}$	$J^{\text{exchange}}/\text{cm}^{-1}$	$J^{\text{dipolar}}/\text{cm}^{-1}$
$J_{\text{Mn}^{\text{II}}-\text{Mn}^{\text{III}}}$	+0.50	+0.52 (1.04/1.10)	-0.02
$J_{\text{Mn}^{\text{III}}-\text{Gd}^{\text{III}}}$	+0.10	-0.12 (-0.08/-0.08)	+0.22
$J_{\text{Mn}^{\text{II}}-\text{Gd}^{\text{III}}}$	-0.16	+0.08 (0.12/0.14)	-0.24





**Fig. 6** (a) *Ab initio* simulated, temperature dependent  $\chi_M T$  versus  $T$  data for 3. The solid black circles are the experimental data and the hollow red circles the *ab initio* derived data. The core structure of 3 with magnetic coupling scheme is shown in the inset. (b) and (c) DFT computed spin density plot together with spin density values on selected atoms for model 3A. (d) Representative molecular orbital showing the  $3d_{xy}|p|4f_y(3x^2-y^2)$  interaction for  $Mn^{III}-Gd^{III}$  pair. See Table S2‡ for the computed overlap integral values for the  $Mn^{II}-Gd^{III}$ ,  $Mn^{II}-Gd^{II}$  and  $Mn^{II}-Mn^{III}$  pairs.

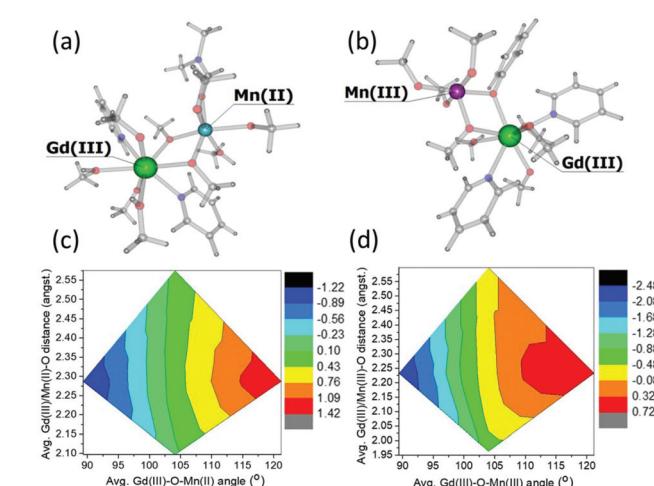
superexchange. It is also worth mentioning here that the *p*-Me groups, which we have used in place of the *t*Bu groups in 3A have a spin density very close to zero, suggesting the model to be reliable.

Previous studies performed on 3d-4f complexes have emphasised the importance of the 3d orbitals of the transition metals in controlling the two possible contributions ( $J_F$  and  $J_{AF}$ ) to the total magnetic exchange interaction.<sup>26</sup> The first contribution,  $J_F$ , where partial electron transfer occurs from the 3d orbitals of the  $Mn^{III}/Mn^{II}$  ions to the empty 5d/6s orbitals of  $Gd^{III}$  ion, adds to the ferromagnetic part of the magnetic exchange interaction. The larger the charge transfer the larger the ferromagnetic contribution. The second contribution,  $J_{AF}$ , arises from overlap between the non-orthogonal, singly occupied molecular orbitals (SOMOs) of the 3d ion with the half-filled 4f orbitals of the  $Gd^{III}$  ions. The former contribution to the magnetic exchange interaction can be estimated using natural bonding orbital (NBO) analysis which investigates the charge transfer, whereas the latter contribution can be estimated by performing overlap integral calculations. For  $J_{Mn^{II}-Gd^{III}}^{exchange}$ , all the overlap integral values are small leading to a small ferromagnetic exchange interaction (Table S2‡). For  $J_{Mn^{III}-Gd^{III}}^{exchange}$ , one overlap integral value is estimated to be relatively strong ( $3d_{xy}|p|4f_y(3x^2-y^2)$ , Fig. 6d) leading to a small anti-ferromagnetic exchange interaction. This is opposite to that obtained from the experimental fit, though we note the absolute magnitude of the difference is extremely small. Larger charge transfer from  $Mn^{II}(3d) \rightarrow Gd^{III}(6s/5d)$  compared to  $Mn^{III}(3d) \rightarrow Gd^{III}(6s/5d)$  further supports this. For  $J_{Mn^{II}-Gd^{III}}^{exchange}$

all the overlap integral values are estimated to be small leading to a small ferromagnetic exchange interaction.

To investigate these interactions a little further, we have performed a magneto-structural correlation by varying the  $Mn^{III}/Mn^{II}-O-Gd^{III}$  angle, the  $Mn^{III/II}/Gd^{III}-O$  distance and the  $Mn^{III/II}-O-Gd^{III}-O$  dihedral angle on bimetallic model complexes designed from complex 3. The models  $3_{Mn^{II}-Gd^{III}}$  and  $3_{Mn^{III}-Gd^{III}}$  are shown in Fig. 7(a) and (b), respectively. The sign and magnitude of  $J_{Mn^{II}-Gd^{III}}^{exchange}$  and  $J_{Mn^{III}-Gd^{III}}^{exchange}$  are in good agreement with those in Table 1 (+0.26  $cm^{-1}$  and  $-0.22\ cm^{-1}$ , respectively). Magneto-structural correlations developed for  $J_{Mn^{II}-Gd^{III}}^{exchange}$  and  $J_{Mn^{III}-Gd^{III}}^{exchange}$  suggest that the  $Mn^{III}/Mn^{II}-O-Gd^{III}$  angle is the most dominant structural parameter (Fig. 7(c) and (d), Fig. S3‡). At smaller angles the anti-ferromagnetic interaction is favoured, at the larger angles the ferromagnetic interaction is favoured. This is as expected, since at smaller angles larger overlap between the  $Gd(4f)$  and  $Mn^{II/III}(3d)$  orbitals are observed, diminishing with increasing angle (Fig. S4, Tables S3 and S4‡). These findings are in agreement with previous theoretical studies on di-, tri- and tetranuclear  $Mn^{III}-Gd^{III}$  cluster compounds.<sup>26</sup>

In search of models representing  $J_{Mn^{II}-Mn^{III}}^{exchange}$ , we have developed two different models ( $3_{Mn^{II}-Mn^{III}} - 1$  and  $3_{Mn^{II}-Mn^{III}} - 2$ , Fig. S5‡). In both models the rigidity provided by the 2,2'-bis-*p*-Bu-calix[4]arene ligand needs to be removed in order to obtain a model whereby structural parameters can be fine-tuned. However, as soon as we remove  $H_8L$ , the sign of the magnetic exchange interaction switches from ferromagnetic to antiferromagnetic (Fig. S5‡) due to presence of two strong magnetic orbital overlaps ( $Mn^{II}d_{yz}|p|Mn^{III}d_{z^2}$



**Fig. 7** Models  $3_{Mn^{II}-Gd^{III}}$  (a) and  $3_{Mn^{III}-Gd^{III}}$  (b) together with the magneto-structural correlation contour plots (c) and (d) performed by varying the average  $Mn^{II}/Mn^{III}-O-Gd^{III}$  angle and average  $Mn^{III/II}/Gd^{III}-O$  distance with respect to the magnetic exchange coupling constants  $J_{Mn^{II}-Gd^{III}}^{exchange}$  and  $J_{Mn^{III}-Gd^{III}}^{exchange}$ . The keys represents the magnitude of the exchange, ranging from most antiferromagnetic (black) to most ferromagnetic (red). For both models, the change in the magnitude of the interaction with respect to the change in  $Mn^{III/II}-O-Gd^{III}-O$  dihedral angle is minimal. See Fig. S3 of the ESI for more details.‡



and  $Mn(\text{II})d_{x^2-y^2}|p|Mn(\text{III})d_{z^2}$  for  $3_{Mn(\text{II})-Mn(\text{III})} = 1$  and  $Mn(\text{II})d_{yz}|p|Mn(\text{III})d_{z^2}$  and  $Mn(\text{II})d_{xz}|p|Mn(\text{III})d_{z^2}$  for  $3_{Mn(\text{II})-Mn(\text{III})} = 2$ , Table S5, Fig. S6 and 7‡). Although this renders any further investigation moot, the above does highlight both the structural and magnetic importance of the calixarene ligand. Ligand rigidity is rarely a consideration in design criteria when contemplating the nature of magnetic exchange. Considering the bond angles and distances in **3** in tandem with previous magneto-structural studies developed for a variety of  $Mn^{\text{III}}-Mn^{\text{II}}$  species, would infer a small ferromagnetic interaction being present in complex **3**, in agreement with our calculated  $J_{Mn(\text{II})-Mn(\text{III})}^{\text{exchange}}$  value.<sup>27</sup>

## Conclusions

Reaction of bis-TBC[4] with  $MnCl_2 \cdot 4H_2O$ ,  $GdCl_3 \cdot 6H_2O$  and  $H_2pdm$  results in the formation of the complex  $[Mn^{\text{III}}Mn^{\text{II}}Gd^{\text{III}}(H_3L)(pdmH)(pdm)(MeOH)_2(dm)]$  (**3**) whose structure describes a triangular arrangement of  $Mn^{\text{III}}Mn^{\text{II}}Gd^{\text{III}}$  ions housed in a  $[Mn^{\text{III}}Mn^{\text{II}}Gd^{\text{III}}(\text{OR})_4]^{4-}$  partial cubane. Although the bis-TBC[4] has undergone conformational change as the penta-anion (Fig. 2A), one lower-rim pocket remains unoccupied which is likely due to the steric constraints enforced by the co-ligands. Compound **3** is the first example of a heterometallic  $[Mn_2Gd]$  triangle containing Mn in the trivalent and bivalent states, although this unit has previously been observed within the larger species  $[Mn_2^{\text{III}}Mn^{\text{II}}Gd^{\text{III}}]$  (**2**) and  $[Mn_8Gd_2]$ , constructed from TBC[4] and bis-TBC[4], respectively. Susceptibility and magnetisation data reveal very weak exchange interactions between the constituent metal centres, with best fit parameters  $J_{Mn(\text{II})-Mn(\text{III})} = +0.415 (1.4 \times 10^{-2}) \text{ cm}^{-1}$ ,  $J_{Mn(\text{III})-Gd(\text{III})} = +0.221 (5.7 \times 10^{-3}) \text{ cm}^{-1}$ ,  $J_{Mn(\text{II})-Gd(\text{III})} = -0.258 (3.8 \times 10^{-3}) \text{ cm}^{-1}$  and  $D_{Mn(\text{III})} = -4.139 (4.8 \times 10^{-2}) \text{ cm}^{-1}$ , consistent with those seen in  $[Mn^{\text{III}}_2Mn^{\text{II}}Gd^{\text{III}}]$  (**2**). *Ab initio* calculated magnetic exchange interactions, anisotropy parameters, and theoretical magneto-structural correlations for **3** are found to be in excellent agreement with the experimental data, highlighting the importance of  $Mn^{\text{III}}/Mn^{\text{II}}-\text{O}-Gd^{\text{III}}$  angles and the rigidity of the 2,2'-bis-*p*-Bu-calix[4]arene ( $H_8L$ ) ligand in governing the sign and magnitude of the exchange interactions.

## Experimental section

$H_8L$  was synthesised according to literature procedure.<sup>13</sup>

### Synthesis of $[Mn^{\text{III}}Mn^{\text{II}}Gd^{\text{III}}(H_3L)(pdmH)(pdm)(MeOH)_2(dm)] \cdot 3\text{MeCN} \cdot dm$ , $3 \cdot 3\text{MeCN} \cdot dm$

$H_8L$  (150 mg, 0.116 mmol),  $MnCl_2 \cdot 4H_2O$  (23 mg, 0.116 mmol),  $GdCl_3 \cdot 6H_2O$  (35 mg, 0.116 mmol) and  $pdmH_2$  (32.2 mg, 0.232 mmol) were suspended in a 1:1 dmf/MeOH mixture (20 mL) and stirred for 10 minutes.  $Et_3N$  (0.15 mL) was added and the resulting purple solution was stirred for additional 2 hours and then filtered. The mother liquor was allowed to

slowly diffuse with acetonitrile vapours, affording dark purple crystals suitable for X-ray diffraction studies. Elemental analysis (%) calculated for **1**,  $C_{116}H_{151}Mn_2GdN_7O_{16}$  ( $M = 2166.6$ ): C, 64.31%; H, 7.02%; N, 4.53%. Found: C, 64.24%; H, 6.83%; N, 4.23%. Yield 51 mg (20.3%). Crystal data for **3** (CCDC 2020261‡):  $C_{116}H_{151}Mn_2GdN_7O_{16}$ ,  $M = 2166.6$ ,  $0.3 \times 0.03 \times 0.01 \text{ mm}^3$ , tetragonal, space group  $P4_12_12$  (no. 92),  $a = 23.2275(8) \text{ \AA}$ ,  $c = 44.2459(18) \text{ \AA}$ ,  $V = 23.871.4(19) \text{ \AA}^3$ ,  $Z = 8$ , Bruker D8 diffractometer equipped with a PHOTON 100 detector, synchrotron radiation,  $\lambda = 0.7749 \text{ \AA}$ ,  $T = 100(15) \text{ K}$ ,  $2\theta_{\text{max}} = 48.852^\circ$ , 151 662 reflections collected, 15 095 unique ( $R_{\text{int}} = 0.0531$ ). Final  $\text{Goof} = 1.037$ ,  $R_1 = 0.0854$ ,  $wR_2 = 0.1763$ .

## Computational details

We have performed *ab initio* CASSCF<sup>20</sup>/RASSI-SO<sup>21</sup>/SINGLE\_ANISO<sup>22</sup> calculations on a model complex, **3A**, made from the X-ray structure to estimate the magnetic coupling constants in complex **3** using the MOLCAS 8.0 suite.<sup>19</sup> We have considered each paramagnetic ion separately by keeping the ions of interest and substituting the third paramagnetic ion with a diamagnetic ion, *i.e.*  $Gd^{\text{III}}/Mn^{\text{III}}/Mn^{\text{II}}$  with  $Y^{\text{III}}/\text{Ga}^{\text{III}}/\text{Zn}^{\text{II}}$ . We have used the H.ANO-RCC...2s, C.ANO-RCC...3s2p., N.ANO-RCC...3s2p., O.ANO-RCC...3s2p1d., Mn.ANO-RCC...5s4p2d1f., Zn.ANO-RCC...5s4p2d., Ga.ANO-RCC...5s4p1d., Y.ANO-RCC...6s5p3d., Gd.ANO-RCC...7s6p4d2f1g basis sets.<sup>28</sup> During CASSCF calculations for a single  $Gd^{\text{III}}$  ion, we have used seven electrons in seven active 4f orbitals. For the  $Mn^{\text{III}}$  and  $Mn^{\text{II}}$  ions we have used four and five electrons, respectively, in five active 3d orbitals. Next, in the RASSI-SO step for the  $Gd^{\text{III}}$  ion, we have used 1, 48 and 76 roots for the octet, sextet and quartet spin multiplicities. For the  $Mn^{\text{III}}$  ion, 5, 45 and 50 roots for quintet, triplet and singlet spin multiplicities have been used, respectively. For the  $Mn^{\text{II}}$  ion, 1, 24 and 75 roots for sextet, quartet and doublet spin multiplicities have been used, respectively.<sup>24,29</sup> The resultant spin-orbit multiplets have been used further to estimate local magnetic properties *via* the SINGLE\_ANISO approach.<sup>22</sup> The magnetic exchange interactions ( $J_s$ ) have been computed between all paramagnetic ions for all complexes by fitting *ab initio* POLY\_ANISO with the experimental data.<sup>23a</sup>

We have also used the G09 programme on model complex **3A** to estimate the magnetic coupling constant.<sup>25</sup> Noddlemann's broken symmetry<sup>30</sup> together with the B3LYP functional<sup>31</sup> is known to be a reliable approach to estimate magnetic exchange coupling constants.<sup>32</sup> We have used the relativistically corrected effective core potential (ECP) basis set of Cundari and Stevens (CSDZ) for the  $Gd^{\text{III}}$  ion,<sup>33</sup> Ahlrichs-TZV basis set for the Mn ions,<sup>34</sup> and the 6-31G\*\* basis set for O, N, C and H atoms.<sup>35</sup> We have computed four spin configurations to estimate three possible exchange coupling constants. The computed spin configurations include a high spin configuration with all spins up and three other configurations with one of the spin centres down. We have used the same methodology mentioned earlier for performing natural bonding orbitals (NBOs) analysis to investigate the charge transfer.<sup>32d,e</sup>



## Conflicts of interest

There are no conflicts to declare.

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