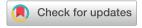
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Insight into the diffusion mechanism of sodium ion-polaron complexes in orthorhombic P2 layered cathode oxide Na_xMnO₂

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Using the density functional theory, we investigated the geometric, electronic structure, phase stability and electrochemical properties of a potential P2 layer orthorhombic cathode material Na_xMnO_2 (0 $\leq x \leq$ 1) applied for sodium-ion batteries. Herein, we shed the light on the undeniable effect of the polaron formation and polaron migration on the diffusion of Na⁺ ions in the orthorhombic P2 layered oxides. Both GGA+U and HSE06 methods agree that, when a Na⁺ ion is removed from the fully charged state of NaMnO₂, the accompanying polaron preferably forms at one of the third nearest Mn (3NN) octahedra to the Na vacancy, implying the oxidization of the Mn^{3+} ion at one of these 3NN sites to Mn^{4+} . The positive polaron migrates simultaneously with the Na vacancy and would hinder the diffusion of Na ions. Two kinds of elementary diffusion processes, named parallel and crossing, have been explored which required almost same activation energy of about 423 meV (518 meV) by GGA+U (HSE06). In the fully discharged state, GGA+U and HSE06 methods indicate that the negative polaron forms at one of the second nearest Mn neighbours (2NN). The activation energy of 273 meV (327 meV) is needed for diffusion in a structure with a low Na concentration, which is much lower than that required for diffusion in the Na-rich regime. Consequently, Na⁺ ions can diffuse easier at lower Na concentrations. With the overall activation energy of 423 meV (518 meV), this material exhibits a faster ion diffusion in comparison with the prevailing lithium-based materials such as olivine phosphate.

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Introduction

In recent decades, secondary lithium-ion batteries (LIBs) have emerged as crucial energy storage components of electronic portable devices and vehicles. However, the Li abundance is just 0.0017% of the Earth's crust.2 With the ever-increasing energy demand and the limited availability of Li element in the Earth's crust, it has been predicted that the Li abundance will be inadequate to the raw materials consumption for the LIBs productions. As a consequence, it has been anticipated that the world's energy storage market would experience a quick upturn in LIBs' prices. In order to meet the highly increasing energy storage applications, several alternative elements such as Na, K, and Mg, have been used as charge carriers in the ion batteries. Among them, Na element is well-known as possessing the innate electrochemical affinity with Li, and recognized as the sixth order in the most plentiful elements, which contributes to 2.3% of the Earth's crust and 1.1% of the ocean.³ Therefore, sodium-based compounds have attracted a great deal of attention and expected to become the next generation of rechargeable batteries, named sodium-ion batteries (SIBs). Various materials such as NASICON, olivine phosphate, have been suggested to be promising candidates with similar electrochemical properties as Li analogous compounds. The apparent explanation is that sodium ions can diffuse easily inside the materials even though it possesses a larger ionic radius and atomic weight (r_{Na} = 0.98 Å, $m_{\rm Na} = 23 \text{ g mol}^{-1}$) compared with those of lithium ($r_{\rm Li} = 0.69 \text{ Å}$, $m_{\rm Li} = 6.9 \text{ g mol}^{-1}$).

In structure, three indispensable components of any rechargeable batteries are cathode, 5-18 anode 19,20 and electrolyte, 21,22 in which the cathode primarily determines the overall cell voltage. Among the materials for cathode, layered oxides A_xMO₂

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Paper

(where A stands for alkali metal with concentration of x, and M represents transition metals such as Mn, Fe, Ni, and Co) are in the spotlight as the most promising alternatives with high voltage (2.0–3.5 V) and capacity (150–210 mA h g $^{-1}$) for both LIBs and SIBs. $^{23-32}$ Among several types of layered oxides classified by Delmas *et al.*, 33 O3 and P2 layered oxides, in which sodium ions locate at octahedral sites (denoted as O) and prismatic sites (denoted as P), respectively; the numbers 3 and 2 stand for the number of MO₂ layers in a unit cell, are two most prevailing synthesized layered oxides groups. Although O3 layered oxides deliver a higher capacity, the better electrochemical performance with lower diffusion barrier and higher ionic conductivity was recorded in P2 layered oxides. In addition, O3 materials often exhibit hygroscopic property while P2 materials are more stable in ambient condition.

Amid the P2 layered transition metals based oxides (Mn, Co, Ni), the sodium manganese oxide Na_xMnO₂ holds scientists spellbound more due to its cheaper cost and easier for synthesis. 37-40 Two single-phase samples reported in experiments by slow cooling and quenching methods show hexagonal (space group P63/mmc, denoted by P2) and orthorhombic (space group Cmcm, denoted by P'2) phases.³⁸ Both two phases exhibit a voltage window of 2.0-3.8 V. Even though the P2 phase samples exhibit a little higher cycle number (120 cycles), the P'2 phase materials deliver a significantly higher specific capacity of 210 mA h g⁻¹ than the P2 phase (140 mA h g⁻¹). Since the concentration of Na reaches more than 0.67 (x > 0.67), P2 layered phase shows a phase transformation to P'2, while P'2 layered material also experiences a phase transformation to OP4 at low concentration (x < 0.25). The phase transformation causes a rough discharging voltage profile over the capacity. An idea of doping other metals such as Fe, Co, Ni, Li, Mg, and Zn, has been indicated in many previous experimental and theoretical investigations to improve the stability and obtain better electrochemical properties. 44-47 Even though the smoother voltage lines have been reported, the phase transformation has been also observed in those doped materials. 46,47 Although there are many investigations of layered oxides for cathode materials, the Jahn-Teller effect and diffusion mechanism have not been addressed clearly so that more profound investigations are essential to perform.

In previous reports, 5,48-51 many scientists pointed out the importance of a quasi-particle, named small polaron, to the diffusion of Li⁺/Na⁺ ion inside the transition-metal-based materials. The small polaron is formed due to the local distortion after the oxidation/reduction of transition metals. With a strong binding energy of 500 meV between the alkali vacancy/ ion and the positive/negative polaron, 48 the polaron migrates simultaneously with the diffusion of Li/Na vacancy/ion, and the polaron migration generally lowers the diffusion of those charge carriers inside the materials. The arrangement of the geometric structure and the polaron effect are incontrovertible during charging/discharging processes and would be clearly depicted for a better diffusion prediction. Several types of elementary diffusion paths might require different activation energies.5 Herein, we present a comprehensive density functional theory (DFT) investigation of the geometrical and

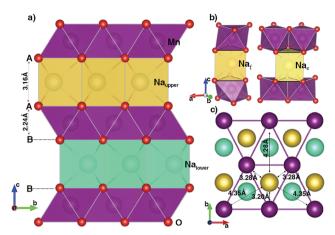


Fig. 1 The geometric structure of P2 orthorhombic NaMnO₂. The violet, red, yellow and cyan balls stand for Mn, O, Na_{upper} and Na_{lower} atoms, respectively. The data is obtained from GGA+*U* method.

electronic structures, the polaron formation and diffusion mechanism of Na ions. Especially, based on the model of polaron–Na ion/vacancy diffusion complex, we shed a light on how the Jahn–Teller polaron formation and polaron migration affect the diffusion of Na $^+$ ions inside the orthorhombic manganese layered oxides Na_xMnO₂ (0 $\leq x \leq$ 1).

Calculation schemes

All DFT energy calculations were performed using the Vienna Ab initio Simulation Package (VASP) within the projector augmented wave (PAW) pseudopotentials.52 Spin polarized calculations were accomplished with an energy cutoff of 700 eV and the 16 \times 8 \times 4 k-point mesh for unit cell (4 formula units) and $4 \times 4 \times 2$ k-point mesh for $2 \times 1 \times 1$ supercell (8 formula units). Since the Perdew-Burke-Ernzerhof (PBE)⁵³ generalized gradient approximation (GGA) over-estimates the delocalization of 3d orbitals of transition metals, hence fails in describing the small polaron formation, a Hubbard like term $U = 4.0 \text{ eV}^{54} \text{ (GGA+}U\text{) of the Dudarev}^{55} \text{ scheme was added.}$ The hybrid functional method HSE06⁵⁶ was also employed for comparison. Previously, DFT functionals combined with the van der Waals of vdW-D3 correction yield better agreement with the experimental results of the layered structure,57 thus the vdW interaction wdW-D3 correction scheme⁵⁸ was introduced. The structure optimization calculations were converged until the residual atomic force was smaller than 1×10^{-2} eV Å⁻¹. Structural stability, Na+-Mn3+-Mn4+ ordering, voltages, densities of states (DOS) and band structure were calculated by both GGA+U and HSE06 methods.

The diffusion mechanism of Na $^+$ ion in the charging and discharging processes inside the 4 × 2 × 1 (32 formula units) supercell was explored by using the nudged elastic band (NEB) approximation 59 employing both GGA+U and HSE06 methods combined with vdW-D3 correction scheme. The spring force between images is set at -5 eV Å $^{-1}$. The NEB calculation was converged when the residual force was smaller than 0.03 eV Å $^{-1}$.

Table	1	The	lattice	constants,	Mn-O	bond	lengths	and	magnetic
mome	nts	in Na	a_x MnO ₂	unit cell (x	= 0, 1)				

		MnO_2		NaMnO ₂		
		$\mathrm{GGA}{+}U$	HSE06	$\mathrm{GGA}{+}U$	HSE06	
Lattice constant (Å)	а	2.9595	2.8672	2.9414	2.8661	
	b	5.1254	4.9574	5.7184	5.6007	
	с	9.6246	9.5440	10.8204	10.6499	
Volume (ų)		145.99	135.66	182.01	170.96	
Mn-O bond (Å)	$1.96 (\times 6)$	1.91 (\times 6)	$1.99 (\times 4)$	$1.94 (\times 4)$		
		, ,		2.41 (\times 2)	$2.37 (\times 2)$	
Average (Å)	1.96	1.91	2.13	2.08		
Magnetic moment (μ	3.229	3.032	3.856	3.734		

Results and discussion

The crystal structure

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The geometric orthorhombic structure of Na_xMnO₂ ($0 \le x \le 1$) is shown in Fig. 1. In the unit cell, two MnO₂ layers, formed by sharing six edges of each MnO₆ octahedron with six nearest MnO₆ octahedrons, contain four oxygen layers alternating an arrangement of A-B-B-A. In the full-unoccupied Na structure MnO_2 (x = 0), the GGA+U (HSE06) results, as shown in Table 1, indicate that each Mn ion is surrounded by six oxygen ions with a same bond length of 1.96 Å (1.91 Å) to create a regular MnO₆ octahedron. The slab distance between two MnO2 layers is 2.88 Å (2.88 Å).

Since Na⁺ ions are inserted in an empty space between MnO₂ layers, they create a sandwich-liked structure. As illustrates in Fig. 1b, sodium ions can locate at atomic environments of edgeshared prisms (Na_e), where each NaO₆ prism shares six edges of two bottom faces with six MnO₆ octahedrons; or of face-shared prisms (Na_f), in which NaO₆ prism shares two bottom faces with two MnO₆ octahedrons in upper and lower MnO₂ layers. In the full Na-occupied sites, our DFT calculations point out that the Na⁺ ions prefer locating at the Na_e sites with the lower total energy of 220 meV f.u. -1 than that at the Na_f site. The insertion of Na atoms to the MnO2 layered structure also results in the reduction reaction of Mn⁴⁺ (d³) to Mn³⁺ (d⁴). As a result, both GGA+U and HSE06 methods unanimously witness a sizable elongation in the bond length of the Mn-O bonds along the [010] direction from 1.96 Å to 2.41 Å by GGA+U (from 1.91 Å to 2.37 Å by HSE06), while four other bonds increase slightly. On average, the bond length increases by approximately 0.17 Å. In addition, the magnetic moments are 3.856 μ_B and 3.229 μ_B obtained by GGA+U (3.734 $\mu_{\rm B}$ and 3.032 $\mu_{\rm B}$ by HSE06) for Mn³⁺ and Mn⁴⁺ ions, respectively. The significant elongation in bond lengths along the [010] direction leads to the increase of the lattice constant b by approximately 11.5% (13.0%). Similarly, inserted positive Na⁺ ions expand the distance between two MnO_2 layers so that the lattice constant c expands by about 12.4% (11.6%). In the case of all Na⁺ ions fully intercalated, the volume of the unit cell increases 19.8% (20.6%).

An important point is the distance relationship between each Na⁺ ion and its nearest Mn³⁺ ions. The distances from each Na⁺ ion to the first, second, and third nearest Mn³⁺ neighbours (1NN, 2NN and 3NN) are 3.28, 4.35, 4.82 Å (3.22, 4.26, 4.72 Å) obtained

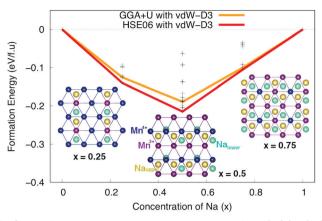


Fig. 2 The formation energy at Na concentrations of x = 0, 0.25, 0.50, 0.75 and 1 of P2 orthorhombic Na_vMnO₂. Insets show the most stable structures at x = 0.25, 0.50 and 0.75, where the violet, blue, yellow and cyan balls stand for Mn³⁺, Mn⁴⁺, Na_{upper} and Na_{lower} ions, respectively.

from GGA+U (HSE06) method, respectively. With the considerable difference in distance, the oxidation/reduction reactions of those Mn groups do not equivalently happen by their nearest Na⁺ ions deintercalation/intercalation.

Phase stability and Na⁺-Mn³⁺-Mn⁴⁺ ordering

Subsequently, Na⁺-Mn³⁺-Mn⁴⁺ ordering structures of Na different concentrations, phase stability and voltage were carefully considered. Nearly 100 configurations of different Na⁺ ion concentrations (x = 0.25, 0.50, and 0.75) were investigated. The formation energy E can be estimated from the following formula:

$$E = E_{\text{Na,MnO}_2} - x E_{\text{NaMnO}_2} - (1 - x) E_{\text{MnO}_2}$$
 (1)

where $E_{\text{Na,MnO}_2}$; E_{NaMnO_2} ; E_{MnO_2} are total energy of the most stable structures Na_xMnO₂, NaMnO₂ and MnO₂, respectively, and x is Na concentration. The $Na^+-Mn^{3+}-Mn^{4+}$ ion ordering and formation energy are given in Fig. 2. From a glance at Fig. 2, the most stable structure is at x = 0.5, in which Mn^{3+}/Mn^{4+} ions prefer to make alternative Mn3+-Mn4+ line along the [100] direction, and Na⁺ ions locate at both Na_e and Na_f sites with a ratio of 2:1 to create a zigzag line along [100] direction. At x = 0.25 and 0.75, the most stable structures are the ones in which all of the Na⁺ ions locate at Nae sites. The Mn ions in the lower layer and their symmetrically equivalent Mn ions in the upper layer along [001] direction tends to be oxidized/reduced concurrently. Obviously, the stable orderings of Na+ ions at different concentrations are related to orderings of Mn⁴⁺-Mn³⁺ ions in MnO₂ layers.

Electronic structure

The density of states (DOS) and the band structures of the most stable structures of Na_xMnO_2 (x = 0, 0.25, 0.50, 0.75 and 1) are illustrated in Fig. 3. At x = 0, both the valence band and conduction bands are mainly contributed by 2p O states and 3d Mn states. The states near the Fermi level come from 2p states dominantly. The estimated up/down-spin gap is 0.82/2.30 eV (2.72/3.10 eV) by GGA+U (HSE06). Since x = 0.25, 0.50, and 0.75,new peaks in the upper valence band of DOS, contributed

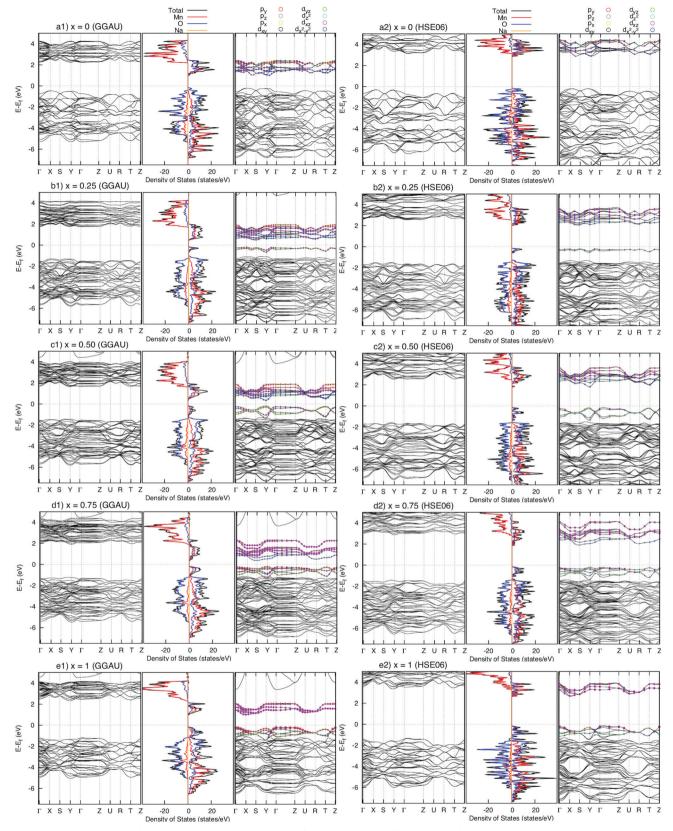


Fig. 3 Density of states (centre) and band structure of up-spin (right) and down-spin (left) of Na_xMnO_2 (x = 0, 0.25, 0.50, 0.75, and 1). The energy origin is set to be the valence band top energy.

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 $\textbf{Table 2} \quad \text{The bond lengths of Mn-O at the Mn$^{3NN}O_6$ octahedron before and after single-Na deintercalation from the NaMnO_2~4 \times 2 \times 1 \text{ supercell lengths}$ obtained by GGA+U (HSE06) method

Mn ^{3NN} -O	O1	O2	О3	O4	O5	O6	Average
Before	1.99 (1.94)	1.99 (1.94)	1.99 (1.94)	1.99 (1.94)	2.41 (2.37)	2.41 (2.37)	2.13 (2.08)
After	1.97 (1.91)	1.97 (1.91)	1.97 (1.92)	1.97 (1.92)	2.03 (1.96)	2.10 (2.03)	2.00 (1.94)

mainly by a combination of $2p_v$ O states with $3d_{vz}$ and $3d_{x^2-v^2}$ Mn states, appear next to the Fermi levels. From the GGA+U(HSE06) method, the up/down-spin gaps are shortened significantly to 0.25/2.66, 0.14/2.68, and 0.17/2.74 eV (1.87/3.69, 1.64/3.76, and 1.71/3.91 eV), for x = 0.25, 0.50, and 0.75, respectively. Obviously, during the intercalation/deintercalation processes, the band gap almost remains so that it likely keeps the electronic conductivity persist. At the concentration of Na⁺ ion of x = 1, the $3d_{xz}$ Mn states predominate the conduction band of NaMnO₂ while the hybrid states of 2p_v O states, 3d_{vz} and $3d_{x^2-v^2}$ Mn states hold the lion's share at states near Fermi level. The up/down-spin band gap estimated by GGA+*U* (HSE06) is enlarged to 0.81/3.11eV (2.48/4.31 eV), which is equivalent to those of full Na-unoccupied structure (x = 0). Understandably, the hybrid states of $2p_{\nu}$ O states, $3d_{\nu z}$ and $3d_{x^2-\nu^2}$ Mn states play the crucial contribution to the electronic structure of the material.

Voltage

The calculated total energies of the most stable structures are used for voltage estimation. The voltage would be obtained by the formula below:

$$V = -\frac{E_{\text{Na}_{x_1}\text{MnO}_2} - E_{\text{Na}_{x_2}\text{MnO}_2} - (x_1 - x_2)E_{\text{Na}}}{(x_1 - x_2)e}$$
(2)

where $E_{\text{Na}_{x_1}\text{MnO}_2}$; $E_{\text{Na}_{x_2}\text{MnO}_2}$; E_{Na} are total energy of $\text{Na}_{x_4}\text{MnO}_2$, $Na_{x_2}MnO_2$, Na metal, respectively. x_1 and x_2 are Na concentration corresponded to Na_x, MnO₂, Na_x, MnO₂. e is the absolute electron charge. The GGA+U (HSE06) estimated voltages at specific capacities of 72, 135, and 191 mA h g^{-1} are 2.82, 2.60, and 1.97V (3.00, 2.73, and 1.99 V), respectively. Those results are well-agreed with experimental results (2.81, 2.26, and 1.86V).45

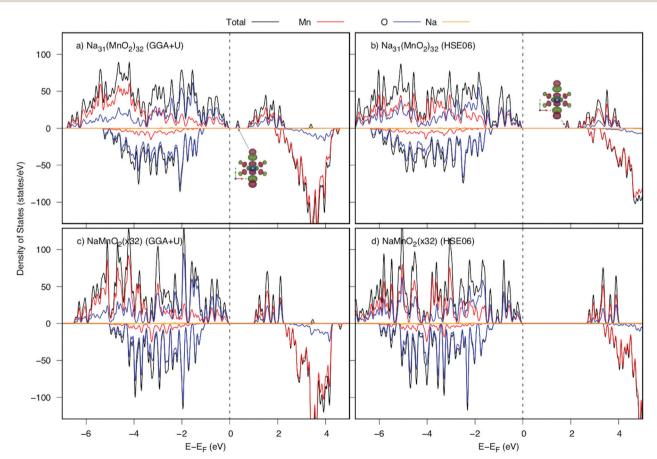


Fig. 4 Density of states of Na_xMnO₂ before and after one Na deintercalation from the NaMnO₂ (32 f.u.) supercell calculated by GGA+U and HSE06. The valence band top is set to be the energy origin (vertical dashed lines). Insets show spatial electron distribution of the lowest unoccupied state at Mn^{3NN} sites indicated with arrows

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Diffusion at high Na concentration

Now, we investigate the Na⁺ diffusion mechanism in the full charging/discharging states. As discussed in the previous article,5 two factors, the so-called quasi-particle named small polaron and geometric arrangement of the framework structure, affect considerably to the diffusion mechanism. Several types of elementary diffusion processes were proposed, including single, parallel and crossing processes. In this work, we carefully analyzed the geometrical structure and polaron migration in the defect structures.

As a Na atom is deintercalated from the full-occupied Na structure, a positive hole is introduced to the structure. Surrounding the Na vacancy, there are six 1NN, four 2NN and two 3NN Mn³⁺ ions. Due to the hole introduced, one of those Mn³⁺ ions would be oxidized to be Mn⁴⁺. As a result, significant shrinkage of Mn-O bonds at Mn site would be observed. Our DFT calculations indicate that the structure possessing a 3NN Mn³⁺ ion oxidized is the most stable one by its lowest energy (approximately 140 meV lower than those of 1NN and 2NN Mn sites). As shown in Table 2, at the Mn^{3NN}O₆ octahedron, two Mn-O5 and Mn-O6 bond lengths along [010] direction significantly decrease from 2.41 Å (2.37 Å) to 2.07 Å and 2.10 Å (1.96 Å and 2.03 Å) after Na deintercalation. Overal, the average bond length is shrunk by approximately 0.13 Å (0.12 Å). Thereby, the magnetic moment at 3NN site reduces from 3.852 to 3.299 $\mu_{\rm B}$ by GGA+U (3.734 to 3.056 $\mu_{\rm B}$ by HSE06). The considerable shortened Mn-O bond length along the [010] direction results in a significant change in electronic structure. The DOSs of the structures before and after a Na deintercalation are shown

in Fig. 4. Compared DOSs of those structures, it is understandable that the newborn bound state appearing right after the Fermi level is contributed mainly by a combination of O's $2p_v$ states with Mn's $3d_{vz}$ and $3d_{x^2-v^2}$ states. The Mn⁴⁺ ion at 3NN sites surrounded by Mn³⁺ ions creates a defect structure in which a local polarized distortion prefers to appear around 3NN sites. It is concluded that a positive polaron is formed at one of the 3NN Mn sites.

The positive polaron binds to the Na vacancy to form a Na vacancy-positive polaron complex. In the layer structure with the arrangement of MnO₆ octahedron as shown in Fig. 1, the single process, which often requires the lowest activation energy, can not occur. Two types of elementary diffusion processes along the [010] direction were explored as shown in Fig. 5.

- (i) The crossing process occurs if the positive polaron hops between the adjacent MnO₂ layers. As illustrated in Fig. 5a, polaron leaps from the MnO₂ lower layer to the upper one; explicitly from Mn_A to its Mn neighbour Mn_B while Na vacancy moves from an edged-share site VeA to another edged-shared site V_{eB}. The reaction coordinate of this process is 3.264 Å by GGA+U (3.55 Å by HSE06).
- (ii) On the other hand, the parallel process occurs if the positive polaron jumps inside the MnO2 layer; explicitly from Mn_C to Mn_B while the Na vacancy diffuses from an edged-share site V_{eA} to another edged-shared site V_{eB} as shown in Fig. 5b. The reaction coordinate is 3.30 Å by GGA+U (3.41 Å by HSE06).

The activation energy profiles obtained from GGA+U and HSE06 methods are shown in Fig. 5c and d. Both the GGA+U and HSE06 methods give the result indicating that the parallel

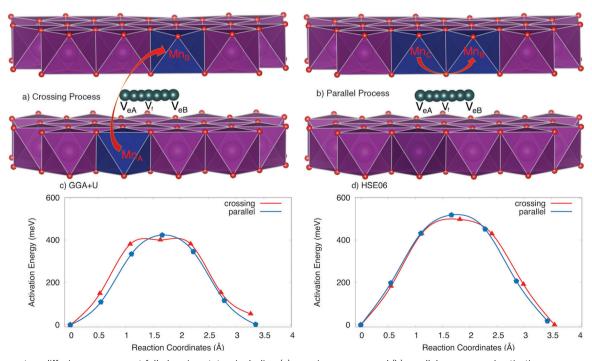


Fig. 5 Elementary diffusion processes at full charging states, including (a) crossing process and (b) parallel process and activation energy profile of Na vacancy-positive polaron complex obtained by obtained by (c) GGA+U and (d) HSE06 methods. The dark blue octahedrons represent the 3NN Mn sites where polaron could be formed, and the dark cyan balls stand for Na vacancy trace diffusion. The other Na atoms are hidden for more clarification.

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 $\textbf{Table 3} \quad \text{The bond lengths of Mn-O at the } Mn^{2NN}O_6 \text{ octahedron before and after a single Na intercalation into } MnO_2 \text{ supercell obtained by } GGA+U \text{ octahedron before } \text{ octahedron before } \text{ octahedron before } \text{ octahedron } \text{$ (HSE06) method

Mn ^{3NN} -O	O1	O2	O3	O4	O5	O6	Average
Before	1.96 (1.91)	1.96 (1.91)	1.96 (1.91)	1.96 (1.91)	1.96 (1.91)	1.96 (2.91)	1.96 (1.91)
After	1.98 (1.93)	1.98 (1.93)	1.99 (1.94)	1.99 (1.94)	2.07 (2.12)	2.10 (2.13)	2.02 (2.00)

process requires a little higher activation energy than crossing one; they are 423 meV and 400 meV by GGA+U (518 meV and 497 meV by HSE06) for the parallel and the crossing processes, respectively. The path from edged-shared vacancy site to its neighbour edged-share vacancy site (Ve-Ve) would be a sum of two sub-paths: the edge-shared vacant site to the face-shared vacant site (Ve-Vf) and then the face-shared vacant site to the edge-shared vacant site (V_f-V_e) . With a scrap of difference, both parallel and crossing processes equivalently occur. Consequently, the overall activation energy is 423 meV (518 meV) obtained by GGA+U (and by HSE06). The influence of the positive polaron migration on the different diffusion paths of Na ion is equivalent.

Diffusion at low Na concentration

Next, we depict the fully discharged state. After the intercalation of the Na atom to MnO2 layered structure, an electron is also introduced to the structure to make a reduction reaction of Mn⁴⁺ to Mn³⁺. Because of creating from almost perfect MnO₆ octahedrons, the Na⁺ ion is surrounded by six 1NN and six 2NN Mn ions. Among those, the Mn ion at the 2NN site prefers to be reduced first. As shown in Table 3, both GGA+U and HSE06 methods agree that there is a significant elongation in the average Mn-O bond length from 1.96 Å (1.91 Å) to 2.02 Å (2.00 Å) by GGA+U (HSE06), along with an increase magnetic moment from $3.299 \mu_B (3.056 \mu_B)$ to $3.856 \mu_B (3.734 \mu_B)$ by GGA+U (HSE06). That implies the Mn4+ ion at 2NN sites would be reduced first to be Mn³⁺ ion. The change in the bond length results in a new peak appeared right next to the Fermi level in DOS as shown in Fig. 6. This bound state comes from a hybrid orbital predominantly of O's $2p_y$ states and Mn's $3d_{yz}$ and $3d_{x^2-y^2}$ states. As different as in the fully charged state, a negative small polaron is formed at the 2NN Mn site.

Since the negative polaron arises in the Na inserted structure, two elementary diffusion processes, including parallel and

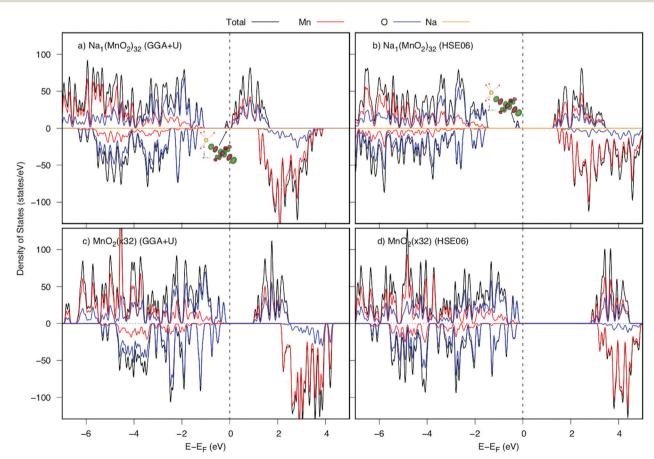


Fig. 6 Density of states of Na_xMnO₂ before and after a Na intercalation into the MnO₂ (32 f.u.) supercell calculated by GGA+U and HSE06. The valence band top is set to be the energy origin (vertical dashed lines). Insets show spatial electron distributions of the highest occuppied states at the Mn^{2NN} sites indicated with arrows

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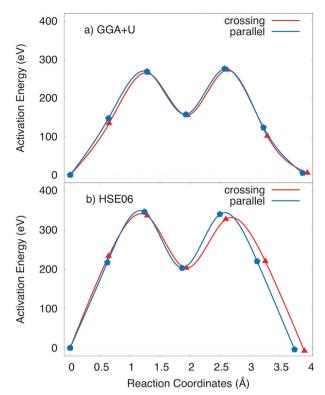


Fig. 7 Activation energy profile of Na⁺ ion-negative polaron complex obtained by (a) GGA+U and (b) HSE06 method.

crossing processes, of Na⁺ ion-negative polaron complexes were explored by employing the GGA+U and HSE06 methods in NEB calculations. As illustrated in Fig. 7, both GGA+U and HSE06 methods agree that the activation energies are almost same for the parallel and crossing processes, which also points toward that the effect of small polaron hopping might be analogous. Obviously, both parallel and crossing processes equivalently occurred. Similar to the Na vacancy diffusion at high Na concentration, the Na_e-Na_e path is also a combination of the two small paths Nae-Naf and Naf-Nae. Evidently, the Naf site is the metastable position of Na⁺ ion. Two summits in the activation energy profile correspond to Na⁺ positions at the intermediate place between Na_e site and Na_f site. The barriers estimated by GGA+U and HSE06 methods are 273 and 327 meV, respectively.

Overall, the energy required for Na diffusion is in the range from 273 meV (327 meV) to 423 meV (518 meV) during the charging/discharging process by GGA+U (HSE06). Both parallel and crossing processes require an approximately same activation energy. Unlike polyanion cathode materials,⁵⁻¹⁰ the effect of polaron migration to overall activation energy is insignificant so that it benefits the diffusion of Na vacancy/ion inside the cathode material. Polaron can jump in the plane of MnO₂ layer, or jump interplane from the upper layer to lower layer or contrariwise required an equivalent energy. Consequently, both processes might occur during the diffusion of Na⁺ ion inside the material. Compared with other common materials such as olivine phosphate (LiFePO₄) with an activation energy of 630 meV,5 it is obvious that the activation energy of the

orthorhombic P2 layered NaxMnO2 is considerably smaller, which benefits the Na⁺ diffusion.

Conclusions

For the sake of brevity, the crystal and electronic structures, stability diagram, voltage as well as diffusion of Na vacancy/ ion-polaron complex in an auspicious cathode material Na_xMnO₂ $(0 \le x \le 1)$ were dissected using GGA+U and HSE06 methods. The most stable structures having different concentrations of Na were explored. At high or low Na concentrations, Na⁺ ions prefer locating only at the edge-shared prism. The material is more stable at x = 0.5. During the charging/discharging process, a conspicuous change in lattice constant b and volume would be observed due to the significant shrinkage/elongation of bonds along the [010] direction. As a result, the hybrid orbital, combined by O's $2p_{\nu}$ states, Mn's $3d_{\nu z}$ and $3d_{x^2-\nu^2}$ states, plays a crucial pivot in the electronic structure of the material during the intercalation/ deintercalation. Also, the electric conductivity is better at the intermediate structures. The voltages against capacity obtained from the most stable structures using GGA+U and HSE06 methods are well-agreed with the experimental result. When a Na⁺ ion is deintercalated from the full-occupied Na structure, the positive small polaron is formed at one of the third nearest neighbours Mn to the Na vacancy. The polaron simultaneously escorts and would hinder the Na vacancy diffusion. Two elementary diffusion processes, including parallel and crossing process would occur equivalently and require an activation energy of 423 meV (518 meV) by GGA+U (HSE06). In the fully discharged state, the insertion of Na⁺ ion leads to the formation of a negative small polaron. Without Na⁺-Na⁺ repulsion, the significantly lower activation energy of 273 meV (327 meV) by GGA+U (HSE06) is required. At low Na concentration regime, Na⁺ ions can diffuse easier than at high Na concentration ones. Unlike polyanion based materials, the effect of polaron hopping is equivalent on the different diffusion paths in Na_xMnO₂. Compared to olivine phosphate, the Na⁺ ion would diffuse in Na_xMnO₂ better than in polyanion framework like LiFePO₄.

Conflicts of interest

There are no conflicts to declare.

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