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p-Synephrine enantiomers: binary phase diagram, crystal structure and kinetic stability of a metastable conglomerate monitored by nonlinear optics†

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The crystal structure of (*S*)-(+)-*p*-synephrine was refined at 296 K from X-ray powder diffraction. The compound crystallizes in the orthorhombic system $P2_12_12_1$ with four molecules per unit cell and $Z' = 1$. The cell parameters are equal to $a = 6.5925(12)$ Å, $b = 7.9915(14)$ Å, and $c = 17.035(4)$ Å. The melting characteristics of the enantiomers were determined at high DSC scan rates. The pure enantiomers melt at $T_{fus} = 176.6 \pm 0.9$ °C with a melting enthalpy equal to 234.2 ± 3.9 J g⁻¹. Coupling DSC and crystallographic analysis, a stable binary phase diagram between these chiral molecules was established taking into account the racemic compound. Two symmetrical eutectic invariants at: 172.7 ± 0.5 °C for $x = 0.05$ and $x = 0.95$ were found pretty close to the melting temperature of the enantiomers. Additionally, the equimolar mechanical mixture of the two enantiomers led to a metastable conglomerate whose melting temperature was estimated to be 149 °C, thanks to the Schröder–van Laar relation. The activation energy of the transition from the metastable conglomerate toward the racemic compound was estimated to be $E_a = 145$ kJ mol⁻¹ by a nonlinear optical method. This new isothermal second harmonic generation application performed at different temperatures is of general applicability for the assessment of the activation energy associated with the irreversible heterogeneous reaction: $\langle R \rangle + \langle S \rangle \rightarrow \langle RS \rangle$.

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Introduction

p-Synephrine (C₉H₁₃NO₂) is an alkaloid naturally contained in some plants.¹ *p*-Synephrine is the *para* isomer of synephrine (Scheme 1). It is a chiral molecule whose equimolar mixture of the two enantiomers (*R*)-(–) and (*S*)-(+)) crystallizes as a racemic compound.

The crystal structure of the crystalline racemic compound was previously solved in a monoclinic system (space group $P2_1/c$, $Z = 4$ ($Z' = 1$), with $a = 8.8504(11)$ Å, $b = 12.1166(15)$ Å, $c = 9.7820(11)$ Å, and $\beta = 122.551(2)^\circ$.² The melting point of

the racemic compound was found to be equal to 199.8 ± 1.3 °C with a melting enthalpy of 57 ± 3 kJ mol⁻¹.²

Regarding the enantiomers, the melting point has been estimated at 169 °C (ref. 3) but no indication was given on the measurement technique of the melting point and no enthalpy value was determined. As for the racemic compound, the enantiomers degrade upon melting. To bypass the degradation process occurring upon melting, differential scanning calorimetry (DSC) can be conducted at high DSC scan rates, as has been previously demonstrated.^{2,4} Then, values of temperature and enthalpy of melting can be proposed with accuracy. As far as the crystal structure of the enantiomer is concerned, nothing was reported in the literature. So to complete the study on this chiral molecule,

Scheme 1 Molecular structure of *p*-synephrine: (*R*)-(–)-4-[1-hydroxy-2-(methylamino)ethyl]phenol (left) and (*S*)-(+)-4-[1-hydroxy-2-(methylamino)ethyl]phenol (right).

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the crystal structure of the enantiomer was determined from X-ray powder diffraction data obtained at room temperature.

The relative stability between the racemic compound and the enantiomers was established by constructing a stable binary phase diagram between one of the two enantiomers and the racemic compound. This study also reports the study of the transition of a metastable conglomerate to the racemic compound by second harmonic generation temperature resolved microscopy (SHG-TR-M). From the results, the activation energy of the transition is then estimated.

Experimental

Chemicals

The samples of pure enantiomers were kindly provided to us by the pharmacognosy laboratory of the Faculty of Pharmacy of Paris 5, with an enantiomeric purity, established by chromatography, of 98% for the (*R*)-enantiomer and 99% for the (*S*)-enantiomer. The racemic compound was purchased from Sigma Aldrich, with purity higher than 98%. All the compounds were used without further purification.

X-ray diffraction

X-ray powder diffraction experiments were performed with a horizontally mounted cylindrical position-sensitive detector CPS-120 (Debye–Scherrer geometry, transmission mode) from INEL, using monochromatic Cu $K\alpha_1$ radiation ($\lambda = 1.54056$ Å), selected with an asymmetric focusing incident-beam curved quartz monochromator. The generator power was set to 1.0 kW (40 kV and 25 mA). The detector consisted of 4096 channels providing an angular step of 0.029° (2) between 4° and 120° . External calibration using the $\text{Na}_2\text{Ca}_2\text{Al}_2\text{F}_{14}$ (NAC) cubic phase mixed with silver behenate was performed by means of cubic spline fittings. From that, each channel was converted into a diffraction angle.

The samples were gently crushed before being introduced into Lindemann glass capillaries with a 0.5 mm inner diameter, which were then rotated perpendicular to the X-ray beam direction in order to decrease as much as possible the effects of preferred orientations.

The crystal structure was determined with the reflex plus module of Materials Studio Modeling 5.5.⁵ First, the pattern was indexed by means of the peak picking option of the software package. Potential solutions for cell parameters and space group were found using the X-cell algorithm.⁶ Then, a Pawley profile-fitting procedure was applied including refined cell parameter experimental profile fitting with a pseudo-Voigt function, zero shift and asymmetry Finger–Cox–Jephcoat function.⁷ Distances, angles and torsions in the molecule were obtained *via* energy-minimization calculations with the Forcite module using the Dreiding force field.⁸ Then, a Monte-Carlo approach, included in the reflex plus module, was carried out in the direct space to solve the structure moving the molecule as a rigid-body and allowing the change of the chain torsion angles.⁹

Thermal analysis

Differential scanning calorimetry experiments were performed using an 822e thermal analyser, equipped with an FRS5 sensor, from Mettler-Toledo (Switzerland). The DSC experiments were carried out in the 25–200 °C temperature range at different scan rates from 5 to 100 °C min^{−1} under a constant nitrogen flow. Temperature and enthalpy calibration of the apparatus were carried out at 10 °C min^{−1} using indium and zinc as standards. The multiple thermocouple sensor technology of the device combined with furnace and sample tau lag calibration eliminates the influence of the heating rate on temperature and heat flux measurements.¹⁰ The tau lag was calibrated for scan rates ranging from 5 to 100 °C min^{−1}, using the procedure described by the manufacturer. Regarding the enthalpy values, the relative standard uncertainty in the values (average of six independent values) was estimated at 5%. For all the experiments, an empty aluminum pan was used as the reference. The melting temperatures were determined at the onset of the corresponding endotherms. *p*-Synephrine samples (approximately 2.5 mg) were weighed with a microbalance sensitive to 1 µg and then introduced into a crucible with a perforated cover. The crystal size distributions of the samples were not taken into account. The standard uncertainty in the temperatures was determined from the standard deviation, with 0.68 level of confidence, of six independent measurements for each enantiomer performed for each scan rate. Mean values of melting temperatures and enthalpies were obtained by averaging the values of three independent measurements of each enantiomer.

Second harmonic generation microscopy (SHG-M)

An Insight X3 single laser with automated dispersion compensation (Spectra-Physics, Santa Clara, USA) and a TCS SP8 MP confocal microscope (Leica Microsystems, Wetzlar, Germany) were used to perform confocal microscopy of the samples. The laser cavity had an average power of over 2.50 W at 900 nm and was tunable from 680 nm to 1300 nm. The repetition rate was 80 MHz and the temporal width at the output of the cavity was around 120 fs (<100 fs between 850 nm and 1050 nm). The laser was controlled with the LASX Leica software. Two Leica hybrid descanned detectors (HyD) were used to record images. Microscope objectives were long working distance dry Leica objectives (HC PL Fluotar 5× NA 0.15, HC PL Fluotar 10× NA 0.3 or HC PL APO 20× NA 0.4 CS2). An electro-optical modulator was used to adjust the laser power at the entrance of the confocal system.

The spectral acquisition was performed using an internal hybrid detector. Collected photons were dispersed by a prism and a specific motorized split mirror selected the spectral detected band before the hybrid detector. Acquisitions were performed between 380 nm and 780 nm every 3 nm and a spectral bandwidth of 5 nm. Typically, the sample is excited at a given wavelength (*e.g.* 1200 nm or 900 nm) while scanned through the emission wavelength (*e.g.* in the 380–

780 nm range). The SHG and THG should appear at the half and at the third of the excitation wavelength, respectively.

Temperature resolved SHG-M

The samples (few mg of powder in an amorphous silica crucible) were placed in a computer-controlled heating/cooling stage (Linkam THMS-600) and were irradiated with the femtosecond laser beam. The samples were cooled and heated between 20 °C and 160 °C at different heating rates. For isothermal monitoring, the sample was heated at the isothermal temperature at a heating rate of 100 °C min⁻¹.

Sample preparation of binary mixtures

The binary mixtures were prepared by mixing in different ratios the racemic compound and one of the enantiomers directly in the DSC pan and the homogenization was carried out by mechanical stirring for 15 minutes. The samples were then introduced at room temperature in DSC aluminum pans, which were hermetically sealed.

Results and discussion

The crystal structure of the *p*-synephrine enantiomer was achieved from the (*S*)-(+)-enantiomer at 296 K. It crystallizes in the orthorhombic space group *P*2₁2₁2₁ with *a* = 6.5925(12) Å, *b* = 7.9915(14) Å, and *c* = 17.035(4) Å with four molecules per unit cell (*Z* = 4, *Z'* = 1). The agreement between the observed and computed diffraction patterns is estimated by an Rwp. The final Rietveld refinement (including Pawley refined parameters, rigid-body molecular units, torsions, preferred orientations and overall isotropic factor) converged to a final reliability factor Rwp value of 3.37 (Fig. 1). Rietveld refinement allowed us to propose the crystal structure presented in Fig. 2.

The asymmetric unit with atom numbering is given in Fig. 3. The refinement was achieved by placing the hydrogen atoms in theoretical positions to get the best H-bonds. Then, as shown in Fig. 3, disorder has been introduced for the

Fig. 1 Final Rietveld refinement of the X-ray diffraction pattern of (*S*)-(+)-*p*-synephrine obtained at 296 K. Empty red circles: experimental pattern, blue line: calculated pattern, green vertical bars: peak positions, and black line: residual XRPD patterns. The inset corresponds to the scale for the data between 40 and 70 magnified 15 times.

Fig. 2 Crystal structure of (*S*)-(+)-*p*-synephrine viewed along *a* (top) and along *b* (bottom).

hydrogen atoms: two positions for the hydrogen atoms of the secondary amine (N9), two positions for the ones of the hydroxyl group (O12) and three positions for the ones of the hydroxyl group (O11). This leads to an occupancy factor of 0.33 for each hydrogen of the hydroxyl group (O11). The occupancy factors are equal to 0.67 for H9A and H12A and 0.33 for H9B and H12B.

The molecular structure is maintained through seven possible inter-molecular H-bonds (Table 1). The refinement also revealed two intra-molecular H-bonds *via* N9 and O12. This double interaction is caused by possible disorder of the hydrogen on the secondary amine and the hydroxyl group, as encountered for the racemic compound.²

Fig. 3 Asymmetric unit of (*S*)-(+)-*p*-synephrine with atom labels.

Table 1 Intra and inter-molecular H-bond distances and angles in the crystal structure of (*S*)-(+)-*p*-synephrine

D	H	A	D–H (Å)	H···A (Å)	D···A (Å)	D–H···A (deg.)	Symmetry
N9	H9A	O11	0.981(17)	1.766(18)	2.736(10)	169.4(16)	a
N9	H9B	O11	0.981(19)	1.950(18)	2.849(12)	151.2(14)	b
O11	H11A	N9	0.964(10)	1.908(12)	2.849(12)	164.8(8)	c
O11	H11B	N9	0.963(10)	1.801(11)	2.736(10)	163.1(9)	d
O11	H11C	O12	0.963(10)	1.670(9)	2.627(9)	172.3(9)	e
O12	H12A	O11	0.948(8)	1.742(8)	2.627(9)	154.0(8)	f
O12	H12B	O11	0.949(10)	2.385(9)	3.243(9)	150.4(5)	b
N9	H9B	O12	0.981(19)	2.300(15)	2.785(12)	109.4(13)	g
O12	H12B	N9	0.949(10)	2.091(12)	2.785(12)	128.7(7)	g

(a) $1 - x, 1/2 + y, 1/2 - z$; (b) $1/2 - x, 1 - y, -1/2 + z$; (c) $1/2 - x, 1 - y, 1/2 + z$; (d) $1 - x, -1/2 + y, 1/2 - z$; (e) $-x, -1/2 + y, 1/2 - z$; (f) $-x, 1/2 + y, 1/2 - z$; (g) x, y, z .

The main conformation differences between the asymmetric units of the enantiomer and the racemic form of *p*-synephrine are mainly noticeable for the hydroxy-methylamino-ethyl group (Fig. 4). The chain is therefore slightly more twisted in the enantiomer than that in the racemic compound (Table 2).

DSC analyses were carried out at different heating rates on both enantiomers. Two independent samples of each enantiomer were analyzed for each heating rate. Then an average value was calculated for the melting temperature and enthalpy. On heating at low scan rates, both enantiomers of *p*-synephrine degrade upon and after melting, as can be seen in Fig. 5 for (*R*)-*p*-synephrine at 5°C min^{-1} . The apparent melting peak is then shifted to low temperatures due to mixing of the degraded product with the pure substance. The DSC signal shows an abrupt return to baseline followed by an exothermic peak characteristic of degradation. On increasing the DSC scan rate up to $100^\circ\text{C min}^{-1}$, the apparent melting temperature shifts to high temperatures and the degradation process moves to higher temperatures (Fig. 5). As previously reported, the decomposition reaction occurring upon melting is significantly shifted towards higher temperatures by increasing the heating rate.^{4,11,12}

The onset of the apparent melting temperature was reported as a function of the heating rate (Fig. 6A). The melting temperature increases with the scan rate to reach a

plateau value at $176.6 \pm 0.9^\circ\text{C}$ for high scan rates, much higher than the 169°C reported in ref. 3.

As far as the apparent melting enthalpy is concerned, the same behavior was observed when the DSC scan rate increased. Then, the values plotted as a function of the scan rate led to a constant value at high scan rates equal to $234.2 \pm 3.9 \text{ J g}^{-1}$ ($39.2 \pm 0.7 \text{ kJ mol}^{-1}$) as shown in Fig. 6B. By comparison, the racemic compound melts at a higher temperature with a higher enthalpy ($199.8 \pm 1.3^\circ\text{C}$ and $57 \pm 3 \text{ kJ mol}^{-1}$, respectively).²

Binary phase diagram between the racemic compound and enantiomers

Different ratios between *RS*- and *S*- or *R*-enantiomers of *p*-synephrine were analyzed by DSC at different scan rates varying between 60 and $100^\circ\text{C min}^{-1}$. In Fig. 7, the experimental values determined from DSC experiments are presented. The representation takes into account that the points are doubled by symmetry with respect to $x = 0.5$, as explained in the caption of Fig. 6. The liquidus curves, obtained for the racemic compound using the Prigogine-Defay equation¹³ and for the enantiomers based on the Schröder-van Laar equation,^{14,15} are also presented in Fig. 7. The melting point characteristics of the racemic compound are from ref. 2 and from this work for the enantiomers. From these curves, the eutectic points were determined at $x = 0.05$ and 0.95 in the (*S*)-enantiomer. Those values fit reasonably well with our experimental data. The stable liquidus of the pure enantiomers are therefore pretty difficult to observe also because of the necessary fast heating rate. We acknowledge that the initial purity of the samples together with a certain

Fig. 4 Conformation of (*S*)-(+)-*p*-synephrine asymmetric unit: enantiomer (top) and racemic compound (bottom).

Table 2 Torsion angles for the (*S*)-(+)-configuration molecule in the enantiomer (this work) and in the racemic compound (ref. 2) of *p*-synephrine

Torsion angles	Enantiomer	Racemate	Difference
C3–C4–C7–O12	–135.4	–149.4	14
C3–C4–C7–C8	–69.6	–87.6	18
C4–C7–C8–N9	–175.5	169.3	15.2
C7–C8–N9–C10	–162.4	180.0	17.6

Fig. 5 Selected normalized DSC curves of (R)-(-)-*p*-syneprine at 5 (black), 20 (blue), 40 (red), 80 (magenta) and 100 °C min⁻¹ (green).

chemical degradation on heating led us to propose a rather 'rough' binary phase diagram.

The mean value of the eutectic temperature, obtained from the DSC curves, was determined at 172.7 ± 0.5 °C (445.7 ± 0.5 K). Moreover, no miscibility in the solid state between enantiomers nor any polymorphism was observed by powder X-ray diffraction (results not shown).

Metastable equilibria

To consider the possibility of a metastable conglomerate, an attempt was made to draw the potential metastable phase

Fig. 6 Temperature (A) and enthalpy (B) of melting of *p*-syneprine enantiomers as functions of the heating rate.

Fig. 7 Temperature-composition solid-liquid stable phase diagram of the *R*-/*S*-*p*-syneprine binary system. *x* stands for the (S)-(+)-enantiomer composition. The experimental data obtained from the thermograms are represented by solid squares and the ones obtained by symmetry are represented by empty squares. Prigogine-Defay and Schröder-van Laar ideal behaviors of the liquidus curves are represented in green and red lines, respectively. The blue line corresponds to the mean value of the eutectic invariant obtained from DSC experiments.

diagram between the two enantiomers. Theoretically, the eutectic temperature should be obtained at *circa* 149 °C as assessed using the Schröder-van Laar relation^{14,15} and shown in Fig. 8.

For that, the two enantiomers were directly mixed in equimolar proportions by mechanical stirring at room temperature. The diffraction pattern of a conglomerate was observed and remained unchanged even after several days of storage. Nevertheless, on heating the mixture, the X-ray diffraction experiments revealed that the equimolar physical mixture transformed into the racemic compound. As we can see in Fig. 9, the X-ray diffraction pattern of the equimolar mixture heated at 130 °C with a heating rate of 60 °C min⁻¹ and quenched at room temperature is the superposition of the X-ray diffraction patterns of the pure enantiomer and the racemic compound.

DSC experiments were conducted on a 50/50 physical mixture of *R*- and (*S*)-*p*-syneprine with a scan rate of 60 °C min⁻¹. Instead of obtaining a single peak, which corresponds to the melting of the eutectic composition, we obtained two peaks (Fig. 10), with an onset temperature corresponding to the eutectic temperature of the stable phase diagram (Fig. 7).

Fig. 8 Temperature-composition solid-liquid metastable phase diagram of the (*R*)-(-)-*p*-syneprine binary system. The ideal liquidus curves (red lines) are obtained using the Schröder-van Laar equation.

Fig. 9 Room temperature X-ray powder diffraction patterns of *p*-syneprine: black line: (S)-(+)-*p*-syneprine pattern, red line: (R)-(-)-*p*-syneprine pattern, and blue line: equimolecular physical mixture of (R)-(-)-*p*-syneprine and (S)-(+)-*p*-syneprine heated at 130 °C.

This corroborates the fact that crystallization of the racemic compounds takes place when temperature is increased.

However, as indicated by the arrow in Fig. 10, a small endothermic event arises at around 145 °C. This signal could be the trace of the portion of the sample that remained as a conglomerate and therefore undergoes the eutectic reaction calculated at 149 °C. This suggests that the entire sample is not in the racemic compound form when the temperature of 172 °C is reached at 60 °C min⁻¹. This is in line with the observation of the second peak in Fig. 10, which then corresponds to the crossing of the liquidus curve. Indeed, the composition which undergoes the eutectic reaction at 172 °C is no longer the equimolar composition.

Because of the weakness of the thermal event associated with the transition from the metastable conglomerate to the stable racemic compound, it is difficult or even impossible to monitor the kinetics of this phase transition by DSC.

Therefore, in order to determine the activation energy of this transformation, temperature resolved second harmonic generation microscopy (TR-SHG-M) was used. Among the various nonlinear effects, second harmonic generation (SHG) is certainly

Fig. 10 DSC curves of the 50/50 mixture of (R)-(-) and (S)-(+) *p*-syneprine obtained at 60 °C min⁻¹. The inset corresponds to a zoom of the DSC trace of the metastable eutectic invariant.

the most popular and can simply be viewed as the interaction of two electromagnetic waves (of the same frequency) in a material that gives rise to a third wave at twice the initial frequency. Nevertheless, SHG is only possible in non-centrosymmetric crystals. Therefore, this technique is of relevance to detect non-centrosymmetry and particularly dedicated to the monitoring of phase transitions involving at least one non-centrosymmetric phase. This technique is also thus useful when conglomerate and racemic compounds have to be differentiated.¹⁶

In order to quantify the SHG intensity emitted by (S)-(+)-*p*-syneprine and to check if the sample produces fluorescence (that can lead to misleading results), spectral emission scans at laser excitation wavelengths of 800 nm, 900 nm, 1000 nm, 1100 nm, 1200 nm and 1300 nm were performed and shown in Fig. S1†. The power of the laser was set to 0.12 W. Fig. S1† shows that (S)-*p*-syneprine produces a relatively strong SHG signal and (for excitation wavelengths of 800, 900 and 1000 nm) a very weak fluorescence. One can also notice that the SHG produced at an excitation wavelength of 900 nm is much higher than at other excitation wavelengths (e.g. 100 times higher compared to the second harmonic emitted at an excitation wavelength of 1300 nm). The small variation of the sensitivity of the detector with the wavelength does not change this ratio. This behavior is probably due to a greater phase mismatch for refractive indexes at 1300 nm and its second harmonic wavelength (650 nm).

To monitor the phase transition, the 900 nm excitation wavelength was selected. This choice is motivated by the weak fluorescence and the strong second harmonic signal at 450 nm that ensures good detection sensitivity.

Fig. 11 shows the comparison between bright field and SHG images of an (S)-(+)-*p*-syneprine sample at the excitation wavelength of 900 nm. One can notice that each particle in the sample emits a second harmonic signal proving that each crystal is non-centrosymmetric.

Kinetic parameters

A common approach to determine the activation energy (E_a) is to track the conversion of the metastable phase by means of isothermal experiments at various temperatures. Isothermal transformation of *p*-syneprine racemic mixtures (i.e. mixture composition containing 50% of (R)-(-)-*p*-syneprine and 50% of (S)-(+)-*p*-syneprine) was studied by monitoring the time dependence of the SHG signal at different temperatures: 120 °C, 130 °C, 140 °C and 150 °C. The laser wavelength was 900 nm and the SHG signal was recorded at 450 nm ± 10 nm. The movies associated with each isotherm are available in ESI-1†. The movies show that the SHG signal progressively vanishes *versus* time during the solid–solid transformation (nevertheless, for a very long acquisition time, a liquid phase can appear, probably as a result of a slight chemical degradation). In Fig. 12, the SHG together with the BF and the overlays of both microscopy images are compared for acquisition times of 0 s (Fig. 12a) and 6700 seconds (Fig. 12b).

Fig. 11 Bright field image (a), SHG microcopy image (b) and overlay of both images (c) of an (S)-(+)-*p*-synephrine sample at an excitation wavelength of 900 nm (green zones correspond to the SHG signal).

The absence of signal means that the crystals evolved towards a centrosymmetric phase, most likely the racemic compound, as evidenced by thermal and XRPD analyses.

The evolution of the transformed fraction x versus time is plotted in Fig. 13: x is defined as the volume fraction of the stable phase (*i.e.* racemic compound) in the sample and is calculated from eqn (1):¹⁷

$$x = 1 - \frac{I_{\text{SHG}}(t)}{I_{\text{SHG}}^0} \quad (1)$$

I_{SHG}^0 is the initial SHG intensity (at room temperature) and $I_{\text{SHG}}(t)$ is the SHG intensity measured at time t .

The necessary time to complete the transition varies exponentially from *circa* 1100 seconds to 40 000 seconds at 150 °C and 120 °C, respectively. The isothermal curves depicted in Fig. 13 exhibit a classical shape for the transformation profile. Nevertheless, the direct fit of these curves using the classical Avrami equation leads to an activation energy of *circa* $100 \pm 10 \text{ kJ mol}^{-1}$ with a relatively poor correlation factor of 0.983 (data not shown).

The transition from the physical equimolar mixture of enantiomers to the racemic crystal involves three different crystal lattices and therefore belongs to a heterogeneous reaction. The kinetics will depend on the mobility of the components in the system where molecules are not readily

Fig. 12 SHG-M, BF and overlay images of the *p*-synephrine physical racemic mixture of (*R*) and (*S*) crystals at 120 °C after 0 seconds (a) and *circa* 6700 seconds (b).

Fig. 13 Reaction extent of the transformation (x) from the racemic mixture toward the racemic compound at different isothermal temperatures. For the sake of clarity, the scale is broken from 10 000 to 30 000 seconds.

available (in contrast to polymorphic transition for instance). Diffusion usually plays a role in the rates of reaction between reacting solids, when reactants are in separate crystal lattices (even if contact interfaces help the transition).

In diffusion-controlled reactions, the rate of formation of the new phase decreases proportionally with the growth because molecules must diffuse through the new solid. It can be shown (for spherical particles) in JMAEK models (which stands for Johnson, Mehl, Avrami, Erofev, and Kholmogorov) modified to account for diffusion (3D diffusion model) that the extent of reaction x is related to kinetic constant $k(T)$ and time t by the following expression:¹⁸

$$\left(1 - \sqrt[3]{1-x}\right)^2 = k(T)t \quad (2)$$

The expression $\left(1 - \sqrt[3]{1-x}\right)^2$ versus the time is plotted in Fig. 14 for different isothermal temperatures. The curves were linearly fitted to determine the $k(T)$ parameters for each temperature and the values are summarized in Table 3. One can notice that the fitting R -squared parameter is rather good ($R^2 > 0.99$).

Isothermal monitoring of the transition at higher temperatures was also conducted but the R^2 values were lower (for fitting from eqn (2)). The main reasons could be the existence of competitive processes: (i) phase transformation, (ii) metastable heterogeneous equilibria that participate to decrease the SHG signal faster over time and (iii) enhanced chemical degradation. For instance, rapidly after reaching 160 °C, a liquid phase appears (see the ESI†). This liquid phase could be associated with the cross of the metastable eutectic although it does not recrystallize in the stable phase, probably because of chemical degradation of the molecule in the liquid phase. It evidences the existence of the metastable eutectic in the range of 150–160 °C, close to the calculated temperature (149 °C).

The $k(T)$ parameter follows the Arrhenius law and can be expressed as:

$$k(T) = k_0 e^{-\frac{E_a}{RT}} \quad (3)$$

Constant k_0 is a pre-exponential frequency factor, E_a the activation energy of the transition, R the universal gas constant and T the temperature (in Kelvin). The Avrami constant $k(T)$ versus the temperature is plotted in Fig. 15 and was fitted using the least-squares Levenberg–Marquardt algorithm and eqn (3). This method has already been applied on organic compounds.^{16,19}

The extracted activation energy is *circa* 145 ± 2 kJ mol^{−1} with a correlation factor R -squared of 0.999. The value of E_a is relatively high and could explain the kinetic stability of the conglomerate at room temperature. For instance, the

Fig. 14 $\left(1 - \sqrt[3]{1-x}\right)^2$ versus time and linear fit for 120 °C, 130 °C, 140 °C and 150 °C of the conglomerate to racemic compound transition.

Table 3 Fit parameters of isothermal SHG measurements at 120 °C, 130 °C, 140 °C, and 150 °C

T (°C)	$k(T) \times 10^5$ (s ⁻²)	R -Squared	Time to complete the reaction (s)
120	1.678 ± 0.003	0.990	40 000
130	8.082 ± 0.012	0.997	10 000
140	26.61 ± 0.09	0.992	3500
150	72.05 ± 0.18	0.998	1100

Fig. 15 $k(T)$ evolution upon temperature and fitted curve from eqn (3). Red zone corresponds to 95% confidence domain.

conglomerate was kept for weeks at room temperature without any detection of the corresponding racemic compound.

Conclusion

Using the same thermal analysis protocol as that used for the racemic compound of (S)-(+)-*p*-synephrine, the melting characteristics of the enantiomers were determined with accuracy. The crystal structure of the enantiomer was also refined from X-ray powder diffraction. Then, a stable binary phase diagram between these chiral compounds was established through the coupling of DSC and crystallographic analyses.

An attempt to construct a metastable binary phase diagram between the two enantiomers was undertaken. Unfortunately, by heating an equimolar mixture of the two enantiomers, the transformation towards the racemic compound was too fast to obtain a clear DSC trace of the metastable eutectic invariant.

In order to bypass the irreversible formation of the racemic compound, it should be possible to use flash-DSC devices that can reach very high heating rates. Unfortunately, those calorimeters work with tiny mass of crystals. It is therefore extremely difficult to introduce an exact equal mixture of enantiomers and on top of that to ensure a good contact between the particles. However, this spontaneous solid-solid reaction could be tracked by TR-SHG microscopy.

This method is only based on several isothermal optical responses of the solid phases and thus overcomes the problem of low thermal trace of the transition and its slow kinetics for most of the temperature ranges investigated. It is therefore conceived as a general method to assess the activation energy of the irreversible heterogeneous reaction: $\langle R \rangle + \langle S \rangle \rightarrow \langle RS \rangle$ in racemic compound forming systems. The activation energy of the transition from the metastable conglomerate toward the stable racemic compound was estimated to be 145 ± 2 kJ mol⁻¹. This value explains the relative kinetic stability of the physical racemic mixture at room temperature. Microscopy also confirms the existence of the metastable eutectic invariant in the range of 150–160 °C.

Conflicts of interest

There are no conflicts of interest to declare.

References

- 1 M. D. Arbo, E. R. Larentis, V. M. Linck, A. L. Aboy, A. L. Pimentel, A. T. Henriques, E. Dallegrave, S. C. Garcia, M. B. Leal and R. P. Limberger, Concentrations of *p*-synephrine in fruits and leaves of Citrus species (*Rutaceae*) and the acute toxicity testing of *Citrus aurantium* extract and *p*-synephrine, *Food Chem. Toxicol.*, 2008, **46**, 2770–2775.
- 2 F. Rosa, P. Négrier, Y. Corvis and P. Espeau, Crystal structure determination and thermal behavior upon melting of *p*-synephrine, *Thermochim. Acta*, 2016, **632**, 18–22.
- 3 K. Honda, Identification of host-plant chemicals stimulating oviposition by swallowtail butterfly, *Papilio protenor*, *J. Chem. Ecol.*, 1990, **16**, 325–337.
- 4 Y. Corvis, M.-C. Menet, P. Négrier, M. Lazerges and P. Espeau, The role of stearic acid in ascorbic acid protection from degradation: a heterogeneous system for homogeneous thermodynamic data, *New J. Chem.*, 2013, **37**, 761–768.
- 5 *Materials Studio Modeling 5.5.*, (<http://accelrys.com/products/collaborative-science/biovia-materials-studio/>).
- 6 M. A. Neumann, X-cell: a novel indexing algorithm for routine tasks and difficult cases, *J. Appl. Crystallogr.*, 2003, **36**, 356–365.
- 7 G. S. Pawley, Unit-cell refinement from powder diffraction scans, *J. Appl. Crystallogr.*, 1981, **14**, 357–361.
- 8 B. D. Mayo and W. A. Goddard III, DREIDING: a generic force field for molecular simulations, *J. Phys. Chem.*, 1990, **94**, 8897–8909.
- 9 G. E. Engel, S. Wilke, O. König, K. D. M. Harris and F. J. J. Leusen, Powder Solve – a complete package for crystal structure solution from powder diffraction patterns, *J. Appl. Crystallogr.*, 1999, **32**, 1169–1179.
- 10 T. Kehl and G. van der Plaats, *US Pat.* 5.033.866, 1991.
- 11 G. F. M. Pinheiro, V. L. Lourenço and K. Iha, Influence of the heating rate in the thermal decomposition of HMX, *J. Therm. Anal. Calorim.*, 2002, **67**, 445–452.
- 12 M. Hurttä, I. Pitkänen and J. Knuutinen, Melting behaviour of d-sucrose, d-glucose and d-fructose, *Carbohydr. Res.*, 2004, **339**, 2267–2273.

- 13 I. Prigogine and R. Defay, *Chemical Thermodynamics*, 4th edn, Longmans, London, 1967.
- 14 I. Schröder, Dependence of the solubility of a solid on its melting point, *Z. Phys. Chem., Stoechiom. Verwandtschaftsl.*, 1893, **11**, 449–465.
- 15 J. J. Van Laar, Process of the fusion curves of firm alloys and amalgams, *Arch. Neerl. Sci. Exactes Nat.*, 1903, **8**, 264–284.
- 16 A. Galland, V. Dupray, B. Berton, S. Morin-Grognet, M. Sanselme, H. Atmani and G. Coquerel, Spotting Conglomerates by Second Harmonic Generation, *Cryst. Growth Des.*, 2009, **9**, 2713–2718.
- 17 S. Clevers, F. Simon, M. Sanselme, V. Dupray and G. Coquerel, Monotropic Transition Mechanism of m-Hydroxybenzoic Acid Investigated by Temperature-Resolved Second Harmonic Generation, *Cryst. Growth Des.*, 2013, **13**, 3697–3704.
- 18 A. Khawam and D. R. Flanagan, Solid-State Kinetic Models: Basics and Mathematical Fundamentals, *J. Phys. Chem. B*, 2006, **110**, 17315–17328.
- 19 D. Wanapun, U. S. Kestur, D. J. Kissick, G. J. Simpson and L. S. Taylor, Selective Detection and Quantitation of Organic Molecule Crystallization by Second Harmonic Generation Microscopy, *Anal. Chem.*, 2010, **82**, 5425–5432.