Simulating protein–ligand binding with neural network potentials†

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Drug molecules adopt a range of conformations both in solution and in their protein-bound state. The strain and reduced flexibility of bound drugs can partially counter the intermolecular interactions that drive protein–ligand binding. To make accurate computational predictions of drug binding affinities, computational chemists have attempted to develop efficient empirical models of these interactions, although these methods are not always reliable. Machine learning has allowed the development of highly-accurate neural-network potentials (NNPs), which are capable of predicting the stability of molecular conformations with accuracy comparable to state-of-the-art quantum chemical calculations but at a billionth of the computational cost. Here, we demonstrate that these methods can be used to represent the intramolecular forces of protein-bound drugs within molecular dynamics simulations. These simulations are shown to be capable of predicting the protein–ligand binding pose and conformational component of the absolute Gibbs energy of binding for a set of drug molecules. Notably, the conformational energy for anti-cancer drug erlotinib binding to its target was found to be considerably overestimated by a molecular mechanical model, while the NNP predicts a more moderate value. Although the ANI-1ccX NNP was not trained to describe ionic molecules, reasonable binding poses are predicted for charged ligands, but this method is not suitable for modeling charged ligands in solution.

Introduction

Molecular simulation of the binding of small molecules to proteins has provided computational prediction and rationalization of the affinity and selectivity of drugs with their targets. These simulations rely on molecular mechanical (MM) force fields to describe the intra and intermolecular interactions of the solvent, protein, and ligand. These “force fields” are constructed from simple mathematical functions that approximate the potential energy surface of the protein–ligand complex. A force field requires the definition of a large set of parameters, which are typically chosen to yield the closest agreement with empirical or quantum chemical data.

Development of accurate models of potential energy terms of protein–ligand binding and their optimal parameters is a long-standing objective in computational chemistry. The electrostatic,1,2 repulsive, and dispersion1,4 interaction terms have been developed actively; however, accurate representation of intramolecular potential energy of the ligand is particularly challenging and no complete, general solution has been developed. Current force fields approximate intramolecular forces using simple but generally effective terms that were introduced more than 50 years ago,3 where bond angles and stretches are described with harmonic potentials (i.e., spring-like) and torsional barriers are defined as the sum of a handful of cosine functions. Force fields for drug-like compounds are particularly difficult to develop because of the enormous variety of chemical motifs, which often feature complex chemical effects like conjugation, hyperconjugation, and aromaticity. This is compounded by the enormous variety of chemical motifs that are possible in chemical drug space, where each could require a distinct set of parameters. For example, the proprietary OPLS3 force field defines 124 atom types and 48 142 torsional parameters.2 Other methods provide options to reparameterize force fields automatically using ab initio calculations2,7–11 although this complicates the simulation workflow and can be computationally expensive.

Recently, machine-learned neural network potentials (NNPs) have emerged as an alternative to conventional MM force fields.12 The ANI models13,14 developed by Roitberg and coworkers define the atomic positions in terms of a set of “symmetry functions”,12 which are constructed from the position of a given atom relative to nearby atoms. A neural network is trained to reproduce the high-level ab initio electronic energies (i.e., CCSD(T)) from these data. These potentials are remarkably robust and predict the structures and relative stabilities of molecular conformations across a broad set of...
chemical structures with similar accuracy to the high-level *ab initio* data they were trained to reproduce. The computational cost of NNPs is comparable to molecular mechanical models, so they can be used to perform nanosecond (ns) length simulations of molecules containing dozens or hundreds of atoms routinely.

Here, we present a strategy to simulate protein–ligand complexes using a machine-learned NNP to represent the intramolecular interactions of the ligand. This model is embedded inside a conventional MM force field for the protein and solvent, so established models for these components can be used without modification. We call this method NNP/MM, as it functions the same as Quantum Mechanical/Molecular Mechanical (QM/MM) models do, but with the NNP used in place of the QM method. This method is tested for its ability to predict the poses of protein-bound drugs in comparison to electron density distributions determined by X-ray crystallography. The Gibbs energies for restraining the ligands to their bound conformations are calculated using NNP/MM and compared to the CGenFF force field.

Computational methods

Theory

In this method, the potential energy of the whole system is defined as the sum of the potential energy of the subsystem described by the NNP (i.e., the intramolecular interactions of the ligand) \( \gamma_{\text{NNP}} \), the potential energy of the environment around the ligand \( \gamma_{\text{MM}} \), and the interactions between the ligand and its environment \( \gamma_{\text{NNP/MM}} \) (eqn (1)).

\[
\gamma(\mathbf{r}) = \gamma_{\text{MM}}(\mathbf{r}_{\text{MM}}) + \gamma_{\text{NNP}}(\mathbf{r}_{\text{NNP}}) + \gamma_{\text{NNP/MM}}(\mathbf{r})
\]

where \( \mathbf{r} \) is the coordinates of the whole system, \( \mathbf{r}_{\text{MM}} \) is the coordinates of the ligand itself, \( \mathbf{r}_{\text{NNP}} \) is the coordinate of the ligand, \( \mathbf{r}_{\text{NNP/MM}} \) is the coordinates of the ligand. The MM region is represented using a conventional MM force field, so \( \gamma_{\text{MM}} \) is calculated in the normal fashion for an additive force field. For non-covalent protein–ligand binding, the \( \gamma_{\text{NNP/MM}} \) term is the conventional MM non-bonded interactions between the protein and the ligand, which is simply the sum of Lennard-Jones and pairwise coulombic interactions between the NNP atoms and MM atoms (eqn (2)).

\[
\gamma_{\text{NNP/MM}}(\mathbf{r}) = \sum_{i,j}^{\text{MM}} \sum_{\text{NNP}} \frac{q_i q_j}{4 \pi \epsilon r_{ij}} + 4 \epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right]
\]

This function similarly to mechanically-embedded QM/MM models, where the NNP serves as the “QM” model embedded within the MM system. This method can be employed in many established simulation codes without modification because they can implemented using existing QM/MM features, which allow the energy and forces of a critical subsection of the system to be calculated using an external method.

The immediate advantage of this method is that highly-accurate intramolecular forces can be calculated for ligands without parameterization and without modifications to current molecular simulation codes. A limitation of this approach is that the protein–ligand interactions are still calculated by the CGenFF/CHARMM electrostatic and Lennard-Jones terms. The development of efficient NNPs that are capable of describing the entire system could provide more accurate and non-empirical protein–ligand binding energies.

There have been several reports where QM/MM simulations were used to model protein–ligand complexes.\(^{17-19}\) The drawback of these QM methods is that typically they use semi-empirical quantum mechanics in order to calculate the energy and forces of the ligand sufficiently quickly to perform sufficiently long MD simulations. These methods generally are less accurate than the ANI NNPs for the calculations of the relative conformational stability of ligand conformations and the computational cost is generally greater. One advantage of QM/MM methods over the NNP/MM method used here is that the electron density of the ligand can be polarized by the protein and solvent (i.e., through electrostatic-embedding QM/MM\(^{20}\)). This is not possible for the NNPs used here because these methods do make any calculation of the electron density of the ligand, so they are effectively mechanically embedded.

Technical details

All molecular dynamics (MD) simulations were performed using NAMD 2.13.\(^{29}\) The ligand intramolecular energies and forces were calculated using the ANI-1ccX\(^{14}\) NNP implemented in the TorchANI package.\(^{21}\) The programs were interfaced through the general-purpose external-force functionality of the NAMD QM/MM code.\(^{22}\) The CHARMM36m force field\(^{23}\) was used to represent the protein and the mTIP3P model\(^{24,25}\) was used to represent the water molecules. Sample input files and our scripts can be downloaded from our online repository\(^{26}\) and will be included in future distributions of NAMD. The CgenFF\(^{27}\) Lennard-Jones and electrostatic parameters were used to calculate the non-bonded ligand–protein interactions (i.e., \( \gamma_{\text{NNP/MM}} \)). Non-bonded interactions were calculated using a 12 Å cutoff, although lattice-summation methods are also available in the QM/MM NAMD interface.

The calculation of the erlotinib potential energy surface was performed using ORCA 4.2.1.\(^{26}\) Optimizations with constraints on the amine torsional angle were performed using the resolution of identity 2nd-order Möller–Plesset theory (RI-MP2) with the def2-TZVP basis set.\(^{29}\) Single point energy evaluations were performed at these optimized structures using Domain-based Local Pair Natural Orbital – Coupled Cluster Singles and Doubles with perturbative triples\(^{29}\) with the def2-TZVP basis set (DLPNO-CCSD(T)/def2-TZVP//RI-MP2/def2-TZVP) to generate the QM potential energy surface.

Test set

To evaluate the ability of the ANI-1ccX potential to predict the pose of a bound ligand, we developed a test set of protein–ligand complexes. We selected a structurally-diverse set of complexes where a high-resolution crystallographic structure of the protein–ligand complex was available, including several where the ligand
is in a conformationally-strained pose. The ANI-1ccX NNP is only defined for carbon, nitrogen, hydrogen, and oxygen, so only ligands comprised of these elements were selected. The full details of the structures are included in the ESL.

Simulations of ligand binding poses

The NNP/MM ligand binding poses were generated by MD simulations of the protein–ligand complexes. The crystallographic structure (including crystallographic water molecules) was placed in a periodic unit cell of liquid water. The protonation states of the protein and ligand were assigned using H++ 3.2 (ref. 31) and by examining the intermolecular interactions of titratable residues in the crystallographic structure. A 5 ns equilibration MD simulation using the CGenFF force field for the ligand was performed where all non-hydrogen atoms of the ligand and protein were restrained to their crystallographic positions. The equilibrated structures were used as the initial structures of 2 ns NNP/MM MD simulations of the complexes. In these simulations, the C\text{α} atom of the protein backbone were restrained to their crystallographic positions using harmonic potentials (k\text{c} = 10 kcal mol\(^{-1}\) Å\(^{-2}\)). These simulations were performed with a thermostat temperature set to correspond to the temperature the crystallographic structure was collected for (e.g., 100 K). The ligand electron density was obtained from the crystallographic electron density map (2\text{f}_{\text{c}} - f_{\text{c}}), selecting all points within 2 Å of the ligand atoms in the PDB structure. An isosurface value of 0.5 was used in the renderings.

Calculation of conformational Gibbs energy

Confine-and-release alchemical free energy perturbation is a popular technique for calculating absolute protein–binding energies.\textsuperscript{30–33} In these methods, the total binding energy is divided into a set of Gibbs energies for each step in a path where the ligand is constrained to its bound conformation and is then decoupled from its environment. The component corresponding to the reversible work required to constrain the ligand to its bound conformation is defined as \(\Delta G_{\text{cons}}\). Physically, this energy corresponds to the reduction of conformational freedom and isomerization to a higher energy conformation that occurs when a ligand binds to a protein. In confine-and-release absolute binding energy calculation schemes, this is the only term where the intramolecular interactions of the ligand are significant. Accordingly, it is only necessary to use the NNP/MM method when calculating this term; the remaining terms can be calculated using conventional force fields. Notably, this step does not include any alchemical transformation, so performing the calculation with NNP/MM does not present any special challenges.

This term can be calculated by defining the root-mean-square deviation (RMSD) of the ligand relative to its bound conformation (\(\xi\)) and then calculating the Gibbs energy required to impose a harmonic restraint on the RMSD \(\left(\frac{1}{2}k_{\xi}\xi^{2}\right)\) so that the ligand is restricted to hold its bound conformation. This procedure is performed for the ligand in solution and in the site to obtain Gibbs energies for restricting the conformation of the ligand in each of these states. The difference of these energies provides the conformational or “strain” component of the absolute binding energy (\(\Delta G_{\text{cons}}\)).

Using umbrella sampling, the potential of mean force (PMF) can be calculated as a function of the RMSD. Integration of this PMF biased by the harmonic restraining function provides the \(\Delta G_{\text{cons,site/solvent}}\) (eqn (3)).

\[
e^{-\Delta G_{\text{cons,site/solvent}}/k_{B}T} = \frac{\int e^{\left[-w(\xi,\text{site/solvent}) + \frac{1}{2}k_{\xi}\xi^{2}\right]}/k_{B}T \, d\xi}{\int e^{-w(\xi,\text{site/solvent})}/k_{B}T \, d\xi}
\]  
\text{(3)}

where \(k_{\xi}\) is a harmonic potential to restrain the conformation of the ligand at the reference structure. In this work, a value of \(k_{\xi} = 10\) kcal mol\(^{-1}\) Å\(^{-2}\) was used.

These PMFs are calculated from an umbrella sampling simulation where the windows were separated by 0.5 Å and a harmonic biasing potential with a spring constant of 50 kcal mol\(^{-1}\) Å\(^{-2}\) was used. Each window was sampled by performing a 1 ns equilibration simulation followed by a 4 ns sampling simulation. The PMF was constructed from the umbrella sampling simulations using Weighted Histogram Analysis Method (WHAM) with statistical uncertainties of the profiles estimated by bootstrap analysis.\textsuperscript{36–38}

These calculations are performed for the ligand bound to the protein and in solution to yield \(\Delta G_{\text{cons,site}}\) and \(\Delta G_{\text{cons,solvent}}\) respectively. The difference of these two energies provides \(\Delta G_{\text{cons}}\) (eqn (4)).

\[
\Delta G_{\text{cons}} = \Delta G_{\text{cons,site}} - \Delta G_{\text{cons,solvent}}
\]  
\text{(4)}

Results and discussion

Prediction of ligand poses

Fig. 1 shows the ligand poses generated from the ANI/MD simulations overlaid with the crystallographic electron density maps of the ligand. Generally, the NNP/MM ligand pose overlaps well with the crystallographic density. The positions of the ligand phenyl rings in the thrombin complex (3DA9) and the biotin carboxylase complex (2W6N) are the most significant deviation. The NNP/MM model still relies on conventional MM parameters for the protein–ligand and water–ligand interactions, so these deviations may not be related to the NNP component of the model.

One notable success of the NNP/MM potential is in predicting the binding pose of erlotinib to the epidermal growth factor receptor (EGFR). The core scaffold of this drug is composed of amine-linked ethynyl-phenyl and quinazoline rings. Crystallographic structures of the protein-bound complex show the quinazoline ring bound in the adenosine-binding site while the ethynyl-phenyl group binds in a pocket formed by the T702, T830, and K721 residues. The binding pose predicted by CGenFF is inconsistent with the XRD data, in which the two rings form a more acute angle relative to each other (\(\phi_{\text{1}} = \text{63} \pm 1^{{\circ}}, \phi_{\text{2}} = \text{4} \pm 1^{{\circ}}\)). The simulation using the NNP/MM model is more consistent with the crystallographic data, (\(\phi_{\text{1}} = \text{44} \pm 1^{{\circ}}, \phi_{\text{2}} = \text{4} \pm 1^{{\circ}}\)).

Surprisingly, the poses predicted for the ligands that contain charged functional groups (2HYY, 3ETA, and 3E1G) are
reasonable even though the ANI-1ccX potential was not designed to describe charged species and none of the molecules this NNP was trained for were charged.

Conformational free energies

The conformational strain of the ligand that occurs in protein–ligand binding arises from the need for the ligand to adopt the conformation it holds in its bound form. The bound conformation may be more strained than the lowest energy conformation it can hold in solution. Further, some ligands can adopt multiple conformations in solution, so limiting the conformational space of the ligand to the bound conformation is endergonic. For example, Roux and coworkers’ calculations of the binding affinity of imatinib to Abl kinase predicted that while the net interaction energy of binding was $-27.7 \text{ kcal mol}^{-1}$, the conformational energy countered this by $11.3 \text{ kcal mol}^{-1}$.\textsuperscript{39} The conformational energies for the test set of ligands were estimated by calculating the PMF ($\mu(w)$) for the deviation from the bound pose using umbrella-sampling MD simulations with both the CGenFF and NNP/MM models. $\Delta G_{\text{cons}}$ was calculated from these PMFs using eqn (3). These energies are collected in Table 1. The PMFs for all complexes are presented in the ESL\textsuperscript{†}

Amongst the neutral ligands, the NNP/MM conformational energies are generally similar in magnitude to the CGenFF strain energies. This indicates that the ANI-1ccX model can achieve similar results to the CGenFF model despite the lack of any explicit parameterization for these molecules. The conformational energies of 4HJO (erlotinib bound to EGFR) show the

<table>
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<th>PDB ID</th>
<th>$\Delta G_{\text{cons,CGenFF}}$</th>
<th>$\Delta G_{\text{cons,NNP/MM}}$</th>
<th>Charge</th>
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<tr>
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<td>3ETA</td>
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<td>$15.2 \pm 0.2$</td>
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</tr>
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Table 1 Conformational Gibbs energy of binding for protein–ligand complexes calculated using the MM(CGenFF) and NNP/MM methods. All energies are in kcal mol$^{-1}$.
The large difference in the ANI-1ccX and CGenFF conformational energies of 4HJO (erlotinib bound to EGFR) originate from the ligand adopting conformations in solution that are drastically different than the bound conformation when the CGenFF model is used, while the NNP/MM model predicts similar conformations in both the binding site and solution. This is evident in the CGenFF PMF of the ligand’s conformation relative to its bound pose in Fig. 2, which is considerably broader than the NNP/MM PMF and is higher energy in the crystallographic pose (RMSD = 0 Å).

The geometry of the erlotinib amine linker and its aromatic substituents deviates sharply from the bound pose in the CGenFF solution structure (Fig. 3(b)); the amine is partially pyramidalized and the aromatic substituents are skew to each other. In contrast, in the NNP/MM simulation, the amine predominantly remains in a planar geometry, conjugated with the quinazoline and phenyl rings.

The potential energy surface corresponding to rotations around the amine torsion angles of erlotinib is presented in Fig. 3(c). The minima on the CGenFF surface corresponds to structures where the amine is significantly pyramidal and the substituent phenyl and quinazoline rings adopt angles that reduce steric repulsion between them. The ANI-1ccX surface is consistent with the DLPNO-CCSD(T) surface, where there is a broad global minimum centered around $\phi_1 = 0^\circ$, $\phi_2 = 0^\circ$ and the amine nitrogen holds a planar arrangement with the aromatic groups.

The failure of the CGenFF force field stems from the lack of a distinct atom type for amines conjugated with aromatic rings. While it would be possible to adjust the parameters of the CGenFF force field to improve its description of the arylamine potential energy surfaces, this introduces a new fitting stage and requires computationally demanding QM calculations to provide the target data. Generally, it is not immediately apparent where a general-purpose force field will fail. By using NNPs to calculate these interactions, these issues are avoided entirely because energy surfaces with near-CCSD(T) accuracy
can be generated efficiently and without the need to parameterize the intramolecular potential energy surface explicitly.

Conclusions

NNPs provide accurate representations of the intramolecular interactions of drug molecules in molecular simulations of protein-ligand binding. These simulations take advantage of established MM models of the protein and solution, while eliminating the need to develop a force field for the intramolecular interactions of each ligand. By employing a NNP that has already been trained on a broad set of molecular species, the fundamental intramolecular interactions that give rise to the molecular energy surface are captured without the need to parameterize a force field. This representation is also free of the harmonic/torsional/improper terms used in conventional force fields. This allows the simulations to be deployed immediately, without the development of parameters for each new chemical moiety.

These methods can be incorporated directly into existing confine-and-release methods to calculate the absolute binding energy because these methods include a step where the ligand’s conformation is constrained to its bound pose. In several cases, the conformational energies calculated using the NNP(ANI-1ccX)/MM model were similar to those predicted by the popular general-purpose CGenFF force field.

The scope of the ligands that can be modelled is limited by the choice of the NNP, which is particularly true for the ANI-1ccX model. Firstly, the ANI-1ccX model only supports molecules containing C, N, O, and H, although many important drug molecules also contain sulfur, phosphorus, boron, or halogen atoms. Secondly, ANI-1ccX NNP was not designed for modeling ionic species. Although the binding poses predicted for these compounds were reasonable, the NNP spuriously favored high-energy conformations in solution. This reflects that the ANI-1ccX training data did not include ionic species. ANI-type models that are trained to describe molecules containing sulfur and halogens, as well as charged molecules, are currently in development.¹²

Conflicts of interest

There are no conflicts to declare.

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Notes and references

42. O. Isayev, personal communication.