Amino acid interacting network in the receptor-binding domain of SARS-CoV-2 spike protein†

Puja Adhikari and Wai-Yim Ching

The relation between amino acid (AA) sequence and biologically active conformation controls the process of polypeptide chains folding into three-dimensional (3d) protein structures. The recent achievements in the resolution achieved in cryo-electron microscopy coupled with improvements in computational methodologies have accelerated the analysis of structures and properties of proteins. However, the detailed interaction between AAs has not been fully elucidated. Herein, we present a de novo method to evaluate inter-amino acid interactions based on the concept of accurately evaluating the amino acid bond pairs (AABP). The results obtained enabled the identification of complex 3d-long-range interconnected AA interacting network in proteins. The method is applied to the receptor binding domain (RBD) of the SARS-CoV-2 spike protein. We show that although nearest-neighbor AAs in the primary sequence have large AABP, other nonlocal AAs make substantial contribution to AABP with significant participation of both covalent and hydrogen bonding. Detailed analysis of AABP in RBD reveals the pivotal role they play in sequence conservation with profound implications on residue mutations and for therapeutic drug design. This approach could be easily applied to many other proteins of biomedical interest in life sciences.

Introduction

Amino acids (AAs) together with the nucleobases in deoxyribonucleic acid (DNA) and ribonucleic acid (RNA) structures with specific base pairs are the fundamental entities in biological science and human evolution.1 The primary structure of a protein refers to the sequence of AAs in the polypeptide chain held together by peptide bonds and controls its stability and functionality. Amino acid mutation refers to random changes in the sequence and minor modifications in the structure that are related to the genetic evolution of species over a long time. All AAs contain a central carbon (C) atom, an amine group and a lone hydrogen (H) atom but they differ from each other with different side chains known as the R group. Some AAs have charged side chains important to their linkage and mutual interaction. The elements C, N and O in AAs form strong covalent or ionic bonds and also the weaker hydrogen bonds (HBs). Cysteine (Cys) and methionine (Met) are the only two AAs that contain S which can form disulfide bonds.

Conservation of AA sequence is considered to hold the key for understanding many of the biological and evolution process.2 A highly conserved sequence is one that has remained relatively unchanged far up in the phylogenetic tree, and hence way back into geological time scale. Traditional analysis of conservation is based on the comparative study of the alignment of AA sequence of different proteins from closely related species or at different times. The compensatory effect in these important interactions exclusively relied on the linear sequence of residue numbers of the AAs. In other words, for a specific AA in the sequence, it only considers the two nearest neighbor (NN) AAs with little consideration of the interactions with other nonlocal AAs in the real three dimensional (3d) space which form secondary or tertiary structures. There have been some recent efforts to go beyond this linear sequence model.3 However, most such analysis depend on statistical methods and probability theory such as multiple sequence alignment (MSA),3 statistical coupling analysis (SCA),4 direct coupling analysis (DCA)4 etc. They all based on the homologous sequence, and sequence alone, of the AAs in the protein. The use of efficient algorithm and combinatorial data analysis scheme had some success in the directional dependence of AAs.5 Nevertheless, they all share the same drawback of lack of numerical quantification of AA-AA interaction that are not NNs. The distance of separation between two neighboring AAs is not a precisely defined quantity as in the case for atoms or small molecules. AAs are essentially biomolecules with different sizes, compositions, structures and orientations. They cannot be easily quantified as a viable parameter routinely used in some published literatures.5 Precise quantification requires accurate first-principles calculation at the atomistic level.
Historically and not too long ago, the Holy Grail in biological research is to predict the structure of unknown proteins using a variety of techniques including existing protein data, various sequence analysis, experimental crystallography and NMR spectroscopy. The discovery of cryogenic electron microscopy (cryo-EM) that can determine bio-molecular structures at near-atomic resolution is the game changer.\textsuperscript{6–8} AA sequences can be reliably determined and their structures are deposited in data banks such as PDB, CNBI, GenBank, etc. with specific identity codes. More recently, it has been reported that the resolution of cryo-EM can be further increased from the current 3.5 Å to less than 1.3 Å with the visualization of H atoms.\textsuperscript{9,10} The new goal now is to accurately determine the structures of new proteins, to verify and validate many unproved hypotheses and to explain some intriguing phenomena. In this regard, their structural refinement to even higher precision using large-scale computational modeling is absolutely necessary. The computationally refined structure can be used to investigate the details of intra- and inter-protein interactions at the atomistic level\textsuperscript{11} and reveal the possible mechanism of biological interaction under different environments. Currently the atomic resolution from cryo-EM is about 3.2–3.5 Å.\textsuperscript{12} Most of the data deposited have the AA sequence but not the H atoms that saturate the dangling bonds. In addition, the atomic coordinates of some AAs in the sequence are sometimes missing for various technical reasons.

The outbreak of the coronavirus disease in late 2019 (COVID-19) has rapidly emerged as an appalling epidemic with no end in sight. It is caused by the new severe acute respiratory syndrome corona virus 2 (SARS-CoV-2). The key to combat this virus is to understand its complex structure and function\textsuperscript{13–19} with the visualization of H atoms.\textsuperscript{20,21} The new goal now is to accurately determine the structures of the S-protein and the use of PBE potential is reasonably accurate for biomolecular systems. The input parameters used are: energy cut-off 500 eV, electronic convergence criterion of 10–4 eV; force convergence criteria for ionic relaxation –10–2 eV Å\textsuperscript{−1} and a single k-point sampling. All VASP structure relaxations were carried out at the National Energy Research Scientific Computing (NERSC) facility at the Lawrence Berkeley Laboratory and Research Computing Support Services (RCSS) of the University of Missouri System. They are fully relaxed and the resulting accuracy in atomic positions is estimated to be less than 0.01 Å. The initial unrelaxed and fully relaxed total energy from VASP relaxation for the small SD1 subdomain is −2370.8472 eV and −2379.2055 eV respectively. The reduction in the total energy of 8.3533 eV lower for 24 AAs with 391 atoms in SD1 implies a reduction of 0.02 eV (1.93 kcal mol\textsuperscript{−1}) per atom.

### Electronic structure, interatomic bonding and partial charge on amino acids

For the electronic structure calculations of the protein domains, we use the in-house developed all-electron orthogonalized linear combination of atomic orbitals (OLCAO) method\textsuperscript{22} with the VASP-relaxed structure as input. The merit of combining the two different DFT codes (VASP for accurate structure optimization and atomic orbital based OLCAO method for bonding analysis) is well documented\textsuperscript{24–27} and it is especially effective for large complex biomolecular systems such as COVID-19 virus. The key point of the success of the OLCAO method is provision of the effective charge (\(Q^*\)) on each atom and the bond order (BO) values \(\rho_{\alpha\beta}\) between any pairs of atoms. They are obtained from the \textit{ab initio} wave functions with atomic basis expansion calculated quantum mechanically:

\[
Q^*_\alpha = \sum_{\text{i m occ.}} \sum_{j} C^\text{ini}_\text{ij}^* C^\text{ini}_\text{ij} S_{\text{ini,j}}
\]

\[
\rho_{\alpha\beta} = \sum_{\text{i m occ.}} \sum_{j} C^\text{ini}_\text{ij}^* C^\text{ini}_\text{ij} S_{\text{ini,j}}
\]

In the above equations, \(S_{\text{ini,j}}\) are the overlap integrals between the \(i\)th orbital in \(\alpha\)th atom and the \(j\)th orbital in \(\beta\)th atom. \(C^\text{ini}_\text{ij}\) are the eigenvector coefficients of the \(m\)th occupied molecular orbital. The partial charge (PC) or \(\Delta Q^* = Q^*_\alpha - Q^*_\beta\) is the deviation of the effective charge \(Q^*_\alpha\) from the neutral atomic charge \(Q^0\) on the same atom \(\alpha\). The BO signifies the strength of the bond between two atoms. The calculation of PC and BO are based on the Mulliken scheme.\textsuperscript{28,29} Hence such calculations are basis-dependent. Comparisons of BO values using different basis or different methods should be treated with caution. The atomic-scale interactions based on DFT calculations are critical for

### Methods

#### Structural construction and relaxation

The structure for the S-protein in SARS-CoV-2 is downloaded from PDB (ID: 6VSB). The missing H atoms in the coordinates are added using standard software Chimera.\textsuperscript{30} This initial structure is then fully relaxed using The Vienna \textit{ab initio} simulation package (VASP).\textsuperscript{31} We used the projector augmented wave (PAW) method with the Perdew–Burke–Ernzerhof (PBE) exchange correlation functional\textsuperscript{23} within the generalized gradient approximation (GGA). While it is possible to use more elaborate potentials within the density functional theory but they are computationally prohibitive due to the large and complex structure of the S-protein and the use of PBE potential is reasonably accurate for biomolecular systems. The input parameters used are: energy cut-off 500 eV, electronic convergence criterion of 10–4 eV; force convergence criteria for ionic relaxation –10–2 eV Å\textsuperscript{−1} and a single k-point sampling. All VASP structure relaxations were carried out at the National Energy Research Scientific Computing (NERSC) facility at the Lawrence Berkeley Laboratory and Research Computing Support Services (RCSS) of the University of Missouri System. They are fully relaxed and the resulting accuracy in atomic positions is estimated to be less than 0.01 Å. The initial unrelaxed and fully relaxed total energy from VASP relaxation for the small SD1 subdomain is −2370.8472 eV and −2379.2055 eV respectively. The reduction in the total energy of 8.3533 eV lower for 24 AAs with 391 atoms in SD1 implies a reduction of 0.02 eV (1.93 kcal mol\textsuperscript{−1}) per atom.

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A number of values of AABP (sequence. The matrix element represents the interaction between all atoms. More details on the OLCAO method can be found in ref. 12 and 23.

Amino acid bond pair (AABP)

In the OLCAO method, the bond order (BO) values \(\rho_{\alpha \beta}\) described above are calculated for every pairs of atoms \((\alpha, \beta)\) within a cutoff distance of 2.5 Å. The position of the atom is a well-defined quantity, whereas the positions of amino acids in the biological system are not because they are essentially biomolecules with different atoms, configurations and orientations. Strictly speaking, to assign a distance of separation between different amino acids in a protein in order to describe their interactions is an ill-conceived parameter based on some vague and arbitrary criteria.

However, with the quantum mechanically based OLCAO method and with the interatomic interaction between all atoms available, we can define the bonding between two amino acids \(u\) and \(v\) with no ambiguity which we coin as amino acid bond pair (AABP):

\[
\text{AABP}(u, v) = \sum_{\alpha \in u} \sum_{\beta \in v} \rho_{\alpha \beta}
\]

where the summations are over atoms \(\alpha\) in AA \(u\) and atoms \(\beta\) in AA \(v\). This is a far more rigorously defined quantity that has never been attempted before. AABP takes into account of all possible bonding between two amino acids, which includes both covalent and hydrogen bonding. This single quantitative parameter from electronic structure reflects the internal bonding strength among amino acids. In addition, it can be resolved into nearest neighbor (NN) and non-local bonding. This quantitative parameter is ideal to understand inter amino acid bonding in different biomolecules. This will be demonstrated in the section where AABP for all AAs in SD1 and RBD domains of the S-protein are presented and discussed.

In principle, interatomic bonding between every pair of atoms in RBD of the S-protein with 2100 atoms in this work is already well defined in eqn (1) and (2) above and calculated by the full diagonalization of the secular equation in the OLCAO method. However, it requires the eqn (3) above to decipher them into pair-wise inter-amino acid bonding from the interatomic bonding that has not been done except may be in few isolated cases of a few amino acids. The merit of the above scheme is that AABP for selected groups can obtained by adding their BO in that group for relative comparisons such as those listed in Table 1 for SD1.

Matrix presentation of nonlocality in AABP

To prepare data for effective representation for AABP \((u, v)\), we design a matrix representation in which the rows \((u)\) and columns \((v)\) designate the each of the amino acids in the sequence. The matrix element represents the \((u, v)\) is the numerical value of AABP \((u, v)\) in unit of electrons. Obviously, this matrix is symmetric and AABP \((u, v) = 0\) for \(u = v\) and AABP \((u \pm 1, v) \neq 0\) since they represent the nearest neighbor (NN) interaction of the primary sequence of the AAs in the protein.

Even though AABP \((u, v)\) is not diagonal but it shows diagonal nature so, we name this NN interaction to be pseudo-diagonal cell in this paper. The nonzero AABP \((u, v)\) represent the nonlocal AABP \((u, v)\) interactions in 3d. The empty cell box in AABP \((u, v)\) simply indicate these pairs are non-interacting since they are too far apart with negligibly small calculated BO between the atoms of different AAs. The RBD domain has 144 AAs and listing a 144 \(\times\) 144 matrix is obviously unpractical. They are divided into 10 submatrices as shown in Fig. S1†. The smaller subdomain SD1 with 24 AAs, the matrix is 24 \(\times\) 24. The matrix presentation for data for AABP \((u, v)\) for SD1 and RBD are shown in Tables S1 and S2† respectively.

### Result and discussion

The spike protein or S-protein in SARS-CoV-2 consists of three chains A, B, C with the chain A in the up conformation most critical since it is receptor accessible. Each chain in S-protein has two subunits, receptor binding S1 and membrane binding S2. S1 consists of N-terminal domain (NTD), receptor binding domain (RBD), SD1 and SD2. S1 has 526 AAs and S2 has 433 AAs as depicted in Fig. 1. So, S-protein has a total of 959 AAs excluding the ones with missing coordinates due to either technical difficulties or because they were deemed to be less important for biological interactions related to coronavirus. SD1 is the smallest subdomain with only 24 AAs and has been used to illustrate new methods, approaches and data analysis, whereas RBD is the most important domain in S-protein since it directly contacts the ACE2. A somewhat minor complication in RBD is that the atomic coordinates on three flexible segments of the AA sequences are missing. The region for SD1 (305–328) also has missing position coordinates for some AAs, which we have simply ignored. Under this scheme, the RBD (330–521) has 144 AAs excluding missing ones as indicated in Fig. 1. This will be alerted in later presentation of figures and tables. Furthermore, there are 6 AAs (329–334) missing their positions between SD1 and RBD. Another critically missing positions are 14 AAs (673–686) near the junction of S1 and S2. This is at the polybasic furin cleavage sites instrumental for viral infection when RBD in S-protein fuses with the ACE-2 cell in human. The ribbon

<table>
<thead>
<tr>
<th>Bond Type</th>
<th>Sum of BO of Type</th>
<th>No. of Bonds</th>
</tr>
</thead>
<tbody>
<tr>
<td>C–H</td>
<td>0.4074</td>
<td>1</td>
</tr>
<tr>
<td>N–C</td>
<td>61.6410</td>
<td>140</td>
</tr>
<tr>
<td>N–H</td>
<td>0.3395</td>
<td>1</td>
</tr>
<tr>
<td>N–O</td>
<td>0.2927</td>
<td>4</td>
</tr>
<tr>
<td>O–H</td>
<td>0.2555</td>
<td>1</td>
</tr>
<tr>
<td>O–N</td>
<td>2.9788</td>
<td>89</td>
</tr>
<tr>
<td>S–S</td>
<td>0.3324</td>
<td>2</td>
</tr>
<tr>
<td>Total</td>
<td>66.1843</td>
<td>238</td>
</tr>
</tbody>
</table>

Table 1: Number of bonds in different types of bonds and the sum of BO for each type in RBD with 8Å cutoff of 2.5 Å
**Fig. 1** The S-protein in SARS-CoV-2 (6VSB) divided into two subunits S1 and S2 with their domains. The missing position coordinates are indicated by vertical black lines with their sequence numbers shown in grey boxes pointed with dashed arrows. The overall number of amino acids, atoms and their sequence number range are marked in upper part of the horizontal bar. The numbers at the bottom of the horizontal bar show the sequence numbers for the domains with their respective color.

**Fig. 2** (a) The ribbon structure of SD1. Ball and stick figure showing (b) SD1 with all 24 AA marked, (c) interaction between the first three amino acids Ser305, Phe306, and Thr307, and (d) interaction among four AAs Glu309, Lys310, Gly311, and Tyr313. Both shows two NNs forming covalent bonds (solid lines) and one off-diagonal HB (dashed line). (e) The ribbon structure of RBD.
structures of SD1 and RBD are shown in Fig. 2(a) and (e) respectively.

We will first use the data for subdomain SD1 (Fig. 2(b)) with only 24 AAs as an example to illustrate the type of results that can be obtained making it easier to understand the results for RBD. The results of AABP for SD1 are listed in Table S1 in the ESI† in the form of a 24 × 24 matrix (see Methods section). The pseudo-diagonal blocks of cells representing the calculated AABP values between the NN pairs are highlighted in yellow. There are only 2 off-diagonal AABP in the matrix for SD1, one between Ser305 and Thr307 with AABP = 0.079 e⁻ and the other one is between Glu309 and Tyr313 with AABP = 0.078 e⁻. The main reason that there are only two off-diagonal AABP pairs is because SD1 is an elongated protein and the AAs are further separated unless they are NNs. This is certainly not the case with RBD to be discussed later. In SD1, the largest AABP value is from Ser305 and Thr307 with AABP value of 0.496 e⁻. The total AABP value for each AA is the sum of NN pairs and off-diagonal AAs. It should be pointed out that both Ser305 and Arg328 have only one NN AA to the right and left respectively giving lower total AABP values. For Ser305 has total AABP value of 0.399 e⁻ + 0.079 e⁻ = 0.478 e⁻. The total AABP values for the other AAs will be twice as larger since they have have contributions from two NNs. For example, Thr307 will have a total AABP value of 0.496 e⁻ + 0.432 e⁻ + 0.079 e⁻ = 1.007 e⁻ including the contribution from the off-diagonal pairs Ser305–Thr307. A typical AA in the middle of SD1 without off-diagonal contributions such as Asn317 has a total AABP value of 0.485 e⁻ + 0.466 e⁻ = 0.951 e⁻, one from the left (Ser316) and the other from right (Phe318).

Fig. 2(c) and (d) show the details of inter-amino acid interactions between 3 AAs (Ser305, Phe306, Thr307) and four AAs (Glu309, Lys310, Gly311, Tyr313) respectively in SD1. In Fig. 2(c) the two covalent bonds are between a C in Ser305 and a N in Phe306 and a C in Phe306 and a N in Thr307 with BO values of 0.399 e⁻ and 0.432 e⁻ respectively. Specific interatomic bonds, covalent and HB, are marked with solid and dashed lines. There is only one HB between an H atom in Ser305 and an O atom in Thr307 with a BO value of 0.079 e⁻. Fig. 2(d) with four AAs have two covalent bonds and one HB.

AABP analysis of RBD

RBD is a very large biomolecule with 144 residues and a total of 2100 atoms. Structural relaxation of proteins with accuracy in atomic coordinates up to 0.01 Å is very important for realistic quantum chemical calculations.12 It is anticipated that such high precision calculations could significantly compliment the experimental work at a much reduced cost in addition to providing the fundamental understanding on various aspects of viral infection. Since RBD has 144 AAs, the data for AABP is massive, with a much larger number of off-diagonal AABP and its presentation for the 3d-connected network will be extremely challenging. The diversity of the distribution of these 144 AAs among the 20 distinct residues in RBD is shown in Fig. 3. All AAs are present except Met and they are very unevenly distributed. Tyr and Val have 13 each followed by Ser has 12. The smallest presence are Glu, Trp and His with frequencies of 3, 2, and 1 respectively. There are 5 Cys (336, 361, 379, 391, 432), less than half of the average. Cys and Met are the only AAs with S–S bonds. It turns out that Cys is quite different from other AAs in the context of the present paper with large contributions to the AABP from the off-diagonal Cys–Cys pairs due to the unique S–S bond. More details will be detailed later in this section.

Like in SD1, the bonding between different AAs consist of covalent bonds and HBs. We first surmise the gross picture of binding in RBD in Table 1. Out of 238 bonds, there are 93 HBs (39.1%), 89 are O–H bonds (95.7% of HBs) and only 4 are N–H bonds (4.3% of HBs). For the bond strength, we list the total bond order (BO) values for each bond types in Table 1. Since HBs are weaker than covalent bonds, its total bond order of 0.2297 + 2.9788 = 3.2085 is only 4.78% (3.21/66.18). This does not mean that HBs are less important in AA interactions since the data in Table 1 constitutes all possible bonds in RBD. We will return to this point later.

Fig. S1† shows the summary of the ten 36 × 36 matrices (MT) data (MT1–MT10) shown in Table S2† for RBD which lists the actual data for the AABP in the form of ten matrices covering all 144 × 144 possible inter-AA interacting pairs. It is similar to Table S1† for SD1 showing all possible interactions among NN pairs with pseudo-diagonal cells highlighted with yellow and non-local AA pairs in off-diagonal cells. The pseudo-diagonal cells represent the primary AA sequence where the AA–AA interaction are between NN pairs with AAs with residue number next to each other (see Methods section). As expected, the pseudo-diagonal cells have much larger AABP values compared to those from off-diagonal cells which constitute the AA interactions in 3d. It should be pointed out that in MT4, MT7, MT9 and MT10, the position coordinates of some AA are missing as shown in Fig. 1 (444–448, 455–490, 501–502) which results in total 36 AAs in the sequence range 443–521. These AA positions are simply eliminated in the RBD calculations (see ref. 12). The missing part in MT4, MT7, MT9 and MT10 are those marked by...
vertical black line in Fig. 1. In this way, the MTs \( (s = 4, 7, 9, 10) \) all have dimension \( 36 \times 36 \) similar to the other 6 MTs. Table S2† shows the 140 AABP values in the primary sequence with an average AABP value of 0.445 electron \( (e^-) \) ranging from 0.397 \( e^- \) (Ala372–Ser373 and Leu517–Leu518) to 0.939 \( e^- \) (Val503–Gly504). There are 75 off-diagonal AABP values with a much smaller average AABP value of 0.052 \( e^- \) ranging from 0.010 \( e^- \) (Gly416–Asp420) to 0.407 \( e^- \) for (Thr500–Tyr505).

Fig. 4(a) shows the sketch of the possible connection among the 144 AAs in the RBD as reflected by their finite AABP values listed in Table S2.† This is a very busy figure in order to show the 3d connection map in a 2d plane by connecting those AAs that are off-diagonal cells in Table S2.† The connected circles with the AA name and sequence number labeled are the primary AA sequence. This figure with a lot of details shows the true nature of the AA interaction in 3d and their nonlocal network in RBD. There are only 41 AAs (no color) or 28.5% that do not have off-diagonal AABP. Careful inspection of Fig. 4(a) shows that there are 68 AAs have 1 off-diagonal AABP (yellow), 26 AAs have 2 off-diagonal AABP (green), 7 AAs have 3 off-diagonal AABP (blue), and 2 AAs have 4 off-diagonal AABP (pink). The amino acids Cys are marked by red star to emphasize the unique Cys–Cys off-diagonal bonding.

The above analysis enables us to quantitatively designate a number characterizing the stability or binding strength for each amino acid in RBD based on the total inter-AA interactions in 3d space. It consists of two parts: (1) AABP from NN AAs in the primary sequence. (2) Contribution from off-diagonal AAs. Each of these two parts can be further divided into those formed with covalent bonds and by HBs. Such detailed analysis of inter-AAs interaction in 3d space is truly de novo and unprecedented. Moreover, they can be connected to the conservation of the amino acid sequence itself.

Table S3† lists the calculated AABP values in RBD from the inter-amino acid interaction. There are two columns: one from NN (pseudo-diagonal) AAs and the other from nearby AAs (off-diagonal). The green cells in Table S3† mark those AAs having a total AABP larger than 0.90 \( e^- \), a reasonable estimation for the high AA binding strength that controls the formation of the 3d-network. Of the 144 AAs in RBD, 60% have AABP sum higher than 0.9 \( e^- \). These data are plotted in Fig. 5 in the form of histogram bars. The three vertical dashed lines show the locations of AA with missing position coordinates. The AAs with only one NN are marked light blue (Leu335, Ser443, Tyr449, Arg454, Pro491, Thr500, Val503 and Pro521). They all have much lower total AABP values. In particular, we note that the

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**Fig. 4** (a) Distribution of AABP in RBD using the data from Table S2† (10 matrix tables). Circle with no color represents the AA with no off-diagonal AABP. Colored circles represent following AAs: yellow represents one off-diagonal AABP, green two off-diagonal AABP, blue three off-diagonal AABP, and pink four off-diagonal AABP. The colored lines are used to show multiple off-diagonal AABP. (b) and (c) are examples for chains with off-diagonal connections.
AAs that have much higher total AABP than the average are those with large contributions from the off-diagonal parts. Ostensibly, both Gly504 and Tyr505 have large total AABP values which will be discussed in more detail in the next section. Another interesting observation is that the total AABP values show some have a correlation with the absolute value of the partial charge (PC) |ΔQ*| (Fig. 2 of ref. 12). They are identified and marked with blue arrows for higher positive PC or red arrows for higher negative PC in Fig. 5. Most of these AAs have AABP values equal or higher than 0.9 e⁻. Interestingly, the five Cys mentioned earlier (marked pink in Table S3†) have large contribution from the off-diagonal contribution but they do not correlate with the PC. The blue bold color in Table S3† indicates those amino acids that have contribution from only one NN. They are either the first or last AA in the sequence, or they are next to the omitted AA with missing coordinates (Fig. 1). In other words, the contribution to the strength of AABP for these AAs should have the NN part doubled. More detailed breakdown of different types of interatomic bonding between all amino acid pairs in RBD are listed in Table S4.†

Details of amino acid interactions

We now present some selected examples vividly illustrating the intricate details on the inter-amino acid interaction that have not been revealed before. Fig. 6 shows the bonding of: (a) Gly504 with three AAs: Val503, Asp405, and Tyr505; (b) Lys386 with four AAs: Ser383, Asp389, Leu387, and Thr385; (c) Asp389 with three AAs: Val503, Asp405, and Tyr505; (d) Lys386 with four AAs: Ser383, Asp389, Leu387, and Thr385; (e) Cys336 with three AAs: Val503, Asp405, and Tyr505; (f) Lys386 with four AAs: Ser383, Asp389, Leu387, and Thr385. Details are described in the figure caption. The entire RBD has been analyzed similarly with detailed results presented in Table S4.† Moreover, we show in Fig. 7, the AABP of entire RBD on the surface. The total AABP value is displayed in different orientations in Fig. 7(a)–(c) and those from the off-diagonal component in Fig. 7(d)–(f). The AAs with higher sum AABP and off-diagonal AABP are marked. The residue Asn343 is the only AA in RBD out of the 22 N-linked glycosylation in the S protein.31 Detailed description is in the figure caption.

Off-diagonal connections of RBD

We now discuss the nonlocality of AA–AA interactions in 3d based on their quantitative values in AABP. Off-diagonal connections form chains from multiple off-diagonal AABP, each contributed from two AAs. This is sketched in Fig. 4(a) using colorful lines. They are summarized in Table S5†. Off-diagonal connections can be implicated since they involve all AAs in the long-range nonlocal interactions, and demonstrate the twists and turns in the protein which is very difficult to characterize based purely on sequence alignment. Table S5† lists the AAs involved in unique chains. The left side of table lists all AAs involved and the right side of table shows the number of AAs involved in each unique chain or the count. The lower limit of the count is 3 since the ones with 2 counts are just off-diagonal AABP shown in Fig. 4(a) (marked with yellow color). Please note that some off-diagonal connections shown in Table S5† might be connected to NN AA. One of such example is Ala344, with 9 different AAs involved in including itself which connects to its NN Thr345. Among the 144 AAs in RBD, 12.5% of AAs has 9 counts, 4.9% of AA has 7 counts, 12.5% of AAs has 6 counts, 6.9% of AAs has 5 counts, 5.6% of AAs has 4 counts, 8.3% of AAs has 3 counts, 20.8% of AAs has 2 counts (off-diagonal AABP) and 28.5% of AAs has 1 count (no off-diagonal AABP). Strangely, there is no chain with 8 counts. An interesting fact regarding Cys is that out of 5 Cys AAs present in RBD two of them Cys379 and Cys432 falls under 9-count off-diagonal connections. The other 2 Cys336 and Cys361 falls under 6-count off-diagonal connections. The remaining one Cys391 does not have any off-diagonal AABP since it is bonded with Cys525 in SD2.

AABP off-diagonal connections and conservation

AABP with its off-diagonal connections is related to conservation of AAs. In ref. 12, we attempted to connect sequence
conservation with intramolecular binding in RBD of SARS-CoV-2. In RBD the AA sequence number from 455 to 505 is considered to be the residues in the binding region in contact with ACE2 receptor.\textsuperscript{12} As described in Fig. 1, there are only 13 AAs with their position coordinates available in this area. Pro499 is one of the 13 AAs with off-diagonal connections with 7 AAs (Table S5\textsuperscript{†} and Fig. 4(b)) and serves as a simple example of branching of off-diagonal connections from Asn439. Among the 13 AAs in the ACE2 receptor binding area only 7 are considered to be conserved.\textsuperscript{12} They are Pro491, Leu492, Tyr495, Gly496, Phe497, Thr500, and Gly504. Two of them, Pro491 and Leu492 do not have any off-diagonal AABP. Four of the 7 conserved AAs each has one off-diagonal AABBP and no off-diagonal connections. They are from pairs Tyr495–Phe497, Gly496–Gln498 and Thr500–Tyr505 with off-diagonal contribution of 0.023 e\textsuperscript{−}, 0.029 e\textsuperscript{−} and 0.407 e\textsuperscript{−} respectively. The last one, Gly504 has 6 off-diagonal connections (Gly504–Asp405–Arg408–Thr376–Ala435–Ser375) (see Table S5\textsuperscript{†} and Fig. 4(c)). In addition, Gly504 has a large off-diagonal AABBP of 0.070 e\textsuperscript{−} from Asp405–Gly504 pair and the highest total AABBP sum of 1.513 e\textsuperscript{−} [see Table S3,\textsuperscript{†} and Fig. 5] among all AAs in RBD. This astonishingly high value approaches that of the pseudo-diagonal contributions in the primary sequence. It is remarkable that Gly504, which falls under conserved ACE2 receptor binding segment of RBD has the largest sum AABBP and large off-diagonal connections. All these factors point to the important role of 3d inter-amino acid bonding in sequence conservation. The NNs of Gly504 are Val503 and Tyr505 with pseudo-diagonal AABPB contributions of 0.939 e\textsuperscript{−} with AABP 0.503 e\textsuperscript{−} respectively. It turns out that both Val503 and Tyr505 have higher negative partial PC\textsuperscript{12} and marked with red arrows in Fig. 5. AAs with higher negative or positive PC are mostly the conserved ones consistent with our claim.\textsuperscript{12} We also note that Tyr505–Thr500 pair has the highest off-diagonal AABBP value of 0.407 e\textsuperscript{−}. It should be pointed out that Thr500 has only one NN with AABBP of 0.437 e\textsuperscript{−} yet their sum still has a very respectable value of 0.845 e\textsuperscript{−}. Thr500 is one of the conserved AAs in the ACE2 receptor binding area with the largest sum AABBP and a large off-diagonal AABBP. In the above, the bond order for the bonds are marked. The dashed lines represent the HB. Some of them have regular covalent O–H bond such as between Lys386 and Asp389 in (b) and (c) with bond order of 0.256 e\textsuperscript{−} and bond length of 1.030 Å.

Fig. 6  Ball and stick figures for 4 examples of inter amino acid interaction in RBD: (a) Gly504 with Asp405, Val503, and Tyr505. Gly504 has the highest total AABBP value of 1.513 e\textsuperscript{−}, which originates from exceptionally strong C–N bonds with its NN Val503 and Tyr505. The contribution of 0.070 e\textsuperscript{−} from off-diagonal bonding to Asp405 is a single O–H HB. (b) Interaction of Lys386 with Ser383, Asp389, Leu387, and Thr385. Lys386 has a large AABBP value of 1.171 e\textsuperscript{−} and the large contribution from off-diagonal part of 0.289 e\textsuperscript{−} (0.256 e\textsuperscript{−} + 0.019 e\textsuperscript{−} + 0.015 e\textsuperscript{−}). (c) Interaction of Asp389 with Lys386, Leu387, and Asn317. Asp38 has the large off-diagonal AABBP of 0.270 e\textsuperscript{−}. (d) Interaction of Cys336 with Leu335, Pro337, Phe338, Cys361 and Val362. Cys336 is bonded to another Cys (Cys361) with an S–S bond and a large off-diagonal AABBP of 0.254 e\textsuperscript{−}. An interesting observation is the relatively strong S–S bond with a BO value of 0.173 e\textsuperscript{−} between Cys336 and Cys361 that contribute to the large off-diagonal AAB. In the above, the bond order for the bonds are marked. The dashed lines represent the HB. Some of them have regular covalent O–H bond such as between Lys386 and Asp389 in (b) and (c) with bond order of 0.256 e\textsuperscript{−} and bond length of 1.030 Å.
of the 7 conserved AAs, this again supports the notion of positive correlation between conservation and AABP.

**Hinge movement in S-protein RBD**

S-protein undergoes a conformational change during infection in which RBD of S1 carries out a hinge-like movement into a receptor-binding active state. Interaction between Ser359 (located in RBD) and Pro561 (located in SD2) are the key for this conformation change according to Roy et al. From Table S5† and Fig. 4, we show that the off-diagonal connections for Ser359 falls under 5 counts (Ser359–Asn394–Glu516–Thr393–Ala520) and is linear with no branching out. Four of these AAs except Thr393 are conserved. The ball and stick figure of these five amino acids are shown in Fig. 8. In this case, all off-diagonal bonding is due to HBs. This shows the nature of most of the off-diagonal bonding in the entire RBD. HBs are one of the important factors in the interaction within the S-protein. In this regard, our method and analysis go beyond NN interaction in the primary sequence and includes the contributions from all nonlocal off-diagonal AAs, identifying their HBs. This is one level deeper in explaining the hinge movement of RBD in S-protein during viral infection. We believe that other AAs with longer 3d chains with their HBs also play key roles which are not revealed yet. Table S5† shows all unique chains and we would like to point out 2 unique chains each with 9 AAs (maximum count), may also have key function in the S-protein.

**Conclusions**

In this paper, we have accomplished the following: (1) presented a de novo method for inter-amino acid interactions based on quantitative quantum mechanical calculation of the bonding between AAs called AABP (u, v) and confirmed that the nearest neighbor AAs predominate the interactions consistent
with using primary amino acid sequence as the key descriptor used in the past theory. (2) Demonstrated quantitatively the nonlocal network structure of amino acids in 3-dimensions and its implication to the conservation of the amino acid sequence. (3) Confirmed the significant contribution of AABP with off-diagonal contributions to the sequence conservation in the receptor binding domain of the S-protein of SARS-CoV-2 virus. (4) Offered detailed site-specific analysis of intricate complex bonding processes in RBD including glycosylation and the prominent role of residue Gly504. (5) Identified the unique bonding of amino acid Cys which contains sulphur in the AABP (u, v) and its specific role in the formation of the AA network. (6) Correlated the AAs involved in the hinge movement around Ser359 with their HBs.

In summary, based on the clearly delineated steps of the proposed methodology and meticulously displayed of the data collected and discussed in various aspects of the impacts of the existence of the non-local amino acid interaction network in RBD of SARS-CoV-2 Spike protein. To the best of our knowledge, this important issue has not been touched upon, at least at the quantitative level in the research community. This new concept and method of AABP for interaction between amino acids is clearly one step beyond the simpler interatomic interactions in proteins. More importantly, the method can be readily applied to and play a crucial role in large-scale computation for protein design and understanding the mutation process leading to effective vaccine and therapeutic drug design in combating COVID-19 pandemics. This is because such urgent research topics require the information on the details of the interaction under different environments, involving a single amino acid or clusters of multiple amino acids. Some of such calculations are currently in progress and will be reported in near future.

Conflicts of interest

There are no conflicts to declare.

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