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7, 9939Layered manganese bismuth tellurides with  
GeBi<sub>4</sub>Te<sub>7</sub>- and GeBi<sub>6</sub>Te<sub>10</sub>-type structures: towards  
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The crystal structures of new layered manganese bismuth tellurides with the compositions Mn<sub>0.85(3)</sub>Bi<sub>4.10(2)</sub>Te<sub>7</sub> and Mn<sub>0.73(4)</sub>Bi<sub>6.18(2)</sub>Te<sub>10</sub> were determined by single-crystal X-ray diffraction, including the use of microfocused synchrotron radiation. These analyses reveal that the layered structures deviate from the idealized stoichiometry of the 12P-GeBi<sub>4</sub>Te<sub>7</sub> (space group  $P\bar{3}m1$ ) and 51R-GeBi<sub>6</sub>Te<sub>10</sub> (space group  $R\bar{3}m$ ) structure types they adopt. Modified compositions Mn<sub>1-x</sub>Bi<sub>4+2x/3</sub>Te<sub>7</sub> ( $x = 0.15-0.2$ ) and Mn<sub>1-x</sub>Bi<sub>6+2x/3</sub>Te<sub>10</sub> ( $x = 0.19-0.26$ ) assume cation vacancies and lead to homogenous bulk samples as confirmed by Rietveld refinements. Electron diffraction patterns exhibit no diffuse streaks that would indicate stacking disorder. The alternating quintuple-layer [M<sub>2</sub>Te<sub>3</sub>] and septuple-layer [M<sub>3</sub>Te<sub>4</sub>] slabs ( $M$  = mixed occupied by Bi and Mn) with 1:1 sequence (12P stacking) in Mn<sub>0.85</sub>Bi<sub>4.10</sub>Te<sub>7</sub> and 2:1 sequence (51R stacking) in Mn<sub>0.81</sub>Bi<sub>6.13</sub>Te<sub>10</sub> were also observed in HRTEM images. Temperature-dependent powder diffraction and differential scanning calorimetry show that the compounds are high-temperature phases, which are metastable at ambient temperature. Magnetization measurements are in accordance with a Mn<sup>II</sup> oxidation state and point at predominantly ferromagnetic coupling in both compounds. The thermoelectric figures of merit of n-type conducting Mn<sub>0.85</sub>Bi<sub>4.10</sub>Te<sub>7</sub> and Mn<sub>0.81</sub>Bi<sub>6.13</sub>Te<sub>10</sub> reach  $zT = 0.25$  at 375 °C and  $zT = 0.28$  at 325 °C, respectively. Although the compounds are metastable, compact ingots exhibit still up to 80% of the main phases after thermoelectric measurements up to 400 °C.

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## 1 Introduction

Layered chalcogenides have received much attention due to their exceptional properties. These include topologically non-trivial electronic structures, charge-density waves, superconductivity or promising thermoelectric properties.<sup>1-7</sup> For thermoelectric waste-heat recovery and Peltier cooling near room temperature (RT), the layered semiconductor Bi<sub>2</sub>Te<sub>3</sub> and its substitution variants with Sb and Se are used in technical applications.<sup>8</sup> The thermoelectric performance of Bi<sub>2</sub>Te<sub>3</sub> has been optimized *e.g.* by Se substitution and Cu doping.<sup>9</sup> In addition to its thermoelectric properties,<sup>10,11</sup> angle-resolved photoemission spectroscopy (ARPES) has proved that Bi<sub>2</sub>Se<sub>3</sub> and Bi<sub>2</sub>Te<sub>3</sub> are topological insulators.<sup>3,12-14</sup> Variants of Bi<sub>2</sub>Te<sub>3</sub> or Bi<sub>2</sub>Se<sub>3</sub> doped with transition metals such as Cr or Fe exhibit different magnetic interactions caused by the dopants; they may represent a new class of magnetic topological insulators in the field of spintronics.<sup>15,16</sup> Probably motivated by its natural abundance, Mn, has widely been used as a dopant in Bi<sub>2</sub>Te<sub>3</sub>; and structural, electrical and magnetic properties have been studied.<sup>17-22</sup> For example, thin-film topological insulators based on Mn- or Cr-doped Bi<sub>2</sub>Te<sub>3</sub> are potential candidates for highly sensitive anomalous Hall effect sensors.<sup>17,23</sup> In contrast to the

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ordinary Hall effect caused by the Lorentz force, the anomalous Hall effect arises from the spin–orbit interaction of spin-polarized charge carriers in conductive ferromagnetic materials and provides an alternative approach for magnetic sensing.

Layered  $\text{Bi}_2\text{Te}_3$  exhibits a 15R stacking sequence of three slabs per unit cell separated by van der Waals gaps (*cf.* Section 3.3, Fig. 5), each slab composed of double layers of  $[\text{BiTe}_6]$  octahedra often called “quintuple layer” as it consists of five atom layers. Many compounds can be derived from  $\text{Bi}_2\text{Te}_3$  by formally inserting  $Tt\text{Te}$  ( $Tt = \text{Pb}, \text{Ge}, \text{Sn}$ ) units.<sup>24</sup> In addition to its thermoelectric behavior,  $\text{SnBi}_2\text{Te}_4$  shows a pressure-induced electronic topological transition between 3.5 and 5.0 GPa.<sup>25</sup> ARPES yields evidence for topological surface states with Dirac dispersion in the indirect bandgap of bulk  $\text{Pb}(\text{Bi}_{1-x}\text{Sb}_x)\text{Te}_4$ .<sup>26</sup> The  $\text{GeBi}_2\text{Te}_4$ -type structure of these compounds is described by a 21R stacking sequence, whose “septuple” layers comprise three triple layers of condensed octahedra as described by  ${}^2_\infty[\text{Te}_{3/3}M(\mu\text{-Te}_{3/6})M(\mu\text{-Te}_{3/6})M\text{Te}_{3/3}]$  ( $M = \text{Ge}, \text{Bi}$ ; usually disordered), again separated by van der Waals gaps.<sup>27,28</sup> Formally adding one  $\text{Bi}_2\text{Te}_3$ -type quintuple layer per  $\text{GeBi}_2\text{Te}_4$ -type septuple building block results in the  $\text{GeBi}_4\text{Te}_7$  structure type with a 12P stacking sequence.<sup>27,29</sup> Insertion of a second  $\text{Bi}_2\text{Te}_3$ -type layer results in the  $\text{GeBi}_6\text{Te}_{10}$  structure type, described by a 51R stacking sequence. From another point of view, these structures can be understood as consisting of distorted rocksalt-type slabs similar to those in  $\text{GeBi}_2\text{Te}_4$  and in  $\text{Bi}_2\text{Te}_3$ , separated by van der Waals gaps.<sup>24</sup> Mn doping and its influence on the thermoelectric properties was also reported for the layered compound  $\text{Ge}_4\text{Sb}_2\text{Te}_7$  crystallizing with a  $\text{Ge}_3\text{As}_2\text{Te}_6$ -type structure.<sup>30</sup>  $\text{MnBi}_2\text{Te}_4$  has been reported to be the first compound of the series  $M\text{Te}(\text{Bi}_2\text{Te}_3)_n$  where  $M$  is a transition metal represented by manganese.<sup>31</sup> Single-crystal data of  $\text{MnBi}_2\text{Te}_4$  revealed Mn/Bi antisite disorder; the magnetic properties are strongly anisotropic and antiferromagnetic ordering is observed below 24 K.<sup>32,33</sup> Investigations on the tentative phase diagram of the system Mn/Bi/Te indicated that there are further layered compounds in that system,<sup>34</sup> and estimates concerning their structures were suggested based on the interpretation of multi-phase powder diffraction patterns. In heterostructured  $\text{Bi}_2\text{Se}_3/\text{MnBi}_2\text{Se}_4$  thin films, which were grown by means of molecular beam epitaxy,  $\text{MnBi}_2\text{Se}_4$  crystallizes in the same structure type as bulk  $\text{MnBi}_2\text{Te}_4$ .<sup>35</sup> We have now synthesized further members of the homologous series  $(\text{MnTe})(\text{Bi}_2\text{Te}_3)_n$  with  $\text{GeBi}_4\text{Te}_7$ -type<sup>27,29</sup> or  $\text{GeBi}_6\text{Te}_{10}$ -type<sup>24</sup> structures. According to single-crystal X-ray data, single-phase syntheses and chemical analyses, their chemical compositions significantly deviate from the idealized formulae given in ref. 34. However, our substances might be the same or rather similar compounds as the ones discussed in this parallel work even though the authors claim that they are stable, whereas our samples are metastable as discussed below (in addition, DSC curves in ref. 34 are different from ours; and as the authors did not obtain single-phase samples and do not show chemical analyses, a detailed comparison is impossible). Measurements of transport properties with respect to thermoelectric behavior represent one step towards characterizing these potential multifunctional materials.

## 2 Experimental

### 2.1 Synthesis

Bulk samples were obtained from the elements Mn (chunks, Onyxmet, 99.9%), Bi (Alfa Aesar, 99.999%) and Te ingots (Haines & Maassen, 99.9%). Mn was heated under vacuum with small silica glass powder at 1000 °C for 1 day to completely remove brownish  $\text{MnO}_2$  from the surface. After this cleaning procedure, Mn was stored under argon to avoid oxidation. Stoichiometric mixtures (approximately 2 g) of the elements according to the various sum formulae mentioned in the following sections were sealed in graphitized flat-bottomed silica glass ampules (inner diameter: 12 mm, wall thickness: 1.5 mm) under argon atmosphere, placed in tube furnaces and heated from RT to 950 °C. The samples were kept at these conditions for 1 d and subsequently cooled to RT by quenching at air. The resulting ingots were then annealed at 575 °C for 1 week, again followed by quenching at air. Disc-shaped ingots used for thermal conductivity measurements were obtained by using flat-bottomed silica-glass ampules. The samples were polished to a plane-parallel thickness of 1.07 mm ( $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ ) or 1.29 mm ( $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$ ), by using SiC grinding powder. Cuboid-shaped samples for measurements of the electrical conductivity and the Seebeck coefficient were fabricated using a diamond wire saw and polished with SiC grinding powder. The samples are dark gray with metallic luster. Upon exposure to air over months, no hydrolysis, oxidation or decomposition were observed, even for powder samples.

### 2.2 Powder diffraction

For powder X-ray diffraction (PXRD) at RT, the samples were crushed and spread on Mylar foil. Data were recorded on a Huber G670 diffractometer (Guinier geometry with imaging-plate detector and integrated read-out system) using  $\text{Cu-}K_{\alpha 1}$  radiation [ $\text{Ge}(111)$  monochromator,  $\lambda = 1.54051 \text{ \AA}$ ]. WINXPOW<sup>36</sup> was used for data evaluation and TOPAS<sup>37</sup> for Rietveld refinements. Reflection profiles were described with fundamental parameters using a direct convolution approach. Crystallite strain was described using a Voigt function, and preferred orientation was refined with spherical harmonics of the 4th order. The background of each diffraction pattern was modelled by a set of 18 parameters (shifted Chebyshev polynomial). Structure models with their equivalent isotropic displacement parameters were taken from the single-crystal data. Temperature-dependent measurements in rotating silica glass capillaries under dry Ar atmosphere were obtained with synchrotron radiation (beamline ID11, ESRF, Grenoble) on a Huber diffractometer ( $\lambda = 0.18972 \text{ \AA}$ ) with a FReLoN 2K CCD detector.<sup>44</sup> A hot-gas blower (GSB 1300, FMB Oxford) with a maximal heating rate of 20 K  $\text{min}^{-1}$  was used. For temperature calibration, hexagonal BN was used since its  $c$  lattice parameter increases with temperature almost linearly.<sup>38</sup> In order to adjust the measured temperatures of the heating and cooling curves according to the calibration, a second-order polynomial fit was used for interpolation.

### 2.3 Single-crystal X-ray diffraction

X-ray diffraction data of a  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  single-crystal were obtained on a STOE STADIVARI diffractometer ( $\text{Ag-}K_{\alpha 1}$  radiation,



$\lambda = 0.56086 \text{ \AA}$ ) with a Dectris Pilatus 300k detector. Integration was done with X-Area<sup>39</sup> and numerical absorption correction using X-RED<sup>40</sup> and X-SHAPE.<sup>41,42</sup> Single-crystal diffraction data of  $\text{Mn}_{0.73}\text{Bi}_{6.18}\text{Te}_{10}$  were obtained using microfocused synchrotron radiation (beamline ID11, ESRF, Grenoble)<sup>43</sup> on a Huber diffractometer ( $\lambda = 0.30996 \text{ \AA}$ ) with a FReLoN 2K CCD detector.<sup>44</sup> Integration was done using CrysAlis Pro<sup>45</sup> and semiempirical absorption correction was applied with SADABS.<sup>46</sup> Incomplete absorption in the CCD phosphor as a function of beam incidence was taken into account.<sup>47</sup> Solution and refinement of both structures was done with SHELX-2014.<sup>48</sup> Further details on the crystal structure analyses can be obtained from the Fachinformationszentrum Karlsruhe, 76344 Eggenstein-Leopoldshafen, Germany (fax: +49-7247-808-666; e-mail: crysdata@fiz-karlsruhe.de) on quoting the depository numbers 1891486 ( $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$ ) and 1891488 ( $\text{Mn}_{0.73}\text{Bi}_{6.18}\text{Te}_{10}$ ). Crystal structures were visualized with Diamond.<sup>49</sup>

## 2.4 Thermal analysis

$\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  powders were analyzed by means of differential scanning calorimetry (DSC) using a Setaram Labsys ATD-DSC device with k-probe (Ni-Cr/Ni-Al;  $T_{\text{max}} = 800 \text{ }^\circ\text{C}$ ) thermocouples and  $\text{Al}_2\text{O}_3$  as a reference compound. Weighted amounts of each specimen (*ca.* 50 mg) were sealed in small evacuated silica ampules and exposed to two consecutive heating and cooling cycles from RT up to  $800 \text{ }^\circ\text{C}$  at the rate of  $2 \text{ K min}^{-1}$ .

## 2.5 Electron microscopy

Scanning electron microscopy (SEM) and energy-dispersive X-ray spectroscopy (EDX) were done using a Zeiss LEO 1530 instrument (acceleration voltage 20 kV) equipped with an EDX detector (INCA software,<sup>50</sup> Oxford Instruments). Selected-area electron diffraction (SAED), high-resolution transmission electron microscopy (HRTEM) and further EDX were executed on a Philips CM-200 STEM (LaB<sub>6</sub> cathode, 200 kV, super-twin lens, point resolution 0.23 nm) equipped with RTEM 136-5 EDX detector (EDAX, Genesis software<sup>51</sup>). A double-tilt low-background sample holder (Gatan) was used. For TEM investigations, the bulk material was manually cut with a diamond saw, glued on a copper ring, mechanically ground to a thickness of approximately 30  $\mu\text{m}$ , polished using a dimple grinder (Gatan) and finally Ar-ion-thinned (Duo-Mill, Gatan). Evaluation of SAED data was done using the ANALYSIS software.<sup>52</sup> For HRTEM and SAED simulations, jEMS<sup>53</sup> was used. Micrographs and diffraction patterns were evaluated using Digital Micrograph.<sup>54</sup>

## 2.6 Thermoelectric characterization

Thermal diffusivity ( $\kappa$ ) was measured under He atmosphere using a Linseis LFA1000 apparatus equipped with an InSb detector (aperture diameter 3 mm). Simultaneous heat loss and finite pulse corrections were applied using Dusza's model.<sup>55</sup> Values were averaged from five measurement points at each temperature. For  $\kappa$  calculation, they were multiplied with the Dulong-Petit heat capacity ( $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$ :  $C_p = 0.1659 \text{ J g}^{-1} \text{ K}^{-1}$ ;  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ :  $C_p = 0.1624 \text{ J g}^{-1} \text{ K}^{-1}$ ) and the density as derived by the weight and the volume determined by Archimedes'

principle with a precision of  $0.03 \text{ g cm}^{-3}$  ( $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$ :  $7.53 \text{ g cm}^{-3}$ ;  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ :  $7.65 \text{ g cm}^{-3}$ ). Densities were at least 98.5% of the corresponding X-ray densities. DSC measurements (*cf.* Fig. S1 – S denotes items in the ESI†) confirm that  $C_p$  corresponds to the Dulong-Petit value within experimental error although DSC measurements of  $\text{Bi}_2\text{Te}_3$ <sup>56</sup> indicate that  $C_p$  near RT is still below the Dulong-Petit value. However, other related compounds such as  $(\text{Sn}_{1-x}\text{Pb}_x)\text{Bi}_2\text{Te}_3$ <sup>57</sup> or  $\text{GeBi}_4\text{Te}_7$ <sup>58</sup> reach this value near RT. The Seebeck coefficient  $S$  (in  $\mu\text{V K}^{-1}$ ) and the electrical conductivity  $\sigma$  (in  $\text{S cm}^{-1}$ ) were measured on cuboid samples ( $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$ :  $8.13 \text{ mm} \times 1.25 \text{ mm} \times 1.76 \text{ mm}$ ,  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ :  $6.92 \text{ mm} \times 1.09 \text{ mm} \times 1.91 \text{ mm}$ ) simultaneously under He atmosphere using a Linseis LSR-3 instrument with NiCr/Ni and Ni contacts and a continuous reversal of the polarity of the thermocouples (bipolar setup). Measurements comprised three heating/cooling cycles  $50\text{--}400\text{--}50 \text{ }^\circ\text{C}$  with  $25 \text{ }^\circ\text{C}$  steps at  $10 \text{ K min}^{-1}$  heating rate and three data points per temperature. The errors of  $S$  and  $\sigma$  are smaller than 10%; for  $\kappa$ , they are *ca.* 5%. The combined uncertainty may amount to  $\sim 15\%$  for the  $zT$  value.

## 2.7 Magnetic measurements

Temperature- and field-dependent magnetic measurements were performed on pressed powder samples (*ca.* 10 mg) using a Superconducting Quantum Interference Device (SQUID) magnetometer (MPMS<sup>®</sup>3) from Quantum Design. Temperature-dependent zero-field-cooled (ZFC) and field-cooled (FC) warming magnetization measurements were performed at magnetic fields of 0.02 T and 1 T in the temperature range from 2–320 K and field-dependent magnetization measurements were done at 2 K and at 300 K.

# 3 Results and discussion

## 3.1 Phase composition and homogeneity

Compounds with nominal compositions  $\text{MnTe}(\text{Bi}_2\text{Te}_3)_n$  with  $n = 2$  or 3 may be expected to crystallize in the  $\text{GeBi}_4\text{Te}_7$ <sup>27,29</sup> or  $\text{GeBi}_6\text{Te}_{10}$ <sup>24</sup> structure types. Corresponding reactions, however, did not lead to single-phase samples. Samples with the nominal composition  $\text{MnBi}_4\text{Te}_7$  contain two phases, *i.e.* a mixture of  $\text{GeSb}_2\text{Te}_4$ -type and  $\text{GeBi}_4\text{Te}_7$ -type compounds (Fig. S2, ESI†). The nominal composition  $\text{MnBi}_6\text{Te}_{10}$  yields a mixture  $\text{GeBi}_4\text{Te}_7$ -type and  $\text{GeBi}_6\text{Te}_{10}$ -type phases (Fig. S3, ESI†). In contrast, nominal compositions such as  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  (derived from single-crystal data, *cf.* Section 3.3) and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  (which was suggested by preliminary single-crystal data) lead to samples that appear to be single-phase according to Rietveld refinements based on PXRD data (Fig. 1 and Tables S1–S3 in the ESI†). In both cases, the refined parameters of the single-crystal structure analyses were used for the Rietveld refinement and only lattice parameters were refined. For  $\text{GeBi}_6\text{Te}_{10}$ -type samples, they agreed with those of the single-crystal. For  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$ , lattice parameters from PXRD differ slightly from those of the single crystal but correspond to those of the  $\text{GeBi}_4\text{Te}_7$ -type phase in heterogeneous samples with the nominal composition  $\text{MnBi}_6\text{Te}_{10}$ , from which the single crystal was isolated (Table S4, ESI†). The deviations from the stoichiometric compositions  $\text{GeBi}_4\text{Te}_7$  and





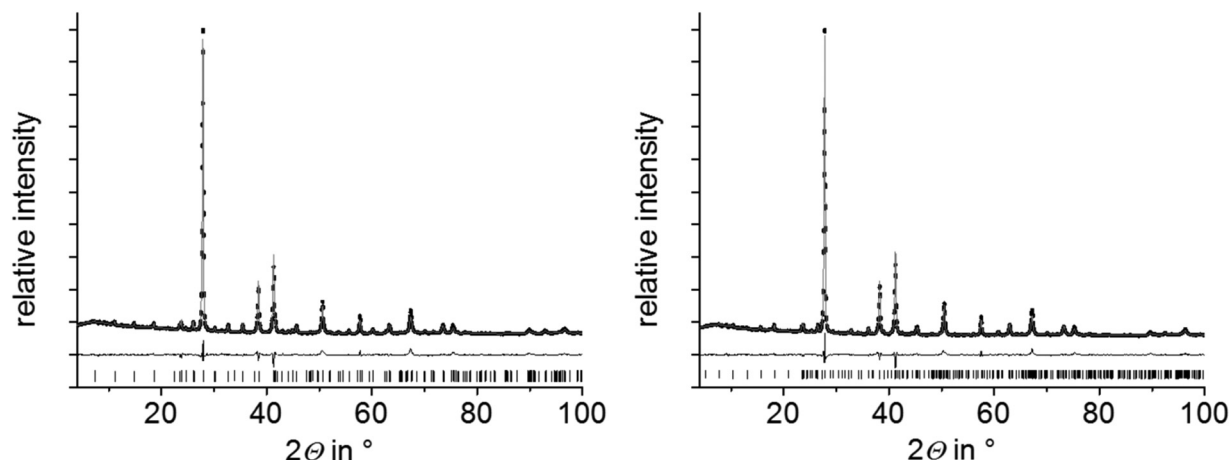


Fig. 1 PXRD patterns of  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  (left) and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  (right); Rietveld refinements taking into account structure models based on SCXRD refinements (Section 3.3) for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  ( $\text{GeBi}_4\text{Te}_7$ -type structure),  $\text{Mn}_{0.73}\text{Bi}_{6.18}\text{Te}_{10}$  ( $\text{GeBi}_6\text{Te}_{10}$ -type structure, the slightly different Mn content has no influence on the Rietveld refinement); experimental data (black points), fitted curves (gray) and difference plots (black, below); reflection markers correspond to the  $\text{GeBi}_4\text{Te}_7$  structure type (left) and the  $\text{GeBi}_6\text{Te}_{10}$  structure type (right), respectively.

$\text{GeBi}_6\text{Te}_{10}$  are consistent with the EDX data obtained from  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  bulk samples (Table S5, ESI†). The measured Mn concentrations match the nominal compositions significantly better than those expected for stoichiometric  $\text{MnBi}_4\text{Te}_7$  and  $\text{MnBi}_6\text{Te}_{10}$ . Very small amounts of a manganese telluride side phase were detected in the bulk sample  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  by SEM-EDX; in  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ , however, appeared to be phase-pure (Fig. S4, ESI†). Note that nominal compositions  $\text{Mn}_{0.92}\text{Bi}_{4.08}\text{Te}_7$  and  $\text{Mn}_{0.85}\text{Bi}_{6.15}\text{Te}_{10}$  derived from refinements not assuming charge neutrality (Section 3.3) but full occupation of all Wyckoff positions yield no single phases according to Rietveld refinements, at least not with the synthesis route described above (Fig. S5, ESI†).

The composition has been varied in order to check whether the compounds form solid solutions. Charge neutrality assuming  $\text{Mn}^{\text{II}}$ ,  $\text{Bi}^{\text{III}}$ ,  $\text{Te}^{-\text{II}}$  and cation vacancies was taken into account as these compounds exhibit small bandgaps (Section 3.6). The composition can be varied in the range of  $x = 0.15\text{--}0.20$  for  $\text{Mn}_{1-x}\square_{x/3}\text{Bi}_{4+2x/3}\text{Te}_7$  and in the range of  $x = 0.19\text{--}0.26$  for  $\text{Mn}_{1-x}\square_{x/3}\text{Bi}_{6+2x/3}\text{Te}_{10}$ . The homogeneity of the corresponding bulk samples has been confirmed by Rietveld refinements and EDX measurements (see Fig. S6 and Table S6, ESI†). Lattice parameters do not change significantly (Tables S4 and S7, ESI†). This might be due to vacancies compensating the effect of different atom radii.

### 3.2 Stability of manganese bismuth tellurides with $\text{GeBi}_4\text{Te}_7$ or $\text{GeBi}_6\text{Te}_{10}$ structure type as a function of particle size

Annealing at 585 °C and subsequent quenching affords phase-pure samples of  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  with  $\text{GeBi}_4\text{Te}_7$ -type structure and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  with  $\text{GeBi}_6\text{Te}_{10}$ -type structure according to PXRD patterns. Temperature-programmed PXRD data show no changes except thermal expansion up to ca. 210 °C (Fig. 2). At this temperature, both compounds start decomposing into phases with  $\text{Bi}_2\text{Te}_3$  structure type and a Mn-rich phase as visible in samples after thermoelectric measurements (Section 3.6, Fig. S7, ESI†).

The decomposition of fine powdered samples is complete at 270 °C for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and at 295 °C for  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ . Fig. 2 shows the disappearance of characteristic low-angle reflections of the long-periodic structures and the emergence of typical reflections of the  $\text{Bi}_2\text{Te}_3$  structure type upon decomposition (Fig. S8, ESI†). Temperature-programmed PXRD data of  $\text{MnBi}_2\text{Te}_4$  show similar decomposition.<sup>31,32</sup> Ref. 34 does not

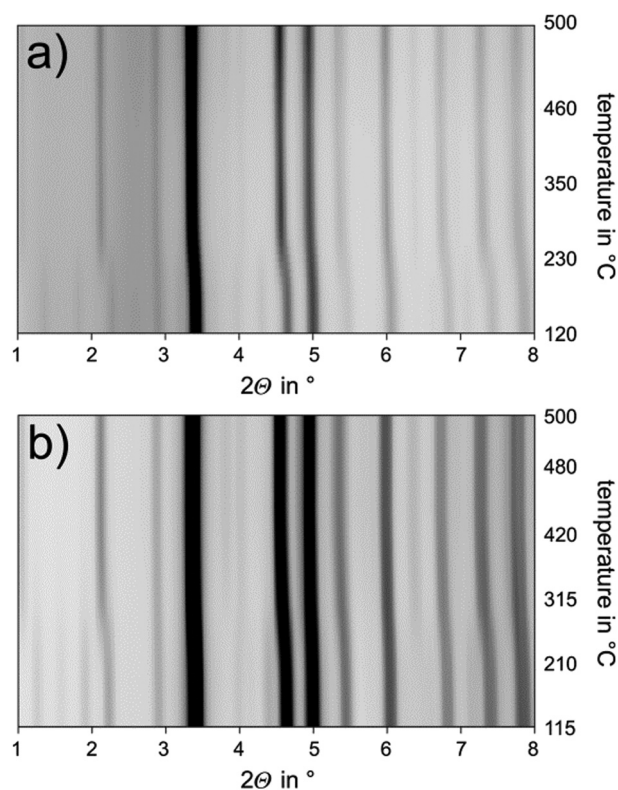


Fig. 2 Temperature-programmed PXRD starting from phase-pure samples with the compositions (a)  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and (b)  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ , synchrotron radiation ( $\lambda = 0.18972$  Å), heating rate 20 K min<sup>-1</sup>.

report this decomposition as temperature-dependent PXRD was not used but is crucial to detect the metastability. In addition, the decomposition of bulk samples is much slower as discussed later in this chapter. As this decomposition extends over a wide temperature range, it cannot be detected in DSC measurements (Fig. 3 and 4), which has been discussed in detail for  $\text{MnBi}_2\text{Te}_4$ .<sup>32</sup> However, there are characteristic DSC signals for other effects, whose tentative assignment is listed for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  in Table S8 and Fig. S9 (ESI†) and for  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  in Table S9 and Fig. S10 (ESI†). Upon heating of  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$ ,

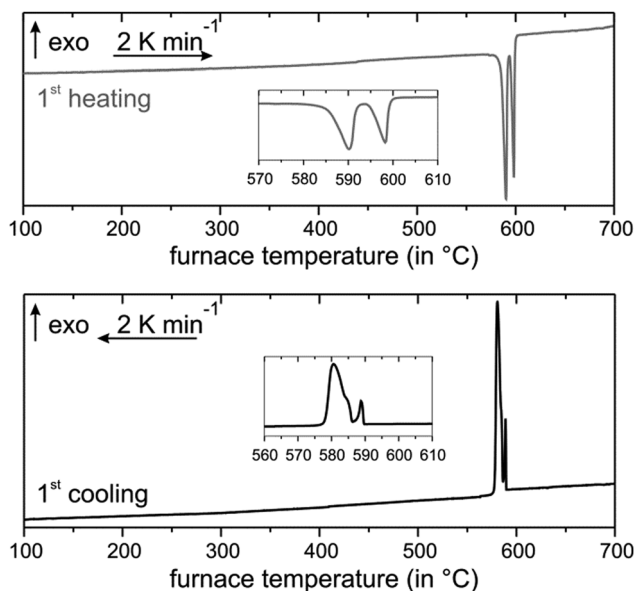


Fig. 3 DSC of  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$ : first heating (top) and cooling (bottom) curves.

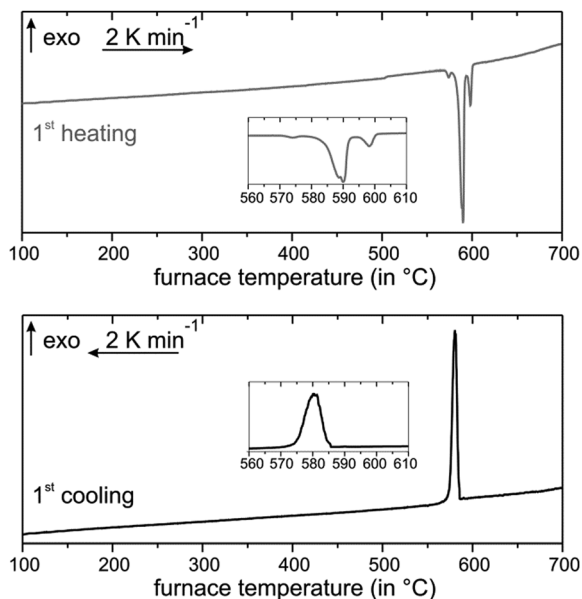


Fig. 4 DSC of  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ : first heating (top) and cooling (bottom) curves.

two endothermic signals are observed (Fig. 3). We attribute the first signal to the melting of  $\text{Bi}_2\text{Te}_3$  (a shoulder on the low-temperature side of the first signal) and of  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$ , since the starting material was partially decomposed (Fig. S11, ESI†). It is followed by the melting of another compound, possibly  $\text{MnBi}_2\text{Te}_4$ , whose slow exothermic formation is unlikely to be detected.<sup>32,33</sup> The first cooling curve shows three exothermic signals, which can be assigned to the solidification of  $\text{Bi}_2\text{Te}_3$ ,  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $\text{MnBi}_2\text{Te}_4$ , respectively, as tentatively confirmed by PXRD (Fig. S12, ESI†). The second heating cycle is similar.

The DSC curve upon heating of  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  shows four endothermic signals (Fig. 4). The first one might indicate small amounts of a Bi-rich bismuth telluride, which could form next to  $\text{MnTe}_2$  by redox decomposition (compare Fig. S13, ESI†). In analogy with the above interpretation for the  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  sample, the following signals probably correspond to the almost simultaneous melting of  $\text{Bi}_2\text{Te}_3$  and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ , then of  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$ , and of  $\text{MnBi}_2\text{Te}_4$ . The cooling curve hosts a broad unstructured signal that may indicate glassy behavior or partial crystallization of disordered compounds (Fig. 4). We speculate that just above the melting point of  $\text{Bi}_2\text{Te}_3$ , the Mn-containing ternaries undergo a series of step-wise structure transformations. The DSC experiment was probably too fast to resolve these transitions. PXRD after the DSC measurement indicates a  $\text{Bi}_2\text{Te}_3$ -type structure mixed with  $\text{GeBi}_4\text{Te}_7$ - and  $\text{GeBi}_6\text{Te}_{10}$ - and possibly  $\text{GeBi}_2\text{Te}_4$ -type structures (Fig. S14, ESI†). The second DSC heating cycle is similar but shows fewer signals during heating (Table S9 and Fig. S10, ESI†).

Due to these complex phase relationships, manganese bismuth tellurides with  $\text{GeBi}_4\text{Te}_7$ -type or  $\text{GeBi}_6\text{Te}_{10}$ -type structure cannot be obtained by quenching or slowly cooling the melt. Annealing in the existence range of the compounds is essential. As they constitute high-temperature phases that decompose at lower temperatures, quenching after the annealing step is beneficial.

However, *ex situ* SEM images and EDX measurements after three heating cycles up to 400 °C, which were performed for thermoelectric characterization (Section 3.6), show that the decomposition is much slower in compact ingots; the samples still consist mainly of the initial phase (Fig. S15 and Table S10, ESI†). Corresponding Rietveld refinements reveal *ca.* 80% of the main phase along with possibly Mn-doped  $\text{Bi}_2\text{Te}_3$ <sup>59</sup> (space group  $R\bar{3}m$ ) and  $\text{MnTe}_2$ <sup>60</sup> with pyrite-type structure (space group  $Pa\bar{3}$ ) (Fig. S7, ESI†). Thus, the metastability with respect to decomposition is best shown using very fine powders.

As mentioned above, this metastability was also observed for  $\text{MnBi}_2\text{Te}_4$ , where the decomposition products should be non-stoichiometric Bi-rich bismuth tellurides<sup>61–63</sup> “ $\text{Bi}_2\text{Te}_{3-x}$ ” and  $\text{MnTe}_{2-y}$ .<sup>31,32</sup> According to temperature-programmed PXRD,  $\text{GeBi}_4\text{Te}_7$ - and  $\text{GeBi}_6\text{Te}_{10}$ -type compounds are not formed from decomposed samples during cooling (Fig. S16 and S17, ESI†). This could mean that the reaction is too slow at 500 °C and below, or that the decomposition products are spatially segregated, resulting in strongly inhibited solid-state reactivity. A possible reason for the increased stability of the bulk material compared to the finely ground samples could be that the



metastable compounds decompose faster after many defects were brought into the crystal structure by crushing and that stresses in compact samples may hinder decomposition.

In order to exclude alternative explanations such as reactions with the silica-glass capillary or impurities, crushed samples of  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  and  $\text{Mn}_{0.85}\text{Bi}_{4.15}\text{Te}_7$  were annealed in silica-glass ampules at 300 °C for 1 day, so that most of the single phases decomposed to a Bi-rich  $\text{Bi}_2\text{Te}_3$ -like phase and  $\text{MnTe}_2$  (pyrite type,  $Pa\bar{3}$ ) (Fig. S18, ESI†). After this treatment, the samples were used as starting material for our synthesis route, *i.e.* they were melted again, followed by annealing and quenching. This again leads to phase-pure samples according to PXRD (Fig. S19, ESI†).

### 3.3 Crystal structures of $\text{Mn}_{0.85(3)}\text{Bi}_{4.10(2)}\text{Te}_7$ and $\text{Mn}_{0.73(4)}\text{Bi}_{6.18(2)}\text{Te}_{10}$

The crystal structures of representative crystals of manganese bismuth tellurides with  $\text{GeBi}_4\text{Te}_7$ -type and  $\text{GeBi}_6\text{Te}_{10}$ -type structures were elucidated from X-ray diffraction data. In the structure refinements, charge neutrality was used as a constraint assuming oxidation states of II for Mn and III for Bi. The presence of  $\text{Mn}^{\text{II}}$  is also in accordance with the magnetization measurements, *i.e.*, the effective moment  $\mu_{\text{eff}}$  is in agreement with the value expected for  $\text{Mn}^{\text{II}}$  for both compounds (*cf.* Section 3.5). Furthermore, other oxidation states seem unlikely as the oxidation potential of Te is not expected to enable higher oxidation states of the cations. Lower oxidation states of Bi are typically characterized by homoatomic bonds.<sup>64</sup> In the related compound  $\text{MnBi}_2\text{Te}_4$ , the exclusive presence of  $\text{Mn}^{2+}$  was shown by X-ray absorption spectroscopy and confirmed by magnetic susceptibility measurements.<sup>32,33</sup> Mixed occupancies of Mn and Bi on all cation sites were refined as indicated by the scattering density present and the resulting *R*-values. Cation vacancies were assumed to be located only on the Wyckoff positions *1b* for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and *3a* for  $\text{Mn}_{0.73}\text{Bi}_{6.18}\text{Te}_{10}$ , which represent the center of the  $\text{GeBi}_2\text{Te}_4$ -type building blocks,

since vacancies close to the van der Waals gaps are very unfavorable due to a resulting very low coordination number 2 for Te atoms at the van der Waals gap.

**$\text{Mn}_{0.85(3)}\text{Bi}_{4.10(2)}\text{Te}_7$ .** Crystallographic data and details of the structure refinement for a crystal with the refined composition  $\text{Mn}_{0.85(3)}\text{Bi}_{4.10(2)}\text{Te}_7$  isolated from a heterogeneous sample with the nominal composition  $\text{MnBi}_6\text{Te}_{10}$  are listed in Table 1, atomic positions and displacement parameters are given in Table 2. In contrast to Mn/Bi intermixing on the cation sites, the vacancy concentration of 5.1(17)% on the *1b* site seems not very significant; the assumption of an idealized composition  $\text{MnBi}_4\text{Te}_7$  results in almost the same residuals ( $R_1 = 0.0332$  for  $I > 2\sigma(I)$ ). However, such an idealized composition yields no single-phase samples (*cf.* Section 3.1). The EDX analysis of the investigated crystal (Fig. S20, ESI†) yields the composition  $\text{Mn}_{5.8(5)}\text{Bi}_{35.9(5)}\text{Te}_{58.3(3)}$ , which confirms a deficiency of Mn in good agreement with the nominal composition of  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7 = \text{Mn}_{7.1}\text{Bi}_{34.3}\text{Te}_{58.6}$  (Table S11, ESI†).

A refinement without assuming charge neutrality but full site occupancies (*i.e.*, no vacancies) also results in similar *R*-values and a composition  $\text{Mn}_{0.92}\text{Bi}_{4.08}\text{Te}_7$ ; however, corresponding reactions also yield no single-phase products (*cf.* Section 3.1).  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  crystallizes in the space group  $P\bar{3}m1$  and can be described by a  $12P$  stacking sequence with two different building blocks (Fig. 5b): double layers of edge-sharing  $[\text{BiTe}_{3/3}\text{Te}_{3/6}]$  octahedra similar to those in  $\text{Bi}_2\text{Te}_3$ <sup>24</sup> (Fig. 5d) and  $\text{GeBi}_2\text{Te}_4$ -type (Fig. 5c) septuple layers of condensed octahedra described by  ${}^2_{\infty}[\text{Te}_{3/3}\text{M}(\mu\text{-Te}_{3/6})\text{M}(\mu\text{-Te}_{3/6})\text{MTe}_{3/3}]$ . The atomic interaction within each layer is much stronger than the interlayer van-der-Waals-like bonding. Similar lattice parameters were reported for Mn-doped  $\text{BiTe}$  (space group  $P\bar{3}m1$ ;  $a = 4.3783(1)$  Å,  $c = 23.8107(8)$  Å),<sup>65</sup> whose  $\text{BiSe}$ -type structure consists of  $\text{Bi}_2\text{Te}_3$ -like layers separated by double layers of Bi atoms resembling those in elemental Bi. However, such a structure model cannot reproduce our diffraction data.

**Table 1** Crystallographic data for the single-crystal structure determination of  $\text{Mn}_{0.85(3)}\text{Bi}_{4.10(2)}\text{Te}_7$  with  $\text{GeBi}_4\text{Te}_7$ -type structure and  $\text{Mn}_{0.73(4)}\text{Bi}_{6.18(2)}\text{Te}_{10}$  with  $\text{GeBi}_6\text{Te}_{10}$ -type structure

Chemical formula	$\text{Mn}_{0.85(3)}\square_{0.05(2)}\text{Bi}_{4.10(2)}\text{Te}_7$	$\text{Mn}_{0.73(4)}\square_{0.09(2)}\text{Bi}_{6.18(2)}\text{Te}_{10}$
<i>M</i> (in g mol <sup>−1</sup> )	1796.72	2608.1
<i>F</i> (000)	726	3154
Crystal system/space group	Trigonal/ $P\bar{3}m1$ (no. 164)	Trigonal/ $R\bar{3}m$ (no. 166)
Lattice parameters (in Å)	$a = 4.3591(3)$ , $c = 23.769(2)$	$a = 4.3698(3)$ , $c = 101.829(8)$
<i>V</i> (in Å <sup>3</sup> )	391.41(6)	1683.9(3)
<i>Z</i>	1	3
$\rho$ (in g cm <sup>−3</sup> )	7.63	7.72
$\mu$ (in mm <sup>−1</sup> )	32.26	13.45
Absorption correction	Numerical	Semiempirical <sup>46</sup>
Radiation	Ag- <i>K</i> <sub>α</sub> , $\lambda = 0.56086$ Å	Synchrotron, $\lambda = 0.30996$ Å
Independent reflections	594	723
<i>d</i> <sub>min</sub> (in Å)	0.68	0.72
Refined parameter/restraints	27/3	36/4
$\theta_{\text{min}}/\theta_{\text{max}}$ (in °)	2.03/24.30	1.83/12.43
Extinction coefficient	—	0.0045(3)
<i>R</i> <sub>σ</sub> / <i>R</i> <sub>int</sub>	0.0322/0.0649	0.0549/0.0706
<i>R</i> indices [ $I > 2\sigma(I)$ ]	$R_1 = 0.0331$ , $wR_2 = 0.0874$	$R_1 = 0.0303$ , $wR_2 = 0.0703$
<i>R</i> indices (all data)	$R_1 = 0.0357$ , $wR_2 = 0.0895$	$R_1 = 0.0312$ , $wR_2 = 0.0712$
GoF (all)	1.08	1.20
$\Delta\rho_{\text{min}}/\Delta\rho_{\text{max}}$ (in e Å <sup>−3</sup> )	−1.52/1.53	−3.19/2.10



**Table 2** Wyckoff positions, atomic coordinates, site occupancies and coefficients of the anisotropic as well as equivalent isotropic displacement parameters (in Å<sup>2</sup>) of Mn<sub>0.85</sub>Bi<sub>4.10</sub>Te<sub>7</sub> ( $U_{eq} = 1/3[(U_{11} + U_{22} + U_{33})]$ )

Atom	W. p.	x	y	z	Occ.
Mn1/Bi1/□	1b	0	0	1/2	0.694(11)/0.255(6)/0.051(17)
Mn2/Bi2	2d	1/3	2/3	0.3423	0.0414(4)/0.959(3)
Mn3/Bi3	2d	1/3	2/3	0.0860	0.035(3)/0.965(3)
Te1	2d	1/3	2/3	0.5680	1
Te2	2c	0	0	0.2703	1
Te3	2d	1/3	2/3	0.8413	1
Te4	1a	0	0	0	1

Atom	$U_{11} = U_{22} = 2U_{12}$	$U_{33}$	$U_{23} = U_{13}$	$U_{eq}$
Mn1/Bi1/□	0.0334(7)	0.0314(10)	0	0.0328(6)
Mn2/Bi2	0.0315(2)	0.0368(4)	0	0.0333(2)
Mn3/Bi3	0.0300(3)	0.0352(3)	0	0.0318(2)
Te1	0.0336(3)	0.0291(5)	0	0.0321(3)
Te2	0.0295(3)	0.0315(5)	0	0.0302(3)
Te3	0.0290(3)	0.0308(5)	0	0.0296(3)
Te4	0.0269(4)	0.0269(6)	0	0.0269(3)

**Mn<sub>0.73(4)</sub>Bi<sub>6.18(2)</sub>Te<sub>10</sub>.** Crystallographic data and details of the structure refinement for a crystal with the refined composition Mn<sub>0.73(4)</sub>Bi<sub>6.18(2)</sub>Te<sub>10</sub> isolated from a heterogeneous sample with the nominal composition MnBi<sub>6</sub>Te<sub>10</sub> are given in Table 1; atomic positions and displacement parameters are listed in Table 3. Based on the above mentioned constraints, the refinement yields a significant vacancy concentration of 9(2)% on the site 1b. Constraining to the stoichiometric composition MnBi<sub>6</sub>Te<sub>10</sub> leads to higher residuals ( $R_1 = 0.0315$  for  $I > 2\sigma(I)$ ) and such an idealized composition does not lead to single-phase samples (cf. Section 3.1). Assuming full occupancies without constraining to charge neutrality yields a composition of Mn<sub>0.85</sub>Bi<sub>6.15</sub>Te<sub>10</sub>, again not suitable for the synthesis of single-phase samples. The EDX analysis of the crystal used for data collection (Fig. S21 and Table S12, ESI†) confirms a Mn deficiency and is in good agreement with the composition Mn<sub>0.73</sub>Bi<sub>6.18</sub>Te<sub>10</sub> obtained in the structure refinement. In space group  $R\bar{3}m$ , the asymmetric unit consists of distorted NaCl-type septuple building blocks similar to those in GeBi<sub>4</sub>Te<sub>7</sub>, which are separated by two Bi<sub>2</sub>Te<sub>3</sub>-like layers, resulting in a deficiency and is in good agreement with the composition 51R stacking sequence (Fig. 5a). Again, Mn/Bi intermixing, especially on the 3a, is a characteristic feature of this structure.

**Comparison of selected interatomic distances with Bi<sub>2</sub>Te<sub>3</sub> and Mn<sub>0.85</sub>Bi<sub>2.1</sub>Te<sub>4</sub>.**<sup>32</sup> Selected interatomic distances are listed in Table S13 (ESI†). Bond lengths in the Bi<sub>2</sub>Te<sub>3</sub>-like quintuple layers in Mn<sub>0.85</sub>Bi<sub>4.10</sub>Te<sub>7</sub>, i.e.  $d(M3-Te) = 3.0543(7)$  Å and  $d(M3-Te4) = 3.2410(4)$  Å (labelling cf. Fig. 5), deviate by only 0.4% from interatomic distances in Bi<sub>2</sub>Te<sub>3</sub><sup>66</sup> itself [ $d(Bi-Te2) = 3.067$  Å,  $d(Bi-Te1) = 3.254$  Å]; they are slightly shorter by ~0.01 Å as the cation position contains 3–4% of Mn<sup>2+</sup>, whose radius (0.81 Å for CN 6), which is smaller than that of Bi<sup>3+</sup> (1.17 Å for CN 6).<sup>67</sup> The quintuple layers in Mn<sub>0.73(4)</sub>Bi<sub>6.18(2)</sub>Te<sub>10</sub> [ $d(M3-Bi3) = 3.0628(5)$  Å,  $d(M3-Te4) = 3.2395(5)$  Å,  $d(M4-Te4) = 3.2536(5)$  Å,  $d(M4-Te5) = 3.0594(5)$  Å] exhibit the same tendency and deviate only up to 0.4% from the interatomic distances in Bi<sub>2</sub>Te<sub>3</sub>. All cation–anion bond lengths in the septuple slab of Mn<sub>0.85</sub>Bi<sub>4.10</sub>Te<sub>7</sub> [ $d(M2-Te2) = 3.0436(7)$  Å,  $d(M2-Te1) = 3.2987(9)$  Å,  $d(M1-Te1) = 2.9909(7)$  Å] and

Mn<sub>0.73</sub>Bi<sub>6.18</sub>Te<sub>10</sub> [ $d(M2-Te2) = 3.0473(5)$  Å,  $d(M2-Te1) = 3.3055(6)$  Å,  $d(M1-Te1) = 2.9969(4)$  Å] host more bismuth are thus slightly longer than the corresponding bond lengths in Mn<sub>0.85</sub>Bi<sub>2.1</sub>Te<sub>4</sub> [ $d(M1-Te2) = 3.027(1)$  Å,  $d(M1-Te1) = 3.291(1)$  Å,  $d(M2-Te1) = 2.977(1)$  Å].<sup>32</sup> On the other hand, the distances across the van der Waals gaps between the quintuple and the septuple slab in Mn<sub>0.85</sub>Bi<sub>4.10</sub>Te<sub>7</sub> [ $d(Te2-Te3) = 3.6559(7)$  Å] and Mn<sub>0.73</sub>Bi<sub>6.18</sub>Te<sub>10</sub> [ $d(Te2-Te3) = 3.6516(5)$  Å] decrease slightly with higher bismuth concentration.

### 3.4 TEM investigations

Structured diffuse scattering was not detected in single-crystal X-ray diffraction patterns of the manganese bismuth tellurides with GeBi<sub>4</sub>Te<sub>7</sub> or GeBi<sub>6</sub>Te<sub>10</sub> structure type (Fig. S22, ESI†), thus stacking disorder is not pronounced in these compounds. In order to further analyze possible stacking faults or superstructures along [001], selected area electron diffraction patterns (SAED) were recorded. Fig. 6 and 7 show experimental diffraction patterns and simulated ones based on the results of the crystal structure analyses (Section 3.3). The absence of diffuse streaks along [001]\* indicates that there is no significant amount of stacking faults. Indexing of the patterns corresponds to the lattice symmetry and unit cell parameters found in the X-ray diffraction experiments. In order to visualize the long-range ordered stacking of the different slabs, HRTEM images were acquired (Fig. 8 and Fig. S23 and S24, ESI†). The structural entities of quintuple slabs as in Bi<sub>2</sub>Te<sub>3</sub> and septuple slabs as in MnBi<sub>2</sub>Te<sub>4</sub> can be clearly identified. Simulated HRTEM images based on the results of the crystal structure analyses fit the experimental ones quite well and thus confirm the structure models (Fig. 8 and 9). Note that single vacancies have very little influence on the contrasts of atom columns that consist of several atoms and can thus not be detected in such images.

### 3.5 Magnetic properties

Temperature- and field-dependent magnetization was measured on pellets from single-phase powders with the compositions Mn<sub>0.85</sub>Bi<sub>4.10</sub>Te<sub>7</sub> and Mn<sub>0.81</sub>Bi<sub>6.13</sub>Te<sub>10</sub>. In low magnetic fields of  $\mu_0 H = 0.02$  T, both compounds demonstrate a temperature-driven





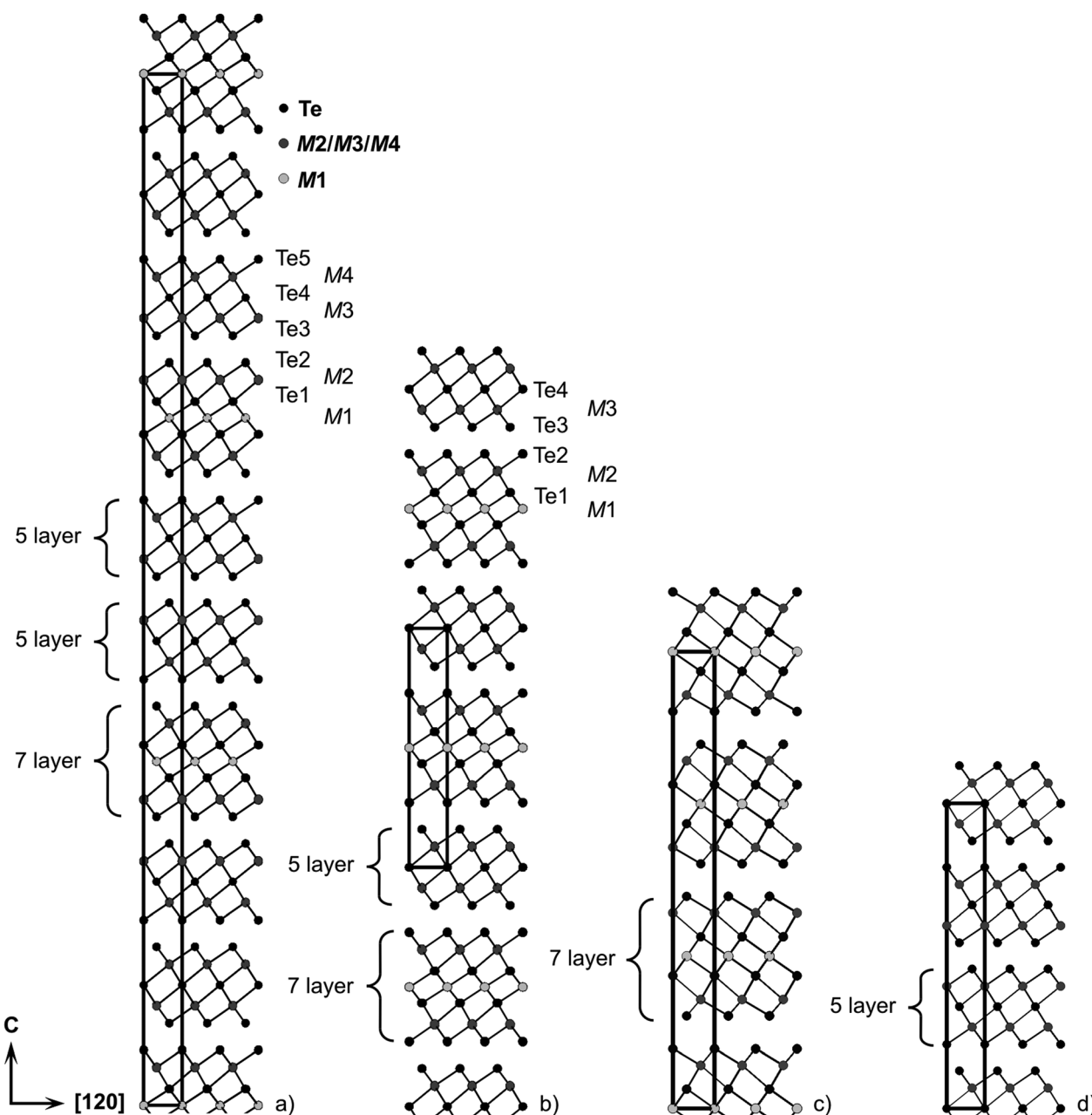


Fig. 5 Crystal structures of (a)  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  with  $\text{GeBi}_6\text{Te}_{10}$ -type structure; (b)  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  with  $\text{GeBi}_4\text{Te}_7$ -type structure; (c)  $\text{Mn}_{0.85}\text{Bi}_{2.1}\text{Te}_4$ <sup>32</sup> with  $\text{GeBi}_2\text{Te}_4$ -type structure; (d)  $\text{Bi}_2\text{Te}_3$ <sup>24</sup> – for cation distribution, including mixed sites, cf. Tables 2 and 4 (M1 is the Mn-rich site).

phase transition from the paramagnetic into magnetically ordered phases. For  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$ , an antiferromagnetic transition can clearly be discerned at  $T_N = 13$  K in low fields (see peak in the inset of Fig. 10a at 13 K), which is followed by a subsequent rearrangement of the microscopic spin alignment at lower temperatures, as indicated by an upturn of the magnetization curve. Given the ferromagnetic hysteresis at  $T = 2$  K in Fig. 11a, a predominantly ferromagnetic alignment with a large ferromagnetic component of the spins can be envisaged at lowest temperatures. The microscopic spin arrangement and the origin of these two transitions for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  should, however, be elucidated in more detail in the future using single crystals. In comparison, for  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  a

very strong upturn of the magnetization below  $T_C = 12$  K together with the splitting of the zero-field-cooled and field-cooled magnetization data indicate a transition into a ferromagnetic phase in this compound.

The effective paramagnetic moment per formula unit can be estimated from the Curie-Weiss fit of the high-temperature data (Fig. 10) and constitutes  $5.7(1) \mu_B$  for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $5.8(1) \mu_B$  for  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ , consistent with the high-spin  $d^5$  configuration of  $\text{Mn}^{2+}$  ( $S = 5/2$ ). Positive values of  $\theta_{CW} = 14(2)$  and  $17(2)$  K for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ , respectively, indicate predominantly ferromagnetic coupling. Magnetization curves as function of the magnetic field (Fig. 11) confirm dominating



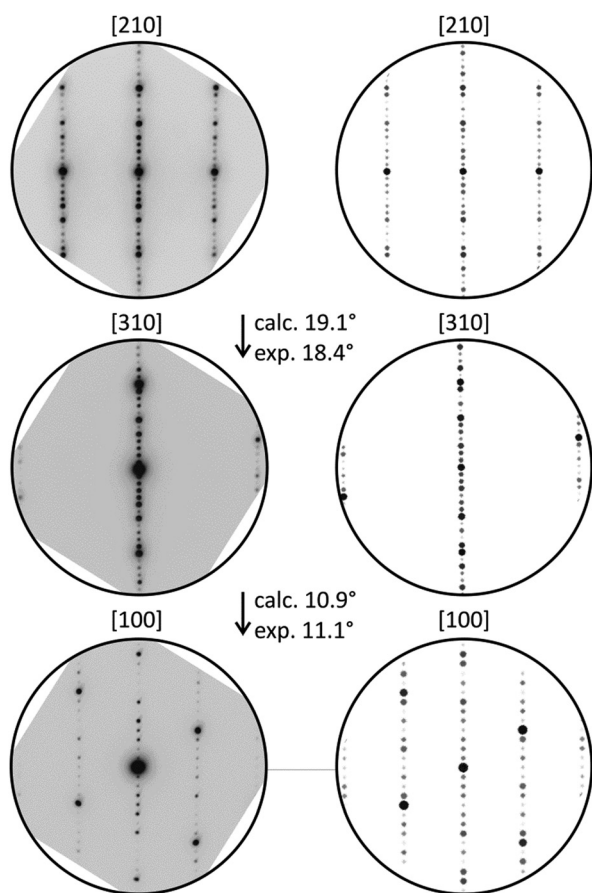
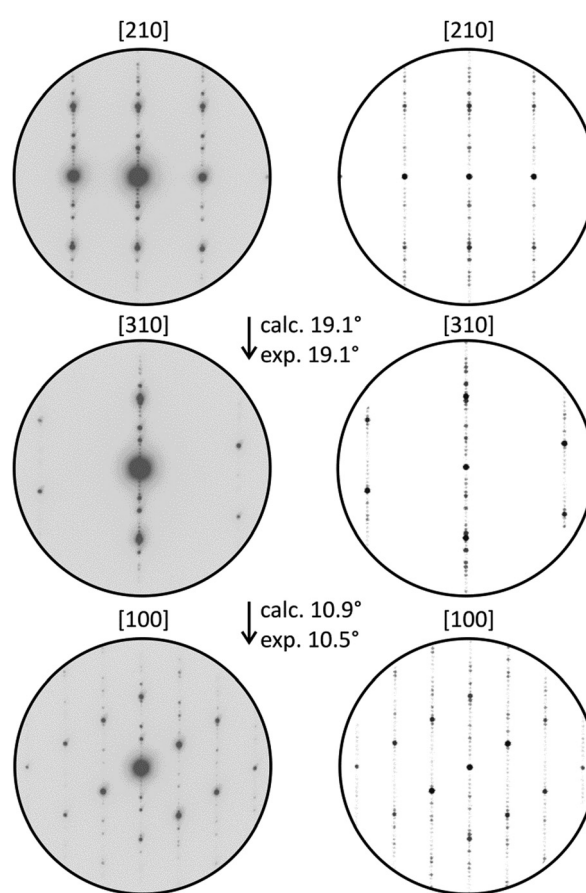


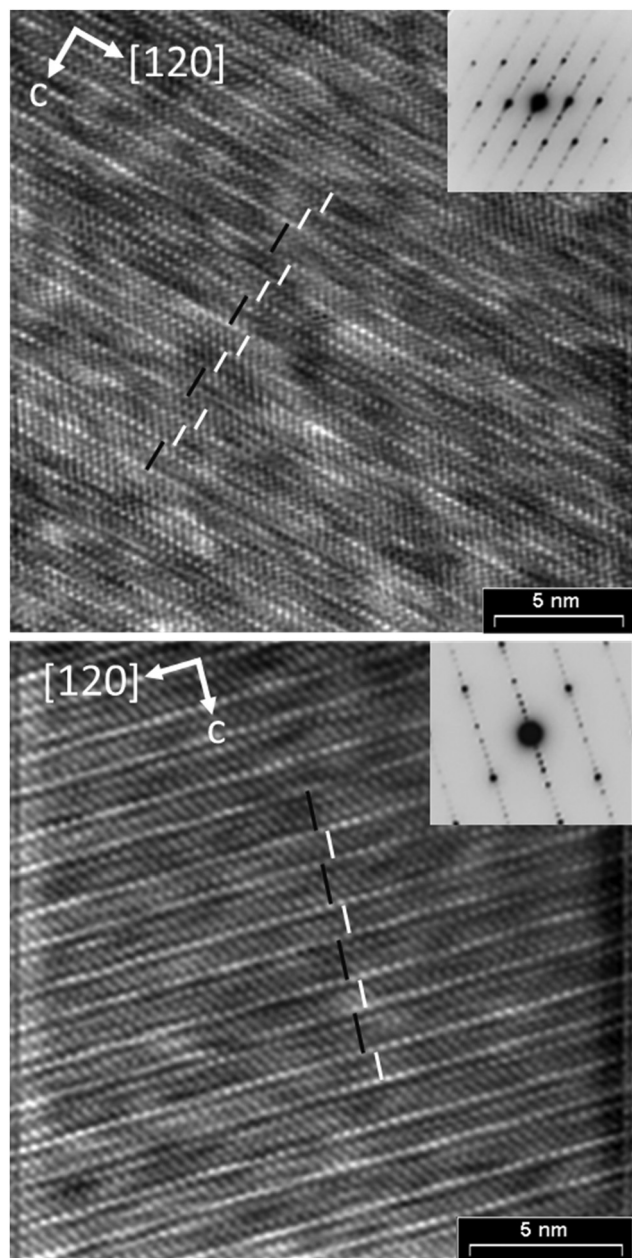
**Table 3** Wyckoff positions, atomic coordinates, site occupancies and coefficients of the anisotropic as well as equivalent isotropic displacement parameters (in Å<sup>2</sup>) for Mn<sub>0.73</sub>Bi<sub>6.18</sub>Te<sub>10</sub> ( $U_{eq} = 1/3(U_{11} + U_{22} + U_{33})$ )

Atom	W. p.	x	y	z	Occ.
Mn1/Bi1/□	3a	0	0	0	0.634(16)/0.275(6)/0.09(2)
Mn2/Bi2	6c	0	0	0.29647(2)	0.017(4)/0.983(3)
Mn3/Bi3	6c	0	0	0.23671(2)	0.015(4)/0.985(3)
Mn4/Bi4	6c	0	0	0.47010(2)	0.014(4)/0.986(3)
Te1	6c	0	0	0.34922(2)	1
Te2	6c	0	0	0.05365(2)	1
Te3	6c	0	0	0.41290(2)	1
Te4	6c	0	0	0.11658(2)	1
Te5	6c	0	0	0.17957(2)	1

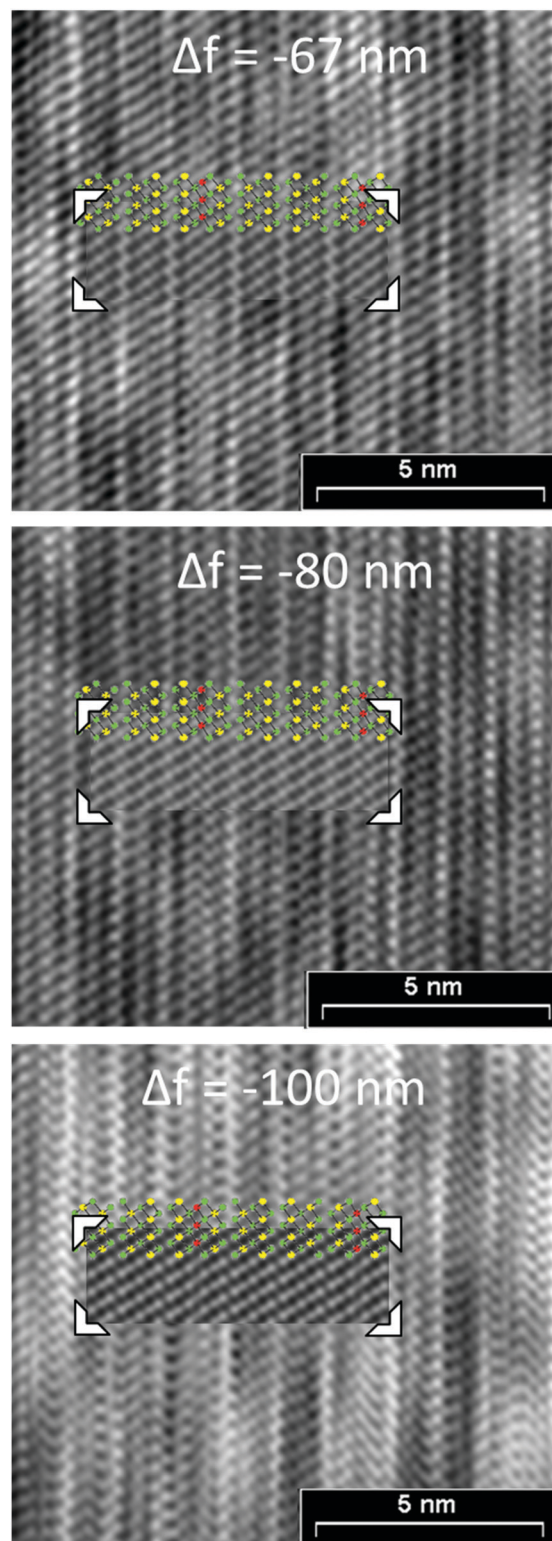
Atom	$U_{11} = U_{22} = 2U_{12}$	$U_{33}$	$U_{23} = U_{13}$	$U_{eq}$
Mn1/Bi1/□	0.0221(5)	0.0238(8)	0	0.0227(4)
Mn2/Bi2	0.02252(17)	0.0278(3)	0	0.02428(16)
Mn3/Bi3	0.0208(2)	0.0269(3)	0	0.02283(19)
Mn4/Bi4	0.0208(2)	0.0265(3)	0	0.02269(19)
Te1	0.0233(2)	0.0207(4)	0	0.0224(2)
Te2	0.0191(2)	0.0229(4)	0	0.0204(2)
Te3	0.0192(2)	0.0204(4)	0	0.0196(2)
Te4	0.0174(2)	0.0176(4)	0	0.0175(2)
Te5	0.0190(3)	0.0205(4)	0	0.0195(2)

**Fig. 6** SAED patterns of a manganese bismuth telluride (from a sample with the nominal composition MnBi<sub>6</sub>Te<sub>10</sub>) with the GeBi<sub>4</sub>Te<sub>7</sub>-type structure and corresponding simulated patterns (kinematical approximation based on the model for Mn<sub>0.85</sub>Bi<sub>4.10</sub>Te<sub>7</sub> from the single-crystal structure analysis) with experimental and calculated tilt angles.**Fig. 7** SAED patterns of a manganese bismuth telluride (from a sample with the nominal composition Mn<sub>0.77</sub>Bi<sub>6.15</sub>Te<sub>10</sub>) with the GeBi<sub>6</sub>Te<sub>10</sub>-type structure and corresponding simulated diffraction patterns (kinematical approximation, based on the model for Mn<sub>0.73</sub>Bi<sub>6.18</sub>Te<sub>10</sub> from the single crystal structure analysis) with experimental and calculated tilt angles.



**Fig. 8** HRTEM images (zone axis [100], Fourier filtered) of manganese bismuth tellurides with the  $\text{GeBi}_4\text{Te}_7$  (bottom) and  $\text{GeBi}_6\text{Te}_{10}$  (top) structure types, each with a corresponding SAED pattern; inset: simulation based on the single-crystal data of  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  ( $\Delta f = -85$  nm,  $t = 8.36$  nm; beam semiconvergence 1.2 mrad, defocus spread 15 nm) and  $\text{Mn}_{0.73}\text{Bi}_{6.18}\text{Te}_{10}$  ( $\Delta f = -67$  nm,  $t = 0.88$  nm; beam semiconvergence 1.2 mrad, defocus spread 15 nm); white bars symbolize quintuple  $\text{Bi}_2\text{Te}_3$ -like slab and black lines symbolize septuple layers characteristic of  $\text{MnBi}_2\text{Te}_4$ .

ferromagnetic interactions in both compounds with pronounced magnetic hysteresis at  $T = 2$  K up to about  $\mu_0 H = 0.2$  T and an almost saturated magnetization close to the expected value for  $\text{Mn(II)}$  for fields above  $\sim 2$  T. The remanent magnetization and the coercive field are slightly larger for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  ( $\mu_0 H_c = 0.08$  T).



**Fig. 9** HRTEM defocus series (zone axis [100], Fourier filtered) from a manganese bismuth telluride with the  $\text{GeBi}_6\text{Te}_{10}$ -type structure, insets:  $\text{GeBi}_6\text{Te}_{10}$ -type structure (green = Te; yellow = Bi-rich; red = Mn-rich: for the exact cation distribution, including mixed sites *cf.* Tables 2 and 4) and simulated images based on the single-crystal data of  $\text{Mn}_{0.73}\text{Bi}_{6.18}\text{Te}_{10}$ ,  $t = 0.88$  nm; beam semiconvergence 1.2 mrad, defocus spread 15 nm, defocus values  $\Delta f$  are given in the images.





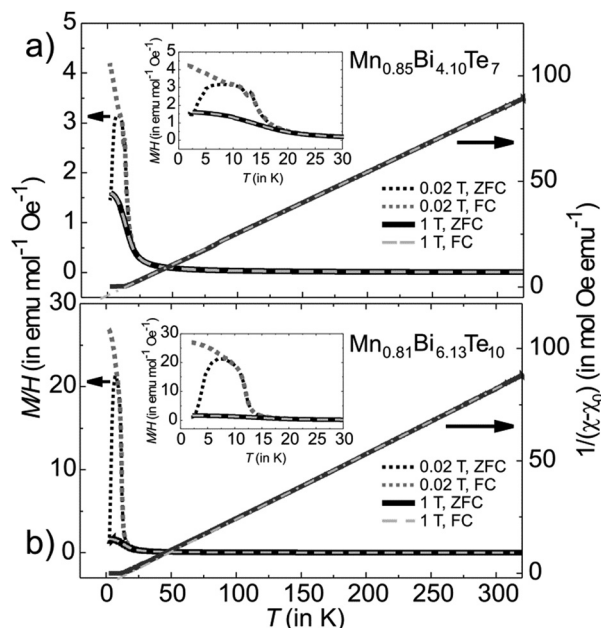


Fig. 10 Magnetization  $M/H$  and reciprocal susceptibility of (a)  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and (b)  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  as a function of temperature measured at various applied magnetic fields. The extrapolated line on the right axis is a Curie–Weiss fit to the high-temperature data indicating a value  $\theta_{\text{CW}}$  of 14(2) and 17(2) K for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ , respectively. A small offset  $\chi_0 \sim -0.0007(3) \text{ emu mol}^{-1} \text{ Oe}^{-1}$  was added to the data to account for the contribution of closed diamagnetic electronic shells.

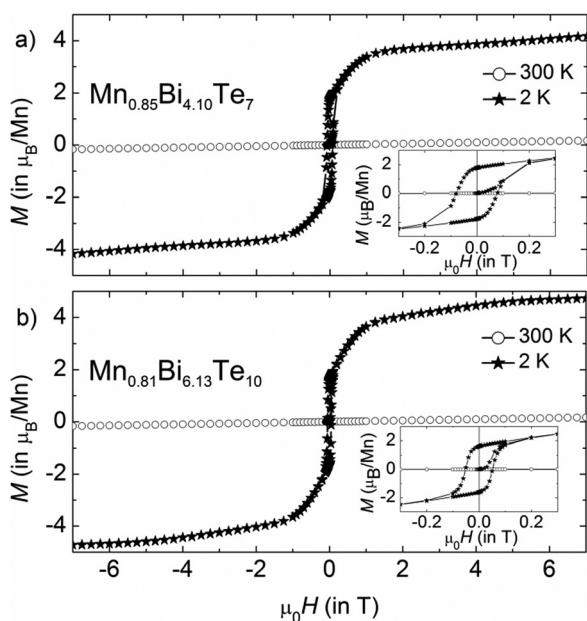


Fig. 11 Magnetic hysteresis curves of (a)  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and (b)  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  at 300 and 2 K. The samples were cooled in zero field from 320 K.

### 3.6 Thermoelectric properties

Thermoelectric measurements (Fig. 12) were conducted on parts of compact ingots between RT and 400 °C in three consecutive cycles. The temperature evolution of the electrical conductivity  $\sigma$  indicates metallic behavior above RT. Whereas  $\text{MnBi}_2\text{Te}_4$  has been

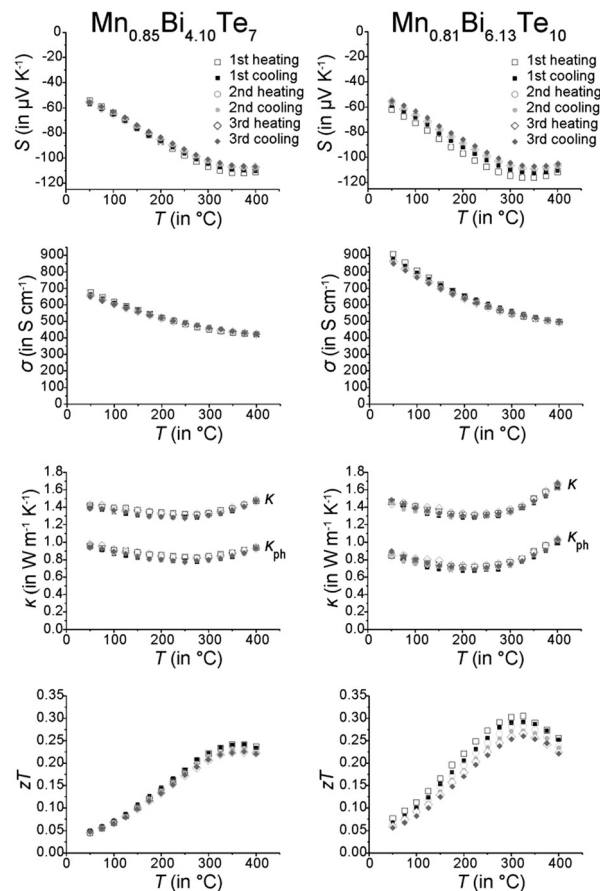


Fig. 12 Thermoelectric properties of  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  (left column) and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  (right column); Seebeck coefficient (first row), electrical conductivity (second row), thermal conductivity and its phononic contribution (third row, calculated according to the Wiedemann–Franz relationship; the decrease of the Lorenz number  $L$  has been derived from the increase of the absolute value of  $S$  according to  $L = 1.5 + e^{-|S|/116}$  where  $L$  is in  $10^{-8} \text{ W } \Omega \text{ K}^{-2}$  and  $S$  in  $\mu\text{V K}^{-1}$ ); this equation is accurate within 5% for single parabolic band/acoustic phonon scattering assumption.<sup>69</sup> and  $zT$  values (fourth row); three subsequent heating and cooling cycles.

reported to be a p-type conductor with rather low  $\sigma$  ( $39 \text{ S cm}^{-1}$  at RT),<sup>31</sup> other investigations on comparable materials indicate n-type conduction, concluding from a negative Seebeck coefficient  $S$  and a much higher  $\sigma$  ( $450 \text{ S cm}^{-1}$  at RT).<sup>32</sup> Similarly,  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  exhibit negative  $S$  and thus are n-type conductors. Despite the shallow minimum in the thermal evolution of  $S$ , the bandgap was roughly estimated using the Goldsmid–Sharp relationship,<sup>68</sup>  $E_g = 2eS_{\text{max}}T_{\text{max}}$ , with the maximum absolute Seebeck coefficient  $S_{\text{max}}$  and the corresponding temperature  $T_{\text{max}}$ . This yields narrow bandgaps of  $E_g \approx 0.14 \text{ eV}$  for both  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ . This bandgap corresponds with the high electrical conductivity and with the  $E_g$  of other compounds with layered  $\text{GeBi}_4\text{Te}_7$ - or  $\text{GeBi}_6\text{Te}_{10}$ -type structures (Table 4).

Thermal conductivities are rather low and almost constant up to 400 °C with  $1.47 \text{ W m}^{-1} \text{ K}^{-1}$  for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $1.63 \text{ W m}^{-1} \text{ K}^{-1}$  for  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ . However, the small value of  $S$  limits the maximum  $zT$  values up to 0.25 at 375 °C and 0.28

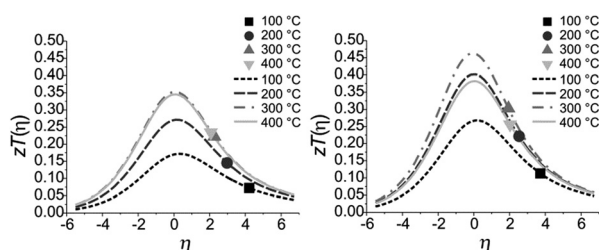
**Table 4** Electronic properties of  $\text{MnBi}_4\text{Te}_7$ ,  $\text{MnBi}_6\text{Te}_{10}$  ( $M = \text{Sn, Pb, Ge}$ ),  $\text{Mn}_{0.85}\text{Bi}_{2.1}\text{Te}_4$ ,  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ 

Compound	$S$ at RT (in $\mu\text{V K}^{-1}$ )	$\sigma$ at RT (in $\text{S cm}^{-1}$ )	$E_g$ (in eV)	Ref.
$\text{MnBi}_2\text{Te}_4$	168	39	$\sim 0.4$	31
$\text{Mn}_{0.85}\text{Bi}_{2.1}\text{Te}_4$	−5	475	0.15	32
$\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$	−55	700	0.14	This work
$\text{GeBi}_4\text{Te}_7$	−127	435	0.21	76
	−160	230		24
$\text{SnBi}_4\text{Te}_7$	−92	250	0.22	76
$\text{PbBi}_4\text{Te}_7$	−68	1666	—	76
	−66	1070		24
$\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$	−60	900	0.14	This work
$\text{GeBi}_6\text{Te}_{10}$	−65	920	—	28
$\text{PbBi}_6\text{Te}_{10}$	−47	870	—	24

at 325 °C for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ , respectively. The  $zT$  values decrease slightly from cycle to cycle, which could be attributed to the metastability of the manganese bismuth tellurides. The *ex situ* PXRD measurements performed after the thermoelectric measurements (Fig. S7, ESI†) show that still up to 80% of the main phase is present in both compounds. SEM investigations (Fig. S15 and Table S10, ESI†) confirm that the samples slowly decompose over several measurement cycles (cf. Sections 3.1 and 3.2).

The quality factor  $B$  (eqn (1)), the figure of merit  $zT = S^2\sigma T/\kappa$  (eqn (2)) and the phononic part of the thermal conductivity  $\kappa_{\text{ph}}$  were calculated as a function of the electrons' chemical potential  $\eta$  from the measured transport properties  $\sigma$ ,  $S$  and  $\kappa$  of the first cycle of the thermoelectric measurement (Fig. 12), which is only very little affected by the decomposition. An effective mass model was used to calculate the optimal carrier concentration  $zT_{\text{opt}}$ . Details of the calculations are described at the end of the ESI† and can also be found in several references.<sup>70–75</sup> This approach allows one to calculate the intrinsic electrical conductivity  $\sigma_{E_0}$  and  $\kappa_{\text{ph}}$  and therefore also the material quality factor  $B$  (eqn (1)). These intrinsic properties are independent of doping and thus can be separated from doping and its optimization. The optimal  $zT$  values for different temperatures and therefore different  $B$  factors are shown in Fig. 13.

$$B = \left(\frac{k_{\text{B}}}{e}\right)^2 \frac{\sigma_{E_0} T}{\kappa_{\text{ph}}} \quad (1)$$



**Fig. 13** Calculated and measured  $zT$  values for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  (left) and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  (right) as a function of  $\eta$  at 100 °C, 200 °C, 300 °C and 400 °C with  $B = 0.047, 0.078, 0.105$  and  $0.102$  for  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $B = 0.076, 0.122, 0.144$  and  $0.115$  for  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$ .

$$zT(\eta) = \frac{S^2(\eta)}{\frac{(k_{\text{B}}/e)^2}{B \ln(1 + e^\eta)} + L(\eta)} \quad (2)$$

The measured  $zT$  values of  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $\text{Mn}_{0.81}\text{Bi}_{6.13}\text{Te}_{10}$  indicate that in both compounds the carrier concentrations are higher than optimal as the measured  $zT$  values are on the high- $\eta$  side of the maximal  $zT(\eta)$  (note that the carrier concentration is a monotonically increasing function of  $\eta$ ). With ideal carrier concentration (*i.e.* optimal  $\eta$ ) the maximum of  $zT$  for manganese bismuth tellurides with  $\text{GeBi}_4\text{Te}_7$ -type structure could increase up to 0.35 at 300 °C and up to 0.47 at 300 °C for the  $\text{GeBi}_6\text{Te}_{10}$ -type structure.

## 4 Conclusions

The crystal-structure determinations of two new compounds in the manganese–bismuth–telluride system reveal unexpected combinations of chemical composition and structure type. Diffraction data of  $\text{Mn}_{0.85}\text{Bi}_{4.10}\text{Te}_7$  and  $\text{Mn}_{0.73}\text{Bi}_{6.18}\text{Te}_{10}$  indicate that the compounds are isostructural to  $\text{GeBi}_4\text{Te}_7$ <sup>27,29</sup> and  $\text{GeBi}_6\text{Te}_{10}$ ,<sup>24</sup> respectively. This is confirmed by a combination of X-ray diffraction, including the application of microfocused synchrotron radiation (for  $\text{Mn}_{0.73}\text{Bi}_{6.18}\text{Te}_{10}$ ), of TEM imaging and of EDX spectroscopy.<sup>43</sup> According to the magnetization measurements, the oxidation state of  $\text{Mn}^{\text{II}}$  is established. This corresponds to the situation in  $\text{MnBi}_2\text{Te}_4$ .<sup>32,33</sup> The structures contain significant amounts of cation vacancies. Intermixing of Mn and Bi on the cation sites is very pronounced and highly significant. Other layered chalcogenides of the  $\text{GeBi}_2\text{Te}_4$ ,  $\text{GeBi}_4\text{Te}_7$  and  $\text{GeBi}_6\text{Te}_{10}$  structure types also exhibit very characteristic mixed cation occupancies.<sup>24,27,28,76–79</sup> This phenomenon is also typical and, in principle, to be expected for manganese bismuth tellurides in these structure types. The non-stoichiometry of  $\text{Mn}_{1-x}\square_{x/3}\text{Bi}_{4+2x/3}\text{Te}_7$  ( $x = 0.15 - 0.2$ ) (space group  $P\bar{3}m1$  with  $\text{GeBi}_4\text{Te}_7$ -type structure) and  $\text{Mn}_{1-x}\square_{x/3}\text{Bi}_{6+2x/3}\text{Te}_{10}$  ( $x = 0.19 - 0.26$ ) (space group  $R\bar{3}m$  with  $\text{GeBi}_6\text{Te}_{10}$ -type structure) is comparable to the situation in the related compound  $33\text{R-Ge}_{4x}\text{Sb}_{2y}\text{Te}_7$  ( $x, y \approx 0.1$ ), which is isostructural to  $\text{Ge}_3\text{Sb}_2\text{Te}_6$  despite a different stoichiometry.<sup>80</sup> The manganese bismuth tellurides with  $\text{GeBi}_4\text{Te}_7$ - and  $\text{GeBi}_6\text{Te}_{10}$ -type structures are metastable and start decomposing at approximately 250 °C into a Mn-doped  $\text{Bi}_2\text{Te}_3$ -like structure, Bi-rich bismuth tellurides and a manganese-rich phase. This result is crucial concerning physical measurements at elevated temperatures. This decomposition was not observed in our DSC measurements, as it is very slow and extends over a wide temperature range ( $\sim 70$  K). Yet, the DSC measurements show that these phases are not accessible by slow cooling of melts. An annealing step in the solid state followed by quenching to room temperature is essential to obtain phase pure samples, as kinetic effects impede the immediate decomposition at elevated temperatures. Small variations in the annealing temperature may lead to different structures. The rather broad DSC signal for the  $\text{GeBi}_6\text{Te}_{10}$ -type structure might indicate other structure variants. The  $zT$  values of these layered manganese bismuth tellurides indicate decent thermoelectric properties and may be





affected by the metastability, but have plenty of room for optimization. The first step towards optimization would be to increase the stability, *e.g.* by partial substitution of manganese with group 14 elements as preliminary experiments indicate that such substitution is possible. For an increased thermoelectric performance, doping should decrease the concentration of the charge carriers. Much beyond thermoelectrics, the access to single-phase compounds in this ternary system is crucial for various more specialized analyses such as ARPES and detailed investigations of magnetic effects.  $\text{MnBi}_2\text{Te}_4$  has attracted much attraction as the first antiferromagnetic topological insulator, with special focus on theoretical calculations.<sup>33,81</sup> As these may be questionable if they are based on simple ordered models, the crystal-structure data presented in this study should be the basis for realistic calculations that take into account vacancies and Mn/Bi disorder. The new layered manganese bismuth tellurides may be promising candidates for topologically non-trivial materials and thus for studies of mutual influence between long-range magnetic ordering at low temperatures and non-trivial band-structure topology. The single-phase materials, which were only accessible by taking the non-stoichiometry into account, may also be a perspective for magnetic sensing if they should exhibit the anomalous Hall effect like, *e.g.*, Mn-doped  $\text{Bi}_2\text{Te}_3$ .<sup>17,82</sup>

## Conflicts of interest

There are no conflicts to declare.

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