A model for dinitrogen binding in the E\textsubscript{4} state of nitrogenase\textsuperscript{†}

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Molybdenum nitrogenase is one of the most intriguing metalloenzymes in nature, featuring an exotic iron–molybdenum–sulfur cofactor, FeMoco, whose mode of action remains elusive. In particular, the molecular and electronic structure of the N\textsubscript{2}–binding E\textsubscript{4} state is not known. In this study we present theoretical QM/MM calculations of new structural models of the E\textsubscript{4} state of molybdenum-dependent nitrogenase and compare to previously suggested models for this enigmatic redox state. We propose two models as possible candidates for the E\textsubscript{4} state. Both models feature two hydrides on the FeMo cofactor, bridging atoms Fe\textsubscript{2} and Fe\textsubscript{6} with a terminal sulfhydryl group on either Fe\textsubscript{2} or Fe\textsubscript{6} (derived from the S\textsubscript{2}B bridge) and the change in coordination results in local lower-spin electronic structure at Fe\textsubscript{2} and Fe\textsubscript{6}. These structures appear consistent with the bridging hydride proposal put forward from ENDOR studies and are calculated to be lower in energy than other proposed models for E\textsubscript{4} at the TPSSh-QM/MM level of theory. We critically analyze the DFT method dependency in calculations of FeMoco that has resulted in strikingly different proposals for this state. Importantly, dinitrogen binds exothermically to either Fe\textsubscript{2} or Fe\textsubscript{6} in our models, contrary to others, an effect rationalized via the unique ligand field (from the hydrides) at the Fe with an empty coordination site. A low-spin Fe site is proposed as being important to N\textsubscript{2} binding. Furthermore, the geometries of these states suggest a feasible reductive elimination step that could follow, as experiments indicate. Via this step, two electrons are released, reducing the cofactor to yield a distorted 4-coordinate Fe\textsubscript{2} or Fe\textsubscript{6} that partially activates N\textsubscript{2}. We speculate that stabilization of an N\textsubscript{2}-bound Fe(1) at Fe\textsubscript{6} (not found for Fe\textsubscript{2} model) via reductive elimination is a crucial part of N\textsubscript{2} activation in nitrogenases, possibly aided by the apical heterometal ion (Mo or V). By using protons from the sulfhydryl group (to regenerate the sulfide bridge between Fe\textsubscript{2} and Fe\textsubscript{6}) and the nearby homocitrate hydroxy group, we calculate a plausible route to yield a diazene intermediate. This is found to be more favorable with the Fe\textsubscript{6}-bound model than the Fe\textsubscript{2}-bound model; however, this protonation is uphill in energy, suggesting protonation of N\textsubscript{2} might occur later in the catalytic cycle or via another mechanism.

Introduction

The mechanism of biological nitrogen reduction, catalyzed by the bacterial nitrogenase enzymes, has remained an unsolved problem in bioinorganic chemistry despite decades of research involving many experimental and theoretical research groups. The nitrogenases are metalloenzymes that catalyze the reductive elimination of dinitrogen to two molecules of ammonia for each molecule of dinitrogen, impressively at ambient conditions.\textsuperscript{1,2} The molybdenum-dependent form is the most active and the best characterized, yet there is no consensus on the dinitrogen binding site on the cofactor nor is there a basic mechanism in place. The complete enzyme consists of a transient complex of the MoFe protein and the Fe protein. The function of the Fe protein is electron transfer to the MoFe protein \textit{via} an [Fe\textsubscript{4}S\textsubscript{4}] cluster in an ATP-dependent process while dinitrogen reduction takes place in the MoFe protein. The active site of the MoFe protein, includes a complex [Mo\textsubscript{Fe}S\textsubscript{6}C] cofactor (FeMoco, shown in Fig. 1) where dinitrogen binds. The kinetic studies by Lowe and Thorneley\textsuperscript{3} resulted in a model for dinitrogen catalysis linking different redox states of the cofactor (denoted E\textsubscript{n}, with \(n\) indicating the number of added electrons and protons) together. The obligatory formation of one molecule of H\textsubscript{2} per molecule of N\textsubscript{2} is an intriguing aspect of the model, suggesting the unusual stoichiometry and the apparent waste of 2 electrons and 4 molecules of MgATP to produce this extra molecule of H\textsubscript{2}.\textsuperscript{4}
N₂ + 8e⁻ + 8H⁺ + 16MgATP → 2NH₃ + H₂ + 16MgADP

Curiously, in the Lowe–Thorneley model (a simplified scheme is shown in Fig. 1), dinitrogen does not bind to the iron–molybdenum cofactor until either the E₃ or E₄ state (after 3 or 4 added electrons and protons to the resting state E₀), concomitant with formation of one molecule of H₂. This obligatory H₂ evolution can occur as side-reactions from the E₂, E₃ and E₄ states, obligatory H₂ evolution is proposed to occur concomitantly as N₂ binds in the E₄ state.

The FeMoco cluster is a highly unusual metallocofactor with a molecular structure that took many years to characterize; it consists of 7 iron ions, 1 molybdenum ion, 9 sulfides and an interstitial carbide.

Recent X-ray magnetic circular dichroism experiments demonstrated the presence of the unusual spin-coupled state of Mo(III) in a related [MoFe₇S₉] model cubane. The charge of the cofactor in the resting state has been determined to be [MoFe₇S₉Cl]⁻ according to Mössbauer analysis, spatially resolved anomalous dispersion refinement and comparison of calculated and crystallographic metal–metal distances. Recent studies of the electronic structure from broken-symmetry (BS) DFT studies reveals a complicated electronic structure featuring both antiferromagnetic coupling, mixed-valence delocalization and partial metal–metal bonding.

Other redox states of FeMoco are less well-characterized but we note recent spectroscopic studies of the E₁ state and the E₂ state. The binding site of dinitrogen is far from obvious from inspection of the cluster in its resting state (E₀) and since little is known about the structure of the E₄ redox state (which has been argued to be the primary state for N₂ binding during turnover), this is one of the most pressing questions in nitrogenase research. Even less is known about the E₃ state and its proposed N₂ binding as the state is EPR silent. A correct structural model for E₄ would arguably reveal (or at least strongly suggest) how dinitrogen can favourably bind to FeMoco and how this typically inert molecule is activated for protonation. An accumulated S = 1/2 E₄ state was originally probed by EPR spectroscopy in a mutant (αₗ-70Val₁₆MgAJ) of MoFe protein and ENDOR spectroscopy revealed that the structure contains 2 chemically near-equivalent bridging hydrides, likely storing the 4 reducing equivalents. Later, the EPR signal and ENDOR hyperfine signals associated with this state were found in the wild-type protein as well. The reductive elimination of H₂ from these two hydrides was furthermore proposed to explain the obligatory H₂ evolution in the mechanism and how dinitrogen is activated for protonation and there is now ample experimental evidence for this proposal. There is, however, no consensus on the structure of the E₃ state, neither the precise coordination of the hydrides, nor the N₂ binding site agreed upon. Mutation studies have previously implicated the Fe₆₋Fe₇–Fe₉–Fe₁₂ face as a likely binding site for dinitrogen as no dinitrogen reduction is observed when the residue αₗ-70Val is mutated into the bulkier αₗ-70Leu. Recent joint experimental–computational studies have proposed E₄ models featuring bridging hydrides (the favoured model features bridging hydrides between Fe₃–Fe₇ and Fe₉–Fe₁₂) while other computational studies have suggested mixed bridging/terminal hydride models or, even surprisingly, structures featuring a protonated carbide with/without bridging hydrides. Additionally, recent crystal structures of a CO-bound form of MoFe protein (CO being an inhibitor) and an XH-ligand-bound (X = N or O) form of VFe protein have emerged, that show CO/XH replacing the Fe₉–Fe₁₂ bridging sulfide in a bridging binding mode (we recently showed via QM/MM calculations that the XH ligand in the FeVco structure is more consistent with an OH). These crystal structures demonstrate the lability of the sulfide bridges, which hints at a possible binding site of dinitrogen or perhaps a binding site of hydrides as discussed by Einsle et al. Overall, there is no consensus on the nature of the E₄ state.

The present study proposes new structural models for the E₄ state of FeMoco as well as a model for dinitrogen binding based on recent X-ray magnetic circular dichroism experiments.
on theoretical calculations. A state-of-the-art QM/MM protocol using the broken-symmetry DFT approach is used that has been previously validated on the resting \( E_0 \) state.\textsuperscript{13} We compare the new structural models to previous proposals by calculating all models at the same QM/MM level of theory. The DFT method dependence of the relative energies is discussed and is put into context with the ability of different computational protocols to describe the electronic structure of the resting state correctly. Two energetically favourable models appear to be consistent with the bridging hydride proposal from experimental ENDOR studies and while favourable dinitrogen binding to both is possible, the \( E_4 \) model featuring an open coordination site at \( \text{Fe}_6 \) binds \( \text{N}_2 \) slightly stronger. Concomitant \( \text{H}_2 \) evolution with the reductive elimination proposal can be explained using our model due to close proximity of the hydrides (favoured over a hydride-proton reaction) and this leads to the stabilization of an \( \text{N}_2 \)-bound \( \text{Fe}(i) \) intermediate at \( \text{Fe}_6 \) (or alternatively to an \( \text{N}_2 \)-bound \( \text{Fe}(ii) \) intermediate at \( \text{Fe}_2 \)). A possible protonation step to yield a FeMoco-bound diazene intermediate is discussed.

**Computational details**

The QM/MM models for \( E_4 \) were based on our model for the \( E_0 \) resting state model that has been previously described.\textsuperscript{13} It is a spherical QM/MM model (42 Å radius and \( \sim 37000 \) atoms) centered on the carbide of FeMoco that includes roughly half of the tetrameric MoFe protein; see ESI† for details about the QM/MM model preparation. In the QM/MM geometry optimizations of \( E_4 \) models the active region consists of 1003 atoms and a QM region of 136 atoms while calculations of \( E_0 \) used a smaller QM region of 54 atoms. All QM/MM calculations were performed in Chemshell\textsuperscript{36,37} using the built-in MM code DL_POLY\textsuperscript{38} with the CHARMM36 forcefield\textsuperscript{39} and ORCA version 4.0 (ref. 40) as QM code. The 136 atom QM region (see Fig. S4 in ESI†) contains the FeMoco cofactor, singly protonated homocitrinate and the side-chains of residues \( \alpha-70 \text{val} \), \( \alpha-96 \text{Arg} \), \( \alpha-191 \text{Gln} \), \( \alpha-195 \text{His} \), \( \alpha-275 \text{Cys} \), \( \alpha-278 \text{Ser} \), \( \alpha-359 \text{Arg} \), \( \alpha-380 \text{Glu} \), \( \alpha-381 \text{Phe} \), and \( \alpha-442 \text{His} \). The QM region thus contains the main residues critical to describing the coordination, electrostatic environment, asymmetry, and hydrogen-bonding environment around FeMoco. This includes residues directly coordinating FeMoco (\( \alpha-442 \text{His} \), \( \alpha-275 \text{Cys} \)), neighboring charged residues (\( \alpha-96 \text{Arg} \), \( \alpha-359 \text{Arg} \), \( \alpha-380 \text{Glu} \)), those capable of participating in hydrogen bonding (\( \alpha-195 \text{His} \), \( \alpha-191 \text{Gln} \), \( \alpha-278 \text{Ser} \)), as well as spatially close residues (\( \alpha-70 \text{Val} \), \( \alpha-381 \text{Phe} \)). \( \alpha-195 \text{His} \) is calculated to be in the \( \text{N}_2 \) protonation state, assuming the residue has donated a proton from \( \text{N}_2 \) to the cofactor and has been reprotonated at \( \text{N}_2 \). All QM/MM calculations used electrostatic embedding, and hydrogen link atoms were used to terminate the QM–MM border together with the charge-shift procedure as implemented in Chemshell. The \( E_4 \) QM calculations primarily used the TPSSh hybrid density functional,\textsuperscript{41,42} a ZORA scalar relativistic Hamiltonian,\textsuperscript{43,44} the relativistically reconstructed def2-TZVP basis set\textsuperscript{45,46} on all metal, sulfur, carbide, homocitrinate and hydride/SH/CH atoms (def2-SVP on other atoms) and a D3BJ dispersion correction.\textsuperscript{47,48} The RIJCOSX approximation\textsuperscript{49,50} with a decontracted Coulomb auxiliary basis set by Weigend\textsuperscript{51} was used. All DFT calculations used tight integration grids (Grid5 Finalgrid6 settings in ORCA). Single-point energy calculations of \( E_4 \) models were performed at the TPSS,\textsuperscript{41} B3LYP\textsuperscript{52–55} and M06-2X\textsuperscript{56} levels using the same basis set. M06-2X calculations used a very large grid (Grid7 in ORCA) due to the grid-dependence associated with this functional.\textsuperscript{57} QM/MM geometry optimizations of the \( E_0 \) state with some functionals always used the D3BJ dispersion correction except in the case of M06-2X where a D3(0) correction was used. Functionals used for \( E_0 \) geometry optimizations were BP86,\textsuperscript{58,59} TPSS,\textsuperscript{41} B3LYP, PBE0,\textsuperscript{60,61} BHLYP,\textsuperscript{61} M06-2X and \( \omega \text{B97M-D3BJ} \).\textsuperscript{62,63} Broken-symmetry solutions of the \( E_4 \) models were found by flipping spins on Fe atoms converging to the \( M_s = 1/2 \) solution. Four different broken-symmetry solutions were explored (with Fe ions 235, 346, 247 or 147 spin down; atom numbering as in crystal structure) as discussed later. Vibrational frequencies of \( \text{N}_2 \)-bound models were calculated from a numerical QM/MM partial Hessian. While all QM/MM calculations minimized the QM/MM energy function, we primarily discussed the polarized QM energy rather than the total QM/MM energy as the former is less sensitive to the unrelated MM energy changes of the MM region.

**Results and discussion**

A. Computational modelling of the \( E_4 \) state

Theoretical modelling of the \( E_4 \) state (here defined as the state after addition of 4e\textsuperscript{−} and 4H\textsuperscript{+} to the resting state \( E_0 \) of FeMoco) has been pursued recently by many groups and their models will be discussed and compared. It is helpful to first discuss criteria that, in our view, a realistic model for the \( E_4 \) state should ultimately fulfil. These criteria are: (i) consistency with available spectroscopic data, (ii) the model being a thermodynamically viable state, (iii) demonstration of favorable \( \text{N}_2 \) binding and consistency with isotope substitution experiments and, (iv) computational consistency.

Regarding criterion i, regrettably, spectroscopic data for the \( E_4 \) state are scarce and are primarily available in the form of EPR and ENDOR data, and primarily on a mutant form of the protein (which appears though to have the same spectroscopic signature as the wild type\textsuperscript{25}). The EPR data indicates a spin state of \( S = 1/2 \) and analysis of the \( ^1 \text{H} \) hyperfine tensors from \( ^1 \text{H} \) ENDOR spectroscopy led to the proposal that the state contains two near-identical metal-bound hydrides, that are bridging rather than terminal and bound to Fe ions rather than the Mo ion according to \( ^{57} \text{Fe} \) ENDOR.\textsuperscript{54} Furthermore, \( ^{57} \text{Fe} \) ENDOR indicates that the overall iron redox level of \( E_4 \) is the same as in the \( E_0 \) state,\textsuperscript{66} which suggests that the two hydrides are acting as carriers of the four added electrons. A recent high-resolution ENDOR study of the same state has additionally revealed signals from two other hydrides, likely present as protons bound to sulfides.\textsuperscript{65} As quantum chemical calculations of FeMoco are currently mostly limited to broken-symmetry DFT approaches (where pure spin states are not calculated) and spin projection schemes are problematic for non-Heisenberg systems like FeMoco, this unfortunately makes a direct comparison of the calculations to magnetic spectroscopy data
from EPR and ENDOR difficult. However, an indirect comparison is still possible, i.e. a comparison of computed structures to the bridging hydride structural motif suggested by the ENDOR analysis.

Regarding thermodynamic stability i.e. criterion ii, kinetic studies of MoFe protein under turnover, indicates the E4 state is only fleetingly stable. The state can be freeze-trapped in a turnover sample with a small population but will evolve H2 with fast rates to fall back to an E2 state (that in turn further evolves H2 and falls back to E0). The fleet nature of this state and the fact that the mechanisms of reduction and protonation are not entirely clear, indicates that thermodynamics alone cannot be the only guiding principle for differentiating between models for E4; however, thermodynamic stability must still be relevant to its formation.

Criterion iii implies that the model should ideally demonstrate favourable N2 binding. Experimental studies indicate N2 binding to be unfavourable in the early redox states, suggesting that the unknown E4 state features a structural component that makes N2 binding favourable (e.g. an empty coordination site), unlike redox states E0–E2 (E1 has also been proposed to bind N2). Furthermore, a model for E4 should offer a plausible explanation or mechanism for the obligatory H2 evolution resulting from the reductive elimination of H2 from two hydrides (as shown by isotope substitution studies) as N2 binds to FeMoco.

Finally, we propose computational consistency as criterion iv, that the computational E4 model should satisfy. By this, we mean that the computational protocol used to propose the model should also be shown to be consistent with other important experimental data of the system such as data for the other redox states. The 1.0 Å crystal structure of the E0 state6 is in our view the most accessible experimental data for gauging the quality of the computational protocols. The quality of the crystal structure of MoFe protein has improved steadily in recent years and has a bond length uncertainty of ~0.02 Å. We consider a satisfactory agreement of the computed resting state structure to the crystal structure to be vital to any computational protocol that is used to suggest new redox state models of FeMoco.

All models that we consider in this study were structurally optimized at the same QM/MM level of theory that we have previously used to describe the resting state E0 and we considered multiple broken-symmetry states for each model. As recently discussed by Raugei et al.,24 the protein environment and the quality of the computational model can make a surprisingly large difference regarding the relative stability of an E4 isomer. Raugei et al. demonstrated e.g. that a protonated carbide model for E4 was only stable for small cluster models of the active site but became unstable when larger cluster models were considered. As our QM/MM model accounts for the explicit protein environment from the beginning (and avoids potentially artificial constraints on residues) and furthermore utilizes a large QM-region (including important charged and hydrogen-bonding residues near FeMoco), our calculations should suffer much less from such artifacts. Our QM/MM methodology has previously been validated by detailed comparison of the calculated molecular structure of the cofactor in the resting state to the available high-resolution crystal structure, giving better agreement for the basic metal framework than cluster models.13 As before, we primarily utilize the TPSSH level of theory (a 10% Hartree–Fock (HF) exchange TPSSH hybrid), a ZORA scalar relativistic Hamiltonian, dispersion correction and a flexible polarized triple-zeta basis set (on the cofactor). The functional dependency of calculations is discussed in chapter C.

Due to the complex open-shell nature of the [MoFe3S12C] cluster, the spin coupling problem of FeMoco is far from trivial. The broken-symmetry DFT methodology used here, flips individual spins on atoms and converges to broken-symmetry SCF solutions with localized alpha and beta spins on different atoms. These BS states likely correspond well to some of the low energy electronic states of FeMoco, but the methodology cannot capture the full multiplet spectrum of such a complex spin-coupled metal-sulfur cluster. Additionally, as discussed in recent multiconfigurational wavefunction theory studies, simplified model Hamiltonians (Heisenberg and Double Exchange Hamiltonians) are likely too simple to give a realistic description for spin-coupled iron–sulfur systems,67 preventing the use of spin-projection schemes. For the resting state, the BS7 class of solutions (that appears to maximize antiferromagnetic interactions) has been consistently found to be most favourable in multiple studies56,58–71. The three BS7 solutions, here labelled according to which Fe ions are spin-down (crystal structure numbering): BS-235, BS-346 and BS-247 have been found to be within ~1 kcal mol−1 of each other (QM/MM-TPSSH level of theory) and in previous work13 we found that the BS-235 solution was in better agreement with the crystal structure than the other spin isomers. As E0 is a different redox state, however, the spin coupling may well have changed completely due to binding of hydrides and in fact the experimental spin state changes from S = 3/2 (E0) to S = 1/2 (E4). Thus a similar BS state to the one in E0 cannot simply be assumed to apply to E4. Cao et al.27 have shown, however, in their work where many different E1–E4 models were considered (featuring many of the models studied herein) that the BS solutions that are consistently lowest in energy are the BS7 class of solutions, thus supporting the hypothesis that maximizing antiferromagnetic coupling remains important, even when hydrides are bound. In this work we have primarily considered the BS7 solutions (BS-235, BS-346 and BS-247) as the most relevant broken-symmetry solutions as well as the BS-147 solution. The BS7 solutions are similar in energy and feature a very similar electronic structure in the resting state E0 (as discussed in ref. 11 and 13); the differing positions of spin-down Fe atoms though has the effect of changing the iron oxidation state at each site, as the mixed-valence pairs or localized ferric/ferrous iron will then involve different atoms in the structure. This local oxidation state interpretation of the different broken-symmetry states has been previously discussed.11,114–115 A BS-147 solution features ferromagnetic alignment of atoms Fe2 and Fe6. As some of the models in this study feature structural changes at these Fe ions, it seems possible that such a solution could become more favourable than other BS solutions. To aid in the computational problem involving many models and many BS states at an expensive level of theory, we have restricted ourselves to
performed geometry optimizations with the BS-235, BS-247, BS-346, BS-147 solutions to explore the energetics of all models in Fig. 2. We additionally explored all 35 BS solutions of two models (I and o) at the single-point level (see ESI, Fig. S5 and S6† respectively). All models assumed a final $M_s = 1/2$ spin state, consistent with the experimental $S = 1/2$ spin state of $E_4$.

B. QM/MM calculations of models of the $E_4$ state

Fig. 2 shows the molecular structures of various proposed $E_4$ models from previous work and new ones, featuring a variety of hydride binding modes and/or sulfide/carbide protonation scenarios. We are aided here by the work of Cao et al., who performed a systematic study of a large number of protonation positions in the $E_0$–$E_4$ redox states. Thus, we have included the most stable $E_4$ models found in their study (the study lacks, however, open sulfide-bridge models) according to the levels of theory employed in their study (TPSS and B3LYP), as well as models from other groups. All models, shown in Fig. 2, can be grouped according to whether they contain a protonated carbide (model a, c and d), whether they feature terminal/bridging hydrides with an intact sulfide bridge (models e, f, g and h) or whether they feature hydrides with an open sulfide bridge in the form of a terminal sulfhydryl group (models b, i, j, k, l, m, n, o).

Models n, m and o were previously discussed as models close in energy to the favoured model e in work by Raugei et al. In this study we introduce models I and model o (though a model like o has been discussed by Raugei et al.24) as plausible candidates for $E_4$ as well as models j and k, being similar to models m and n, and model b featuring two terminal sulfhydryl groups and two bridging hydrides. Model i also has a terminal sulfhydryl group like i but has a different sulfide protonation state.22 The models with a terminal sulfhydryl group at Fe$_2$/Fe$_6$ (rather than at Fe$_3$/Fe$_5$ or Fe$_5$/Fe$_7$) seem consistent with crystal structures of ligand-bound states12,31 lacking S2B (that bridges Fe$_2$ and Fe$_6$), suggesting some lability of this particular sulfide bridge. Fig. 2 and Table 1 contains data for the lowest energy BS solution but data for all broken-symmetry solutions can be found in Tables S1–S5† along with Mulliken spin populations for each state.

As shown in Fig. 2 and Table 1, the relative energies (polarized QM energies at QM/MM geometries) at the TPSSH level of theory indicate models featuring protonated carbides (a, c, d) are strongly disfavoured, appearing much too high in energy (17–32 kcal mol$^{-1}$ higher in energy than the lowest energy model n) to be likely candidates for the $E_4$ state. Additionally, models e, f, g, h, featuring an intact sulfide bridge also appear rather high in energy ranging from 13–22 kcal mol$^{-1}$. Only open sulfide bridge models, j–o, featuring a terminal sulfhydryl group...
Table 1  Calculated relative energies (kcal mol\(^{-1}\)) of the E\(_\text{4}\) models investigated (shown in Fig. 2) with different functionals, with the lowest energy broken symmetry solution indicated for each model. For TPSSH, both the polarized QM energies (MM point charges included in the QM calculation) and total QM/MM energies are given. Single-point (polarized) QM calculations with TPSS, B3LYP and M06-2X used the TPSSH geometries. See Tables S2–S5 in the ESI for data on all BS solutions calculated.

<table>
<thead>
<tr>
<th>TPSSH Model (BS-state)</th>
<th>Single-point QM energies (E_{\text{QM}}) (kcal mol(^{-1}))</th>
<th>Single-point QM energies (E_{\text{QM/MM}}) (kcal mol(^{-1}))</th>
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<tbody>
<tr>
<td>a (147)</td>
<td>31.46</td>
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<td>b (247)</td>
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<td>17.66</td>
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<tr>
<td>d (147)</td>
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<td>g (346)</td>
<td>21.80</td>
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<td>13.02</td>
</tr>
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</tr>
<tr>
<td>o (147)</td>
<td>2.48</td>
<td>2.25</td>
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</table>

at Fe\(_2\) or Fe\(_6\) are found to be similarly low in energy, suggesting that it is generally thermodynamically favourable to alter the coordination of a protonated sulfide bridge to aid stabilizing hydrides (bridging, terminal or dihydrogen-like). Model b with two open sulfide bridges is an exception to this trend. This energetic analysis suggests that models j–o are the most viable models for the E\(_4\) state (at the TPSSH-QM/MM level). Open sulfide-bridge models like j–o were not considered in the study by Cao \textit{et al.}\(^{27}\) but some open-sulfide bridge models were discussed by Raugei \textit{et al.}\(^{24}\) and were found to be similar in energy to model e, which, however, is not in agreement with our results. We attribute this disagreement to different modelling aspects, i.e. cluster modelling vs. QM/MM modelling, as well as BS-solution dependence and functional dependence, which will be discussed in the next section.

C. Computational protocol dependence

As has recently been discussed in the literature, by Raugei \textit{et al.}\(^{24}\) and especially by Cao \textit{et al.}\(^{27,27}\) there is a considerable functional dependency present in calculations of FeMoco, affecting e.g. whether carbide protonation is favoured or not, or the structure of FeMoco. Thus, when hybrid density functionals with $\approx20\%$ HF exchange such as B3LYP (20\% HF exchange) and M06-2X (54\% HF exchange) have been used in the computational protocol, carbide protonation models have been found to be favoured over models with only hydrides. This is at odds with our relative energy comparison at the TPSSH level (10\% HF exchange), shown in Fig. 2. We have been able to confirm some of this behaviour by performing single-point energy calculations using these functionals with the TPSSH-optimized geometries. As shown in Table 1, the energy comparison of models is dramatically altered when these hybrid functionals are considered. Meanwhile, results from the non-hybrid functional TPSS are more similar to the TPSSH results. As an example of this strong functional dependency, model e (a protonated carbide model found in the study by Cao \textit{et al.}), is predicted to be only $\sim2.5$ kcal mol\(^{-1}\) higher in energy than the lowest energy model (m) at the B3LYP level of theory but $\sim17$ kcal mol\(^{-1}\) higher in energy than the lowest model (n) at the TPSSH level of theory. Structural optimization at the same level of theory would likely further stabilize model c. This effect of using a higher HF exchange hybrid is further magnified when using the M06-2X functional (having 54\% HF exchange); this even leads to model c becoming the most stable model as seen in Table 1 (and the energy gap between models becoming 114 kcal mol\(^{-1}\)). The M06-2X functional has been used to suggest carbide protonation as an important aspect of the mechanism.\(^{29}\)

The large energy changes seen for different functionals echo the results of Cao \textit{et al.}\(^{27}\) We also note the pronounced sensitivity w.r.t. which BS-solution is calculated (see Tables S1–S2\(^{\text{†}}\)), underlining the importance of studying multiple BS states in calculations of FeMoco. Such a large functional dependency of the relative energies (even when the same TPSSH geometries are used) naturally calls into question the reliability of the DFT calculations to distinguish energetically between E\(_4\) models of these complex systems. In fact, these results strongly suggest that the different functionals are describing the electronic structure of the FeMoco E\(_4\) state very differently. Such a different description of electronic structure with different functionals for FeMoco in the E\(_4\) state should be apparent in the E\(_0\) state as well (despite an absence of hydrides and protonated sulfides/carbide). In fact, when different functionals are used to describe the electronic structure of FeMoco in the E\(_0\) state, there are notable differences in the spin populations and isosurface plots of the spin density (see ESI, Fig. S13 and S14, Tables S9 and S11\(^{\text{†}}\)). These differences can partly be attributed to the differing delocalization of electrons in FeMoco as well as the strength of Mo–Fe interactions (as discussed in previous studies the Mo electrons are partially delocalized towards the Fe ions, suggesting some Mo–Fe bonding\(^{2,4,11,13}\)). A functional such as B3LYP for example shows a slightly more localized description of unpaired electrons in FeMoco and this effect is magnified
when going to functionals with more HF exchange like BHLYP or M06-2X. In fact, when QM/MM geometry optimizations of the E₀ state are performed with hybrid functionals with HF exchange \( \geq 20\% \) (such as B3LYP, BHLYP and M06-2X), large structural changes occur. This can be seen for Mo–Fe, Fe–Fe and Fe–C distances in Fig. 3 which shows the mean deviation of specific atom–atom distances w.r.t. crystal structure (more data available in the ESI, Fig. S10–S12†). Especially noteworthy is the up to 0.8 Å deviation seen for the Mo–Fe₁ distance (see ESI, Fig. S10†) that suggests that the basic structure of the cofactor is very badly described at some of these same hybrid levels. As discussed further in the ESI† the largest structural deviations involve Mo–Fe distances, and for BHLYP and M06-2X, this can be attributed to a completely different electronic structure on the molybdenum, giving rise to a high-spin Mo(IV) instead of the non-Hund Mo(III) configuration. The oxidation state of Mo as Mo(III) in FeMoco is now firmly established from Mo K-edge and L-edge XAS spectroscopy and theoretical calculations.⁸,⁹ Additionally, the unusual spin-coupled non-Hund Mo(III) configuration, first proposed by theoretical calculations⁸ has now experimental support via recent Mo L-edge and XMCD spectra.¹⁰ Thus, computational protocols giving rise to long Mo–Fe₅/Fe₆/Fe₇ distances (>3 Å) by stabilizing a high-spin Mo(IV) ion are not only incompatible with the experimental molecular structure data (high resolution crystallography) but experimental electronic structure data (XAS and XMCD) as well. The QM/MM B3LYP results in Fig. 3 and the ESI† show considerable deviations with respect to the crystal structure (though not as large as the BHLYP and M06-2X results); however, this effect is further magnified if the QM/MM model is replaced by a simpler cluster model instead. The B3LYP cluster model data shown in the figures are from Siegbahn⁸⁸ and give deviations as bad as the BHLYP and M06-2X QM/MM data. As shown in the ESI† there are also dramatic changes in the electronic structure of the B3LYP cluster model, especially regarding the oxidation state of Mo, again indicating a Mo(IV) oxidation state. It is also worth noting that overestimated Fe–C bond lengths (suggesting destabilized Fe–C chemical bonds) are seen from functionals/protocols that show more favourable carbide protonation according to Table 1 and these functionals/protocols have been used in studies that suggest carbide protonation occurring in reduced states of FeMoco. The non-hybrid functionals, BP86 and TPSS, give structures in better agreement with the experimental crystal structure (though showing underestimation of distances instead of overestimation). TPSS shows relative energies of E₁ models more similar to TPSSh than the hybrid functionals, at least regarding the stability of carbide-protonation models. FeMoco is thus an interesting example of where there is quite a strong relationship between electronic structure (and hence reaction energies) and molecular structure.

The good agreement seen between our TPSSh-QM/MM E₀ structure and the high resolution crystal structure of E₀ strongly suggests that we are describing the electronic structure of the system more correctly with TPSSh, clearly much better than the higher exchange hybrids and also better than non-hybrid functionals such as BP86 and TPSS. We note that our calculations include dispersion corrections, a large polarized triple-zeta basis set (on the cofactor) that should be close to the basis set limit, as well as scalar relativistic effects (via ZORA) and we account for the explicit protein environment from the beginning; the good agreement seen with our TPSSh calculations should thus primarily be due to a more correct description of the electronic structure rather than being due to accidental

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![Graph](https://www.sciencedirect.com/science/article/pii/S2040167119302158)  
**Fig. 3** Mean deviations (Å) of Fe–Fe, Mo–Fe, Fe–C, Fe–S and Mo–S distances of resting state FeMoco (relative to crystal structure), calculated with various functionals using the same QM/MM protocol. Also shown is a B3LYP cluster model from Siegbahn.⁸⁸
error cancellations of both model and method errors. Whether this ability to describe the resting state FeMoco well, carries over to describing the relative stability of hydrides and protonation of a metal-carbide is not as clear. We note though that the TPSSh functional has been shown to be a reliable functional for many problems in inorganic and bioinorganic chemistry giving both good structures\(^7\) and reaction energies.\(^6\) It appears most likely to us that the higher HF exchange in hybrids such as B3LYP, BHLYP and M06-2X is responsible for introducing severe artifacts in the basic electronic structure of FeMoco, that would carry over to the description of all redox states. Results from these functionals, such as a tendency to favour protonated carbides (not found with functionals that describe the E\(_0\) structure well), should therefore be regarded with high suspicion, in our view, as 20% or higher HF exchange appears to destabilize metal–ligand and metal–metal bonding in FeMoco (resulting even in a wrong Mo oxidation state) that is arguably crucial to its reactivity.

In our view, the relative energy comparison at the TPSSh level is at this point the most reliable as only this level of theory describes the electronic structure of the cofactor accurately in the resting state. This comparison indicates E\(_4\) models j–o as the most energetically favourable E\(_4\) models. We note that the stability of such open sulfide-bridge models is for the most part also found at the non-hybrid level of theory (TPSS) while the higher HF exchange hybrids predict a very different energy landscape. Geometry optimizations with these hybrid functionals (B3LYP, M06-2X) would no doubt further change the energy landscape of E\(_4\) models (likely further stabilizing protonated carbide models), however, this would not lead to any useful comparison, in view of the aforementioned electronic structure artifacts.

Thus, models j–o appear to be viable choices for the E\(_4\) state of FeMoco. We hesitate to distinguish further between these models based on their energetics. There is ample uncertainty regarding the reliability of relative energies with our DFT level of theory but it is also worth noting that the E\(_4\) state is thermodynamically not stable with respect to H\(_2\) formation (that leads back to the E\(_2\) state) according to experiments. The E\(_4\) state must then be a state that is kinetically trapped behind a barrier, and not necessarily at the lowest energy configuration (prior to H\(_2\) dissociation). The E\(_4\)-n model is the lowest in energy according to our energetic comparison but this is a state where H\(_2\) has already formed, bound to Fe\(_2\) with a Kubas-type metal-dihydrogen geometry. Our calculations indicate an almost barrierless H\(_2\) dissociation from this state (a path leading to the E\(_2\) redox level) and this H\(_2\) formation (involving hydrides) would thus occur without N\(_2\) involvement which is inconsistent with isotope-substitution experiments. Those experiments showed that N\(_2\) is necessary for H\(_2\) formation via the hydrides (criterion iii from Section A.). Additionally, the E\(_4\)-n model does not feature bridging hydrides, at odds with the structural interpretation of the ENDOR studies (criterion i from Section A.). The E\(_4\)-n state, while energetically favourable, may thus be a state never formed under experimental conditions, it most likely represents an alternative path towards E\(_4\)–E\(_2\) relaxation, but likely one that would not be seen experimentally.

If we focus on models that seem broadly consistent with the ENDOR proposal of two almost chemically equivalent bridging hydrides then models E\(_4\)-l and E\(_4\)-o (see Fig. 4) appear to be the most appealing models as these models feature two almost equivalent hydrides with considerable bridging character. These two models are also among the most thermodynamically stable models according to our TPSSh protocol and there is very likely a kinetic barrier towards H\(_2\) formation involving these hydrides that could be affected by N\(_2\) binding, making a reductive elimination step possible.

On the other hand, model E\(_4\)-c has been previously suggested by Hoffman and coworkers to be a structure that is consistent with the ENDOR data. In a very recent study,\(^{25}\) a case was made for this model being in the best agreement with even higher resolution ENDOR data while a structure similar to model E\(_4\)-o was considered less likely. This comparison was based on calculated hyperfine tensor orientations with a simplified point-dipole approximation where the metal ions are assumed to all be high-spin and to behave as localized “spherical balls of spin”. The latter seems questionable, in our view, considering the strong delocalization of electrons seen in calculations of FeMoco and we also note that calculated spin populations of almost all E\(_4\) models (including E\(_4\)-l, E\(_4\)-o and E\(_4\)-c, see Tables S2–S5†) show reduced spin populations on some Fe ions, calling into question the high-spin nature of all Fe ions in the E\(_4\) models. A direct calculation of the \(^{1}\)H hyperfine tensors of the hydrides of these models via multireference wavefunction theory may in fact be required to confidently tell apart models based on the hyperfine tensors. Such calculations are unfortunately still out of reach but may become possible in the near future. Our QM/MM calculations of E\(_4\)-c do not suggest the state as a thermodynamically favourable model for the E\(_4\) state compared to open-sulfide bridge models (with no functional tested). Further studies will be required to determine whether such a model could be favourable under some conditions or even whether such a model represents a kinetically trapped state.

The energetically favourable E\(_4\)-l and E\(_4\)-o models (at TPSSh level of theory), featuring bridging hydrides (in agreement with ENDOR analysis), will be studied further in the next section. The energy surface and barriers that connects all of the states j–o will be reported on later; at present it is not clear whether all of these states are accessible to each other and this requires careful mapping of the minimum energy paths between them.

D. Molecular and electronic structure of E\(_4\)-l and E\(_4\)-o

The two models E\(_4\)-l and E\(_4\)-o both feature the same bridging hydride structure with the hydrides between Fe\(_5\) and Fe\(_6\) but the models differ in the position of the terminal sulphydryl group (Fe\(_2\) vs. Fe\(_8\)) derived from sulfide S2B (Fig. 4). Sulphide SSA is also protonated in these models but remains bridging. The two hydrides in these models are mostly but not completely bridging between Fe\(_5\) and Fe\(_6\). For model E\(_4\)-l, both hydrides are slightly more associated with Fe\(_8\) (Fe\(_8\)–H distances of 1.61 and 1.63 Å) than Fe\(_5\) (Fe\(_5\)–H distances of 1.73 and 1.67 Å) and for model E\(_4\)-o, we see similarly stronger binding to Fe\(_8\) as well,
with Fe$_2$–H distances of 1.61 and 1.59 Å and Fe$_3$–H distances of 1.71 and 1.74 Å. The coordination of these two new ligands to Fe$_2$ and Fe$_6$ change the geometry of these Fe ions from approximate tetrahedral to five- and six-coordinate geometries (distorted octahedral geometries), which naturally has a pronounced effect on the electronic structure of both Fe ions. In fact, the electronic structure of the two models reveal a change in the local spin state of both Fe ions in the lowest energy solution found for both, BS-147. With hydrides known to act as strong-field ligands and the change in four-coordinate local tetrahedral geometry to five or six-coordinate geometry this is perhaps not surprising. The change in local spin state is revealed in the change of spin population at Fe$_2$ and Fe$_6$ (from >3 to 2.4–2.5, see Table S6f for spin populations) and the localized orbitals reveal more clearly spin-pairing occurring at Fe$_2$ and Fe$_6$. The electronic structure appears consistent with intermediate spin $S = 3/2$ Fe($n$) ions but this will require further study. In this context it is worth noting that such a double-hydride bridging geometry between two Fe ions has precedent in the form of synthetic dimeric Fe compounds from the groups of Peters$^{27}$ and Holland$^{38}$ though these synthetic compounds have a planar Fe–H–Fe–H geometry.

A bridging hydride structure, with two hydrides between Fe$_2$ and Fe$_6$, has also been discussed by Einsle and coworkers as a possible E$_4$ structure.$^{35,39}$ However, that structure assumed an absent sulfide, in line with the hypothesis that the sulfide S2B leaves to open up a binding site, as crystal structures have shown that the sulfide can be displaced by CO or NH/OH.$^{13,33}$ Importantly, in our E$_4$ models, the S2B sulfide is protonated and remains present as a terminal sulhydryl group on either Fe$_2$ or Fe$_6$. Dance has recently explored the thermodynamic feasibility of completely dissociating S2B in the form of SH$^{-}$ or H$_2$S and found it not to be favourable$^{40}$ and our own preliminary results suggest this as well. It is presently not clear under what conditions (or when in the cycle) complete sulfide removal from the cofactor (as shown by the crystal structures) occurs.

Based on the similarity of models E$_4$-I and E$_4$-o in terms of structure and energy, we cannot easily distinguish between them. Both appear reasonable candidates for the E$_4$ state; only one of them may be formed under turnover conditions, however, and this may depend on the precise way that protons and electrons get introduced into the active site. Unfortunately, these mechanisms are not well established.

**E. Dinitrogen binding to E$_4$-I and E$_4$-o**

With the change in coordination by introduction of bridging hydrides, one of the Fe ions in each state is coordinately unsaturated with respect to a six-coordinate octahedral geometry. This makes N$_2$ binding to Fe$_4$ (in E$_4$-I) or Fe$_5$ (in E$_4$-o) a feasible scenario. In fact the synthetic Fe($n$)–(μH)$_2$–Fe($n$) dimer featured a bound N$_2$ ligand on one of the Fe ions and 1-electron reduction to give a Fe($n$)–Fe($i$) dimer resulted in a large increase in the binding affinity of a second N$_2$.$^{77}$ There is thus precedent for a similar bridging-hydride dimer structure to be capable of favorable N$_2$ binding.

We explored N$_2$ binding to the empty coordination site at Fe$_2$/Fe$_6$ for both E$_4$-I and E$_4$-o models to give N$_2$-bound models E$_4$-I-N$_2$ and E$_4$-o-N$_2$ (shown in Fig. 5). N$_2$ binding is found to be thermodynamically favourable (w.r.t. free N$_2$) for both E$_4$-I (bound to Fe$_2$) and E$_4$-o (bound to Fe$_2$) states, with an electronic binding energy of $\Delta E = -13.5$ kcal mol$^{-1}$ for the E$_4$-I-N$_2$ state and a slightly weaker binding of $\Delta E = -10.2$ kcal mol$^{-1}$ is found for the E$_4$-o-N$_2$ state. We note that accounting for translational entropy (10.7 kcal mol$^{-1}$ based on gas phase statistical mechanics) would reduce these electronic binding energies by that amount, leading to slightly endothermic 0.5 kcal mol$^{-1}$ binding for E$_4$-o and exothermic 2.8 kcal mol$^{-1}$ for E$_4$-I. Different broken-symmetry solutions (BS-235, BS-346, BS-247 and BS-147) were tested for the N$_2$-bound states E$_4$-I-N$_2$ and E$_4$-o-N$_2$ that turned out to be crucial, as the energies of different states differed by up to 14 kcal mol$^{-1}$ (see ESI, Table S6f), with some BS states not showing favorable N$_2$ binding. For E$_4$-I-N$_2$ and E$_4$-o-N$_2$ models, the BS-235 and BS-346 solutions were lowest in energy, respectively. We note that these results are in sharp contrast with a recent study by Raugei et al.$^{24}$ that found N$_2$ binding (in a bridging geometry between Fe$_2$ and Fe$_6$) to be endothermic by 5 kcal mol$^{-1}$ ($\Delta E$).

N$_2$ binds end-on to Fe$_2$/Fe$_6$ in these E$_4$-I-N$_2$ and E$_4$-o-N$_2$ structures resulting in an unusual distorted octahedral geometry at the participating Fe. This favorable binding of N$_2$ to a FeMoco redox state is notable; N$_2$ will unsurprisingly not bind to FeMoco at the E$_0$ redox level in our calculations (no minimum found) but the same applies to a 1-electron reduced state. Our model for the E$_4$ redox state (one of two favoured models from a recent joint EXAFS-QM/MM study$^{45}$) involves an added electron to the [MoFe$_3$S$_3$C] sub-cubane and a protonated S2B sulfide bridge (multiple BS states with $M_S = 2$ were calculated). Even when the E$_1$-N$_2$ optimization is started from a structure with a terminal sulhydryl group bound to Fe$_2$ and N$_2$ in close proximity to Fe$_6$, then N$_2$ spontaneously dissociates. Thus neither 1-electron reduction of the cofactor or protonation of the sulfide bridge alone is sufficient for favorable N$_2$ binding to occur at the cofactor. N$_2$ will also not bind favorably to other Fe ions in the E$_4$-I model; while a stable minimum is found when N$_2$ is placed at Fe$_7$, the binding is endothermic ($\sim$5.5 kcal mol$^{-1}$).
These results suggest that the hydride ligands at Fe₂ and Fe₆ in E₄-l and E₄-o are responsible for the favorable formation of the N₂-binding states, E₄-l-N₂ and E₄-o-N₂, likely due to the unique ligand-field now found at these Fe ions. In support of this, we have also calculated a model for the E₂ state of FeMoco, analogous to E₄-l (with a sulphydryl group at Fe₂) but with only one bridging hydride between Fe₂ and Fe₆. This state (BS-235 and Mₛ = 3/2) interestingly features favorable N₂ binding (ΔE = -6.9 kcal mol⁻¹), about half of the binding energy to the E₄-l state. The calculated N₂ binding of this E₂ model may, however, not be enough to overcome entropy and implies that the presence of two hydrides at the same Fe may be required for favorable dinitrogen binding.

Electronic structure aspects of dinitrogen binding of FeMoco will be explored in more detail in a future study. Our current interpretation of the electronic structure behind the favorable Fe₆–N₂ binding in the E₄-I→E₄-I-N₂ step is that the low-spin configuration found at Fe₆ in E₄-I-N₂ (spin population of 0.46) is a vital aspect of the N₂ binding. The localized orbital analysis of Fe₆ in E₄-I-N₂ reveals that this iron can be interpreted as a low-spin octahedral S = 1/2 Fe(III) ion with doubly occupied dₓz and dᵧz orbitals. This low-spin configuration must arise via the strong-field hydride ligands as well as due to the N₂ ligand.

As is now well established from experiments, H₂ is eliminated from the E₄ state as N₂ binds, via a reductive elimination mechanism involving the hydrides.⁴⁻¹⁻²¹ Due to the proximity of

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**Fig. 5** N₂ binding of E₄-I and E₄-o models compared to models of earlier redox states according to QM/MM calculations. The E₂ model features a 1-electron reduced FeMoco (Mₛ = 2) with S2B protonated while the E₄ model (BS-235, Mₛ = 3/2) is analogous to the E₄-I model with a bridging hydride between Fe₂ and Fe₆ and a terminal sulphydryl group on Fe₂. N₂ binding energies (kcal mol⁻¹) are relative to free N₂ and are electronic energies. Accounting for translational entropy, (10.7 kcal mol⁻¹, based on gas phase statistical mechanics), would decrease the binding energies by that amount.
the two hydrides in the E4 and E4-N2 models discussed in the
previous chapters, one can imagine how such a reductive
elimination step could proceed from our models. Isotope
substitution experiments indicate that H2 evolution via reduc-
tive elimination can only proceed in the presence of N2.
Experiments performed in the absence of N2 indicate that a
regular hydride-proton reaction is responsible for the H2
formed from the E4 state (leading to the unproductive E4→E2
side-reaction). This implies that as N2 binds to the E4 state,
either the H2 formation via reductive elimination is favoured
thermodynamically over a hydride-proton reaction or it is
kinetically favoured by lowering of the barrier for reductive
elimination (relative to a hydride-proton reaction).

A future study will explore in detail the reaction barriers for
H2 formation via both reductive elimination and hydride-
proton mechanisms from our E4 models. However, there is
a simple argument in favour of reductive elimination over
a more normal hydride-proton reaction that applies to both E4-I-
N2 and E4-o-N2 models. The simplest hydride-proton reaction
would involve combining one of the bridging hydrides with the
proton from a sulphydryl group (the closest accessible proton).
The required deprotonation of the terminal sulphydryl group
(to act as proton donor) would be highly unfavoured as the
terminal deprotonated sulfide is prevented from recombining
with Fe6/Fe2 to reform the sulfide-bridge due to the presence
of the other hydride in this position (in fact, calculations indicate
such a step to be uphill by 15.1 kcal mol\(^{-1}\)). The dinitrogen
ligand would furthermore block a hydride-proton pathway
involving the hydroxy proton from the Mo-bound homocitrate
and possibly other proton donors. The molecular structures of
the E4-I-N2 and E4-o-N2 models thus appear to offer an intuitive
explanation for why the reductive elimination step can only
occur in the presence of N2. Without the N2 ligand (i.e. in the
absence of N2 gas), a hydride-protonation reaction (i.e. a E4→E2
step) should be more likely to occur, probably due to a lower
barrier of a hydride-proton reaction compared to a hydride–
hydride reaction. This could occur e.g. by hydride protonation
via the hydroxy group on Mo-bound homocitrate or via the
sulphydryl group (and a possible transformation of the
remaining bridging hydride to a terminal hydride and refor-
mation of the sulfide bridge). With the N2 ligand present,
however, reductive elimination could be the only favoured H2
evolution pathway.

This reductive elimination step involving two hydrides
(formally storing four electrons) releases two electrons in the
form of H2 and makes two electrons now available to the
cofactor in states we call E4-I-N2 and E4-o-N2 (see Fig. 6). Our
calculations predict an electronic energy change (\(\Delta E\)) of
+3 kcal mol\(^{-1}\) uphill. While this step is predicted to be mildly
endothermic according our calculations, this result is not in
strong disagreement with experiment. In fact, kinetic studies
show this step to be reversible,\(^a\) meaning the step is close to
thermoneutral. Additionally, the translational entropy contri-
bution to the free energy would favour the elimination of H2. We
have opted for not adding gas phase translational entropy
corrections (\(-8.4\) kcal mol\(^{-1}\) for H2 elimination) to our energies
as the entropic contribution could be more complicated for

- a complex condensed phase macromolecular system such as
  nitrogenase (as has been discussed by Reither and coworkers\(^b\)),
  however, the entropy contribution would likely be the same
  magnitude as the gas phase value. The fact that the
  E4-N2→E4-N2\(^*\) step is predicted to be close to thermoneutral
  (\(\Delta E\)) according to our calculations is due to the nature of the
  reductive elimination. A regular H2 formation step should be
  quite exothermic (our calculations for hydride-proton reactions
  for an E4→E2 predict exothermicity of \(-20\) kcal mol\(^{-1}\)).
  The lack of strong exothermicity for E4-N2→E4-N2\(^*\) step stems
  from the fact that the metal cofactor is reduced (by 2 electrons)
during the reaction, as previously the four electrons were stored
in the form of the hydrides and two leave in the form of H2. This
rather unfavorable two-electron reduction of the metal cofactor
may thus be offset via the exothermicity of the H2 formation.

The molecular and electronic structure of the E4-I-N2\(^*\) and the
E4-o-N2\(^*\) states is thus of interest as the metal ions of the cofactor
are now more reduced than before and the structures lack the
hydrides that previously helped bind N2. The local Fe geome-
tries of the Fe2/Fe6 ions in E4-I-N2 and E4-o-N2\(^*\) are unusual. A
terminal sulphydryl group is still present on Fe2 or Fe6. Attempts
reform the sulfide bridge (with sulfide still protonated) were
not successful as the system returns to a geometry with the
terminal sulphydryl group. Clearly, the distorted geometries at
Fe2/Fe6 are stable, though this is presently not well understood.
Using the \(t_1\) and \(t'_1\) structural metrics\(^c\) for 4-coordinate
compounds, we find that the Fe2 and Fe6 in both E4-I-N2 and
E4-o-N2\(^*\) models are about halfway between a tetrahedral
geometry and a seesaw geometry (see ESI, Tables S7 and S8,\(^\dagger\)
for calculated \(t_1\) and \(t'_1\) parameters for all Fe ions in multiple E4
models). We note that such geometries have previously been
found in DFT calculations of FeMoco.\(^e\)

Analysis of the electronic structure suggests that the dis-
torted N2-bound Fe2\(^\*\) in E4-o-N2\(^*\) can be described as an \(S = 1\)
Fe(iii) ion. However, remarkably, the distorted Fe6\(^\*\) in E4-I-N2\(^*\)
best fits the description of an \(S = 3/2\) Fe(i) ion according to the
localized orbitals (see ESI, Fig. S9\(\dagger\)), revealing a stark difference
between the two states and the nature of the different binding
site. Both E4-I-N2 and E4-o-N2\(^*\) states feature doubly occupied \(d_{yz}\)
and \(d_{xz}\) orbitals that likely account for the favorable dinitrogen
binding via metal backbonding (similarly to the E4-I-N2 and E4-
o-N2\(^*\) models despite the absence of hydrides).

While distinguishing between the E4-I and E4-o pathways is
not quite clear based on the calculated energies, it is tempting
to attribute the presence of Fe(i) in E4-I-N2\(^*\) as a potentially
important aspect of the mechanism when going forward. The
interpretation of the reductive elimination is then that the
electrons in the reductive elimination step are used to reduce
the N2-binding Fe6\(^\*\) ion to an Fe(i) ion. Compared to the resting
state \(E_0\), the mixed-valent delocalized Fe6(2.5)–Fe2(2.5) pair has
then been reduced to a pair of localized Fe5(1) and Fe3(2) ions.
Thus, the reductive elimination step could be imagined as a
specific mechanism towards stabilizing an Fe(i)–N2 species
without going to the strongly negative potentials such as those
required for mononuclear complexes. Indeed, low-valent
mononuclear iron complexes from Jonas Peters and
coworkers have been found to act as catalysts for N2 reduction;
A possible subsequent protonation step of N2 intermediates group and the hydroxy group, we get lower-energy diazene transfer step is calculated, however, using both the sul group of homocitrate, reforms the sulfide bridge between Fe2 and Fe6 to form diazene-bound intermediates **E4-l-NH**2 or **E4-o-NH**2 at either Fe2 or Fe6.

The nitrogem of either free N2 and by the decrease in N–N potential of the Fe protein. Access low (Fe(I), Fe(0) and Fe(II)) oxidation states that bind and active N2. Reductive elimination could thus enable reduction of an Fe ion to Fe(i) while using the same low potential of the Fe protein.

The N2 ligand in **E4-l-N2** and **E4-o-N2** is only weakly activated as seen in a small increase in N–N bond length of 0.021 and 0.023 Å for **E4-l-N2** and **E4-o-N2** respectively, when compared to free N2 and by the increase in N–N vibrational frequency of 242 and 255 cm\(^{-1}\) for **E4-l-N2** and **E4-o-N2** respectively, when compared to free N2. The N2 activation is greater than in the **E4-l-N2** and **E4-o-N2** models (N–N bond length shifts of 0.014 and 0.017 Å and frequency shifts of 172 cm\(^{-1}\) and 202 cm\(^{-1}\)). A high-spin Fe(i)–N2 complex was first synthesized by Harman and coworkers. Unlike the **E4-N2** states proposed here, the synthetic Fe(i)–N2 complex has C\(_{3v}\) symmetry and the dinitrogen activation is stronger with a N–N stretching frequency shift of 372 cm\(^{-1}\) compared to free N2.

While activation of the N2 ligand in the in **E4-l-N2** and **E4-o-N2** states is thus still considered weak, and protonation might be considered unlikely, we tested simple protonation reactions by transferring nearby protons to the nitrogen atoms of the ligand. Two possible protonation agents seem likely, one being the terminal sulphydryl group on Fe2/Fe6 and the hydroxy group of homocitrate, reforms the sulphydryl group and hydroxy group of homocitrate, reforms the sulfide bridge between Fe2 and Fe6.

While this intermediate is still unprotonated, **E4(2N2H)** by Hoffman and coworkers and discussed as “a state in which FeMo-co binds the components of diazene, which may be present as N2 and two [e\(^-\)/H\(^+\)] or as diazene itself” EPR and ENDOR studies of this same intermediate showed \(^{15}\)N hyperfine coupling (using \(^{15}\)N2) but no hyperfine coupling from hydrogens was seen. A single \(^{15}\)N hyperfine signal was found, suggesting end-on binding which fits well with our **E4-o-N2** models. A recent EPR/ENDOR study of synthetic mononuclear Fe–N2 compounds by Peters and coworkers of states featuring either a single and double protonated N2 ligand: Fe–N2H and Fe–N2H\(_2\) (distal protonation) revealed a clear hyperfine signal from the hydrogens. These experiments may thus be an indication that the experimental dinitrogen-bound intermediate, “**E4(2N2H)**” is still unprotonated. Based on our computational modelling, it is possible that the experimental intermediate “**E4(2N2H)**” could correspond to the **E4-l-N2** model (or possibly **E4-o-N2**) rather than a diazene-bound intermediate like **E4-l-NH**2/**E4-o-NH**2. An alternative explanation is that the hyperfine couplings from the hydrogens in a diazene intermediate may be too weak to be measured. Additional spectroscopy is required to clarify the nature of this intermediate.

**Conclusions**

We have presented QM/MM calculations of possible models for the Fe4 state of nitrogenase and how dinitrogen can bind to some...
of these models. In view of the thermodynamic stability of our model for the E_4 state and the favourable dinitrogen binding we have presented, our work looks promising as a step towards a mechanistic understanding of biological dinitrogen reduction. Questions remain about the reliability of calculated reaction energies for this complicated cofactor and a stronger connection to experiment would be much desired, requiring more spectroscopy on nitrogenase intermediates.

In this context, we should note that a recent ENDOR study^{25} combined with calculations has presented evidence in favour of another model (model e in article) as the structure of the E_4 state. Our QM/MM calculations of that model suggest it to be higher in energy than all open-sulfide bridge models (with all calculated functionals) and this model has not been found to bind dinitrogen favorably.^{24} Additional spectroscopic data on the E_4 state to sort out this disagreement would therefore be desirable.

Our proposed mechanism for binding of dinitrogen and reductive elimination suggests a role for many of the components of the complicated cofactor of nitrogenase. The size of the cofactor and the nature of the fused iron–sulfur double-cubane may play a primary role of favourably accepting electrons and storing them as hydrides at the same potential as provided by the Fe protein; the stability of the hydride geometries being facilitated by a labile sulfide bridge between cubanes. Furthermore, our calculations suggest the strong-field nature of the hydrides to aid the binding of dinitrogen by a local high-spin \( \rightarrow \) low-spin electronic structure change at Fe_6 or Fe_7. The reductive elimination step then maintains the low-spin structure while doubly reducing the cofactor and partially activating the N_2 ligand. The carbide may play a role in tuning the redox potential for the reduction steps but it may also play a role in either binding or activation of N_2. The carbide being approximately trans to the N_2 ligand in our E_2-N_2/E_1-N_2 structures, suggests a link to the model chemistry of Peters and coworkers^{7,8} where carbide and boride-containing mononuclear trigonal bipyramidal Fe complexes were found to be active catalysts for dinitrogen reduction. Similar to the model compounds, the carbide in FeMoco may aid in pushing electron density into the π-accepting orbitals of the N_2 ligand. The molybdenum ion likely also has an effect on the redox potential of the cofactor (the redox potential can in fact be tuned by heterometal substitution as known by synthetic [XFe_3S_4] chemistry where X = Mo, V, W\(^{9,10}\)). We speculate that the role of the molybdenum may also be vital in stabilizing the N_2-bound Fe(i) ion in E_1-I-N_2, formed after the reductive elimination step, making the electrons available for partial activation of the N_2 ligand. The homocitrate ligand likely plays a role in protonation steps and the proton on the Mo-bound alcohol group of homocitrate is in an ideal position to protonate the N_2 ligand when bound to Fe_6 in the E_1-I-N_2 state; it may also help deliver protons in the early redox states (becoming protonated sulfides or hydrides).

Finally, we emphasize that this work presents only a preliminary mechanism for dinitrogen binding to FeMoco that relies primarily on calculated energies with density functional theory approximations (where a large functional dependency is seen) and where only a small part of chemical space has been explored. More experimental data on the E_4 and E_2-N_2 states are urgently needed to further constrain the mechanistic possibilities of FeMoco as well as to help benchmark the theoretical methodology employed. The precise way in which the N_2 ligand is activated for protonation is also not clear from our results. At the very least this computational study has presented falsifiable ideas about the mechanism of biological nitrogen reduction that can be confirmed or ruled out by suitable experiments.

Conflicts of interest
There are no conflicts to declare.

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