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Computational design of syntheses leading to compound libraries or isotopically labelled targets.

Karol Molga†‡, Piotr Dittwald†‡, Bartosz A. Grzybowski1,2*

1 Institute of Organic Chemistry, Polish Academy of Sciences, ul. Kasprzaka 44/52, Warsaw 01-224, Poland

2 IBS Center for Soft and Living Matter and Department of Chemistry, UNIST, 50, UNIST-gil, Eonyang-eup, Ulju-gun, Ulsan, 689-798, South Korea

† Authors contributed equally

*Correspondence to: nanogrzybowski@gmail.com

ABSTRACT

Although computer programs for retrosynthetic planning have shown improving and in some cases quite satisfactory performance in designing routes leading to specific, individual targets, no algorithms capable of planning syntheses of entire target libraries – important in modern drug discovery – have yet been reported. This paper describes how the network-search routines underlying existing retrosynthetic programs can be adapted and extended to multi-target design operating on one common search graph, benefitting from the use of common intermediates, and reducing the overall synthetic cost. Implementation within the Chematica platform illustrates the usefulness of such algorithms in the syntheses of either (i) all members of a user-defined library, or (ii) the most synthetically accessible members of this library. In the latter case, the algorithms are also readily adapted to the identification of the most facile syntheses of isotopically labelled targets. These examples are industrially relevant in the context of hit-to-lead optimization and syntheses of isotopomers of various bioactive molecules.
INTRODUCTION

Capitalizing on the advances in artificial intelligence\(^1\)-\(^4\) and constantly increasing computing power, recent years have brought revived interest and significant progress in the decades-old challenge of teaching computers the design of multistep organic syntheses\(^5\)-\(^9\). Various platforms, differing in the underlying details of search algorithms and reaction-rule formats, have been developed\(^10\)-\(^21\) and one of these platforms, our own Chematica\(^17\)-\(^21\), has been validated experimentally via successful execution of multiple routes leading to diverse, high-value, medicinally relevant small molecules\(^18\) and, more recently, natural products\(^19\). To date, a main effort in this emerging area of chemical research has been on algorithms designing syntheses to one specified target at a time. In several practically/industrially important situations, however, it is desirable to simultaneously design routes to multiple targets. For instance, a medicinal chemist might wish to optimize an existing scaffold and place various substituents in positions of interest (e.g., \(R_1\), \(R_2\), \(R_3\) in Figure 1a). Such hit-to-lead or lead optimizations\(^22\),\(^23\) encompass libraries of multiple synthetic targets, raising some pertinent questions: (1) Which of the targets are most readily synthesizable? or (2) How to synthesize all of the targets while making use of some possible common intermediates? Another situation of interest is when one wishes to design isotopically-labelled compounds that differ from the parent, non-labelled compound by a certain increment of molecular mass – this ability is important to determine drug’s pharmacokinetics\(^24\),\(^25\), to study environmental fates of pesticides\(^26\),\(^27\), to ascertain food safety\(^28\)-\(^30\), or to quantify food flavourings\(^31\)-\(^33\), in many cases using the so-called isotope dilution mass spectroscopy (IDMS) techniques and assays\(^34\). Because isotope labels can be placed in various positions and in various configurations within the molecule leading to isotopomers (Figure 1b) they, again, constitute a small library of potential targets. In this case, question (1) – which of the labelled
compounds offering a desired mass increase are most readily makeable – appears most relevant. Currently, there are no retrosynthetic algorithms with which one could address such questions for arbitrary targets. The closest analogue is our earlier work on the so-called Network of Organic Chemistry\textsuperscript{35-37} (NOC), in which we used Monte-Carlo searches to select (but not design) optimal syntheses leading to multiple targets of interest\textsuperscript{37}. Unfortunately, NOC is a static network comprising only published literature precedents and so its analyses are limited to already known targets and existing synthetic routes. In addition, Monte Carlo searches are computationally very intensive and typical execution times for the NOC were in days. Here, we describe significantly more efficient and general algorithms for \textit{de novo} retrosynthetic planning (i.e., planning based on general reaction rules, not existing literature precedents) producing routes to small libraries of arbitrary – that is, both known and unknown – targets, including labelled ones. In our algorithms, retrosynthetic searches for individual targets share the same search graph and can benefit from common intermediates and synthetic strategies. In several cases, these searches utilize cyclically-inspected list of priority-queue-based data structures rather than a single priority-queue; this construction ensures that the overall, multi-target search is not dominated by a sub-search for any individual target. Examples of specific and in all cases viable syntheses we describe evidence that multi-target planning routines make efficient use of common intermediates, reduce the search space significantly (compared to individual, target-by-target searches), and yield complete library-wide plans within minutes. Overall, the methods we describe extend applicability of computational retrosynthetic planning to problems that are ubiquitous and important in pharmaceutical and agrochemical industries, offering savings in terms of planning time and the overall cost of synthesis of compound libraries, as well as minimization of waste (through the maximally efficient use of common intermediates and “root” reactions in the global, library-wide reaction plans). In a broader context, the multi-
target design harnesses computer’s ability to store, analyze, and optimize large, interconnected networks of synthetic plans – which may be difficult to human chemists accustomed to planning synthetic solutions to specific targets, one target at a time.

**COMPUTATIONAL METHODS**

Modern retrosynthetic planners (e.g., MIT’s ASCKOS\(^{15}\), Waller’s MCTS\(^{14}\), or our Chematica\(^{17-21}\)) differ in the origin of the underlying reactions rules (machine extracted vs. expert coded) and details of the search routines, but they all rely on the iterative expansion of parent/retron nodes into progeny/synthon nodes and on navigating (with the help of functions scoring individual reaction moves) the thus created bipartite graphs of synthetic options until simple and commercially available substrates are found. This procedure yields pathways that lead to a given target of interest and in which all chemical nodes are “synthesizable” (i.e., they are targets of at least one synthetic pathway tracing back to commercially available substrates) and the reaction nodes as “viable” (i.e., all their substrates are synthesizable). The problem we focus on in the current paper is how to extend such generic routines to enable simultaneous synthesis of multiple targets ("a library").

**Algorithm seeking the syntheses of all targets.** We begin by discussing the simplest problem of identifying syntheses of all members of a library. The algorithm (**Figure 2** and pseudocode in SI, **Section S1**) initializes by performing dummy “multicomponent” reaction, \( r_{\text{dummy}} \), such that the root node (i.e., the library) is “made” in one step from all molecules in the library, \( \{m_i\}, i = 1, \ldots, N \), serving as its substrates. Chemically, this is a purely fictitious operation but algorithmically, such search-graph construction is important as it serves as an “AND” condition ensuring that any viable syntheses (cf. definition of viability above and in \(^{21}\)) of the root node will also have to make all substrates for the ultimate \( r_{\text{dummy}} \) reaction – in other words, the search algorithm will not stop until viable syntheses of all \( m_i \) molecules in
the library are identified. Of course, this dummy reaction is not supposed to skew the real
searches for \( m_i \)'s in any way, and its execution cost is assigned as zero. Starting from the \( m_i \)
nodes, the search graph is iteratively expanded as described before\(^{18} \), with the already-
evaluated sets of synths stored in a single priority-queue-based data structure (PQ), and
with further synthetic navigation guided by desired scoring functions (in Chematica, the
synthetic moves are guided by summing the costs of the already-performed reactions and the
complexity of synths created by each reaction\(^{17,18} \); in programs like ASKCOS or Waller’s
MCTS, the navigation is based on the scores provided by neural networks trained on large
numbers of reaction precedents\(^{14-15} \)). The stop points for the search are known and/or
commercially available molecules with prices of the latter typically taken from commercial
catalogues.

As the search is allowed to progress, multiple viable synthses are typically found,
forming a solutions’ graph from which most economical plans can be selected (by iteratively
propagating the yield-scaled costs from substrates to products and thereby assigning a
realistic, monetary cost to each plan). In addition to the selection procedures detailed in our
recent publication\(^{21} \), a unique feature of library-wide design is that we wish to promote
convergent synthetic plans that make use not only of common intermediates but also of the
smallest number of different synthetic methodologies – to this end, a penalty is added to any
new reaction type encountered in the solutions’ graph. Chemically, such penalization ensures
that it is more economical to perform the same reaction on a, say, 2 mol scale, rather than two
different types of reactions –requiring separate set-ups and likely different reagents – each on
the scale of 1 mol.

We observe that if the searches for each library member were performed separately,
selection would be made from each individual solutions’ graph and no synergies in terms of
common intermediates or reaction types could, in general, be expected. Also, in terms of
computational efficiency, the search on a common graph is significantly more compact than the sum of individual searches – as quantified for specific examples we discuss later in the text (cf. Figures 4, 5 and Table S1), the number of graph nodes explored before finding the first viable solution is about an order of magnitude smaller for the library-oriented, global search than for separate searches, each ran for a different library member.

Algorithm seeking the easiest syntheses of some targets. In some cases, not all members of a library are equally difficult to synthesize, and one could wish to commit to wet-lab execution only those that are most readily makeable. Algorithmically, this task is a bit more nuanced than finding syntheses to all targets in the library. To illustrate, let us assume that a search for the synthesis of target $m_i$ does not find any solutions after a certain time – if this target is extremely hard to make and yet the algorithm continues to find its synthesis, it might be stuck in this one search while other targets could yield solutions in shorter times. On the other hand, we do not know a priori if these other targets are any simpler. To overcome such problems, we implemented a multi-priority-queue algorithm that allows syntheses of different targets to be explored to comparable levels, while sharing the information about common intermediates and chemistries, and returning the best-scoring pathways taking into account aggregated results for all targets considered. Specifically, the algorithm (Figure 3 and pseudocode in the SI, Section S2) initializes not from a single “dummy” reaction (cf. previous section) but from $N$ such reactions, each linking the terminal root/library node with one specific member of the library $\{m_1, ..., m_N\}$. This construction serves as an “OR” condition and ensures that any viable pathway to the root node will also synthesize one of the $m_i$ molecules. Moreover, to ensure that all targets $m_1, ..., m_N$ are being analyzed to comparable degrees, we use the priority-list, PL, rather than a single, global priority queue-based data structure, PQ. This PL: (1) has length $N$; (2) its $i$-th element, PL[$i$], is a PQ
initialized with single-element set $\{m\}_i$; (3) synthon sets from PL are retrieved in circular order, i.e., PL[1], PL[2], ..., PL[N], PL[1], PL[2], ...; (4) when a synthon set S is taken from PL[i], and is further expanded into progeny synthon sets, these progenies are also inserted to PL[i]. In other words, although the search uses one common graph and still benefits from the use of common intermediates/chemistries, each target has its separate PQ which stores the synthetic options for this target and, importantly, is inspected cyclically. As solutions are being found, selection procedure \(^2\) is applied to the entire solutions’ graph (encompassing pathways leading to different targets), to select the best individual syntheses (shortest, most economical, chemically diverse routes). Unlike the “find all” modality we described earlier, for which the outcome was a global graph encompassing syntheses of all library members, the end result of the “find best” analysis is a list of individual synthetic solutions ranked in descending order of the ease of synthesis.

**Algorithm seeking the most feasible syntheses of multiple isotopomers.** For this sub-problem, our aim is to find the most readily synthesizable isotopomer that increases molecular mass by a user-specified value. The library here is the set of possible isotopomers and the search problem itself is identical to the one described in the previous section with the searches terminating in isotopically labelled (and possibly some non-labelled), commercially available starting materials. The difference lies in the way in which the target library is generated – in particular, we would like to automate the generation of all isotopomers offering the desired mass increase. The procedure to do so begins with specifying the non-labelled target molecule, a desired mass shift, $S$ (positive or negative), and available_iso list of isotopes one wishes to use. The list should contain isotopes with only positive or only negative mass shifts, corresponding to the sign of $S$ (e.g., if $S > 0$, \(^{13}\text{C}$ but not \(^{11}\text{C}$ should be used). This condition precludes generation of several nonsensical isotopomers in which, for example, mass shift of +1 could be obtained by introducing two \(^{13}\text{C}$’s and one \(^{11}\text{C}$.
Additionally, one may wish to specify which atoms should not be labelled (e.g., $^2$H labelled carboxylic acids, amines, or alcohols are labile, whereas $^{13}$C labelling should be avoided in metabolically unstable fragments such as esters or N-methylamines).

With such assumptions, the atoms of the target are arbitrary ordered, $a_1, \ldots, a_M$, and the recursive procedure (for pseudocode, see SI, Section S3) is applied to generate a set of desired isotopomers. To explain this procedure, let us consider methanol as target, a hypothetical $\text{available}_\text{iso} = [^2\text{H}, ^{17}\text{O}, ^{18}\text{O}]$, and $S = 2$. Let us define $\text{labellings}(j, k, S)$ as a set of labellings of atoms $a_j, \ldots, a_k$, giving mass shift $S$. Then $\text{labellings}(1, M, S)$ refers to the set of isotopomers we ultimately seek (pending de-duplication of possible identical structures). For the specific CH$_3$OH target, let us order atoms $a_1, a_2, a_3, a_4, a_5, a_6 = \text{C, H}_1, \text{H}_2, \text{H}_3, \text{O, H}_4$ (upper-right indices are used to distinguish between hydrogen atoms), and commence from $a_1 = \text{C}$. As $\text{available}_\text{iso}$ does not contain any isotopic label for carbon, no isotopic labelling can be applied to $a_1$ and the set of appropriate labellings can be therefore written recursively as equation (*) $\text{labellings}(1, M, S) = \{a_1 := ^{12}\text{C}\} \times \text{labellings}(2, M, S)$, where $\times$ stands for set multiplication. Moving to the second atom, $a_2 = \text{H}_1$, it can be labelled by deuterium (mass shift of +1) or left unlabelled (no mass shift), and so we have (***) $\text{labellings}(2, M, S) = \{a_2 := ^2\text{H}\} \times \text{labellings}(3, M, S-1) \cup \{a_2 := ^1\text{H}\} \times \text{labellings}(3, M, S)$. By combining (*) and (***) we obtain $\text{labellings}(1, M, S) = \{a_1 := ^{12}\text{C}, a_2 := ^2\text{H}\} \times \text{labellings}(3, M, S-1) \cup \{a_1 := ^{12}\text{C}, a_2 := ^1\text{H}\} \times \text{labellings}(3, M, S)$. The procedure is continued until the last atom is reached ($a_6$ for methanol) and all acceptable labelling options are returned. For the methanol example we considered, after de-duplicating the same chemical structures (i.e., removing molecules with the same canonical SMILES representation), there are five viable isotopomers, written here in SMILES notation that is used as input to the retrosynthetic search: [2H]CO[2H], C[18O], [2H][17O]C, [2H]C([2H])O, [2H]C[17O].
RESULTS AND DISCUSSION

**Chemical examples implemented in Chematica.** The algorithms detailed in the preceding sections can be implemented within various retrosynthetic platforms. Since we have been actively involved in the development of and continue to have access to Sigma-Aldrich’ Chematica, we illustrate how the algorithms function in this particular environment.

As described in several of our publications on Chematica\(^\text{17-21}\), this platform is based on the knowledge-base of over 75,000 expert-coded reaction rules reflecting reaction mechanisms, delineating carefully substituent scope as well as contextual information about potential cross-reactivity conflicts, protection requirements, selectivity issues, etc. (for examples, see \(^\text{17}\) and supplementary materials to \(^\text{18,20}\)). The rules have variants applicable to synthesis of isotopically-labelled compounds, and are augmented by various modules based on quantum-mechanical, molecular-mechanical, machine-learning, or heuristic measures of reactions’ electronic and steric requirements\(^\text{17,20,39}\). The bipartite synthetic graphs created by the application of reaction rules are navigated with the help of scoring functions assigning costs for each reaction operation performed (with additional costs added to reactions requiring, e.g., protection chemistries) and evaluating structural complexity of the sets of synthon molecules produced in each step. The searches are supplemented by routines checking the multi-step logic of syntheses – for instance, they prevent dragging highly reactive groups along multiple steps, penalize contraction of certain macrocycles, or allow overcoming local complexity maxima by the use of the so-called tactical combinations. Once feasible routes are found, they are scored according to realistic pricing models\(^\text{21}\) based on the prices of commercially available starting materials (>200,000 chemicals from Sigma-Aldrich including ~1,100 isotopically labelled ones) and approximate yet realistic reaction yields\(^\text{40,41}\).
The chemical correctness of all these algorithms has been corroborated by successful experimental execution of a number of Chematica-planned, multistep syntheses\textsuperscript{18,19}.

The multi-target design interfaced with Chematica entails specification of the target library, either by drawing all its members in a structure editor or by defining a Markush structure written in SMILES notation\textsuperscript{42} (Figure 1c,d) or, for isotopomers, by specifying the desired mass increase and the isotopes that can be used. The results of the searches are presented to the user as a “global” graph encompassing, depending on the search modality, syntheses of all or some, most synthetically accessible targets. Each substance and reaction node can be expanded to provide, respectively, additional structural and synthetic details (see SI, Sections S5-S11).

**Synthesis of all members of a Prozac-derived library.** Let us begin with a simple example in which we seek syntheses of all members of a small library around selective serotonin reuptake inhibitor, fluoxetine (Prozac). The library admits four different substituents (\(p\)-F, \(p\)-Cl, \(p\)-CF\(_3\) and H) in the aryl ether part of fluoxetine and three different moieties on the \(N\)-terminated side chain (NHMe, NHEt and NHAc), corresponding to 12 compounds in total (Figure 4a). Within ca. 5 min, Chematica produced tens of global plans for the syntheses of all the library members, with the top-scoring solution graph shown in Figure 4b and with chemical details elaborated in Figure 4c (for raw Chematica screenshots and suggested reaction conditions, see Figure S4). The common root of all syntheses is the Friedel-Crafts acylation of benzene with acyl chloride derived from the \(N\)-Acetyl \(\beta\)-amino propionic acid. Subsequent enantioselective reduction (controlled, e.g., by Corey-Bakshi-Shibata catalyst\textsuperscript{43} or Noyori’s catalyst\textsuperscript{44}) yields the enantioenriched secondary alcohol which is reacted with appropriate phenols under Mitsunobu conditions to give desired \(N\)-acyl series A\(_2\)-D\(_2\). The \(N\)-ethyl substituted compounds A\(_3\)-D\(_3\) can then be obtained in one step via reduction of the acetyl moieties while the preparation of \(N\)-methyl series A\(_1\)-D\(_1\) requires
hydrolysis of acetamide and subsequent reductive amination with formaldehyde. Importantly, the entire scheme to prepare 12 different compounds requires only 18 individual reactions and takes advantages of several common intermediates including interconversions of some library members. We note that proposed strategy, comprising enantioselective reduction of appropriate β-aminoacetophenone\textsuperscript{44-46} and Mitsunobu displacement with phenol\textsuperscript{47-48} has already been used in several syntheses of structurally related compounds including our synthesis of hydroxyduloxetine\textsuperscript{18}. We also emphasize that this “global” synthetic plan is different from the plans that Chematica produces for each target separately – for instance, if the program’s task is to make des-trifluoromethyl congener of fluoxetine A1 \textit{(Figure 5a-c and Figure S5)}, it uses the enantioselective allylation of aldehyde and ozonolysis mimicking Bracher’s approach\textsuperscript{49}. The same strategy is returned as the top solution if A3 \textit{(Figure 5d and Figure S6)} or D3 \textit{(Figure 5e and Figure S7)} are individual targets. We note that none of the top-three approaches found by Chematica in single-target-oriented searches for A1 \textit{(Figure 5a-c and Figure S5)} – relying on either the Friedel-Crafts acylation with carbamate protected β-aminopropionic acid\textsuperscript{50} or enantioselective arylation of aldehyde\textsuperscript{51,52} – are desirable for the design of the entire library. This is so because these syntheses cannot take advantage of late common intermediates and require several additional reactions (e.g., for the optimal individual solution to A1, adaptation to the all-library synthesis would entail total of 21 distinct reactions: allylation, four displacements with phenols, four hydroborations, and twelve aminations). The software is not using the elegant three-component Mannich reaction (one we employed previously in ref.\textsuperscript{18} for the construction of structurally similar scaffold of hydroxyduloxetine) because it cannot be adapted for the synthesis of the current library – in particular, Mannich reaction cannot be performed with acetamide instead of methylamine to yield the N-Ac series A2-D2. We also note that this design example illustrates well typical gains in terms of computational efficiency: The search on a common graph to identify the
first viable solution requires exploration of ca. 10 times less nodes compared to the case when the syntheses of the 12 targets are searched for separately (cf. Table S1 in SI, Section S4).

**Synthesis of all members of Almorexant-derived library.** In a more chemically advanced example, we consider synthesis of a library centered around Almorexant, a drug developed by Actelion and GSK for the treatment of insomnia. The library admits four different substituents (\(p\)-F, \(p\)-CF\(_3\), \(p\)-tBu and 3,4-diOMe) in the phenylethyl part of Almorexant and two different \(N\)-substituents, corresponding to eight compounds in total (inset in Figure 6a). Within ca. 30 min, Chematica identified global synthetic plans with the top-scoring solution graph shown in Figure 6a and with chemical details elaborated in Figure 6b (for raw Chematica screenshots and suggested reaction conditions, see SI, Figure S8). The synthesis of each library member commences with the oxidation of appropriate terminal alkenes to aldehydes. The key formation of chiral tetrahydroisoquinolines leading to four common intermediates (marked with arrows in Figure 6a and colored orange in Figure 6b) is accomplished via enantioselective Pictet-Spengler cyclisation controlled either by chiral auxiliary or chiral catalyst\(^{54}\). Subsequent alkylation with the commercially available secondary benzyl bromide \(A\) or condensation with derivative of mandelic acid \(B\) yields the target molecules.

**Synthesis of all members of a library of RANKL/RANK inhibitors.** Our last example of all-library design is important in that the computer’s autonomous design can be directly compared with and validated against recent experimental work. Specifically, we challenged Chematica with the synthesis of a subset of a library of RANKL/RANK inhibitors reported very recently by Yang and co-workers\(^ {53}\). In this task the library, represented as Markush structure in the inset of Figure 7a (for full representation see Figure S9), consisted of 20 derivatives of tryptophan with different \(N\)-alkyl (\(Z = \text{CH}_2\)) or \(N\)-acyl fragments (\(Z = \text{C}=\text{O}\)), different linker lengths (\(n = 1–4\)) and substituents (\(R = \text{alkyl, aryl, heteroaryl}\)).
search was allowed to run for ca. 15 min and returned as the top-scoring solution the synthetic plan shown as a graph in Figure 7a and further detailed in Figures S10 and S11. Within this plan, the synthesis of each library member is accomplished in a short (three-four steps) sequence, commencing with the coupling between commercially available N-Boc tryptophan and 2,6-dimethylaniline. Subsequent removal of protecting group gives the common intermediate (in Figure 7a, the rightmost node marked with an orange arrow). Finally, couplings with appropriate carboxylic acids or primary mesylates lead to N-acyl or N-alkyl target molecules, respectively. Remarkably, this approach mirrors closely the strategy used in Yang and co-workers’ experiments\textsuperscript{53}.

**Synthesis of the most accessible derivatives of a κ-opioid agonist.** To illustrate synthetic design of not all but only the most accessible members of a given library, we considered derivatives of selective κ-opioid agonist\textsuperscript{55} ICI-199441 (Figure 8). The ICI-199441 scaffold was decorated with three substituents in N-terminated side chain, four substituents in the benzylamine part, and four combinations of halogens in arylacetic acid part, overall corresponding to 48 distinct members of the library (Figure 8a). Top five of the several hundred of viable pathways (identified within \(\sim 10\) min) are shown in Figures 8b-f and further detailed in and Figure S12. In each of these plans, the molecule of interest (one node before the yellow node; compare with scheme in Figure 3b) can be obtained in three steps using alkylation of appropriate secondary amine with a commercially available protected phenylglycinol, removal of the protecting group, and sulfur catalyzed Wilgerodt-Kindler (WK) reaction\textsuperscript{56} yielding the desired arylacetic acid amides from acetophenones. The application of this last methodology – while chemically correct – might, at first glance, appear counterintuitive given that such amides are usually\textsuperscript{55,57} formed in reactions of acyl halides or carboxylic acids. These more conventional plans were, indeed, present in the top 100 solutions the software identified, but the algorithm correctly gave them lower scores.
based on higher prices of substrates – namely, application of the WK reaction allowed for the use of cheaper acetophenone substrates rather than appropriate arylacetic acids ($1.91 vs. $3.23 per g of dichloroderivative and $3.21 vs. $5.81 per g of 4-F-3-Cl derivative). Consequently, the diethylamino-congeners were found more accessible than morpholino- or cyclopentylamino ones. We also note that none of the compounds substituted in the benzylamine part appeared among the most accessible targets as their synthesis requires construction of appropriate chiral aminoalcohols.

**Syntheses of isotopically labelled targets.** In our last set of examples, we used the algorithm to determine which isotopically labelled compounds from a given library of isotopomers are synthetically most readily accessible.

(i) Cinacalcet. Figure 9 shows five top-scoring syntheses of Amgen’s Cinacalcet (Sensipar/Mimpara), whose mass we wish to increase by $S = 1$ by single labelling with either $^{13}\text{C}$ or $^2\text{H}$ (there are 39 unique isotopomers). In the first proposed synthesis (Figure 9a), the $^{13}\text{C}$ isotopic label is located on the methyl group and introduced from bromomethane. In the first step, chiral-auxiliary-directed addition\textsuperscript{58,59} of an organometallic reagent derived from $^{13}\text{CBr}$ yields the enantioenriched secondary amine which is then alkylated with a commercially available alcohol to give the molecule of interest. In the second plan (Figure 9b), the $^2\text{H}$ isotope label is introduced from $\text{D}_2\text{O}$ during Shapiro reaction proposed as the first step. Subsequent Rh-mediated hydroaminomethylation gives the $^2\text{H}$-cinacalcet also after 2 steps. In the third plan (Figure 9c), $^{13}\text{C}$ labelled Cinacalcet is made in only one step, via three-component hydroaminomethylation utilizing commercially available styrene, enantioenriched secondary amine, and $^{13}\text{C}$ carbon monoxide. We observe that such carbonylative approach has been already used by Amgen to prepare unlabeled Cinacalcet\textsuperscript{60}. In the fourth plan (Figure 9d), the labelled $^{13}\text{C}$ atom is located at the chiral carbon and comes from the $^{13}\text{C}$ acetic acid used in the initial Friedel-Crafts acylation of naphthalene\textsuperscript{61}. 

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Subsequent reductive amination guided by a chiral auxiliary\textsuperscript{62} or a chiral catalyst\textsuperscript{63,64} yields the secondary amine transformed into the target molecule following steps from the first plan. Finally, Cinacalcet can be labelled with $^2\text{H}$ located at the methyl group with deuterium atom introduced from $^2\text{H}$-methyl iodide participating in direct enantioselective alkylation of naphthylacetic acid\textsuperscript{65} controlled by a chiral diamine (Figure 9e). Subsequent transformation of carboxylic acid to secondary amine via Schmidt reaction\textsuperscript{66} yields the amine which is subject to reaction with alcohol to give the target molecule. We note that the proposed approaches relying on the alkylation of chiral naphthylamine are corroborated by published syntheses\textsuperscript{67-71} of unlabeled Cinacalcet.

\textbf{(ii) AMG-319. }The second example in this section describes synthesis of M+1 isotopomers of Amgen’s AMG-319, inhibitor targeted for autoimmune diseases\textsuperscript{72} and head and neck squamous-cell carcinomas\textsuperscript{73}. The proposed solution (Figure 10a) commences with the Suzuki coupling of 2-piridyld boronic acid and 2-chloropyridine. Subsequent conversion to an imine and stereoselective addition\textsuperscript{58} of organometallic reagent derived from $^{13}$CBr yields the enantioenriched benzylic amine which is coupled with hypoxanthine in the last step. We note that this computer-designed synthetic plan resembles Amgen’s original route\textsuperscript{72} to unlabelled AMG-319.

\textbf{(iii) Lasmiditan. }In the third example, the algorithm is used to design syntheses of [M+1] Lasmiditan developed by Eli Lilly for the treatment of acute migraine. After specifying the admissible isotope label (here, $^{13}$C), desired mass shift $S = 1$ (corresponding to 15 isotopomers) and excluding $^{13}$C N-methylated isotopomer prone to hepatic cleavage observed previously for N-methyl piperazines\textsuperscript{23,74-76}, the search was run for ca. 10 min and returned hundreds of viable synthetic plans from which the top-scoring one is shown in Figure 10b. In the first step, the appropriate 2-chloropyridine is constructed in one step via addition of a Grignard reagent, obtained from the N-methyl-4-bromopiperidine, to 2-cyano-6-
chloropyridine. The isotope label is introduced from $^{13}\text{CO}_2$ used for the formation of carboxylic acid from the organolithium reagent derived from trifluorobenzene. The following steps resemble the original route to Lasmiditan. Subsequent amination of 2-chloropyridine and reaction with labelled benzoic acid yield the molecule of interest in a four-step sequence.

(iv) Roluperidone. In the fourth example, Chematica designs syntheses of M+1, $^{13}\text{C}$ labelled congener of Roluperidone developed by Minerva Neurosciences for the treatment of schizophrenia. The top-scoring plan returned after ca. 10 min is shown in Figure 10c. The proposed short sequence commences with the $N$-alkylation of hydroxymethylpiperidine with the appropriate chloroacetophenone. Subsequent alkylation of 2-bromobenzylamine with the remaining primary alcohol yields the substrate amenable to intramolecular carbonylative amidation. The $^{13}\text{C}$ label is introduced in this step and sourced from $^{13}\text{CO}$, completing the synthesis in just three steps. The proposed plan resembles the Mitsubishi’s synthesis of Roluperidone utilizing proposed hydroxymethylpiperidine and phenacyl bromide as building blocks and participating in $S_N2$ alkylations of benzolactam and secondary amine; moreover, the proposed carbonylative $N$-alkylation has been used in Astellas’ synthesis of $N$-benzyl benzolactams.

(v) Pitolisant. The fifth example illustrates efficient preparation of M+1, $^{13}\text{C}$ labelled Pitolisant (Wakix), developed by Bioprojet for the treatment of hypersomnia. The search performed for ca. 10 min returned multiple solutions from which the top-scoring one is shown in Figure 10d. The entire sequence requires only two steps and sources the $^{13}\text{C}$ atom from labelled bromoacetic acid used in the first step to $N$-alkylate $^{85}$ hydroxypropylpiperidine. The obtained alkoxyacid is then used in MacMillan’s decarboxylative coupling with commercially available phenethyl bromide to give the target molecule. The proposed plan
resembles the Bioprojet’s one-step solution\(^\text{87}\) which also used hydroxypropylpiperidine alkylated with the appropriate alkyl bromide.

**(vi) Almotriptan.** In the sixth and last example, we aim to design routes to labelled Almotriptan developed by Almirall for the treatment of heavy migraine headache. After specifying the plausible isotopes \((^{13}\text{C})\) and mass shift \(S = 1\) and precluding the \(N\)-Me labelled isotopomers prone to hepatic cleavage\(^\text{23,88-90}\), the search was run for \(~10\) min and returned as its top-scoring solution pathway shown in Figure 10e. Somewhat counterintuitively, the isotope label in the most accessible isotopomer is located inside the indole ring and comes from \(^{13}\text{CO}\). The proposed synthetic plan starts from the commercially available aniline transformed into appropriate hydrazine. Subsequent Rh-catalyzed tandem hydroformylation/indolisation\(^\text{91}\) builds the central ring system, introduces the isotope label and attaches the dimethylaminoethyl side chain and yields the target molecule in two-step sequence. Similar, elegant carbonylative tandem indolisation was already used in Sheldon’s one-pot synthesis of unlabeled melatonin\(^\text{92}\).

**CONCLUSIONS**

In summary, we described how the search routines over large graphs of retrosynthetic scenarios can be adapted to find all or some members of target compound libraries. For the find-all variant, the “global” synthetic plans can benefit from the use of common intermediates and can be significantly different from optimal solutions found for each target separately – that is to say, the global solutions might be counterintuitive for human planners accustomed to optimizing specific synthetic routes rather than interconnected networks of such routes. Another application we consider quite useful is the synthesis of isotopomers. Here, the catalogs of isotopically labelled starting materials are significantly less populous than those of unlabelled building blocks, and many blocks that are considered “basic” are not
available in labelled forms. Consequently, synthetic design is often non-intuitive and it is not straightforward to predict which of the potential isotopomers would be the easiest one to make – a question our algorithms can handle rapidly and efficiently. Overall, this work extends the scope of computer-assisted synthetic planning to new problems that are common and important in pharmaceutical and agrochemical industries.
CONFLICT OF INTEREST

While Chematica was originally developed and owned by B.A.G.’s Grzybowski Scientific Inventions LLC, neither he nor the co-authors no longer hold any stock in this company, which is now property of Merck KGaA, Darmstadt, Germany. The authors continue to collaborate with Merck within the DARPA “Make-It” award. All queries about access options to Chematica (now rebranded as Synthia™), including academic collaborations, should be directed to Dr. Sarah Trice at sarah.trice@sial.com.

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Figure 1. Examples of multiple-target libraries. a) Library of chlorcyclizine derivatives screened for the treatment of Hepatitis C virus in \(^{38}\). b) Isotopomers of ibuprofen. Top row has two examples of M+1 isotopomers possible with \(^{13}\)C (left) and \(^2\)H (right) labelling. Bottom row has two examples of M+2 isotopomers available via \(^{13}\)C (left) and \(^2\)H (right) labelling. Green numerals within the molecules give the total numbers of unique (note: some hydrogens and carbons are equivalent) labelled compounds for each case. For the M+2 labelling of this structurally simple target, there are already 49 \(^{13}\)C and 28 \(^2\)H labelling combinations. The number of isotopomers corresponds to sets without \(^2\)H labelling of the COOH group which is extremely easily exchangeable. c) To specify multiple targets of retrosynthetic analyses, it is often convenient to use the so-called Markush structures. Here, a set of molecules is represented as a SMILES string (black) with numbered dummy atoms (\([-;1],[*,2]\)) and dictionary of substituents marked in red and green for positions #1 and #2, respectively. Position \([-;1]\) can correspond to either an aromatic carbon or nitrogen (to yield,
respectively, biphenyl and 2-phenylpyridine series), whereas position [*:2] admits either a nitrile, CN, or F, or Cl atoms. In all, the small library thus defined will have \( N = 6 \) six members shown in panel d).
Figure 2. Schematic description of the algorithm seeking the syntheses of all targets. a) The user specifies target set (here, TS = library of four targets), defining the root node (yellow circle) of the search graph to be explored (shaded parts represent regions of the graph not yet expanded). b) The search graph is extended by adding four additional substance nodes (violet circles labelled \( m_1, m_2, m_3, m_4 \)), linked with the root node via the same dummy reaction (orange diamond). The search algorithm utilizes single priority-queue-based data structure, PQ, to navigate the graph expansion according to scores assigned to specific synthetic “options” encountered during the search. For this illustrative example, the algorithm first expands node \( m_2 \), having a better score than nodes \( m_1, m_3, m_4 \). c) Three explored reactions (grey diamond-shaped reaction nodes) lead to possibly overlapping substrate sets – i.e., nodes labelled \{1, 2\}, \{2, 3\}, \{4, 5\}, respectively. Violet circular nodes denote molecules that are unknown in literature and not commercially available; red circular nodes refer to terminal, commercially available, chemicals. Here, one synthesis, i.e., \( 4, 5 \rightarrow m_2 \), gives viable synthesis plan for target \( m_2 \) (green halo denoting that \( m_2 \) is synthesizable). The search
proceeds to (i) find syntheses for the remaining targets \( m_1, m_3, m_4 \), and (ii) find alternative synthesis plans for target \( m_2 \). **d)** Search continues expanding node \( m_4 \), giving reactions with substrates \{6, 7\}, and \{8\}, then expanding node \( m_3 \) **e)** resulting in reactions’ substrate sets \{5\}, \{6\}, \{9\} (nodes 5 and 9 were already visited in previous expansions; moreover, as node 5 is terminal, path 5 \( \rightarrow \) \( m_3 \) is a viable synthesis for \( m_3 \)). **f)** Furthermore, the region of the search graph related to the synthesis of \( m_1 \) is visited by exploring node 10, and nodes 11 and 12. **g)** The path 12 \( \rightarrow \) 10 \( \rightarrow \) \( m_1 \) is a viable synthesis, so the target \( m_1 \) is now also synthesizable. **h)** Then, node 6 is expanded, giving terminal node 13. Of note, 6 is a common intermediate for syntheses of targets \( m_3 \), and \( m_4 \), and these two targets have new viable syntheses (13 \( \rightarrow \) 6 \( \rightarrow \) \( m_3 \), and 13 \( \rightarrow \) 6,7 \( \rightarrow \) \( m_4 \)). Target \( m_4 \) is now synthesizable, and viable synthesis plans can by retrieved for all targets from initial target set (operation performed by selection algorithm, see main text). **i)** The search continues to find more synthesis options, here exploring node 8 to give reaction with substrates 13 and 14 (resulting in alternative synthesis for target \( m_4 \): 13,14 \( \rightarrow \) 8 \( \rightarrow \) \( m_4 \)).
Figure 3. Schematic description of the algorithm seeking the syntheses of some, most-synthetically-accessible targets. a) The root node (yellow circle) corresponds to the target set (here, TS = library of four targets). b) The graph is extended by creating four substrates (violet circles denoted \( m_1, m_2, m_3, m_4 \)), each linked with the root node via a separate dummy reaction (orange diamonds). Additionally, four priority-queue-based data structures, \( PQ_1 \), \( PQ_2 \), \( PQ_3 \), \( PQ_4 \), each corresponding to a separate target node, compose a priority-list, PL, inspected in circular order (first \( PQ_1 \), then \( PQ_2 \), \( PQ_3 \), \( PQ_4 \), \( PQ_1 \), etc.). PL is responsible for balanced exploration of syntheses leading to each target. c) According to \( PQ_1 \) (orange halo marks this data structure as currently inspected), \( m_1 \) is expanded, identifying a reaction (grey diamond) from substrates 1 and 2 (violet circle nodes refer to unknown chemicals). d) Then, as \( PQ_2 \) is inspected, node \( m_2 \) is expanded and two reactions are added to the graph (with
substrate sets \{3,4\} and \{5,6\}, respectively; red circular nodes represent terminal, commercially available chemicals). Target \(m_2\) is now synthesizable (green halo), with a viable synthesis \(3,4 \rightarrow m_2\) already satisfying the condition of finding a synthesis of at least one member of the target library. The search continues to find alternative pathways. e) According to \(PQ_3\), node \(m_3\) is expanded, and reactions with substrates \{6,7\} and \{8\} are identified (6 already appeared while searching for syntheses of \(m_2\)). f) Then, as \(PQ_4\) is inspected, \(m_4\) is expanded, giving reaction from node 8 (now, a common intermediate in the synthesis plans leading to \(m_3\) and \(m_4\)) and node 9. g) Inspection of the priority lists now returns to \(PQ_1\), nodes 1 and 2 (previously visited while searching for synthetic scenario of \(m_1\)) are explored, giving new nodes 10, 11, 12, and 13. h) As the search continues, \(PQ_2\) is inspected again, discovering viable synthesis (from terminal node 14) leading to a common intermediate of \(m_2\) and \(m_3\), i.e., node 6. Consequently, \(m_3\) becomes synthesizable, and pathways \(14 \rightarrow 5, 6 \rightarrow m_2\) and \(14 \rightarrow 6, 7 \rightarrow m_3\) become plausible solutions of the initial task. i) Subsequently, the algorithm inspects \(PQ_5\), node 8 is explored by two reactions, each starting at terminal nodes (15 and 16), and \(m_4\) becomes synthesizable (newly discovered pathways are 15 \(\rightarrow 8 \rightarrow m_3\), 16 \(\rightarrow 8 \rightarrow m_3\), 15 \(\rightarrow 8 \rightarrow m_4\), and 16 \(\rightarrow 8 \rightarrow m_4\)). All viable pathways identified during the search are retrieved and ranked according to a separate selection algorithm (see ref \textsuperscript{21}).
Figure 4. Retrosynthetic search to synthesize all members of a library around fluoxetine scaffold. 

a) All members of the library. b) The corresponding Markush structure and the screenshot from Chematica showing the top-scoring solution to synthesize all of the specified targets. In this graph, yellow circular node = Markush structure; small, blue, diamond-shaped node = “dummy” reaction connecting all specific targets A1 – D3 to the root node; leftmost column of 12 circular nodes = specific A1 – D3 targets, mostly unknown in the NOC
repository but one known (D1, number 9 inside of the node means that nine syntheses of this compound have been reported in the literature); red nodes = terminal, commercially available chemicals, numbers inside the nodes indicate prices per gram (from Sigma-Aldrich catalog). Note that several substances are common intermediates in multiple pathways and all 18 compounds are made in 12 steps in total. Details of synthetic plans are provided in panel c). For raw Chematica output and further details, see Figure S4.
Figure 5. Top-scoring solutions proposed by Chematica for the synthesis of individual members of the fluoxetine library: a-c) target A1, d) target A3, and e) target D3. Node coloring scheme is as in Figure 4. For raw Chematica output and synthetic details, see Figures S5-S7.
Figure 6. Retrosynthetic search to synthesize all members of a library of analogues of Almorexant. a) Markush structure representing proposed library (white inset, top-left), lists of substituents (bottom left) and graph representation of the top-scoring solution. Chemical details are shown in panel b). Note that several substances (marked with arrows and colored orange in panel b) are common intermediates in multiple pathways while the entire library is prepared from single phenylethylamine. For raw Chematica output and further details, see Figure S8. Node coloring scheme is as in Figure 4.
Figure 7. Retrosynthetic search to synthesize a subset of a recently reported library of tryptophan derivatives acting as RANKL/RANK inhibitors\textsuperscript{53}. a) Markush structure representing proposed library (white inset) and graph representation of the top-scoring solution. All members of the library are prepared from one common intermediate marked with arrow in a) and colored orange in panel b) which details synthesis of one of library’s members. For Chematica’s raw output for the entire library, see Figures S10-S11.
Figure 8. Retrosynthetic analysis of ICI199441 derivatives. **a)** Left portion shows the Markush structure and dictionary of substituents defining the library of 48 members; right structure is the original ICI199441 compound. **b-f)** Five top-scoring synthetic plans for library from **a**. Note that in plan (d), the algorithm found a commercially available advanced intermediate (red node with price per gram = $58.60) but continued the search until it found less expensive substrates with prices per gram below the user-specified threshold of $50/g. For further synthetic details, see **Figure S12**.
Figure 9. Syntheses of Cinacalcet singly-labelled with either $^2$H and $^{13}$C. Several thousands of viable routes were identified within 10 min; five top-scoring routes are shown. For further synthetic details, see Figure S13.
Figure 10. Retrosynthetic design of isotopically-labeled drug molecules. In all cases, $^{13}$C labeling was allowed and the desired mass shift was $S = +1$. Top-scoring and in all cases chemically viable solutions obtained for a) a library of 21 isotopomers of AMG-319; b) a library of 14 isotopomers of Lasmiditan; c) a library of 18 isotopomers of Roluperidone; d) a library of 13 isotopomers of Pitolisant; e) a library of 13 isotopomers of Almotriptan. For further details of the pathways, see Figures S14-S18.