

PAPER

View Article Online

View Journal | View Issue



Cite this: RSC Adv., 2019, 9, 37258

Photoabsorption markers of pressure-induced phase changes in small mercury clusters. A case study on Hg₈

Martina Šarmanová,†^{ab} Aleš Vítek,^a Rajko Ćosić pac and René Kalus ** **

Photoabsorption spectra of Hg_8 have been calculated at various cluster temperatures and external pressures. A diatomics-in-molecules method has been used to model cluster electronic structure and classical isothermal-isobaric Monte Carlo simulations have been employed for sampling representative cluster configurations. Contributions of different structural isomers of the Hg_8 cluster have been analyzed and related to structural transitions in the cluster, particularly those induced by an increased pressure.

Received 2nd October 2019 Accepted 5th November 2019

DOI: 10.1039/c9ra08000g

rsc.li/rsc-advances

1. Introduction

Flexible, weakly bound complexes may undergo, in contrast to covalently bound molecules, significant changes in their geometric structure if they are exposed to increased temperature. These changes comprise either deformations of their equilibrium structure (represented by the global minimum on their potential energy surface and often denoted as the stable isomer of the complex) or switches between the global minimum and other, local minima (metastable isomers) or between various local minima. If different local minima become accessible under specific conditions, so called phase changes^{1,2} take place in the studied system. Alternatively, structural changes can be achieved by varying the external pressure the studied system is exposed to if metastable isomers are more compact than the stable one.^{3,4}

The phase changes can be identified by inspecting temperature and/or pressure dependences of specific properties of the system which are directly or indirectly sensitive to changes of the layout of atoms of the system in space. For example, internal energy (enthalpy), heat capacity, correlations between various quantities (like the Pearson coefficient for the energy and the system volume³), and Lindemann index⁵ are used to pinpoint regions on the temperature and/or pressure scales where the phase changes take place (so called coexistence regions since various structural motifs coexist during a particular phase

One of the physical properties which are sensitive to the geometric structure of flexible complexes is the way they interact with electromagnetic radiation, experimentally represented by their photoabsorption spectra. For these systems, the photoabsorption spectrum usually consists of a set of more or less broad absorption bands the positions and heights of which may considerably change after ambient conditions have been modified. Moreover, photoabsorption spectra can readily be recorded and, thus, used in experimental studies of phase changes in small systems for which more conventional methods (like heat capacity measurements) are not easily practicable. As a consequence, modelings aimed at shedding light on the nature the interaction of the studied system with radiation is influenced by ambient conditions (temperature and pressure) is of particular interest.

Small mercury clusters, Hg_N , are very appropriate for such studies. Firstly, if small sizes $(N \leq 13\text{-}20)$ are considered, the clusters are bound by weak forces of the van der Waals type^{7,8} and even if the size is increased and the bond type changes from van der Waals to semi-covalent and metallic, their flexibility is conserved. Secondly, they exhibit⁹ quite strong absorption in the UV region (resulting from $6s \rightarrow 6p$ excitations in the Hg atom). Thirdly and most importantly, this photoabsorption can be rather easily modeled in theoretical calculations by taking advantage of a computationally cheap and, at the same time, realistic model of intra-cluster interactions^{10,11} providing both the electronic ground state as well as all relevant excited states of a Hg_N cluster of basically any size.

The interaction of mercury clusters with electromagnetic radiation have received a considerable attention, both experimentally. 9,12–17 and theoretically, 18–20 in the literature. 21 The topics covered comprise, *e.g.*, photoabsorption of ionic 12–14,20 as well as

change^{1,2}). Note, however, that none of the quantities is of a universal use and they must be often combined to identify phase changes of various kinds as completely as possible.

^aTT4Innovations, VŠB-Technical University of Ostrava, 17. listopadu 2172/15, 708 00 Ostrava-Poruba, Czech Republic. E-mail: rene.kalus@vsb.cz

^bOlga Havlová Grammar School, Marie Majerové 1691, 708 00 Ostrava-Poruba, Czech Republic

Department of Applied Mathematics, VŠB-Technical University of Ostrava, 17. listopadu 2172/15, 708 00 Ostrava-Poruba, Czech Republic

[†] Present address: Faculty of Mathematics and Physics, Charles University, Ke Karlovu 2027/3, 121 16 Praha 2, Czech Republic.

Paper

oen Access Article. Published on 14 November 2019. Downloaded on 12/9/2025 12:06:03 PM

neutral9 mercury clusters, photoionization and photoelectron spectroscopy of the latter, 15,16 their post-excitation dynamics, 18,19 or even photoinduced nucleation in mercury vapor.17 Note, however, that gas-phase conditions have been mostly considered in those preceding studies without any explicit control of clusters temperature and/or external pressure.

Recently, we have performed a series of gas-phase (zeropressure) calculations of the photoabsorption spectra of smallest Hg_N clusters ($N \le 5$) covering a broad range of clusters temperatures.22 The potential energy surfaces of these smallest clusters are, however, too simple (they contain only one, global minimum) to lead to qualitative changes in the calculated photoabsorption spectra with increased temperature and/or pressure. It is the main aim of the present work to extend this preceding study to larger cluster sizes for which more than one structural isomer exist and observable changes in their structure and, consequently, in their response to electromagnetic radiation may be expected. Specifically, changes induced by increased pressure are of particular interest here.

The smallest cluster of this more complex type is the mercury hexamer, Hg₆, with two structural isomers, followed by 4, 5, 14, and (probably more than) 24 structural isomers existing for Hg₇, Hg₈, Hg₉, and Hg₁₀, respectively. Since the main interest of the present work is on pressure-induced phase changes, several conditions must be obeyed for the cluster to be useful for related computations: (a) metastable, energetically richer isomers must have smaller volumes than the stable, lowestenergy isomer (so that the decreased PV term in the cluster enthalpy is able to compensate the increased cluster energy if metastable isomers get into play) and (b) differences between binding energies of the isomers must be small enough (so that such a compensation can efficiently apply at not too high pressures). Two Hg_N clusters meet these conditions for the cluster sizes considered here: Hg₈ (the binding energies and volumes of its structural isomers are shown in Table 1) and Hg₉, the first metastable isomer of which has the volume by about $\Delta V_e \approx 30 \text{ Å}^3$ smaller than the stable isomer while its binding energy is only slightly higher ($\Delta D_{\rm e} \approx 15$ meV).²³ For computational reasons, the smaller cluster, Hg₈, is considered.

The rest of the paper is organized as follows. First, methodological and computational approaches relevant to the present computations (electronic structure model and simulation methods, including methods for finite system volume evaluation) are summarized in Sec. 2, then, main results (temperature and/or pressure dependent photoabsorption spectra of the Hg₈ cluster, including resolved contributions from various structural isomers) are presented and discussed in Sec. 3, and finally, conclusive remarks and outlooks are provided in Sec. 4.

Methods and computations

The photoabsorption spectrum of a system is quantitatively represented via the effective photoabsorption cross-section. For a flexible system, it is calculated, within a semiclassical approximation, from the probabilities of transitions from the electronic ground-state to relevant electronically excited states which are averaged over an ensemble of (classical) nuclear ambient configurations corresponding particular to conditions,24,25

$$\sigma(E_{\rm phot}) = \lim_{\Delta E \to 0} \frac{1}{\Delta E} \frac{\pi}{3\varepsilon_0 c \hbar} \frac{\sum_{\mathscr{K}=1}^{\mathscr{N}} \sum_{\rm a} E_{\rm a}^{(\mathscr{K})} |\mu_{\rm a}^{(\mathscr{K})}|^2 \delta_{\Delta E} (E_{\rm a}^{(\mathscr{K})} - E_{\rm phot})}{\mathscr{N}}. \tag{1}$$

In this equation, σ is the photoabsorption cross-section, $E_{\rm phot}$ denotes the energy of the impacting photon, & distinguishes between different nuclear configurations sampled on the system ground-state potential energy surface, the first sum on the right-hand-side runs over a sufficiently large ensemble of such configurations, the second sum covers all the relevant electronic states of the system with $E_a^{(\mathcal{K})}$ and $\mu_a^{(\mathcal{K})}$ respectively denoting their vertical excitation energies and transition dipole moments from the ground state, and $\delta_{\Delta E}(X) = 1$ for $|X| \leq \Delta E/2$ and zero otherwise. The other symbols have the usual meaning, ε_0 is the vacuum permittivity, c stands for the vacuum light velocity, and $\hbar = h/2\pi$ denotes the reduced Planck constant.

The following is thus needed for a photoabsorption crosssection calculation: (a) an electronic structure method providing, with a sufficient accuracy, electronic energies of both the electronic ground-state and all relevant excited states as well as related transition dipole moments and (b) an efficient method for sampling nuclear configurations. The former subject (a) has already been described in detail in the preceding paper²² (as well as in other studies cited therein) and only a short account is provided for reader's convenience in the

Table 1 Classical (D_e) and quantum (D_0) atomization energies ($Hg_8 \rightarrow 8Hg$), monomer evaporation energies ($Hg_8 \rightarrow Hg_7 + Hg$, ΔD_e and ΔD_0 , respectively), principal values of the moment of inertia (divided by the atomic mass), and classical volumes (V_e) of structural isomers of the $electronically\ ground-state\ Hg_{8}\ cluster.\ All\ the\ energies\ are\ given\ in\ eV,\ inertia\ moments\ and\ volumes\ are\ provided\ in\ \mathring{A}^{2}\ and\ \mathring{A}^{3},\ respectively,\ and\ delectronically\ ground-state\ Hg_{8}\ cluster.$ all the values are rounded to the last significant digit

Isomer	Symmetry	$D_{ m e} \left(\Delta D_{ m e} ight)$	$D_0 \left(\Delta D_0 ight)$	Moments of inertia	$V_{ m e}$
1	C_{s}	1.289 (0.170)	1.222 (0.162)	32.7 46.3 58.5	225
2	$C_{ m 2v}$	1.288 (0.170)	1.221 (0.160)	31.0 47.1 52.8	220
3	$D_{ m 3d}$	1.227 (0.108)	1.162(0.101)	23.8 62.4 62.4	207
4	$C_{ m 2v}$	1.209 (0.091)	1.145 (0.085)	33.1 50.4 59.7	209
5	$T_{ m d}$	1.199 (0.081)	1.137 (0.076)	46.9 46.9 46.9	247

immediately following subsection. The methods of sampling nuclear configurations (b) are discussed in a somewhat greater detail afterwards.

2.1. Electronic structure calculations

The effective electronic Hamiltonian used in our calculations is constructed within the diatomics-in-molecules (DIM) approach.²⁶ This method consists of writing the overall electronic Hamiltonian operator as a sum of diatomic and atomic contributions,

$$\hat{H} = \sum_{K=1}^{N-1} \sum_{L=K+1}^{N} \hat{H}_{KL} - (N-2) \sum_{K=1}^{N} \hat{H}_{K}, \tag{2}$$

and expanding the corresponding Hamiltonian matrix over a properly chosen basis set of electronic wave functions. This leads to Hamiltonian matrix elements expressed in terms of diatomic and atomic energies. In our calculations, a specific DIM model has been used as originally proposed by Kitamura. Of this model, the basis set comprises valence-bond wave functions representing all the $6s^2 \rightarrow 6s^16p^1$ atomic excitations localized on particular Hg atoms and another wave function of the same kind corresponding to an ensemble of Hg atoms in their electronic ground state $(6s^2)$. As a consequence, totally 12N+1 basis functions are used for a Hg $_N$ cluster. As discussed in the preceding paper, the model should be capable to realistically describe the photoabsorption of the Hg $_N$ clusters up to photon energies of about $E \approx 7.5$ eV.

Since the basis sets usually used in DIM models are rather small, the method itself is not of a very high quality. Its popularity stems, however, from the known fact that its accuracy can be dramatically increased if highly accurate diatomic and atomic inputs are employed (as discussed, e.g., for rare-gas cluster cations in ref. 27-29). These inputs are usually taken from high-level ab initio calculations and/or experiments. In this way, reliable results can be obtained for large systems, e.g., at the expense of ab initio calculations performed on much smaller subsystems (diatomic and atomic fragments). In our calculations, diatomic inputs have been taken from accurate ab initio calculations,30-32 and the atomic inputs, namely the atomic excitation energies (without the inclusion of the spinorbit coupling) of the $6s^2(^1S) \rightarrow 6s^16p^1(^1P)$ and $6s^2(^1S) \rightarrow$ 6s¹6p¹(³P) transitions, have been adopted as proposed in ref. 10. For a more detailed description, see either our preceding paper²² or the original papers by Kitamura. 10,11

Another important advantage of the DIM approach, when applied to mercury clusters, is the possibility to easily include the spin-orbit (SO) coupling¹⁰ using a simple atoms-in-molecules scheme.³³ Most importantly, this approach does not extend the dimension of the electronic Hamiltonian matrix and requires only two additional parameters to be supplied from outside. Specifically, a parameter representing the SO splitting of the ³P electronic state of the Hg atom is needed together with another parameter quantifying the interaction between the ³P and ¹P atomic states. In this work, the two SO coupling constants have been derived from experimental data as reported in ref. 34.

he transition dipole moments (TDMs) between the Hg_N electronic ground-state and excited states have been calculated, as proposed in ref. 10 and used in our preceding paper, 22 from another atoms-in-molecules model. After some computations (see ref. 22 for a detailed explanation), the following formula is obtained after one denotes the electronic ground state of the Hg_N cluster by $|X\rangle$ and a particular excited state by $|\Psi\rangle$,

$$\left|\left\langle \Psi\right|\overrightarrow{\mu}\left|X\right\rangle\right|^{2} = \mu_{11}^{2} \sum_{M_{I}} \left|C_{M_{L}}\right|^{2},\tag{3}$$

where $C_{M_L} = \sum_K c_{K_0 M_L 0}^{\Psi}$ and $c_{K_0 M_L 0}^{\Psi}$ represents the expansion coefficient of the Hg_N excited state, $|\Psi\rangle$, with respect to the DIM basis set wave function corresponding to the ¹P atomic (Hg) excitation localized on atom *N* and with the projection of the electronic orbital angular momentum M_L ; μ_{11} is the atomic TDM corresponding to the ¹S \rightarrow ¹P transition, $\mu_{11} = 1.55$ bohr.¹⁰

2.2. Sampling of nuclear configurations

A Monte Carlo method for sampling in the isothermal–isobaric ensemble has been used. The method is based on a usual Metropolis algorithm,³⁵ originally proposed for canonical (isothermal–isochoric) simulations, with only the canonical weight, $\rho_c \sim \exp[-\beta E(\mathbf{R})]$, replaced by a weight appropriate for the isothermal–isobaric ensemble,

$$\rho \sim e^{-\beta [E(\mathbf{R}) + PV(\mathbf{R})]}.$$
 (4)

Here, $E(\mathbf{R})$ and $V(\mathbf{R})$ are the potential energy of the electronic ground state of the cluster and its volume, respectively, both calculated for cluster configuration \mathbf{R} , and β and P stand for reciprocal temperature ($\beta = 1/k_BT$) and external pressure, respectively. More specifically, the algorithm consists of two repeatedly performed steps. First, a new configuration, \mathbf{R}_{new} , is proposed from the current one, R_{\varkappa} , using a random and isotropic displacement of a one-by-one selected atom36 and, then, the new configuration is accepted, $\mathbf{R}_{\mathcal{K}+1} = \mathbf{R}_{\text{new}}$, with probability min $\{1, \rho(\mathbf{R}_{\text{new}})/\rho(\mathbf{R}_{\mathcal{K}})\}$ and rejected, $\mathbf{R}_{\mathcal{K}+1} = \mathbf{R}_{\mathcal{K}}$, with complementary probability, $\max\{0, 1 - \rho(\mathbf{R}_{\text{new}})/\rho(\mathbf{R}_{\mathcal{K}})\}$ The cluster volume has been estimated, after each proposal step, as the volume of a convex hull of nuclei represented by spheres of a radius equal to the van der Waals radius of the mercury atom $(r = 1.55 \text{ Å})^{37,38}$. An in-house code implementing the QuickHull algorithm39 has been used for cluster convex hull calculations. The maximum distance of the displacement in the proposal step has been adjusted dynamically so that the average acceptance probability has been kept around 0.5.40 The simulated cluster has always been placed in a hard-wall spherical container of radius $R_c = 100 \text{ Å}$ to avoid escapes of atoms to "infinity", which may occur at high temperatures and low pressures and which would eventually lead to the crash of a particular simulation.

A cycle comprising all the attempts to change the positions of all the atoms in the cluster will be denoted as a sweep. Typically, 13×10^6 sweeps have been generated for each temperature and pressure with 5×10^5 of them ignored at the

Paper RSC A

beginning of each simulation to allow a proper equilibration of the simulated cluster. Only each 50th sweep has been taken into account afterwards to avoid non-physical correlations between generated samples. As a consequence, about $\mathcal{N} \approx 2.5 \times 10^5$ cluster configurations have been used in eqn (1).

A parallel-tempering algorithm^{41–43} has been employed to enhance the efficiency of convergence of performed simulations. Such an enhancement is necessary for larger clusters, unlike the preceding calculations²² focusing on clusters for which only one minimum exists on their ground-state potential energy surfaces, since, in the present work, several structurally different minima are involved and transitions between them have to be included properly. A two-dimensional variant of the parallel-tempering approach⁴⁴ has been used consisting in (a) simulating the cluster at different temperatures and pressures in parallel and (b) periodically swapping configurations between neighboring temperatures and/or pressures. To preserve the detailed balance, a proposed swap of configurations between systems A and B has been accepted with probability⁴⁴

$$P_{A \leftrightarrow B} = \min \left\{ 1, \frac{e^{-\beta_A (E_B + P_A V_B)} e^{-\beta_B (E_A + P_B V_A)}}{e^{-\beta_A (E_A + P_A V_A)} e^{-\beta_B (E_B + P_B V_B)}} \right\}$$
 (5)

and rejected with the complementary probability, $1-P_{\text{A}\leftrightarrow\text{B}}$. The swaps between neighboring temperatures and pressures have been evoked with a period of one sweep and the pairs of (neighboring) systems to be swapped have been chosen by random. Grids of $n_T=36$ temperatures between $T_{\min}=5$ K and $T_{\max}=150$ K⁴⁵ and $n_P=12$ pressures between $P_{\min}=10^5$ Pa and $P_{\max}=10^9$ Pa have been employed with geometric progressions obeying $T_j=T_{\min}(T_{\max}/T_{\min})^{(j-1)/(n_T-1)}$ and $P_k=P_{\min}(P_{\max}/P_{\min})^{(k-1)/(n_P-1)}$. In this way, the average swapping rate has mostly been between 0.5 and 1.0 for all performed simulations and has never dropped below 0.2.

As a complement to the Monte Carlo sampling described above, another sampling approach has also been used to identify contributions of various structural isomers of the simulated cluster to the overall photoabsorption spectrum. This approach consists of sampling cluster configurations from the square of the ground-state nuclear vibrational wave functions calculated at the harmonic approximation level (see, e.g., ref. 46). It means that, first, equilibrium geometries of different structural isomers are found as local minima on the cluster (ground-state) potential energy surface and, then, the Hessian matrix is calculated for each isomer and diagonalized. The latter leads to harmonic vibrational frequencies and normal vibrational modes of the cluster. The ground-state vibrational wave function is then expressed as a product of independent normal modes Gaussians, which can easily be used to sample normal modes coordinates. Finally, the eigenvectors of the Hessian matrix enable to return back to simulation (usually Cartesian) coordinate system. Effectively, this sampling approach corresponds to a full quantum description of nuclei moving around the potential energy minimum corresponding to a particular structural isomer of the cluster at zero temperature and zero pressure.

3. Results and discussions

3.1. Structures and zero-temperature photoabsorption spectra of Hg₈ structural isomers

We start our discussion with analyzing contributions of different structural isomers of the Hg₈ cluster to its overall photoabsorption spectrum. For this, spectra of particular isomers found for this cluster have been calculated using their ground-state vibrational wave functions obtained at the harmonic approximation level.

First, the isomers have been identified by locally optimizing the configurations resulting from high-temperature runs of the performed Monte Carlo simulations. Results are summarized in Tables 1 and 2. Altogether, five isomers have resulted from these optimization calculations. Interestingly, the first metastable isomer (isomer 2), has almost the same binding energy as the stable isomer (isomer 1), either with the zero-point energy considered or not, despite the fact that their equilibrium geometries are quite different. As a consequence, both isomers may play a role even at low temperatures and, at the same time, their contributions to the photoabsorption spectrum of Hg₈ are expected to visibly differ from each other. The other isomers are somewhat higher in energy and they cannot get into play at temperatures below $T \approx 40\text{--}60 \text{ K}$ (a rough estimate made from the assumption of the equipartition of thermal energy). Another interesting observation is obvious if one inspects estimated volumes of the isomers. Except for the highest isomer (isomer 5), all the other metastable isomers have the volumes significantly lower than the stable one. As a consequence, these isomers are expected to gradually enter the game as the external

Table 2 Graphical representations of the structural isomers of ${\rm Hg_{8}}$. For a better idea, two perpendicular views are provided for each isomer (note that the front view and side view of isomer 5 are identical due to its high symmetry)

Isomer	Front view	Side view	
1		•	
2	•		
3			
4		8 .	
5			

pressure is increased (due to the *PV* term in eqn (4)). This particularly holds for isomer 2 which is only marginally higher in energy than the stable isomer.

The results of Table 1 can be directly compared with the data published recently by Calvo et al., 47 which were obtained using the same interaction model as that employed in the present work. In that study, however, only stable isomers have been reported for mercury clusters. For the Hg₈ cluster, the C_8 geometry of its stable isomer we have obtained from our calculations compares, on one hand, very well with the geometry reported in ref. 47. The binding energy provided for this isomer by Calvo et al. ($D_{\rm e}=1.299$ eV) slightly differs, on the other hand, from our estimate ($D_e = 1.289$ eV). Since the Hg₈ potential energy surface is simple enough for any optimization method to arrive at a true global minimum, we believe that the observed deviation must be due to numerical differences in the interaction model implementations by Calvo et al. and ours. Probably different methods used to represent the diatomic inputs of the DIM model contribute.

A lot of other theoretical studies on the equilibrium structures of mercury clusters of small and medium sizes have been published in the literature. They comprise calculations based on semiempirical models,48,49 calculations using DFT-based methods,50-52 as well as post Hartree-Fock correlated calculations. 50,53,54 However, the data (most importantly, geometric structures and binding energies of the clusters) reported from those calculations differ significantly from one another and a thorough analysis of these differences goes clearly beyond the scope of the present work. Shortly, the DFT-based methods seem to provide a promising way towards a reliable modeling of structures and energetics of mercury clusters. For example, they provide51,52 basically the same equilibrium structure of the Hg8 cluster as that resulting from our calculations and similar calculations by Calvo et al. Reported binding energies, however, strongly depend on a particular exchange-correlation functional used.50-52 A proper inclusion of the dispersion interaction55 seems crucial.56

Photoabsorption spectra of the five structural isomers of Hg₈ are depicted in Fig. 1. All the isomers are considered in the main panel to get a global view while the absorption profiles of the two expectedly most important isomers 1 and 2 are depicted separately in the inset for clarity. As expected, quite complex structure of absorption peaks is seen if all the isomers are considered, mainly because their capability to absorb photons of various energies are quite different due to different geometric structures (see Table 1). For example, in the main absorption band observed between $E_{\rm phot} \approx 7.3$ eV and $E_{\rm phot} \approx 7.7$ eV, both the stable and all the metastable isomers contribute. The contributions of the metastable isomers are, however, visibly shifted, with respect to the peak attributed to the stable isomer 1, either to lower (isomers 2-4) or to higher (isomer 5) photon energies. Alike, the contributions of the metastable isomers at lower photon energies ($E_{\rm phot} \lesssim 7.0 \text{ eV}$) differ considerably from the contributions of the stable isomer as well as from one another. As a consequence, absorption features of specific structural isomers of Hg₈ are expected to be well distinguishable in the overall photoabsorption spectrum.

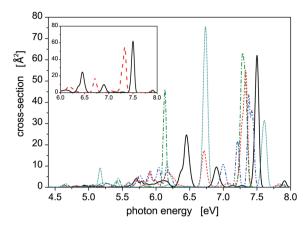


Fig. 1 Photoabsorption spectra of structural isomers of the Hg_8 cluster calculated at T=0 K using the harmonic zero-point nuclear vibration wave function, isomer 1- solid, isomer 2- dash, isomer 3- dash-dot, isomer 4- dash-dot-dot, isomer 5- dot. In the inset, a simplified view is provided comprising only isomers 1 and 1, i.e., the supposingly most relevant isomers under the conditions considered in this work.

Let us further briefly discuss another interesting question, namely how much the SO coupling influences the capability of the Hg₈ cluster to absorb photons of various energies. To illustrate this, photoabsorption spectra of isomer 1 and isomer 2, calculated using the DIM method with and without the inclusion of the SO coupling terms, are depicted in Fig. 2. Interestingly, the effect of the SO coupling is only moderate, maybe except for the region of $E_{\rm phot} \approx 5.5$ -6.3 eV where the differences between corresponding SO and SO-free curves are better pronounced. In the latter case, however, the absorption efficiency of the Hg8 cluster is only marginal and observed peaks are unimportant as compared to other photon energies. For the main absorption peaks, the exclusion of the SO coupling almost does not change their heights and only slightly shifts the peaks to lower photon energies (on average, by about 0.05 eV). This holds for both isomer 1 and isomer 2. Note, however, that

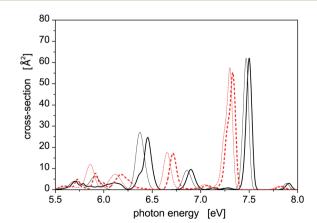


Fig. 2 Comparison of the photoabsorption spectra of structural isomers 1 (solid lines) and 2 (dashed lines) of the Hg_8 cluster calculated in the same way as the spectra reported in Fig. 1 with (thick lines) and without (thin lines) the spin–orbit coupling included.

regardless of this observation we do consider the SO coupling in all the remaining calculations reported in this work since no computational overhead is associated with doing so.

3.2. Dependence of the Hg₈ photoabsorption spectrum on temperature

Photoabsoprtion spectra of Hg₈ calculated at atmospheric pressure ($P=10^5$ Pa) and selected temperatures lying below the estimated evaporation temperature ($T_{\rm evap}\approx 110$ K)⁴⁵ are depicted in Fig. 3. In the recorded profiles, five main absorption peaks representing contributions of different isomers are seen. Interestingly, only two energetically lowest isomers contribute. The five peaks are best pronounced for the lowest temperature (T=10 K), three of them belonging to isomer 1 ($E_{\rm phot}\approx 7.5$ eV, $E_{\rm phot}\approx 6.9$ eV, and $E_{\rm phot}\approx 6.4$ eV) and two more corresponding to contributions of isomer 2 ($E_{\rm phot}\approx 7.3$ eV and $E_{\rm phot}\approx 6.7$ eV). As the cluster temperature increases, the peaks become broader and lower and the two peaks of isomer 1 and isomer 2 seen at $E_{\rm phot}\approx 7.3$ –7.5 eV gradually merge together.

Note that even for the highest temperature we have considered, no higher metastable isomers contribute (as verified by local optimizations of structures recorded during the simulations) even though they should if only energetic openness of their appearance were considered. For example, only traces of isomer 3 (0.03%) have been detected at T=90 K, not below, however, and no energetically reacher isomers 4 and 5 have been detected even at this rather high temperature. Probably, entropic effects are responsible for this behavior. Moreover, the stable isomer 1 prevails at all the temperatures considered, even though its abundance slightly decreases from about 75% obtained at T=10 K to about 65% recorded at T=90 K.

A note concerning the cluster temperature is needed here. All the calculations presented in this work have been performed using classical Monte Carlo methods, *i.e.*, nuclear quantum effects have not been considered explicitly. As discussed in the preceding paper,²² this may not be fully correct, despite the fact that heavy atoms are involved, if low temperatures are considered. Therefore, increased effective temperatures are needed in

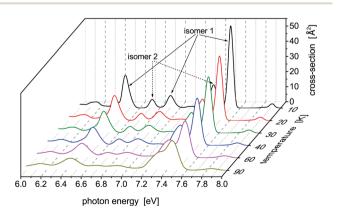


Fig. 3 Photoabsorption spectra of the Hg₈ cluster calculated *via* the classical isothermal–isobaric Monte Carlo approach at low pressure ($P = 10^5$ Pa) and various temperatures. Contributions of different structural isomers of Hg₈ are indicated for T = 10 K.

classical calculations to take quantum nuclear delocalization into account. For example, preliminary path-integral Monte Carlo⁵⁷ calculations seem to indicate that, in the case of the Hg₈ cluster, the lowest temperature considered in the present classical calculation, T=10 K, corresponds to $T_{\rm quant}\approx 5$ K used in the quantum calculation (photoabsorption spectra recorded at these two temperatures in classical and quantum calculations, respectively, are very close to each other) and that the classical and quantum temperatures become more or less the same once the temperature rises above $T\approx 15$ –20 K. As a consequence, the lowest temperature considered in this work represents a cluster temperature which would be about twice lower if nuclear quantum effects were taken into account while at higher temperatures nuclear quantum effects seem to disappear and classical simulations are highly probably fully applicable.

3.3. Dependence of the Hg_8 photoabsorption spectrum on pressure

While no dramatic changes occur in the photoabsorption spectrum of Hg_8 when the cluster temperature is increased, the situation is quite different if external pressure increases. This is clearly seen in Fig. 4 where the evolution of the Hg_8 photoabsorption spectrum with increasing pressure is depicted. For clarity, only two cluster temperatures are considered in two separate figure panels.

For the lower temperature (T = 10 K), the picture we obtained is better resolved and sharper. Up to $P \approx 150$ MPa, the stable isomer 1 dominates. However, at $P \approx 190$ MPa the contributions of isomer 1 and isomer 2 become more or less the same and, finally, at the highest pressure (P = 1 GPa) the contribution of isomer 1 completely disappears. A similar picture is seen for the higher temperature (T = 40 K), just the isomer 1 to isomer 2 transition is pushed to higher pressures (the contributions of the two isomers become of the same value at about $P \approx 450$ MPa) and even at P = 1 GPa isomer 1 still contributes. One can thus conclude that, at high pressures, isomer 2 of the Hg₈ cluster becomes more important than isomer 1 (due to its smaller volume) and that this fact is observably reflected in the Hg₈ photoabsorption spectrum by a well seen shift of the main absorption bands along the photon energy axis as pressure increases.

The increased role of isomer 2 is further illustrated in Fig. 5 where average abundances of isomers 1 and 2 are plotted, for selected temperatures, against the external pressure the cluster is subjected to. In this figure, the same features are seen as above: (a) the dominance of the stable isomer 1 at low pressures (irrespective of cluster temperature), (b) a transition from isomer 1 to isomer 2 at intermediate pressures (the higher is the cluster temperature, the higher pressure is needed), and (c) a dominance of isomer 2 at high pressures. Isomer 1 will highly probably completely disappear at sufficiently high pressures. In the pressure range considered in this work, this occurs for the lowest temperature. For higher temperatures, higher pressures (P > 1 GPa) would be needed, but the approach of the abundance of isomer 1 to zero with increased pressure is clear.

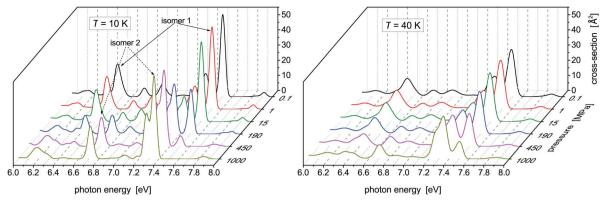


Fig. 4 Photoabsorption spectra of the Hg₈ cluster calculated via the classical isothermal-isobaric Monte Carlo approach at two representative temperatures and various pressures.

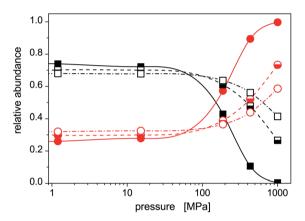


Fig. 5 Pressure dependences of relative abundances of isomer 1 (squares) and isomer 2 (circles) of the Hg₈ cluster calculated via the classical isothermal-isobaric Monte Carlo approach for selected cluster temperatures, solid symbols T = 10 K, half-filled symbols T = 40K, and open symbols T = 60 K.

Conclusions

Photoabsorption spectra of Hg₈ have been calculated for selected temperatures and pressures $(T \in [10, 90] \text{ K and } P \in [0.1,$ 1000] MPa) using a parallel-tempering Monte Carlo method for the classical isothermal-isobaric ensemble⁴⁴ and a diatomicsin-molecules electronic structure model. 10,11 The main emphasis has been placed on the identification of changes in the calculated spectra with increased cluster temperature and (mainly) external pressure and on relating them to structural (phase) changes occurring in the cluster. The structural changes themselves have been identified using relative abundances of structural isomers of the Hg8 cluster calculated at different temperatures and pressures by locally optimizing the Hg₈ geometries sampled in Monte Carlo simulations.

Five structural isomers have been found for the Hg₈ cluster (see Table 1 for a summary). However, only two of them, the stable isomer (isomer 1 in Table 1) and the energetically lowest metastable isomer (isomer 2), contribute at pressures and temperatures considered in this work. The photoabsorption spectra of the two isomers (see Fig. 1) differ visibly from each other and, consequently, changes in isomers abundances are well reflected in the overall photoabsorption profiles recorded for the Hg₈ cluster (see Fig. 3 and 4).

At low pressures, the evolution of the Hg₈ spectrum is smooth and no major (qualitative) changes are observed if cluster temperature is changed and pressure is kept constant. This is mainly due to the fact that the abundances of the two contributing isomers of the Hg₈ cluster do not change much with temperature in this pressure range.

If the external pressure is increased, on the other hand, well pronounced and significant changes are observed in the calculated photoabsorption spectra. Such behavior stems from a transition in the population of Hg₈ from the stable isomer to the lowest metastable isomer as pressure increases, mainly because the two isomers have close binding energies, but differ nonnegligibly in their volumes. The volume of isomer 2 is by about $\Delta V \approx 5 \,\text{Å}^3$ smaller than the volume of isomer 1. The PV term in the isothermal-isochoric statistical weight (see eqn (4)) induces then a decrease of the abundance of isomer 1 in the Hg₈ population in favor of isomer 2 as pressure increases and eventually leads to its complete disappearance (see Fig. 5). These changes are clearly reflected in the change of patterns seen in the Hg₈ photoabsorption spectrum as the external pressure increases.

Note also that similar effects, like those discussed in the present work for Hg₈, could as well be expected for other small Hg_N clusters (cf. a short discussion on this subject in the Introduction section). Presently, additional calculations are running with the main goal to in detail describe and understand pressure-induced phase changes in small mercury clusters and to analyze the possibility of their detection through Hg_N photoabsorption measurements.

Conflicts of interest

There are no conflicts of interest to declare.

Acknowledgements

A support by the Ministry of Education, Youth and Sports of the Czech Republic via the National Programme of Sustainability,

Paper RSC Advances

NPS II (grant no. LQ1602), is greatly acknowledged. The calculations have been performed using the IT4Innovations infrastructure supported from the Large Infrastructures for Research, Experimental Development and Innovations grant (LM2015070) and made available to us through computational grants OPEN-10-47 and OPEN-14-20. Partial financial support from VSB–Technical University of Ostrava (grants no. SP2019/162 and SP2019/84) is also acknowledged.

Notes and references

- 1 R. S. Berry, *Theory of Atomic and Molecular Clusters*, Springer, 1999, pp. 1–26.
- 2 R. S. Berry, *Handbook of Nanophysics. Principles and Methods*, CRC Press, 2017, pp. 20.1–20.15.
- 3 A. Vítek, A. Ofiala and R. Kalus, *Phys. Chem. Chem. Phys.*, 2012, 14, 15509.
- 4 A. Vítek, D. J. Arismendi-Arrieta, R. Rodríguez-Cantano, R. Prosmiti, P. Villarreal, R. Kalus and G. Delgado-Barrio, Phys. Chem. Chem. Phys., 2015, 17, 8792.
- 5 F. A. Lindemann, Z. Phys., 1910, 11, 609.
- 6 H. Haberland, *Atomic Clusters and Nanoparticles*, Springer, 2000, pp. 29–56.
- 7 C. Bréchignac, M. Broyer, P. Cahuzac, G. Delacretaz, G. Labastie and L. Wöste, *Chem. Phys. Lett.*, 1985, 120, 559.
- 8 C. Bréchignac, M. Broyer, P. Cahuzac, G. Delacretaz, G. Labastie, J. P. Wolf and L. Wöste, *Phys. Rev. Lett.*, 1988, **60**, 275.
- 9 K. Rademann, M. S. O. Dimopoulou-Rademann, U. Even and F. Hensel, *Phys. Rev. Lett.*, 1992, **69**, 3208.
- 10 H. Kitamura, Chem. Phys., 2006, 325, 207.
- 11 H. Kitamura, Chem. Phys. Lett., 2006, 425, 205.
- 12 H. Haberland, B. von Issendorff, J. Yufeng and T. Kolar, *Phys. Rev. Lett.*, 1992, **69**, 3212.
- 13 H. Haberland, B. von Issendorff, J. Yufeng, T. Kolar and G. Thanner, *Z. Phys. D: At., Mol. Clusters*, 1993, **26**, 8.
- 14 S. Grabowski, M. E. Garcia and K. H. Bennemann, *Phys. Rev. Lett.*, 1994, 72, 3969.
- 15 B. Kaiser and K. Rademann, Phys. Rev. Lett., 1992, 69, 3204.
- 16 J. Blanc, M. Broyer, P. Dugourd, P. Labastie, M. Sence, J. P. Wolf and l. Wö, *J. Chem. Phys.*, 1995, **102**, 680.
- 17 H. Uchtmann, R. Dettmer, S. D. Baranovskii and F. Hensel, *J. Chem. Phys.*, 1998, **108**, 9775.
- 18 M. E. Garcia, D. Reichardt and K. H. Bennemann, J. Chem. Phys., 1998, 109, 1101.
- 19 M. E. Garcia, H. O. Jeschke, I. Grigorenko and K. H. Bennemann, *Appl. Phys. B*, 2000, **71**, 361.
- 20 N. Gaston, P. Schwerdtfeger and B. von Issendorff, *Phys. Rev.* A, 2006, 74, 043203.
- 21 Note that only an incomplete selection of the published studies can be given here due to limited space and interested readers are referred to the cited references for a more complete view.
- 22 R. Ćosić, A. Vítek and R. Kalus, *Phys. Chem. Chem. Phys.*, 2018, **20**, 28871.
- 23 The metastable isomer of the Hg₆ cluster has as well smaller volume than the stable one (by about $\Delta V_{\rm e} \approx 2~{\rm \AA}^3$), but its

energy is too high ($\Delta D_{\rm e} \approx 45~{\rm meV}$) for it to become important unless very high pressures are involved. For the remaining cluster sizes, Hg₇ and Hg₁₀, all the metastable isomers have larger volumes than corresponding stable ones and no pressure-induced phase changes are thus expected in these clusters.

- 24 A. Bastida and F. X. Gadea, Chem. Phys., 1996, 209, 291.
- 25 T. Ikegami and S. Iwata, J. Chem. Phys., 1996, 105, 10734.
- 26 F. O. Ellison, J. Am. Chem. Soc., 1963, 85, 3540.
- 27 P. J. Kuntz and J. Valldorf, Z. Phys. D: At., Mol. Clusters, 1988, 8, 195.
- 28 M. Amarouche, G. Durand and J. P. Malrieu, *J. Chem. Phys.*, 1988, **88**, 1010.
- 29 P. Milko, R. Kalus, I. Paidarová, J. Hrušák and F. X. Gadéa, *Theor. Chem. Acc.*, 2009, **124**, 169.
- 30 E. Czuchaj, F. Rebentrost, H. Stoll and H. Preuss, *Chem. Phys.*, 1997, 214, 277.
- 31 E. Pahl, D. Figgen, C. Thierfelder, K. A. Petterson, F. Calvo and P. Schwerdtfeger, *J. Chem. Phys.*, 2010, **132**, 114301.
- 32 The ground-state potential of ref. 31 has been represented by an analytic formula reported therein for the CCSDT data and the discrete points calculated for electronically excited states of Hg₂ in ref. 30 have been interpolated *via* cubic splines.
- 33 J. S. Cohen and B. I. Schneider, J. Chem. Phys., 1974, 61, 3230.
- 34 P. J. Hay, J. T. H. Dunning and R. C. Raffenetti, *J. Chem. Phys.*, 1976, **65**, 2679.
- 35 N. Metropolis, A. W. Rosenbluth, M. N. Rosenbluth, A. H. Teller and E. Teller, *J. Chem. Phys.*, 1953, 21, 1087.
- 36 The following procedure has been employed in our calculations to generate isotropic atomic displacements. First, a random vector, $\Delta \vec{r}$, has been proposed with components selected uniformly from interval $[-d_{\text{max}}, d_{\text{max}}]$, d_{max} being the current maximum size of the atomic displacement. Then, if the vector belongs to a sphere of radius d_{max} , $\Delta r \leq d_{\text{max}}$, the coordinates of the particular atom have been changed by adding it, otherwise a new attempt to generate $\Delta \vec{r}$ has been performed.
- 37 A. Bondi, J. Phys. Chem., 1964, 68, 441.
- 38 The volume of the cluster depends on a particular estimate of the atomic van der Waals radius since, for a convex hull of non-overlaping spheres of radius r, the following formula holds (see, e.g., ref. 58): $V(r) = V_0 + A_0 r + M_0 r^2 + 4/2 r^2$ $3\pi r^3$ with V_0 , A_0 , and M_0 being respectively the cluster volume, surface, and integral mean curvature calculated for r = 0. As a consequence, if a value of the Hg van der Waals radius different from that used in the present calculation is considered, the estimates of the pressures at which structural changes take place in Hg₈ will change. This change adopts a form of a simple multiplicative scaling and it follows from our calculations that this scaling is almost identical for all the isomers found for Hg_8 , $P(r) \approx P(r = 1.55)/(0.07234 + 0.44038r + 0.04795r^2 + 0.04795r^3)$ $0.03493r^3$), where r is to be provided in A. As a consequence, this simple scaling rule may be used to easily recalculate transition pressures provided in this work to those corresponding to different estimates of r.

39 C. B. Barber, D. P. Dobkin and H. Huhdanpaa, *ACM Trans*.

- 39 C. B. Barber, D. P. Dobkin and H. Huhdanpaa, *ACM Trans. Math Software*, 1996, **22**, 469.
- 40 The maximum displacement has been adjusted each 20th sweep (all-atoms move) by multiplying or dividing its current value by 1.05, a factor only slightly different from 1. Further, it is important to emphasize that a systematic drift of the maximum displacement value has only occurred during the equilibration phase of performed calculations, during which sampled configurations have been discarded. After equilibrium has been achieved, only small-magnitude oscillations around the desired value (0.5) have been observed. The detailed balance conditions have thus been only marginally disturbed by these adjustments.
- 41 R. H. Swendsen and J. S. Wang, *Phys. Rev. Lett.*, 1986, 57, 2607.
- 42 C. J. Geyer, Computing Science and Statistics Proceedings of the 23rd Symposium on the Interface, New York, 1991, p. 156.
- 43 C. J. Geyer and E. A. Thompson, *J. Am. Stat. Assoc.*, 1995, **90**, 909
- 44 T. Okabe, M. Kawata, Y. Okamoto and M. Mikami, *Chem. Phys. Lett.*, 2001, 335, 435.
- 45 The upper temperature used in the present parallel tempering calculations has been chosen so that it is well above the lowest estimate of the Hg_8 evaporation temperature ($T_{\rm evap}^{\rm (min)} \approx 110$ K) and, consequently, should be sufficiently high for overcoming the barriers which may be present on the Hg_8 potential energy surface. The lowest estimate of the evaporation temperature has been calculated form the assumption of the equipartition of the

- thermal energy in the Hg₈ cluster and from the energy difference ($\Delta D_{\rm e}$) between equilibrium structures of Hg₈ and Hg₇, (3 × 8 6) $k_{\rm B}T_{\rm evap}^{\rm (min)} = \Delta D_{\rm e} \approx 0.17$ eV (in the present work, the classical binding energy of Hg₇ is estimated to $D_{\rm e} = 1.119$ eV).
- 46 N. L. Doltsinis and P. J. Knowles, Chem. Phys. Lett., 1999, 301, 241.
- 47 F. Calvo, E. Pahl, P. Schwerdtfeger and F. Spiegelman, *J. Theor. Comput. Chem.*, 2012, **8**, 639.
- 48 B. Hartke, H.-J. Flad and M. Dolg, *Phys. Chem. Chem. Phys.*, 2001, 3, 5121.
- 49 H. Kitamura, Eur. Phys. J. D, 2007, 43, 33.
- 50 N. Gaston and P. Schwerdtfeger, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2006, 74, 024105.
- 51 J. Kang, J. Kim, H. Ihee and Y. S. Lee, J. Phys. Chem. A, 2010, 114, 5630.
- 52 A. S. Chaves, M. J. Piotrowski and J. L. F. D. Silva, *Phys. Chem. Chem. Phys.*, 2017, **19**, 15484.
- 53 G. E. Moyano, R. Wesendrup, T. Söhner and P. Schwerdtfeger, Phys. Rev. Lett., 2002, 89, 103410.
- 54 Y. Wang, H.-J. Flad and M. Dolg, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2000, **61**, 2362.
- 55 R. Hatz, V. Hänninen and L. Halonen, *J. Phys. Chem. A*, 2014, **118**, 5734.
- 56 F. Karlický and M. Novotný, University of Ostrava, unpublished results.
- 57 D. M. Ceperley, Rev. Mod. Phys., 1995, 67, 279.
- 58 L. Maibaum, M. Schmidt and H. Löwen, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2001, **63**, 051401.