Investigation of the structural, optical, elastic and electrical properties of spinel LiZn\(_2\)Fe\(_3\)O\(_8\) nanoparticles annealed at two distinct temperatures\(^\dagger\)

D. Bouokkeze,\(^a\) J. Massoudi,\(^b\)\(^*\) W. Hzez,\(^a\) M. Smari,\(^b\) A. Bougoffa,\(^b\) K. Khirouni,\(^c\)\(^*\) E. Dhahri\(^b\)\(^*\) and L. Bessais\(^c\)

Nanoparticles of Li\(_{0.5}\)ZnFe\(_{1.5}\)O\(_4\) (LiZn\(_2\)Fe\(_3\)O\(_8\)) with the spinel structure were prepared by a sol–gel auto-combustion method at two different annealing temperatures. X-ray diffractograms and Rietveld refinement confirmed the formation of the spinel structure. The morphology was analyzed by electron microscopy, which showed that the grains were composed of different crystallites. Elastic properties were determined from infrared spectroscopy. It was found that the elastic parameters increased with the increase in annealing temperatures. The band gap depends on the annealing temperature and it decreased on increasing the particle size. The conductivity of the specimen annealed at 500 °C followed either the Jonscher’s model or Drude’s model depending on the temperature range. This conductivity decreased when the annealing temperature was raised by 600 °C. AC conductivity was found to be controlled by the hopping model. A single relaxation phenomenon was evidenced for each sample from impedance analysis. The Nyquist diagram proved that the samples were simultaneously capacitive and resistive and also supported the presence of multiple relaxation times.

1. Introduction

Ceramics like metals and polymers are receiving significant attention from scientists and even companies on account of their interesting features that lead to various potential applications.\(^7\) Among them, spinel, with formula AB\(_2\)O\(_4\), where A represents a tetrahedral site and B refers to an octahedral site,\(^3\) has received special interest. On account of having multiple properties, scientists have never stopped considering spinel as an exciting matter for potential applications. Iron ions with magnetic properties due to their unpaired d electrons and electrical properties due to the relatively easy release of d electrons make most ferrite spinels multiferroic. These features elucidate why more scientific curiosity is targeted towards ferrite as compared to other spinels, as evidenced by the tremendous number of characterizations conducted on it.\(^7\)\(^6\) It has been found that ferrite possesses many applicable distinguishable properties,\(^7\)\(^8\) which are sensitive to composition.\(^8\) In this context, ferrite has been treated with a wide range of chemical elements, such as Zr, Zn,\(^6\) Ni,\(^10\) and Co,\(^11\) for better satisfying the requirements of today. Relatively strong qualities were obtained by inserting Zn into the matrix, e.g., the high electrical resistivity of ZnFe\(_2\)O\(_4\).\(^12\) This high resistivity makes ferrite with Zn a suitable candidate for certain applications, such as circulators, isolators, and phase shifters.\(^6\) Doping with Zn seems to expand the range of applications of spinel. For further widening this range, one of the practical hints is to fill the A-site with lithium\(^13\) because ferrite with lithium has been found to serve as an excellent solid-state electrolyte.\(^1\) In this paper, we elaborate and report the spinel oxide of Li\(_{0.5}\)ZnFe\(_{1.5}\)O\(_4\). Since it contains zinc with a relatively low volatilization temperature, it involves a low sintering temperature, which makes the preparation process less expensive as compared with that of other spinels.\(^14\)

According to Reddy \emph{et al.}, one may predict some physical properties of ferrite by looking at the magnitude and type of its conductivity.\(^*\) However, which carriers are responsible for conductivity in lithium ferrite with a spinel structure is a matter of debate. This poor understanding of the origin of conductivity is due to the simultaneous presence of Li\(^+\) with mixed-valence transition metal ions, Fe\(^{2+}\) and Fe\(^{3+}\) in our case. This paper addresses the electrical properties of the considered lithium zinc ferrite. Since conductivity depends on the preparation
conditions including annealing temperature,15,16 we annealed the specimens in question at 500 °C and 1100 °C. After discussing the structure of the liquid phase, we explain in detail the transport properties by combining conductivity and impedance formalism. The optical properties, under UV-visible irradiation, are reported. The main aim of this study is to determine some key optical and elastic parameters pertaining to the size of the particle; in spite of being equivalent, they provide distinct information. Further characterizations will be conducted.

2. Experimental section

Analytical reagents of Fe(NO$_3$)$_3$·9H$_2$O, Zn(NO$_3$)$_2$·6H$_2$O, LiNO$_3$ and Cu$_2$H$_2$O$_7$ were obtained from Sigma-Aldrich and used as received without purification. Li$_{0.5}$ZnFe$_{1.5}$O$_4$ was synthesized by a facile sol-gel auto combustion method followed by annealing at 500 and 1100 °C. In a typical experiment, stoichiometric amounts of Fe(NO$_3$)$_3$·9H$_2$O, Zn(NO$_3$)$_2$·6H$_2$O and LiNO$_3$ were dissolved in 100 ml of distilled water with vigorous stirring to form a solution, followed by the addition of citric acid (C$_6$H$_7$O$_5$) with a 1:2 molar ratio of metal cation (Fe + Zn + Li) to citric acid. The resulting mixed solution was magnetically stirred at 80 °C until a viscous gel was formed. The viscous gel was heated on a hot plate at 300 °C until it self-ignited, yielding dark brown ash. The auto combustion was carried out using a vacuum thermal evaporator. A silver wire was then attached by silver lacquer on each side. The explored range of samples had to be in the form of dipoles so a silver thin film of nanometers thickness was coated on the face of each pellet using a vacuum thermal evaporator. A silver wire was then attached by silver lacquer on each side. The explored range of frequency was between 40 Hz and 110 MHz. The temperature ranged from 300 K to 600 K. The samples were characterized under an excitation alternative signal of 50 mV. Absorption spectra were obtained at room temperature using a Shimadzu UV-3101PC scanning spectrophotometer.

3. Results and discussion

3.1 Thermal analysis

In order to investigate the formation process of the Li$_{0.5}$ZnFe$_{1.5}$O$_4$ powders, thermogravimetric measurements were used to analyze the thermal behavior of the reagents. Fig. 1 shows the typical TGA and DTG curves obtained for the as-burnt powder. It can be seen from Fig. 1 that the TGA curve can be divided into three regions with various processes taking place in each region, i.e., 10–175 °C, 175–425 and 425–1000 °C. In the first region (10–175 °C) the initial weight loss in the TGA curves is due to the loss of water molecules with a mass loss of 4%. A major weight loss can be seen in the second region (175–425 °C) in the TGA curve and the DTG curve could be attributed to the decomposition of unreacted reactants present in the as-prepared samples. The third region (425–1000 °C) of the TGA curve could be attributed to the crystallization of the self-combusted final product. It was concluded from the TGA results that an optimal temperature of 450 °C is suitable for annealing the as-prepared sample, and thus the samples that were used for further characterization were annealed at 500 °C (Zn500) and 1100 °C (Zn1100) for 8 h.

3.2 Structure and morphology

The Rietveld refinement of the X-ray diffraction patterns of LiZn$_2$Fe$_3$O$_8$ ferrites obtained for Zn500 and Zn1100 are shown in Fig. 2(a). The Rietveld FULLPROF program was used for the structural refinements.17 The XRD spectra confirmed the formation of a single-phase cubic spinel structure with a space group ($Fd\bar{3}m$) without any extra peaks of a secondary phase (ZnO or Fe$_3$O$_4$) and there is a good agreement between the calculated and observed profiles. As the sintering temperature increases, the peak width decreases due to an increase in crystallite size. The obtained Rietveld refinement parameters for the two samples were computed and are given in Table 1. More details

![Fig. 1 TGA-DTG curves of the as-burnt powder.](image-url)
in the Rietveld analyses have been reported in our previous work.\textsuperscript{18} Fitting parameters were found to be comparable to those of similar spinel ferrite samples.\textsuperscript{18,19} The unit cell parameters and atomic positions along with the AO\textsubscript{6} octahedral and BO\textsubscript{4} tetrahedral sites of the Li–Zn ferrite are shown in the inset of Fig. 2(a). For minimizing both systematic and random errors, an accurate estimation of the exact lattice constant \(a_0\) was made using the extrapolation function \(F(\theta)\), i.e., the Nelson–Riley (N–R) function, for each reflection of the studied ferrite samples.\textsuperscript{20}

\[
F(\theta) = \frac{1}{2} \left[ \frac{\cos^2 \theta}{\sin \theta} + \frac{\cos^2 \theta}{\theta} \right]
\]

The values of the lattice parameters obtained from each reflected plane were plotted against the N–R function and are shown in Fig. 2(c). It can be observed from Table 1 that there is a small deviation between the exact \((a_0)\) and Rietveld \((a_R)\) values of the lattice parameter. The exact values of the lattice parameter were observed to be slightly small as compared to the

<table>
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<tr>
<th>Parameter</th>
<th>Zn500</th>
<th>Zn1100</th>
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<tr>
<td>(a_0) (Å)</td>
<td>8.390</td>
<td>8.404</td>
</tr>
<tr>
<td>(a_R) (Å)</td>
<td>8.391</td>
<td>8.405</td>
</tr>
<tr>
<td>(V) (Å(^3))</td>
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</tr>
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<td>(R_p) (%)</td>
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<td>50.7</td>
</tr>
<tr>
<td>(R_w) (%)</td>
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<td>17.7</td>
</tr>
<tr>
<td>(R_e) (%)</td>
<td>11.6</td>
<td>14.5</td>
</tr>
<tr>
<td>(\chi^2)</td>
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<td>1.477</td>
</tr>
<tr>
<td>(D_{BC}) (nm)</td>
<td>17</td>
<td>45</td>
</tr>
<tr>
<td>(D_{W-H}) (nm)</td>
<td>15</td>
<td>32</td>
</tr>
<tr>
<td>(\varepsilon)</td>
<td>(-8.10^{-4})</td>
<td>(-10^{-3})</td>
</tr>
</tbody>
</table>
Rietveld values. It is also evident that both the exact and Rietveld lattice parameters decrease with the decrease in the particle size. G. Datt et al. have reported that the decrease in the lattice constant with the increase of the annealing temperature of the Ni–Co ferrite nanoparticles is attributed to the presence of OH\(^{-}\) groups in the crystalline structure due to the synthesis process. However, the low values of the goodness of fit \( \chi^2 \) are quite satisfactory for the refinement, indicating that the quality of fit for these XRD patterns was quite good and that the samples obtained were of high quality. The average crystallite size of the ferrite samples was calculated by using the Scherrer equation for the line broadening of the most intense (311) peak:

\[
\beta \cos \theta = \frac{K\lambda}{D_{sc}}
\]

where \( D_{sc} \) is the crystallite size, \( K \) is a dimensionless shape factor whose value is taken to be \( 0.9 \), \( \lambda \) is the wavelength of Cu K\( \alpha \) radiation (1.5406 Å), \( \theta \) is the diffraction Bragg angle of the most intense peak (311) and \( \beta \) is the full-width at half maximum intensity (FWHM). The estimated crystallite sizes \( D_{sc} \) were around 17 nm and 45 nm for Zn500 and Zn1100, respectively. The line width (\( \beta \)) was measured for different XRD peaks corresponding to the different \((hkl)\) planes and the average crystallite size \( D_{W-H} \) can be calculated using the Williamson–Hall equation:

\[
\beta \cos \theta = \frac{K\lambda}{D_{WH}} + 4\epsilon \sin \theta
\]

This gives a linear relationship between \( \beta \cos \theta \) and \( 4 \sin \theta \) and the intercept of the line gives the crystallite size \( D_{W-H} \) while the slope gives the induced strain \( (\epsilon) \). Representative Williamson–Hall (W–H) plots of Li\(_{0.5}\)ZnFe\(_{1.5}\)O\(_4\) synthesized at different annealing temperatures are shown in Fig. 2(b). It is possible to observe that the straight line intercepts all points, indicating the presence of a homogeneous microstrain and a homogeneous crystallite size distribution. Average crystallite sizes calculated by using Scherrer's formula and the Williamson–Hall plot are listed in Table 1 for the two samples. The lattice microstrain of each sample obtained using the Williamson–Hall method displays a positive value, indicating lattice expansion. As can be seen in Table 1 the average particle size estimated from the Scherrer equation is quite different from that obtained by the W–H plot. This difference can be explained by the fact that the micro-stress can induce a larger widening of the diffraction peak, whereas, in the Scherrer equation, the total width of the diffraction peak is taken into account in the calculation.

The X-ray density (\( \rho_{X-ray} \)), apparent density (\( \rho_{app} \)), porosity (\( P \)), specific surface area (\( S \)) and X-ray parameters, viz. the A-site radii (\( r_A \)), B-site radii (\( r_B \)), tetrahedral bond length (\( d_{A\text{tet}} \)), octahedral bond length (\( d_{A\text{oct}} \)), the jump length of the A-site (\( l_A \)) and jump length of the B-site (\( l_B \)) are shown in Table 2, and were calculated using the standard relations shown in eqn (S1)–(S15), respectively (ESI). Table 2 shows that the length of the tetrahedral link, the length of the octahedral link, the tetrahedral edge, the shared and non-shared octahedral edge increase with the increase in the annealing temperature. This may be due to the large distance between magnetic ions. The increase in crystallite size resulted in a decrease in the porosity, which has the effect of increasing the apparent density, as we have seen experimentally. The specific surface area decreased from 72.6 to 27.6 \( m^2 \cdot g^{-1} \) with the increase in the particle size. However, the high surface area value of LiZn\(_{2}\)Fe\(_{2}\)O\(_{4}\) nanoparticles suggests that Zn500 nanoparticles could be used as sensors for detecting gases.

The high-resolution TEM image of a single grain (single-crystalline nature) is shown in Fig. 2(d). The TEM image depicts that the particles are non-uniform in size and spherical in nature with some agglomerations. The average particle size estimated from the TEM image was 22 nm (inset of Fig. 2(d)). We also carried out SEM studies. Fig. 2(e) shows the typical SEM image of sample Zn1100. The average grain size increased to the micrometer range for this sample. It is worth mentioning that the average particle size is in agreement with the crystallite size deduced from the XRD data for the sample Zn500, which indicates the single domain nature of the sample. However, the increase in the annealing temperature up to 1100 °C led to the formation of particles with size corresponding to the multidomain state for the sample Zn1100. Evidently, the particle sizes observed by SEM are several times larger than the crystallite size calculated from XRD, which indicates that each particle consists of several crystallized grains. In order to check the existence of all elements in these compounds, energy dispersive X-ray analysis (EDAX) in field emission SEM was carried out, which indicated no inhomogeneity of the chemical composition. The EDAX spectrum represented in the inset of Fig. 2(d) reveals the presence of Zn, Fe and O elements. It was not possible to detect Li for the obvious reason that the X-ray fluorescence is extremely low for elements such as Li or Be. The presence of peaks due to other elements, as either dopants or impurities, was not detected, which confirmed the purity of synthesized material.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Zn500</th>
<th>Zn1100</th>
</tr>
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<tbody>
<tr>
<td>( L_A (\AA) )</td>
<td>3.633</td>
<td>3.639</td>
</tr>
<tr>
<td>( L_B (\AA) )</td>
<td>2.966</td>
<td>2.971</td>
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<tr>
<td>( R_A (\AA) )</td>
<td>1.904</td>
<td>1.907</td>
</tr>
<tr>
<td>( R_B (\AA) )</td>
<td>2.047</td>
<td>2.050</td>
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<tr>
<td>( r_A (\AA) )</td>
<td>0.584</td>
<td>0.587</td>
</tr>
<tr>
<td>( r_B (\AA) )</td>
<td>0.727</td>
<td>0.730</td>
</tr>
<tr>
<td>( d_{A\text{tet}} (\AA) )</td>
<td>1.904</td>
<td>1.907</td>
</tr>
<tr>
<td>( d_{A\text{oct}} (\AA) )</td>
<td>2.048</td>
<td>2.052</td>
</tr>
<tr>
<td>( d_{B\text{tet}} (\AA) )</td>
<td>2.824</td>
<td>2.829</td>
</tr>
<tr>
<td>( d_{B\text{oct}} (\AA) )</td>
<td>3.109</td>
<td>3.114</td>
</tr>
<tr>
<td>( d_{R\text{tet}} (\AA) )</td>
<td>2.968</td>
<td>2.973</td>
</tr>
<tr>
<td>( \rho_{X-ray} (\text{g cm}^{-3}) )</td>
<td>4.86</td>
<td>4.84</td>
</tr>
<tr>
<td>( \rho_{app} (\text{g cm}^{-3}) )</td>
<td>3.71</td>
<td>3.97</td>
</tr>
<tr>
<td>( P (%) )</td>
<td>24</td>
<td>18</td>
</tr>
<tr>
<td>( S (\text{m}^2 \cdot \text{g}^{-1}) )</td>
<td>72.6</td>
<td>27.6</td>
</tr>
</tbody>
</table>
3.3 Infra-red and elastic properties

The bands in the infrared range in solids are generally attributed to ion vibrations in the crystal lattice. The FTIR spectra of the Li–Zn ferrite nanoparticles were also obtained and exhibit absorption bands in good agreement with the FTIR characteristic bands of the ferrite spinel (Fig. 3). However, for spinel ferrites, the vibrational band around 600 cm\(^{-1}\) corresponds to the intrinsic stretching vibration of the tetrahedral site and the vibrational band around 400 cm\(^{-1}\) is attributed to the stretching vibration of metal cations in the octahedral site.\(^{25,26}\) For the Zn500 sample, absorption bands at 3200 to 3600 cm\(^{-1}\) may be related to water symmetric stretching and anti-symmetric stretching \((\text{O–H})\) vibrations.\(^{37}\) The peak observed at around 1627 cm\(^{-1}\) is attributed to the stretching vibration of metal cations in the tetrahedral site and the vibrational band around 400 cm\(^{-1}\) is attributed to the stretching vibration of metal cations in the octahedral site.\(^{25,26}\) The presence of such hydroxyl species causes the nanocrystals to be easily dispersed in polar solvents and the dispersions are also stable such that they can be used in many optoelectronic applications. These bands vanish completely in the Zn1100 sample. The appearance of bands around 2300–2400 cm\(^{-1}\) is due to the atmospheric CO\(_2\) absorbed on the surface of NPs during the FTIR measurements.\(^{28}\) However, the presence of the two modes \(\nu_1\) and \(\nu_2\) for both samples is due to the stretching vibration of metal cations in the tetrahedral and octahedral sites, respectively. The positions of IR absorption peaks of Li–Zn ferrite are illustrated in Table 3. These absorption bands further confirm the formation of the spinel-structured Li–Zn ferrite. Waldron found evidence that the FTIR spectra are useful for calculating the threshold energy \(E_{\text{th}}\) associated with the electronic transition from the threshold wavenumber \(\nu_{\text{th}}\), which is determined from the maximum point of the absorption spectra, where it reaches a limiting value.\(^{28,30}\) The threshold energy can be calculated using the following relation:

\[
E_{\text{th}} = hC\nu_{\text{th}},
\]

where \(C\) is the velocity of light \((C = 2.99 \times 10^{10} \text{ cm s}^{-1})\) and \(h\) is the Planck constant. The values of \(\nu_{\text{th}}\) and \(E_{\text{th}}\) are shown in Table 2 and are consistent with those reported for mechanically milled Ni\(_{3}\)Zn\(_{0.5}\)Fe\(_{2}\)O\(_{4}\).\(^{28}\) The \(\nu_{\text{th}}\) was found to shift towards the lower frequency side and accordingly, \(E_{\text{th}}\) was found to decrease on increasing the annealing temperature. This decrease in threshold energy has been explained by the improvement of the electron hopping between the Fe\(^{2+}\) and Fe\(^{3+}\) ions in the octahedral coordination and is given by Fe\(^{2+}\) ↔ Fe\(^{3+}\) + e\(^{-}\).\(^{29}\)

It is well known that the wavenumbers \((\nu_{1,2})\) of the infrared active phonon modes are connected to the force constant \((F)\) and reduced mass \((\mu)\) of the metal–oxygen bond; the values of the force constants for the A-site \((K_{A})\) and B-site \((K_{B})\) were calculated using the following formula:27,31,32

\[
K_{\nu_{1,2}} = 4\pi^2C^2\nu_{1,2}^2\mu
\]

where \(\nu_{1,2}\) is the vibrational frequency for tetrahedral or octahedral sites and \(\mu\) is the reduced mass for the Fe\(^{3+}\) ions and the O\(^{2-}\) ions \((\sim 2.065 \times 10^{-26} \text{ kg mol}^{-1})\). It is clear from Table 3 that the values of the force constants \(K_{A}\) and \(K_{B}\) decrease and increase, respectively, as the size of the particle increases. This behavior has been attributed to the variation in cation–oxygen bond lengths at the A and B-sites.\(^{31}\)

Elastic constants can be used to measure the resistance of a crystal to an externally applied stress. Therefore, the elastic properties of ferrites are important in industry because their elastic data determine the strength of the materials under various strained conditions. In basic research, the study of the elastic properties of ferrites is useful for obtaining insight into the nature of the inter-atomic and inter-ionic forces and their thermal behavior. For the spinel ferrite and garnet systems, Modi et al.\(^{14-37}\) developed a technique based on the infrared spectroscopy and structural data to calculate the elastic parameters. The stiffness constants \((\text{according to Waldron},^{28})\) for the material systems with cubic symmetry possessing isotropic nature, \(C_{11} = C_{12}\), bulk modulus \(B\), Young’s modulus \(E\), rigidity modulus \(G\), Poisson’s ratio \(\sigma\), longitudinal wave velocity \(V_l\), transverse wave velocity \(V_t\), and mean velocity \(V_{\text{m}}\) were calculated using the following relations:\(^{28,25}\)

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Zn500</th>
<th>Zn1100</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\nu_1) (cm(^{-1}))</td>
<td>546</td>
<td>561</td>
</tr>
<tr>
<td>(\nu_2) (cm(^{-1}))</td>
<td>453</td>
<td>470</td>
</tr>
<tr>
<td>(\nu_3) (cm(^{-1}))</td>
<td>499.5</td>
<td>515.5</td>
</tr>
<tr>
<td>(\nu_{\text{th}}) (cm(^{-1}))</td>
<td>849</td>
<td>767</td>
</tr>
<tr>
<td>(E_{\text{th}}) (eV)</td>
<td>0.105</td>
<td>0.095</td>
</tr>
<tr>
<td>(K_1) (N m(^{-1}))</td>
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</tr>
<tr>
<td>(K_2) (N m(^{-1}))</td>
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<td>203.4</td>
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<td>(K_3) (N m(^{-1}))</td>
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<td>247</td>
</tr>
<tr>
<td>(G) (GPa)</td>
<td>277</td>
<td>294</td>
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<tr>
<td>(V_1) (m s(^{-1}))</td>
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<td>(V_2) (m s(^{-1}))</td>
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<tr>
<td>(E) (GPa)</td>
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<td>(\sigma)</td>
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<td>(\theta_1) (K)</td>
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<td>(\theta_2) (K)</td>
<td>656</td>
<td>678</td>
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Fig. 3 FT-IR spectra of samples Zn500 and Zn1100.
Stiffness constant:

\[ C_{11} = \frac{K_a}{a} \]

Bulk modulus:

\[ B = \frac{1}{3}(C_{11} + 2C_{11}) = C_{11} \]

Transverse wave velocity:

\[ V_t = \sqrt{\frac{C_{11}}{\rho}} \]

Longitudinal wave velocity:

\[ V_l = \frac{V_t}{\sqrt{3}} \]

Poisson’s ratio:

\[ \sigma = \frac{3B - 2G}{6B + 2G} \]

Young’s modulus:

\[ E = (1 + \sigma)2G \]

Mean wave velocity:

\[ V_m = \left[ \frac{1}{3} \left( \frac{2}{V_t^2} + \frac{1}{V_l^2} \right) \right]^{-1/3} \]

where \( K_a = \frac{K_t + K_o}{2} \) is the average force constant, \( a \) is lattice parameter and \( \rho \) is the X-ray density.

The variation of the elastic modulus of Li–Zn ferrite samples can be noticed from Table 3. The value of the Poisson’s ratio (\( \sigma = 0.35 \)) remains constant as a function of the annealing temperature and lies in the range of 0.1 to 0.5, which is in accordance with the theory of isotropic elasticity\(^n\) (hence good elastic behavior). This value of the Poisson ratio is in good agreement with other spinel ferrites.\(^{28,36-37}\) The calculated values of \( G, \sigma, E, V_t, V_l \) and \( V_m \) for the two samples are consistent with those obtained from the ultrasonic pulse transmission (UPT) technique\(^{39-41}\) and for various ferrite spinels using FTIR data.\(^{42,43}\) In addition, unless corrected to a void-free state, the measured elastic moduli are not significant. Therefore, the values of elastic moduli have been corrected to zero porosity using the Hosselman and Fulrath model, Ledbetter and Datta model and elastics theories (see ESI†). The values of elastic moduli are given in Table S1 (ESI†). These values are higher than the uncorrected data of the elastic moduli. Moreover, the values of elastic moduli and Poisson’s ratio decreased with an increase in the annealing temperature, while the uncorrected data of the elastic moduli increase, which suggests the strong effect of the porosity on the elastic properties. Generally, the variations in elastic moduli are sensitive to inter-atomic bonding lengths. However, A. Bhaskar et al.\(^{44}\) reported that the increase in the values of the elastic moduli suggests that the strength of the interatomic bonding between the ions of Mn added Mg–Cu–Zn ferrites increases with an increase in the sintering temperature. Therefore, the decrease in the elastic moduli for pore-free Li–Zn ferrites may be due to a decrease in the inter-atomic bonding between various atoms in the lattice.

To distinguish whether the material under investigation is ductile or brittle in nature, according to the Pugh criteria,\(^{45,46}\) a useful value of bulk modulus to rigidity modulus, \( B_0/G_0 \), was inspected. \( B_0/G_0 \) must be greater than 1.75 for the ductile nature and less than 1.75 for the brittle nature. The calculated values of \( B_0/G_0 \) in our case (according to Ledbetter and Datta model) were 4.55 and 4.02 for Zn500 and Zn1100, respectively, qualifying for a ductile nature.

Finally, the Debye temperature is the temperature at which the maximum vibration of the network takes place and simplifies the integration of thermal capacity. It was calculated using the equation given by Waldron:\(^{47}\)

\[ \Theta = \frac{hC}{K} \rho \]

where \( \rho \) is the average value of the wavenumbers of bands, \( h \) is Planck’s constant, \( k \) is Boltzmann’s constant, \( C \) is the velocity of light, and the value of \( hC/k \) for the ferrite materials is taken as 1.438.

From the mean velocity \( V_m \), the Debye temperature can also be estimated by using Anderson’s formula:\(^{48}\)

\[ \theta_D = \frac{h}{K} \left( \frac{3 \rho \nu_A}{4 \pi M} \right)^{1/3} V_m \]

where \( h \) is Planck’s constant, \( k \) is Boltzmann’s constant, \( \nu_A \) is Avogadro’s number, \( \rho \) is the density, \( M \) is the molecular mass and \( q \) is the number of atoms per unit formula (in the present case \( q = 7 \)). On the basis of specific heat theory,\(^{47} \) it is possible to interpret the variation of the Debye temperature. The increase in both the Debye temperature \( \theta_D \) and \( \theta_{19} \) (Table 3) manifested a decrease in the conduction electron number \( N_e \) and the increase in the number of conduction holes \( N_h \) (p-type). In addition, this increase in the Debye temperature can be associated with the increase in the rigidity of the LiZn\(_2\)Fe\(_3\)O\(_8\) samples.

### 3.4 Raman spectroscopy analysis

Raman spectroscopy provides an important tool for probing the structural properties of synthesized Li\(_{0.5}\)ZnFe\(_{1.5}\)O\(_4\) ferrites. Raman spectra of the Li–Zn ferrite (Zn500 and Zn1100) were collected at room temperature in the spectral range of 100–800 cm\(^{-1}\) and are shown in Fig. 4. According to literature, only 5 Raman active phonons (\( A_{1g} + E_g + 3F_{2g} \)) are known for the cubic spinel structure belonging to the \( O_h \) (Fd\(_{3d}\)m) space group.\(^{44}\) The \( A_{1g} \) and \( F_{2g}(1) \) phonons are associated with the symmetric
stretching of metal–oxygen bonds and the translation movement of the whole at the tetrahedral site, respectively. The \( Eg \), \( F_{2g}(3) \) and \( F_{2g}(2) \) modes represent the symmetric, asymmetric bending and asymmetric stretching vibrations of the metal–oxygen bonds at the octahedral site, respectively.\(^{26}\) In order to determine the natural frequency of the Raman results, we have carried out a deconvolution of the experimental data with the Lorentzian peak shape function and the best-fit values for the peak positions are given in Table 4. No signal associated with secondary phases or impurities has been identified, especially for hematite (\(α\)-Fe\(_2\)O\(_3\)) impurities, which is consistent with the XRD data. The Raman bands observed at 164, 316, 445, and 523 cm\(^{-1}\) could be attributed to the \( F_{2g}(1), Eg, F_{2g}(2), \) and \( F_{2g}(3) \) Raman modes, respectively. The last peak, at about 637 cm\(^{-1}\), corresponds to a phonon with \( A_{1g} \) symmetry and can be deconvoluted into two Lorentzian-shaped peaks at 637 cm\(^{-1}\) and 675 cm\(^{-1}\); these peaks are typically characteristic of the mixed-as well inverse-spinel. Therefore, a detailed analysis of the asymmetry of some modes could be employed to estimate the cation disorder in the spinel structure. The Raman spectra confirmed the formation of the phase pure \(Fd3m\) spinel ferrite Li\(_{0.5}\)Zn\(_{1.5}\)Fe\(_2\)O\(_4\) nanoparticles.

It can be seen that the Raman modes of the Zn500 sample are enlarged and their frequencies are shifted to the lowest values compared to those of the Zn1100 sample. However, a breakdown of the momentum conservation rule occurs when the particle size (around 20 nm in our case) is sufficiently smaller than the wavelength of the exciting radiation (532 nm); this leads to the selection rule for the momentum vector \( (q' = 0) \), and is replaced by the \( q' \)-vector relaxation model.\(^{28}\) Therefore, this broadening and shifting of Raman modes in nanoparticles may be due to phonon confinement and variations in phonon relaxation with particle size. These results are comparable to those previously obtained in spinel ferrite nanoparticles by Datt \textit{et al.}\(^{21}\) as well as Wang \textit{et al.}\(^{21}\).

Moreover, Zn vacancies were formed in the crystal lattice at such a high temperature. This led to the reduction of some of the Fe\(^{3+}\) ions from the B-site to Fe\(^{2+}\) ions to compensate for the loss of Zn, which eventually hopped to the Zn site. The local system is no longer in equilibrium with its neighbors after the hopping of the central Fe ions towards the A-sites from their initial stable configurations. To stabilize the new ion positions, other surrounding ions must move accordingly. Therefore, this hopping process will have a substantial impact on the vibrational frequencies of the associated modes of the BO\(_6\) octahedral site. The proposed hopping process is also supported through conductivity studies, which will be discussed in the next section. Note that this ion jumping leads to the presence of Fe\(^{3+}\) and Fe\(^{2+}\) in the system, which increases the conductivity with increasing temperature.

### Table 4

<table>
<thead>
<tr>
<th>Raman mode</th>
<th>Zn1100 Position (cm(^{-1}))</th>
<th>Zn500 Position (cm(^{-1}))</th>
<th>Assigned polyhedra</th>
</tr>
</thead>
<tbody>
<tr>
<td>( A_{1g} )</td>
<td>637</td>
<td>624</td>
<td>FeO(_4) tetrahedra</td>
</tr>
<tr>
<td>( F_{2g}(3) )</td>
<td>523</td>
<td>505</td>
<td>FeO(_4) octahedra</td>
</tr>
<tr>
<td>( F_{2g}(2) )</td>
<td>445</td>
<td>433</td>
<td>FeO(_6) octahedra</td>
</tr>
<tr>
<td>( E_g )</td>
<td>316</td>
<td>294</td>
<td>FeO(_4) octahedra</td>
</tr>
<tr>
<td>( F_{2g}(1) )</td>
<td>164</td>
<td>137</td>
<td>FeO(_4) tetrahedra</td>
</tr>
</tbody>
</table>

3.5 Electrical characterization

#### 3.5.1 Analysis of conductivity

The conductivity spectra are shown in Fig. 5 for each of the studied samples, Zn500 and Zn1100, over a wide temperature range. Each curve constitutes a frequency-independent domain next to a dispersive region; the former represents the direct current conductivity, \( \sigma_{dc} \) whereas the latter refers to alternating conductivity denoted as \( \sigma_{AC} \). The curves in Fig. 5(a and b) are spaced further apart relative to Fig. 5(c), in which they tend to extend partially.

Regarding Zn500, the conductivity responds to the frequency in two different ways depending on the temperature. It reacts to frequency in conformity with Jonscher’s law (\( \sigma_{AC} = A \omega^s \) where \( A \)
is a constant and $\omega$ is the angular frequency) up to 590 K; beyond that, it varies with frequency in agreement with Drude's model. Further, the frequency-independent region extends thermally to 590 K, above which it begins shrinking.

Concerning Zn1100, the conductivity is correlated with frequency according to Jonscher's model over the entire explored temperature scale. The low-frequency plateau continuously becomes larger as temperature increases. The low-temperature peak in Fig. 5(c) shifts to the right side of the plot with temperature. It seems to be out of the tested frequency scale for relatively high temperatures. The representative conductivity curve fitted to Jonscher's model is shown in Fig. S1 (ESI†).

According to S. F. Mansour et al. along with M. Abdullah Dar and coworkers, frequency contributes to an increase in the number of mobile carriers by virtue of its pumping force. On this basis, we inferred that the mobile carriers at low frequencies are the ones unleashed due only to temperature, whereas the mobile carriers at high frequencies are those released due to temperature as well as frequency; i.e., the free carriers are boosted in number as frequency increases. It makes sense that the conductivity of a semiconductor increases with frequency. This information is not in opposition to M. Abdullah Dar's insight. Thus, we conclude from Fig. 5 that Zn500, down to 590 K, and Zn1100 behave as though they were semiconductors; this is corroborated by the continuous increase in their $\sigma_{dc}$ upon heating.

The conductivity of Zn500 above 600 K will be discussed separately. On the one hand, the direct decrease in $\sigma_{AC}$ without increasing frequency over the dispersive region is a typical feature of metals. On the other hand, the increase in $\sigma_{dc}$ with temperature is typical behavior for semiconductors. We concluded that above 600 K, Zn500 functions as a metal or semiconductor, according to the frequency.

The number of mobile carriers in Zn1100 is supposed to increase with frequency as mentioned above; however, the $\sigma_{AC}$ does not. This implies that the concentration of mobile carriers no longer controls the conductivity at 600 K and so, in addition to carriers and their charges, mobility plays a role in conductivity. Therefore, the decrease in $\sigma_{AC}$ refers to a restriction in mobility; this is ascribed with confidence to the presence of gas carriers at such frequencies. The scattering due to the vibration of ions may contribute to the decrease in mobility.

We will only consider the low-temperature peak seen in Fig. 5(c); we surmised that the absence of peaks in Fig. 5(a and b) is somehow related to the annealing temperature. The
alternating voltage of 50 meV causes free carriers to move through matter along its direction, resulting in a net electrical conductivity. Certain mobile carriers are unable to keep up with the excitation above a specific frequency, which reduces the conductivity. This elucidates the appearance of a peak in Fig. 5(c). According to R. W. Christy, mobility is boosted exponentially as temperature increases; a slight increase in temperature makes carriers move even faster, implying that the frequency, beyond which they no longer follow the excitation, is also thermally activated. This explains why the peak, before disappearing, shifts toward higher frequencies once there is continuous heating.

The microstructure of ferrite with zinc is so sensitive to annealing temperature in the opinion of A. M. Kumar, whose results proved that the grain boundary concentration peaks at 1100 °C. It is boosted with annealing temperature up to 1100 °C, which means that the grain boundaries within the current samples are strongly expected to increase in concentration on going from 500 °C to 1100 °C. Since they serve as barriers capable of impeding carriers from going around, it is harder for carriers to move through Zn1100 due to their possession of further inter-grains. It can be concluded that the mobility of carriers in Zn1100 is relatively low. Since the mobility somehow mirrors relaxation frequency, this point will be made in detail on treating impedance formalism, it becomes evident that the relaxation frequency of Zn1100 at a given temperature is lower compared to Zn500; this is an argument for elucidating why peaks appear in Fig. 5(c) but not in Fig. 1(a). We assume the peaks in Fig. 5(a) are out of the explored frequency scale and may emerge beyond 10 MHz.

The curves in Fig. 5(c) are closer to each other as compared to the others, which is a strong sign that the conductivity of Zn1100 is less dependent on temperature. Annealing at 1100 °C stems the creation of further barriers to restrict carriers from moving, reinforcing A. M. Kumar’s insight. This idea is supported by Fig. 7(a); the extra barriers are assumed to be intergrains.

The dominant conduction mechanism according to which \( \sigma_{AC} \) occurs will be discussed in this section. On the one hand, certain researchers think that the increase of this parameter is proof of the hopping process; on the other hand, others have proved that a rise in \( \sigma_{AC} \) is sometimes due to other mechanisms like tunneling. It becomes clear that by itself, the conductivity spectrum is not a powerful tool for approaching alternating conductivity in terms of mode of transport. The popular alternative is to consider the thermal variation of the frequency exponent “s” appearing in Jonscher’s law, shown in Fig. 6 as estimated from the dispersive regime in Fig. 5.

In the case of the Zn500 sample, according to the overlapping large polaron tunneling (OLPT) model, the values of “s” decrease with increasing temperatures to a minimum value and then rise when the temperature increases. This is in good agreement with the obtained results in the studied temperatures (Fig. 6(a)). Therefore, the OLPT model is usually described as the predominant conduction mechanism in the semi-conducting Zn500 sample. In this conduction type, the large-polaron wells at two sites are assumed to overlap, thus reducing the polaron hopping energy, which is given by:

\[
W_H = W_{110}(1 - r_p/R)
\]

where \( W_{110} \) is associated with the activation energy, \( r_p \) is the radius of a large polaron and \( R \) is the inter-site separation. The relation between the power parameter \( s \) and temperature for the OLPT mechanism is as follows:

\[
s = 1 - \frac{8\alpha R_o + 6W_{110}r_p}{kT R_o} \frac{1}{\left(2\alpha R_o + \frac{W_{110}r_p}{kT R_o}\right)^2}
\]

where \( \alpha \) is the spatial extent of the polaron, \( R_o \) is the hopping length at the angular frequency \( \omega \), \( k \) is the Boltzmann constant and \( T \) is the temperature. The higher values of activation energy in our case also support this argument. Likewise, conductivity can be approached by polarons with tunneling between Fe\(^{2+}\) and Fe\(^{3+}\) sites. This factor indicates that the sample displays the commonly observed electrical characteristic after the endothermic transition and that a charge-ordering transition takes place in the prepared material. The polaron formation in the nano ferrite system can be due to the defect levels introduced by the size reduction. The same behavior is presented for other
spinel ferrite nanoparticles.\textsuperscript{61,62} However, a detailed theoretical study is essential for exploring the different aspects of this type of conduction mechanism in nanostructured Li–Zn ferrite.

For the Zn1100 sample, “s” decreases gradually upon heating, which proves that transport from one site towards an equivalent site takes place predominantly, but not exclusively, in conformity with the correlated barrier hopping (CBH) model.\textsuperscript{63} According to this model, the transport process arises by a single or bipolaron hopping mechanism through the Coulomb barrier between two trap centers. The frequency exponent “s” in this model can be expressed as follows:\textsuperscript{64}

\[ s = 1 - \frac{6kT}{W_M - kTln(\omega_0)} \]

where \( T \) is the temperature, \( k \) is the Boltzmann constant, \( \omega \) is the angular frequency, \( \tau_0 \) is the relaxation time and \( W_M \) is the maximum barrier height. For large values of \( W_M/kT \), the parameter “s” can be reduced to\textsuperscript{64}

\[ s = 1 - \frac{6kT}{W_M} \]

The values of \( W_M \) were determined from the slope of the curve of 1 s versus the temperature for the Zn1100 sample (Fig. 6(b)). A value of \( W_M = 286 \) meV was obtained. However, if the maximum barrier height \( W_M = E_a/2 \), bipolaron hopping dominates, while if \( W_M \) is a quarter of the activation energy \( E_a \), the single polaron dominates the conduction mechanism (the values of \( E_a \) were extracted from the \( \sigma_{dc} \) fits with small polaron hopping (SPH) model (Fig. 7(b)). From the above-mentioned considerations, the maximum barrier height \( W_M \) is approximately half of the activation energy, which indicates that the bipolaron hopping is the dominant conduction mechanism for this sample. This behavior indicates that the conduction process is dominated by the jumping mechanism and confirms the thermal activation of materials. It can be said that the annealing temperature of the Li–Zn ferrite sample largely influences the conduction mechanism. The change in the s value with respect to temperature is an indication of the thermally active polarization mechanism.

Fig. 7(a) illustrates the thermal variation of \( \sigma_{dc} \), the magnitude of which for every single specimen goes up intensively and then slightly as temperature increases. The space between the curves becomes continuously larger up to 580 K, beyond which it becomes almost constant. This indicates that thermal activation in \( \sigma_{dc} \) is a typical trend for semiconductors.

The \( \sigma_{dc} \) of Zn500 is higher as compared with that of Zn1100, which is in agreement with many works. Some reports have stated that the \( \sigma_{dc} \) of ferrite compounds like the spinel structure runs inversely to the sintering temperature.\textsuperscript{8,15} Varying the latter from 500 °C to 1100 °C caused the \( \sigma_{dc} \) to be greatly restricted. At 490 K, it was decreased by one hundred S m\(^{-1}\), while it was reduced by one thousand S m\(^{-1}\) at 590 K. Such a strange large drop in magnitude refers to more grain boundaries with
ultrafine grains within Zn1100. This implies that grains along with grain boundaries are very sensitive to the value of the annealing temperature. It does not oppose the common information that says the microstructure depends on the annealing temperature. In order to acquire information about the type of conduction mechanism present in this spinel ferrite, two hopping models were used to fit the experimental data of Fig. 7(a) at different temperatures. At high temperature, the small polaron hopping (SPH) model can be mathematically described by the following relation:\(^\text{67}\)

\[
\sigma_{dc} T = \sigma_0 \exp \left( - \frac{E_a}{kT} \right)
\]

where \(\sigma_0\) is the pre-exponential factor, \(E_a\) is the activation energy, \(T\) is the absolute temperature and \(k\) is the Boltzmann constant. The SPH model fits \(\sigma_{dc}\) as Fig. 7(b) demonstrates. The activation energy can be estimated from the slope of the segment of lines. Based on the work of M. Idrees, the activation energy with small magnitude up to 200 meV is an indicator of electron hopping.\(^\text{68}\) We are not against this point because this is enough energy to unleash the light tiny electrons. However, from certain distinct works, one may evidently conclude that activation energy with high values of hundreds of meV can be related to more than one origin, involving a better understanding of the physical problem. Among these origins, the main ones are electron hopping in ferromagnetic intra-grains\(^\text{69}\) and the simultaneous presence of multiple mechanisms.\(^\text{4}\) It is evident that one fails to predict the dominant conducting carriers within Zn500 and Zn1100 from the current activation energy of 1366 meV and 573 meV, respectively. One of the alternative approaches is to consider the present matters in the physical sense. Moreover, it was found that the activation energy increased as the size of the particles increased. The decrease in the activation energy can be related to the increase in the density of charge carriers. In the low temperature, \(\sigma_{dc}\) was also analyzed by employing the variable range hopping model (VRH) for which the dependence of the dc conductivity can be described by the following relation:\(^\text{67}\)

\[
\sigma_{dc} = \sigma_0 \exp \left( - \frac{T_0}{T} \right) - 0.25
\]

where \(T_0\) is the characteristic temperature coefficient, being a measure of the degree of disorder, given by\(^\text{67}\)

\[
T_0 = \frac{24}{\pi k N(E_F)} \xi^4
\]

where \(\xi\) represents the decay length of the localized wave function (the value of \(\xi\) is equal to the cation–cation distance for the octahedral sites in Li0.5ZnFe2O4 and \(N(E_F)\) is the density of the localized states at the Fermi level \(E_F\). The obtained \(T_0\) values from the best fit to the data (Fig. 7(c)) are 2 × 10^10 K and 1.62 × 10^10 K, for Zn500 and Zn1100, respectively. In ferrite materials, these values can be used to calculate the density of the localized states at the Fermi level. The obtained \(T_0\) values suggest that the density of states at the Fermi level is lower in Zn500 samples (\(N(E_F)\) = 1.6 × 10^17 eV cm\(^{-3}\) for Zn500 and 2 × 10^21 eV cm\(^{-3}\) for Zn1100 sample). This result can be explained by the presence of only one type of ferrite particle in the Zn500 sample, while the annealed sample at 1100 °C contained a mixture of substances.\(^\text{70}\) Using the value of \(T_0\), at a particular temperature \(T\), the activation energy \(W\) is given by\(^\text{67}\)

\[
W = 0.25kT^{3/4}T_0^{1/4}
\]

Assuming the value of \(\xi\) to be equal to the cation–cation distance for the octahedral sites in Li–Zn ferrite, which is about 3 Å, and using the values of \(N(E_F)\), the hopping range of polarons \(R\) is given by\(^\text{67}\)

\[
R = \xi^{1/4}(8\pi k N(E_F) T)^{1/4}
\]

The calculated values of \(W\) at 350 K are 0.65 eV and 0.062 eV for the Zn500 and Zn1100 samples, respectively. The values of the hopping range of polarons \(R\) at 350 K for both studies compounds were found to be 71 Å for sample Zn500 and 6.7 Å for sample Zn1100. Therefore, our results suggest that the conduction mechanism in our ferrite spinel is governed by the SPH model in the high-temperature region and by the VRH model in the low-temperature region (polaronic in nature).

In spite of being volatile, Zn ions were remarkably found to never escape from the spinel structure because annealing goes up to 1100 °C.\(^\text{4,13}\) Therefore, we conclude that on firing Li0.5\text{ZnFe}_{1.5}O4 at 500 °C and even 1100 °C, the zinc content remains almost stoichiometric. Thus, the valence of Zn with Fe is governed by how many oxygen and lithium vacancies were created in the tested samples.

Annealing at 1100 °C certainly forces a finite fraction of lithium and oxygen to distill out of the surface of the pellet.\(^\text{8}\) The loss of oxygen enhances the release of electrons while the volatilization of zinc promotes the formation of holes. Since these two mechanisms function against each other, we ought to determine which one dominates under our annealing conditions. According to M. Amemiya et al.,\(^\text{7}\) the concentrations of created electrons and holes, due to firing lithium ferrite at 1100 °C and under an oxygen atmosphere, were almost equal. From this information, we believe that on annealing the tested specimens under similar conditions, the effects due to the volatilization of zinc and oxygen cancel each other. Due to the presence of nitrogen under atmospheric conditions, more electrons are present in the considered system and there is more evaporation of oxygen as compared to an environment containing oxygen only.

Assuming that the free carriers in this specimen are only electrons, \(\sigma_{dc}\) of Zn1100 is larger as compared to \(\sigma_{dc}\) of Zn500 because electrons are lighter than ions. Since this is not the case, our assumption is wrong and the dominant free carriers in Zn1100 are also ions. To recap, the electrical conductivities of both samples are absolutely ionic. Although Zn and O ions may participate in conduction, lithium with a relatively smaller weight is certainly the mobile ion. Nevertheless, we are incapable of judging whether it is a lithium vacancy and/or lithium interstitial.
3.5.2 Impedance formalism study. Fig. 8 illustrates a spectroscopic display of $Z'$, the real part of impedance, of Zn500 and Zn1100 over a large temperature scale. The two plots are typical for spinel with Zn.$^{71}$ Up to intermediate temperatures, Zn500 and Zn1100 react nearly similarly to frequency. $Z'$ remains constant at low frequencies, where it looks like a plateau. $Z'$ then starts to decrease with further increase in frequency. However, at high temperatures, the samples respond differently to frequency. $Z'$ becomes constant for Zn500, while remaining frequency-dependent for Zn1100. The curves in Fig. 8(b) are closer to one another for Zn1100 as compared with Zn500. The increase in measured temperature by 170 °C forces the low-frequency $Z'$ of Zn500 to decrease in value by four decades, whereas it causes the low-frequency $Z'$ of the other sample to decrease in magnitude by merely two decades. Nevertheless, no similar change was observed on the high-frequency scale, where curves showed a strong tendency to overlap.

The frequency-dependent and independent regions together are a signature of a relaxation phenomenon.

Grain boundaries and grains are essentially active through low and high-frequency ranges, respectively.$^{72}$ The mismatch between the low-frequency $Z'$ of Zn500 and Zn1100 is great, whereas the difference between their high-frequency $Z'$ is small. We deduce that annealing temperature impacts more on grain boundaries than grains. We corroborate this idea from A. M. Kumar et al., who postulated that grain boundaries in spinels are a signature of a relaxation phenomenon.$^{16}$

The magnitude of the low-frequency $Z'$ is great, which indicates that something is impeding carriers from moving easily at low frequencies where grain boundaries are active. When the free carriers reach those boundaries, they accumulate. However, the magnitude of the high-frequency $Z'$ is low, so we assumed that there were no such resistive obstacles that are capable of restricting carriers from moving over the high-frequency range where grain boundaries are supposed to be active. This implies that carriers no longer reach them by virtue of the short period.$^{16,73}$ We, therefore, concluded that the space charge phenomenon occurs at low frequencies but not at high frequencies where carriers are unleashed from grain boundaries.$^{74}$

The spectroscopic display of normalized $Z''$, the imaginary component of impedance, for Zn500 and Zn1100 at variable temperatures is indicated in Fig. 9(a and b). It does not conflict with the common behavior of lithium matter with spinel structure.$^{75}$ Both plots appear similar to each other in terms of shape. $Z''$ at a given temperature has frequency up to a specific value termed relaxation frequency, beyond which it begins falling, forming a peak. That cut-off frequency shifts towards higher values as temperature increases. It increases relatively rapidly with temperature in Fig. 9(a).

The presence of only one peak indicates that only the single relaxation phenomenon is covered through the explored frequency scale. We associate this with grain boundaries being more active at low frequencies than grains.$^{76}$ The lack of grain response may be explained either by the grains being conductive relative to grain boundaries, or that the measured frequency range is too limited to cover them.

The relaxation frequency reflects the degree of ease with which carriers move over matter, across which an alternating electric field is applied.$^{77}$ We wanted to determine whether the cut-off frequency is somehow proportional to mobility. The continuous rise in its value, as illustrated in Fig. 9(a and b), is an asymptote of mobility within Zn1100 and Zn500 ($T < 520$ K), which is thermally activated. Once carriers travel a path, they may collide with ions. When the temperature is sufficiently high, the ions will vibrate more and more around their equilibrium positions, resulting in more collisions, which could reduce the mobility. Since this is not the case, we concluded that the scattering phenomenon within Zn1100 and Zn500 ($T < 520$ K) is not significant.

An increase in the annealing temperature by 600 °C sharply restricts the relaxation frequency. For instance, at 520 K, it was approximately 1 MHz for Zn500, while being just 2 kHz for Zn1100, which means that it is harder for carriers within Zn1100 to move. This insight is one of the arguments explaining why the conductivity of Zn500 is relatively great as shown in Fig. 5.

Each peak in Fig. 9 is wide, which is an indication of the distribution of relaxation time.$^{71}$ The period required for accomplishing hopping from one site to an equivalent site is not the same. The existence of no single relaxation time is due

![Fig. 8](image-url) Frequency-dependence of $Z'$ (a) Zn500 and (b) Zn1100.
to multiple causes, for instance, dipole–dipole interactions\textsuperscript{78} and defects.

Since there are multiple relaxation times, the concept of just “relaxation time” does not make sense for the entire specimen. The most accurate concept is “mean relaxation time” denoted as $\tau$. This value at a given temperature is deduced from the relaxation frequency.\textsuperscript{79} We plotted $\tau$ versus one thousand over temperature in Fig. 9(c), which increased linearly for both samples, implying that $\tau$ varies with temperature according to Arrhenius law:\textsuperscript{69}

$$\tau = \tau_0 \exp \left( \frac{E_{a1}}{kT} \right)$$

where $\tau_0$ and $E_{a1}$ refer to a constant, and activation energy, respectively. The other parameters correspond to their common meaning. According to the above equation, it is obvious that the magnitude of activation energy is estimated from the slope of the lines in Fig. 9(c). The calculated values are shown inset.

Temperature ranges, where $\tau$ of Zn500 and Zn1100 fit the Arrhenius model, do not overlap. Thus, it is not possible to compare the activation energies from Fig. 9(c). Also, the temperature scales, over which activation energies for conduction and relaxation phenomena in Zn500 were estimated, do not extend, and in turn, it is impossible to compare them with each other. In contrast, these distinct activation energies of Zn1100 were estimated over nearly the same temperature ranges. On the one hand, the conduction activation energy of 1366 meV for Zn500 is higher than its relaxation energy of 1035 meV, which agrees with M. Idrees’s point.\textsuperscript{68} According to Idrees, the relaxation phenomena involve only hopping energy, whereas the conduction process requires disorder and binding energies in addition to hopping energy. On the other hand, the mismatch of approximately 331 meV is not negligible, implying that conduction and relaxation processes within Zn500 are due to the different types of carriers.

The Nyquist diagrams of Zn500 along with Zn1100 at selected temperatures are indicated in Fig. 10. They are typical for spinel.\textsuperscript{79} The patterns of curves at a fixed temperature are close. The data at a given temperature falls into a semicircle. That curve becomes smaller with increasing temperature.

Since reporters normally simulate the loop using a capacitor and resistor connected to each other in parallel, we suggest that the current specimens are simultaneously capacitive and resistive. The presence of only one semicircle indicates that the single relaxation phenomenon occurs over the measured frequency range as deduced from Fig. 9.

The restriction in diameter refers to an increase in conductivity with temperature.\textsuperscript{73} Here, we reconsider the movement of carriers. An ion of tiny size is subject to the quantum mechanical rules; therefore, they can tunnel through, in addition to hopping over, barriers. The former mechanism depends predominantly on the width of barriers, but slightly on temperature. However,
the hopping process is strongly temperature sensitive, as is resistance, as shown in Fig. 10. Therefore, carriers with high energy contribute to conductivity according to the hopping mechanism, rather than the tunneling process; this corroborates the above conductivity analysis.

Since the pattern remains unperturbed in spite of annealing at different temperatures (500 °C and 1100 °C), we inferred that increasing the annealing temperature by 600 °C does not influence the type of active regions. It is worth noting that annealing from 500 °C to 1100 °C neither creates further microstructure-like surface layers nor cancels out already existing regions such as grain boundaries. The loop with the center below the real axis is a little smooth, unlike a perfect semicircle; this reinforces the distribution of relaxation time.

Finally, these results suggest that both LiZnZnFe3O8 samples (Zn500 and Zn1110) can be promising in the use of fuel cells (higher conductivity), microwave application and low-temperature co-fired ceramics (LTCC) technology applications.

3.6 Optical characterization

It is known from past reports that the sizes and morphologies greatly affect the optical properties of semiconductor nanomaterials.82,83 Fig. 11(a) shows the room temperature UV-visible absorption spectra of the two annealed samples of LiZnFe3O8 in the range 450–1100 nm, in which the absorption edges were found to be in the visible region, illustrating its suitability for visible light photocatalysis and photovoltaic application. The strong absorption can generally be related to the electronic transition from the valence band to the conduction band (O2p Fe3d). In other words, a considerable amount of visible light was absorbed due to electron excitation from the O2p level (valence band) to the Fe3d level (conduction band).83 However, the band gap energies calculated by plotting the Tauc relation with photon energy hv (Fig. 11(b)) were found to be 1.41 and 1.36 eV for Zn500 and Zn1100, respectively. This indicates that the band gap decreases with the increase in particle size. The decrease in the band gap could be attributed to the basis of weak quantum confinement effects.84 A red shift for our samples was observed when compared to the pure bulk ZnFe2O4 (1.9 eV).85 This decrease in band gap may be attributed to the additional sub-band-gap energy levels that were induced by interface defects and the abundant surfaces in the agglomerated nanoparticles and to interfacial chemical conditions.84,85 Since these values of the bandgap energies are greater than the
theoretical value of the energy needed for water splitting ($\lambda > 1.23$ eV), the lithium zinc ferrite samples are therefore suitable for the role of solar light photocatalysts.

4. Conclusion

We prepared Li$_2$Zn$_2$Fe$_3$O$_8$ with the spinel structure using a sol–gel auto-combustion route with an annealing temperature of 500 °C and 1100 °C. From X-ray diffraction investigation, it was found that both samples crystallized in the cubic spinel structure with the space group (Fd3m). The crystallite size increased and a microstress was induced when the annealing temperature was increased. Morphological observations confirmed the crystalline structure and showed that the grains were composed of several crystallites. FTIR and Raman spectroscopies affirmed the purity and the existing chemical bonds. They also allowed the extraction of the elastic parameters, which were found to increase with the annealing temperature. The change in the grain size is correlated to the effects of grains and grain boundaries.

Conflicts of interest

There are no conflicts to declare.

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References
