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High efficiency $Mg_2(Si,Sn)$-based thermoelectric materials: scale-up synthesis, functional homogeneity, and thermal stability†

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Considering the need for large quantities of high efficiency thermoelectric materials for industrial applications, a scalable synthesis method for high performance magnesium silicide based materials is proposed. The synthesis procedure consists of a melting step followed by high energy ball milling. All the materials synthesized *via* this method demonstrated not only high functional homogeneity but also high electrical conductivity and Seebeck coefficients of around 1000 Ω^{-1} cm^{-1} and -200 μV K^{-1} at 773 K, respectively. The measured values were similar for all the samples extracted from the ∅50 mm and ∅70 mm compacted pellets and were stable upon thermal cycling. Thermal stability experiments from 168 hours to 720 hours at 723 K revealed no significant change in the material properties. The low thermal conductivity of $\sim$2.5 W m^{-1} K^{-1} at 773 K led to a maximum figure of merit, zT_{max}, of 1.3 at the same temperature and an average value, zT_{avg}, of 0.9 between 300 K and 773 K, which enables high efficiency in future silicide-based thermoelectric generators.

1. Introduction

Contemplating the decades of space exploration missions, thermoelectric (TE) materials are auspiciously established as a unique energy supplier for space explorers such as Cassini, the Voyager probes, and most recent Mars rover Curiosity.[1,2] Moreover, this notable capacity is not limited to the space program, and also TE materials are now on the verge of waste heat recovery for stationary[3] and non-stationary[4,5] applications. In order to alleviate the destructive impact of climate change on our planet, both CO_2 emission and fossil fuel consumption need to be reduced. Therefore, it is vital to recuperate as much waste heat as possible. In that context, TE materials, which are made of cost effective, environmentally benign elements, and have high efficiency, are inimitable.[6] The criterion to evaluate the efficiency of a TE material is called figure of merit, z, which is commonly defined in its dimensionless form through $zT = S^2\sigma(\kappa_{ph} + \kappa_e)^{-1}T$, where S, σ, κ_{ph}, κ_e, and T represent Seebeck coefficient, electrical conductivity, lattice thermal conductivity, electronic thermal conductivity, and absolute temperature, respectively.[7]

Magnesium silicide based TE materials are worth investigating as potential candidates for module fabrication due to fulfilling most of the above-mentioned criteria. Mg_2Si adopts an anti-fluorite cubic structure which belongs to the high symmetry $Fm\bar{3}m$ space group with a band gap of $\sim$0.77 eV.[8] The combination of low intrinsic carrier concentration ($\sim$3 × 10^{17} cm^{-3} at 300 K) and a high symmetry structure consisting of light atoms with strong covalent bonds manifests itself in low electrical conductivity ($\sim$2 Ω^{-1} cm^{-1} at 300 K) and high thermal conductivity ($\sim$10 W m^{-1} K^{-1} at 300 K) leading to a zT of below 0.1 at 300 K, which does not significantly enhance even at high temperature.[9,10] Increasing the electrical conductivity can be achieved *via* increasing the carrier density through doping with non-isoelectronic elements. So far, for n-type doping, group XV elements such as bismuth (Bi)[11–18] and antimony (Sb),[19–25] which replace silicon (Si), appear to be the most potent in enhancing the carrier concentration (more than 10^{20} cm^{-3} at 300 K); therefore, increasing the electrical conductivity.[16] Reducing the

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† Electronic supplementary information (ESI) available: Fig. S1: surface Seebeck scans of both base faces of the ∅30 mm $Mg_{1.97}Li_{0.03}Si_{0.3}Sn_{0.7}$ pellet. Fig. S2: X-ray diffraction patterns on the both surfaces and cross section of the 50 mm $Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ sample. Table S1: density and specific heat of 4 samples extracted from 50 mm pellet. Table S2: density and specific heat of 3 samples extracted from 70 mm pellet. Fig. S3: X-ray diffraction patterns on the top and bottom surfaces (left) and surface Seebeck scan on cross section (right) of the $Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ sample with current passing through the sample. Fig. S4: frequency count of surface Seebeck scan performed on one of the surfaces of 50 mm $Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ sample. Fig. S5: SEM image together with EDX analysis along the cross section of the 50 mm $Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ sample. Fig. S6: XRD patterns on the surface of the 70 mm $Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ sample. Table S3: thermoelectric properties of samples extracted from 70 mm pellet before and after heat treatment. Fig. S7: SEM image of the sample (top) before and (bottom) after heat treatment at 723 K for 720 hours. See DOI: 10.1039/c9ra04800f

thermal conductivity is also attainable by reducing the lattice contribution (κ_{ph}) *via* phonon scattering. To enhance this scattering effect, alloying with both heavier and larger isoelectronic atoms, such as germanium (Ge)[26–28] and tin (Sn)[29–32] on the Si position, have demonstrated to efficaciously reduce the thermal conductivity by 70% as compared to its non-alloyed value (from ~10 W m^{-1} K^{-1} to ~2.5 W m^{-1} K^{-1}).[10,17] In order to reach lattice thermal conductivity values close to the alloy limit, phonons with a wide range of wavelengths need to be scattered *via* integrating other strategies, such as nano-structuring,[33–36] nano-inclusion,[10,37–39] and modulation doping,[40] with alloying. The best performing materials in the $Mg_2(Si,Sn)$ system usually contain ~23 ± 3 at% Sn, which is where the conduction band convergence is taking place,[41,42] and all exhibit a maximum figure of merit, zT_{max}, of 1.4 ± 0.2, satisfactory for the device applications.[43]

As for industrial applications, in addition to the electrode development which is in good progress,[44–46] a large amount of material is required; thus, a scalable synthesis method that sustains the outstanding TE properties of the material needs to be established. The up-scaling process can be challenging due to occurrence of de-mixing phenomena such as the formation of Si-rich and Sn-rich regions induced by gravity.[47] Moreover, with respect to the larger amount of Mg and longer processing time, controlling the evaporation of Mg could be problematic. Although a previous study showed that the Mg loss in an up-scaling process can be tackled utilizing the gas atomization technique,[48] this method is not commonly available in material synthesis laboratories. In this study, a practical scalable procedure for synthesis of high efficiency Bi-doped $Mg_2(Si,Sn)$ based TE materials together with the effect of heat treatment on the microstructure and TE properties of these materials will be discussed. The proposed procedure comprises less steps and shorter duration compared to the conventional solid state reaction which was employed for large scale Bi-doped Mg_2Si production,[49] and the samples demonstrate higher structural stability than those of up-scaled Bi-doped and Sb-doped $Mg_2Si_{0.4}Sn_{0.6}$ upon thermal cycling.[50] Although this study focuses on the high performance n-type material, we believe the technique can be applied to this class of material with different doping or Si/Sn ratio (Fig. S1†) with subtle adjustments, and is a step forward towards the technological feasibility of silicide based thermoelectric generators (TEGs).

2. Experimental section

$Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ samples were prepared by using Mg pellets (99.99%, Evochem, 3–6 mm), Si powder (99.9%, Alfa Aesar, −100 mesh), Sn granules (99.99%, Evochem, 1–4 mm), and Bi granules (99.999%, Goodfellow, ~7 mm) for the synthesis. The elements were placed inside a graphite crucible in an argon filled glove box according to the stoichiometric ratios plus ~6 wt% of excess Mg to compensate for the evaporation during high temperature steps of the material preparation. The crucible was then transferred to a Direct-Current Sintering Press (Dr. Fritsch GmbH, DSP 510 SE) for the melting process. Subsequently, melting was performed at various temperatures (from 973 K to 1273 K) for three times consecutively to increase stoichiometric homogeneity. To complete the reaction and facilitate the homogenization process, the obtained ingot was then ball-milled for around 12 hours using a high-energy SPEX Sample Prep 8000D Mixer Mill with stainless steel balls and vials, where the weight of the collected powder is more than 98% of the targeted initial mass. To obtain compacted pellets, the as-milled powder was sintered at 973 K for 20 minutes under ~40–60 MPa and partial Ar atmosphere using DSP 510 SE with graphite dies of 50 mm and 70 mm inner diameter, respectively. To alleviate strain and stress on the pellets, the pressure was released during their natural cooling process.

A D8 Discover Bruker X-ray diffractometer with Cu-Kα_1 radiation and a HI-STAR-2D area detector was used to determine the purity of the synthesized samples. X-ray patterns on the pellets (Fig. S2†) revealed small traces of Mg from the excess amount used, and magnesium oxide (MgO) which is a well-known side product in Mg_2Si based compounds.[51–53]

The pressed pellets were 50 mm and 70 mm in diameter and ~5 mm in thickness. The functional homogeneity of the pellets was investigated by an in-house developed surface scanning Seebeck microprobe (PSM).[54] For measuring the electrical conductivity (σ) and Seebeck coefficient (S), the pressed pellets were subsequently cut into bars with the dimensions of approximately 10 × 10 × 4 mm. The measurements were carried out under helium (He) atmosphere between 300 K and 773 K by utilizing an in-house developed facility (High Temperature Seebeck and Sigma Measurement Instrument) applying a four-probe method.[55] The detailed analysis of the Seebeck coefficient measurement is explained elsewhere;[56] the uncertainty of the measurement can arise from various sources such as cold finger effect[57] and is estimated to be around 5%.[58] To study the effect of heat treatment on the microstructure of the samples, scanning electron microscopy (SEM) analysis was performed on parts of pellets using an ULTRA 55 electron microscope equipped with a Zeiss QBSE detector associated with an Oxford energy dispersive X-ray (EDX) device, EDAX PentaFETx3.

Thermal diffusivity (α) of the pressed pellets was measured between 300 K and 773 K under Ar flow using the laser flash Netzsch LFA 427 apparatus. The measured values were then multiplied by the density (ρ) of the pellets, measured *via* the Archimedes method in ethanol, and the specific heat (C_p) of the compounds, calculated utilizing the Dulong–Petit approximation, to obtain the thermal conductivity (κ), $\kappa = \alpha \times \rho \times C_p$. The calculated specific heat together with the obtained densities of all the samples is available in Tables S1 and S2.† The Dulong–Petit approximation was previously confirmed to be well within the accepted accuracy for Mg_2Si based materials.[26,59]

Thermal stability experiments were performed on boron nitride coated samples under partial Ar pressure using a GERO-D7531 vertical resistance heater furnace. The annealing temperature was fixed at 723 K and the test duration varied between 168 hours and 720 hours.

3.   Results and discussion

First of all, it is worth to mention that the initial attempts on large scale synthesis of high performance $Mg_2(Si,Sn)$ materials led to a clear agglomeration of Sn and Sn-rich phases at the bottom of the compacted pellet (Fig. S3†). This could be due to the current passing through the sample during sintering which softened the heavier Sn-rich phases with low melting points. As a consequence, these compositions accumulate at the bottom of the as-sintered pellet. To tackle this issue, the current path through the sample is blocked through non-conductive coating and a gradual heating procedure is then employed for the sintering process. The surface Seebeck scan of both surfaces together with the cross section of the ∅50 mm pellet made by pressing 50 grams of $Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ powder is shown in Fig. 1.

   The negative values of the Seebeck coefficient on all the surfaces confirm electrons to be the major charge carriers, as expected due to bismuth doping on the silicon position. All the surfaces exhibit high functional homogeneity with the average Seebeck value of -122 ± 7 μV K^{-1} in majority of the areas. The obtained average value is well within the range of previously reported Bi-doped $Mg_2(Si,Sn)$ samples with the optimized doping level.[15,17] As an example, the frequency count of Seebeck values for one of the surfaces is illustrated in Fig. S4† demonstrating mainly a single peak distribution behaviour. Moreover, the scanning electron image together with the compositional EDX analysis along the cross section of the sample (Fig. S5†) show rather uniform compositions close to the nominal values (Mg ∼ 66.7 at%, Si ∼ 10.0 at%, Sn ∼ 22.5 at%, Bi ∼ 0.8 at%). For the transport property measurements, the ∅50 mm sample was divided into quarters (numbered as I–IV) and one sample from each quarter was extracted to assure and confirm the consistency of the observed values. Fig. 2 shows the temperature dependent Seebeck coefficient of all samples in one heating and cooling cycle from ∼300 K to ∼773 K. The average Seebeck value of all samples at ∼300 K is around -115 ± 6 μV K^{-1} which is in good agreement with the value obtained from surface Seebeck measurement on the whole pellet. This value is in the expected range for the heavily doped n-type $Mg_2(Si,Sn)$ compounds due to the high carrier concentration in the order of 10^{20} cm^{-3}.[17,23,43] By increasing the temperature, the absolute Seebeck value is increased for all the samples and reached an average maximum value of -200 ± 10 μV K^{-1} at ∼773 K.

   The electrical conductivity of all the samples is presented in Fig. 3. All samples exhibit fairly similar (within the uncertainty range of the measurement) electrical conductivity of above 2000 Ω^{-1} cm^{-1} at ∼300 K that proves their heavily doped character compared to ∼2 Ω^{-1} cm^{-1} at ∼300 K for an undoped material.[10] All samples follow the degenerate semiconductor behavior with increasing the temperature, and their electrical conductivity decreases due to a decrease in mobility.[60] Even though magnesium oxide can reduce the electrical conductivity at lower temperatures,[53] we only observed the usual decrease with elevated temperature due to the scattering of electrons with acoustic phonons, indicating that the detected MgO amount
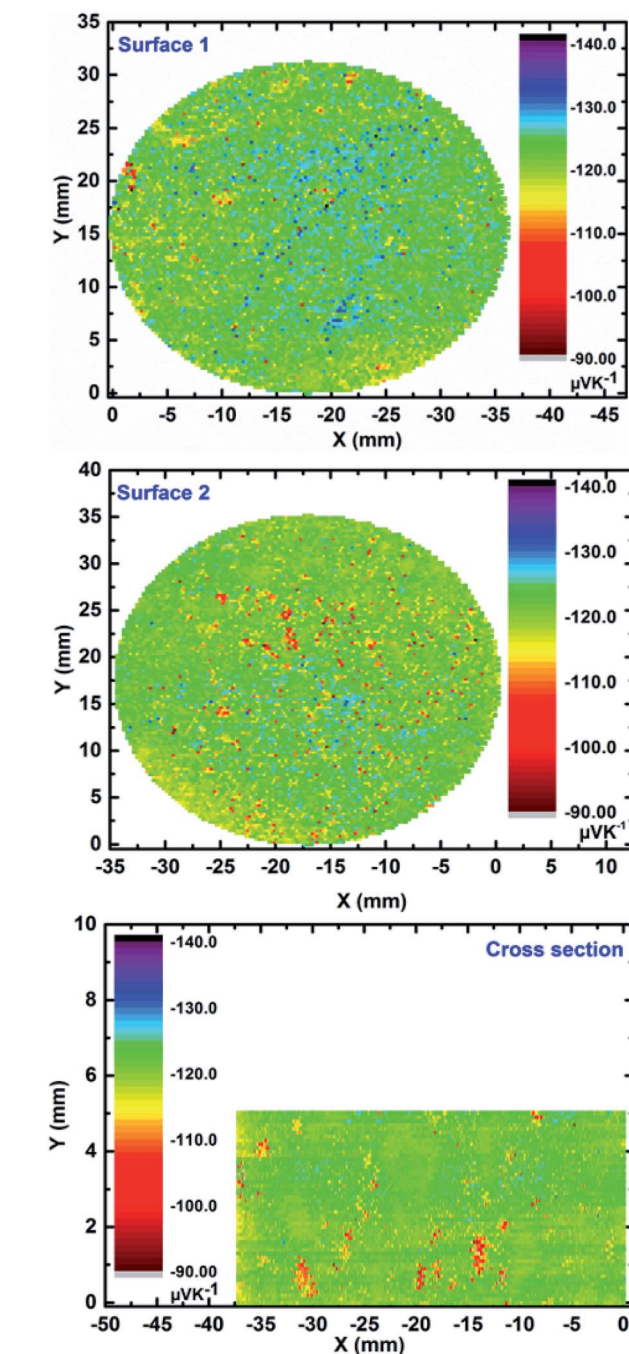

Fig. 1 Surface Seebeck scans of both base faces and cross section of ∅50 mm $Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ pellet compacted from 50 grams of material (error 5%).

does not significantly influence the thermoelectric properties. All samples reach a value of around 1000 Ω^{-1} cm^{-1} at ∼773 K which is quite comparable with the values previously reported for Bi-doped $Mg_2(Si,Sn)$ with similar composition.[15,17,43] Although the Seebeck values of these samples are similar to those of the $Mg_2Si_{0.5875}Sn_{0.4}Sb_{0.0125}$ samples synthesized using gas atomization technique,[48] the initial electrical conductivities (∼2500 Ω^{-1} cm^{-1}) are around 25% higher, which could be attributed to both higher doping level (higher carrier

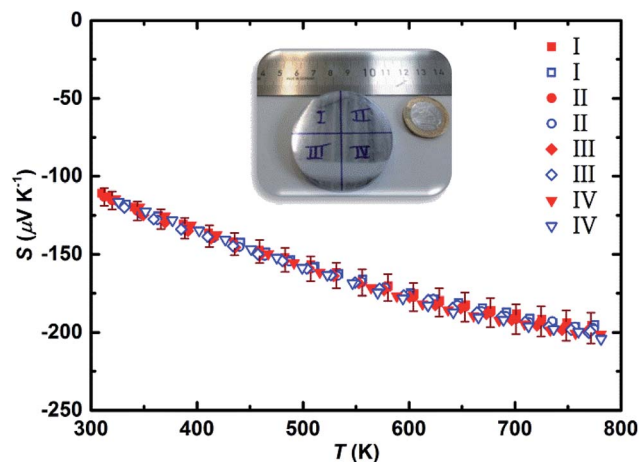**Fig. 2** Seebeck coefficient of the four samples extracted from the ⌀50 mm $Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ pellet (I–IV) (error 5%). The solid and open symbols represent the heating and cooling cycles, respectively.

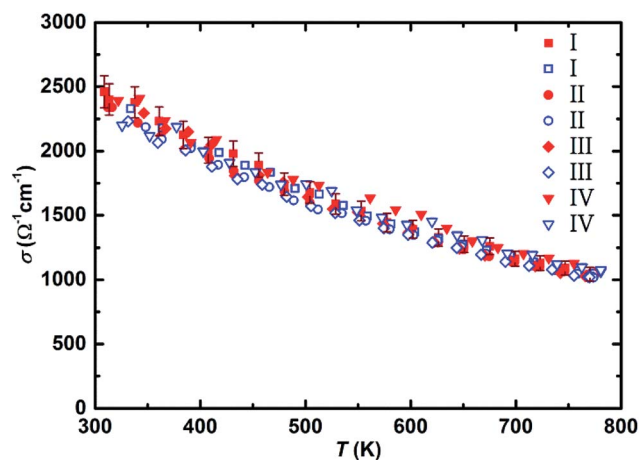**Fig. 3** Electrical conductivity of the four samples extracted from the ⌀50 mm $Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ pellet (I–IV) (error 5%). The solid and open symbols represent the heating and cooling cycles, respectively.

concentration) and optimum Sn content leading to less alloy scattering (*i.e.* higher carrier mobility).

To be able to calculate the dimensionless figure of merit (zT) for all the samples, the thermal conductivity of sample number I is measured and used for the calculation. Since all the samples have the same chemical composition and manifest rather identical electrical conductivity, Seebeck coefficient, and density values, no significant difference is expected for their thermal conductivity.

Fig. 4 shows the temperature dependent total thermal conductivity together with the lattice and bipolar contributions of the thermal conductivity of sample I. The thermal conductivity decreases from 2.82 W m^{-1} K^{-1} at ~350 K to reach a minimum value of 2.35 W m^{-1} K^{-1} at ~700 K. For the temperature above 700 K, a slight increase in thermal conductivity is observed which is due to the excitation of intrinsic carriers (bipolar contribution) leading to a value of 2.47 W m^{-1}
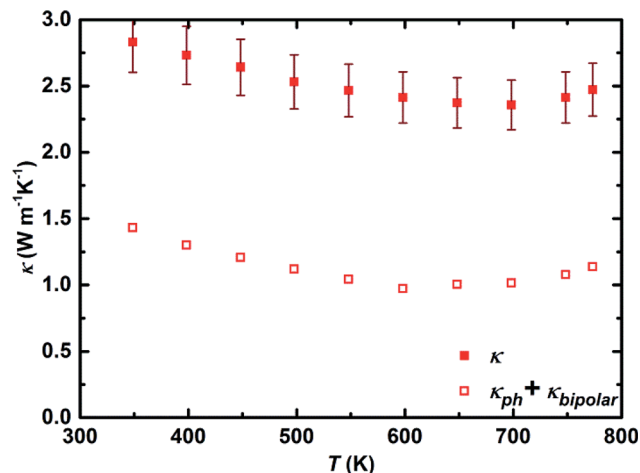

Fig. 4 Total thermal conductivity (solid symbols), lattice and bipolar thermal conductivity (open symbols) of sample I (error 8%).

K^{-1} at ~773 K. The obtained values are very well comparable with the previously reported ones for $Mg_2Si_{0.3}Sn_{0.7-x}Bi_x$ composition.[17] The $Mg_2Si_{0.5875}Sn_{0.4}Sb_{0.0125}$ sample synthesized using gas atomization showed slightly lower thermal conductivity at high temperatures (>700 K), which could be due to more alloy scattering (less Sn substitutions), less bipolar contribution (larger band gap originating from lower Sn content), and smaller grain sizes.[48]

The lattice and bipolar contributions to the thermal conductivity, $\kappa_{ph} + \kappa_{bipolar}$, were extracted from the total thermal conductivity (Fig. 4), κ, by deducting the electronic part of the thermal conductivity, κ_e, which was calculated employing the Wiedemann–Franz law, $\kappa_e = L \times \sigma \times T$. To calculate κ_e, the temperature dependence of the Lorenz number, L, was obtained through the L (10^{-8} V^2 K^{-2}) = 1.5 + exp[$-|S|$/116 µV K^{-1}] equation, where S is in µV K^{-1}, and L is expressed in 10^{-8} V^2 K^{-2}. Assuming the validity of a single parabolic band model and elastic carrier scattering, the obtained Lorenz number values are within 5% accuracy and in good agreement with the previously reported values for the Mg_2(Si,Sn) system.[17,61] The lattice thermal conductivity of 1.4 W m^{-1} K^{-1} and 1.1 W m^{-1} K^{-1} at ~350 K and ~773 K, respectively, indicates that nearly half of the total thermal conductivity is carried by phonons. To further reduce the thermal conductivity, it is worthwhile to examine approaches that affect phonon scattering by extended structural defects such as grain boundary engineering,[62,63] mesostructuring,[64] and hierarchical architectures.[65] The dimensionless figure of merit, zT, of all samples in the temperature range of 300 K to 800 K is presented in Fig. 5. The figure of merit of all samples starts from around 0.3 at ~300 K and enhances with increasing temperature to around 1.3 at ~773 K, that is quite comparable to the as-synthesized sample using gas atomization method and among the highest so far reported efficiency for this class of material.[12,15,17,23,66] This provides an average zT of 0.9 over the whole temperature range which is distinctly beneficial from the module fabrication point of view. The figure of merit of all samples is within the accepted uncertainty range of calculation (10–20%).[67]
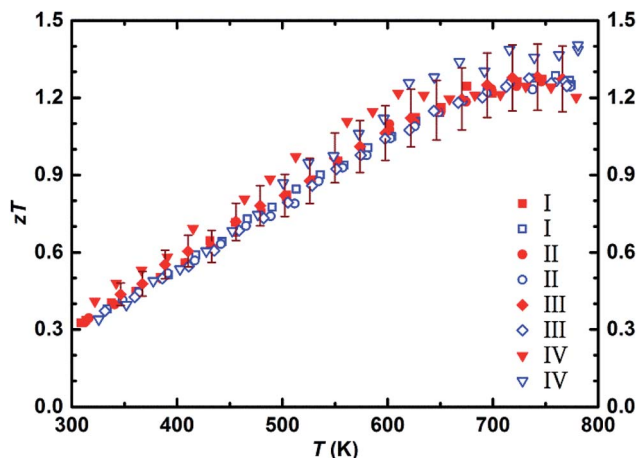
Fig. 5 Temperature dependent dimensionless figure of merit of four samples extracted from the ∅50 mm $Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ pellet (I–IV) (error 10%).

In another attempt to expand the scalability of this method, 75 grams of the material synthesized through a similar procedure was pressed using the ∅70 mm graphite die. The X-ray diffraction analysis made on 10 different points on the sample (Fig. S6†) reveals similar phase homogeneity to what was achieved for the ∅50 mm pellet. The comparison between the electronic transport properties of 50 gram and 75 gram sample is illustrated in Fig. 6. Across the entire temperature range, both electrical conductivity and Seebeck coefficient values can be considered analogous within the accepted uncertainty of the measurement.

To be able to employ the high efficiency of the synthesized material for module fabrication, it is crucial to have knowledge concerning the thermal stability of the material. For this purpose, three samples (numbered I to III) were extracted from the ∅70 mm pellet and annealed at 723 K (*i.e.* operational temperature at the hot side of $Mg_2(Si,Sn)$ based thermoelectric module) for the durations of 168 hours, 336 hours, and 720 hours, respectively. Fig. 7 shows the electrical conductivity and Seebeck coefficient of the samples before and after heat treatment. Since MgO formation was previously observed on the samples heat treated in air,[68–70] partial Ar atmosphere was chosen for our experiments.

Boron nitride (BN) coating was shown earlier to be a potent high temperature coating for $Mg_2Si_{0.3}Sn_{0.7}$ sample in order to prevent Mg loss and oxidation;[71] therefore, it is also applied to our samples. Table S3† summarizes the electronic transport properties of all the samples before and after heat treatment at ~773 K. No significant change is observed in any of those properties, corroborating the stability of the synthesized material under the examined conditions. To be able to successfully operate the $Mg_2(Si,Sn)$ based devices in air, an anti-oxidation layer needs to be developed covering the materials' exposed surfaces. For instance, yttria-stabilized zirconia $((Y_2O_3)_{0.08}(ZrO_2)_{0.92}$, YSZ) appeared to be an effective anti-oxidation barrier for Mg_2Si legs heat treated at 973 K in air, which hampered the oxygen diffusion without significantly
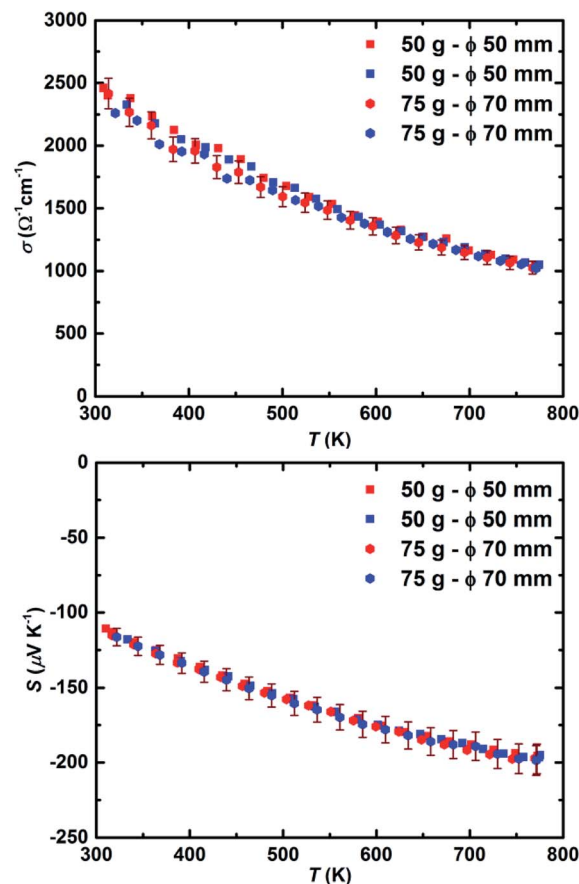

Fig. 6 Electrical conductivity (top) and Seebeck coefficient (bottom) of the samples extracted from the ∅50 mm and ∅70 mm $Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ pellets (error 5%, red and blue symbols represent heating and cooling cycles, respectively).

affecting the electrode contact resistance.[72] Hence, it is worth to investigate later the effect of yttria-stabilized zirconia coating on the high efficiency $Mg_2(Si,Sn)$ based legs. Although a slight decrease in electrical conductivity and a small increase in Seebeck coefficient observed after 720 hours of annealing, this could also be partly attributed to the grain growth detected on the SEM image of the sample before and after heat treatment (Fig. S7†). However, it should be noted that these changes are still within the error ranges of the measurements meaning the materials remain functionally stable after this long period of heat treatments.

All in all, the materials obtained from this scalable synthesis route not only show a high performance zT reaching around 1.3 at 773 K, but also are scalable and stable under heat treatment up to 720 hours. To the best of our knowledge, there are very few reported works on the successful large scale synthesis of high efficiency magnesium silicide-based compounds; aside from our method, the other approaches include gas atomization[48] and solid state reaction.[50] On the one hand, the gas atomization was successful in producing large quantities of material with high performance ($zT_{max} \sim 1.4$ at 800 K), but the apparatus is not easily accessible and operable in usual material science laboratories. On the other hand, the solid state reaction was
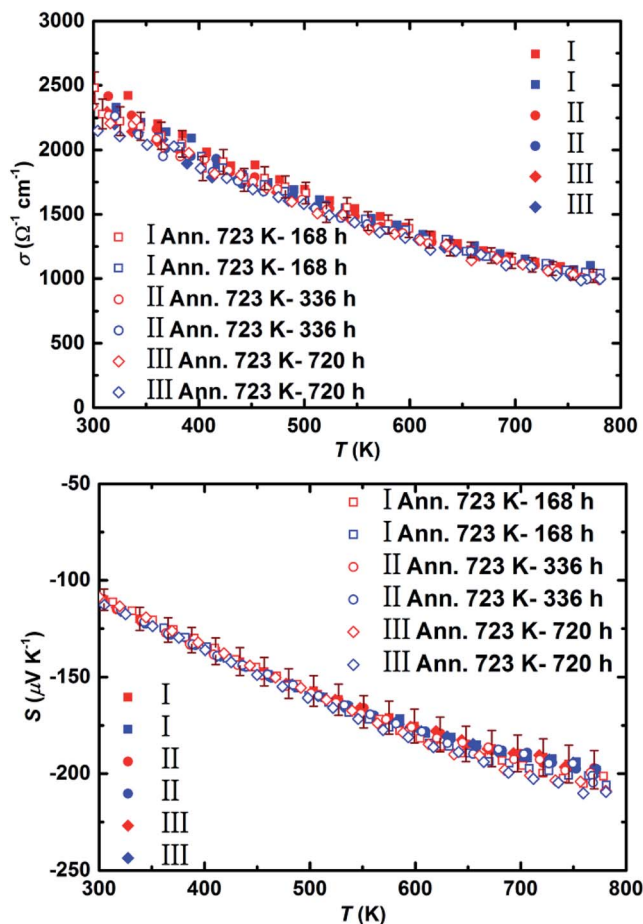
Fig. 7 Electrical conductivity (top) and Seebeck coefficient (bottom) of the samples extracted from the ∅70 mm pellets before (solid symbols) and after (open symbols) heat treatment (error 5%, red and blue symbols represent heating and cooling cycles, respectively).

used to make around 100 grams of sample in one batch. Unfortunately, the synthesized materials show a low thermal stability and performance ($zT_{max} \sim 0.28$ at 650 K) due to the Sn-rich phase segregation.[50] Here, our method has proven its advantages of producing batches up to 100 grams of high performance materials by means of easily accessible and operable apparatus. Even though this achievement is a great starting point for silicide based module fabrication, further studies such as applying temperature gradients on the pellets and annealing beyond 720 hours are indispensable.

4. Conclusions

Large scale high efficiency $Mg_2Si_{0.3}Sn_{0.675}Bi_{0.025}$ samples were successfully synthesized utilizing the combination of melting and ball milling techniques. By this synthesis route a high functional homogeneity is achieved on the surfaces and cross section of the pellets. All samples exhibited heavily doped semiconducting character with the electrical conductivity of above 2000 Ω^{-1} cm^{-1} at room temperature. The Seebeck coefficient of all the samples culminated around -200 μV K^{-1} at 773

K. The effect of heat treatment on the thermoelectric properties of the prepared samples verified the stability of the TE material for at least 720 hours at 723 K. Lastly, all the samples attained a maximum zT of approximately 1.3 at 773 K, which is among the highest hitherto proclaimed for $Mg_2Si_{1-x}Sn_x$ based thermoelectric materials. Subsequently, fabricating larger scales and different compositions as well as understanding the effect of temperature gradient on the microstructure and TE properties of these materials can be explored.

Conflicts of interest

The authors declare no conflict of interest.

Acknowledgements

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