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# Theoretical predictions for low-temperature phases, softening of phonons and elastic stiffnesses, and electronic properties of sodium peroxide under high pressure†

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High-pressure phase stabilities up to 600 K and the related properties of Na<sub>2</sub>O<sub>2</sub> under pressures up to 300 GPa were investigated using first-principles calculations and the quasi-harmonic approximation. Two high-pressure phases of Na<sub>2</sub>O<sub>2</sub> that are thermodynamically and dynamically stable were predicted consisting of the *Amm2* (distorted  $P\bar{6}2m$ ) and the *P2<sub>1</sub>/c* structures, which are stable at low temperature in the pressure range of 0–22 GPa and 22–28 GPa, respectively. However, the  $P\bar{6}2m$  and *Pbam* structures become the most stable instead of the *Amm2* and *P2<sub>1</sub>/c* structures at the elevated temperatures, respectively. Interestingly, the softening of some phonon modes and the decreasing of some elastic stiffnesses in the *Amm2* structure were also predicted in the pressure ranges of 2–3 GPa and 9–10 GPa. This leads to the decreasing of phonon free energy and the increasing of the ELF value in the same pressure ranges. The HSE06 band gaps suggest that all phases are insulators, and they increase with increasing pressure. Our findings provide the *P–T* phase diagram of Na<sub>2</sub>O<sub>2</sub>, which may be useful for investigating the thermodynamic properties and experimental verification.

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## 1 Introduction

Sodium peroxide (Na<sub>2</sub>O<sub>2</sub>) is of great interest because of its broad applications, for example as a bleaching agent, oxidizing agent, and in breathing apparatus.<sup>1,2</sup> Na<sub>2</sub>O<sub>2</sub> is also utilized as an oxygen source by capturing carbon dioxide to generate oxygen and sodium carbonate.<sup>1</sup> Moreover, Na<sub>2</sub>O<sub>2</sub> has attracted much attention in energy storage for Na–O<sub>2</sub> batteries due to its high energy density.<sup>3</sup> However, the formation of a discharge product of Na<sub>2</sub>O<sub>2</sub> on the cathode of the batteries leads to poor reversibility and increasing overpotential during recharge.<sup>3</sup> Therefore,

obtaining in-depth understanding about the structural and thermodynamic stabilities of Na<sub>2</sub>O<sub>2</sub> is of fundamental importance for improving the performance of Na–O<sub>2</sub> batteries.

It is well-known that pressure can be employed to synthesize novel materials with different electronic structures, properties, and stoichiometries.<sup>4</sup> Consequently, an in-depth understanding of the structural phase transitions and related properties (*e.g.* elastic, vibrational, and electronic properties) of Na<sub>2</sub>O<sub>2</sub> under high pressure is paramount. Previously, the crystal structure of Na<sub>2</sub>O<sub>2</sub> at ambient conditions has been investigated. Tallman *et al.* and Föppl independently studied this at room temperature using single-crystal/powder X-ray diffraction measurements. They found that the crystal structure of Na<sub>2</sub>O<sub>2</sub> is hexagonal with the  $P\bar{6}2m$  space group and lattice constants of  $a = 6.22$  Å and  $c = 4.47$  Å were reported by Tallman *et al.*<sup>5</sup> and of  $a = 6.208$  Å and  $c = 4.469$  Å were reported by Föppl<sup>6</sup> (see Table S1, ESI†). However, although the lattice constants of Tallman's and Föppl's structures are not significantly different within the maximal error of  $\pm 0.01$  Å, the atomic positions of Na1 and Na2 are significantly different with atomic displacements of 0.118 Å and 0.012 Å, respectively. Thus, the most stable structure at room temperature should be identified theoretically. Very recently, Dunst *et al.*<sup>7</sup> used the Rietveld refinement methods to analyze the X-ray powder diffraction patterns of microcrystalline and nanocrystalline Na<sub>2</sub>O<sub>2</sub>. The obtained structures were

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consistent with Föppl's structure. In addition, Tallman *et al.*<sup>8</sup> reported evidence for two new phases of Na<sub>2</sub>O<sub>2</sub> that were observed over the range of 25–550 °C. One was found at 512 °C, and the other was found at room temperature and was prepared by pouring liquid Na<sub>2</sub>O<sub>2</sub> into liquid air.<sup>8,9</sup> They suggested that the quenched Na<sub>2</sub>O<sub>2</sub> may be stable in the temperature range of 596–675 °C or at low temperature.<sup>8</sup> However, the crystal structures of the two phases have not been identified. Therefore, the determination of new phase structures of Na<sub>2</sub>O<sub>2</sub> at room and high temperature needs guidance from theoretical prediction.

As for previous high-pressure study, Deng *et al.*<sup>10</sup> investigated the structural phase transition of Na<sub>2</sub>O<sub>2</sub> in the range of 0–100 GPa using first-principles calculations. They employed the particle swarm optimization algorithm (CALYPSO) to search the lowest enthalpy structures at given pressures and optimized them using the projected augmented-wave potentials with 3s<sup>1</sup>p<sup>0</sup> and 2s<sup>2</sup>2p<sup>4</sup> as valence electrons for Na and O, respectively, and the Perdew–Burke–Ernzerhof (PBE) functional as implemented in the Vienna *Ab initio* Simulation Package (VASP). They predicted that the hexagonal *P62m* structure transforms to the orthorhombic *Pbam* structure at around 28 GPa.<sup>10</sup> However, since the high-pressure phases of Na<sub>2</sub>O<sub>2</sub> are waiting for experimental confirmation, the structural phase transition is an open question for further theoretical prediction, which has been conducted in the present work.

In this work, the first-principles calculations based on the density functional theory (DFT) formalism and the quasi-harmonic approximation (QHA) were employed to investigate thermodynamic phase stabilities in order to find new structures of Na<sub>2</sub>O<sub>2</sub> at high pressures. Here the *ab initio* random structure searching (AIRSS) method was used to search the lowest enthalpy structures. Moreover, the structural phase transition in Na<sub>2</sub>O<sub>2</sub> was also reviewed and extended up to 300 GPa based on the DFT calculations. The elastic, vibrational, and electronic properties of Na<sub>2</sub>O<sub>2</sub> at high pressures were also calculated to describe their properties. In addition, the VESTA program was also employed to visualize all crystal structures.<sup>11</sup>

## 2 Computational methods

All calculations were performed using the Cambridge Serial Total Energy Package (CASTEP),<sup>12</sup> which is based on DFT calculations. Ultrasoft pseudopotentials<sup>13</sup> were generated for Na: 2s<sup>2</sup> 2p<sup>6</sup> 3s<sup>1</sup> and O: 2s<sup>2</sup> 2p<sup>4</sup>, and the GGA–PBE exchange–correlation functional<sup>14</sup> was employed with a plane-wave basis cutoff of 760 eV and a *k*-point grid spacing of 2π × 0.04 Å<sup>-1</sup>. In order to optimize the unit cells, the ultrafine quality of convergence tolerance was set as follows: energy change less than 1.0 × 10<sup>-6</sup> eV atom<sup>-1</sup>, a residual force less than 0.01 eV Å<sup>-1</sup>, atomic displacement within 5.0 × 10<sup>-4</sup> Å, and stress below 0.02 GPa. Furthermore, to calculate the phonon and electronic properties, the cells were optimized again with a denser grid spacing of 2π × 0.02 Å<sup>-1</sup> and maximum force less than 0.001 eV Å<sup>-1</sup>.

In order to search the lowest enthalpy structure in the pressure range of 0–300 GPa, the AIRSS technique<sup>15</sup> was performed at 0, 10, 20, 30, 100, 200, and 300 GPa by generating the

random cells that contained Na<sub>2</sub>O<sub>2</sub> with 1, 2, 3, 4, and 6 formula units (f.u.). Furthermore, the random atomic displacements and random unit cell deformations (namely “shaking”)<sup>4</sup> were also used to generate the mutated structures of the Tallman's and the Föppl's structures at ambient pressure. By generating initial structures with different lattice parameters and number of formula units that implemented reasonable bond lengths and unit cell volumes at each pressure, the structures were relaxed to the enthalpy minimum and then the lowest enthalpy structure selected for refining the structures and their energies.<sup>15,16</sup> The simple linear approximation was employed to estimate the enthalpies (*H*) of structures at given pressures:

$$H(P) \approx H(P_s) + (P - P_s)V_s, \quad (1)$$

where *H*(*P*<sub>s</sub>) is the lowest enthalpy of the most stable structure at pressure *P*<sub>s</sub> with volume *V*<sub>s</sub>, while *H*(*P*) is the enthalpy of different structures which may become more stable at another pressure *P*.<sup>15</sup> To obtain the pressure dependence of enthalpy for the lowest enthalpy structure, the total energy *versus* unit cell volume relations were fitted using the third-order Birch–Murnaghan equations of states,<sup>17</sup> and the enthalpies at the pressures from 0 to 300 GPa were calculated using the formula *H* = *E* + *PV*.

Elastic constants calculations were performed to analyze the evolution of the elastic constants, bulk and shear moduli, and elastic anisotropy of Na<sub>2</sub>O<sub>2</sub> for the ambient phase at elevated pressure. By generating the set of distorted structures that is required by the symmetry, the full 6 × 6 tensor of elastic constants was produced to determine the stress–strain relationships.<sup>18</sup> Furthermore, the universal elastic anisotropy index (*A*<sup>U</sup>) was used to quantify the elastic anisotropy, which was obtained from the formula<sup>19</sup>

$$A^U = \frac{K^V}{K^R} + 5 \frac{G^V}{G^R} - 6, \quad (2)$$

where the superscripts R and V represent the lower (Reuss) and upper (Voigt) bounds on the bulk (*K*) and shear moduli (*G*), respectively. Reuss and Voigt of the bulk (*K*<sup>R</sup>, *K*<sup>V</sup>) and shear moduli (*G*<sup>R</sup>, *G*<sup>V</sup>) were calculated from the elastic constants using the Voigt–Reuss–Hill approximations.<sup>20</sup>

To verify the dynamical stability of the predicted structures, phonon dispersions and phonon density of states were calculated using the finite-displacement supercell method.<sup>21</sup> Moreover, the phase stabilities of the predicted structures under different pressures and temperatures were also verified by comparing the differences of Gibbs free energies ( $\Delta G$ ) between those structures. The Gibbs free energies, *G*(*P*, *T*), as a function of pressure and temperature were calculated using the standard thermodynamic relations *G* = *F* + *PV*, and the thermodynamic calculations were conducted based on the QHA.<sup>22</sup> Helmholtz free energies, *F*(*V*, *T*), were calculated as

$$F(V, T) = E(V) + F_{\text{ph}}(V, T), \quad (3)$$

$$F_{\text{ph}}(V, T) = k_{\text{B}}T \int_0^{\infty} g(\omega) \ln \left[ 2 \sinh \left( \frac{\hbar\omega}{2k_{\text{B}}T} \right) \right] d\omega, \quad (4)$$



where  $E(V)$  is the ground-state total energy at 0 K as a function of volume, and  $F_{\text{ph}}(V, T)$  represents the phonon free energy at volume  $V$  as a function of temperature  $T$  including the zero-point vibrational energy.  $\omega = \omega(V)$  stands for the volume dependence of phonon frequencies, and  $g(\omega)$  is the phonon density of states.  $\hbar$  and  $k_{\text{B}}$  are the reduced Planck's and Boltzmann's constants, respectively.<sup>23</sup> Thus,  $G(P, T)$  can be rewritten as follows:

$$G(P, T) = E(V) + F_{\text{ph}}(V, T) + P(V, T)V, \quad (5)$$

$$P(V, T) = -\frac{\partial F(V, T)}{\partial V} = P(V) - \frac{\partial F_{\text{ph}}(V, T)}{\partial V}, \quad (6)$$

$$G(P, T) = E(V) + F_{\text{ph}}(V, T) + P(V)V - V\frac{\partial F_{\text{ph}}(V, T)}{\partial V}. \quad (7)$$

In eqn (7),  $E(V)$  and  $P(V)$  were obtained from the DFT calculations that were fitted using the third-order Birch–Murnaghan equations of states and  $F_{\text{ph}}(V, T)$  was obtained from eqn (4). The relationships between  $F_{\text{ph}}(V, T)$  and  $V$  for various volumes at the same temperature were obtained from using the third-order polynomial fitting and then calculating the last term of  $\partial F_{\text{ph}}(-V, T)/\partial V$  at various temperatures  $T$ . Finally, the relationships between  $G(P, T)$  and  $P$  at the same temperatures were also fitted using the third-order polynomial function in order to calculate the  $G(P, T)$  for each structure at given pressures and temperatures.

In order to investigate the electronic properties and bonding in the predicted structures of  $\text{Na}_2\text{O}_2$  at high pressures, the electronic band structures and the partial density of states (PDOSs) were determined using the PBE<sup>14</sup> and HSE06<sup>24</sup> functionals. The HSE06 band structures and their PDOSs were calculated using the relaxed structures obtained from the PBE functional. Furthermore, ELF's were also calculated to describe the pressure effect on the chemical bonding in the *Amm2* phase of  $\text{Na}_2\text{O}_2$ .

## 3 Results and discussion

### 3.1 Structural phase transitions and phase stabilities

**3.1.1 High-pressure structural phase transitions at 0 K.** By employing the AIRSS search for  $\text{Na}_2\text{O}_2$  structures in the pressure range of 0–300 GPa, the findings at 0, 10, and 20 GPa revealed the two stable structures consisting of the hexagonal *P62m* structure (3 f.u. per cell) and the orthorhombic *Amm2* structure (6 f.u. per cell), when their enthalpy difference is only 2 meV f.u.<sup>-1</sup> (Fig. 1). However, the *Amm2* structure is a slightly distorted version of the *P62m* structure because the *P62m* structure can be relaxed to be the *Amm2* structure, and their simulated X-ray diffraction (XRD) patterns are slightly different (Fig. S1(a), ESI†). Moreover, the two crystal structures which are the monoclinic *P21/c* structure (2 f.u. per cell) and the orthorhombic *Pbam* structure (2 f.u. per cell) are also found at 30 GPa (Fig. 1). The enthalpy difference between the *P21/c* and *Pbam* structures is small. Nevertheless, the XRD patterns of both structures are significantly different (Fig. S1(b)†). Furthermore, the *P21/c*

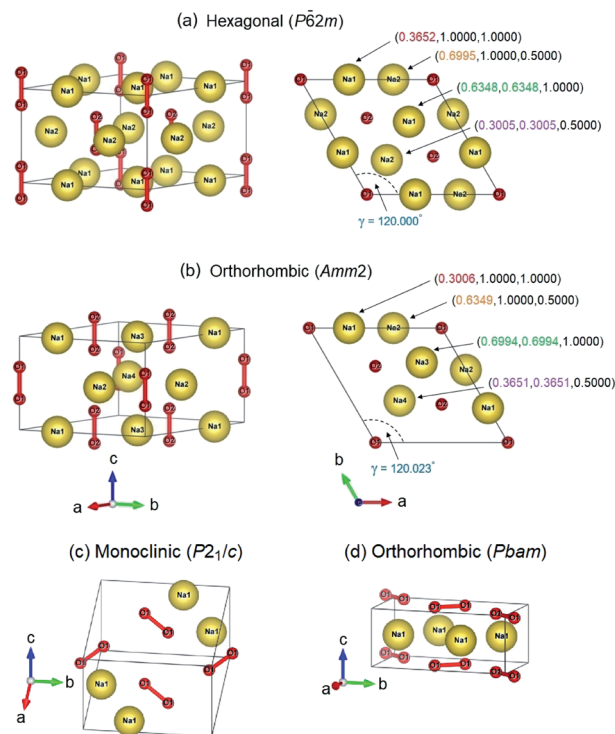


Fig. 1 The crystal structures: (a and b) the *P62m* and the primitive *Amm2* structures viewed along two directions at ambient pressure. The mapping of atomic positions for the Na atoms marked by the same color. (c) The *P21/c* structure at 22 GPa, and (d) the *Pbam* structure at 28 GPa.

structure is dynamically stable at 30 GPa but unstable at 40 GPa, while the *Pbam* structure is dynamically stable at 30–300 GPa (Fig. S2, ESI†). Here the *Pbam* structure is same as the structure proposed by Deng *et al.*<sup>10</sup> when the structure is shifted to  $(0, 0, 1/2)$ .

Moreover, the AIRSS results at ambient pressure revealed that the simulated XRD patterns of the structures look like the XRD patterns calculated from the experimental results of Tallman *et al.*<sup>8</sup> One is the *I4/mmm* structure which is approximate to the  $\text{Na}_2\text{O}_2$ -II at 550 °C (Fig. S3, ESI†), and the other structures (*C2/m*, *Pmmm*, and *Immm*) are close to the  $\text{Na}_2\text{O}_2$ -Q at room temperature (Fig. S4, ESI†). The *I4/mmm* structure is higher enthalpy than the *P62m* structure by 0.560 eV f.u.<sup>-1</sup>, while the *C2/m*, *Pmmm*, and *Immm* structures are higher enthalpy than the *P62m* structure by 0.018, 0.019, and 0.021 eV f.u.<sup>-1</sup>, respectively. With increasing pressure, these structures have increasing trends of enthalpy with respect to the *P62m* structure in the pressure range of 0–22 GPa, and they have increasing trends of enthalpy with respect to the *P21/c* and *Pbam* structures in the pressure range of 22–100 GPa as well (Fig. S5, ESI†). This suggests that these structures become more unstable with elevated pressure. Therefore, at high temperature below the melting point of 948 K, the *I4/mmm* structure might be a candidate for the  $\text{Na}_2\text{O}_2$ -II phase, whereas the *C2/m*, *Pmmm*, and *Immm* structures might be candidates for the  $\text{Na}_2\text{O}_2$ -Q phase. Generally, the symmetry of the crystal structure can be



increased by increasing the temperature. Thus, the *Immm* structure may become stable at a high temperature as it is higher symmetry than the other structures.

Using geometry optimization, the *Amm2* structure at 0 GPa has an energy lower than that of the *P6̄2m* structure by 2.1 and 0.4 meV f.u.<sup>-1</sup> calculated by the GGA-PBE<sup>14</sup> and LDA<sup>25,26</sup> functionals, respectively. These energies are slightly significant within the tolerance of the calculations. Herein the PBE functional was selected to quantify the energy difference between the *Amm2* and *P6̄2m* structures. Furthermore, the relaxed lattice parameters for the *P6̄2m* structure are in agreement with previous studies:<sup>2,5,6,27</sup>  $a = b = 6.282$  Å,  $c = 4.511$  Å, and  $\gamma = 120.000^\circ$ . The *Amm2* structure can be reduced to a primitive cell with the relaxed lattice parameters,  $a = b = 6.284$  Å,  $c = 4.510$  Å, and  $\gamma = 120.023^\circ$ , which are slightly different from those of the *P6̄2m* structure (Fig. 1). These lattice parameters also support that the *Amm2* structure is the distorted *P6̄2m* structure. Moreover, we found that there are angle differences in the same hexagonal Na layer between the  $2 \times 2 \times 2$  supercell of the primitive *Amm2* and the *P6̄2m* structures that were verified dynamically. The angles in the hexagonal Na layer of the *P6̄2m* structure are  $60.000^\circ$ ,  $55.031^\circ$ ,  $60.000^\circ$ ,  $55.031^\circ$ ,  $60.000^\circ$ , and  $69.938^\circ$  as marked by  $\theta_1$ ,  $\theta_2$ ,  $\theta_3$ ,  $\theta_4$ ,  $\theta_5$ , and  $\theta_6$ , respectively (Fig. S6(a), ESI†). These angles indicate that the *P6̄2m* structure has the distorted close-packed Na layers. However, these angles are slightly different from that of the primitive *Amm2* structure. The angles of the *Amm2* structure are  $59.995^\circ$ ,  $55.060^\circ$ ,  $60.003^\circ$ ,  $55.059^\circ$ ,  $60.003^\circ$ , and  $69.881^\circ$  as marked by  $\theta_1$ ,  $\theta_2$ ,  $\theta_3$ ,  $\theta_4$ ,  $\theta_5$ , and  $\theta_6$ , respectively (Fig. S6(b), ESI†). In addition, these angles have three trends of change with elevated pressure consisting of an increase of  $\theta_6$ , a decrease of  $\theta_2$  and  $\theta_4$ , and no change in  $\theta_1$ ,  $\theta_3$ , and  $\theta_5$ . The differences in these angles between both structures at the same pressures are shown in Fig. S7, ESI.† This

suggests that the primitive *Amm2* structure is a more distorted close-packed Na layer than the *P6̄2m* structure (deviation from  $60^\circ$ ). These suggest that the *Amm2* (distorted *P6̄2m*) structure is slightly different to the *P6̄2m* structure. However, this results in significant differences in their phonon dispersions and their electronic band structures, which will be discussed, respectively. Consequently, it is possible that the  $\text{Na}_2\text{O}_2$  phase at extremely low temperature favors the lower symmetry (*Amm2*, No. 38) rather than the higher symmetry (*P6̄2m*, No. 189).

Moreover, Fig. 2 also shows differences in the phonon dispersion and the partial phonon density of states between the primitive *Amm2* and the *P6̄2m* structures at ambient pressure. At the  $\Gamma$  point, the phonon frequencies of the *Amm2* structure at  $\sim 23.3$  and  $\sim 23.5$  THz have higher values than those of the *P6̄2m* structure, of about 5 and 4  $\text{cm}^{-1}$ , respectively, while the highest frequency of both structures are slightly different. Because these phonon frequencies directly relate to the O-O stretching modes, they suggest that the O-O bonding in the *Amm2* structure at ambient pressure is stronger than that of the *P6̄2m* structure. Furthermore, the phonon frequencies below 5 THz at the  $\Gamma$ , Y and S points of the *Amm2* structure are less than those of the *P6̄2m* structure at the  $\Gamma$ , K, and M points, respectively. Although both structures were different, there was no imaginary phonon frequency in both curves indicating the dynamical stability of the *Amm2* and *P6̄2m* structures at 0 K. Moreover, as there were several different phonon frequencies, it is possible to have different Helmholtz free energies at elevated temperature.

In addition, the formation enthalpy of  $\text{Na}_2\text{O}_2$ ,  $\text{Na}_2\text{O}$ , and  $\text{NaO}_2$  compounds at 0 K and the selected pressures of 0, 10, 20, 30, and 50 GPa were calculated to verify the phase stability of  $\text{Na}_2\text{O}_2$  using the formula:  $\Delta H_f = [H(\text{Na}_x\text{O}_y) - xH(\text{Na}) - yH(\text{O})]/(x + y)$ , where  $H(\text{Na}_x\text{O}_y)$  is the enthalpy of the considered

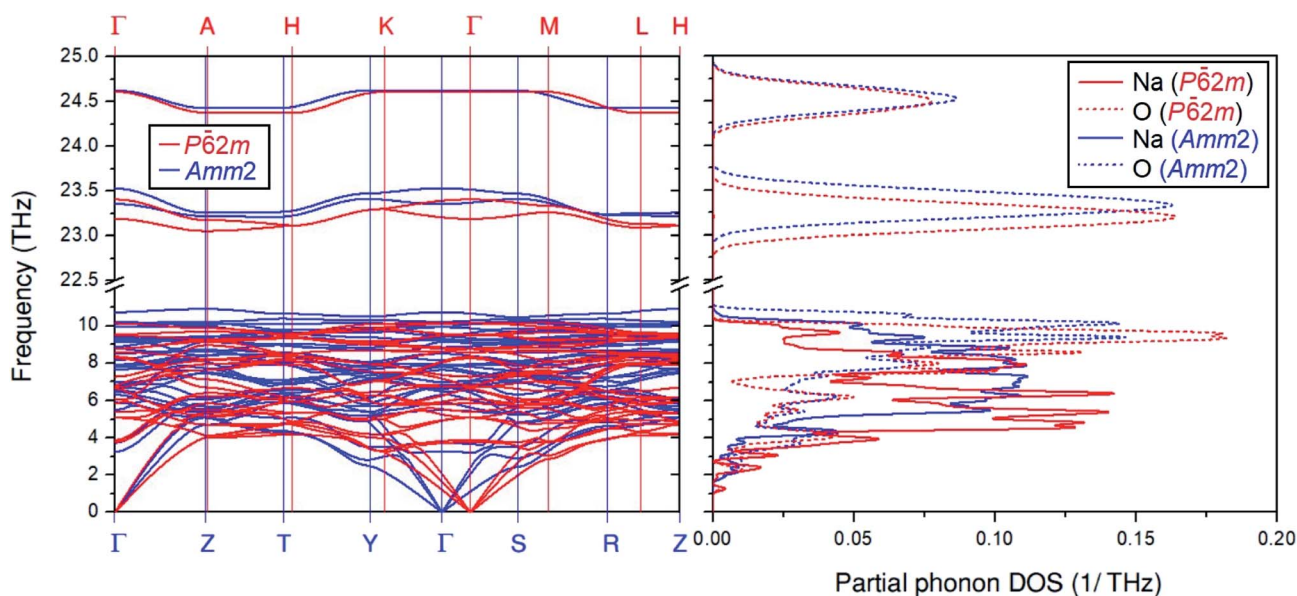


Fig. 2 The overlay plot of the phonon dispersion curves for the primitive *Amm2* and the *P6̄2m* structures and their overlay plot of the partial phonon density of states. The blue and red lines represent the primitive *Amm2* and the *P6̄2m* structures, respectively.



compound, while  $H(\text{Na})$  and  $H(\text{O})$  are the enthalpy of Na and solid O, respectively. The findings suggest that  $\text{Na}_2\text{O}_2$  is more stable with increasing pressure against decomposition into Na and  $\text{O}_2$  (Fig. 3(a)). Similarly, the enthalpies of  $\text{Na}_2\text{O} + \text{O}$ ,  $\text{NaO}_2 + \text{Na}$ , and  $(2/3)\text{Na}_2\text{O} + (2/3)\text{NaO}_2$  at the same pressures are higher than that of  $\text{Na}_2\text{O}_2$ , and these enthalpy differences become greater with elevated pressure (Fig. 3(b)). These suggest that  $\text{Na}_2\text{O}_2$  is still stable against decomposition over the pressure range studied.

In order to investigate the structural phase transitions in  $\text{Na}_2\text{O}_2$  under high pressure, the enthalpy differences of the various structures *versus* pressure were calculated (Fig. 4). The findings revealed that the enthalpies of the  $\text{Amm}2$  structure have lower values than those of the  $\text{P}62m$  structure over the pressure range with values of 2 meV f.u.<sup>-1</sup> at 0 GPa and 1.6 meV f.u.<sup>-1</sup> at 20 GPa. By comparing the total energy ( $E$ ) and the work done ( $PV$ ), we found that all  $E$  of the  $\text{Amm}2$  structure are lower than those of the  $\text{P}62m$  structure, whereas its  $PV$  values are higher (Fig. S8, ESI†). This implies that the  $PV$  plays a key role as a driving force for the high-pressure structural phase transition of the  $\text{Amm}2$  structure at 0 K. However, the  $\text{Amm}2$  structure becomes higher enthalpy than the  $\text{P}2_1/c$  structure at 22 GPa (Fig. 4). The lower enthalpy of the  $\text{P}2_1/c$  structure is maintained in the short pressure range of 22–28 GPa because the  $\text{Pbam}$  structure becomes a lower enthalpy structure at 28 GPa. There was no imaginary phonon frequency in the phonon dispersion curve of the  $\text{P}2_1/c$  structure at 22 GPa and the  $\text{Pbam}$  structure at 28 GPa, which satisfies the dynamical stability (Fig. S2(a) and (c), ESI†). Thus, the first structural phase transition is predicted at 22 GPa, the  $\text{Amm}2$  structure transforming to the  $\text{P}2_1/c$  structure, and the second structural phase transition is predicted at 28 GPa, the  $\text{P}2_1/c$  structure transforming to the  $\text{Pbam}$  structure. The transition pressure at 28 GPa is the same value as predicted by Deng *et al.*<sup>10</sup>

To investigate the driving force for the structural phase transitions, the changes of lattice constants and volume for the  $\text{Amm}2$ ,  $\text{P}2_1/c$ , and  $\text{Pbam}$  structures at high pressures were considered (Fig. S9, ESI†). At the first transition pressure of 22 GPa, the lattice constants ( $b$ ,  $c$ ) and volume ( $V$ ) of the  $\text{P}2_1/c$  structure collapsed at  $\gamma = 141.583^\circ$  by about 31.4, 37.1, and 10.0% compared to the  $\text{Amm}2$  structure, respectively. However, the lattice constant  $a$  was extended by about 11.8%. This suggests that the driving force at 22 GPa strongly affects the  $bc$ -plane. At the second transition pressure of 28 GPa,  $a$ ,  $b$ , and  $c$  of the  $\text{Pbam}$  structure collapsed by about 21.8, 0.0, and 20.4% compared to the  $\text{P}2_1/c$  structure at  $\gamma = 141.483^\circ$ , respectively. Although there was no collapse in the  $b$ -axis and volume, the fact that the  $a$ -axis collapsed rather than the  $c$ -axis leads to the alignment of the peroxide groups on the (001) plane of the  $\text{Pbam}$  structure (Fig. S11(d), ESI†).

Considering the peroxide groups' (O–O single bonds) alignment in each phase of  $\text{Na}_2\text{O}_2$  (Fig. S11, ESI†), the peroxide groups in the  $\text{Amm}2$  structure aligned in parallel with the [100] direction, whereas they aligned in parallel with the [001] direction in the  $\text{P}62m$  structure. In the case of the  $\text{P}2_1/c$  structure at 22 GPa, the peroxide groups tilted with an angle of  $\sim 24^\circ$  with respect to the  $ab$ -plane and deviated from the [100] direction by  $\sim 39^\circ$ . As for the  $\text{Pbam}$  structure at 28 GPa, the peroxide groups aligned on the (001) plane but deviated from the [100] direction by  $\sim 52^\circ$ . Moreover, at 300 GPa, the peroxide group alignment was not different from that at 28 GPa. This suggests that the alignment of the peroxide groups for each phase is significantly different, which may affect the thermodynamic stability of these structures.

### 3.1.2 Phase stabilities at high pressures and temperatures.

To verify the thermodynamic stability for the predicted structures of  $\text{Na}_2\text{O}_2$ , the QHA was employed to calculate their Gibbs free energies at various pressures up to 300 GPa and various

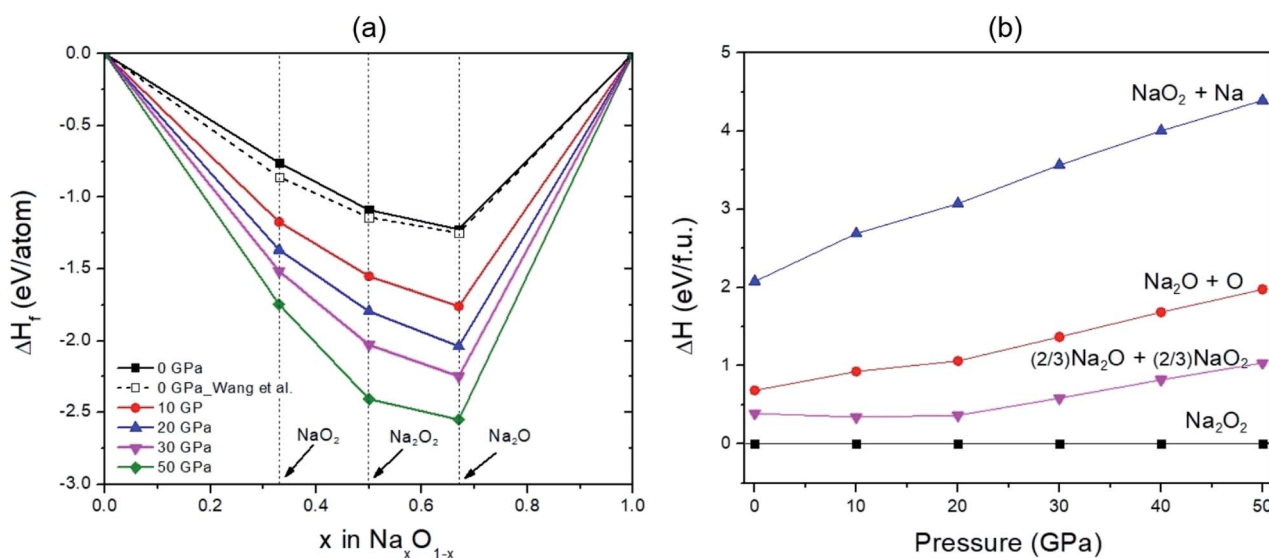


Fig. 3 (a) Predicted formation enthalpy of Na–O compounds at different pressures with respect to decomposition into Na and  $\text{O}_2$ . Dashed and solid lines connecting the data points denote the convex hull. The white squares represent the results predicted by Wang *et al.*<sup>35</sup> (b) Relative enthalpy of the decomposition with respect to  $\text{Na}_2\text{O}_2$  in the pressure range of 0–50 GPa.



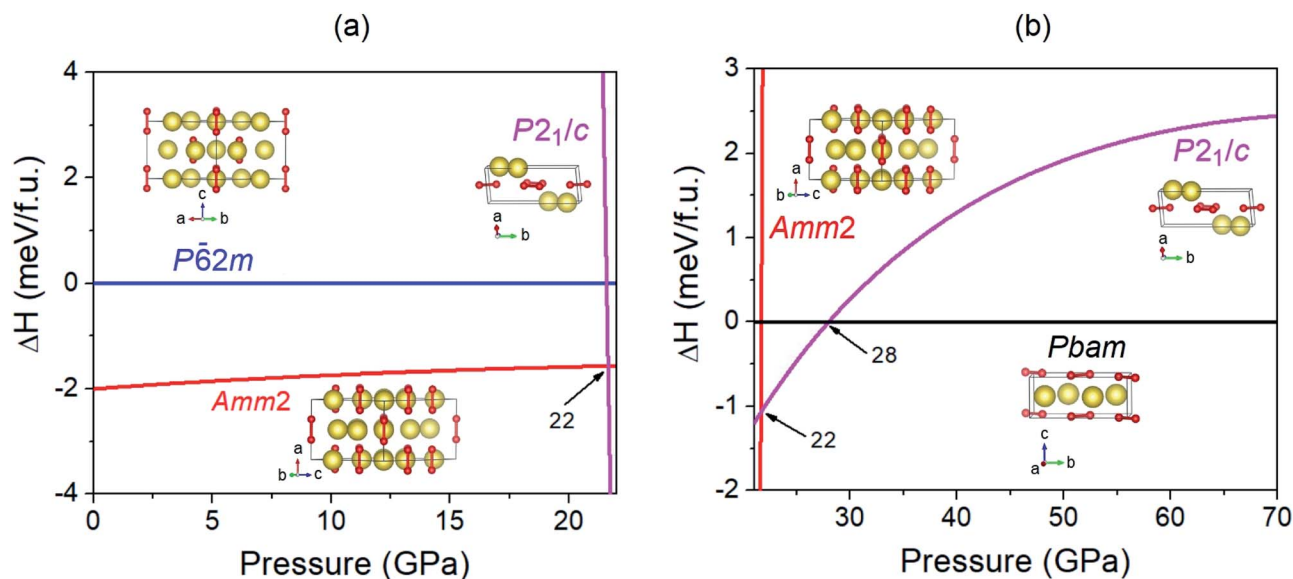


Fig. 4 (a) The enthalpy differences ( $\Delta H$ ) for the *Amm2* and *P2<sub>1</sub>/c* structures with respect to the *P6̄2m* structure versus pressure from 0 to 22 GPa and (b) the enthalpy differences ( $\Delta H$ ) for the *Amm2* and *P2<sub>1</sub>/c* structures with respect to the *Pbam* structure versus pressure from 22 to 70 GPa. Large and small spheres in all crystal structures represent the Na and O atoms, respectively.

temperatures up to 600 K. The findings showed that the Gibbs free energies decrease with increasing temperature, whereas they increase with increasing pressure (Fig. S12, ESI<sup>†</sup>). Moreover, the Gibbs free energy changes of the *Amm2* structure with respect to the *P6̄2m* structure at 0, 5, 10, 15, and 20 GPa have higher values than those of the *P6̄2m* structure at the transition temperature around 120, 125, 185, 200, and 75 K, respectively (Fig. 5(a)). This suggests that the *P6̄2m* structure becomes thermodynamically stable at these conditions. That is why the *P6̄2m* structure has been found to be stable at room temperature by previous measurements.<sup>5,6</sup> Similarly, at 22 GPa, the *P2<sub>1</sub>/c*

structure at below 105 K has the lowest free energy compared to the other structures, while the *Pbam* structure becomes the lowest free energy structure in the temperature range from 105 to 600 K (Fig. S12(b), ESI<sup>†</sup>). Moreover, at 28 GPa, the *Pbam* structure is thermodynamically stable in the temperature range of 0–600 K (Fig. S12(c), ESI<sup>†</sup>). Based on these findings, the predicted *P*–*T* phase diagram of  $\text{Na}_2\text{O}_2$  was constructed as shown in Fig. 5(b).

As for the *P6̄2m* structure, although there was no difference in the *P6̄2m* structures at 0 K and ambient pressure that were obtained from the AIRSS searches and the relaxed Tallman's/

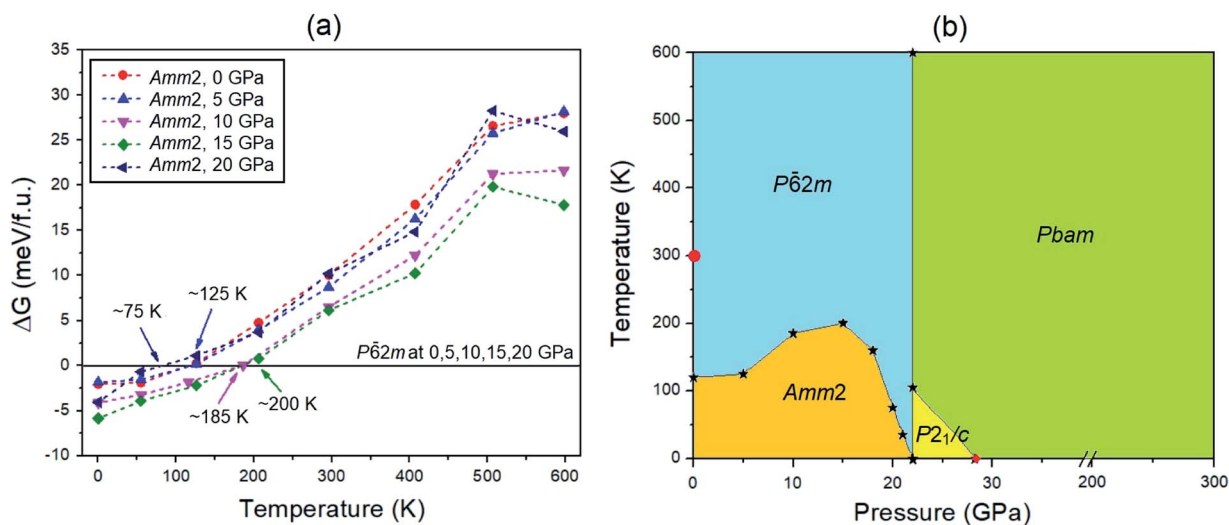


Fig. 5 (a) Gibbs free energy changes of the *Amm2* structure compared to the *P6̄2m* structure at the same pressures (0, 5, 10, 15, and 20 GPa) in the temperature range of 0–600 K. (b) The predicted phase diagram of  $\text{Na}_2\text{O}_2$  in the pressure range from 0 to 300 GPa and at temperatures up to 600 K. The circle indicates the *P6̄2m* structure at ambient conditions measured by Tallman *et al.*<sup>5</sup> and Föppel.<sup>6</sup> The diamond represents the *Pbam* structure predicted by Deng *et al.*<sup>10</sup>



Föppl's structures, there was a small significant atomic displacement of the Na1 and Na2 atoms between the Tallman's and Föppl's structures at room temperature (Fig. S13, ESI†) as discussed before. The consequence is the small difference in the XRD pattern between both structures (Fig. S14, ESI†). In particular, the intensity of the (100) peak of Tallman's structure is higher than that of Föppl's structure by about 2 percent. These suggest that Tallman's and Föppl's structures observed at room temperature are slightly different. To identify the most stable structure at elevated temperature, we calculated the Gibbs free energy for the relaxed Tallman's and Föppl's structures at ambient pressure as a function of temperature up to 600 K. The findings revealed that the free energy of Tallman's structure is not different to that of Föppl's structure in the temperature range of 0–45 K, yet it becomes lower than that of Föppl's structure by  $\sim 1.7$  and 4 meV f.u.<sup>-1</sup> at 300 and 550 K, respectively (Fig. S15, ESI†). Theoretically, this suggests that Tallman's structure is likely favored over Föppl's structure at higher temperatures. However, the free energy differences are very small and are beyond experimental resolution. Therefore, Tallman's and Föppl's structures should be considered to be similar.

### 3.2 Elastic behavior at high pressures

The present work determined the elastic constants, elastic anisotropy, and elastic moduli of the *Amm2* and *P6̄2m* structures in order to analyze the elastic properties of both structures at high pressures. In addition, the elastic stabilities for both structures were also verified. Theoretically, the hexagonal *P6̄2m* structure has five independent elastic constants:  $C_{11}$ ,  $C_{33}$ ,  $C_{44}$ ,  $C_{12}$ , and  $C_{13}$ , while the orthorhombic *Amm2* structure has nine independent elastic constants:  $C_{11}$ ,  $C_{22}$ ,  $C_{33}$ ,  $C_{44}$ ,  $C_{55}$ ,  $C_{66}$ ,  $C_{12}$ ,  $C_{13}$ , and  $C_{23}$ . The elastic stability conditions for hexagonal and orthorhombic crystal systems under hydrostatic pressure ( $P$ ) are given by  $B_{11} > |B_{12}|$ ,  $2B_{13}^2 < B_{33}(B_{11} + B_{12})$ , and  $B_{44} > 0$  for the

hexagonal case and  $B_{11} > 0$ ,  $B_{44} > 0$ ,  $B_{55} > 0$ ,  $B_{66} > 0$ ,  $B_{11}B_{22} > 2B_{12}^2$ ,  $B_{11}B_{22}B_{33} + 2B_{12}B_{13}B_{23} - B_{11}B_{23}^2 - B_{22}B_{13}^2 - B_{33}B_{12}^2 > 0$  for the orthorhombic case, where  $C_{ij}$  and  $B_{ij}$  are the elastic constants and elastic stiffnesses, respectively.<sup>28</sup> The  $B_{ij}$  are calculated from the expressions as the following:  $B_{ii} = C_{ii} - P$ ,  $B_{12} = C_{12} + P$ ,  $B_{13} = C_{13} + P$ , and  $B_{23} = C_{23} + P$ , where  $i = 1, 2, 3, \dots, 6$ .<sup>29</sup>

The findings revealed that the elastic stiffnesses of the *P6̄2m* and *Amm2* structures satisfy their elastic stability conditions. This indicates that both structures are mechanically stable. Moreover, the elastic stiffnesses also demonstrate the slight difference between the *P6̄2m* and *Amm2* structures at pressures from 0 to 15 GPa (see Fig. 6). Generally, the trend is that the elastic stiffnesses increase with increasing pressure, which indicates that the *P6̄2m* and *Amm2* structures stiffen with increasing pressure. Nevertheless,  $B_{44}$  of the *Amm2* structure and the  $(B_{11} - B_{12})/2$  term of the *P6̄2m* structure have decreasing trends with elevated pressure. This leads to elastic instability for the *P6̄2m* structure when  $B_{12}$  exceeds  $B_{11}$ , which called tetragonal shear instability.<sup>30</sup> Likewise, the *Amm2* structure has shear instability when  $B_{44}$  is equal to zero. Using linear approximation, the elastic instability of both structures was found at around 35 GPa, which is higher than the predicted transition pressure of 22 GPa. However, elastic instability occurring at a higher pressure than the transition pressure which satisfied the thermodynamic stability condition has also been proposed in other ionic compounds such as MgO and CaO. It has been interpreted that the existence of a significant activation barrier along the phase transformation path leads to the inconsistent transition pressure.<sup>30</sup> Interestingly,  $B_{11}$  of the *Amm2* structure and  $B_{33}$  of the *P6̄2m* structure stiffen dramatically at 2 GPa and then soften at 3 GPa corresponding to the unusual decreasing of the interatomic distances of O1–O1 and O2–O2 at 3 GPa (Fig. S10(a), ESI†). Moreover,  $B_{22}$ ,  $B_{23}$ , and  $B_{44}$  of the *Amm2* structure, and  $B_{12}$  and  $B_{33}$  of the *P6̄2m* structure at 9 GPa also soften slightly. This suggests that the *Amm2* structure has more

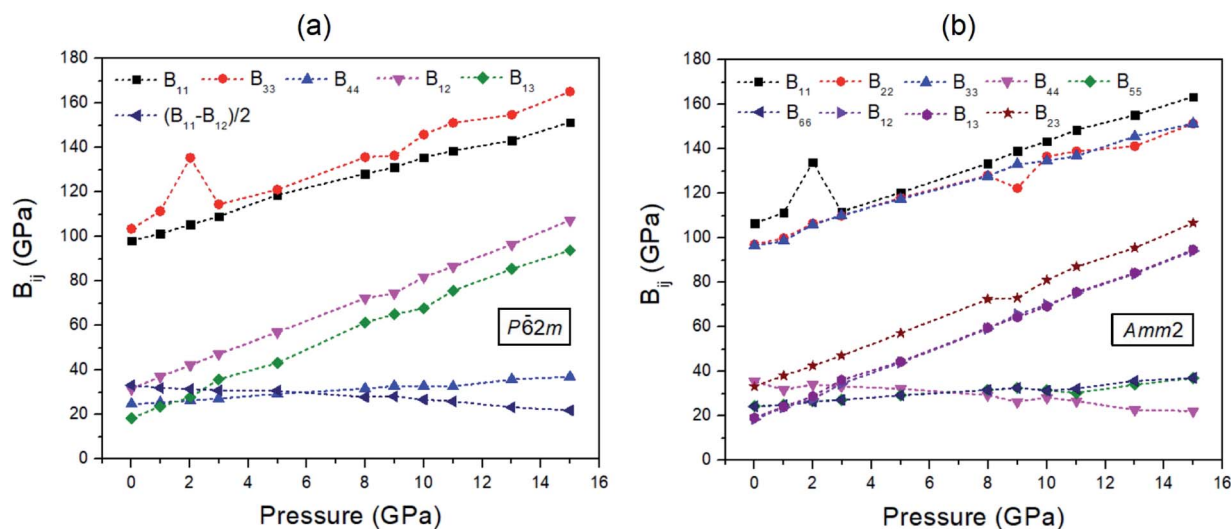


Fig. 6 The elastic stiffnesses ( $B_{ij}$ ) of two crystal structures at pressures ranging from 0 to 15 GPa for: (a) the *P6̄2m* structure and (b) the *Amm2* structure.



elastic deformation than the  $P\bar{6}2m$  structure, which may lead to thermodynamic instability at the transition temperature.

To quantify the effect of pressure on the elastic anisotropy of the crystal structures, the universal elastic anisotropy index ( $A^U$ ) of the  $Amm2$  and the  $P\bar{6}2m$  structures were calculated using eqn (2). At ambient pressure, the  $A^U$  of the  $Amm2$  and  $P\bar{6}2m$  structures were slightly different with values of 0.28 and 0.24, respectively (see Fig. S16, ESI†). The  $A^U$  of the  $P\bar{6}2m$  structure corresponds to that of 0.22 calculated by the previous study.<sup>31</sup> At elevated pressure, the  $A^U$  of both structures decreased up to 8 GPa, and then it became increasing at around 9 GPa. Moreover,  $A^U$  significantly increased at 2 GPa and drastically decreased at 3 GPa, which is consistent with the changes of the elastic stiffnesses at 2 and 3 GPa. Higher values of  $A^U$  indicate increasing elastic anisotropy, and when  $A^U = 0$  the structure is a locally isotropic crystal.<sup>19</sup> Thus, the findings suggest that pressure induced the changes of elastic anisotropy in the  $Amm2$  and  $P\bar{6}2m$  phases of  $\text{Na}_2\text{O}_2$ , and their  $A^U$  are very close to that of

a locally isotropic crystal with  $A^U = 0.03$  at 9 GPa, similar to other hexagonal crystals (*e.g.*, Ru,  $\alpha\text{-Hf}$ , and  $\alpha\text{-Gd}$ ).<sup>19</sup>

In addition, the calculated bulk and shear moduli of the  $Amm2$  and  $P\bar{6}2m$  structures at ambient pressure are shown in Table S2, ESI.† The findings demonstrated that the bulk and shear moduli of the  $Amm2$  and  $P\bar{6}2m$  structures at ambient pressure are slightly different. It is known that the elastic moduli calculated by LDA are usually overestimates, whereas those of GGA are underestimates.<sup>32</sup> Based on this reason, our results suggest that the measured bulk ( $K$ ) and shear moduli ( $G$ ) at ambient pressure should be  $K = 49.15\text{--}64.55$  GPa and  $G = 30.49\text{--}39.29$  GPa for the  $Amm2$  structure, and  $K = 48.95\text{--}64.73$  GPa and  $G = 29.01\text{--}37.88$  GPa for the  $P\bar{6}2m$  structure, respectively. Compared to the bulk moduli ( $B_0$ ) obtained from the third-order Birch–Murnaghan equations of state,  $B_0$  for the  $Amm2$  and  $P\bar{6}2m$  structures were 49.25 and 49.26 GPa, respectively. These values are in excellent agreement with the previous studies with the value of 49 GPa (ref. 31) obtained from the elastic constants calculations and 56.40 GPa (ref. 2) obtained

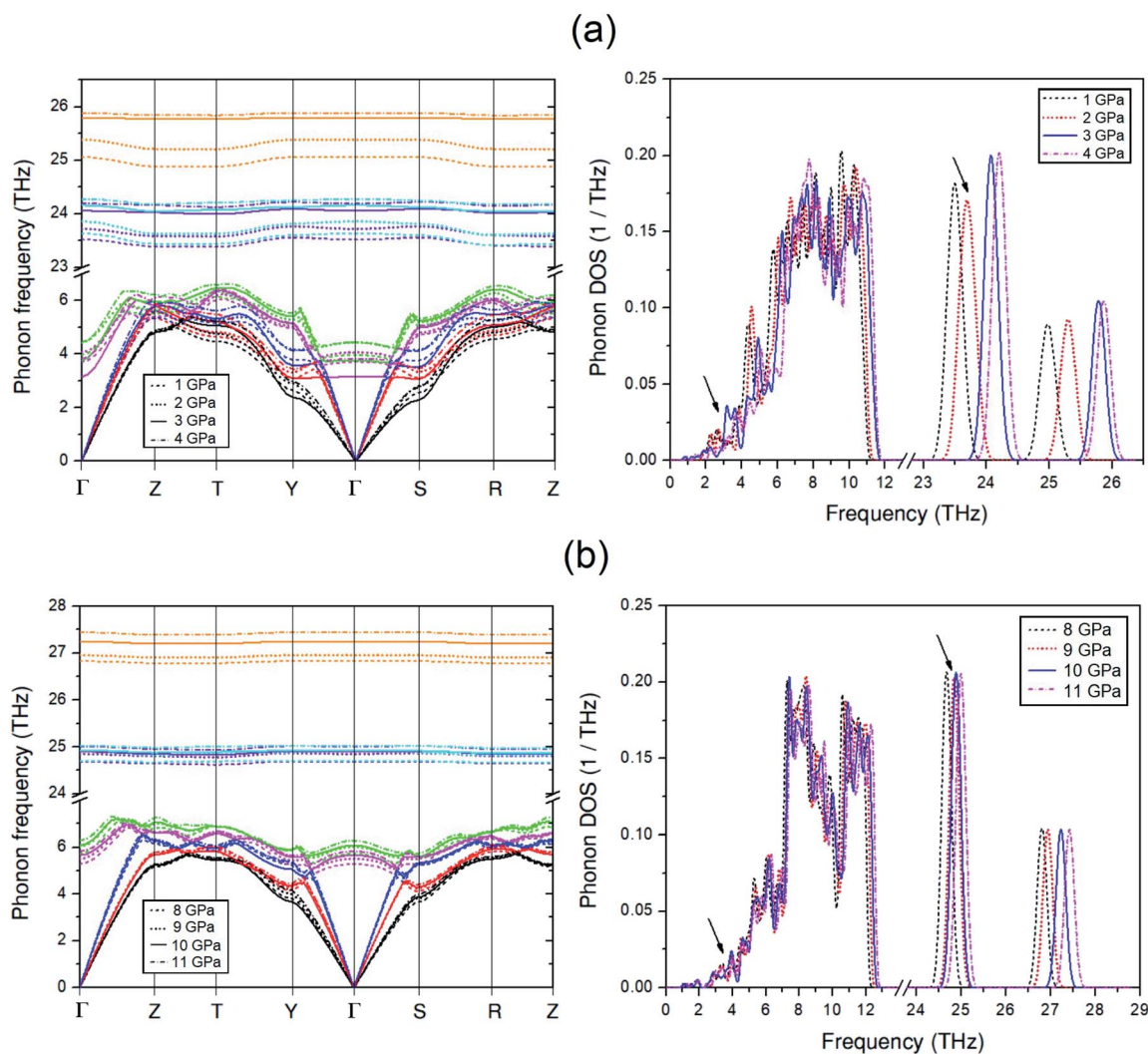


Fig. 7 Phonon dispersion curves and their phonon DOSs of the  $Amm2$  structure: (a) at 1, 2, 3, and 4 GPa and (b) at 8, 9, 10, and 11 GPa. The phonon frequency modes in the phonon dispersion curves are distinguished by different colors.



from the third-order Birch–Murnaghan equations of states. Based on the PBE functional using single-point energy calculations, the calculated bulk and shear moduli at room temperature were 55.82 GPa and 31.14 GPa for the  $P6_2m$  structure proposed by Tallman *et al.*,<sup>5</sup> and 57.16 GPa and 32.11 GPa for the  $P6_2m$  structure proposed by Föppl *et al.*,<sup>6</sup> respectively. This demonstrates the small significant difference under the upper and lower bounds on the bulk and shear moduli for the  $P6_2m$  structure. It is possible to note that the elastic properties of Tallman's and Föppl's structures at room temperature are slightly different.

### 3.3 Vibrational properties at high pressures

Although the  $Amm2$  and  $P6_2m$  structures were slightly different, there was a significant difference in their vibrational properties. Using the group theory analysis of eigenvectors, the results revealed that the vibrational modes of the  $Amm2$  structure at the  $\Gamma$  point consist of  $B_1$ ,  $B_2$ ,  $A_1$ , and  $A_2$  modes with 36 frequencies. The phonon acoustic modes are  $\Gamma_{act} = B_1 + B_2 + A_1$ , while the phonon optical modes are  $\Gamma_{opt} = 9B_1 + 8B_2 + 10A_1 + 6A_2$ . In the case of the  $P6_2m$  structure, the vibrational modes consist of  $A_2'$ ,  $E'$ ,  $A_1'$ ,  $A_1''$ ,  $A_2''$ , and  $E''$  modes with 36 frequencies as well. The phonon acoustic modes are  $\Gamma_{act} = A_2'' + 2E'$ , whereas the phonon optical modes are  $\Gamma_{opt} = 3A_2' + 12E' + A_1' + 4A_1'' + 3A_2'' + 10E''$ . We here predicted that there are differences in the phonon frequencies in each mode and activity in the IR and Raman spectra between the  $Amm2$  and the  $P6_2m$  structures at ambient pressure (see Table S3, ESI†). That is, all of the phonon frequencies in the optical modes of the  $Amm2$  structure at the  $\Gamma$  point are Raman active, while for the  $P6_2m$  structure some of them are Raman active consisting of  $E'$ ,  $A_1'$ , and  $E''$  modes only. Similarly, only the optical modes of  $A_2$  and  $E'$  for the  $P6_2m$  structure are IR active, whereas all of the optical modes for the  $Amm2$  structure are IR

active, except the  $A_2$  mode. These results suggest that it is possible to observe the  $Amm2$  structure using IR and Raman spectroscopies at temperatures below 120 K. In addition, Table S3 (ESI†) also provided the phonon frequencies in each vibrational mode, IR and Raman active modes for the  $P2_1/c$  structure at 22 GPa and the  $Pbam$  structure at 30 GPa. These results might be useful for experimentally identifying the structural phase transitions at those pressures.

To discuss the effect of the elastic stiffness stiffening at 2 GPa and softening at 3 and 9 GPa in the  $Amm2$  structure on phonon frequencies, we here considered the phonon dispersion curves and their phonon DOSs at 1, 2, 3, and 4 GPa and at 8, 9, 10, and 11 GPa as shown in Fig. 7. Moreover, we also plotted the phonon frequency shifts from that of 0 GPa *versus* pressure at the  $\Gamma$  and Y points in the pressure range of 0–15 GPa (Fig. 8). Normally, the phonon frequencies of a crystal structure increase with increasing pressure, which suggests the chemical bond stiffening. However, we found that three acoustic phonon frequencies ( $\omega_1$ ,  $\omega_2$ , and  $\omega_3$  in Fig. 8(b)) below 4 THz obviously decrease at 3 GPa around the Y and S points (Fig. 7(a)). These softening frequencies also appear in their phonon DOSs below 4 THz. Similarly, the two lowest of the optical phonon frequencies ( $\omega_4$  and  $\omega_5$  in Fig. 8(a)) near 4 THz at the  $\Gamma$  point significantly decrease at 3 GPa (Fig. 7(a)). However, although there was no unusual change in the three highest frequencies of the optical modes ( $\omega_{34}$ ,  $\omega_{35}$ , and  $\omega_{36}$ ) at those pressures, the increase of frequency from 2 to 3 GPa was slightly more than that from 1 to 2 GPa and 3 to 4 GPa, and similar to the increase of frequency from 9 to 10 GPa. Additionally there was an unusual decrease in the interatomic distances of the O1–O1 and the O2–O2 at 3 GPa (Fig. S10(a), ESI†). Furthermore, the phonon DOSs of the  $\omega_{34}$  and/or the  $\omega_{35}$  decrease significantly at 2 GPa (Fig. 7(a)). This may be a consequence of the increasing of the elastic stiffness  $B_{11}$  at 2 GPa. Likewise, at 10 GPa, the  $\omega_1$  and  $\omega_3$  below 5 THz

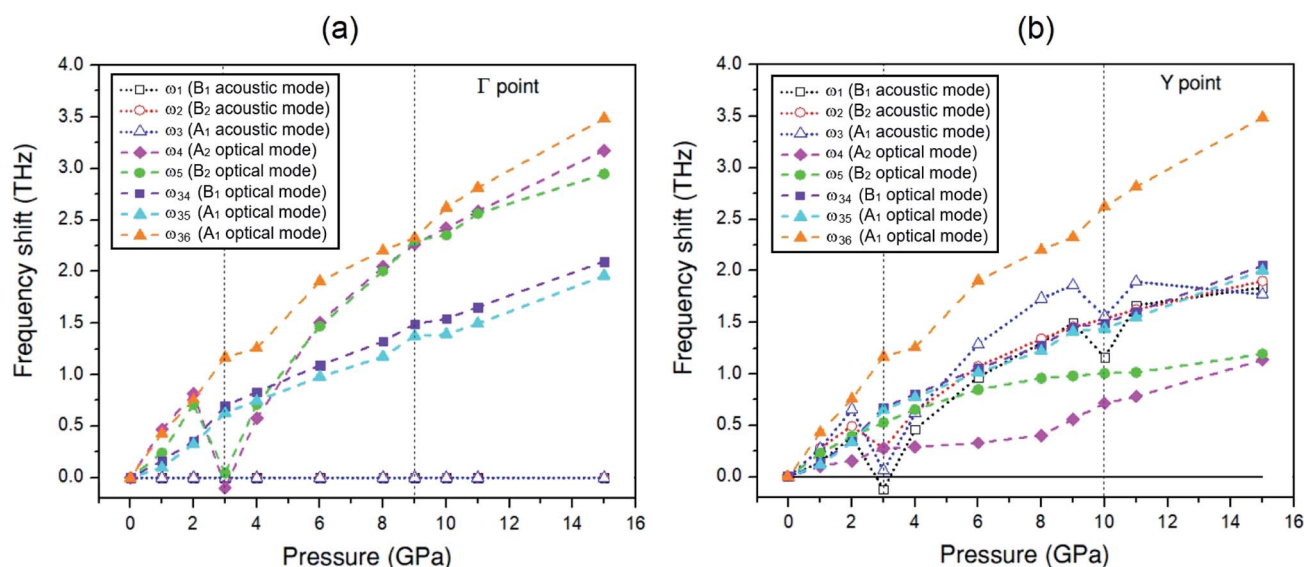


Fig. 8 The selected phonon frequency shifts *versus* pressure ranging from 0 to 15 GPa for 3 frequencies of the acoustic modes and 5 frequencies of the optical modes at different  $k$ -points of the  $Amm2$  structure: (a) at the  $\Gamma$  point and (b) at the Y points.



obviously decrease around the Y point (Fig. 7(b)). In addition, these phonons softening result in the decreasing of the phonon free energy at 3 and 10 GPa with respect to the trend line (Fig. S17, ESI†) as well. However, this effect decreases with elevated temperature. Therefore, it is possible to note that the pressure induced the decreasing of elastic stiffness and the phonon softening resulting in the decreasing of phonon free energy at 3 and 10 GPa.

### 3.4 Electronic properties and chemical bonding

To investigate the electronic properties of  $\text{Na}_2\text{O}_2$  under high pressure, the PBE and HSE06 functionals were employed to calculate the electronic band structures and the partial density of states (PDOSs) for the ground state of the *Amm2*,  $\bar{P}62m$ ,  $P2_1/c$ , and *Pbam* structures (Fig. 9). The difference in the band structures of the *Amm2* and  $\bar{P}62m$  structures at the T/H points is around  $-0.5$  and  $-3.5$  eV, at the Y/K points is around  $-0.7$  and  $-4.5$  eV, and at the Z/H point is around  $-0.4$ ,  $-1.0$ ,  $-3.3$ , and  $-4.0$  eV (*Amm2*/ $\bar{P}62m$ ). Furthermore, the band structure of the *Amm2* and  $\bar{P}62m$  structures show indirect band gaps with the same value of 1.79 eV calculated by the PBE functional, while the band structure of the  $P2_1/c$  and *Pbam* structures suggest direct band gaps. Compared to the HSE06 band structure, the PBE band structure is similar. However, the HSE06 functional, which usually provides a more reliable band gap than the PBE functional, predicted that the band gap of the *Amm2* structure is higher than that of the  $\bar{P}62m$  structure by 2 meV. The PBE band gap of the  $\bar{P}62m$  structure is consistent with the previous study with the value of 1.76 eV.<sup>33</sup> At elevated pressure, the PBE and HSE06 band gaps of all structures have the same increasing trends (Fig. 10). However, the HSE06 band gap of the  $P2_1/c$

structure at 22 GPa is higher than that of the *Pbam* structure at about 13 meV, which suggests a difference between the structures.

As for the PDOSs of Na and O in the *Amm2*,  $\bar{P}62m$ ,  $P2_1/c$ , and *Pbam* structures (Fig. 9), they showed that the p-states of O mainly contribute to both the valence and conduction bands with small partial contributions from the p-states of Na, the s-states of Na, and a very small partial contribution from the s-states of O. Furthermore, the direct overlap of orbitals also suggests  $\sigma$  bonding of the O–O in these structures of  $\text{Na}_2\text{O}_2$ .

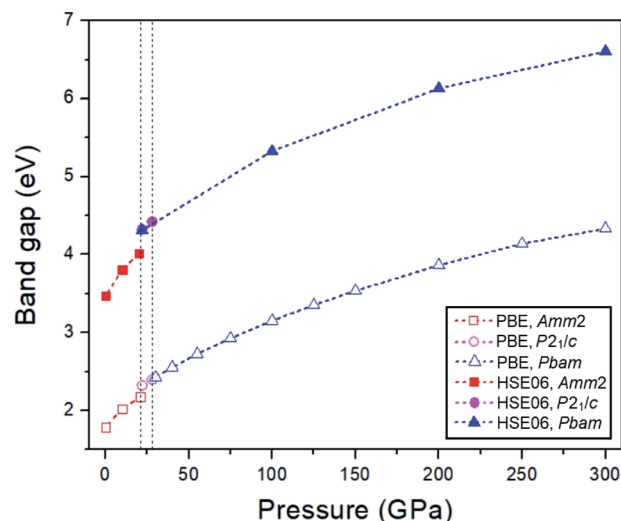


Fig. 10 The PBE and HSE06 band gaps versus pressure for the *Amm2*,  $P2_1/c$ , and *Pbam* structures.

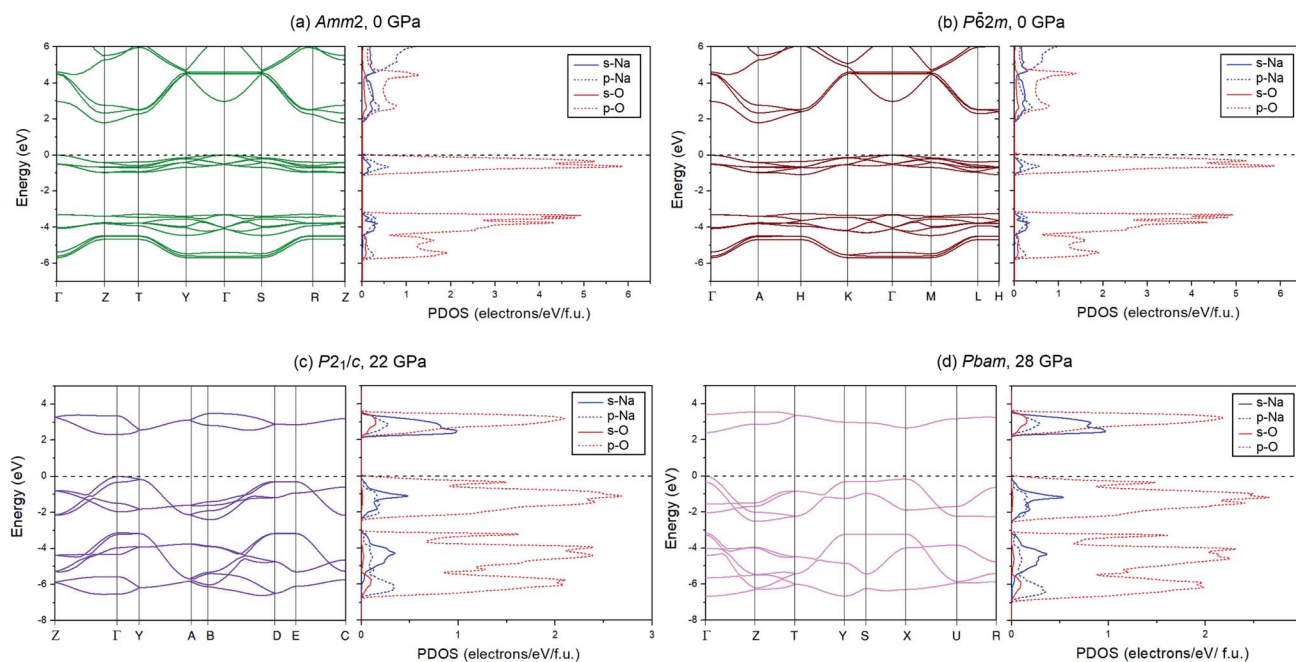


Fig. 9 Electronic band structures and their PDOSs for 4 structures at different pressures: (a) the *Amm2* structure at 0 GPa, (b) the  $\bar{P}62m$  structure at 0 GPa, (c) the  $P2_1/c$  structure at 22 GPa, and (d) the *Pbam* structure at 28 GPa.



To investigate the behavior of the O–O bonds in the *Amm2* structure of  $\text{Na}_2\text{O}_2$  at high pressures, we calculated their ELF in the pressure ranging from 0 to 21 GPa (Fig. 11). The findings predicted that the ELF has a decreasing trend with elevated pressure, which suggests the decreasing of shared electrons in the O–O bonds. Dramatically, however, the ELF turned to increase in the pressure ranges of 2–3 GPa and 9–10 GPa. The change at 3 GPa corresponds to the softening of elastic stiffness  $B_{11}$  and the softening of phonon frequencies of the acoustic modes at the Y point and the two-lowest frequencies of the optical modes at the  $\Gamma$  point as discussed before. Similarly, the change at 10 GPa significantly relates to the softening of phonon frequencies of the two acoustic modes at the Y point. However, the change of elastic stiffness  $B_{22}$  at 9 GPa has no correlation with the drastic increasing of the ELF at 10 GPa. Therefore, these suggest that the significantly elevated ELF at 3 and 10 GPa significantly relate to the softening of phonon frequencies of the acoustic mode and/or the optical modes at 3 and 10 GPa. Moreover, this leads to the stiffening of the O1–O1 and the O2–O2 bonds at 3 GPa as well. However, the unusual change of the O–O bond length at 10 GPa was not found, but there was a significant decrease of the cell angle,  $\gamma$ , of the primitive *Amm2* structure at 10 GPa (Fig. S9(d), ESI<sup>†</sup>). In addition, dramatic changes of ELF have also been predicted in the  $P6_3/mmc$  structure of  $\text{Li}_2\text{O}_2$  at 11 and 40 GPa.<sup>34</sup> It was predicted that there is some charge transfer between the O and Li atoms at these pressures. However, the charge transfer may also occur in the *Amm2* structure of  $\text{Na}_2\text{O}_2$ , but the marked change of the partial density of states of the Na and O atoms was not found in this work.

In addition, we also plotted the two-dimensional ELF for the *Amm2* structure at ambient pressure projected onto the (110) plane, the  $P2_1/c$  structure at 22 GPa projected onto the (200) plane, and the *Pbam* structure at 28 and 300 GPa projected onto the (001) plane (Fig. 12). The findings showed the shared electrons in the O–O bond and the p-orbital shape of the O–O,

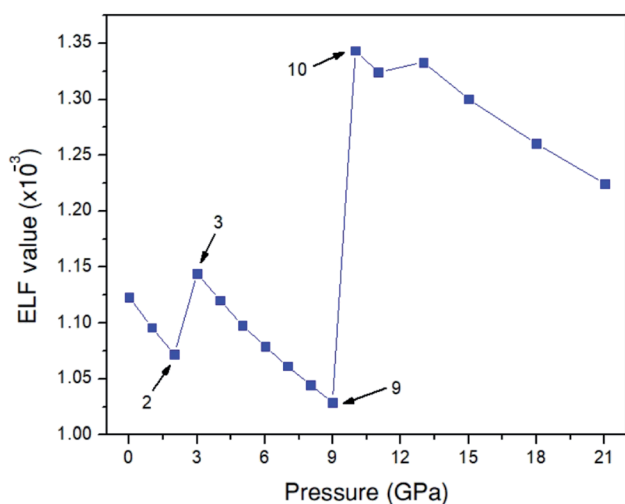


Fig. 11 Electron localization function (ELF) for the *Amm2* structure in the pressure range of 0–21 GPa.

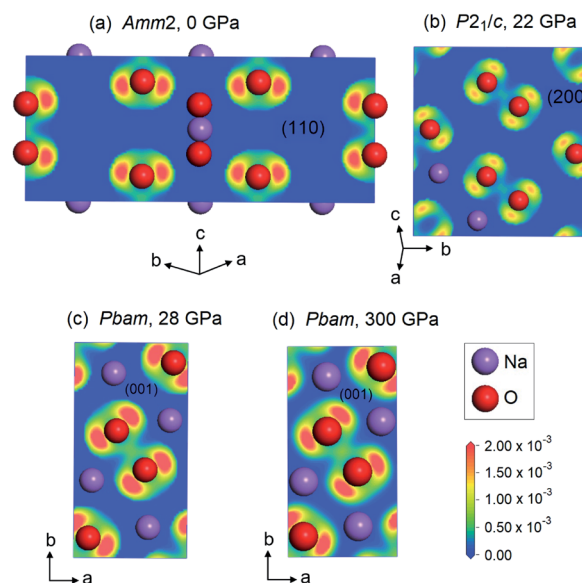


Fig. 12 Two-dimensional ELF for various structures of  $\text{Na}_2\text{O}_2$  at different pressures: (a) the *Amm2* structure at 0 GPa projected onto the (110) plane, (b) the  $P2_1/c$  structure at 22 GPa projected onto the (200) plane, and (c and d) the *Pbam* structure at 28 and 300 GPa projected onto the (001) plane.

which indicates that the O–O single bonds in these structures of  $\text{Na}_2\text{O}_2$  remain up to 300 GPa.

## 4 Conclusions

The present work used the DFT calculations and the QHA to predict the phase stabilities of  $\text{Na}_2\text{O}_2$  at high pressure up to 300 GPa and temperatures up to 600 K. The AIRSS searches were used to find the lowest enthalpy structure at 0 K, and the dynamical and thermodynamic stabilities of the lowest free energy structure candidates were estimated using the phonon dispersion and Gibbs free energy calculations, respectively. The findings revealed the two stable structures as the low-temperature phase of  $\text{Na}_2\text{O}_2$ . One is the *Amm2* (distorted  $P\bar{6}2m$ ) structure, which is dynamically and thermodynamically stable in the pressure range of 0–22 GPa at low temperature. However, the  $P\bar{6}2m$  structure becomes more thermodynamically stable than the *Amm2* structure at elevated temperatures. Furthermore, Tallman's structure is likely to be favored at higher temperature rather than Föppl's structure. The other is the  $P2_1/c$  structure, which is dynamically and thermodynamically stable in the pressure range of 22–28 GPa at extremely low temperature. Nevertheless, the *Pbam* structure becomes the favored structure instead of the  $P2_1/c$  structure at elevated temperatures. Moreover, the AIRSS searches also revealed the high-temperature phase candidates of  $\text{Na}_2\text{O}_2$ -II and  $\text{Na}_2\text{O}_2$ -Q, which are  $I4/mmm$  and *Immm* structures, respectively.

Interestingly, the findings suggest the softening of the elastic stiffnesses,  $B_{11}$ , at 3 GPa and  $B_{22}$ ,  $B_{44}$ , and  $B_{23}$  at 9 GPa, and the decreasing of the universal elastic anisotropy index at 3 GPa. At the Y point, there are three phonon acoustic modes and all



three soften at 3 GPa and two of them soften at 10 GPa. Similarly, at the  $\Gamma$  point, the two lowest phonon optical modes at 3 GPa also soften. This leads to the decreasing of phonon free energies and the increasing of the ELF at 3 and 10 GPa. Although the O–O bond lengths unusually decrease at 3 GPa, the unusual change of the O–O bond length is not found at 10 GPa, while a significant decrease of the cell angle,  $\gamma$ , of the primitive *Amm2* structure also appears. These suggest the mechanism for maintaining the stability of  $\text{Na}_2\text{O}_2$  at high pressures.

In addition, the PBE and HSE06 band gaps for the three phases of  $\text{Na}_2\text{O}_2$  increase with elevated pressure, whereas they have no sign of unusual change. This suggests that the softening of the elastic stiffnesses and the softening of the phonon frequencies in the *Amm2* structure have no significant effect on its band gap. Moreover, the ELFs reveal the existence of the peroxide group in  $\text{Na}_2\text{O}_2$  up to 300 GPa. Therefore, our findings provide the two stable structures at low temperature, the candidate structures for the high-temperature phases, the *P-T* phase diagram, and related properties of  $\text{Na}_2\text{O}_2$  at high pressures, which might be useful for investigating the thermodynamic stability of  $\text{Na}_2\text{O}_2$  in the Na–O<sub>2</sub> battery and the oxidizing efficiency of  $\text{Na}_2\text{O}_2$ .

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

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