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Bi₂Te₃ single crystals with high room-temperature thermoelectric performance enhanced by manipulating point defects based on first-principles calculation†

Chunmei Tang,^a Zhicheng Huang,^a Jun Pei,^a Bo-Ping Zhang,^a  [✉] Peng-Peng Shang,^b Zhihang Shan,^a Zhiyue Zhang,^a Haiyun Gu^a and Kaibin Wen^a

Intrinsic Bi₂Te₃ is a representative thermoelectric (TE) material with high performance at low temperature, which enables applications for electronic cooling. However, antisite defects easily form in p-type Bi₂Te₃, resulting in the difficulty of further property enhancement. In this work, the formation energy of native point defects in Bi₂Te₃ supercells and the electronic structure of Bi₂Te₃ primitive unit cell were calculated using first-principles. The antisite defect Bi₁Te₁ has a lower formation energy (0.68 eV) under the Te-lack condition for p-type Bi₂Te₃. The effects of point defects on TE properties were investigated via a series of p-type Bi₂Te_{3-x} ($x = 0, 0.02, 0.04, 0.06, 0.08$) single crystals prepared by the temperature gradient growth method (TGGM). Apart from the increased power factor ($PF_{||}$) which originates from the increased carrier concentration ($n_{||}$) and m^* , the thermal conductivity ($\kappa_{||}$) was also cut down by the increased point defects. Benefitting from the high $PF_{||}$ of 4.09 mW m⁻¹ K⁻² and the low $\kappa_{||}$ of 1.77 W m⁻¹ K⁻¹, the highest $ZT_{||}$ of 0.70 was obtained for $x = 0.06$ composition at 300 K, which is 30% higher than that (0.54) of the intrinsic Bi₂Te₃.

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1. Introduction

Thermoelectric (TE) materials have been investigated for use in power generation and semiconductor refrigeration based on the Seebeck and Peltier effects for decades, and are considered as a promising candidate to remit the energy shortages and environmental issues.^{1–3} However, the poor properties and conversion efficiencies of TE materials limit their applications on a world-wide scale. The conversion efficiencies of TE materials are determined by the dimensionless figure of merit, $ZT = \alpha^2 \sigma T / \kappa$, where α , σ , T and κ are the Seebeck coefficient, the electrical conductivity, the absolute temperature and the thermal conductivity, respectively.^{4,5} A high ZT value requires a high power factor ($PF = \alpha^2 \sigma$) and a low κ . Research aimed at increasing PF values in recent decades is focused on optimizing and stabilizing the carrier concentration (n),^{6,7} engineering distortions of the electronic density of states near the Fermi energy (resonant levels)^{8,9} and achieving band convergence.^{10–12} The κ value can be significantly reduced by introducing point defects, dislocations and nanostructures.^{13–15}

Intrinsic Bi₂Te₃ is a representative TE material with high performance at low temperature, which enables applications for electronic cooling.^{16,17} Bi₂Te₃ with a space group of $R\bar{3}m$ shows a lamella structure which consists of a five atomic layer in the order of Te₁–Bi–Te₂–Bi–Te₁ along the c axis as shown in Fig. S1a.† The Bi₂Te₃ unit cell contains one type of Bi site (0.0000, 0.0000, 0.4000) and two types of Te sites (Te₁ (0.0000, 0.0000, 0.2095) and Te₂ (0.0000, 0.0000, 0.0000)).^{18,19} The intra-layer bonds of Bi₂Te₃ are covalent while the interlayer bonds are the van der Waals interaction force and hybrids of the electrostatic interaction.²⁰ The first work of Bi₂Te₃ as a TE material for refrigeration was reported in 1954 by Goldsmid.²¹ In the last decades, the TE properties of Bi₂Te₃ polycrystals were enhanced by point defects,^{22–24} textures^{25–27} and dislocation arrays²⁸ and further optimized by alloying with isostructural Sb₂Te₃ (ref. 9–31) or Bi₂Se₃.^{22,32} The ZT of Bi_{0.5}Sb_{1.5}Te₃ was dramatically increased to 1.86 at 320 K via full-spectrum phonon scattering which has a minimal charge-carrier scattering.²⁸ In fact, producing point defects is convenient and effective to develop high-performance TE materials, which can simultaneously optimize the electrical transport properties and lattice thermal conductivity. However, the enhancement of TE performance via manipulating point defects in polycrystals is hard to understand rather than in single crystals. Preparations of Bi₂Te₃-based single crystals are usually achieved by the Bridgman^{33–35} and Zone Melting (ZM)^{36–38} methods, which need to move or rotate the crystal growth device and supply an inert atmosphere.

^aThe Beijing Municipal Key Laboratory of New Energy Materials and Technologies, School of Materials Science and Engineering, University of Science and Technology Beijing, Beijing 100083, China. E-mail: bpzhang@ustb.edu.cn

^bDepartment of Chemistry and Material Science, Shandong Agricultural University, 61 Daizong Road, Tai'an, Shandong 271018, China

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A simple and convenient temperature gradient growth method (TGGM) only needs a vertical furnace compared with Bridgman and ZM, which has been provided to prepare high-performance SnSe single crystal as described by Duong *et al.*³⁹ And the preparation of Bi₂Te₃ single crystal by TGGM was only reported in Mn-doped⁴⁰ and Cu-doped⁴¹ Bi₂Te₃, but didn't detailedly investigate the TE properties of Bi₂Te₃. This motivates us to prepare Bi₂Te₃-based single crystals by TGGM method and investigate the effects of native point defects on TE properties.

In this work, we expect to prepare Bi₂Te₃ single crystals by TGGM method and enhance the TE properties of Bi₂Te₃ *via* combining an optimized carrier concentration with a reduced thermal conductivity. A series of p-type Bi₂Te_{3-x} ($x = 0, 0.02, 0.04, 0.06, 0.08$) single crystals were successfully prepared by applying TGGM. The phase structure, microstructures, and TE transport properties of Bi₂Te_{3-x} ($x = 0, 0.02, 0.04, 0.06, 0.08$) single crystals were investigated carefully. The electrical transport properties calculated by BoltzTraP2,⁴² and the electronic structure and the formation energy were associated to well understand the variation of TE properties for Bi₂Te₃ single crystals. The carrier concentration of in-plane ($n_{||}$) was significantly improved by adjusting the amount of Te. Owing to the increase of PF_{||} (power factor of in-plane) and the reduction of $\kappa_{||}$ (thermal conductivity of in-plane), a significantly enhanced ZT_{||} (ZT of in-plane) was achieved.

2. Method

2.1 Computational details

A plane-wave pseudopotential method in the Vienna *ab initio* Simulation Package (VASP) was used to achieve the density functional theory (DFT) calculations.^{43,44} The exchange and correlation function was described *via* Perdew–Burke–Ernzerhof generalized gradient approximation (GGA-PBE).⁴⁵ The projector augmented wave (PAW) potentials were applied to describe the interaction between electrons and ions.⁴⁶ The DFT-D3 method with Becke–Jonson damping implemented in the VASP code was used to describe the van der Waals interaction within the PBE function.^{47,48} By considering van der Waals forces and spin–orbit coupling (SOC), the electronic structure of Bi₂Te₃ primitive unit cell (Fig. S1c†) was calculated along the special lines connecting the high-symmetry points P (0.822852, 0.338574, 0.338574), a (0.661426, 0.419287, 0.419287), Γ (0, 0, 0), Z (0.5, 0.5, 0.5), Γ (0, 0, 0), L (0.5, 0.5, 0) according to the report of Brillouin zone by Setyawan *et al.*⁴⁹ as shown in Fig. S1b.† The inertial effective masses m_{xx}^* , m_{yy}^* and m_{zz}^* of holes along different principal axes were calculated as defined in eqn (1):^{50,51}

$$\frac{1}{m_{ij}^*} = \frac{1}{\hbar^2} \frac{\partial^2 E_n(\mathbf{k})}{\partial k_i \partial k_j}, i, j = x, y, z \quad (1)$$

here, \hbar is the reduced Planck constant, x, y, z represent the directions in the reciprocal Cartesian space, $E_n(\mathbf{k})$ is the dispersion relation for the n -th electronic band.

The calculation of formation energy was performed with a plane-wave cutoff of 500 eV and a $5 \times 5 \times 5$ Monkhorst–Pack

k -mesh basing on the $2 \times 2 \times 2$ perfect and defective Bi₂Te₃ supercells. The defective supercells contain vacancies on the Bi (V_Bi), Te₁ (V_Te₁) and Te₂ (V_Te₂) sublattices and antisite defects on Te₁ (Bi_Te₁), Te₂ (Bi_Te₂) and Bi (Te_Bi) sublattices. The total energy converged to 1.0×10^{-4} eV and the Hellman–Feynman force was smaller than -1.0×10^{-2} eV Å⁻¹ in the optimized structures. The crystal of Bi₂Te₃ obtained from the Inorganic Crystal Structure Database (ICSD) (*R3mH*, $a = b = 4.39$ Å and $c = 30.50$ Å) was taken as initial geometry. The formation energy (ΔE_F) of Bi₂Te₃ with a native point defect (D) can be calculated as defined in eqn (2):^{52–55}

$$\Delta E_F = E_D - E_{\text{bulk}} - \sum_i n_i \mu_i + q E_f \quad (2)$$

where E_D and E_{bulk} are the total energy of the defective supercell containing the defect D and the perfect supercell, respectively; n_i is the number of change for i type atom such as Bi or Te and n_i should be >0 or <0 when i type atom is added or removed from the supercell; μ_i represents the corresponding chemical potential of the i type atom; q is the charge of the defect and E_f is the Fermi level. In this work, the variation of $q E_f$ is ignored. The rhombohedral phase of Bi and the trigonal phase of Te were used as the reference elemental bulk phases for the chemical potentials.

2.2 Sample preparation

Commercial powders of Bi (99.99%) and Te (99.999%) were weighed according to the chemical formula of Bi₂Te_{3-x} ($x = 0, 0.02, 0.04, 0.06, 0.08$). The powders were mixed manually for 30 minutes under an agate mortar using pestle and pressed into disks. The disks were loaded into quartz ampoules and flame-sealed at a pressure of $2-3 \times 10^{-3}$ Pa. Another bigger quartz ampoule was sealed to prevent the inner ampoule from breaking during sintering. The quartz ampoules were slowly heated (10 K h^{-1}) up to 913 K and soaked for 30 h at 913 K. Finally, the quartz ampoules were slowly cooled (1 K h^{-1}) to 733 K and then to room temperature by furnace cooling. The schematic diagram of the preparation process for Bi₂Te_{3-x} single crystals by the TGGM is shown in Fig. S2.†

2.3 Characterization

The X-ray diffraction (XRD, SmartLab, Japan) with Cu K α radiation was used to identify the phase structure. The observation of morphology for the single crystals was achieved *via* a field emission scanning electron microscope (FESEM, SUPRA™ 55, Germany). The transmission electron microscopy (TEM), high-resolution (HRTEM) images and the selected area electron diffraction (SAED) pattern were obtained by a transmission electron microscope (JEOL 2100F, Japan). The obtained single crystal was cut into bar-shaped samples with dimensions *ca.* 7.00 mm \times 2.20 mm \times 2.20 mm for electronic property measurements and square planar samples *ca.* 6.00 mm \times 6.00 mm \times 1.10 mm for the measurements of thermal diffusivity along different directions (out-plane, in-plane). The electrical conductivity (σ) and Seebeck coefficient (α) were measured in a helium atmosphere as increasing temperature from 300 K



to 573 K via a Seebeck coefficient/electric resistance measuring system (Cryoall CTA-3, China). A Hall measurement system (ResiTest 8340DC, Tokyo, Japan) was applied to measure the Hall coefficient (R_H). According to $n = 1/(eR_H)$ and $\mu = R_H/\rho$, the carrier concentration (n) and mobility (μ) were computed. The laser flash method (Netzsch LFA457, Germany) was applied to measure the thermal diffusivity (D). The specific heat C_p was estimated according to the Dulong–Petit limit. The Archimedes method was used to estimate the mass density (d). The total thermal conductivity (κ) was computed using $\kappa = DC_p d$. All physical quantities of in-plane and out-plane were indicated by subscripts of \parallel and \perp to represent parallel and perpendicular to cleavage plane, respectively.

3. Results and discussion

3.1 Electronic structure calculation

Fig. 1 shows the band structure, total density of state (TDOS) and projected density of state (PDOS) for the intrinsic Bi_2Te_3 . The valence band maxima (VBM) for Bi_2Te_3 is located at (0.51, 0.32, 0.32) along the $a \rightarrow \Gamma$ direction, while the conduction band minima (CBM) is located at (0.50, 0.50, 0.38) along the $Z \rightarrow \Gamma$ direction as shown in Fig. 1a. Bi_2Te_3 has a strong spin-orbit coupling (SOC) near the Fermi level due to the presence of the Bi 6p states, which can produce a low band gap (E_g).^{56,57} Herein, the calculated E_g 0.08 eV of Bi_2Te_3 is lower than the band gap obtained from experiments (0.13–0.16 eV),^{58,59} but it is well consistent with the literature calculated data (0.05–0.09 eV).^{57,60,61} The band structure is very similar to the early reports.^{62–64} The inertial effective masses m_{xx}^* , m_{yy}^* and m_{zz}^* of holes along the different principal axes were calculated to be

0.31 m_0 , 0.04 m_0 and 0.04 m_0 , respectively, indicating that the TE properties of p- Bi_2Te_3 may be anisotropic.

The valence electrons of Bi and Te are treated explicitly as 15 ($5d^{10}6s^26p^3$) and 6 ($5s^25p^4$), respectively. As shown in Fig. 1c, Bi atoms play a dominant role to the PDOS near the CBM, indicating that Bi atoms will lose electrons and compose the conduction bands. On the other hand, Te_1 and Te_2 atoms contribute most to the PDOS near the VBM, which indicates that Te atoms will receive electrons and compose the valence bands.⁶⁵ Fig. 1d shows that only the 6p orbitals of Bi atoms predominate near the CBM, while the Bi-6s and Bi-6p orbitals have a strong combined contribution near the VBM. Te_1 -5p and Te_2 -5p orbitals predominate both in the CBM and VBM as shown in Fig. 1e and f.

Fig. 2 shows the chemical potential dependence of electrical transport properties for Bi_2Te_3 along the in-plane and out-plane, which is simply evaluated by the BoltzTraP2. The chemical potential ($\mu - \mu_0$) represents the doping level near the Fermi energy and τ is the relax time. $(\sigma/\tau)_{\parallel}$ of both p-type and n-type Bi_2Te_3 at 300 K is higher than that of $(\sigma/\tau)_{\perp}$ when the doping level is low as shown in the inset of Fig. 2a, which means the σ is anisotropic.⁶⁶ However, the curves of α_{\parallel} and α_{\perp} are similar in Fig. 2b, indicating the isotropy of α . Due to the higher $(\sigma/\tau)_{\parallel}$, the power factor $(\alpha^2\sigma/\tau)_{\parallel}$ in Fig. 2c is higher than $(\alpha^2\sigma/\tau)_{\perp}$ when the doping level is low, which is coincided with the experiment data in Fig. 5 and S4.† What's more, the electrical transport properties of p-type Bi_2Te_3 are superior to that of n-type Bi_2Te_3 according to Fig. 2c.⁶²

3.2 Formation energy calculation

Formation energy (ΔE_F) of native point defects V_{Bi} , V_{Te_1} , V_{Te_2} , Bi_{Te_1} , Bi_{Te_2} and Te_{Bi} in Bi_2Te_3 for Te-lack condition

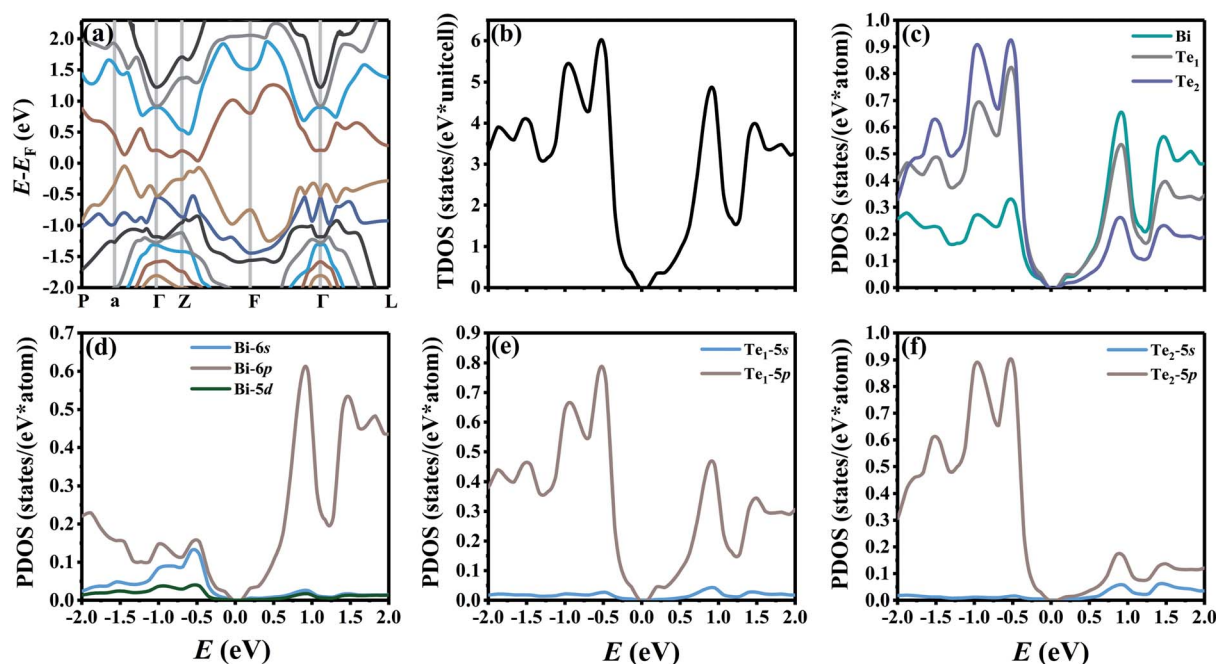


Fig. 1 (a) The band structure along the high-symmetry points P-a- Γ -Z-F- Γ -L, (b) the total density of state (TDOS), and (c-f) projected density of state (PDOS) for the intrinsic Bi_2Te_3 .



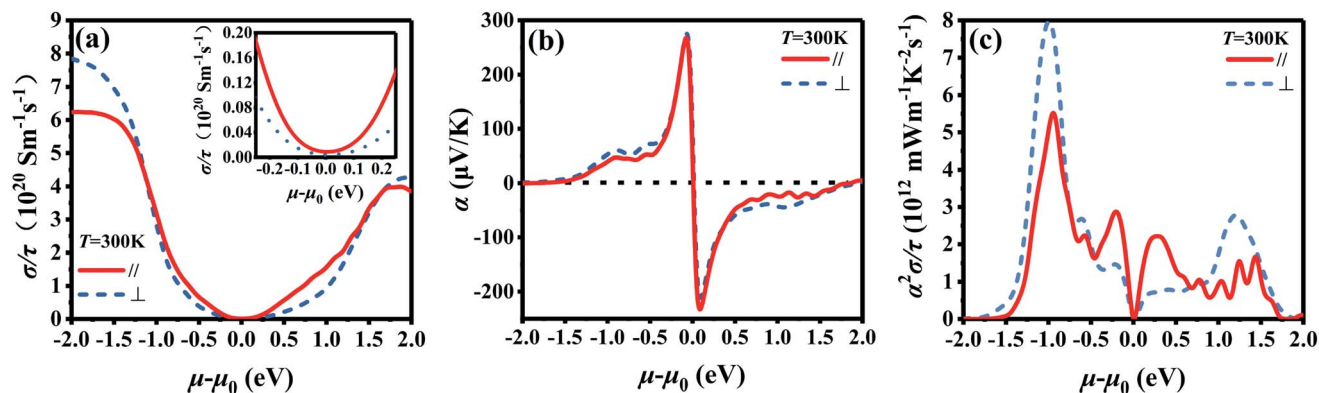


Fig. 2 Chemical potential dependence of (a) electrical conductivity/relax time (σ/τ) calculated by BoltzTraP2, (b) Seebeck coefficient (α), and (c) power factor/relax time ($\alpha^2\sigma/\tau$) for the intrinsic Bi_2Te_3 along the in-plane (\parallel) and out-plane (\perp) at 300 K.

is listed in Table 1, which is 2.48, 1.20, 1.51, 0.68, 1.14 and 1.54 eV, respectively. The calculated ΔE_F indicates that the antisite defect Bi_{Te_1} is the easiest to form and will play a dominant role in Bi_2Te_3 under the Te-lack condition. However, for the Bi-lack condition, ΔE_F of native point defects V_{Bi} , V_{Te_1} , V_{Te_2} , Bi_{Te_1} , Bi_{Te_2} and Te_{Bi} in Bi_2Te_3 is 2.00, 1.52, 1.83, 1.48, 1.94 and 0.75 eV, respectively, implying that Te_{Bi} will predominate in Bi_2Te_3 under the Bi-lack condition.⁶⁷

The lattice constants and unit cell volumes obtained from the optimized structures are listed in Table 2. The lattice constants ($a = b$, c) and unit cell volume ($a \times b \times \sin \gamma \times c$) of the Bi_2Te_3 are 4.39 Å, 30.34 Å and 505.30 Å³, respectively. The reduction of a and c results in smaller unit cell volumes of defective Bi_2Te_3 with V_{Bi} , V_{Te_1} , V_{Te_2} , Bi_{Te_1} and Bi_{Te_2} , which are 490.22, 497.66, 497.17, 503.35 and 502.89 Å³ respectively. It is worth to note that the lack of Bi can generate a significant variation in unit cell volume, while the changes of volumes from the antisite defects are relatively small. However, the a of Bi_2Te_3 with the defect Te_{Bi} is increased along with a decreased c , which has a unit cell volume of 501.80 Å³. The Fermi level relative to the reference level defined in the pseudopotentials is 6.39 eV for Bi_2Te_3 and decreases to 6.02, 6.15 and 6.18 eV for Bi_2Te_3 containing the defects of V_{Bi} , Bi_{Te_1} and Bi_{Te_2} , respectively, implying that V_{Bi} , Bi_{Te_1} and Bi_{Te_2} would act as p-type dopants. On the contrary, the Fermi level of Bi_2Te_3 with the defects of V_{Te_2} and Te_{Bi} turns into 6.46 and 6.81 eV, respectively, which indicates V_{Te_2} and Te_{Bi} would act as n-type dopants. Although the Fermi level 6.31 eV of V_{Te_1} is slightly lower than that (6.39 eV) of Bi_2Te_3 , V_{Te_1} should also be

a n-type dopant. The reason for this result may be that the band structures of defective and perfect supercells were not lined up.

3.3 Microstructure and phase characterizations

Fig. 3 shows the typical TEM and high-resolution TEM (HRTEM) images of $x = 0$ bulk. The TEM image without obvious grain boundary in a large scale is shown in Fig. 3a. The selected area electron diffraction (SAED) pattern of $x = 0$ bulk in the inset of Fig. 3a shows a clear lattice structure, which indicates the good crystallization of the bulk. The lattice spacings of 0.2228 and 0.2167 nm in the HRTEM image as shown in Fig. 3b correspond to (01 $\bar{1}$ 1) and (11 $\bar{2}$ 0) planes of Bi_2Te_3 , respectively.

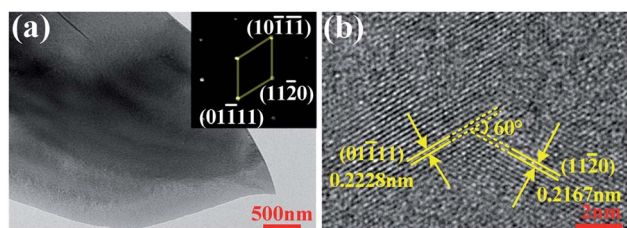
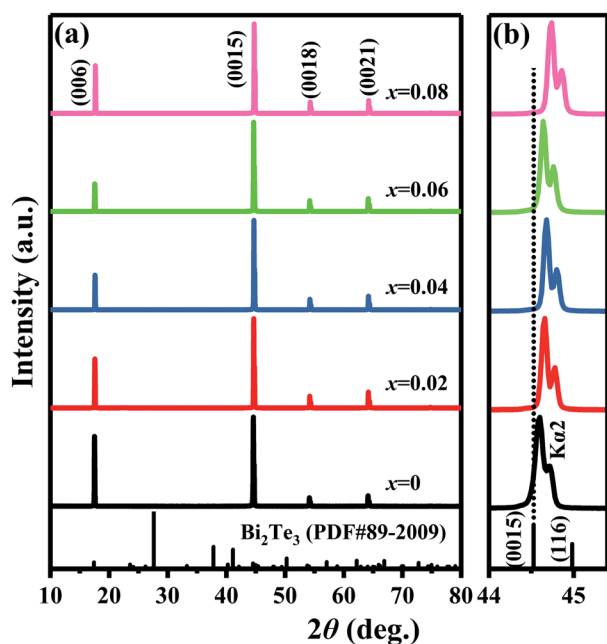
Fig. 4 shows the XRD patterns of cleavage planes for $\text{Bi}_2\text{Te}_{3-x}$ ($x = 0, 0.02, 0.04, 0.06, 0.08$) single crystals. Only (00 l) diffraction peaks can be observed in all the XRD patterns, indicating that the $\text{Bi}_2\text{Te}_{3-x}$ single crystal whose crystallographic c axis is perpendicular to the cleavage plane were synthesized. The field emission scanning electron microscope (FESEM) images in Fig. S3† exhibit a layered micro-structure with an average thickness about 1 μm, and the energy dispersive spectrometer (EDS) mapping indicates that compositional distribution of Bi and Te is very uniform for $x = 0$ single crystal with an atomic ratio of Bi : Te = 59.69 : 40.31. In order to analyse the variation of lattice constants and point defects, the rhombohedral Bi_2Te_3 ($R\bar{3}m$, PDF#89–2009) was chosen as a reference. To analyse the influences of insufficient Te on the lattice variation of the host Bi_2Te_3 phase, the 2θ angle of the strongest diffraction peak (0015) (abbreviated as $2\theta_{(0015)}$) is highlighted in Fig. 4b. The

Table 1 Formation energy of native point defects in Bi_2Te_3 under Te-lack and Bi-lack conditions calculated using DFT

| Native point defects in Bi_2Te_3 | Total energy of Bi_2Te_3 (E_{bulk}), eV | Chemical potential of Bi (μ_{Bi}), eV | Chemical potential of Te (μ_{Te}), eV | Native point defects in Bi_2Te_3 | | | | | |
|--|--|--|--|--|--------------------------|--------------------------|---------------------------|---------------------------|-------------------------|
| | | | | V_{Bi} | V_{Te_1} | V_{Te_2} | Bi_{Te_1} | Bi_{Te_2} | Te_{Bi} |
| Total energy, (E_{D}), eV | −149.07 | −4.05 | −3.14 | −142.46 | −144.41 | −144.10 | −149.05 | −148.59 | −146.86 |
| Formation energy (ΔE_F), (eV) | | | | | | | | | |
| Te-lack | — | −4.13 | −3.46 | 2.48 | 1.20 | 1.51 | 0.68 | 1.14 | 1.54 |
| Bi-lack | — | −4.60 | −3.14 | 2.00 | 1.52 | 1.83 | 1.48 | 1.94 | 0.75 |

Table 2 Lattice constants and the Fermi level of defective Bi₂Te₃ calculated using DFT

| Point defect | <i>a</i> = <i>b</i> (Å) | <i>c</i> (Å) | $\alpha = \beta$ (°) | γ (°) | Unit cell volume (Å ³) | Fermi level (eV) |
|---------------------------------|-------------------------|--------------|----------------------|--------------|------------------------------------|------------------|
| Bi ₂ Te ₃ | 4.39 | 30.34 | 90 | 120 | 505.30 | 6.39 |
| V _{Bi} | 4.34 | 30.00 | | | 490.22 | 6.02 |
| V _{Te} ₁ | 4.36 | 30.22 | | | 497.66 | 6.31 |
| V _{Te} ₂ | 4.37 | 30.03 | | | 497.17 | 6.46 |
| Bi _{Te} ₁ | 4.38 | 30.32 | | | 503.35 | 6.15 |
| Bi _{Te} ₂ | 4.38 | 30.27 | | | 502.89 | 6.18 |
| Te _{Bi} | 4.40 | 29.89 | | | 501.80 | 6.81 |

Fig. 3 (a) TEM image and the SAED pattern and (b) HRTEM image for the *x* = 0 bulk.Fig. 4 XRD patterns of cleavage planes for Bi₂Te_{3-x} (*x* = 0, 0.02, 0.04, 0.06, 0.08) single crystal at (a) 10–80° and (b) 44–45.4°.

shoulder peak next to (0015) diffraction peak comes from the diffraction of Cu K α 2 line.⁶⁸ The $2\theta_{(0015)}$, interplanar spacing of the strongest diffraction peak (0015) (abbreviated as $d_{(0015)}$) and lattice constant of *c* axis are shown in Table 3. The $2\theta_{(0015)}$ shifts from 44.60° to 44.68° when *x* increases from 0 to 0.04 and is higher than that (44.53°) of the standard card (Bi₂Te₃, PDF#89–2009), which corresponds to the decrease of lattice constant *c* from 30.45 Å to 30.40 Å. The $2\theta_{(0015)}$ decreases to 44.64° at *x* = 0.06, which has a trend of returning to 44.53° of the standard card, but turns to higher angle (44.74°) by further increasing *x* to

0.08. At the same time, the lattice constant *c* increases to 30.42 Å at *x* = 0.06, then reduces to 30.36 Å at *x* = 0.08.

The native point defects in the intrinsic p-type Bi₂Te₃ include V_{Bi}, V_{Te} and Bi_{Te},^{23,24} which can be described as eqn (3)–(5), where *y* and *z* are the content of volatilization for Bi and Te during the sintering process. According to Table 2 and eqn (3), the volatilization of Bi can produce negatively charged vacancy V_{Bi}^{'''} and extra holes (h⁺), causing a large decrement of lattice constants for Bi₂Te₃. The volatilization of Te can generate positively charged vacancy V_{Te}^{''} and extra electrons (e[−]) as described in eqn (4). The formation of V_{Te}^{''} is easier than V_{Bi}^{'''} during the sintering process because of the lower energy of evaporation for Te (52.55 kJ mol^{−1}) compared with Bi (104.80 kJ mol^{−1}). So, eqn (4) plays a dominant role, which is coincided quite well with the calculation of formation energy in Table 1. However, the close electronegativity between Bi (2.02) and Te (2.01) makes it easy for Bi to jump to the Te-sites, forming antisite defects along with h⁺ generated as shown in eqn (5). What's more, V_{Bi}^{'''} and V_{Te}^{''} can cancel each other out with a ratio of 2 : 3, as described in eqn (5).

Hence, the increased $2\theta_{(0015)}$ at $0 \leq x \leq 0.04$ is attributed to the substitution of Te^{2−} (*r* = 2.21 Å) by Bi³⁺ (*r* = 0.96 Å) which can shrink the lattice of Bi₂Te₃ as shown in Tables 2 and 3 and increase the h⁺ concentration as shown in Fig. 6a. When *x* = 0.06, eqn (5) still plays a dominant role in Bi₂Te₃ and increases $n_{||}$. However, a small amount of Bi may fill into V_{Bi}^{'''} and fix h⁺ as described in eqn (6) and enlarge the lattice of Bi₂Te₃ as shown in Fig. 4b. With the further lack of Te, the effect of eqn (5) is enhanced while the function of eqn (6) is limited, resulting in the shrinkage of Bi₂Te₃ lattice in Fig. 4b and the enhancement of $n_{||}$ in Fig. 6a. According to the above analysis, the point defect Bi_{Te} plays a dominant role in all Bi₂Te₃ bulks and leads to the decrease of lattice constant *c* as shown in Table 3, which is corresponding to the reduction of lattice constant *c* from DFT calculation as shown in Table 2.

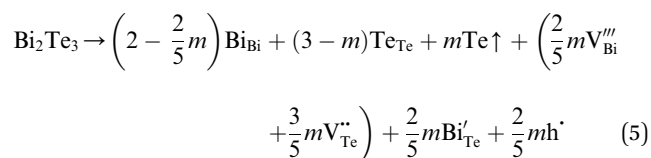
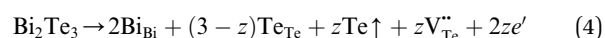
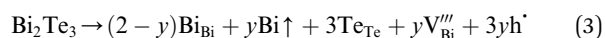
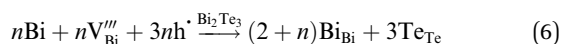


Table 3 The 2θ angle ($2\theta_{(0015)}$), the interplanar spacing ($d_{(0015)}$) of the strongest diffraction peak (0015) and lattice constant c for $\text{Bi}_2\text{Te}_{3-x}$ ($x = 0, 0.02, 0.04, 0.06, 0.08$) samples

| Sample | PDF#89-2009 | $x = 0$ | $x = 0.02$ | $x = 0.04$ | $x = 0.06$ | $x = 0.08$ |
|---------------------------------|-------------|---------|------------|------------|------------|------------|
| $2\theta_{(0015)}$ ($^\circ$) | 44.53 | 44.60 | 44.66 | 44.68 | 44.64 | 44.74 |
| $d_{(0015)}$ (\AA) | 2.0331 | 2.0300 | 2.0275 | 2.0265 | 2.0281 | 2.0240 |
| c (\AA) | 30.50 | 30.45 | 30.41 | 30.40 | 30.42 | 30.36 |



3.4 TE transport properties

Fig. 5 shows the TE transport properties of $x = 0$ bulk along the in-plane and out-plane. σ_{\parallel} of $x = 0$ in Fig. 5a decreases from $3.87 \times 10^4 \text{ S m}^{-1}$ (300 K) to $3.38 \times 10^4 \text{ S m}^{-1}$ (342 K), and then increases to $7.02 \times 10^4 \text{ S m}^{-1}$ (573 K) in the whole measured temperature ranging from 300 K to 573 K. σ_{\perp} has the same variation with σ_{\parallel} . The lower σ_{\perp} compared to σ_{\parallel} is attributed to a lower carrier mobility (μ_{\perp}) for the interlayer direction. α_{\parallel} and α_{\perp} in Fig. 5b decrease with an increase of temperature. α_{\parallel} changes from positive to negative between 400 K and 500 K, meaning the transformation of p-type to n-type semiconductor, while α_{\perp} is positive in the whole measured temperature. The anisotropy of α may be attributed to the ratio of the mobility of holes to the mobility of electrons is different along the in-plane

and out-plane, which is also reported by Situmorang⁶⁹ and Dennis.⁷⁰ A highest PF_{\parallel} $3.37 \text{ mW m}^{-1} \text{ K}^{-2}$ is obtained at 300 K as shown in Fig. S4a.† The anisotropy of TE properties for Bi_2Te_3 corresponds well with the calculation results in Fig. 2.

As shown in Fig. 5c, κ_{\parallel} and κ_{\perp} at 300 K are 1.88 and $0.98 \text{ W m}^{-1} \text{ K}^{-1}$, respectively. The solid points in Fig. 5c indicate that the sum of lattice thermal conductivity (κ_{lat}) and bipolar thermal conductivity (κ_{bip}) makes a significant contribution to the total κ . Owing to the dominance of electrical properties rather than the thermal properties, a highest ZT_{\parallel} 0.54 is obtained at 300 K as shown in Fig. 5d. The unsatisfactory ZT mainly attributes to the low σ deriving from the inferior n , and also a high κ . Therefore, further research on optimizing of n by increasing antisite defects was conducted through adjusting the Te content, which is a simple and effective approach. On the other hand, the increased point defects can enhance the scattering of phonons and reduce κ . A higher TE performance is expected to obtain by simply adjusting the amount of Te.

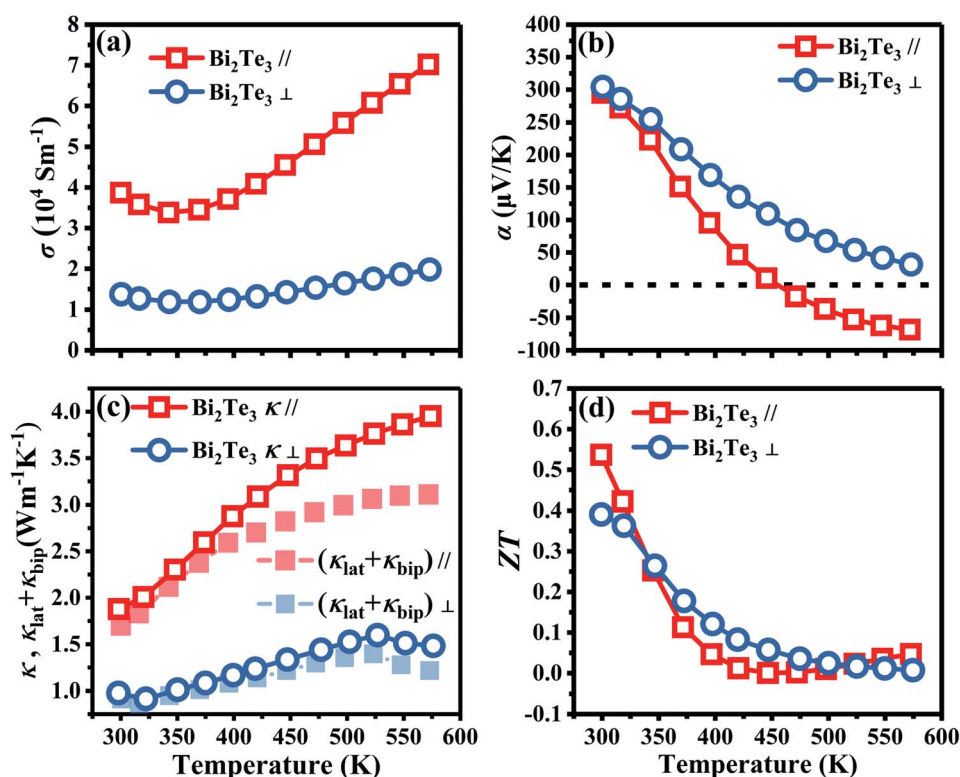


Fig. 5 Temperature dependence of TE properties along the in-plane (\parallel) and out-plane (\perp) for $x = 0$ bulk. (a) Electrical conductivity (σ), (b) Seebeck coefficient (α), (c) total thermal conductivity (κ) and the sum of lattice thermal conductivity and bipolar thermal conductivity ($\kappa_{\text{lat}} + \kappa_{\text{bip}}$), and (d) figure of merit (ZT).



Hereafter, a series of p-type $\text{Bi}_2\text{Te}_{3-x}$ ($x = 0, 0.02, 0.04, 0.06, 0.08$) bulks were prepared by TGGM and the TE transport properties of in-plane with a subscript of \parallel will be discussed.

Fig. 6 shows the electrical transport properties for $\text{Bi}_2\text{Te}_{3-x}$ ($x = 0, 0.02, 0.04, 0.06, 0.08$) single crystals along the in-plane. The n_{\parallel} and μ_{\parallel} in Fig. 6a show an inverse variation. The n_{\parallel} of $x = 0$ bulk is $8.01 \times 10^{18} \text{ cm}^{-3}$ and slowly increases to $8.89 \times 10^{18} \text{ cm}^{-3}$ ($x = 0.02$) and $9.68 \times 10^{18} \text{ cm}^{-3}$ ($x = 0.04$). When the amount of Te is further reduced, the n_{\parallel} is significantly enhanced to $1.36 \times 10^{19} \text{ cm}^{-3}$ ($x = 0.06$) and $1.73 \times 10^{19} \text{ cm}^{-3}$ ($x = 0.08$). The μ_{\parallel} is *ca.* $294.32\text{--}312.53 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ at $0 \leq x \leq 0.04$ and decreases to $259.40 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ($x = 0.06$) and $183.28 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ($x = 0.08$). The reduction of μ_{\parallel} may be caused by the change of effective masses (m^*) as expressed in eqn (7):²

$$\mu = \frac{e\tau}{m^*} \quad (7)$$

where e is the electron charge and τ is the carrier scattering time. Eqn (7) indicates that an enhanced m^* will result in a reduced μ . What's more, m^* can be simply estimated by the Pisarenko relationship between α and n based on the single parabolic band (SPB) model according to eqn (8):⁷¹

$$\alpha = \frac{8\pi^2 k_B^2}{3eh^2} \left(\frac{\pi}{3n}\right)^{2/3} m^* T \quad (8)$$

where k_B is the Boltzmann constant and h is the Planck constant. On the basis of eqn (8), the α is proportional to m^* and inversely to n . As shown in Fig. 6b, the theoretical Pisarenko curve with m^* of $1.29 m_0$ and the experimental data at room

temperature are depicted by the gray line and marks, respectively. The experimental data at $0 \leq x \leq 0.04$ agree every well with the theoretical Pisarenko curve and follow a SPB behavior. The reduced α_{\parallel} of $0 \leq x \leq 0.06$ bulks in Fig. 6b at 300 K is dominated by the significantly increased n_{\parallel} rather than the varied m^* ($x = 0.06$). Although the n_{\parallel} is enhanced at $x = 0.08$, the α_{\parallel} holds a similar value with $x = 0.06$ due to the further increased m^* . According to PDOS in Fig. 1e and f, Te atoms contribute most near the VBM and the large lack of Te ($0.06 \leq x \leq 0.08$) in this work may play as a dopant and cause the change of band structure which could increase m^* . The E_g is also estimated using the maximum Seebeck coefficient (α_{\max}) and the corresponding temperature (T) as shown in eqn (9):^{71,72}

$$E_g = 2e\alpha_{\max}T \quad (9)$$

The calculated E_g is *ca.* 0.17 eV for $0 \leq x \leq 0.04$ and reduces to 0.16 eV for $0.06 \leq x \leq 0.08$, resulting an increased n . The schematic of the variation for band structure and E_g is shown in Fig. 6c. The widened valence band and narrowed E_g can enhance the m^* and n , respectively, as shown in Fig. 6a and b. σ_{\parallel} of all bulks shows a similar temperature dependence as increasing temperature in Fig. 6d. The σ_{\parallel} increases from $3.87 \times 10^4 \text{ S m}^{-1}$ ($x = 0$) to $5.64 \times 10^4 \text{ S m}^{-1}$ ($x = 0.06$) and then decreases to $5.08 \times 10^4 \text{ S m}^{-1}$ ($x = 0.08$) at 300 K, which is the results of the combination of n_{\parallel} and μ_{\parallel} according to $\sigma = ne\mu$. All bulks in Fig. 6e have a positive α_{\parallel} at room temperature indicating a p-type semi-conductive behavior, but show

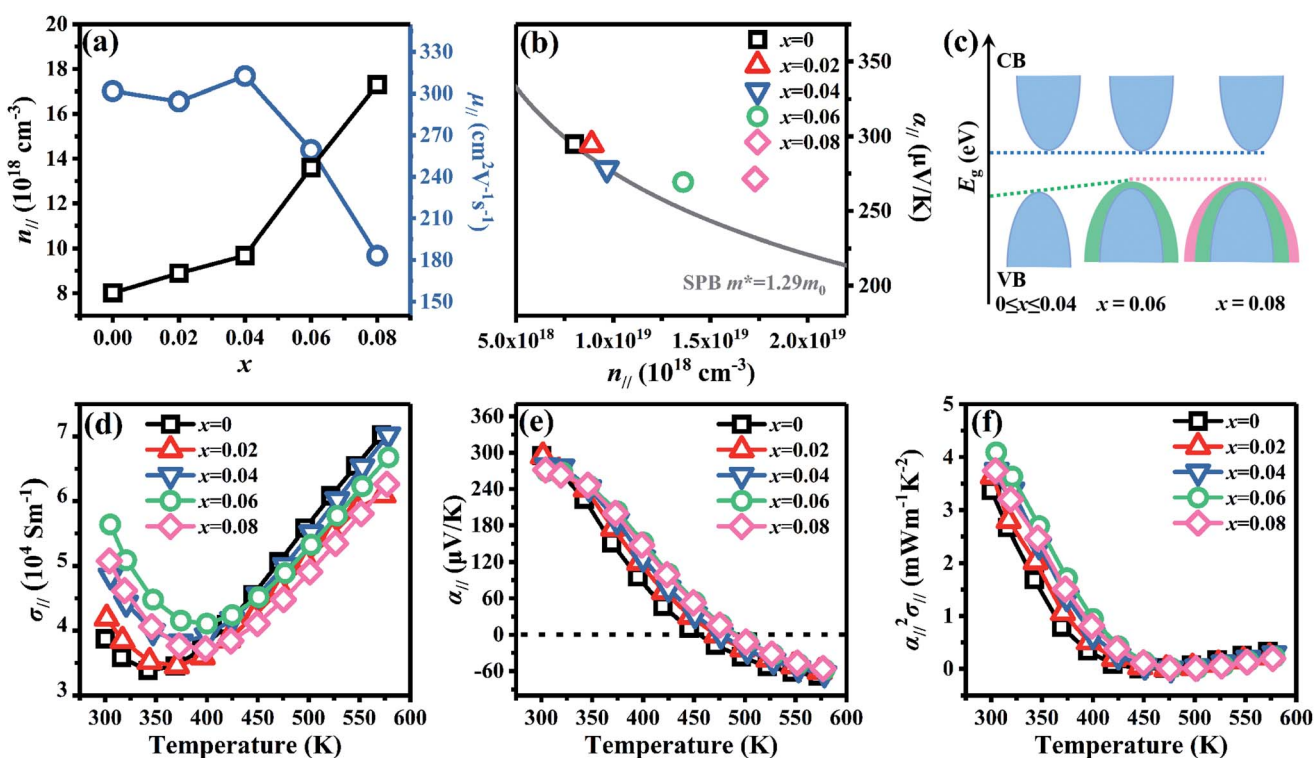


Fig. 6 Electrical transport properties for $\text{Bi}_2\text{Te}_{3-x}$ ($x = 0, 0.02, 0.04, 0.06, 0.08$) single crystal along the in-plane. (a) Carrier concentration (n_{\parallel}) and mobility (μ_{\parallel}), (b) dependence between the α_{\parallel} and n_{\parallel} (the Pisarenko curve) at 300 K, (c) schematic representation of the band structure, (d) electrical conductivity (σ_{\parallel}), (e) Seebeck coefficient (α_{\parallel}), and (f) power factor ($\alpha_{\parallel}^2 \sigma_{\parallel}$).



a transformation from p-type to n-type between 400 K and 500 K. As increasing x , $\alpha_{||}$ decreases from 294.89 $\mu\text{V K}^{-1}$ at $x = 0$ to 269.30 $\mu\text{V K}^{-1}$ at $x = 0.06$ due to the significantly increased $n_{||}$ in Fig. 6a. Owing to the high $\sigma_{||}$ ($5.64 \times 10^4 \text{ S m}^{-1}$) and $\alpha_{||}$ (269.30 $\mu\text{V K}^{-1}$), a maximum $\text{PF}_{||}$ 4.09 $\text{mW m}^{-1} \text{ K}^{-2}$ is obtained at 300 K for $x = 0.06$ as shown in Fig. 6f, which has an enhancement of 21% compared with the intrinsic Bi_2Te_3 at the same temperature.

Fig. 7 shows the temperature dependence of thermal transport properties for $\text{Bi}_2\text{Te}_{3-x}$ ($x = 0, 0.02, 0.04, 0.06, 0.08$) single crystals along the in-plane. The thermal diffusivity ($D_{||}$) of all bulks monotonously increases as increasing the temperature from 300 K to 573 K in Fig. 7a. $D_{||}$ decreases from 1.52 $\text{mm}^2 \text{ s}^{-1}$ for $x = 0$ to 1.39 $\text{mm}^2 \text{ s}^{-1}$ for $x = 0.08$ at 300 K. $\kappa_{||}$ of all bulks in Fig. 7b presents the similar varying trend with $D_{||}$ as increasing the temperature. κ is the sum of the κ_{ele} (electronic thermal conductivity), the κ_{lat} (lattice thermal conductivity) and the κ_{bip} (bipolar thermal conductivity). And κ_{ele} can be estimated by the Wiedemann–Franz relation: $\kappa_{\text{ele}} = L\sigma T$, where L is the Lorenz number, T is the absolute temperature, respectively. The L can be calculated basing on SPB model using eqn (10)–(12).⁵⁰

$$L = \left(\frac{k_B}{e}\right)^2 \left[\frac{(r + 7/2)F_{r+5/2}(\eta)}{(r + 3/2)F_{r+1/2}(\eta)} - \left(\frac{(r + 5/2)F_{r+3/2}(\eta)}{(r + 3/2)F_{r+1/2}(\eta)} \right)^2 \right] \quad (10)$$

$$F_n(\eta) = \int_0^\infty \frac{x^n}{1 + e^{x-\eta}} dx \quad (11)$$

$$\alpha = \pm \frac{k_B}{e} \left[\frac{(r + 5/2)F_{r+3/2}(\eta)}{(r + 3/2)F_{r+1/2}(\eta)} - \eta \right] \quad (12)$$

where r , $F_n(\eta)$ and η are the scattering parameter, the Fermi integral and reduced Fermi energy, respectively. The varying trend of calculated κ_{ele} in Fig. 7c is similar to that of $\sigma_{||}$ (Fig. 6d). The highest κ_{ele} is 0.86 $\text{W m}^{-1} \text{ K}^{-1}$ for $x = 0.04$ at 573 K, while the lowest $(\kappa_{\text{lat}} + \kappa_{\text{bip}})_{||}$ is 1.45 $\text{W m}^{-1} \text{ K}^{-1}$ obtained at $x = 0.08$ at 300 K, indicating that $(\kappa_{\text{lat}} + \kappa_{\text{bip}})_{||}$ plays a dominant role in thermal transport properties for all bulks. $(\kappa_{\text{lat}} + \kappa_{\text{bip}})_{||}$ decreases from 1.70 $\text{W m}^{-1} \text{ K}^{-1}$ to 1.45 $\text{W m}^{-1} \text{ K}^{-1}$ as x increasing from 0 to 0.08 as shown in Fig. 7d. The reduction of $(\kappa_{\text{lat}} + \kappa_{\text{bip}})_{||}$ is attributed to the enhancement of point defects which can enhance the scattering of phonons. Fig. 8a shows the temperature dependence of $ZT_{||}$ for $\text{Bi}_2\text{Te}_{3-x}$ ($x = 0, 0.02, 0.04, 0.06, 0.08$) single crystals along the in-plane. The deteriorated $\alpha_{||}$ results in a reduction of $ZT_{||}$ with increasing temperature. However, owing to the high $\text{PF}_{||}$ in Fig. 6f and low $\kappa_{||}$ in Fig. 7b, the $x = 0.06$ bulk attains the highest $ZT_{||}$ value of 0.70 at 300 K, which is 30% higher than that (0.54) of the intrinsic Bi_2Te_3 , indicating that producing point defects is effective to enhance the TE properties of Bi_2Te_3 single crystals. Fig. 8b shows a comparison of the TE properties at 300 K for p-type Bi_2Te_3 -based bulks prepared by different methods. The result shows that the TE properties of Bi_2Te_3 single crystals prepared by TGGM described in this work is comparable with other early reported values.^{73–75} This result indicates that TGGM is a simple and effective method to prepare Bi_2Te_3 -based single crystals.

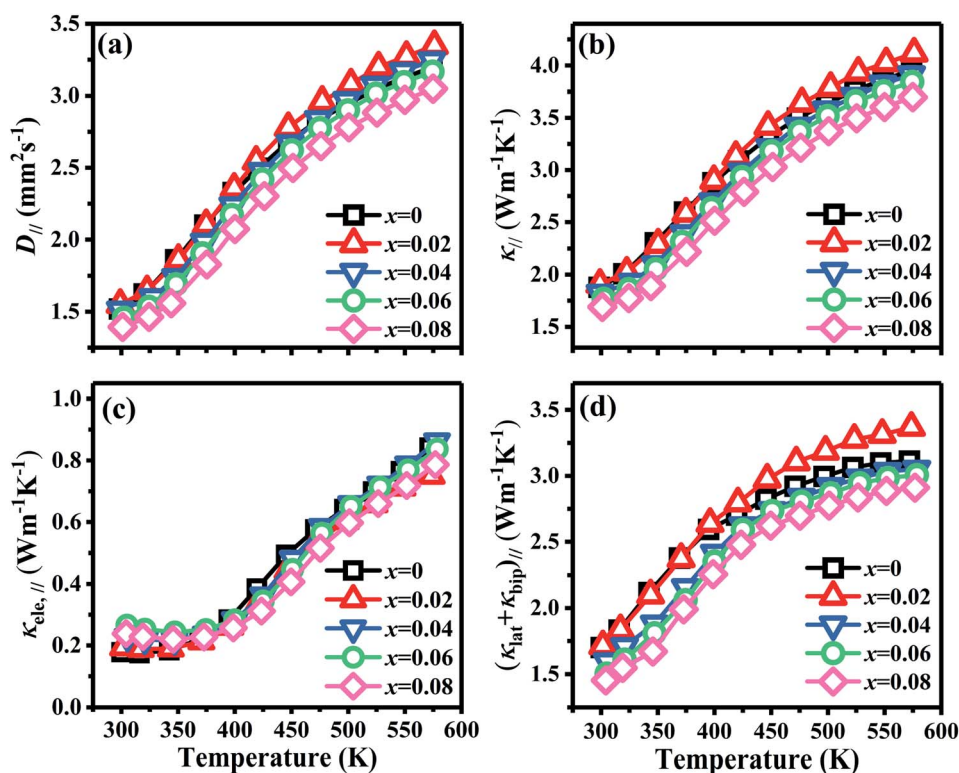


Fig. 7 Temperature dependence of thermal transport properties for $\text{Bi}_2\text{Te}_{3-x}$ ($x = 0, 0.02, 0.04, 0.06, 0.08$) single crystal along the in-plane. (a) Thermal diffusivity ($D_{||}$), (b) total thermal conductivity ($\kappa_{||}$), (c) electronic thermal conductivity ($\kappa_{\text{ele}, ||}$), and (d) the sum of lattice thermal conductivity and bipolar thermal conductivity ($(\kappa_{\text{lat}} + \kappa_{\text{bip}})_{||}$).



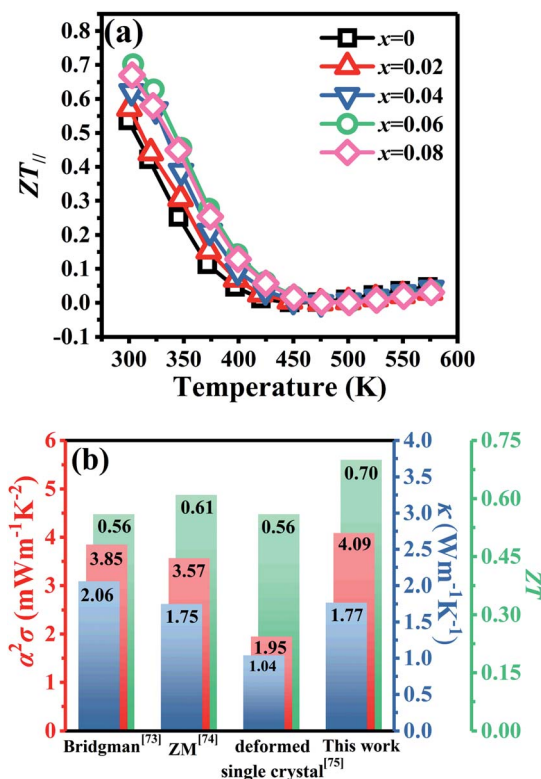


Fig. 8 (a) Temperature dependence of figure of merit (ZT_{\parallel}) for $\text{Bi}_2\text{Te}_{3-x}$ ($x = 0, 0.02, 0.04, 0.06, 0.08$) single crystals along the in-plane and (b) comparison of TE properties with early reports.

4. Conclusions

In Bi_2Te_3 single crystals, the calculated electronic structure indicates that Te atoms play a dominant role near valence band maxima (VBM), whereby the change of Te atoms may broaden the band structure and enhance m^* . The calculated formation energy under the Te-lack condition indicates that Bi can easily enter into Te-sites to form antisite defects and provide holes. The effects of point defects on TE properties were investigated detailedly by preparing a series of p-type $\text{Bi}_2\text{Te}_{3-x}$ ($x = 0, 0.02, 0.04, 0.06, 0.08$) single crystals *via* TGGM. The lack of Te increases antisite defects and broadens the band structure which can increase n_{\parallel} and m^* , respectively, apart from an increased PF_{\parallel} 4.09 $\text{mW m}^{-1}\text{K}^{-2}$ for $x = 0.06$ composition, also contributing the lowest κ_{\parallel} 1.69 $\text{W m}^{-1}\text{K}^{-1}$ at $x = 0.08$ achieved by the increased scattering of phonons. Owing to the simultaneous optimization of electrical transport properties and thermal conductivity, a highest ZT_{\parallel} 0.70 was obtained for $x = 0.06$ composition at 300 K, which is 30% higher than that (0.54) of the intrinsic Bi_2Te_3 .

Conflicts of interest

There are no conflicts to declare.

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