Improvement of electric field-induced strain and energy storage density properties in lead-free BNKT-based ceramics modified by BFT doping

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In this research, the effects of Ba(Fe0.5Ta0.5)O3 (BFT) additive on the phase evolution, the dielectric, ferroelectric, piezoelectric, electric field-induced strain responses, and energy storage density of the Bi0.5(Na0.80K0.20)0.5TiO3–0.03(Ba0.75Sr0.25)TiO3 (BNKT–0.03BSrT) ceramics have been systematically investigated. The ceramics have been prepared by a solid-state reaction method accompanied by two calcination steps. X-ray diffraction indicates that all ceramics coexist between rhombohedral and tetragonal phases, where the tetragonal phase becomes dominant at higher BFT contents. The addition of BFT also promotes the diffuse phase transition in this system. A significant enhancement of electric field-induced strain response (Smax = 0.42% and d′33 = 840 pm V−1) is noted for the x = 0.01 ceramic. Furthermore, the giant electrostrictive coefficient (Q33 = 0.0404 m4 C−2) with a giant normalized electrostrictive coefficient (Q33/E = 8.08 × 10−9 m5 C−2 V−1) are also observed for this composition (x = 0.01). In addition, the x = 0.03 ceramic shows good energy storage properties, i.e. it has a high energy storage density (W = 0.65 J cm−3 @ 120 °C) with very high normalized storage energy density (W/E = 0.13 μC mm−3), and good energy storage efficiency (η = 90.4% @ 120 °C). Overall, these results indicate that these ceramics are one of the promising candidate piezoelectric materials for further development for actuator and high electric power pulse energy storage applications.

Introduction

For actuator applications, electrostriction is an important property which describes how the material deforms when polarization develops inside. Electrostriction occurs in materials with either centro or noncentrosymmetric crystal structures, and is caused by a slight displacement of ions (or complexes) in the crystal lattice when the material is subjected to an applied field. In the case of electrostriction, the field-induced strain (S) can be simply related to the polarization (P) by: S = Q13P, where Q13 represents the electrostrictive coefficient.2-5 A large Q13 value of ~0.020 m4 C−2 with a good hysteresis-free electrostrictive strain (~0.1%) can be observed in some lead-based relaxor ferroelectrics, such as Pb(Mg1/3Nb2/3)O3 (PMN),3 which is known as an important electrostrictive material.2 However, because of the concern for environmental problems that lead-based materials pose, the development of lead-free electrostrictive piezoelectric materials has been urgent in recent years.3,5-6

Among many lead-free piezoelectric materials, (Bi0.5Na0.5)TiO3-based (BNT) ceramic is an interesting material due to its relatively excellent electrical properties, especially for ferroelectric and piezoelectric properties i.e. high electric energy densities6 and ultra-high strain under a high electric field (≥50 kV cm−1).3 However, the large coercive electric field (Ec = 7.3 kV mm−1) and high electrical conductivity made it difficult to be polarized during the poling process, which often leads to undesirable piezoelectricity (d33 = 73–95 pC N−1) and limited its applications.10 In order to reduce the Ec and improve the electrical properties, researches on composition-modified BNT systems have been conducted such as BNT–BT,11,12 BNT–ST,13 BNT–BZT–SBT,14 and BNT–BKT.15,16 Ullah et al.17 studied the effect of (Ba0.7Sr0.3)TiO3 (BST) on the structure and electrical properties of the Bi0.5(Na0.4K0.1)TiO3 (BNKT) ceramic. They reported that this ceramic exhibited good electrical properties i.e. the ceramics presented high piezoelectric coefficient (d33 = 223 pC N−1) with dielectric loss (tan δ) of 3% at 1 kHz. They also found that the La additive interrupted the P–E hysteresis loops of the BNKT–BST ceramics, which lead to a reduction in Pε and Ec values.18 However, the destabilization of the ferroelectric order corresponded to a significant increase of the unipolar strain which showed the highest value of ~0.39% and

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corresponding a normalized strain \( \left( d_{33}^* = S_{\text{max}}/E_{\text{max}} \right) \) of 650 pm V\(^{-1}\)\(^{19}\). Therefore, research on modified BNKT–BST ceramics is an important topic in order to develop lead-free ceramics with high electrical properties.

An interesting work for electrostrictive materials was performed by Zhang et al.\(^{20}\) who provided a research direction to develop the \((1 - x)[0.94\text{Bi}_0.5\text{Na}_0.5\text{TiO}_3-0.06\text{BaTiO}_3-x\text{K}_0.5\text{Na}_0.5\text{NbO}_3\) system with a large electrostrictive coefficient \(Q_{33} \approx 0.021-0.027 \text{ m}^4 \text{ C}^{-2} \) and the maximum strain \( (S_{\text{max}} \approx 0.12-0.30\%) \) values simultaneously. Beside Zhang et al.’s work, a large electrostrictive effect with \( Q_{11} = 0.0297 \text{ m}^4 \text{ C}^{-2} \) was also obtained by Shi et al.\(^{21}\) in the \((0.94 - x)[\text{Bi}_0.5\text{Na}_0.5\text{TiO}_3-0.06\text{BaTiO}_3-x\text{SrO}_2\text{Bi}_0.5\text{Bi}_0.5\text{O}_3] \) system, in which its \( Q_{11} \) exhibits a high temperature stability between ambient temperature to 180 °C.\(^{22}\) Moreover, a high strain \( \left( S_{\text{max}} \approx 0.45\% \right) \) was also found in the \([\text{Bi}_0.5\text{Na}_0.5\text{TiO}_3-\text{BaTiO}_3-0.03\text{Fe}_2\text{O}_3] \) powders before being uniaxially pressed into discs 10 mm in diameter. The green pellets were sintered at 1125 °C for 2 h by using a heating and cooling rate of 5 °C min\(^{-1}\).

Experimental

The conventional mixed oxide technique was used to synthesize the \( (1 - x)[\text{Bi}_0.5\text{Na}_0.5\text{K}_0.2\text{Bi}_0.3\text{O}_3-0.03\text{Ba}_0.7\text{Sr}_0.3\text{O}_3] \text{TiO}_3-x\text{BaFe}_0.5\text{Ta}_0.5\text{O}_3 \) or \((1 - x)[\text{BNKT-0.03BST}]-x\text{BFT} \) powders. The analytical grade reagents of metal oxide powders, including \( \text{Na}_2\text{CO}_3, \text{Bi}_2\text{O}_3, \text{K}_2\text{CO}_3, \text{TiO}_2, \text{Fe}_2\text{O}_3, \text{SrCO}_3, \text{BaCO}_3, \) and \( \text{Ta}_2\text{O}_5 \) were used as starting materials. All carbonate powders were first dried at 120 °C for 24 h in order to eliminate any moisture. The raw materials of \( \text{BNKT-0.03BST} \) and BFT were stoichiometrically weighed, ball milled for 24 h in an ethanol solution, and then dried in an oven. Since there is a large difference in calcination temperatures between \( \text{BNKT-0.03BST} \) \((900 \text{ °C}) \) and BFT \((1200 \text{ °C}) \) powders, two calcination steps were employed i.e. the \( \text{BNKT-0.03BST} \) and BFT powders were synthesized separately. The resulting powders were weighed, mixed and then dried to obtained a powder of \((1 - x)[\text{BNKT-0.03BST}]-x\text{BFT} \) with \( x = 0, 0.02 \) and 0.03 mol fraction. A few drops of polyvinyl alcohol (PVA) binders (4 wt%) were added to the obtained powders before being uniaxially pressed into discs 10 mm in diameter. The green pellets were sintered at 1125 °C for 2 h by using a heating and cooling rate of 5 °C min\(^{-1}\).

Bulk density was determined by the Archimedes’ method. A scanning electron microscope (SEM, JEOL JSM-6335F) was used to study microstructural features of the ceramics. An X-ray diffractometer (XRD-Phillip, X-pert) was used to study the phase evolution of all ceramics. Grain size of the ceramics was evolved out by using linear intercept method (ASTM no. E112-88). Before investigating the electrical measurements, all samples were polished into a parallel surface with 1 mm thickness. Silver paste was subjected onto both sides of the sample. Then the samples were heated at 700 °C for 30 min to form electrodes. Dielectric properties as a function of temperature \((25-400 \text{ °C}) \) were carried out using an LCR-meter (HP model 4192A) at frequencies ranging from 1 to 1000 kHz. The ferroelectric properties were carried out by a Radiant Precision ferroelectric tester both at room temperature (RT) and high temperatures (HT) of 25–150 °C. A maximum electric field of 50 kV cm\(^{-1}\) at a frequency of 1 Hz was applied to each studied sample. Remanent polarization \( (P_r) \), maximum polarization \( (P_{\text{max}}) \), and coercive field \( (E_c) \) values were determined from the hysteresis loops or \( P-E \) loops. By using data from ferroelectric properties, the energy storage density \( (W) \) and energy storage coefficient \( (\eta) \) values were also calculated. Strain–electric field \( (S-E) \) data at RT were carried out using an optical displacement sensor (Potonic Sensor model MTI-2100) injection with a Radiant ferroelectric test system. A maximum electric field of 50 kV cm\(^{-1}\) and a frequency of 0.1 Hz were used to measure the bipolar and unipolar strain curves. The maximum strain \( (S_{\text{max}}) \) and the negative strain \( (S_{\text{neg}}) \) values were carried out from the bipolar curve. The normalized strain coefficient \( d_{33}^* \) was also determined following: \( d_{33}^* = S_{\text{max}}/E_{\text{max}} \). The electrostrictive coefficient \( (Q_{33}) \) was determined from \( S-P \) curves using equation: \( S = QP^2 \). For piezoelectric measurement, all samples were poled at
RT with an applied DC electric field of 5 kV mm\(^{-1}\) (for 15 min) and using silicone oil as the media. The low-field piezoelectric coefficient \(d_{33}\) was determined by a \(d_{33}\)-meter.

### Results and discussion

#### Phase formation and microstructure

Fig. 1(a) shows the X-ray diffraction patterns with different doping contents of the \((1 - x)[BNKT-0.03BSrT]-xBFT\) ceramics. Within the resolution limit of XRD, all ceramics exhibit a single phase of perovskite structure with no secondary phase, confirming that BFT has been incorporated into the BNKT-0.03BSrT lattice to form solid solutions of the end compounds. For analyzing the phase transition process, the XRD patterns for selected narrow angular ranges of \(2\theta = 39-41^\circ\) and \(2\theta = 44-48^\circ\) are presented in Fig. 1(b) and (c), respectively. The \(x = 0\) ceramic presents a mixed phase of rhombohedral and tetragonal structure, which is demonstrated by a slight splitting of the \((111)_{R}/(111)_{R}\) at \(2\theta \sim 40^\circ\) and splitting of the \((200)_{R}/(002)_{T}\) peaks at \(2\theta \sim 46^\circ\). This result also agrees with the result observed by Ge et al.\(^{a}\) However, the coexistence of the mixed rhombohedral and tetragonal phases transforms into a tetragonal-rich phase at higher BFT contents. This can be evidenced by, the existence of the splitting \((200)_{R}/(002)_{T}\) peaks, and the merger of the \((111)_{R}/(111)_{R}\) peak into a single \((111)_{T}\) peak, thus indicating that the amount of tetragonal phase is higher than that of the rhombohedral phase, with increasing BFT content. To check the appearance of the phase transformation in more detail, the tetragonality ratio \((c/a)\) was determined and its values are listed in Table 1. The \(c/a\) value increases from 1.0105 for the \(x = 0\) ceramic to 1.0128 for the \(x = 0.03\) ceramic, as expected. Furthermore, the diffraction peaks gradually shift to a lower angle with increasing BFT content. This can be caused by the differences in the ionic radii between Na\(^{+}\), Bi\(^{3+}\), K\(^{+}\), Sr\(^{2+}\), and Ba\(^{2+}\) at the A-site and Ti\(^{4+}\), Fe\(^{3+}\), and Ta\(^{5+}\) at the B-site\(^{a}\) which, as a result, can induce a structural distortion such as an enlargement of unit cell size, as shown in Fig. 2. A similar peak slightly shifted by partial substitution of Ba\(^{2+}\) for [Bi\(_{0.5}(Na_{0.80}K_{0.20})\]\(^{2+}\) and Zr\(^{4+}\) for Ti\(^{4+}\) was reported by Chen et al.\(^{a}\) in the BNKT-BZT system. They also found that the \((110)\) peak shifted to lower \(2\theta\) angles could produce an increase in the lattice constant and the unit cell dimension with increasing BZT fraction.

SEM micrographs and their corresponding histogram of grain size distribution of the \((1 - x)[BNKT-0.03BSrT]-xBFT\) ceramics are shown in Fig. 3. The average grain size values are also summarized in Table 1. The SEM result confirms that all samples are dense with relatively high densities (5.80–5.86 g cm\(^{-3}\)). Furthermore, the porosity levels evident in the micrographs are noted to be consistent with the trend of measured density value, where the density increases with increasing BFT content. Most grains of all samples show a clear grain boundary with round and cubic shapes. The addition of BFT seems to have a slight influence on the microstructure as well as the average grain size of the BNKT-BSrT ceramics. The average grain size values of all samples are rather similar (0.56–0.61 \(\mu m\)) and the grain size distribution shows a monomodal normal distribution. However, a slight narrow grain size distribution is noted for a ceramic containing a higher amount of BFT. This suggests that the microstructure can be improved by a BFT additive.

#### Results and discussion

**Table 1** Phase, physical, microstructure and dielectric properties of the \((1 - x)[BNKT-0.03BSrT]-xBFT\) ceramics

<table>
<thead>
<tr>
<th>(x)</th>
<th>Density (g cm(^{-3}))</th>
<th>Relative density (%)</th>
<th>(c/a)</th>
<th>Unit cell volume (Å(^3))</th>
<th>Grain size (µm)</th>
<th>(T_{\text{ms}}) (°C)</th>
<th>(\varepsilon_{\text{max}}) (@1 kHz)</th>
<th>(\delta_{a}^{\text{a}}) (K)</th>
<th>(\delta_{b}^{\text{b}}) (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>5.80</td>
<td>98</td>
<td>1.0105</td>
<td>60.18</td>
<td>0.61</td>
<td>316</td>
<td>5156</td>
<td>83</td>
<td>73</td>
</tr>
<tr>
<td>0.01</td>
<td>5.83</td>
<td>98</td>
<td>1.0117</td>
<td>60.28</td>
<td>0.59</td>
<td>303</td>
<td>5151</td>
<td>91</td>
<td>94</td>
</tr>
<tr>
<td>0.02</td>
<td>5.85</td>
<td>99</td>
<td>1.0121</td>
<td>60.43</td>
<td>0.58</td>
<td>292</td>
<td>4814</td>
<td>94</td>
<td>117</td>
</tr>
<tr>
<td>0.03</td>
<td>5.86</td>
<td>99</td>
<td>1.0128</td>
<td>60.46</td>
<td>0.56</td>
<td>284</td>
<td>4716</td>
<td>105</td>
<td>123</td>
</tr>
</tbody>
</table>

\(^{a}\) Polled sample. \(^{b}\) Unpoled sample.
values of the $x = 0$ ceramic in this study are observed from Fig. 4 to be 316 and 5156, respectively. The $\varepsilon_{\text{max}}$ decreases with increasing BFT content. Furthermore, the $T_m$ also shifts from 316 °C for the $x = 0$ ceramic to 284 °C for $x = 0.03$ ceramic. This result also agrees with the results of previous report for other BNKT-based ceramics.\(^\text{34}\)

To study the diffuse phase transition in this system, the diffuseness of the phase transition was calculated by a modified Curie–Weiss law eqn (1) which is given by ref. 37 and 38.

$$\frac{\varepsilon_{\text{max}}}{\varepsilon_I} = 1 + \frac{(T - T_m)^2}{\Delta^2},$$  

(1)

where $\Delta$ is the diffuseness parameter. The $\Delta$ value can be carried out from the curve of $\ln(\varepsilon_{\text{max}}/\varepsilon_I - 1)$ vs. $\ln(T - T_m)^2$, where the curve should be linear.\(^\text{37}\) The $\Delta$ is used to compare the degree of diffuseness of the phase transition for many materials. The $\Delta$ values for poled and unpoled ceramics are summarized in Table 1. Based on Table 1, it can be seen that the addition of BFT has an effect on the degree of diffuseness, where the $\Delta$ value increases with increasing BFT content. This result corresponds to the previous work,\(^\text{39}\) which indicates that the addition of BFT produces a higher degree of diffuseness for the phase transition in the modified BNKT ceramics.

**Polarization and strain behaviors**

The $P$–$E$ hysteresis and bipolar strain–electric field ($S$–$E$) loops measured at room temperature (RT) and electric field of 50 kV cm\(^{-1}\) are shown in Fig. 5 and 6, respectively. The related values are also listed in Tables 2 and 3. The $x = 0$ ceramic displays a small pinched loop with the maximum values of $P_{\text{max}} = 37.70 \mu$C cm\(^{-1}\), $P_r = 21.74 \mu$C cm\(^{-1}\) and $E_c = 12.87$ kV cm\(^{-1}\). The $S$–$E$ curve for this sample also exhibits a butterfly-shaped loop. The $S_{\text{max}}$ and $d_{33}^*$ of this ceramic are 0.33% and 650 pm V\(^{-1}\), respectively. The ferroelectric loop indicates a ferroelectric domain switching at $E_c$, where the largest $S_{\text{neg}}$ is −0.11%. However, this ceramic sample should contain a mixed phase

**Dielectric properties**

Temperature dependence of the dielectric properties, including constant ($\varepsilon_I$) and dielectric loss (tan $\delta$) of the poled $(1-x)$ [BNKT–0.03BSrT]–xBFT ceramics measured at different frequencies from 1–1000 kHz are shown in Fig. 4, and the related values are also listed in Table 1. It can be seen that the $\varepsilon_I$ versus temperature ($\varepsilon_I$–$T$) curves for all ceramics exhibit two dielectric anomaly peaks at $\sim$100 °C and 300 °C.\(^\text{33,34}\) Normally, the high temperature anomaly peak is called $T_m$, where the dielectric constant reaches its maximum value.\(^\text{44–46}\) The lower anomaly peak is located near $T_{P-R}$, which is known as the ferroelectric (FE) to ergodic relaxor (ER) phase transition temperature.\(^\text{6}\) Normally, the $T_{P-R}$ can be usually carried out from the peak of tan $\delta$–$T$ curve of a poled sample. However, the $T_{P-R}$ could not be detected from the tan $\delta$–$T$ curves for this work. The $T_m$ and $\varepsilon_{\text{max}}$
between FE and ER, since the $P$–$E$ loop presents a small pinched shape. For the $x = 0.01$ ceramic, however, the $P$–$E$ hysteresis loop exhibits a more pinched loop with a decrease of $P_r$ from 21.74 μC cm$^{-2}$ to 8.15 μC cm$^{-2}$ and $E_c$ from 12.87 kV cm$^{-1}$ to 7.34 kV cm$^{-1}$. The hysteresis loop shows a clear pinching-type character with further increasing BFT content, similarly observed in previous works.$^{6,33}$ The pinched $P$–$E$ loops corresponded with the two current peaks (denoted as “1” and “2”) in the $I$–$E$ curves (Fig. 5), where it has been suggested that this evidence indicates a formation of ER phase.$^{14,36}$

The more pinched $P$–$E$ loops result also corresponds to a large electric field-induced strain response with $S_{\text{max}}$ of 0.42% and $d_{33}^{\text{max}}$ of 840 pm V$^{-1}$ along with a drastic reduction in $S_{\text{neg}}$ from $-0.11\%$ to 0% for the $x = 0.01$ ceramic in bipolar $S$–$E$ loops. This enhancement is also confirmed by the unipolar $S$–$E$ loops, as shown in Fig. 7(a). It is seen that the unipolar $S$–$E$ loops for all compositions show a similar trend as compared to that of the bipolar $S$–$E$ loops, where the maximum strain value of the unipolar strain is 0.42% for the $x = 0.01$ ceramic (Fig. 7(b)). The pinching of the $P$–$E$ hysteresis loops with rapid reductions of $P_r$ and $E_c$ can be correlated with the increase of $S_{\text{max}}$ along with a drastic reduction in $S_{\text{neg}}$. This may be related

![Figure 6](image6.png)  
**Fig. 6** Bipolar strain–electric field ($S$–$E$) loops of the $(1-x)$[BNKT–0.03SrTi]–xBFT ceramics where $x = 0$–0.03, measured at RT under an electric field of 50 kV cm$^{-1}$ and a frequency of 0.1 Hz.

![Figure 7](image7.png)  
**Fig. 7** Plots of (a) unipolar strain–electric field ($S$–$E$) loops of the $(1-x)$ [BNKT–0.03SrTi]–xBFT ceramics where $x = 0$–0.03, measured at RT under an electric field of 50 kV cm$^{-1}$ and a frequency of 0.1 Hz and (b) plots of the maximum strain ($S_{\text{max}}$) and normalized strain coefficient ($d_{33}^{\text{max}}$) as a function of BFT content (inset: $Q_{33}$ value as a function of BFT content).

<table>
<thead>
<tr>
<th>$x$</th>
<th>$P_{\text{max}}$ (μC cm$^{-2}$)</th>
<th>$P_r$ (μC cm$^{-2}$)</th>
<th>$E_c$ (kV cm$^{-1}$)</th>
<th>$W^a$ (J cm$^{-3}$)</th>
<th>$W^b$ (J cm$^{-3}$)</th>
<th>$W^c$ (J cm$^{-3}$)</th>
<th>$\eta^a$ (%)</th>
<th>$\eta^b$ (%)</th>
<th>$\eta^c$ (%)</th>
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<tr>
<td>0</td>
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<td>12.87</td>
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<td>0.63</td>
<td>60.7</td>
<td>90.4</td>
<td>92.1</td>
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* Ferroelectric data obtained at high temperature of 25 °C and a frequency of 1 Hz. $^b$ Ferroelectric data obtained at high temperature of 120 °C and a frequency of 1 Hz. $^c$ Ferroelectric data obtained at high temperature of 150 °C and a frequency of 1 Hz.

<table>
<thead>
<tr>
<th>$x$</th>
<th>$S_{\text{max}}$ (%)</th>
<th>$S_{\text{neg}}$ (%)</th>
<th>$d_{33}^{\text{max}}$ (pm V$^{-1}$)</th>
<th>$H$ (%)</th>
<th>$Q_{33}$ (m$^4$ C$^{-2}$)</th>
<th>$d_{33}$ (pC N$^{-1}$)</th>
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<tr>
<td>0</td>
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<td>650</td>
<td>78.9</td>
<td>0.0376</td>
<td>172</td>
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<td>38</td>
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<td>0.02</td>
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<td>29</td>
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<td>0.03</td>
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<td>654</td>
<td>39.3</td>
<td>0.0368</td>
<td>28</td>
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with a phase transition from a ferroelectric (FE) to an ergodic relaxor (ER) phase, accompanied by the disruption of long-range ferroelectric order with increasing BFT content. Normally, the free energy of FE and ER phases is comparable under zero field, thus it can be easily induced by an external electric field to become saturated. Therefore, ER phase can be transformed reversibly into FE phase by an external electric field. This behaviour consists with the work done by Dong et al., who also reported that the $(1-x)0.8Bi_{1/2}Na_{1/2}TiO_3-0.2Bi_{1/3}K_{1/3}TiO_3$ x $\pm$BiMg$_2/3$Nb$_1/3$O$_3$ or (BNKT$–$BKT)$–$BMN system produced a large strain response when a small amount of BMN was added into the BN$–$BKT ceramic. The addition of 2 mol% BMN into the BNT$–$BKT ceramic shows a pronounced ergodic relaxor (ER) characteristic, which is confirmed by the absence of $S_{\text{neg}}$, the pinched $P$–$E$ loop and the double current peaks of $I$–$E$ loop. However, in the present work when $x > 0.01$, the strain is reduced gradually. Therefore, the small amount of BFT additive has effects on the piezoelectric properties of the BNKT$–$0.03BSrT ceramics. It should be noted that the $S_{\text{max}}$ in this work ($x = 0.01$) is considered high when compared with other lead-free piezoelectric ceramics (see Table 4). Furthermore, the bipolar strain loops for the present work exhibit a low anti-symmetry in their shape compared to many previous works for the giant strain response which showed high anti-symmetry.

In the present work, an average maximum strain ($S_{\text{max}}$) was calculated to be used as a parameter to check for overall averaged maximum strain under the bipolar strain loop, where $S_{\text{max}}$ averaged from maximum strain between the right and left hand sides of the bipolar strain loop. The result is also shown in Table 4. The obtained $S_{\text{max}}$ for the present work is considered high for the lead-free piezoelectric ceramics.

The $Q_{13}$ was determined from the slope of $S$ vs. $P^2$ curve. The plotting of $Q_{13}$ value as a function of BFT content is shown in inset of Fig. 7(b). The highest $Q_{13}$ of 0.040 m$^2$ C$^{-2}$ is noted for the $x = 0.01$ ceramic. It is evident that the currently presented $Q_{13}$ value is highly competitive to many materials. In addition, a comparison of the room temperature $Q_{13}$ and normalized $Q_{13}$ ($Q_{13}/E$) values with other lead-based and lead-free BNT-based electrostrictive materials are summarized in Table 5. It should be noted that the $Q_{13}/E$ value for the present work is very high for both lead-based and lead-free BNT-based piezoelectric materials. Therefore, the $(1-x)[BNKT$–$0.03BSrT]$–$xBFT compound may be a promising candidate for new electromechanical devices due to its giant $Q_{13}$ value.

Normally for the actuator applications, a large strain with low hysteresis is necessary. The degree of strain hysteresis ($H$) can be determined from the following equation:

$$H = \frac{\Delta S_{\text{max}}}{S_{\text{max}}} \times 100\%,$$

where the $\Delta S_{\text{max}}$ is the strain deviation during the application and removal of the field which is carried out at half of the maximum electric field. The $H$ values of all ceramics are summarized in Table 3. It was found that the $H$ decreases with

### Table 4 Comparison of $S_{\text{max}}$ and $d_{33}^*$ values of the $(1-x)[BNKT–0.03BSrT]$–$xBFT$ ($x = 0.01$) with other lead-free ceramics

<table>
<thead>
<tr>
<th>Systems</th>
<th>$S_{\text{max}}$ (%)</th>
<th>$S_{\text{max}}$ (%)</th>
<th>$d_{33}^*$ (pm V$^{-1}$)</th>
<th>$E_{\text{max}}$ (kV cm$^{-1}$)</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.99[BNKT–0.03BSrT]$–0.01$BFT</td>
<td>0.42</td>
<td>0.42</td>
<td>827</td>
<td>50</td>
<td>This work</td>
</tr>
<tr>
<td>BNKT$–$BKT$–$La$_{0.1}$</td>
<td>0.39</td>
<td>0.39</td>
<td>650</td>
<td>60</td>
<td>18</td>
</tr>
<tr>
<td>Bi$<em>{0.9}$Na$</em>{0.1}$K$<em>{0.2}$Ti$</em>{0.75}$Zn$_{0.25}$O$_3$, $x = 0.03$</td>
<td>0.43</td>
<td>0.43</td>
<td>614</td>
<td>70</td>
<td>41</td>
</tr>
<tr>
<td>Bi$<em>{0.9}$Na$</em>{0.1}$K$<em>{0.2}$Ti$</em>{0.75}$Ta$_{0.25}$O$_3$, $x = 0.015$</td>
<td>0.62</td>
<td>0.42</td>
<td>1240</td>
<td>50</td>
<td>42</td>
</tr>
<tr>
<td>BNKT$–$BKT$–$Nb$_{0.1}$, $x = 0.02$</td>
<td>0.38</td>
<td>0.38</td>
<td>634</td>
<td>60</td>
<td>43</td>
</tr>
<tr>
<td>Bi$<em>{0.9}$Na$</em>{0.1}$K$<em>{0.2}$Ti$</em>{0.75}$O$_3$, $x = 0.015$</td>
<td>0.40</td>
<td>0.40</td>
<td>579</td>
<td>70</td>
<td>44</td>
</tr>
<tr>
<td>[(Bi$<em>{1.2}$Na$</em>{0.8}$K$<em>{0.6}$)$</em>{0.6}$Sb$<em>{0.4}$]$</em>{0.3}$Ti$<em>{0.75}$Nb$</em>{0.25}$O$_3$, $x = 0.025$</td>
<td>0.70</td>
<td>0.39</td>
<td>1400</td>
<td>50</td>
<td>45</td>
</tr>
<tr>
<td>Bi$<em>{0.9}$Na$</em>{0.1}$K$<em>{0.2}$Ti$</em>{0.75}$O$_3$–0.03BiFeO$_3$</td>
<td>0.37</td>
<td>0.36</td>
<td>676</td>
<td>50</td>
<td>46</td>
</tr>
<tr>
<td>Bi$<em>{0.9}$Na$</em>{0.1}$K$<em>{0.2}$Ti$</em>{0.75}$O$<em>3$–0.05Ba[(Ti$</em>{0.96}$Sn$<em>{0.04}$)$</em>{0.10}$]O$_3$</td>
<td>0.36</td>
<td>0.36</td>
<td>649</td>
<td>55</td>
<td>47</td>
</tr>
<tr>
<td>[0.93Bi$<em>{0.3}$Na$</em>{0.1}$K$<em>{0.2}$Ti$</em>{0.75}$O$_3$–0.07BaTiO$_3$–0.03BiFeO$_3$]–Pr</td>
<td>0.43</td>
<td>0.42</td>
<td>770</td>
<td>50</td>
<td>48</td>
</tr>
</tbody>
</table>

### Table 5 Comparison of $Q_{13}$ and $Q_{13}/E$ values of the $(1-x)[BNKT–0.03BSrT]$–$xBFT$ ($x = 0.01$) with other lead and lead-free ceramics

<table>
<thead>
<tr>
<th>Systems</th>
<th>$S_{\text{max}}$ (%)</th>
<th>$Q_{13}$ (m$^2$ C$^{-2}$)</th>
<th>$Q_{13}/E_{\text{max}}$ (m$^2$ C$^{-2}$ V$^{-1}$)</th>
<th>$E$ (kV cm$^{-1}$)</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.99[BNKT–0.03BSrT]$–0.01$BFT</td>
<td>0.42</td>
<td>0.0404</td>
<td>8.08</td>
<td>50</td>
<td>This work</td>
</tr>
<tr>
<td>Pb(Mg$<em>{1/3}$Nb$</em>{2/3}$)$_2$O$_5$</td>
<td>—</td>
<td>0.023</td>
<td>—</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>PLZT 8/65/35</td>
<td>0.16</td>
<td>0.015</td>
<td>5.00</td>
<td>30</td>
<td>52</td>
</tr>
<tr>
<td>0.96BNKT$–0.04$BiFeO$_3$</td>
<td>0.38</td>
<td>0.0250</td>
<td>4.17</td>
<td>60</td>
<td>53</td>
</tr>
<tr>
<td>0.93BNKT$–0.05$BiFeO$_3$</td>
<td>0.32</td>
<td>0.0300</td>
<td>5.00</td>
<td>60</td>
<td>53</td>
</tr>
<tr>
<td>N44B48T94$–$6BT or [Na$<em>{0.7}$Bi$</em>{0.3}$]$\pm$T$_{1-x}$Ba$_x$TiO$_3$</td>
<td>0.48</td>
<td>0.0260</td>
<td>3.71</td>
<td>70</td>
<td>54</td>
</tr>
<tr>
<td>8% Sn-doped Bi$<em>{1.2}$(Na$</em>{0.8}$K$<em>{0.2}$)$</em>{0.5}$TiO$_3$</td>
<td>0.14</td>
<td>0.0230</td>
<td>3.83</td>
<td>60</td>
<td>55</td>
</tr>
<tr>
<td>BNKT100y$–$xKNN ($y = 0.20$, $x = 0.16$)</td>
<td>0.10</td>
<td>0.0250</td>
<td>3.12</td>
<td>80</td>
<td>56</td>
</tr>
<tr>
<td>(0.94 $–$ x)Bi$0.5$(La$<em>{0.5}$Na$</em>{0.4}$)$<em>{0.10}$Ti$</em>{0.38}$Zr$<em>{0.02}$O$</em>{3-\delta}$, $x = 0.02$</td>
<td>0.09</td>
<td>0.0260</td>
<td>3.25</td>
<td>80</td>
<td>57</td>
</tr>
<tr>
<td>Bi$<em>{0.5}$La$</em>{0.5}$Na$<em>{0.4}$K$</em>{0.2}$Ti$<em>{0.38}$Zr$</em>{0.02}$O$_{3-\delta}$, $x = 0.02$</td>
<td>0.42</td>
<td>0.0360</td>
<td>6.00</td>
<td>60</td>
<td>58</td>
</tr>
</tbody>
</table>
increasing BFT concentration. The lowest hysteresis of 39.3% is obtained at $x = 0.03$ @ 50 kV cm$^{-1}$, which reveals that BFT doping obviously reduces the strain hysteresis. A comparison of the $H$ value for selected ceramic samples with other lead-free ceramics is shown in Table 6. The result clearly demonstrates that the $H$ value of the present work is low when compared to that of many previous works (for the lead-free piezoceramics with $d_{33}^*$ value > 450 pm V$^{-1}$). This suggests that a BFT modifier can improve the actuating performance.

Polarization-temperature analysis

Temperature dependence of polarization–electric field ($P$–$E$) hysteresis loops of the $(1 - x)[BNKT-0.03BSrT]_x$BFT ceramics where $x = 0-0.03$, measured under an electric field of 50 kV cm$^{-1}$ and a frequency of 1 Hz is shown in Fig. 8. It can be seen that the $P$–$E$ hysteresis loop for the $x = 0$ ceramic shows slightly pinched loops at RT (25 °C). When the temperature increases to 120–150 °C, the $P$–$E$ hysteresis loops become more pinched, confirming that the ferroelectric to relaxor phase transition is induced by thermal activation, thus leaving an ergodic relaxor (ER) state at zero electric field. On the other hand, the modified ceramics ($x \geq 0.01$), exhibit an ER characteristic at RT. With further increasing temperature, the drastic decrease in both $P_r$ and $E_c$ values may also be related to the onset of strong ergodicity. Thus, both chemical modification and temperature can disrupt the FE long-range order leading to a decrease in the polarization states. This phenomenon agrees with that observed in many lead-free piezoelectric materials.

<table>
<thead>
<tr>
<th>Systems</th>
<th>$H$ (%)</th>
<th>$S_{max}$ (%)</th>
<th>$d_{33}^*$ (pm V$^{-1}$)</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.99[BNKT-0.03BSrT]-0.01BFT</td>
<td>55.0</td>
<td>0.42</td>
<td>840</td>
<td>This work</td>
</tr>
<tr>
<td>0.97[BNKT-0.03BSrT]-0.03BFT</td>
<td>39.3</td>
<td>0.32</td>
<td>654</td>
<td>This work</td>
</tr>
<tr>
<td>Bi$<em>{12}$(Na$</em>{0.82}$K$<em>{0.12}$)$</em>{12}$Ti$<em>{12}$I$</em>{12}$-x(Fe$<em>{0.5}$Nb$</em>{0.5}$)$<em>{0.05}$O$</em>{34}$, $x = 5%$</td>
<td>57.0</td>
<td>0.46</td>
<td>660</td>
<td>32</td>
</tr>
<tr>
<td>BNKT20–1.5SZ</td>
<td>51.6</td>
<td>0.39</td>
<td>488</td>
<td>60</td>
</tr>
<tr>
<td>BNT–BKT–5La</td>
<td>60.3</td>
<td>0.38</td>
<td>857</td>
<td>61</td>
</tr>
<tr>
<td>BNT–25ST</td>
<td>45.8</td>
<td>0.29</td>
<td>650</td>
<td>62</td>
</tr>
<tr>
<td>BNKT–3 mol% CZ</td>
<td>49.0</td>
<td>0.37</td>
<td>603</td>
<td>63</td>
</tr>
<tr>
<td>BNKT–2 mol% BCZ</td>
<td>25.0</td>
<td>0.30</td>
<td>549</td>
<td>63</td>
</tr>
<tr>
<td>$(\text{Ho},\text{Sr})$-modified (Bi$<em>{0.5}$Na$</em>{0.5})<em>{0.945}$Ba$</em>{0.055}$TiO$_3$</td>
<td>39.0</td>
<td>0.37</td>
<td>463</td>
<td>64</td>
</tr>
<tr>
<td>BNBT6.5–100rES, $x = 0.50%$</td>
<td>39.0</td>
<td>0.40</td>
<td>500</td>
<td>65</td>
</tr>
<tr>
<td>BNT–BKT–xBZT, $x = 0.02$</td>
<td>40.0</td>
<td>0.32</td>
<td>503</td>
<td>66</td>
</tr>
</tbody>
</table>

Fig. 8 Temperature dependence on polarization–electric field ($P$–$E$) hysteresis loops of the $(1 - x)[BNKT-0.03BSrT]_x$BFT ceramics where $x = 0-0.03$, measured under an electric field of 50 kV cm$^{-1}$ and a frequency of 1 Hz.

Fig. 9 Plots of (a) energy storage density ($W$) and (b) energy storage coefficient ($\eta$) as a function of temperature of the $(1 - x)[BNKT-0.03BSrT]_x$BFT ceramics.
et al. also studied the temperature dependence of $P$-$E$ hysteresis loops of the lead-free $(1-x)[0.8Bi_{1/2}Na_{1/2}TiO_3-0.2Bi_{1/3}K_{1/3}TiO_3]$-$xBiMg_{2/3}Nb_{1/3}O_3$ ceramics. With increasing temperature, the $P_r$ and $E_m$ values decrease gradually while $P_{max}$ slight changed and the $P$-$E$ hysteresis loop showed severe pinches. This indicated the presence of an ergodic relaxor (ER) state, i.e. there exists a temperature-caused ferroelectric-to-relaxor phase transformation in their work.

### Energy storage density

The polarization and dielectric breakdown strength are two important parameters related to the energy storage performance. As is known to all, the BNT–BKT ceramics with high $P_r$ of 34 $\mu$C cm$^{-2}$ and low breakdown field ($E_b \approx 50$ kV cm$^{-1}$) are difficult to a satisfactory characteristic for high energy storage applications. Therefore, the design of BNT–BKT energy storage materials with low $P_r$, large $P_{max}$ as well as the improvement of $E_b$ become two critical issues.

To evaluate the capability of the studied ceramics for energy storage applications, the energy storage density ($W$) was calculated from the $P$-$E$ hysteresis loop as shown in the following equation:

$$W = \int_E^{P_{max}} E dP,$$  \hspace{1cm} (3)

where $E$ is the electric field, $P$ the polarization, $P_{max}$ the maximum polarization, and $P_r$ is the remnant polarization. For practical applications, higher energy storage efficiencies ($\eta$) are required. The $\eta$ value is calculated by using the following formula:

$$\eta(\%) = \frac{W}{W + W_{loss}} \times 100,$$  \hspace{1cm} (4)

where $W_{loss}$ is the energy loss density. In this work, the energy storage density properties are summarized in Table 2. At RT, the $W$ and $\eta$ of the $x = 0$ ceramic are 0.20 J cm$^{-3}$ and 20.0%, respectively. In this composition, the high $E_r$ and low $P_{max} - P_r$ values are observed, which led to a low energy storage density, high energy loss, and low efficiency. The $x = 0.01$ ceramic with a pinched $P$-$E$ hysteresis loop shows relatively high $W = 0.37$ J cm$^{-3}$ and $\eta = 38.6\%$ values when compared with those observed for the $x = 0$ ceramic. This improvement can be related with the decreases in $P_r$, and slight invariant $P_{max}$ with the degradation of the long range FE order and a relatively easy reorientation of the micro-domains. The $W$ and $\eta$ values increase with increasing BFT content and exhibit the maximum values of 0.49 J cm$^{-3}$ and 60.7% at the electric field of 5 kV mm$^{-1}$ for the $x = 0.03$ ceramic. These values are also higher than the value obtained for the $x = 0$ sample by $\sim 145\%$ and 203%, respectively. In addition, the $W$ and $\eta$ values as a function of temperature of the $(1-x)[0.03Bi_{0.5}Na_{0.5}TiO_3]$-$xBFT$ ceramics are presented in Fig. 9. It can also be seen that the $W$ and $\eta$ increase with increasing temperature for all compositions and reach the maximum value of $\sim 0.65$ J cm$^{-3}$ and 90.4% at 120 $^\circ$C for the $x = 0.03$ ceramic. These obtained $W$ values are close to the value obtained in $Bi_{0.48}La_{0.02}NKTZ$ ceramics ($W \sim 0.63$ J cm$^{-3}$, at RT) as reported by Butnoi et al.

A comparison of normalized energy storage density ($W/E$) with the previous reports is presented in Table 7. The comparison of $W/E$ value with previous results clearly shows the superiority of this composition ($x = 0.03$) in terms of high $W/E = 0.13$ $\mu$C mm$^{-2}$ and $\eta = 90.4\%$. The obtained $W/E$ value is high for Bi-based piezoelectric ceramics. Based on the obtained results, it is suggested that these synthesized ceramics are promising materials for actuator, high electric power and energy storage applications.

### Conclusions

In this work, the BNKT–0.03BnT doped with BFT ceramics have been successfully synthesized by a solid-state mixed oxide method. The coexistence of rhombohedral and tetragonal phases is present throughout the entire compositional range, while a dominant tetragonal-rich phase is observed at a higher BFT content. The $x = 0.01$ ceramic shows the high $S_{max}$ of 0.42%, $d_33$ of 840 pm V$^{-1}$, and high $Q_{33}$ of 0.0404 m$^3$/C$^{-2}$ (at RT) with a very high $Q_{33}/E$ (8.08 $\times 10^{-9}$ m$^3$ C$^{-2}$ V$^{-1}$). The maximum
energy storage density \((W = 0.65 \text{ J cm}^{-3} \text{ @ 120 °C})\) and energy storage efficiency \((\eta = 90.4\% \text{ @ 120 °C})\) with large improvements are obtained for the \(x = 0.03\) ceramic. The studied results indicate that BFT enhances the electric field-induced strain, electrostrictive coefficient and energy storage density performances in BNKT-based ceramics. These ceramics can be considered promising candidates for actuator and high electric power pulse energy storage applications.

**Conflicts of interest**

There are no conflicts to declare.

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**References**