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Strong interfacial interactions induced a large reduction in lateral thermal conductivity of transition-metal dichalcogenide superlattices

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van der Waals heterostructures formed by vertically stacking two-dimensional (2D) crystals can not only harness the already fascinating properties of their constituent monolayers but also extend them due to the coupled interlayer interactions. With their emerged interlayer and intralayer excitons, 2D transition metal dichalcogenides (TDMC) crystals and their heterostructures have drawn growing attention for the applications of nanoelectronics, optoelectronics and nanophotonics. Yet, there are few studies on how interlayer and interfacial interactions influence the thermal transport in TDMC heterostructures which is critical for heat management. In this work, we investigate the lateral and out-of-the-plane thermal conductivity (κ) of four prototype TDMC heterostructures (bilayer MoS_2 and WS_2 , heterobilayer MoS_2/WS_2 and superlattice MoS_2/WS_2) by solving the phonon Boltzmann transport equation from first-principles. The calculated room-temperature lateral κ of bilayer MoS_2 and WS_2 are $61.13 \text{ W m}^{-1} \text{ K}^{-1}$ and $87.52 \text{ W m}^{-1} \text{ K}^{-1}$, respectively, in reasonable agreement with literature experiments. The weak interlayer interactions in the heterobilayer MoS_2/WS_2 help preserve the high lateral thermal transport ($70.01 \text{ W m}^{-1} \text{ K}^{-1}$) of its constituent monolayer. In the superlattice MoS_2/WS_2 , there exist strong interlayer and interfacial interactions between the alternating MoS_2 and WS_2 monolayer which reduce the lateral κ to be $7.22 \text{ W m}^{-1} \text{ K}^{-1}$ by a factor of 10. The greatly reduced lateral κ of the superlattice mainly arises from the low phonon relaxation time, which indicates the existence of strong interfacial anharmonic phonon scattering. This work aims at uncovering the physics of emerged thermal transport properties in TDMC heterostructures and helps advance their applications in heat management among nanoelectronics and optoelectronics.

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1. Introduction

With their unique combination of direct bandgaps, atomic-scale thickness, strong light-matter interactions and spin-orbital coupling, and favorable mechanical properties, two-dimensional (2D) transition metal dichalcogenides (TDMC) have become the emerging class of materials for applications in next-generation nanoelectronics, spintronics and nanophotonics.^{1–7} Considerable efforts have enabled the robust growth of heterostructures and superlattices from 2D TDMCs with predetermined attributes and functionalities.^{8–12} Held together by van der Waals forces, different TDMC layers with diverse properties vertically stack on each other and their quantum states interact and couple to one another, which could generate fascinating electrical, optical and thermal properties in 2D heterostructures and superlattices.^{13–16}

Among those properties, exploring thermal transport in the 2D TDMC heterostructures and superlattices is not only of fundamental physics interest but also crucial to advance heat management for their applications in nanoelectronics and

optoelectronics. Using a refined optothermal Raman technique, Zhang and co-workers¹⁷ measured the lateral thermal conductivity (κ) and interfacial thermal conductance of suspended single and bilayer MoS_2 and MoSe_2 at room temperature. By analyzing the temperature and excitation dependences of active Raman modes, Peimyo *et al.*¹⁸ determined the lateral κ of suspended single and bilayer WS_2 . Using classical molecular dynamics, Zhang and co-workers¹⁹ calculated the lateral κ of heterobilayer $\text{MoS}_2/\text{MoSe}_2$ and showed that it preserved the high thermal conductivity of most 2D TDMC materials. Moreover, the interfacial interactions had little influence on the lateral thermal performance. Those studies greatly advance the understanding of thermal transport in 2D TDMC and the related heterostructures. Yet to modulate and engineer thermal transport in the 2D TDMC heterostructures with a higher precision, it requires a sound knowledge on phonon transport in 2D TDMCs and how the vertically stacking TDMCs layers influence the quantum behaviors of phonons.

In this work, we choose four prototype TDMCs, bilayer MoS_2 and WS_2 , heterobilayer MoS_2/WS_2 and superlattice MoS_2/WS_2 , and investigate their lateral and out-of-the-plane κ using first-principles calculations without empirical parameters. By analyzing anharmonic lattice dynamics coupled with the Boltzmann transport theory, the calculated lateral κ of bilayer

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MoS₂ and WS₂ agree with previous experiments. In comparison, the lateral κ of heterobilayer MoS₂/WS₂ preserves the high values of bilayer MoS₂ and WS₂, and the interlayer van der Waals forces has little influence on it. By comparing heterobilayer and superlattice MoS₂/WS₂, it shows that the strong interfacial interactions in the superlattice greatly affect the lateral κ of heterobilayer and reduce it by a factor of 10.

II. Computational methodology

The 2D TDMC semiconductors exhibit 2H symmetry with the general formula MX₂, where M = Mo, W; X = S, Se and Te. In Fig. 1, the lattice structures of bilayer MoS₂ and WS₂, heterobilayer MoS₂/WS₂ and superlattice MoS₂/WS₂ are presented. After structure optimization, the thickness of bilayer MoS₂ and WS₂ and heterobilayer MoS₂/WS₂ is 0.9605 nm, 0.9633 nm and 0.9622 nm, respectively. To avoid the interlayer van der Waals interaction, one 1 nm-thick vacuum layer was introduced. The relaxed lattice parameter for the superlattice MoS₂/WS₂ was a (b) = 0.3281 nm and c = 1.2986 nm. After performing the phonon dispersion relation calculations, the nonexistence of imaginary phonon modes indicates the dynamic stability of those TDMCs structures.

In 2D TDMC semiconductors, the thermal transport is dominated by the free carriers of phonons whose transport capacities are mainly limited by the intrinsic phonon-phonon

interaction.^{20–22} According to Boltzmann transport theory, κ is determined by^{23,24}

$$\kappa = \frac{1}{N\Omega} \sum_{q\nu} C_{q\nu} v_{q\nu}^2 \tau, \quad (1)$$

where N is the total number of q points in the first Brillouin zone, Ω is the volume of unit cell, $C_{q\nu}$, $v_{q\nu}$ and τ is the specific heat, group velocity and phonon relaxation time, respectively. Within the three-phonon scattering scheme, the key parameter τ determining thermal transport capability is given by^{25,26}

$$1/\tau = \frac{2\hbar\pi}{N} \sum_{q'v'q''v''} \left| V_{q\nu q'v'q''v''}^{\pm} \right|^2 (n_0 + 1) \left(n_0' + 1/2 \pm 1/2 \right) n_0'' \delta \left(\omega_{q\nu} \pm \omega_{q'v'} - \omega_{q''v''} \right), \quad (2)$$

where n_0 is the Bose–Einstein distribution statistics of phonons and the delta function δ ensures energy conservation during phonon scattering process. The V^{\pm} is the relevant three-phonon scattering matrix and determined by^{25,26}

$$V_{q\nu q'v'q''v''}^{\pm} = \sqrt{\frac{1}{8\omega_{q\nu}\omega_{q'v'}\omega_{q''v''}}} \sum_i \sum_{j,k} \sum_{\alpha\beta\gamma} \Phi(R_i^{\alpha}, R_j^{\beta}, R_k^{\gamma}) \times \frac{e_{q\nu}^{\alpha}(i) e_{\pm q'v'}^{\beta}(j) e_{-q''v''}^{\gamma}(k)}{\sqrt{M_i M_j M_k}}, \quad (3)$$

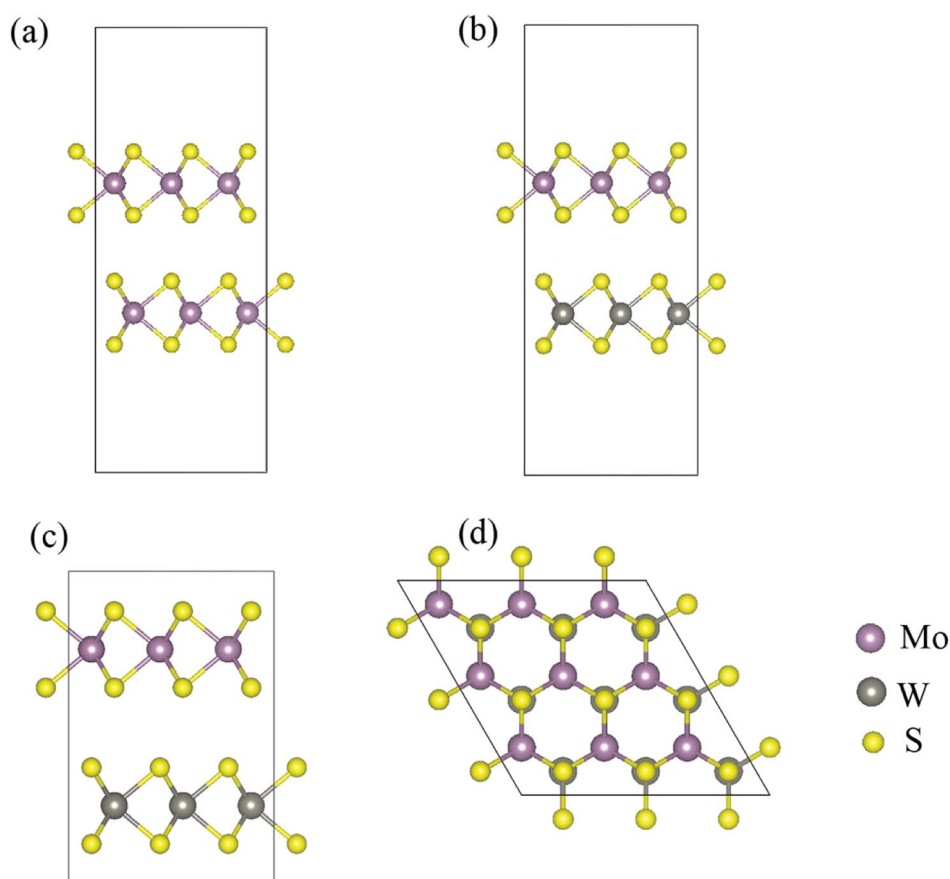


Fig. 1 The side view of bilayer (a) MoS₂, (b) heterobilayer MoS₂/WS₂, (c) superlattice MoS₂/WS₂ and (d) top view of TDMC heterostructures.



where M is the corresponding mass, R is the position for atoms i, j and k in the simulated cell, Φ is the third-order interatomic force constant (IFC), and e is the normalized eigenfunction and α, β , and γ denote the Cartesian coordinates. To calculate V^{\pm} , it requires the harmonic interatomic force constants to obtain phonon dispersion relation and eigenvectors and third-order IFCs. To calculate the harmonic and third-order IFCs, we built a $5 \times 5 \times 1$ supercell containing 150 atoms and applied the finite-difference approach.²⁷ During the calculation of third-order IFCs, the 8th nearest neighbor was chosen and the cutoff radius was 0.65 nm.

To calculate the harmonic and third-order IFCs, we employed the Vienna ab initio simulation package (VASP)²⁸ which uses the projector augmented wave (PAW) method.²⁹ The Perdew–Burke–Ernzerhof (PBE)^{30,31} exchange–correlation functional was adopted and the vdW-DF2 functional³² was included to calculate the van der Waals forces. The Brillouin-zone integration was computed with the $12 \times 12 \times 1$ ($12 \times 12 \times 12$ for superlattice) Monkhorst–Pack k -mesh³³ and the cutoff energy was 600 eV. For the structural relaxation, the force convergence threshold was set as $0.1 \mu\text{eV} \text{ \AA}^{-1}$. After collecting the harmonic and third-order IFCs, the phonon relaxation time and thermal conductivity were computed with the ShengBTE package.²⁵ The automatically generated $20 \times 20 \times 1$ ($20 \times 20 \times 20$ for the superlattice) q grid was employed and the Gaussian smearing with breadth of 1 was applied.

III. Results and discussions

Phonon dispersion relation

Prior to computing thermal conductivity of TDMC heterostructures, it is essential to understand their quantum behaviors of phonons. In Fig. 2, the phonon dispersion relations and projected density of states (PDOS) of bilayer MoS₂ and WS₂, heterobilayer MoS₂/WS₂ and superlattice MoS₂/WS₂ are presented and compared. Since van der Waals (vdW) forces hold the TDMC layers together in the above heterostructures, the inclusion of vdW functional for the force calculations helps stabilize the bilayer, heterobilayer and superlattice heterostructures and eliminate the imaginary phonon modes. Due to the same 2H symmetry in lattice structure, there exists large similarity in the phonon dispersion relation of bilayer MoS₂ and WS₂ except that bilayer MoS₂ has relatively higher phonon frequencies. That is because the mass of Mo (95.94 amu, 1 amu = 1.660539×10^{-27} kg) is much lighter than that of W (183.84 amu). By vertically stacking one MoS₂ layer on top of one WS₂ layer, the newly formed MoS₂/WS₂ heterobilayer still keeps the 2H symmetry and its phonon dispersion keeps the similar shape of bilayer MoS₂ and WS₂. However, the phonon degeneracy is decreased and more phonon modes are generated, which is mainly caused by the coupled quantum states between MoS₂ layer and WS₂ layer. By periodically alternating the MoS₂ and WS₂ layer, the superlattice MoS₂/WS₂ is built. By comparing

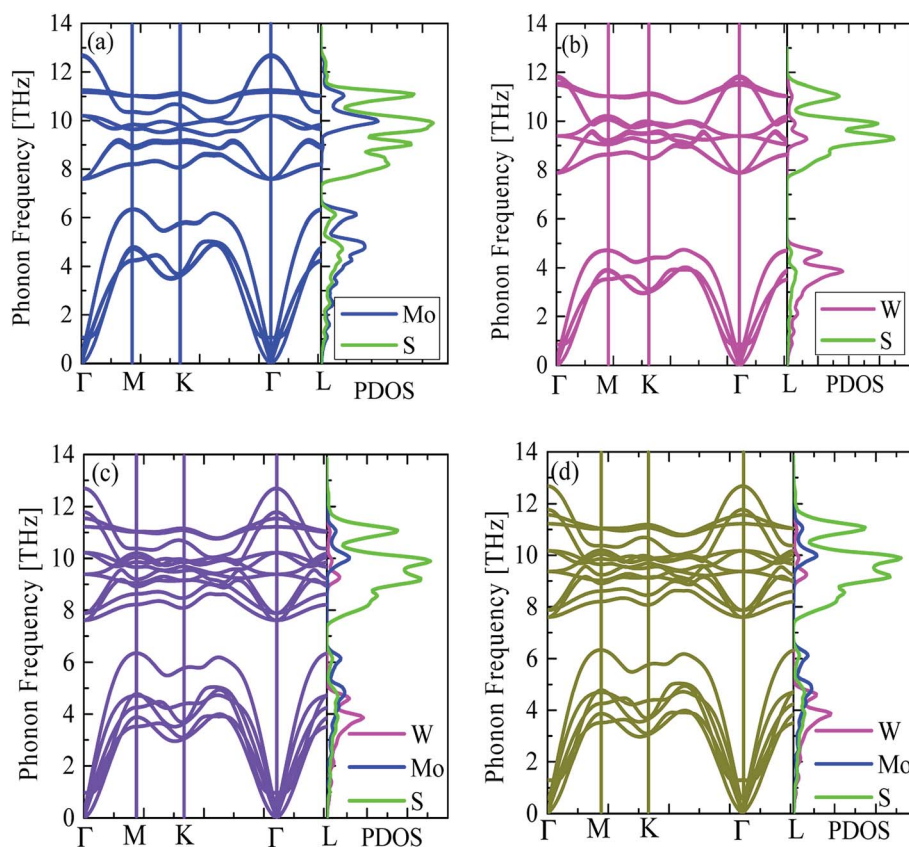


Fig. 2 Phonon dispersion relation and projected phonon density of states (PDOS) of bilayer (a) MoS₂, (b) WS₂, (c) heterobilayer MoS₂/WS₂ and (d) superlattice MoS₂/WS₂.



the heterobilayer and superlattice MoS₂/WS₂, it finds that their phonon dispersion relations along the lateral direction are the same and interlayer van der Waals forces don't affect the lateral phonon dispersions.

Lateral thermal conductivity

In Fig. 3(a), the calculated lateral κ of bilayer MoS₂ and WS₂, heterobilayer MoS₂/WS₂ and superlattice MoS₂/WS₂ are presented and compared with literature experimental data, in order to study the influence of interlayer interactions on lateral thermal transport. By only considering the phonon-phonon interaction, the calculated lateral κ of bilayer MoS₂ at 300 K and 500 K is 61.13 W m⁻¹ K⁻¹ and 36.77 W m⁻¹ K⁻¹, respectively, in good agreement with the measured value of 77 ± 25 W m⁻¹ K⁻¹ and 29 ± 10 W m⁻¹ K⁻¹.¹⁷ For the bilayer WS₂, the calculated lateral κ at 300 K is 87.52 W m⁻¹ K⁻¹, relatively higher than the measured value of 53 W m⁻¹ K⁻¹.¹⁸ This difference may be caused by the neglect of electron-phonon interaction (EPI)

which shows strong effect in the few-layer WX₂ (X = S, Se and Te) crystals.^{34–36} Yet the neglect of EPI calculations which require heavy computing resources does not affect our conclusion about the influence of interlayer interactions on lateral κ . By comparing the bilayer MoS₂ and WS₂, heterobilayer MoS₂/WS₂, it shows that the lateral κ lies between that of bilayer MoS₂ and WS₂ and preserves the high thermal performance, indicating that the interlayer van der Waals force in the heterobilayer MoS₂/WS₂ does not affect the lateral κ . However, in the superlattice MoS₂/WS₂ with alternating MoS₂ and WS₂ monolayer, the interlayer van der Waals forces has a strong effect and reduces the room-temperature lateral κ of heterobilayer MoS₂/WS₂ from 70.01 W m⁻¹ K⁻¹ to 7.22 W m⁻¹ K⁻¹ by a factor of 10.

To interpret such large reduction in lateral κ , we further compare the calculated τ and averaged square group velocity ($\langle v^2 \rangle$) which are the two relevant parameters dominating lateral thermal transport. In Fig. 4(a), by analyzing the cumulative lateral κ with phonon frequency, it shows that the propagating phonons mainly (more than 90%) contributing to the lateral thermal transport lie in the energy range of 1–5 THz. In Fig. 4(b), by comparing τ in the energy range of 1–5 THz, it observes that the calculated value of superlattice MoS₂/WS₂ is one order of magnitude lower than that of bilayer MoS₂ and WS₂ and heterobilayer MoS₂/WS₂. On the other hand, there is little difference in the calculated $\langle v^2 \rangle$ along the lateral direction in the energy range of 1–5 THz, as shown in Fig. 4(c). Therefore, it can conclude that the low τ leads to the greatly reduced lateral κ of the superlattice MoS₂/WS₂, compared with the heterobilayer. The low τ means the existence of strong phonon-phonon interaction in the superlattice. To explain it, we first analyze the lattice structures. The structural difference between superlattice and heterobilayer MoS₂/WS₂ is that there exists periodically alternating MoS₂ and WS₂ monolayer in the superlattice, while in the heterobilayer there is a large vacuum layer on top of MoS₂/WS₂. The periodically alternating MoS₂ and WS₂ monolayer introduce large van der Waals forces and induce strong interactions. This will bring large restoring forces for atoms and lead to large group velocity. In Fig. 4(d), the calculated $\langle v^2 \rangle$ of superlattice MoS₂/WS₂ along the out-of-the-plane direction is eight orders of magnitude larger than that of heterobilayer, which justifies the existence of strong interlayer interactions in the superlattice. Furthermore, the analysis of charge density distribution in Fig. 5 shows that there is a relatively large interlayer charge density along the out-of-the plane direction in the superlattice, while in the heterobilayer there is no interlayer charge density due to the existence of vacuum layer. The existence of interlayer charge density in the superlattice can help explain the strong interlayer interactions. On the other hand, in the alternating MoS₂ and WS₂ layer of neighboring unit cell in the superlattice, there exists large charge density around Mo and W atoms, respectively, which would induce the strong interfacial interactions as shown in Fig. 5. The interfacial interactions can enhance the anharmonic scattering among propagating phonons along the plane direction and thus reduce the lateral κ . To peer more microscopic insights on the interfacial interactions of superlattice MoS₂/WS₂, one can analyze the kinetic diffusion and collision process among lateral and

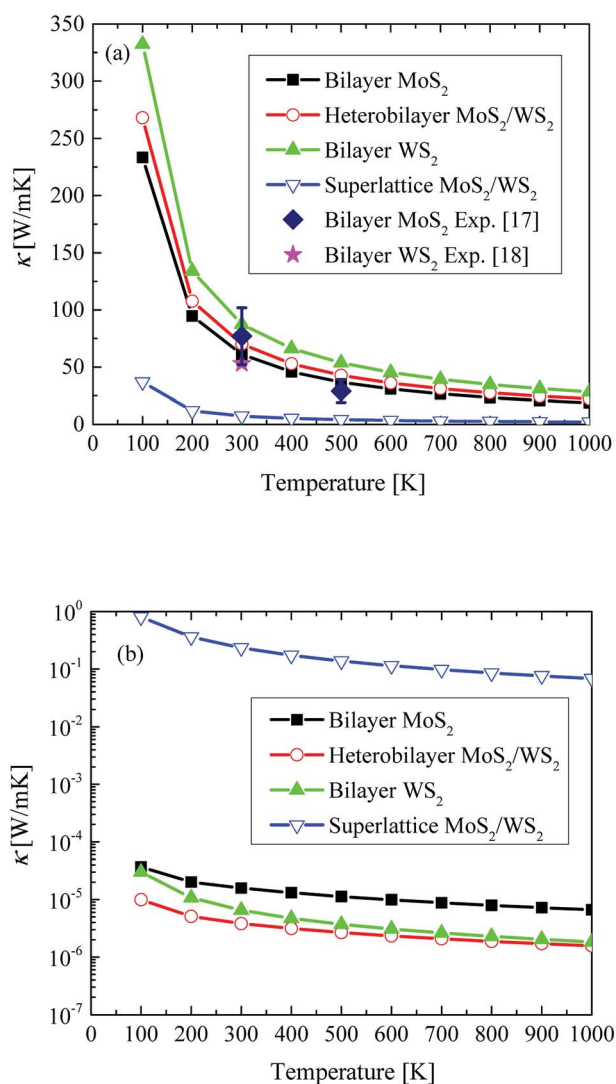


Fig. 3 The calculated (a) lateral and (b) out-of-the-plane κ of bilayer MoS₂ and WS₂, heterobilayer MoS₂/WS₂ and superlattice MoS₂/WS₂, in comparison with literature data of ref. 17 and 18.



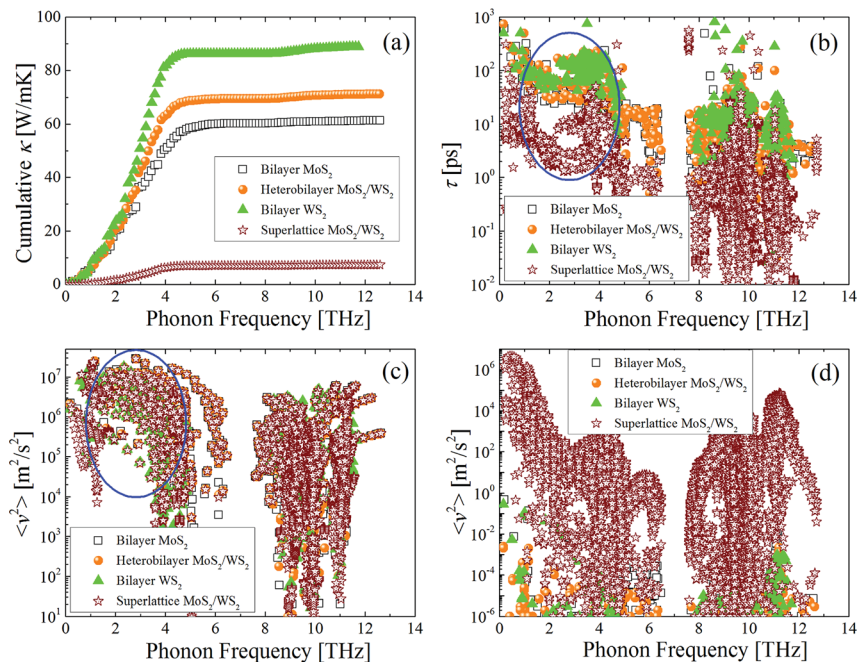


Fig. 4 The (a) cumulative lateral κ , (b) phonon relaxation time, (c) and (d) averaged square group velocity along lateral and out-of-the-plane direction, respectively, of bilayer MoS_2 and WS_2 , heterobilayer MoS_2/WS_2 and superlattice MoS_2/WS_2 . The blue ellipse pinpoints the major propagating phonons between 1–5 THz.

flexural phonon modes using the phonon wave-packet dynamics method.³⁷ It would require the separation of lateral and flexural phonons but it is beyond the capability of present method.

Out-of-the-plane thermal conductivity

For the 2D TDMC heterostructures, the interfacial (out-of-the plane) thermal conductance is of great importance for the

heat management. In Fig. 3(b), the out-of-the-plane κ of bilayer MoS_2 and WS_2 , heterobilayer MoS_2/WS_2 and superlattice MoS_2/WS_2 are presented. With its nanometer thickness, the room-temperature out-of-the-plane κ of bilayer MoS_2 and WS_2 and heterobilayer MoS_2/WS_2 is limited to be $1.58 \times 10^{-5} \text{ W m}^{-1} \text{ K}^{-1}$, $6.52 \times 10^{-6} \text{ W m}^{-1} \text{ K}^{-1}$ and $3.86 \times 10^{-6} \text{ W m}^{-1} \text{ K}^{-1}$, respectively. It shows that the vertically stacking MoS_2 and WS_2 monolayer do not influence the interfacial thermal

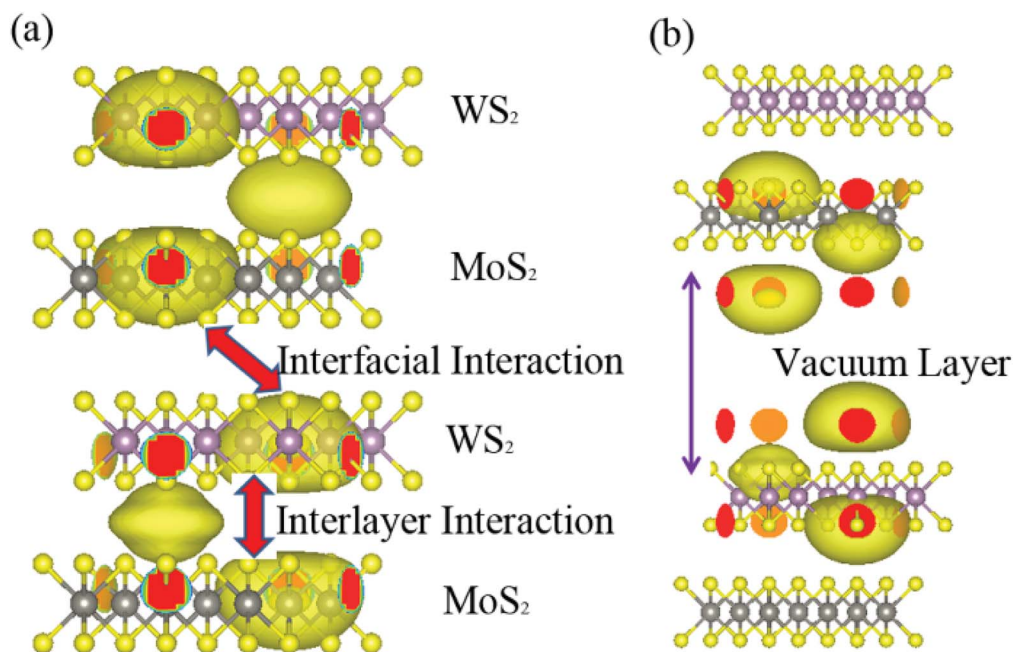


Fig. 5 Charge density distribution of (a) superlattice and (b) heterobilayer MoS_2/WS_2 .



conductance. By periodically alternating MoS₂ and WS₂ monolayer with strong interlayer interactions, the room-temperature out-of-the-plane κ of superlattice MoS₂/WS₂ is increased to be 0.23 W m⁻¹ K⁻¹ and 5 orders of magnitude larger than that of heterobilayer.

IV. Conclusions

In summary, we have calculated four prototype TDMC heterostructures (bilayer MoS₂ and WS₂, heterobilayer MoS₂/WS₂ and superlattice MoS₂/WS₂) and investigated their lateral and out-of-the-plane κ from first-principles. By analyzing the anharmonic lattice dynamics coupled with solving the phonon Boltzmann transport equation, the calculated lateral κ of bilayer MoS₂ and WS₂ at 300 K is 61.13 W m⁻¹ K⁻¹ and 87.52 W m⁻¹ K⁻¹, respectively, in reasonable agreement with experimental data of 77 ± 25 W m⁻¹ K⁻¹ and 53 W m⁻¹ K⁻¹. By vertically stacking the MoS₂ and WS₂ monolayer together and applying a nanometer-sized vacuum layer on its top, the heterobilayer MoS₂/WS₂ forms and it preserves the high lateral κ of 70.01 W m⁻¹ K⁻¹ at 300 K, which indicates that the weak interlayer interactions do not affect the lateral thermal transport. Moreover, the coupled quantum states of vertically stacking MoS₂ and WS₂ monolayer do not influence the out-of-the-plane κ . For the superlattice composed of periodically alternating MoS₂ and WS₂ monolayer, the charge density distribution analysis shows that there exist strong interlayer and interfacial interactions. Consequently, the interfacial anharmonic phonon scattering is enhanced and phonon relaxation time is greatly decreased for the propagating phonons, leading to a significant reduction of lateral κ from 70.01 W m⁻¹ K⁻¹ to 7.22 W m⁻¹ K⁻¹ almost by a factor of 10. This work shows that the strong interfacial interactions indeed influence the lateral thermal transport in the superlattice MoS₂/WS₂. The physical insights obtained from this work can help predict the thermal transport in other TDMC heterostructures and advance the thermal management in their applications in nanoelectronics and optoelectronics.

Conflicts of interest

There are no conflicts to declare.

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