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Reaction and characterisation of a two-stage thermoset using molecular dynamics
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The two-stage curing reaction of unsaturated polyester polyurethane hybrid resins is modelled using all-atom molecular dynamics simulations. The reactions – a urethane reaction and a radical polymerisation – are modelled based on atom distances and probabilities calculated by an Arrhenius law, without the need for intermediate minimisation steps. As representatives of this thermoset class two resin systems are considered. First, a simple virtual resin with just enough structure to be capable of the described reactions is used to verify the reaction process. Second, a system is studied which is designed to be similar to a commercially available hybrid resin used in conjunction with fibre reinforcements. Both systems are simulated and the results are used to evaluate the chemical reaction process and then to identify the resulting material’s macroscopic properties and behaviour. These properties are determined at different cross-linking stages of the curing process providing a unique insight into the development of these parameters during the chemical reaction.

1 Introduction

Unsaturated polyester polyurethane hybrid (UPPH) resins, a relatively new thermoset class, combine the strengths of unsaturated polyester (UP) and polyurethane (PU) technologies.1 The chain-forming urethane polyaddition gives the cured resin flexibility and toughness, while the follow-up UP-based radical polymerisation leads to a three-dimensional cross-linked network resulting in stiffness and temperature resistance. A key motivation for the development of these advanced resin systems is their suitability for application in the progressively expanding use of fibre-reinforced polymers (FRP) in high performance applications within the aerospace, automotive and energy sector. From a macroscopic view point, reinforcing fibres with diameters in the micrometer range are common,2,3 e.g. glass or carbon fibres, but there is also extensive research on improving the structural performance of a polymer by introducing reinforcements on a nano-scale,4–8 e.g. nano-fibres. In conjunction with short cycle times, control and prediction of the curing reaction becomes fundamental to enhance the production process and to guarantee product quality. The relevance of understanding the curing process arises from its overall influence on the final material properties and behaviour.9 Hence, identification of material properties during this process is a necessary task. Performing an experimental characterisation during an active curing process poses a difficult challenge. This is why simulative determination of developing material properties becomes desirable.

Molecular dynamics (MD) simulations are a computational method that follows motion on an atomic level and is free from many experimental constraints that make material characterisation difficult. From its origins by Alder and Wainwright10–12 MD has developed into a widely used simulation technique in physics, chemistry, and biology. With ever growing computational power, engineering fields are also becoming more and more involved with MD, mainly to support experiments and to better understand material behaviour.

Early work on simulating thermosts in MD was done by Barton et al.13,14 and Hamerton et al.,15 who investigated cross-linked or network-building polymers. In these works the three-dimensional network structures were generated artificially and the main focus lay on the prediction of mechanical and thermal behaviour. An improvement is found in the work of Doherty et al.,16 who presented MD simulations including the execution of a cross-linking process. Bond creation was allowed when reactive parts of the monomers or polymers moved within a certain distance of each other, which is still a common criterion in these kind of simulations. However, they did not analyse the resulting cross-linked polymer in that...
work. Among others, Yarovsky and Evans,17 Heine et al.18 and Wu and Xu19 combined the simulative cross-linking and the follow-up calculation of material properties of a cured thermoset was published by Li et al.20,21 A recent development in bond creation criteria is the utilisation of an Arrhenius type equation. Okabe et al.22,23 introduced this probabilistic feature to account for activation energies in the cross-linking process and used it in addition to the distance criterion. Research on the effect of varying water content on curing rate and the glass transition temperature was done by Sharp et al.24 Work on thermo-mechanical properties includes Gao et al.,25 who studied the impact of two differently cured epoxy resins on material characteristics, and Saiev et al.,26 who investigated the behaviour of polybenzoxazine thermosets.

In this paper, recently developed bond creation algorithms are applied to the two-stage curing reaction of UPPH resins. In particular, the distance criterion as well as an Arrhenius type equation is used to form new bonds, which is done on-the-fly without intermediate minimisation steps during a regular MD simulation run. The reaction algorithms furthermore were modified to capture the individual reaction steps, namely a urethane reaction and a radical polymerisation. The new algorithms are applied to the hybrid resin systems, whose partially and fully cured states are then analysed. The main goal is to characterise the thermoset through derivation of macroscopic material properties. Firstly, a simplified and virtual example of the hybrid resin class is examined before a more specific example similar to a commercially available virtual example of the hybrid resin class is examined before a

The paper is organised as follows: in section 2 the resin system we investigate is described, which is followed by the applied models and algorithms in section 3. Before discussing the results of the simulations in section 5, the setup of specific systems is given in section 4. In section 6 the findings are summarised and conclusions drawn.

2 Resin system

UPPH resins are mixtures of resins blended with the goal of combining advantages and overcoming disadvantages of their single components and technologies: PU gives the cured resin flexibility and toughness while UP provides stiffness and thermal resistance. For a further discussion the reader is referred to Verleg and Hummer.1

Generally, UPPH resins consist of isocyanate, unsaturated polyester and peroxide molecules, which enable the resin to perform two reactions: a urethane polyaddition reaction and a radical polymerisation. The isocyanate molecules often come in the form of (poly-)methylene diphenyl diisocyanates ([P]-MDI, see Fig. 1a), which are typical for polyurethane formation. UP is usually cut with styrene (see Fig. 1b), both containing carbon double bonds for a radical cross-linking reaction. To enable the resin to form polyurethane chains, the UP molecules also have hydroxyl groups. Additionally, a small amount of the hybrid resin is peroxide molecules (see Fig. 1c), which are needed solely to initiate the radical polymerisation. In general, ([P]-MDI and UP can appear not only with different lengths but also differing numbers of functional groups. In the following the reactions of the two-stage resin system are described.

2.1 Polyurethane reaction

Once all components are mixed together (see Fig. 2a) the polyurethane reaction is initiated at room temperature. On a molecular scale the isocyanate groups of the ([P]-MDI react with the hydroxyl groups of the UP.

This leads to the formation of long polyurethane chains (see Fig. 2b) stretching across wide areas of the resin. On a macro-scale this results in the thickening of the resin which changes from a fluid to a gum-like consistency. When used with fibres to form a fibre-reinforced polymer (FRP), these have to be placed in the resin during this step. In this semi-finished state the thickened sheets may be stored several weeks before further processing.

2.2 Radical polymerisation

Upon heating the (thickened) resin above 60 °C, the peroxide O–O bonds start to cleave. This leaves the oxygen atoms electrophilic and starts a radical polymerisation process, in which they move to nucleophile centres, namely the unsaturated carbon double bonds of the (now) polyurethane chains and the styrene. After breaking a carbon double bond and establishing a new bond between the oxygen and one of the carbon atoms, the left over carbon atom becomes electrophilic itself and continues the radical reaction (see Fig. 2c). The chain propagates until it is terminated by the radical tip of another chain, which means that the tips of two cross-link branches form a bond, thereby stopping and finalising the reaction in these branches. De facto, the reaction also comes to a halt when there are no carbon double bonds left within reach. At the end of the process, the polyurethane chains are three-dimensionally cross-linked by styrene chains leading to a rigid polymer network.
On a macro-scale this process goes along with moulding: if the previously mentioned semi-finished sheets are used, these are placed in a pre-heated mould where they cure under pressure to produce the final shape. In this step the material develops its final material properties and behaviour.

2.3 Virtual resin system

To test our reaction process modelling and to provide a minimal example for the reader, a simple virtual resin system is introduced. This system is not based on a specific resin but

Fig. 2  (a) Resin system before any reaction, all components mixed, (b) schematic of the first reaction step, where isocyanate and hydroxyl groups form urethane connections (in violet) and (c) schematic of the second reaction step, where peroxide bonds break and initiate the radical polymerisation (in light grey), which cross-links the previously formed polyurethane chains with styrene molecules. The radical propagation depends on breaking unsaturated carbon bonds.
only serves as an illustrative example for the chemical reactions involved. Its simplicity provides a less computationally intensive system for simulation. Its molecules have the same functional groups and unsaturated carbon double bonds as the general hybrid resin class. For the molecules' structure rather simple backbones are assigned, even styrene is simplified to ethylene. The molecules involved and their structure are specified in Table S1.† The number of functional groups is kept consistent with the commercial resin described in section 4 to guarantee a certain comparability, but for convenience the functionality of the (P-)MDI is reduced to 2 (cf. Table 2). Therefore the reactions stay the same. The general composition of the virtual resin system used for simulation is specified in Table 1, which is derived from the weight fractions listed in Table 3.

The composition is given as unit composition, i.e. number of molecules as the smallest whole numbers possible regarding the compound composition, and each constituent is monodisperse. This composition is the basis for the simulation setup of the virtual resin system.

2.4 System based on a commercial hybrid resin

A representative of the type of two-stage hybrid resin we would like to model is DARON® AQR 1009, which is commercially available from ALIANCYS AG. This resin system consists of three components: A (P-)MDI in the form of LUPRANATE® M 20 R, available from BASF SE, DARON® AQR 1009, a UP dissolved in styrene available from ALIANCYS AG and which is also the name giving component to the resin system, and TRIGONOX® C, an organic peroxide for initiating radical polymerisation available from AKZO NOBEL N.V.

For all three components there is no chemical data sheet disclosed or information publicly available. Hence the authors do not know the exact chemical structure of the molecules involved so are forced to come up with chemical structures consistent with the available information. This choice is not unique. A few properties and structural information which are provided by ALIANCYS AG are listed in Table 2.

Schematics of the molecular structure used in the simulations are given in Fig. 1. While this is based on an educated guess of the structure of DARON® AQR 1009, we emphasise that while the schematic is consistent with what we do know there are ambiguities in the available data that necessitated filling in unknown details. As a result, there may be some material properties that we measure in our system that may differ somewhat from the actual commercial resin. Based on the available information, we surmise that each UP molecule always has two hydroxyl groups. For (P-)MDI the non-integer functionality underlines that there has to be a range of molecules with a different amount of isocyanate groups, and the NCO equivalent weight indicates that each isocyanate group is connected to a part of the molecule's backbone which takes up an atomic weight of 135.0. There is no information on the organic peroxide, but as it only serves as an initiator for the radical polymerisation the structure is of less importance. From this information a compound consistent with this is calculated as presented in Table 3, which is used as the basis for the simulation setup for this resin system.

The derived composition is given in Table 1. The unit composition in the third column is the same as for the virtual resin, while the molecules of the main resin constituents are not monodisperse. Further details on this are found in ESI section I and Table S2.†

3. Model and algorithms

The models described in this section are implemented in the open source MD code LAMMPS27,28 (acronym for Large-scale Atomic/Molecular Massively Parallel Simulator). Reaction algorithms presented in section 3.2 are built upon LAMMPS fixes bond/create and bond/break. These fixes were then modified making use of the work of Timothy Sirk (e.g. Jang et al.29). We then made some additional changes to accommodate all the reactions as described below.

3.1 Molecule description

The behaviour of all atoms in the system is governed by the COMPASS force-field.30–32 It is composed of intra- and inter-
molecular potentials and depends on relative atom positions \( r_{ij} \) and their combinations as bond length \( \rho_{ij} \), angle \( \varphi_{ijk} \), dihedral or torsion angle \( \chi_{ijk} \) and out-of-plane angle \( \chi_{ijk} \), where the indices indicate the involved atoms. The total potential function may be written as

\[
E_{\text{tot}} = E_{\text{bonds}} + E_{\text{angles}} + E_{\text{dihedrals}} + E_{\text{impropers}}
+ \frac{E_{\text{bond-bond}}}{r_{12}^6} + \frac{E_{\text{bond-angle}}}{r_{12}^3}
+ E_{\text{middle-bond-torsion}} + E_{\text{end-bond-torsion}} + E_{\text{angle-torsion}}
+ E_{\text{angle-angle-torsion}} + E_{\text{bond-bond-11-torsion}}
+ E_{\text{angle-angle}} + E_{\text{endW}} + E_{\text{Coulomb}}.
\] (1)

The intra-molecular or valence potentials have cross-coupling terms provided and include all terms except for \( E_{\text{endW}} \) and \( E_{\text{Coulomb}} \). These are the inter-molecular or non-bonded interaction terms, which may also act on distant atoms of the same molecule. The van der Waals interactions are modelled by a Lennard-Jones (L-J) \( 9-6 \) potential while the coulombic potential controls the electrostatic behaviour. The expanded form of eqn (1) and further information on the COMPASS force-field are given in ESI section II. Additional details and the parameters involved for the force-field can be found in the work of Sun et al.\(^{30-32} \) A small number of potentials were not parametrised in the referenced literature. In these cases they have potentials assigned from as closely matching atoms as possible (potentially atoms of the same group in the periodic table). Mixed terms (e.g. terms mixing bond and angle potentials) are typically small and are set to zero if parameters are not available.

### 3.2 Reaction algorithms

Bonds can only be created if appropriate reaction partners are in fairly close proximity. Exploiting this, a distance criterion helps in preselecting reactive groups that move closer than a specified cut-off distance, e.g. as described in Dohery et al.\(^{16} \)

In general, this cut-off distance is chosen as the maximum distance at which bond formation is presumably still possible from an energetic point of view. With this simple, but quite rigid, criterion considerable computational effort can be saved by applying advanced reaction algorithms only to these preselected reactive groups within a promising distance. Generally, we extend this criterion by an Arrhenius type function based on arguments similar to Okabe et al.\(^{22,23} \) and modify the process of bond formation. We elaborate below on this approach for each distinguishable chemical process of peroxide bond dissociation and polyurethane as well as radical bond formation.

Firstly, the bond dissociation procedure is described. Pseudo-code is given in Algorithm S1.\(^{†} \) Whenever the system temperature \( \Theta \) rises above a threshold temperature \( \Theta_{\text{min}} \), all bonds are checked to see if their type is allowed to break. Each of these eligible bonds draw a random number between zero and one (probability \( P \)) and compare it to a bond-specific calculated threshold fraction. The calculation of this fraction is based on the Arrhenius equation

\[
F = \exp \left( \frac{-\Delta E}{k_B \Theta} \right),
\] (2)

where \( k_B \) is the Boltzmann constant and \( \Delta E \) should mimic some kind of activation energy. Instead of actual activation energies, which would need a quantum-mechanical calculation to determine, we use \( \Delta E = E^b - E^a \) to dissociate the bond. Here, \( E^b \) is the potential energy of the bond and \( E^a \) is the energy at which the bond dissociates (e.g. see ref. 33–35 for values used in this work). Hence, if the bond is close to equilibrium length, its threshold fraction is barely below \( F = 1 \) and the bond has very little chance to break even at a drawn probability \( P \gg 0 \). With a higher temperature, the probability that a bond tends to stretch into an unnatural length is higher. This reflects in a higher bond energy \( E^b \), which leads to a lower threshold fraction \( F, P > F \) becomes more probable and when fulfilled the bond is broken. Whenever a bond is broken, the neighbourhood of the previously bonded atoms has to be updated according to the molecular description presented in section 1. This means angles, dihedral and impropers, which became void, are deleted from their respective lists to make the division of the molecule complete.

In a next step, the bond formation procedure is explained on the basis of the polyurethane reaction. A summary is available in the form of Algorithm S2.\(^{†} \) Each atom is checked to see whether it is part of a creatable bond. If this is true, its neighbourhoood is scanned for atoms with atom types that can complete the bond. After a suitable bond partner is found, two criteria have to be fulfilled to establish the bond. As a first criterion the aforementioned distance check is used to neglect partners too far apart. The second criterion draws a random number between zero and one and compares it against a fraction delivered by a Arrhenius type equation (same as used in the bond dissociation process). In contrast to breaking a bond, here we want the probability value to be lower than the Arrhenius value to ensure the bond is only established when the atoms are close to the new bond’s equilibrium distance. With this, unnatural bond stretches when forming the bond are avoided. Another aspect of this procedure is the handling of further atoms to be exchanged during the bond creation. In the case of the polyurethane reaction, \( cf. \) Fig. 2b, this deals with the hydrogen atom of the hydroxyl group, which is donated to the nitrogen atom of the isocyanate group. In general, the distance between these two atoms may be far from equilibrium upon forming the bond between the oxygen and carbon atom. To take care of this, we establish a transient bond between the hydrogen and the nitrogen. This means the bond is already in formation, but not fully established yet. In this state the two atoms are excluded from standard potentials but move closer by a Coulomb’s potential and an eased bond potential. With this a smooth and continuous transition of the hydrogen atom is ensured and unnaturally high forces are avoided. The transient bond is checked in the same Arrhenius type way as described above and is fully established as soon as the probability criterion is met by releasing it from the transient state. As before, after each change of the bonds, the molecular topology is updated with respective angles, dihedrals and improppers.

Lastly, additional measures for the radical reaction are discussed. Here, the basic approach is the same as for the poly-
urethane formation. When proceeding naturally, the chemical reactions can continue for several seconds before completion throughout a macroscopic sample. This is beyond the time scale of an MD simulation. Our reactions are sped up by the essentially perfect mixing (impossible to achieve in an experiment) of our starting state thus meaning a reaction partner is always fairly close. In addition, to mimic electrophile and nucleophile centres, in force calculations atom types belonging to this group receive an additional force component as described in Algorithm S3.† For this purpose a coulombic force is calculated exclusively acting between electrophile and nucleophile centres. Hence, these centres are preferably found by each partner thus taking care to produce a proper radical propagation. While physically motivated, this added force is of an artificial nature (it is not fit from anything other than to result in the correct bonding). We use the parameters of this force (mainly the size of this auxiliary charge, \( q_{\text{aux}} \)) to adjust the speed of the reaction (Fig. 3). By accelerating the reaction, the process should take place in a reasonable temporal frame without having an overall influence on how bonds are formed. This does not mean that bonds always form between the same molecules, but that the resulting molecular structure is similar at a comparable reaction state, i.e. the authors expect properties to be a function of curing degree and that the time scale to get to this curing degree should not significantly impact the final material properties of the network, as long as the reaction is “slow enough”. Without further studies we cannot say that this statement is universally true, but that it is a reasonable assumption in this context, which is also necessary to carry out the reaction simulations within the MD time scale.

Fig. 3a illustrates how increasing the auxiliary charges raises the conversion speed. Auxiliary charges of \( \pm 1.25 \) or greater are needed to achieve 50% conversion in a reasonable time scale. Increasing the charge beyond \( \pm 1.75 \) results in only slightly faster conversion rates. Fig. 3b shows the energies and distances at which new bonds are formed. While the shape of the curve is determined by the bond energy versus distance relationship (black curve), the range of values (bandwidth) at which bonds actually form is shown by the shifted lines, with the median indicated by a point. These curves lead to the conclusion that higher auxiliary charges narrow the bandwidth of energies and distances in which new bonds are formed. This is a result of the higher attractive forces of the reactants, which

![Figure 3](image_url)
moves them closer very quickly during a few numerical time steps. For the reaction algorithm this means that bond formation for two atoms might be unlikely at one time step, but at just the next it might be very probable. This can also be seen in the depicted median point, which moves towards $\Delta E = 0$. At higher auxiliary charge this effect starts to reverse, probably due to an elevated local temperature due to high velocities or other chaotic effects. Hence, a trade-off between distance and energy bandwidth, respectively, and a reasonable reaction speed has to be found. This suggests using an auxiliary charge in the lower end of $\pm 1.50$ to $\pm 2.00$ range, where the bandwidth does not change much. Additionally, bond formation opportunities, which might be natural on a longer time scale, e.g. due to slow re-configuration of molecules bringing energetically more favourable bond partners closer, might be lost with elevated reaction speeds. This could lead to different material properties when higher auxiliary charges are chosen. We examine this possibility for the thermal conductivity $\kappa$ in Fig. 3c. While the mean value of $\kappa$ does not change much, the values do become more anisotropic (reflected by the larger error bars) for large and small values of the auxiliary charge. In the case of the virtual resin system, auxiliary charges of $\pm 2.00$ or less seem to be acceptable. However, charges lower than $\pm 1.50$ may result in more anisotropic results (e.g. in the thermal conductivity tensor) probably because fewer bond partners may be able to move close enough to form a bond. This might cause bond formation only for easily accessible configurations, narrowing the overall range of possible bond configurations. Hence, in the following, auxiliary charges are chosen to be in the identified range of small anisotropy, but also with respect to general molecule size and numerical stability. In contrast to the above discussed urethane reaction, the radical polymerisation, which typically involves small and compact molecules may be achieved with smaller auxiliary charges.

4. Simulations

As mentioned in the previous section the MD software LAMMPS is used for all simulations. The basic setup uses an NPT ensemble, hence constant number of atoms, constant pressure and constant temperature, which is realised by fix nve in conjunction with a Langevin thermostat (fix langevin) and a Berendsen barostat (fix berendsen/press). The creation of the basic all-atom molecules is done in AVOGADRO.36,37

In all simulations periodic boundaries and LAMMPS real units were used. To setup the simulations we used the information provided in sections 3 and 4. We built each component with AVOGADRO and filled the simulation domains with the given compound in Table 3 using the all-atom molecule structures. The initial volume was larger than the operational volume to allow molecules to be placed randomly in position and orientation. Before simulating the reactions, the system was equilibrated to the operational state via the following steps (illustrated in Fig. 4):

- randomisation at high absolute temperature and a large constant volume,
- step-wise volume shrinkage towards the expected mass density at room temperature, cycling sub-steps compressing, minimisation and equilibration,
- final equilibration at room temperature and standard pressure, letting the domain adjust to its desired mass density.

In the case of the commercial resin system the simulation domains have a mass density of approximately 1.089 g cm$^{-3}$ at 293 K after undergoing the above procedure (cf. Table 9). The DARON® AQR 1009 product data sheet only gives the mass density for the fully cured resin, as the uncured components start reacting upon mixture (cf. section 2). By using a typical value for volume shrinkage for a UPPH resin, an initial mass density of about 1.082 g cm$^{-3}$ is found at 296 K. The closeness of the two mass densities leads to the conclusion, that the mole-

![Fig. 4](https://example.com/fig4.png)

Fig. 4 Steps taken to setup a typical simulation domain: the step-wise compression consists of a loop cycling compression, minimisation and equilibration. The mass density data shown corresponds to the commercial resin system.
Table 4 Parameters used for different steps of the simulations, adjusted to match industry processes^39

<table>
<thead>
<tr>
<th>Run</th>
<th>Time in ns</th>
<th>Δt in fs</th>
<th>Ensemble</th>
<th>Temperature in K</th>
<th>Pressure in atm</th>
</tr>
</thead>
<tbody>
<tr>
<td>Urethane</td>
<td>0.5</td>
<td>0.1</td>
<td>NPT</td>
<td>313.0</td>
<td>1.00</td>
</tr>
<tr>
<td>Radical</td>
<td>0.5</td>
<td>0.1</td>
<td>NPT</td>
<td>418.0</td>
<td>98.69</td>
</tr>
</tbody>
</table>

...The reaction simulations are carried out in a two-step procedure based on the curing steps used during an industrial production process summarised in Table 4. Firstly, the poly-urethane reaction is simulated: the temperature is set to 313 K and the bond formation between hydroxyl and isocyanate groups is allowed. This reaction is accelerated by auxiliary charges of ±1.5 as described at the end of the previous section. The simulations are stopped when a conversion to urethane connections of approximately 50% is reached, which was always achieved within 0.5 ns. Secondly, the radical polymerisation is enabled where the temperature is elevated to 418 K, causing the peroxide to cleave. Simultaneously, the pressure is set to 10 MPa (≈ 98.69 atm). The temperature and pressure in this step are based on typical process parameters of industrial compression moulding. Here, auxiliary charges for radical centres are set to \( q^{aux} = ±1.0 \) to mimic free electrons that occur in radical bond formation. After another 0.5 ns the reactivity of the second simulation step diminishes and the simulation is stopped. The reaction simulations are performed for a set of different systems. The virtual resin system is used for simulations of about 7500 atoms and in one configuration, which is twice the composition given in Table 1. The complex resin system is used in two different sizes, which have about 14 000 and 110 000 atoms. Here, the small systems use again directly the composition given in Table 1, while the large system is the eightfold unit cell. The smaller system comes in three different configurations (started from independent random initial conditions), whereas the large one is used in one configuration.

5. Results

For visualisation the software package OVITO\(^40,41\) is used. In general, all quantities are calculated on the basis of fluctuation dissipation relations (see e.g. Frenkel and Smit\(^42\)) or non-equilibrium molecular dynamics (see e.g. Rapaport\(^43\)) for various degrees of cure to catch their development during the chemical reaction. Furthermore changes during cooling to room temperature are measured and presented, if meaningful. The virtual resin system, which serves as a prototypical example, is only evaluated for the purely thermal properties, i.e. specific heat capacity and thermal conductivity.

The degrees of cure \( ζ \), which are of interest and each referenced to maximum conversion, preferably are for the urethane reaction \( ζ_u = \{0\%, 50\%\} \) and for the radical reaction \( ζ_r = \{0\%, 20\%, 40\%, 60\%, 80\%, 100\%\} \), or as close as the simulation results are available. It is assumed that 50% of theoretically possible urethane connections is a upper limit in an experimental setup. Therefore a total number of seven data points are examined along the curing reaction. In the following a short notation of the form UxRy is used, where x and y indicate the conversion in percent for the urethane and the radical reaction, respectively. For example \( ζ_u = 50\% \) and \( ζ_r = 0\% \) is noted by writing U50R0. Temperature dependence is essentially evaluated either around room temperature (293 K) or around the mould temperature (418 K). To characterise the vicinity of these temperatures, the data points for temperature are set in the range \( Θ ∈ [273 K, 313 K] \) and for mould relevant curing degrees additionally in the range \( Θ ∈ [398 K, 438 K] \).

5.1 Curing reaction

The curing reaction is separated into urethane polyaddition and radical polymerisation for each of the resins, both carried out under isothermal-isobaric conditions through the applied NPT ensemble (see Table 4). For both, bond formation and dissociation progress were tracked to gain information about reaction behaviour and remaining volatile organic compound (VOC, Table 7).\(^44\) From equilibrated states at the beginning and the end of the reaction steps chemical volume shrinkage \( χ \) at different temperatures (Table 8) and released reaction enthalpy \( Δ h \) (Table 10) was calculated.

Evaluation: Both resin systems execute their chemical reactions in a comprehensible way: the auxiliary charges speed up the reactions to make them happen on an MD time scale (compared to several minutes in experiments). For the radical reac-

Table 5 Overview of bonds formed during the curing simulation of the virtual resin system

<table>
<thead>
<tr>
<th>Reaction steps in virtual resin</th>
<th>Formed bonds (max)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Urethane</td>
<td>80 (160)</td>
</tr>
<tr>
<td>Peroxide dissociation</td>
<td>8 (8)</td>
</tr>
<tr>
<td>Chain initiation</td>
<td>16 (16)</td>
</tr>
<tr>
<td>Chain propagation</td>
<td>668 (668)</td>
</tr>
<tr>
<td>Chain termination</td>
<td>6 (16)</td>
</tr>
</tbody>
</table>
tion (see Fig. 5) the models follow the reaction schematic by rapidly dissociating peroxide bonds due to the elevated temperature, which causes radical chain initiations and propagation, which steadily connects the polyurethane backbones. If free radicals meet, chains are terminated.

As listed in Table 5 and illustrated in Fig. 6, the virtual resin shows a high reactivity and is able to reach 100% conversion for both, the urethane and the radical reaction. This is mainly due to the virtual resin system being composed of shorter molecules than the commercial resin. These shorter molecules are able to move faster and so the reactive atom groups on the molecule find a reaction partner fairly quickly. For the same reasons, the commercial resin system, Fig. 7, with its larger and long-chained molecules behaves relatively slowly and 100% conversion is not reached. As listed in Table 6, for both system sizes all peroxide bonds dissociate and the respective number of radical chain initiation are conducted.

The cross-linking styrene molecules, which drive the chain propagation, need an increasingly amount of time to propagate the cross-links, which significantly slows down the reaction at the end of the simulation. Only a few chains terminate due to a merge of two cross-linking branches. The slowed down chain propagation indicates that the remaining amount of cross-linkers listed in Table 7 would not remarkably decrease in longer simulation runs.

These remaining unlinked molecules are identified as VOC, which may diffuse out of the polymer network over time and cause its characteristic odour. Depending on the molecule type, large amounts of VOC may harbour health risks. The volume shrinkage exhibited by our commercial-analog resin system is similar to that seen in other hybrid thermosets. Furthermore, for the small and large realisations the volume shrinkage is almost the same (see Table 8).

For the virtual resin the volume shrinkage is significantly higher and may result from the small and short polymer chains used, which, when bonded, do not allow for much free volume in between. Together with initially low mass density (see Table 9) this underlines the purely exemplary nature of the virtual resin system, which does not follow standard thermoset behaviour. The gas-like behaviour at low degrees of cure and

Table 6 Overview of bonds formed during the curing simulation of the commercial resin system

<table>
<thead>
<tr>
<th>Reaction steps in commercial resin</th>
<th>Formed bonds (max)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>small system</td>
</tr>
<tr>
<td>Urethane</td>
<td>77^{+}0</td>
</tr>
<tr>
<td></td>
<td>(154)</td>
</tr>
<tr>
<td>Peroxide dissociation</td>
<td>4^{+}0</td>
</tr>
<tr>
<td></td>
<td>(4)</td>
</tr>
<tr>
<td>Chain initiation</td>
<td>8^{+}0</td>
</tr>
<tr>
<td></td>
<td>(8)</td>
</tr>
<tr>
<td>Chain propagation</td>
<td>323^{+}0</td>
</tr>
<tr>
<td></td>
<td>(334)</td>
</tr>
<tr>
<td>Chain termination</td>
<td>1^{+}1</td>
</tr>
<tr>
<td></td>
<td>(8)</td>
</tr>
</tbody>
</table>
high temperature further stresses that this artificially designed resin system is disconnected from industrial application or physical and chemical reasonable thermosets in general.

A similar picture is observed for the change in enthalpy of the radical reaction step (see Table 10). Again, the calculated values for the small and large commercial resin systems are nearly identical. For the virtual resin system, similar to the volume shrinkage, the enthalpy change found is analogously higher.

### 5.2 Specific heat capacity

The calculation of the specific heat capacity at constant volume, \( c_V \), is performed in an NVT ensemble. In thermodynamics the heat capacity at constant volume is defined as

\[
C_V = \left. \frac{\partial E^{\text{tot}}}{\partial \Theta} \right|_{V,N},
\]

where \( E^{\text{tot}} \) is the total energy and \( \Theta \) the absolute temperature. Division by mass \( m = \rho V \) yields the specific quantity \( c_V \). In statistical mechanics this can be re-written on the basis of the ensemble average of the total energy to

\[
c_V = \frac{\langle E^{\text{tot}} \rangle - \langle E^{\text{tot}} \rangle^2}{k_B\Theta^2}.
\]

**Evaluation:** Simulations of partially cured configurations (where reactions are paused during the measurement) were carried out in an NVT ensemble for 1 up to 5 ns. In Fig. 8 and 9 the results are shown and listed in Tables S3 and S4, respectively. The basic, underlying calculation of the mass-specific heat capacity uses cumulative averages for total energy and temperature expressions, and is applied to every data point in temperature and degree of cure.

The virtual resin system shows a non-monotonous development with degree of cure and temperature. If the three presumed outliers at U50R20, U50R40, U50R60 and \( \Theta = 273 \) K are excluded from the interpretation, and the region with low degree of cure and high temperature is neglected due to the irregular behaviour of the mass density (cf. Table 9), a qualitative pattern may be identified. A distinct ditch is visible along a degree of cure of U50R20, and for lower and higher values of degree of cure, \( c_V \) generally rises moderately. No generally

| Table 7 Remaining cross-linking molecules: volatile organic compounds |
|-------------------------|-------------------------|-------------------------|
| Virtual resin (ethylene) | Commercial resin (small, styrene) | Commercial resin (large, styrene) |
| Remaining cross-linkers | 0.00% | 4.01 ± 0.57% | 4.39% |

| Table 8 Volume changes due to the chemical reactions (\( p = 1 \) atm): volume shrinkages are listed for the total and only the radical reaction |
|--------------------------|---------------------|---------------------|
| Volume shrinkage in %    | Virtual resin       | Commercial resin    |
|                         | (small)             | (large)             |
| \( \chi_{\text{tot}} \) (293 K) | -57.01              | -5.33 ± 0.24        |
| \( \chi_{\text{r}} \) (293 K) | -77.35              | -4.70 ± 0.34        |
| \( \chi_{\text{u}} \) (418 K) | ~30 000             | -10.59 ± 0.66       |

| Table 9 Mass densities due to the chemical reactions (\( p = 1 \) atm): mass densities are given in the uncured, intermediate (after the urethane reaction) and fully cured state |
|-----------------|---------------------|---------------------|
| Mass density in g cm\(^{-3}\) | Virtual resin (small) | Commercial resin (large) |
| \( \rho_{\text{uncured}} \) (293 K) | 0.614               | 1.089               |
| \( \rho_{\text{urethane}} \) (293 K) | 0.547               | 1.098               |
| \( \rho_{\text{urethane}} \) (418 K) | 0.003               | 1.002               |
| \( \rho_{\text{full}} \) (293 K) | 0.971               | 1.148               |
| \( \rho_{\text{full}} \) (418 K) | 0.921               | 1.108               |

| Table 10 Change in enthalpy due to radical reaction at \( \Theta = 293 \) K and \( p = 1 \) atm |
|-----------------|-----------------|-----------------|
| \( \Delta h \) in kJ kg\(^{-1}\) | Virtual resin (small) | Commercial resin (large) |
| -568.27         | -80.47 ± 1.43   | -80.90          |

Fig. 8 Virtual resin system: (a) Exemplary specific heat capacity evaluation for U50R60 at 313 K, (b) specific heat capacity dependent on temperature \( \Theta \) and degree of cure \( \zeta \).
occurring pattern for a change in temperature is visible, except for higher degrees of cure, where $c_V$ drops with increasing temperature. This generally non-monotonous behaviour is observed with real thermosets, e.g. for temperature changes,\textsuperscript{45,46} and is not a result of this being a virtual resin. The use of more system domains or larger system domains may help to further smooth and clarify the results, including the detection of possible outliers. As this is only a virtual resin system, this was not prioritised in this study.

For the commercial resin system all three small domains are used for the calculation of $c_V$. As the three systems may not have exactly the same degree of cure $\zeta$, the calculation is done for the closest values available and the $c_V$ shown is from a weighted average. The commercial resin system also shows a prominent valley, which is found along temperature for a degree of cure of about U50R40. Lower and higher degrees of cure give a crest in $c_V$, and especially for high temperature and high degrees of cure a peak is identified. Comparing this behaviour and the general range of the specific heat capacity at constant volume to other thermosets (see, e.g. literature values in ref. 47 and 48), an agreement in magnitude and in general behaviour with temperature is found. Especially the non-monotony with temperature is not uncommon.\textsuperscript{45,46} Similar to the virtual resin system, a larger set of system domains may help in further smoothing out the results, but the overall trends are already clear.

5.3 Thermal conductivity
Thermal conductivity is described by Fourier’s law as the proportionality tensor between heat flux $J_i$ and temperature gradient

$$J_i = -\kappa_i \frac{\partial \Theta}{\partial x_i} .$$

With the Green–Kubo formalism\textsuperscript{49–51} thermal conductivity can be expressed by the ensemble average of the auto-correlation of the heat flux.

$$\kappa_{ij} = \frac{1}{k_B \Theta V} \int_0^\infty (J_i(0)J_j(t)) dt$$

gives the thermal conductivity in $ij$-direction, where $i$ and $j$ represent the Cartesian coordinates $\{x, y, z\}$. Isotropy is usually assumed because amorphous thermosets are generally unstructured and hence do not have a predominant direction for the heat flux. Therefore, the thermal conductivity tensor is expressed by a scalar $\kappa_{iso} = (\kappa_{xx} + \kappa_{yy} + \kappa_{zz})/3$. We measure the components separately to test the isotropy before combining.

Evaluation: As above for the specific heat capacity, simulations were carried out on partially cured configurations in an NVT ensemble for 1 up to 5 ns. The thermal conductivity is calculated in intervals of 8000 time steps by the Green–Kubo equation (6), which turned out to be sufficient for the auto-correlation of the heat flux to decay before the end of the time interval. Hence, the formalism converges towards constant values of $\kappa_{ij}$, which are evaluated for the last 1 ns of the overall simulation time. For the simulation, to suppress undesired convective heat fluxes, the centre-of-mass motion is subtracted.\textsuperscript{52}

The results of the virtual resin system are depicted in Fig. 10 and listed in Table S5.\textsuperscript{†} The general trend shows a decreasing thermal conductivity $\kappa_{iso}$ for higher degrees of cure and for lower temperatures. Higher temperatures at lower degrees of cure show a deviation from this behaviour, which might be associated to the still low number of cross-links and a low mass density (cf. Table 9), hence less possibilities for heat transport. Analogously to the specific heat capacity evaluation, a larger set of simulations could help in clarifying the trends and behaviour, but this is not of great interest for the virtual resin.

The results of the commercial resin system are shown in Fig. 11 and Table S6.\textsuperscript{†} As previously for the specific heat capacity, the calculated thermal conductivities of all three small domains (see, e.g. Fig. 11a) are used for a weighted average for every data point in degree of cure and temperature. The isotropic thermal conductivity $\kappa_{iso}$ grows with higher degrees of cure and higher temperatures. The behaviour with changing temperature as well as the magnitude of $\kappa_{iso}$ is again similar to thermosets found in literature.\textsuperscript{37,48}

The increase in thermal conductivity with degree of cure may be explained by the increased cross-linking density, which results in better transmission of thermal energy. Therefore,
the overall pattern in Fig. 11b is fairly clear if one neglects the statistical fluctuations.

5.4 Thermal expansion and glass transition temperature

Thermodynamics define the (isotropic and) volumetric thermal expansion coefficient as (see e.g. Landau and Lifshits)

\[ \alpha_{\text{vol}} = \frac{1}{V} \frac{\partial V}{\partial \theta} \]

at constant pressure and in relation to the volume \( V \). The pressure is set to \( p = 1 \) atm. Assuming \( \alpha_{\text{vol}} \ll 1 \), the linear thermal expansion coefficient is simply related via \( \alpha_{\text{lin}} = \alpha_{\text{vol}} / 3 \).

The glass transition temperature \( \Theta_g \) is determined by recording the volume over a range of absolute temperatures. When the polymer switches from a rubbery to a glassy state, the change in slope of the volume curve indicates \( \Theta_g \). In the following, only the commercial resin system is evaluated.

**Evaluation:** For every degree of cure a series of simulations based on the large commercial resin setup is run. Each simulation is conducted in an NPT ensemble with pressure \( p = 1 \) atm and temperatures ranging from 103 K to 563 K in 20 K steps. Between 203 K to 433 K every 10 K a simulation is performed. Every simulation is run for 500 ps, and the simulation domain’s volume is averaged over the last 100 ps. For evaluation, we use the natural logarithm of the volume expressed in relation to the volume at a temperature of \( \Theta_{\text{Ref}} = 293 \) K.

The slopes of the curves plotted in Fig. 12 represent the volumetric thermal expansion coefficients, and the points where the slope changes are identified as the glass transition temperatures \( \Theta_g \). Due to the finite size of our system, rather than a well-defined kink the data sets show a smooth transition region for the change of slope from the glassy to rubbery state.

This crossover region is excluded from the data for the piecewise linear fits (for the simple reason that the data is not linear in this region). We do this in a two-step procedure. In a first step we calculate the local second derivatives of the full data sets. The transition region is located where the second derivative peaks (i.e. where the curve is non-linear). Based on this we exclude data points in the range of ±20 K around this preliminary \( \Theta_g \). This range is chosen with respect to the largest occurring spacing between two data points of a data set. The data sets with excluded transition region now serve as input for the piecewise linear fits with one break point, where the break point is associated with the corrected \( \Theta_g \) and the slopes are the volumetric thermal expansion coefficients. The resulting fits of this evaluation procedure are shown in Fig. 12.
The respective linear thermal expansion coefficients are calculated from their volumetric counterparts and are listed in Table 11. The thermal expansion coefficients are found to be similar in magnitude to typical thermosets found in the literature.\cite{56,57} The increase in glass transition temperature $\Theta_g$ with progressing curing reaction appears to be in a range of standard thermosets.\cite{56,57} However, the DARON® AQR 1009 product data sheet\cite{38} indicates a final glass transition temperature of $\Theta_g \approx 403$ K (130 °C). This deviation may be related to finite size effects or that the simulated cross-linking is not close enough to the real chemical process, especially in density of the formed cross-links\cite{57} (we start with a perfectly mixed system which is an ideal limit for an experiment). In addition, the width of the transition region in our finite-sized system broadens at the higher degrees of cure which may also mean that we have underestimated the uncertainties in $\Theta_g$ at high cure.

To review the development of $\Theta_g$ in the radical reaction step, DiBenedetto’s approach may be used.\cite{58} Following the development of $\Theta_g$, the data points are sufficiently matched, and the general shape is comparable to other thermosets (see Fig. 13).\cite{56,59} As above, for smoother results either a larger set of realisations of the same resin setup or a larger resin setup is needed.

### Table 11

<table>
<thead>
<tr>
<th>$\zeta$</th>
<th>$\Theta_g$ in K</th>
<th>$\alpha_{\text{vol}}$ in $10^{-5}$ K$^{-1}$</th>
<th>$\alpha_{\text{lin}}$ in $10^{-5}$ K$^{-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>U0R0</td>
<td>267.8</td>
<td>36.0</td>
<td>83.4</td>
</tr>
<tr>
<td>U50R0</td>
<td>275.0</td>
<td>34.1</td>
<td>79.1</td>
</tr>
<tr>
<td>U50R20</td>
<td>284.7</td>
<td>30.0</td>
<td>71.9</td>
</tr>
<tr>
<td>U50R33</td>
<td>295.9</td>
<td>28.3</td>
<td>66.8</td>
</tr>
<tr>
<td>U50R67</td>
<td>320.0</td>
<td>23.2</td>
<td>52.8</td>
</tr>
<tr>
<td>U50R82</td>
<td>346.8</td>
<td>22.3</td>
<td>46.4</td>
</tr>
<tr>
<td>U50R95</td>
<td>362.1</td>
<td>21.6</td>
<td>42.6</td>
</tr>
</tbody>
</table>

5.5 Bulk modulus

In its solid form the thermoset’s overall mechanical behaviour is assumed to be visco-elastic, where the viscous part is only associated to pure shear deformation. Shear deformations of interest in real systems occur over a much longer time scale than is accessible in MD so for simplicity only the bulk modulus $K$ of the commercial resin is characterised in the following. The characterisation happens with non-equilibrium molecular dynamics simulations (NEMD), which determine $K$ by a volume tension-compression test varying all box lengths by 1% in compression and tension ($\approx 3.03\%$ in volume). The thermodynamic background of this is the definition of the bulk modulus $K$ (see e.g. Landau and Lifshits\cite{60}),

$$\frac{1}{K} = -\frac{1}{V} \frac{\partial V}{\partial p},$$

which is defined at constant temperature.

**Evaluation:** The bulk modulus simulations were carried out in an NVT ensemble for 6 ns. For each set of $\{\zeta, \Theta\}$ one cycle of the volume tension-compression test was recorded (e.g., Fig. 14a). The cycle starts with compression and is controlled by *fix deform*. The evaluation for one data point is shown in Fig. 14a, where the volume and pressure change are referenced to their initial values.

The linear regression, whose slope gives the bulk modulus, is done on the basis of the averaged data, and the first quarter of the cycle was neglected to exclude undesired start-up effects. The resulting bulk moduli over the examined parameter range are depicted in Fig. 14b and listed in Table S7.\dagger The magnitude of the bulk modulus is in common ranges of thermosets.\cite{37,48} Both, changes in temperature and degree of cure, show a nearly linear dependence and follows the reasoning that less interconnection or higher temperature reduces the stiffness. Some of the bulk modulus values were calculated from MD simulations using *fix nve/ limit* as a time integrator (marked with the numeral 1 in Table S7). For the numerical background the reader is referred to ESI section V.\dagger
6. Conclusion

We detailed algorithms describing bond formation and dissociation procedures, and use them on-the-fly in reaction simulations on the class of thermoset hybrid resins. For application, two hybrid resins of the same class are introduced: a virtual resin and one derived from a commercially available resin. The reaction runs are analysed themselves, but also different stages of the simulated chemical reaction are used to calculate the temperature-dependent material property development.

The radical reaction step of the two-stage reaction simulation has similarities in behaviour and shape compared to experimental findings in literature. Also derived quantities, such as the volume shrinkage have the same magnitude as resins of the same thermoset class. The calculated material properties of the commercial-type resin, thermal as well as mechanical, are in a reasonable range of typical thermosets and their behaviour with degree of cure and temperature follows physical premises. Nevertheless, a larger variety of initial or larger system domains may further smooth out outliers or finite-size effects in the pattern of results.

Experimentally determined material properties of this resin type are necessary to quantify calculated material properties more clearly.

Conflicts of interest

There are no conflicts to declare.

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