1. Introduction

Dissolution of naturally occurring and commercial solid metal oxide nanoparticles in the environment and in therapeutic applications can have important consequences for ecotoxicity and human health. Research on nanoparticle dissolution in aqueous systems has increased recently, even though the general problem has been known for some time. The silver nanoparticle dissolution rate is higher for smaller sizes. Silver loss appears to occur at the surface as there are few changes in the crystallite lattice parameters of the nanoparticle core. Silver nanoparticles may undergo shape changes and multistep oxidation of the partially oxidized silver atoms that form a surface monolayer. Its dissolution can be impacted by surface coatings, and has been modeled using first- and second-order kinetics. Dissolution has been observed for silica, copper, zinc-containing (ZnS, ZnO), magnetite (Fe₃O₄), and ceria (nanoceria (CeO₂)) nanoparticles. Silica nanoparticle dissolution rates increase as particle size decreases, although Diedrich et al. reported that dissolution rates decrease with decreasing particle size due to changes in surface mechanisms. Zinc-containing nanoparticles have also been shown to have faster dissolution rates for smaller particle sizes. Nanoceria solubility has been measured as a function of pH in perchloric acid systems. Some researchers have recognized the need for dissolution rate data and dissolution rate constants as part of the risk assessment of nanomaterials. Nonetheless, there have been few attempts to develop rate models for dissolution.
processes under conditions linked to ecotoxicity or therapeutic applications.

1.1 Ecotoxicity of nanoceria

It is well-known that plants secrete carboxylic acids from their root systems, which can complex metals in the rhizosphere, such as aluminum. Several researchers have shown that cerium can be taken into plant root systems. In the cucumber, only a portion of ceria nanoparticles formed Ce(III)-carboxyl complexes and showed no phytotoxicity.20 Nanoceria is known to dissolve and transform in acidic plant growth media.17 Citric acid coatings on nanoceria reduced its toxicity and cerium uptake in radish seedlings in water.21 Nanoceria can biotransform with the aid of organic acids after adsorption on cucumber root surfaces.22 Nanoceria dissolution at the radish root is enhanced by low molecular weight organic acids, e.g., succinic acid.23 Transformation of ceria nanoparticles in cucumbers appears to be influenced by phosphate.24 In general, there are not many studies on the effects of nanoceria size on ecotoxicity, which has been identified as a research gap.25

1.2 Therapeutic applications of nanoceria

Nanoceria surfaces are redox active and can cycle between Ce(III) and Ce(IV)26 as confirmed by DFT modelling of Fourier transform infrared (FTIR) absorption spectra of nanoceria particle surfaces.27 This auto-catalytic property leads to a number of commercial applications.28-30 In the life sciences, nanoceria might treat a number of therapeutic conditions, such as elevated oxidative stress and inflammation, cancer, radiation damage, bacterial infection, stroke-induced ischemia, and retinal degeneration.31 Nanoceria size is known to affect its hepatotoxicity. When HepG2 cells were exposed to nanoceria, the smaller, but not larger size, (8 vs. 58 nm nominal diameter) had metabolomic effects, increasing the concentrations of many lipids, especially fatty acids32 and altering pathways of mitochondrial function, apoptosis, and the tricarboxylic acid (Krebs) cycle.33 Smaller nanoceria cause aerobic glycolysis33 (the Warburg effect, important for oncology), for which high rates of glycolysis are followed by lactic acid fermentation even with abundant oxygen levels. Generally, nanoceria are only sparingly soluble in water, particularly at physiological pH (7.4).34 However, nanoceria can bioaccumulate in various organs (liver, spleen, bone marrow).35 30 nm nanoceria has been shown to biotransform to cerium phosphate (CePO4), possibly via a dissolution/recrystallization process. Cerium phosphate nanocrystals would have different reactivities with respect to oxidative stress and inflammation mechanisms, leading to loss of therapeutic benefits of nanoceria. Nanoceria has also been shown to have phosphatase activity39 and to react with organophosphates.40,41

1.3 Experimental design for measurement of long-term nanoceria dissolution rates

Solid particle dissolution is often controlled by mass transfer from the particle through the thin liquid film adjacent to its surface. For slowly dissolving solids, the rate-limiting mechanism can be breaking chemical interactions of surface atoms or molecules and forming ligand complexes that are soluble in the liquid phase.42,43 Nanoceria dissolution data were obtained for a series of aqueous carboxylic acid solutions at 37 °C and pH 4.5, conditions relevant to ecotoxicity and inside phagolysosomes. The carboxylic acids selected have structures related to citric acid, which is known to interact with nanoceria surfaces.44-47 Solubilized cerium was measured as a function of time. Dissolution rate coefficients, estimated using a surface-controlled process model, are expected to link to both nanoceria ecotoxicity and therapeutic applications. DFT was used to model the energy of formation for cerium-ligand complexes to assess whether the dissolution process is expected to proceed.

One ml of nanoceria dispersion in iso-osmotic citric acid was loaded into a dialysis cassette (Slide-A-Lyzer®) that was placed in 200 ml of iso-osmotic solution containing a carboxylic acid or control ligand (Fig. 1). The nanoceria slowly dissolved into the dialysis cassette liquid, releasing salts that diffused across the cassette membrane, and into the bath. The 2 kDa molecular weight cut-off cassette membrane is known to prevent nanoceria particles > 1 nm from passing, while permitting salts to diffuse.48,49 Samples from the bath and cassette were withdrawn periodically for Ce analysis by ICP-MS. Samples were also taken for nanoparticle size and shape determination by TEM. There can be water evaporation from the bath and solution flux between the cassette and the bath.

Dissolution experiments were carried out for 28 to 30 weeks. Bath Ce concentrations were measured each week by withdrawing 1 ml samples for ICP-MS analysis. Dialysis cassette Ce concentrations were determined by withdrawing 75 μL samples occasionally from the cassette. Additionally, 25 μL samples were occasionally withdrawn from the cassette for TEM imaging of the nanoparticles. Sampling removed Ce ions from the bath, nanoceria from the cassette, and Ce ions from the cassette, changing the amounts of nanoceria and Ce in the cassette, Ce in the bath, and Ce in the total system. The final cassette and bath volumes were measured.

![Fig. 1 Dissolution system sketch: dialysis membrane cassette in a carboxylic acid bath.](image-url)
Evaporative losses from the bath changed its volume but removed only water. Cassette volume changes occurred due to a net flux of the bath solution either into or out of the cassette. Material balance equations are provided in ESI.†

The carboxylic acids studied were citric acid, analogs of citric acid with similar or related structures (glutaric, hydroxybutyric, lactic, malic, succinic, and tricarboxylic acids), acetic acid, which is known to bind to nanoceria surfaces,30 and adipic and pimelic acids, which are known to bind solely to nanoceria’s (100) crystallite face.51 Three control solutions were used: ammonium ion (a positively charged species), horseradish peroxidase/H₂O₂ (a free radical mediator reported to facilitate carbon nanotube dissolution52), and water (a substance that should have minimal effects). Carboxylic acid structures are shown in Fig. S1 (ESI†).

1.4 Surface-controlled dissolution rate

Early in the study, zero-, first-, and second-order kinetic models were applied to dissolution data. All of these models showed generally poor correspondence. There was good correspondence between data and prediction when a model for surface-controlled dissolution of solid particles43,53 was applied to the bath data. This model links the rate of solid dissolution from a spherical particle to its current surface area. It requires knowledge of the particle size and/or size distribution, the number of Ce atoms in a particle of a specific size, and the number of nanoceria particles in the cassette. It was assumed that Ce ion/carboxylic acid ligands do not reform nanoceria and that the chemical potential for dissolution does not change during the experiments. With these assumptions, the dissolution process is dependent only on the number of nanoceria particles in the cassette and their size. The apparent dissolution rate constant is estimated by nonlinear regression to minimize the differences between the measured Ce ion concentrations in the bath and the model predictions, using the discrete balances to adjust for nanoceria mass loss from the cassette, and Ce ion loss from the bath. Withdrawal of the dispersion changes the number of nanoparticles remaining in the cassette, but not their size. Furthermore, we assume that the dissolved Ce salts are sufficiently soluble in the aqueous phase so as to not create a thermodynamic barrier to CeO₂ dissolution. The only identified report of a value reported its solubility to be 3.02 and 6.40 g L⁻¹ in H₂O at 20 and 90⁰C, respectively,54 greater than the cerium concentration if all of the nanoceria in the dialysis cassette equally distributed throughout the dialysis/dissolution system (∼0.00250 g L⁻¹).

The loss rate of Ce ions from a nanoceria particle is:

\[-\frac{dn_i(t)}{dt} = k \cdot S_i(t)\]  \hspace{1cm} (1)

where \(n_i(t)\) is the number of atoms in a nanoparticle with diameter, \(d_i\) (nm); \(k\) is the dissolution rate constant (Ce atoms nm⁻² h⁻¹), and \(S_i(t)\) is the surface area of the particle (nm²).43,53 The present study used nanoceria with an average diameter of ∼4 nm, so the number of Ce atoms in the nanoparticle was selected as the metric. Balances are required for the nanoparticle size (atoms per nanoparticle) and the number of nanoparticles in the cassette dispersion. Nanoceria particles have been modelled as spheres for the purpose of linking volume to surface area to diameter. The nanoparticle volume is:

\[V_i(t) = \frac{\pi}{6} d_i(t)^3\]  \hspace{1cm} (2)

The nanoparticle surface area is:

\[S_i(t) = 4 \pi r_i(t)^2 = \pi d_i(t)^2\]  \hspace{1cm} (3)

The number of Ce atoms in particles with initial size \(n_1\) is:

\[n_i(t) = \frac{\pi}{6} \left( \frac{d_i(t)}{10^{9}} \right)^3 \frac{\rho}{F_{w,\text{ceria}}} N_{Av}\]  \hspace{1cm} (4)

where \(\rho\) is the nanoparticle density (7.22 g cm⁻³), \(F_{w,\text{ceria}}\) is the formula weight of ceria (172.11 g ceria per g mol; there is one mole of cerium per mole of ceria), and \(N_{Av}\) is Avogadro’s number. Eqn (4) can be rewritten as:

\[-\frac{dn_i(t)}{dt} = k S_i(t) = \alpha (n_i(t))^{2/3}\]  \hspace{1cm} (5)

where

\[\alpha = k \pi^{1/3} (6 F_{w,\text{ceria}} 10^{21} / \rho N_{Av})^{2/3}\]  \hspace{1cm} (6)

The factor \(\alpha\) has units of (atoms)¹/³ per h. The solution of eqn (6) is:

\[n_i(t) = \left[ n_i^{1/3} (t = 0) - \frac{\alpha}{3} t \right]^{3}\]  \hspace{1cm} (7)

This equation gives negative values of \(n_i(t)\) when the particle is fully dissolved. If desired, this can be corrected by applying the Heaviside step function.43 Eqn (7) gives the number of Ce atoms remaining in a nanoparticle of size \(n_i\) at any time after the start of the experiment. For any two discrete sampling times, eqn (7) can be used to compute the difference, \(n(i + 1) - n(i)\), giving the net change in atoms/particle over that time interval. Details for the discrete material balances are shown in ESI.† Nanoceria size changes during growth and dissolution were imaged via HRTEM and analyzed using ImageJ and methods for particle size distributions by TEM.55–57

1.5 Two dissolution pathway elements: carboxylic acids binding to ceria surfaces and stability estimates for soluble Ce-carboxylic acid complexes

If nanoceria dissolves in aqueous carboxylic acids, then carboxylic acid complexes are shown in Fig. S1 (ESI†)
important first step for the dissolution process. Carboxylic acids are known to adsorb on nanoceria surfaces in aqueous solutions. As examples, citric acid is used as the seed particle stabilizer for nanoceria synthesis method used in this work, and some uncarboxylic acid ligands have their maximum adsorption on ceria surfaces at pH 4.5. DFT shows that acetic acid binds in the bidentate chelating mode to oxidized ceria surfaces, but binds in both bidentate chelating and bridging modes to partially reduced ceria surfaces. Also, dissociated adsorption was more favorable on uncoordinated (high energy) corner sites. Some carboxylic acids preferentially adsorb to specific nanoceria crystal faces. On nanoceria surfaces composed mostly of Ce$^{4+}$ species, acetate ions bind more strongly to the nanoparticles than water. The ‘outward-directed’ portion of adsorbed carboxylic acids might affect agglomeration of the nanoceria in aqueous dispersions.

On the other end of the dissolution process pathway, it would be useful to know which stoichiometrically possible cerium-carboxylate complexes will be thermodynamically stable. Complexes of carboxylic acids with cerium and other lanthanides have been reported in the patent and journal literature. Hawkins reported complexes of Ce(III) coordinated with 2 anions of organic compounds, which could be used for clean combustion of hydrocarbon fuels and higher drying rates of paints. Kalsotra reported complexes of Ce(IV) with uncarboxylic acids. Other researchers have prepared Ce(III)-carboxylate acid complexes for a variety of applications. Azenha has reported that trivalent lanthanides can have bidentate coordination with carboxylates, such as cerium(III) acetates. Therefore, it appears possible that cerium(IV) or cerium(III)-carboxylic acid complexes can be formed. If Ce-bidentate carboxylic acid chelates are thermodynamically stable, polar groups on their non-complexing ‘tails’ might improve Celigand solubilities in aqueous solutions.

2. Materials and experimental methods

2.1 Materials

The chemicals, their sources, purity, and CAS numbers were adipic acid, TCI, ≥99%, 124-04-9; ammonium nitrate, Fisher, ACS grade, 6484-52-2; citric acid monohydrate, Fisher, ACS grade, 5949-29-1; DL-3-hydroxybutyric acid sodium salt, Chem Impex Int'l Inc., 100.30%, 150-83-4 & 306-31-0; DL-malic acid, Alfa Aesar, 98%, 6915-15-7; glutaric acid, Acros organics, ≥99%, 110-94-1; hydrogen peroxide 3% W/W, BDH chemicals, 150-250 U mg$^{-1}$, 9003-99-0; lactic acid, TCI, ≥85%, 50-21-5; pimelic acid, Alfa Aesar, 98%, 50-21-5; sodium azide, Sigma, 99.8%, 7722-84-1; horseradish peroxidase type II, Sigma, 150–250 U mg$^{-1}$, 9003-99-0; sodium nitrate, BDH chemicals, ACS grade, 7631-99-4; succinic acid, TCI America, ≥99%, 110-15-6; glutaric acid, Aldrich, ≥99%, 50-21-5; sodium azide, Sigma, 99.8%, 110-94-1; sodium azide, Sigma, 99.8%, 110-94-1; sodium azide, Sigma, 99.8%, 26628-22-8; sodium nitrate, BDH chemicals, ACS grade, 7631-99-4; succinic acid, TCI America, ≥99%, 110-15-6; and tricarboxylic acid, Alfa Aesar, 98%, 99-14-9. The electron microscopy grids were 200 mesh carbon support film on hexagonal copper square grids from Electron Microscopy Sciences. Pierce Biotechnology’s Slide-A-Lyzer™ dialysis cassettes were used. Trace metal grade concentrated nitric acid was from Fisher. ICP/DCP Ce ion standard solution was from Aldrich.

2.2 Nanoceria synthesis and characterization

A polyhedral, polycrystalline citrate-coated nanoceria was synthesized using a hydrothermal approach. A 1.0 M CeCl$_3$ solution with citric acid was reacted for 24 hours in excess 3.0 M ammonia water at 323 K. The temperature was increased to 353 K for 24 hours to crystallize the nanoceria. The solid product was dialyzed 5 times, 12 h each, against iso-osmotic citric acid at pH 7.4 to remove Ce and reactants not incorporated in the solid nanoceria product. Nanoceria primary and hydrodynamic particle sizes were determined by TEM using a 200 keV field emission analytical transmission electron microscope [JEOL JEM-2010F, Tokyo, Japan] and dynamic light scattering (DLS) using a 90Plus Nanoparticle Size Distribution Analyzer; Brookhaven Instruments Corp., Holtsville, NY. A sample of the citrate-coated nanoceria was dialyzed against ten volumes of water for 24 h with 3 changes of water, then dried. Nanoceria was stored at room temperature in the dark. The nanoceria dispersion was sterilized by autoclaving prior to introduction into the dialysis cassettes.

2.3 Dissolution conditions

Nanoceria (containing ~500 µg Ce) in 1 ml of iso-osmotic citric acid was introduced into dialysis cassettes immersed in 400 ml beakers containing 200 ml of aqueous carboxylic acid solutions plus 0.02% sodium azide as a bacteriostatic and fungistatic agent. This nanoceria concentration was used by Dahle, et al. The test solutions’ pH and components are shown in Table S1. Each condition, except water, was studied in duplicate, e.g., citric acid-1 and citric acid-2. The concentration of most ligands (110 mM) was based on the concentration of citric acid to produce an iso-osmotic solution, if it totally dissociated. Horseradish peroxidase (15 nmoles) was introduced into the cassette at pH 6.1, the pH of its maximal activity. H$_2$O$_2$ was added to the bath at the beginning of the experiment and each time the bathing medium was sampled. Determination of the osmotic strength of 110 mM citric acid revealed that it did not produce an iso-osmotic solution, presumably due to the lack of complete ionization (non-adherence to van’t Hoff’s law at this concentration). Sodium nitrate was added to all solutions (except water) to bring them to iso-osmotic strength. In a separate experiment, a Ce ligand (Ce nitrate) was allowed to diffuse across the membrane in order to compare its diffusion rate to the dissolution rates of nanoceria in the various carboxylic acid solutions. The Ce ligand should diffuse at least an order of magnitude faster than the dissolution rate for the bath and cassette solutions to be near equilibrium with each other. Ce ion concentration in the bath was measured using ICP-MS.

2.4 Ce measurement

Samples containing nanoceria were digested with 2:1 HNO$_3$ : H$_2$O$_2$ in Teflon vessels in a CEM MARS Xpress microwave
digested system (Matthews, NC, USA). Tb was added as an internal standard, and analyzed compared to external calibration standards. Ce was quantified by ICP-MS (Agilent 7500cx, Agilent Technologies, Inc., Santa Clara, CA).

2.5 Nanoceria size and shape distributions
Nanoceria size and shape distributions were obtained by acquiring TEM images of cassette dispersions, using automated methods for particle capture (ImageJ), comparing distribution statistics, fitting the parameters of reference distribution models, and evaluating bivariate correlations. These are programmed in R and have been implemented in a series of ShinyApp tools that are available on the web. Changes in size and shape distributions were quantified and compared to confirm nanoceria dissolution. Five particle size and shape descriptors were measured: area, equivalent circular diameter (ECD), Feret diameter (Feret; the maximum length of the particle), minimum Feret diameter (minFeret; the maximum width of the particle), and aspect ratio (aspectR = minFeret/Feret). The ECD is an appropriate choice to link with \( d_i(t) \) in order to obtain \( n_i(t) \) (eqn (4)) in the modeling exercises.

Typically, 50 to 100 nanoceria particle images are analysed to produce repeatable size and shape distributions.

2.6 Computational methods
Density functional theory was used to estimate enthalpies of formation for possible Ce(IV) products to show whether their formation was thermodynamically favored. DFT methods have been used for a wide variety of energy calculations of lanthanides and carboxylic acids. Formation energies of possible Ce-ligand complexes were defined relative to the computed bulk energy per chemical unit of CeO₂ and the energy of isolated acid molecules. The commercially available VASP plane-wave-pseudopotential code was used for all calculations. Pseudopotentials based on the Perdew–Burke–Ernzerhof (PBE) formalism were used for all atoms. Ce 4f5s5p6d6s and O 2p2s electrons were treated as valence electrons. The wavefunction was expanded in plane waves with an energy cutoff of 400 eV. These four conditions have previously been used for DFT computations of dissociated binding of acetic acid on nanoceria surfaces in water. Calculation cells of 2 nm on a side were used for all molecule and complex calculations; these cells were large enough to accommodate one CeO₂ molecule plus carboxylic acid ligands, or a Ce-carboxylate ligand complex. A \( 1 \times 1 \times 1 \) k-point mesh centered at the \( \Gamma \)-point was used, yielding k-point densities of 2 k-points per nm, similar to those used previously for Ce-containing nanoparticles. The bulk CeO₂ reference energy was calculated for a single CeO₂ unit cell using a k-point density equivalent to that used in the molecule calculations (that is, 2 k-points per nm). Tests show that computed enthalpies are converged to within 0.1 eV with respect to k-point density. Initial atomic configurations were relaxed according to the calculated interatomic forces until binding energies were converged to \( 10^{-3} \) eV per atom or better.

3. Results and discussion
3.1 Ce salt diffusivity through the cassette membrane
The rate of diffusion of Ce ligands through the membrane should be at least an order of magnitude faster than the dissolution rate of nanoceria so that the Ce ligand concentration in the bath is near its concentration in the cassette. Ce concentration in the bath was measured as a function of time (\( M_b \)) for comparison to the amount of Ce expected in the bath at equilibrium (\( M_{eq} \)). See Fig. S2 (ESI†) to see the fits between datasets and the model for the diffusivity experiment. The half-time for the Ce nitrate diffusion process is 12.5 hours. The shortest dissolution half-life for nanoceria was 840 hours (seven weeks) in the presence of lactic acid. Using the half-life ratio, the membrane diffusion process is over 60 times faster than the nanoceria dissolution rate. The assumption that the Ce ion concentration in the bath is similar to that in the cassette appears sound.

3.2 Dissolution effects on nanoceria size and shape distributions
TEM images of cassette dispersions were used to evaluate dissolution effects on nanoceria size and shape distributions. Synthesis reproducibility with respect to nanoparticle size was good: Masui et al. reported an average nanoceria particle size of 3.9 nm (equivalent to a surface area of 211 m² g⁻¹) while this lab produced average nanoceria particle sizes of 4.24 nm (equivalent to a surface area of 196 m² g⁻¹). At this particle size, there is a mixture of Ce³⁺ and Ce⁴⁺ on the nanoceria surfaces. Fig. 2a and b show nanoceria samples at \( t = 0 \) and \( t = 7 \) weeks, respectively. Nanoceria crystallites with clear edges were outlined using ellipses and analyzed using ImageJ software. The outlined particles were chosen such that the image was deemed to be a single crystallite with clear areal boundaries.

ANOVA analysis of each descriptor for the two samples of Fig. 2 show that the means of size and shape descriptor distributions are statistically different between the two datasets, except for the Feret diameter. Therefore, the average area and the average shape of nanoceria changes as it dissolves. Fig. 3 shows the two cumulative distributions with a Rosin–Rammler curve (often used for crystallization growth information) fitted to the data by nonlinear regression. The protocol is given in ESI†.

Table S2† also shows a comparison for the predicted diameter of an average nanoceria particle at seven weeks (shown in italics) for the two experimental trials with citric acid solutions. The measured change in the equivalent circular diameter was 12%, while those predicted using the model coefficients for each experiment were 11% and 13%. Thus, there is good correspondence between the nanoceria size predicted by the surface-controlled dissolution model and the ECD particle size as estimated from the particle area.
distribution. Additional TEM images of the nanoceria at several time points and for all carboxylic acids in the study can be found in Fig. 6 of Yokel et al.74

Bivariate plots are an alternative way to show differences in size and shape of nanoparticle populations.56 Fig. 4 shows two contour plots of the aspect ratio as a function of nanoceria area for the citric 1 experiment, \( t = 0 \) and \( t = 7 \) weeks.

The starting material \((t = 0)\) appears to have two size clusters (area = 10 and 22 nm²) with the aspect ratio ranging from 0.65 to 0.98 for each of these. After seven weeks of dissolution, there are no particles with areas greater than 20 nm², no apparent bimodal appearance to the area distribution, and an expanded aspect ratio range, 0.50 to 0.98. Bivariate analysis56 of the two datasets also confirms that they are different statistically. The \( p \)-values between the two plots were much less than 0.05. Therefore, particle area is being reduced and the remaining nanoceria have a lower average aspect ratio.

The current implementation of the model assumes spheroidal particles, but TEM images demonstrate asymmetric particles after dissolution. The change in aspect ratio appears to be driven by a reduction in nanoparticle width rather than nanoparticle length. As shown in Table S2,† the two Feret diameter distributions have mean values that are similar while the two minFeret diameter distributions have different mean values. Lu et al.75 reported the dissolution of nanoceria crystallines in radiolytic water, showing a transformation to lower

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**Fig. 2** a. TEM of nanoceria as placed in the cassette. Ellipses show nanoceria outlines (ImageJ). b. TEM of nanoceria after 7 weeks of dissolution. Ellipses show nanoceria outlines (ImageJ). Citric acid = 110 mM, pH 4.5.

**Fig. 3** Feret cumulative distributions for week 0 and week 7 nanoceria dissolution in citric acid. Week 0 data is black open circles with the black curve for the fitted Rosin-Rammler equation. Week 7 data is red open circles with the red curve for the fitted Rosin-Rammler equation.

**Fig. 4** Aspect ratio/area (nm²) bivariate plots: starting sample \((t = 0)\) = left side; seven week sample = right side.
oxygen coordinated phase, Ce$_2$O$_3$. Progressive, layer-by-layer, dissolution of nanoceria crystallites at one crystal face in strong acid resulted in a change in crystallite shape from a cube to a polyhedron (Fig. 2, frames g, h, i, and j of this reference). The particle size and shape distribution changes shown in Fig. 4 are consistent with a higher rate of dissolution at a specific crystallite face.

As exposure time increased, most nanoceria particle surfaces showed effects of rounding at crystallite edges and corners, likely due to the high energy sites at these locations. This is consistent with dissolution of nanoceria in vivo within both rat liver and spleen macrophages, previously reported by Graham et al.,$^{36-38}$ and that caused significant particle rounding over time. Nanoceria surface structure near edges and corners is complex,$^{27,7,26}$ which directly impacts the local redox potentials as well as the possible surface adsorption of water and carboxylic acid moieties into the distorted crystal lattice, accelerating the dissolution rate.

3.3 Analysis of model results

3.3.1 Overall material balance. The discrete sampling approach raises the possibility that there are sampling errors. These have been quantified by estimating the error in the overall material balances for each trial. These were determined by using the ICP-MS measurements for the bath as the key metric for fitting the model to the data and computing the changes for the nanoceria in the cassette using the model. For 24 trials, duplicates of 12 experiments with two controls (horseradish peroxidase and ammonium) plus ten carboxylic acids, the average error for the overall material balances was 7.7 ± 3.2% (assuming a normal distribution for the errors). Typical error between analyses of replicate dilutions are ∼3%, accounting for about half of the material balance error. Based on these average material balance errors, dissolution rate constants have been reported to two significant digits. There was no apparent correlation between the estimated dissolution rate constants and the mass balance errors. Therefore, the experimental method was deemed appropriate for estimating apparent surface-controlled dissolution coefficients.

3.3.2 Dissolved Ce in bath: model and experiment. Fig. 5 and 6 show the measured and modelled levels of Ce in the bath for glutaric and lactic acid, respectively. The glutaric acid experiment had nine samples taken from the cassette over the course of the lactic acid experiment. Because of the higher dissolution rate, Lactic acid solutions caused nearly complete dissolution of the nanoceria prior to the end of the 28 week sampling event. For both lactic acid experiments, the predicted Ce level in the bath decreased more rapidly with time than was predicted; notice that the red open squares in Fig. 6 go through a maximum and decrease with time. Sampling removed about 11% of the nanoceria from the cassette over the course of the lactic acid experiment. Because of the higher dissolution rate, demonstrated that a model based on the empirical size distribution (binned into five fractions of 20% each and represented by their average size) provides a much better fit to the shapes of the bath Ce mass versus time plots. However, such a model would best be implemented when the minimum size of nanoceria in the bath solution is known. When this minimum stable size is reached, the unstable ceria nanoparticle should dissolve into the liquid phase. And, the minimum stable size might vary with each carboxylic acid, depending on its ability to stabilize small nanoceria particles. Such a model modification is expected to be done in future work.

Fig. 5 Ce (µg) in bath: glutaric acid. Black circles = ICP-MS data for bath; red open squares = model prediction Ce in the bath; blue open diamonds = cumulative amount of nanoceria dissolved.

Fig. 6 Ce (µg) in bath: lactic acid. Black circles = Ce in bath (ICP-MS data); red open squares = model prediction Ce in the bath; blue open diamonds = cumulative amount of nanoceria dissolved.
constant, the overall dissolution rate of nanoceria is less affected by the presence of the smallest size ‘bin’ and the model fits the initial data well. Nanoceria particles greater than the average have higher surface areas and greater loss rates of atoms per nanoparticle, per eqn (7). However, as their size becomes smaller, so does the surface area and the Ce atom loss rate, flattening the red square curve, and perhaps eliminating the maximum predicted by the model. This provides additional incentive to link the nanoceria surface area to particle size, shape, and crystallite facets.

3.3.3 Dissolution process rate coefficients. Table 1 shows the surface-controlled dissolution rate coefficients, as averages of the two experimental trials. The water and horseradish peroxidase controls are more than an order of magnitude lower than those of the carboxylic acids, confirming that these systems did not have significant levels of nanoceria dissolution.

The ammonium system has a rate coefficient about 2/3rds of those of the slowest carboxylic acid system, showing that it affects nanoceria dissolution over 28 weeks. Since ammonia water plus citric acid was used in the synthesis of these nanoceria, it is not surprising that an ammonia solution at pH 4.5 in the absence of citric acid might permit the dissolution of nanoceria particles.

Carboxylic acid solutions accelerated dissolution and the ligand matters. The pK_a’s of the acids do not correlate with dissolution rate. All of the carboxylic acids caused measurable nanoceria dissolution over this time scale. Dissolution rates are partially controlled by the particle’s surface area and occur layer-by-layer, as the particles are not porous. Since carboxylic acids are known to stabilize nanoceria during particle growth, it should not be surprising that they can influence nanoceria dissolution rates.

Vlasova and coworkers have shown that monocarboxylic acids, such as benzoic and cinnamic acids, are near their maximum surface complexation at pH 4.5, the level studied in this work. Carboxylic acids that complex with nanoceria surfaces are known to stabilize their dispersions. In related work, Yokel and coworkers74 (see Fig. 6 of this reference) have shown that lactic, malic, and succinic acids reduce agglomeration of nanoceria, while the rest of the carboxylic acids do not inhibit agglomeration. Surface complexation appears to be a dynamic equilibrium process that might slow rather than prevent dissolution.

3.3.4 Nanoceria population balance and size prediction (cassette). The nanoparticle population in the cassette versus time was different for each experiment due to variations in sampling times and the dissolution process itself. Based on the assumption that the thermodynamic driving force remains constant, the rate of dissolution from nanoceria would not be affected by changes in its population in the cassette. The discrete material balances take such changes into account and allow flexibility in system operation.

Fig. 7 shows model predictions of the number of cerium atoms in the nanoceria particles of three carboxylic acids vs. time. Lactic acid had the highest dissolution rate coefficient and, by the end of 21 weeks, nanoceria was essentially depleted from the cassette. While the discrete balance shows that particles are still in the cassette, the computed number of Ce atoms per particle is quite low. At the end of 28 weeks, both the adipic acid and glutaric acid experiments still had nanoceria nanoparticles with sizes observable by conventional TEM. The total Ce in the nanoceria is given by the product of the number of particles times the atoms in each particle.

While the surface-controlled dissolution model can calculate down to one atom of Ce in a nanoceria particle, it is more likely that there is a lower size limit for a stable nanoceria particle in the various carboxylic acid solutions. Fig. 8 shows the calculated size of nanoceria (d(t)) for a lactic acid experiment. The nanoceria diameter decreases linearly with time, which is expected since the overall dissolution rate depends on the number of Ce atoms in the particle (n_I(t)) to the 1/3rd power (eqn (7)).

Two reports suggest lower limits on the size of stable nanoceria particles. Reed and coworkers26 estimated the size

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<th>Dissolution rate coefficients: controls and carboxylic acids</th>
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<td>Key component</td>
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<td>Tricarballylic acid</td>
</tr>
<tr>
<td>α,3-Hydroxybutyric acid</td>
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<tr>
<td>Pimelic acid</td>
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<tr>
<td>Citric acid</td>
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<td>Acetic acid</td>
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<tr>
<td>Adipic acid</td>
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<td>Succinic acid</td>
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<tr>
<td>α-Malic acid</td>
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<tr>
<td>Lactic acid</td>
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![Fig. 7](Image) Number of Ce atoms in nanoparticles: solid line = glutaric acid, dashed line = adipic acid, double line = lactic acid.
of the smallest nanoceria particle as a truncated octahedron of ~2 nm that is a surface-terminated cube of ~2 × 2 × 2 nm, approximately Ce$_{80}$O$_{160}$ (no hydroxyls per an in vacuo assumption). This limit is illustrated in Fig. 8 by the dashed line crossing the $d_i(i)$ data. Assuming that a nanoceria particle less than this size would quickly ‘dissolve’, this would represent about 8% of the total Ce material for this dissolution experiment. A second potential limit for particle size was obtained by USAXS measurements for growing nanoceria particles by Allen et al. The measurements were done on a hydrothermal synthesis system based on Ce nitrate as the precursor and hexamethylene tetramine (HMT) as an agent for NH$_4$ generation in situ. Their nanoceria product had particle sizes greater than 6 nm (octahedral or truncated octahedral morphologies, with (111) and (100) faces), but they also observed fine nanoparticles (termed ‘features’) in the order of ∼1 nm. It is possible that these represent ‘stable’, Ce/HMT complexes, but there are other explanations as well. This possible limiting size is shown as the solid line in Fig. 8 and would represent only 1.2% of the total Ce in the system.

Fig. 9 shows a dissolution cascade computed for lactic acid dissolution based on the measured initial particle size distribution binned into five elements of equal particle numbers, represented by an average size, and using a 2 nm value for the minimum size of a stable nanoparticle. After 7 weeks of dissolution (1176 hours), particles in the two lower particle sizes are predicted to dissolve. For the largest and smallest of these 5 bins, the nanoparticle surfaces areas differ by a factor of ~6 so the large particles are dissolving at a much higher loss rate per particle. However, the smallest particles are much closer to the assumed minimal stable particle size and they disappear from the cosphere first.

Our high resolution TEM images of a carbon support film that was passed through the bathing medium (citric acid = 110 mM, pH 4.5 after a 16 week dissolution period) detected a few isolated, subnano-scale particles associated with the carbon film (Fig. 10). These few crystallites were in the size range of ~0.75–1 nm, which is in good agreement with Reed and coworker’s findings that nanoceria below this size limit should be unstable. Ultrafine ‘features’ have also been reported by Allen and coworkers in nanoceria growth experiments. The ultrafine particles appear crystalline rather than amorphous and may represent the minimum stable size for CeO$_2$ crystallites in the presence of citric acid. These ultrafine particles are too small for EELS analysis to determine composition (CeO$_2$ or Ce$_2$O$_3$). More work is needed to compare results for the other carboxylic acids. If ultrafine crystallites can associate with lacy carbon films (Fig. 10), then a similar uptake mechanism could also be present in vivo. Ultrafine crystallites could attach to a variety of surfaces, contributing to the long retention of nanoceria in mammalian organs that is not very well understood at this time.

### 3.4 Density functional theory: energy of formation of cerium ligand complexes

The dissolution experimental data place significant constraints on the possible atomistic mechanisms driving ligand-assisted nanoceria solubility. First, the dissolution of atoms from the surface must conserve the surface chemistry and charge as well as the conditions in the bath. Otherwise, the rate model of surface dissolution would require additional terms beyond simply the surface area of the solid particle in order to account for these changes over time. Secondly, experiments show that the ligands themselves must be directly involved in the dissolution mechanism (e.g. as a catalyst or as components in a chelated metal complex). Based on these constraints, we considered potential dissolution products from a thermodynamic perspective only, seeking to identify chelated metal complexes containing Ce($\nu$) that are more stable than the combination of precursor nanoceria (CeO$_2$) and isolated acid molecules. These DFT calculations do not assume a particular charge state on Ce when computing the energy of either bulk CeO$_2$ or Ce-containing molecules. Instead, the calculations allow redistribution of charge.

![Fig. 8](image-url) Calculated $d_i(i)$ (nm) for the lactic acid system. Open circles = predicted nanoceria diameter, dashed line = in vacuo stable particle, solid line = experimental fine particles by USAXS.

![Fig. 9](image-url) Dissolution cascade for 5 bins of nanoceria. Solid line is $d_i(0) = 2.34$ nm; small dashed line is $d_i(0) = 3.61$ nm; large dashed line is $d_i(0) = 4.24$ nm; dash/dot line is $d_i(0) = 5.01$ nm; double line is $d_i(0) = 5.87$ nm.

**Fig. 10** Proposed mechanism for the uptake of nanoceria particles from the bloodstream. The arrows indicate the possible pathways for the removal of nanoceria particles from the nanoparticles. The dashed lines represent the possible pathways for the dissolution of the nanoparticles. The solid lines represent the pathways for the uptake of the nanoparticles. The blue arrows represent the pathways for the removal of the nanoparticles from the bloodstream. The red arrows represent the pathways for the uptake of the nanoparticles into the cells. The green arrows represent the pathways for the dissolution of the nanoparticles. The black arrows represent the pathways for the uptake of the nanoparticles into the cells. The yellow arrows represent the pathways for the dissolution of the nanoparticles. The purple arrows represent the pathways for the uptake of the nanoparticles into the cells. The orange arrows represent the pathways for the dissolution of the nanoparticles. The white arrows represent the pathways for the uptake of the nanoparticles into the cells.
such that atoms in the computational system “relax” to their minimum energy state. Ce atoms coordinated to four O atoms have valence state Ce\(^{IV}\), simply because stoichiometric CeO\(_2\) is most stable when each Ce atom transfers 1 electron to each of the 4 coordinated Os. Complexes containing Ce\(^{III}\) could be formed, e.g., by adding an H atom to the double-bonded O, but doing so would imply that the CeO\(_2\) dissolution consumes H atoms, further implying that the pH of the solvent is time dependent—a situation not observed here. In addition, computing formation energies for single-ligand complexes with an additional H atom would require knowledge of the chemical potential of H in the system, which is beyond the scope of this paper.

We considered the general dissolution of exactly one CeO\(_2\) formula unit to one and/or two ligand complexes of a subset of the acids examined experimentally. Computed formation energies are referenced to the energy of perfect, bulk CeO\(_2\). In all cases, complex cerium salts with one ligand have positive formation energies, meaning that they are not thermodynamically favored. Cerium salts with two ligand complexes have negative formation energies (shown as the blue square on the enthalpy of formation scale), indicating that the complexes are more stable than a reference state of bulk CeO\(_2\) and the isolated acid molecules. There is a thermodynamic driving force for dissolution and formation of a bi-ligand salt.

Fig. 11 shows DFT-computed enthalpy of formation scale for various precursors and products. Specific Ce\(^{IV}\) dicarboxylic acid (“two-ligand”) complexes (blue block with thick border) are stable with respect to bulk CeO\(_2\) (black horizontal line). Single-ligand complexes have positive enthalpies of formation (blue block with thin border). In real systems, such as ceria nanoparticles, surface groups and defects will increase the energy of the ceria surface relative to that of the ideal bulk. Nanoceria particles (gray-colored band in Fig. 11) are less stable than perfect bulk ceria regardless of surface termination or defect concentration compared to the reference energy of bulk CeO\(_2\). If a particular combination of surface facets or defect arrangements rendered a ceria nanoparticle more stable than bulk ceria, then bulk ceria would spontaneously decompose into the nanoparticles.

Bulk Ce\(_2\)O\(_3\) surfaces, shown as the red horizontal bar in Fig. 11, have a heat of formation of +2.4 eV/Ce atom. They are less stable with respect to bulk CeO\(_2\) surfaces. The surfaces of Ce\(_2\)O\(_3\) nanoparticles will be less stable than their bulk counterpart and are indicated by the red-colored band. In O-rich conditions, surface Ce\(_2\)O\(_3\) has a positive formation enthalpy and is unstable relative to CeO\(_2\). While the exact conditions of O availability in solution are complex, we expect that conditions are sufficiently O-rich for Ce\(_2\)O\(_3\) to remain unstable with respect to CeO\(_2\). If this were not true, after long times we would expect to observe small ceria particles in the Ce\(_2\)O\(_3\) structure. Variations in the relative abundance of Ce\(_2\)O\(_3\) and CeO\(_2\) observed by EELS\(^{62}\) are only consistent with effects of decreasing particle size, and not with reduction of the nanoparticles in an O-poor environment.

Fig. 12 shows the relaxed state for a double-lactic acid cerium complex, which has the most negative heat of formation as modelled. This complex is stoichiometrically equivalent to two acid molecules plus one CeO\(_2\) unit. The bond angles between the hydroxyl groups and the lactate groups are similar and the two lactate groups have a bond angle of 128°. The
Carboxylate ‘bonds’ should be considered an electron resonating between one oxygen and the other, that is, a bidentate bond. These calculations appear to be consistent with the results of Lu for bidentate binding of acetic acid to oxidized ceria surfaces and the results of Hawkins for Ce(IV) complexes with two ligands.

Fig. 13 shows relaxed states of double- and single-glutaric acid complexes with cerium. The single-glutaric acid complex is stoichiometrically equivalent to one acid molecule plus one CeO₂ unit. These configurations yield Ce(IV) with a Ce=O bond, a hydroxyl, and coordinated with a carboxylic acid group, which has a positive enthalpy of formation and is not thermodynamically stable. Complexes containing Ce(III) could be formed, e.g., by adding an H atom to the double-bonded O but doing so would imply that CeO₂ dissolution consumes H atoms, further implying that the pH of the solution is time dependent—a situation not observed here. In addition, computing formation energies for single-ligand complexes with an additional H atom would require knowledge of the chemical potential of H in the system, determination of which, for the present experimental conditions, is beyond the scope of this paper.

The relative instability of single-ligand Ce(IV) complexes does not rule out the possibility that such single-ligand Ce(IV) or Ce(III) complexes are formed (either as an intermediate state during dissolution or as a minority product), but rather that bi-ligand Ce(IV) complexes are preferred to deprotonated (and therefore Ce(IV)-containing) single-ligand complexes. In addition, previous experiments have examined various binding geometries of carboxyl groups to CeO₂ surfaces and found that the bidentate chelating configuration is favoured over bridging and monodentate configurations. The present results are consistent with these findings, as the low-energy Ce–carboxyl configurations identified are bidentate chelating.

3.5 Comparison of heats of formation with dissolution rate coefficients

While the formation enthalpies of two-ligand complexes varies with the structure of the relevant acids, these variations do not fully explain differences in dissolution rates (Fig. 14). While the lactic acid complex does have the most negative formation energy (that is, the strongest thermodynamic driving force for complex formation, −0.94 eV per complex) and exhibits a high dissolution rate, the other acid complexes studied have formation energies and dissolution rates clustered with no obvious pattern. Succinic and glutaric acid complexes exhibit nearly identical formation energies, but significantly different dissolution rates, while the citric acid complex has a much less negative formation energy (that is, would be expected to be less thermodynamically stable) than adipic and pimelic acid complexes, but exhibits a similar dissolution rate. This implies that structural and conformational factors influence the dissolution rate mechanism in addition to thermodynamics.

Yokel et al. provided descriptive interpretations on the differential effects of carboxylic acids on nanoceria dissolution, which are relevant to in vivo and environmental systems. EELS plots in this reference (Fig. 7) have been used to...
dissolved, %. Ratios of Ce\textsuperscript{3+}, Ce\textsuperscript{4+} EELS peak heights from Fig. 7 of Yokel et al.

4. Conclusions

The dialysis cassette experiment coupled with a surface-controlled dissolution model appears to be a sound method for estimating dissolution rate coefficients for nanoceria exposed to a variety of carboxylic acids. This model predicts that the number of atoms dissolved per unit time is directly proportional to nanoparticle surface areas; larger particles dissolve faster. The general approach could be extended to study the dissolution of other metal oxides and metals in various aqueous systems relevant to environmental and medical exposures. All of the carboxylic acid solutions dissolved nanoceria at pH 4.5, producing soluble products. Comparison of initial and seven week dissolution populations using TEM images verified that nanoceria size and shape varied due to dissolution. ANOVA and bivariate analysis of size and shape descriptor distributions confirmed that dissolution created statistically different nanoceria populations. The surface-controlled dissolution model fit the nanoceria dissolution data for all carboxylic acids and the experimental controls using the ECD descriptor to represent \( d_{ij}(t) \). Lactic acid solutions gave dissolution rate coefficients of 0.014 Ce atoms h\textsuperscript{-1} nm\textsuperscript{-2} with the coefficients of the other carboxylic acids ranging from 1/3 to 1/2 of this value.

DFT calculations on possible soluble Ce-carboxylates showed that di-ligand complexes with the carboxylic acids of this study should be thermodynamically stable and would have bidentate bonding between cerium and ligand. Careful comparison of experimental and model results to nanoceria literature suggest that models of the dissolution process could be improved by: 1) better understanding of the lower size limit for stable nanoparticles in aqueous media, 2) implementing the model with empirical nanoparticle size distributions rather than an average diameter, 3) determining the dissolution rates of different crystallite surfaces in carboxylic acid solutions, which could lead to acentric shape distributions, 4) implementing particle shape in the dissolution model, and 5) confirming 3) with analyses of crystallite structure during the dissolution process. Estimates of the energy of formation for some possible dissolution products of CeO\textsubscript{2} show that Ce(VI) complexed with two carboxylic acid ligands in bidentate structures would be thermodynamically possible. Since the dissolution rate coefficients do not seem to correlate with either p\textsubscript{Ka} of the various carboxylic acids or estimates of the energy of formation for some possible dissolution products, it appears likely that nanoceria surface structures plus ligand adsorption mechanisms could contribute to the dissolution process.

Author contributions

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Conflicts of interest

There are no conflicts of interest to declare.

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References


