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Cite this: *Energy Environ. Sci.*,  
2019, 12, 656

# Quantifying lithium concentration gradients in the graphite electrode of Li-ion cells using *operando* energy dispersive X-ray diffraction†

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Safe, fast, and energy efficient cycling of lithium ion batteries is desired in many practical applications. However, modeling studies predict steep  $\text{Li}^+$  ion gradients in the electrodes during cycling at the higher currents. Such gradients introduce heterogeneities in the electrodes, which make it difficult to predict cell lifetimes as different portions of the cell age at different rates. There is a dearth of experimental methods to probe these concentration gradients across the depth of the electrode. Here we use spatially resolved energy dispersive X-ray diffraction to obtain a “movie” of lithiation and delithiation in different sections of the cell and quantify lithium gradients that develop in a porous graphite electrode during cycling at a 1C rate. Inhomogeneity in the total Li content, and in the individual ordered  $\text{Li}_x\text{C}_6$  phases formed during lithium insertion into (and extraction from) the graphite, has been observed in an *operando* fashion. The complex dynamics of lithium-staging in graphite with the distinct front propagation of phase changes have been characterized and new features of these dynamics are highlighted here. As large  $\text{Li}^+$  ion gradients contribute to cell polarization, our results suggest that Li plating conditions can be met near the graphite electrode surface, even when the cell is charged at a moderate (1C) rate.

Received 14th August 2018,  
Accepted 15th November 2018

DOI: 10.1039/c8ee02373e

rsc.li/ees

## Broader context

To meet the expectations of today's consumers, charging of lithium-ion batteries in electric vehicles needs to become faster for these vehicles to become more widely adopted. A major obstacle to increasing the charging current is the steep gradient in lithium concentration that develops in the electrode matrix when the lithium ion flux into the active material, driven by the applied current, exceeds the transport capability of the electrolyte and/or the material. While numerous modeling studies have predicted such inhomogeneity, there are few experimental studies in which such concentration gradients are observed directly with the required temporal and spatial resolution. Here an *in situ* X-ray technique is used to obtain a “movie” of graphite electrode lithiation and delithiation during cycling of a cell at a  $\sim 1\text{C}$  rate (full discharge in 1 hour). As lithium intercalates between the graphene layers, ordered  $\text{Li}_x\text{C}_6$  phases emerge in succession, which are identified and quantified through their X-ray diffraction patterns. Our results provide evidence for steep gradients in the  $\text{Li}_x\text{C}_6$  phase concentration, and in the total concentration of intercalated lithium, in the direction of the ionic current. Previously predicted behaviors, and surprising new features still awaiting an explanation, are revealed in this study.

## 1. Introduction

Faster charging of Li-ion batteries (LIBs) would enable wider adoption of electric vehicles, as it would shorten the time needed to refill these vehicles bringing it closer to consumer's

expectations informed by the use of gasoline-fueled cars. The current LIBs predominantly use porous graphite (Gr) anodes (negative electrodes) and layered metal oxide cathodes (positive electrodes). At cycling rates below 1C (full discharge in 1 hour), these LIBs can go through hundreds of cycles of operation with minimal performance degradation. However, at higher cycling rates, the capacity, cycle life, and thermal stability of these LIBs is known to degrade.<sup>1–9</sup> Theoretical studies of lithium intercalation using Newman-type models<sup>10</sup> attribute these effects to lithium plating, kinetic losses, and  $\text{Li}^+$  concentration gradients (causing polarization of the cell) occurring both in the electrolyte filling the matrix pores and in the graphite electrode itself.<sup>9,11,12</sup> Our focus

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† Electronic supplementary information (ESI) available. See DOI: 10.1039/c8ee02373e



will be the latter gradients that are a complex function of  $\text{Li}^+$  diffusion coefficients, intercalation rates, ion transference numbers, and the electrode thickness ( $t$ ), porosity ( $\epsilon$ ), and tortuosity ( $\tau$ ).<sup>9–11</sup> For example, low porosity and high tortuosity in the electrode decrease the effective diffusion coefficient  $D_{\text{eff}} = (\epsilon/\tau)D_{\text{bulk}}$  of the  $\text{Li}^+$  ions in the matrix relative to the solvent bulk.<sup>13,14</sup> At high charge rates, this lower mobility leads to greater differentials in lithium concentration in the direction of the flowing  $\text{Li}^+$  ion current (that we take as the  $z$ -direction of the laboratory frame with  $z = 0$  corresponding to the electrode surface near the separator between the electrodes).<sup>10,12,15,16</sup>

Such  $\text{Li}^+$  ion gradients are problematic on at least three counts. First, they impose gradients in the lithium intercalation rates and the corresponding electrode overpotentials.<sup>1,17,18</sup> The latter causes polarization of the cell, so the cut-off voltage can be reached prematurely before Li is fully extracted from the cathode, resulting in a lower capacity. Second, this heterogeneous lithiation can lower the (negative) electrode potential creating conditions facilitating lithium plating, especially in regions adjacent to the separator.<sup>9,18</sup> Third, these  $\text{Li}^+$  gradients facilitate structural stresses within the graphite particles (causing their fracture)<sup>17,19–21</sup> and in the electrode matrix at large (causing the coating to peel off the current collector).<sup>18,20</sup> The higher the current flowing through the cell, the steeper the  $\text{Li}^+$  gradients, and greater their effect on cell performance and life.

Graphite electrodes have particularly high tortuosities due to the high aspect ratio of the pancake-shaped flakes.<sup>13</sup> The effects of the packing of such particles on a cell's electrochemical performance have been demonstrated by Billaud *et al.*<sup>22</sup> Out-of-plane alignment of graphite flakes in a strong magnetic field resulted in tripling of the specific discharge capacity at 1C rate, as the axial tortuosity of the electrode matrix decreased from  $\sim 14$  to  $\sim 3.8$  after this alignment.<sup>22</sup> This problem is compounded by another concern inherent to the lithiated graphite as a charge storage medium: the potential for Li insertion into the graphite (85 to 220 mV vs.  $\text{Li}/\text{Li}^+$ ) is perilously close to the Li plating potential,<sup>23–26</sup> so even a relatively small electrode overpotential can result in Li deposition on the graphite particles competing with Li intercalation into the particles.

While there have been many modeling studies of concentration gradients developing in LIBs during high-current cycling,<sup>10</sup> the experiments directly observing and quantifying these gradients are still lacking. With this study, we seek to close this gap in knowledge. To this end, we use energy dispersive X-ray diffraction (EDXRD) to spatially resolve Li concentration profiles during cycling of a Li-ion cell at 1C rate. With this technique, narrowly focused polychromatic (“white light”) beams of synchrotron photons are used to obtain diffraction patterns at a fixed angle  $\theta$ , so the Bragg condition,  $2d \sin \theta = n \times \lambda$ , is satisfied for some wavelengths  $\lambda$  in the light continuum. This method is complementary to the commonly used angle-dispersive XRD method, which uses monochromatic X-ray beams and scans the angle  $\theta$  to satisfy the Bragg condition. As lithium intercalates into the graphite crystal, it fills layers

between the graphene sheets (“staging of the graphite”) yielding distinctive, ordered  $\text{Li}_x\text{C}_6$  phases ( $0 \leq x \leq 1$ ) that can be easily recognized even from a single Bragg peak. The intensities of these peaks can be used to quantify the concentration of each  $\text{Li}_x\text{C}_6$  phase, and through such quantification we determine the exact phase composition of each probed layer in the solid matrix. As only ordered  $\text{Li}_x\text{C}_6$  phases contribute to the diffraction signal, this method is blind to  $\text{Li}^+$  ions in the electrolyte and/or potential disordered solid compounds in the matrix. Using the EDXRD technique, the succession of  $\text{Li}_x\text{C}_6$  phases formed during the electrochemical lithiation and delithiation of graphite has been studied with a spatial resolution of 20  $\mu\text{m}$  and a time resolution of one minute. Below we describe how this technique helps to quantify and visualize lithium gradients in the electrode and discuss the insights obtained from these data. Figures and tables with index S (e.g. Fig. S1) are contained in the ESI.†

## 2. Experimental

### 2.1. Materials

A standard 2032-type coin cell, containing a Gr based anode and a  $\text{Li}_{1.03}(\text{Ni}_{0.5}\text{Co}_{0.2}\text{Mn}_{0.3})\text{O}_2$  (NCM523) based cathode, was used in our experiments. The detailed composition, sources, and properties of the cell materials are given in Table S1 (ESI†). Briefly, the anode contained 92 wt% graphite, 2 wt% conductive carbon particles, and 6 wt% polymer binder, while the NCM523 cathode contained 90 wt% oxide, 5 wt% conductive carbon particles, and 5 wt% polymer binder. The slurries were prepared by mixing the particles in a planetary centrifugal mixer using *N*-methyl-2-pyrrolidone as a solvent. Electrode laminates were fabricated by casting these slurries onto a 10  $\mu\text{m}$  battery grade copper foil for the Gr electrode and 20  $\mu\text{m}$  battery grade aluminum foil for the NCM523 counter electrode, using a battery coater at the Cell Analysis, Modeling and Prototyping (CAMP) facility at Argonne National Laboratory (ANL). After drying of the solvent, the Gr electrode was calendered to obtain uniform thickness. The NCM523 cathode was not calendered, in order to retain maximum porosity in the matrix and ensure minimal interference during the high rate cycling. Before cell assembly, the electrodes were dried at 120  $^\circ\text{C}$  for 12 h, and the separator was dried at 70  $^\circ\text{C}$  for 24 h, both in a vacuum oven. The assembled cell contained 40  $\mu\text{L}$  of 1.2 M  $\text{LiPF}_6$  in ethyl carbonate/ethyl methyl carbonate mixture (3:7 w/w). This electrolyte filled a microporous Celgard 2325 separator sandwiched between the two electrodes (1.58  $\text{cm}^2$  areas). The Gr electrode had an areal capacity of  $\sim 5 \text{ mA h cm}^{-2}$ ; a positive-to-negative electrode capacity ratio of 1.13 was chosen to enable deep lithiation and delithiation of the graphite electrode.

### 2.2. Cycling conditions

The cycling tests were conducted at 30  $^\circ\text{C}$ . The C-rates, state-of-lithiation, and cell capacities were calculated with respect to the theoretical capacity of the Gr, which is 372  $\text{mA h g}^{-1}$ . The applied current of 5.6 mA corresponded to a  $\sim 1\text{C}$  rate for the full cell. Prior to the XRD experiment, the cell was cycled twice

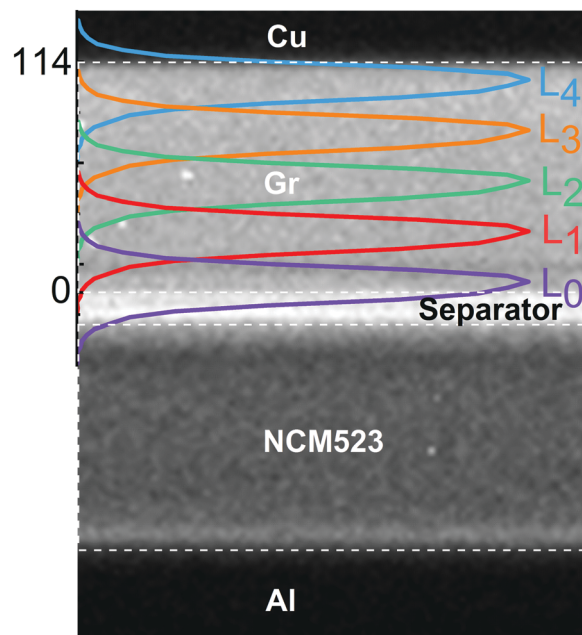


at a C/20 rate in the 3–4.1 V range (see Fig. S1, ESI<sup>†</sup>), in order to stabilize the solid electrolyte interphase (SEI) on the graphite electrode; this SEI protects the graphite from solvent intercalation and the electrolyte from runaway reduction reactions on the electrode. Three additional cycles were conducted during the XRD experiment: the cycling was performed in a galvanostatic regime until an upper cut voltage of 4.4 V or a lower cut voltage of 3.0 V were attained on charge (Gr lithiation) and discharge (Gr delithiation), respectively. Upon attainment of the set voltages, the cell operated in a potentiostatic regime for 30 min (referred to as “potentiostatic hold”).

### 2.3. Energy dispersive X-ray diffraction (EDXRD)

The EDXRD setup at beamline 6BM-A of the Argonne's Advanced Photon Source was used to observe the diffraction patterns of the pristine graphite and ordered  $\text{Li}_x\text{C}_6$  phases in an operating Gr/NCM523 cell described above. The X-ray photons with energies between 5 and 250 keV (that corresponds to 47 to 1 Å in  $d$ -spacing) readily transmit through the stainless-steel casing of the coin cell. A Ge detector placed at a fixed angle  $\theta \approx 3^\circ$  in the vertical plane with respect to the incident X-ray beam collected and averaged the diffraction patterns at a rate of 1 min per acquisition for a total period of 3 h per charge/discharge cycle. The probe X-ray beam was  $18.3 \mu\text{m}$  (fwhm)  $\times$   $1045 \mu\text{m}$ ; this beam propagated along the plane of the Gr electrode “slicing” it in steps of  $25 \mu\text{m}$ , to give a total of five minimally-overlapping layers numbered from  $L_0$  to  $L_4$  in Fig. 1 (see Section S1, ESI<sup>†</sup> for calculation of layer centroids). The X-ray power in the overlapping region was calculated to be  $\sim 12\%$  of the total beam power. The absolute position of the coin cell with respect to the X-ray beam in the transverse direction was controlled using a stepper motor, and care was exercised to perfectly align the beam with the plane of the Cu current collector. As shown in Fig. 1, layer  $L_0$  was adjacent to the separator and layer  $L_4$  was adjacent to the Cu current collector.

In order to establish the position of the  $10 \mu\text{m}$  thick Cu current collector supporting the Gr coating within the reference frame of the X-ray diffractometer stage, we took the following steps. First, the current collector was located using a coarse scanning of the incident X-ray beam along the entire thickness of the cell noting the stage position and the intensity (or absence thereof) of the  $\text{Cu}(002)$  peak at  $\sim 1.808 \text{ \AA}$   $d$ -spacing. Upon identifying a strong presence of the  $\text{Cu}(002)$  peak, a fine  $5 \mu\text{m}$  step scan in a narrow  $30 \mu\text{m}$  span around the Cu position was collected. By fitting a Gaussian shape to the collected intensities of the  $(002)$  peak during the scan, the estimated position of maximum intensity was taken as the midsection of the foil and used as reference in positioning the slices across the graphite electrode. To obtain the profile of the beam as it crosses the Gr matrix, a radiograph through the cell was collected (Fig. 1). The pixel intensity map represents the beam intensity distribution, which is overlaid onto the radiograph. The five layers were sampled in a round-robin fashion. To obtain the gradient plots discussed later, linear interpolation was used to bring the elucidated  $\text{Li}_x\text{C}_6$  concentrations found in the successive measurements to the same points in time.



**Fig. 1** X-ray radiograph of the cell used in our study (a transverse cross section), showing the  $10 \mu\text{m}$  thick Cu current collector (at the top), the  $114 \mu\text{m}$  thick porous graphite electrode, the separator, the  $111 \mu\text{m}$  thick cathode, and the  $20 \text{ mm}$  thick Al current collector (at the bottom). The X-ray beams ( $20 \mu\text{m}$  nominal height) penetrate the cell from the left. Gaussian-shaped colored lines represent the actual profiles of the X-ray beam as determined from a radiograph intensity map and by the depth calibration. Layers  $L_n$  ( $n = 0-4$  with  $n$  increasing in the direction of the electrode depth  $z$  away from the separator) are overlapping sections of the cell that are probed by the X-ray beams. During charge, a  $\text{Li}^+$  ion current flows from the NCM523 cathode to the Gr anode (graphite lithiation); the reverse happens during discharge (graphite delithiation). The depth  $z$  (in  $\mu\text{m}$ ) is shown to the left of the Gr image.

The Li-Gr intercalation system exhibits several phases (commonly referred to as stages). Through literature review, five main stages are identified and deconvoluted from the spectra collected using their reported  $d$ -spacing ranges: dilute stage I (denoted  $I'$ ), stage IV/III, stage III, stage II, and stage I.<sup>26–29</sup> The following equation is used to estimate the average lithium content  $x$  of each layer (expressed in Li atoms per  $\text{C}_6$ ):

$$x = \sum_i x_i = \sum_i \Gamma_i / \sum_j f_j^{-1} \Gamma_j \quad (1)$$

where  $\Gamma_j = I_j^{hkl} / (m_j^{hkl} |F_j^{hkl}|^2)$ ,  $f_j$  is the fractional Li content of the corresponding  $\text{Li}_x\text{C}_6$  phase  $j$ ,  $I_j^{hkl}$  is the relative integrated flux of scattered X-ray photons from phase  $j$ ,  $m_j^{hkl}$  is the multiplicity of the Bragg reflection with the Miller indices  $(hkl)$  originating from phase  $j$  in the peak region of interest, and  $F_j^{hkl}$  is the corresponding scattering factor (see Section S2, ESI<sup>†</sup> for derivation of this equation). These parameters are given in Table S2 (ESI<sup>†</sup>). Because each layer probes a different section of the cell, the corresponding X-ray fluxes have been normalized by the flux of photons scattered by the graphite in each probed layer prior to the electrochemical experiment, as explained in Section S2 (ESI<sup>†</sup>). The quantities  $\Gamma_j / \sum_i \Gamma_i$  represent the





normalized average concentration of phase  $j$  in the probed volume, whereas  $f_j$  in eqn (1) gives the Li content in each phase  $j$  (per  $C_6$  units in the graphite matrix). These quantities are independent of the material distribution, porosity, and masking of the X-ray beam by non-graphitic materials. The stoichiometry of stages I' and IV/III which are solid solution stages (the average Gr interlayer spacing increases with lithiation) varies with cell capacity. For these stages, a linear fit to  $d$ -spacing vs. capacity ( $f_j \approx 1.53 \cdot d - 5.11$ ) was used to estimate the Li content.<sup>26</sup>

### 3. Results

The voltage–capacity curves from the Gr/NCM523 cell during cycling at a C/20 rate (cycle 2, 3–4.1 V) and a 1C rate (cycle 5, 3–4.4 V) are shown in Fig. 2. From the measured specific capacity, one can calculate the cell average lithium content  $\bar{x}$  that we express in Li atoms per  $C_6$  unit of the graphite present in the electrode; the  $\bar{x}$  value is given at the top of Fig. 2. During 1C galvanostatic charging, the upper cut-off voltage of 4.4 V was attained at  $\bar{x} = 0.58$ , which increased to  $\bar{x} = 0.68$  at the end of the 30 min potentiostatic hold. During the 1C discharge, the lower cut voltage of 3.0 V was attained at  $\bar{x} = 0.1$ , which decreased to  $\bar{x} = 0.02$  at the end of the 30 min hold.

Typical XRD patterns collected during the continuing cycling are shown in Fig. 3. Only X-ray data collected during the fifth cycle are given below to highlight the major features and trends observed during cell cycling; data from cycles 3 and 4 showed similar features and are included in Fig. S2 (ESI†). In the  $d$ -spacing range shown, only the major Bragg peak for each

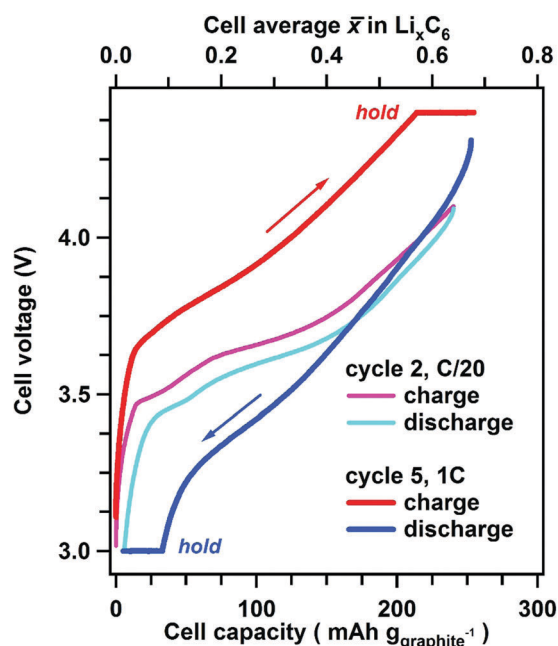


Fig. 2 Voltage–capacity plots for cycling of Gr/NCM523 cell at C/20 and 1C rates (cycles 2 and 5, respectively). Specific capacities of the graphite electrode are shown at the bottom, and the estimated cell average lithium content of this electrode is shown at the top. The arrows indicate the direction of the  $\text{Li}^+$  ion current. For cycle 5, the red color corresponds to charge and the blue color corresponds to discharge of the cell.

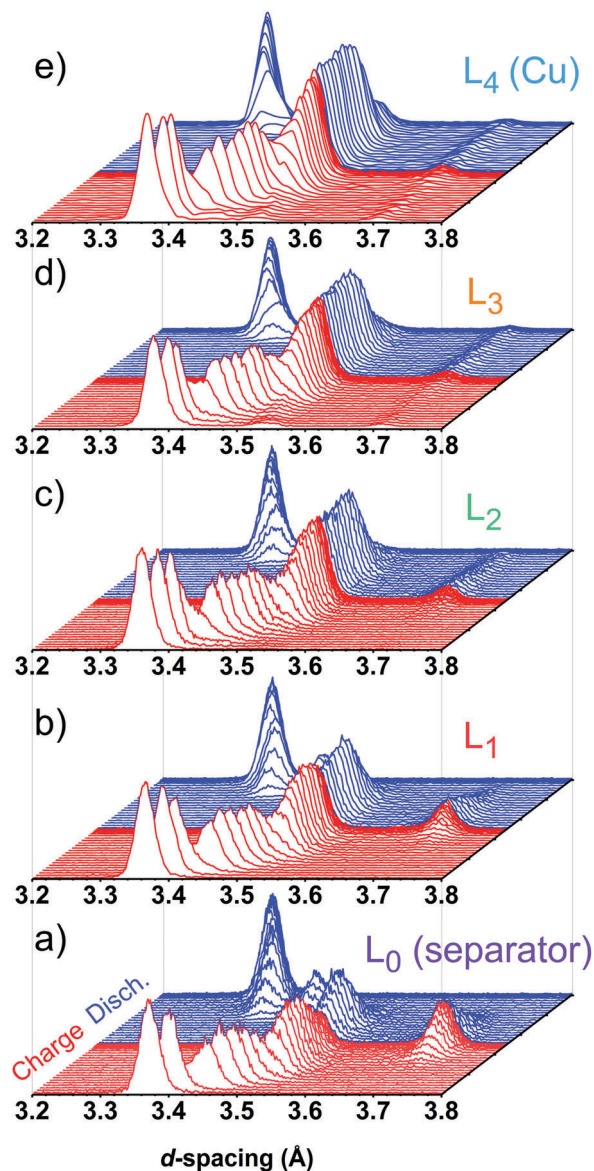


Fig. 3 XRD patterns in the 3.2–3.8 Å  $d$ -spacing region collected during charge and discharge of the cell at a 1C rate (cycle 5 shown in Fig. 2). Panels (a) to (e) correspond to layers  $L_0$  to  $L_4$ , respectively, as labeled in Fig. 1. The diffraction intensities have been normalized by the initial intensity of the graphite in each layer and shown on the same scale. The red color corresponds to charge and the blue color corresponds to the discharge of the cell. Different Bragg peaks in this plot correspond to different 'stages' of graphite lithiation, as explained in the text.

one of the  $\text{Li}_x\text{C}_6$  phases is visible. The  $d$ -spacings corresponding to these peaks are shown in Fig. 4 and their Miller indices are listed in Table S2 (ESI†). For example, stage I ( $\text{LiC}_6$ ) is represented by (001) peak, stage II ( $\text{LiC}_{12}$ ) by (002) peak, and stage IIL ( $\text{LiC}_{18}$ ) by (004) peak. The peaks of stage I', stage IV/III, and stage IIL overlap in  $d$ -spacing (Fig. 3). An uncertainty is introduced during deconvolution of the XRD pattern into pseudo-Voigt profiles that was used for integration; the associated errors in the quantification of lithium content can become significant especially after the formation of stage IIL ( $\text{LiC}_{18}$ ).



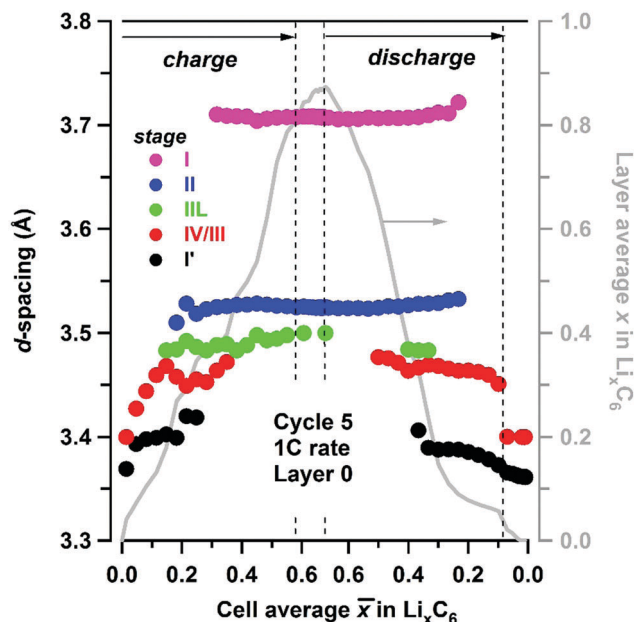


Fig. 4 Experimental  $d$ -spacing (filled circles, axis to the left) for  $\text{Li}_x\text{C}_6$  phases present in layer  $L_0$ , observed during cycling at 1C rate and plotted as a function of the cell average lithium content  $\bar{x}$  in the matrix. The lithiation stages are color-coded as shown in the inset. The vertical dashed lines indicate the potentiostatic hold. Shown to the right in grey is the layer average lithium content  $\bar{x}$  calculated using eqn (1).

Another source of error arises from uncertainties in the scattering factors themselves (see Section S2, ESI†). For convenience, the concentrations of the  $\text{Li}_x\text{C}_6$  phases reported below have been adjusted by the fractional Li content  $f_i$  of the phases; therefore these concentrations reflect the availability of Li in each phase averaged in a given layer.

For the slow C/20 cycle, the voltage–capacity curves shown in Fig. 2 reveal characteristic steps attributable to the graphite electrode (known as “stages”); the stages of graphite correspond to progressive filling of spaces between the adjacent graphene sheets. As the cycling rate increases to 1C, these steps become blurred due to Li heterogeneity in the matrix, but the distinct  $\text{Li}_x\text{C}_6$  phases are seen in the X-ray diffraction patterns during layer-by-layer sectioning as shown in Fig. 3. In particular, a well-separated Bragg peak at 3.7 Å is observed, which originates from the  $\text{LiC}_6$  phase (stage I in Fig. 4) that is formed in the final stages of lithiation. Excess Li transported to the graphite matrix beyond this final stage can become deposited as Li metal. Also clearly distinguished at the outset of charging is the rapid disappearance of dilute  $\text{Li}_x\text{C}_6$  phases that correspond to a solution of Li in graphite (stage I' in Fig. 4). For this stage I' ( $x < 1/8$ ) and stage IV/III ( $1/4 < x < 1/3$ ) peaks, the  $d$ -spacing changes with the extent of the lithiation  $x$  (as the unit cell dilates when the lithium content increases), whereas for stages I ( $x = 1$ ), II ( $x = 1/2$ ), and III ( $x = 1/3$ ) this dependence is weak. The gaps seen in Fig. 4 correspond to lithiation regimes in which the peak positions cannot be determined due to weakness of the corresponding Bragg peaks relative to the prevalent  $\text{Li}_x\text{C}_6$  phases. For  $\bar{x} > 0.3$ , the two prevalent phases,  $\text{LiC}_6$  and  $\text{LiC}_{12}$ , yield almost all of the

diffraction signal. At peak charge ( $\bar{x} \approx 0.68$ , Fig. 4) the layer average lithiation  $x$  for layer  $L_0$  as positioned in Fig. 1 is  $\sim 0.87$ ; as the  $\text{LiC}_6$  phase permeates this layer, relatively little  $\text{LiC}_{12}$  is observed.

Due to this pinning of lattice parameters and relatively strong scattering factors of  $\text{LiC}_6$  and  $\text{LiC}_{12}$  phases, their concentrations can be determined more accurately than those of the other  $\text{Li}_x\text{C}_6$  phases. In Fig. 5 we show the time progression of the  $\text{LiC}_6$  and  $\text{LiC}_{12}$  phase concentrations during cycling; the changes in the other stages/phases are included in Fig. S3 and S4 (ESI†). Near the electrode surface, the concentration profiles for lithiation and delithiation mirror each other, whereas deeper into the matrix they become asymmetric as it takes time for the formation and depletion fronts to reach the back of the electrode matrix during charging and discharging of the cell, respectively. The onset of  $\text{LiC}_{12}$  formation in layer  $L_0$  is at  $\bar{x} > 0.2$ ; for  $\bar{x} > 0.4$  this phase begins to convert to  $\text{LiC}_6$  that reaches the maximum concentration of 0.72 at the peak charge. Conversely, at this peak charge, the concentration of  $\text{LiC}_6$  in  $L_4$  at the back of the Gr electrode is lower than 0.1, indicating a steep gradient of the  $\text{LiC}_6$  phase in the cell.

These differences are more clearly seen in Fig. 6, in which we show the concentrations of all stages in layers  $L_0$  and  $L_4$ . On lithiation, the extrema stages I' and I decrease from a

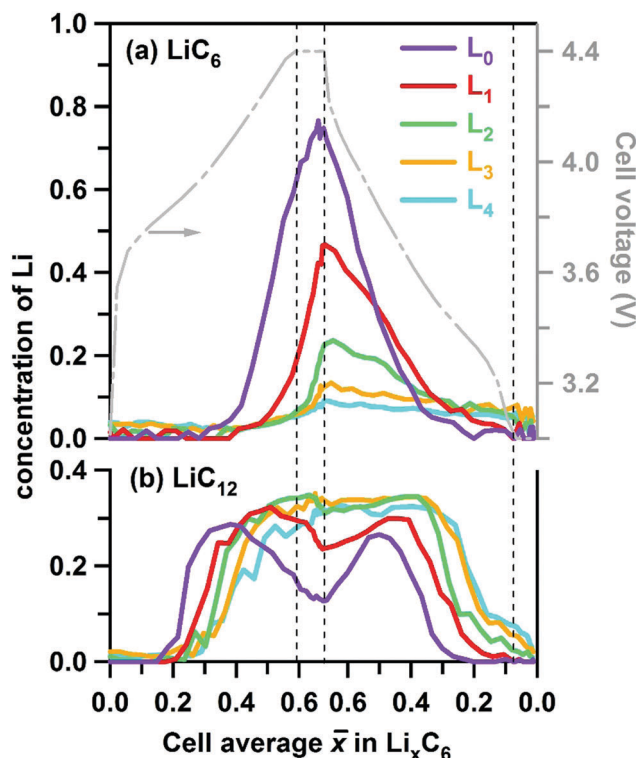


Fig. 5 Layer average Li content of (a)  $\text{LiC}_6$  and (b)  $\text{LiC}_{12}$  phases given in atoms per  $\text{C}_6$  units in the graphite matrix (to the left) and plotted as a function of the cell average lithium content in this matrix during charge and discharge at 1C rate. The vertical dashed lines indicate the 30 min potentiostatic hold periods. The cell voltage is shown by the grey line (see axis to the right). The five layers are in the order of increasing depth and color coded as in Fig. 1 above.



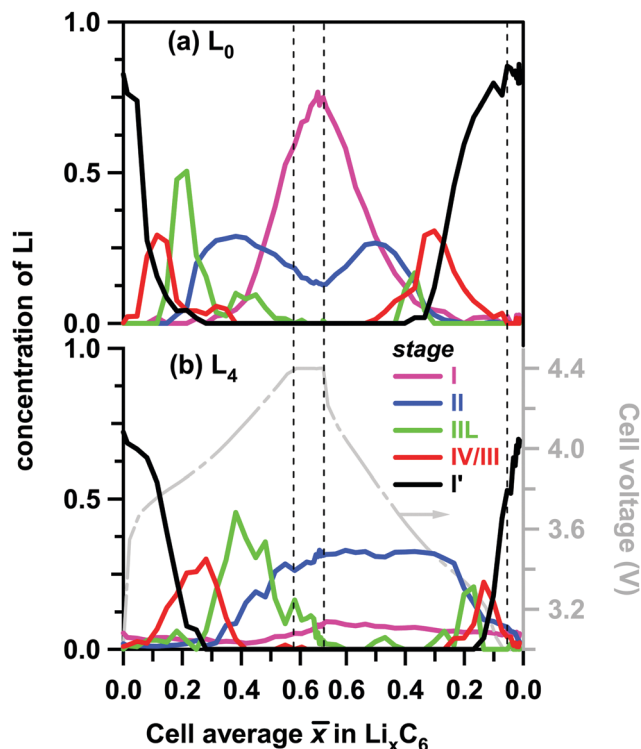


Fig. 6 Layer average Li content in the ordered  $\text{Li}_x\text{C}_6$  phases (to the left) plotted as a function of the cell average Li content in the graphite matrix during charge and discharge at 1C rate. The color scheme for the lithiation stages in the inset follows the conventions of Fig. 4 above. Panel (a) is for layer  $L_0$  (near the separator) and panel (b) is for layer  $L_4$  (near the Cu current collector). Shown to the right in grey is the cell voltage. Stages I, II, III, IV/III and I' are distinguished by their XRD patterns and associated with the  $\text{Li}_x\text{C}_6$  phases with  $x = 1$ ,  $x = 1/2$ ,  $x = 1/3$ ,  $1/6 < x < 1/4$ , and  $0 < x < 1/8$ , respectively.

maximum value or grow from a minimum value, respectively. In layer  $L_0$  where almost complete lithiation is observed, stage I reached a maximum concentration of  $\sim 0.75$  in good agreement with the initial concentration of stage I' of 0.76. The intermediary stages IV/III, IIL, and II all show concentration peaks reflecting their formation, growth, and conversion to subsequent stages. Note that each of these three stages peak at a delayed time (that is, greater  $\bar{x}$ ) in the back layer  $L_4$  relative to their counterpart in the surface layer  $L_0$ . As the lithiation progresses, the  $\text{LiC}_{12}$  phase arises. Even in layer  $L_0$  this  $\text{LiC}_{12}$  phase is not fully replaced by  $\text{LiC}_6$ , and residual  $\text{LiC}_{12}$  remains in layer  $L_4$  even at the peak of charge. In this deepest layer, during discharge of the cell (delithiation of graphite) the  $\text{LiC}_6$  and  $\text{LiC}_{12}$  phases also persist much longer than in the surface layer; it takes time for the lithium to flow out of the electrode before the depletion front reaches the back of the cell. Intriguingly, some of these  $\text{Li}_x\text{C}_6$  phases persist in the electrode even after the 30 min potentiostatic hold at 3 V.

Using the concentration of each phase, the layer average Li content of layers  $L_0$  through  $L_4$  can be determined using eqn (1) and compared with the cell average Li content  $\bar{x}$  determined electrochemically (see Fig. 7 and Table S3, ESI†). We reason that for sufficiently smooth concentration profiles the arithmetic

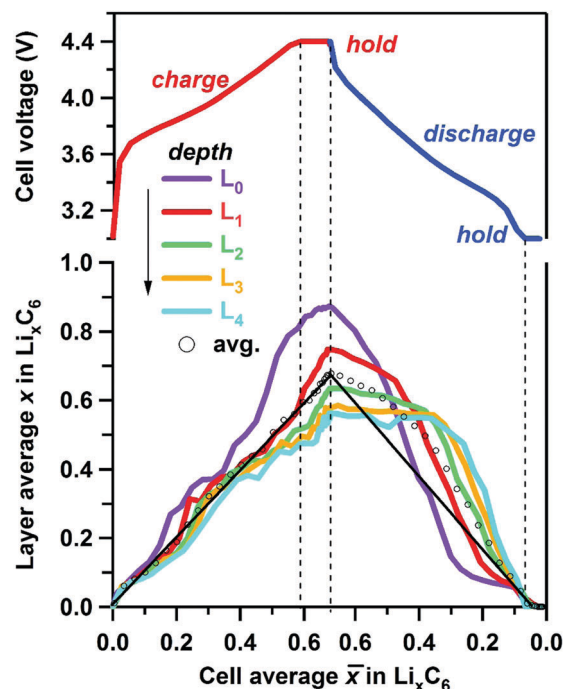


Fig. 7 Layer average lithium content  $x$  in the ordered  $\text{Li}_x\text{C}_6$  phases estimated using eqn (1) plotted as a function of the cell average lithium content of the graphite matrix determined electrochemically. The layers are color coded as shown in the inset. The vertical dashed lines correspond to the potentiostatic hold periods (see voltage plot at the top). The arrow shows the direction of increasing depth. The open circles indicate the five-layer average, and the straight line is  $\bar{x}$ .

average of these layers would be sufficiently close to the cell average (open circles in Fig. 7), *i.e.* the two metrics are expected to be close to each other (straight black lines in Fig. 7). This is indeed the case during charge, and this validation gives us certain confidence in our use of eqn (1). It is also seen from these plots that at the peak of charge,  $x$  for  $L_0$  is considerably above the cell average  $\bar{x}$ , whereas  $x$  for  $L_4$  is significantly below  $\bar{x}$ . The inhomogeneity in the quantity of individual phases in each layer across the graphite electrode (greater amount of  $\text{LiC}_6$  at the electrode surface compared to deeper layers for example) as shown in Fig. 5 and 6 is reflected in the calculated Li content of the layers, with significant difference observed only when  $\bar{x} > 0.2$ . A surprising feature of Fig. 7 is the asymmetry of the traces: the delithiation of the electrode does not mirror the lithiation run “in reverse”; this asymmetry becomes even more noticeable for the deepest layers. Most strikingly, during the rapid discharge (in contrast to charge) the arithmetic mean of layer averages (open symbols in Fig. 7) strongly deviates from  $\bar{x}$  for  $\bar{x} > 0.3$ , suggesting (among other possibilities) that the Li concentration profile may have sharp features, so our averaging of the layer Li contents becomes a poor estimate of the actual average Li concentration.

To better visualize the inhomogeneities across the electrode, in Fig. 8 we plot Li content in each layer at different states of charge as a function of the centroid depth; this information is also given in Table S3 (ESI†). The smooth lines drawn through these symbols are B-splines added as a guide to the eye. In the





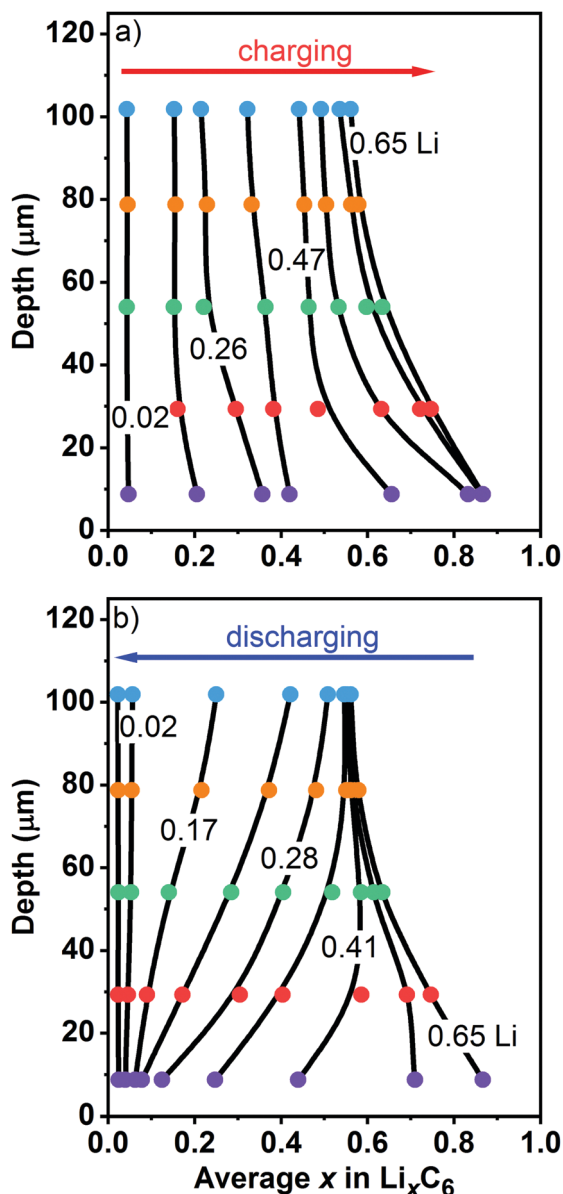


Fig. 8 Layer average Li content  $x$  in the ordered phases (filled circles, to the bottom) plotted vs. the median depth of these layers (to the left). Panel (a) is for charge and panel (b) is for discharge of the cell at 1C rate vs. the graphite electrode capacity. On charge, Li-content lines are shown for of 0.02, 0.18, 0.26, 0.34, 0.47, 0.58, 0.63, and 0.65. On discharge, Li-content lines are shown for of 0.65, 0.52, 0.41, 0.33, 0.28, 0.23, 0.17, 0.10, and 0.02. The layers are color coded as in Fig. 1 and 7 above. The smooth lines are guides to the eye. The numbers in the plot give the overall cell average lithium content of the graphite matrix calculated based on the electrochemically measured cell capacity.

initial stages of charging (Fig. 8a), the Li content is nearly uniform across the electrode. As the cell is charged further, a concentration gradient develops, with more lithium present near the surface ( $L_0$ ) than at the back ( $L_4$ ). This transformation nearly coincides with the moment when  $\text{LiC}_6$  becomes the prevalent phase near the surface in this particular graphite electrode. During cell charge (Fig. 8a), the gradient  $d[\text{Li}]/dz$  remains negative across the electrode depth. During cell

discharge (Fig. 8b), there is Li depletion near the surface that gradually spreads deeper into the matrix until it reaches the back of the cell. After that, the Li gradients once again become lower, and in the advanced stages of delithiation they become too small to observe. The complex shape of Li profiles during the cell discharge (Fig. 8b) compared to the profiles during the cell charge (Fig. 8a) is the primary reason for the asymmetries seen in Fig. 7, including the behavior of the arithmetic average of layer averages.

In Fig. 9, we use polynomial fits to extrapolate the concentration profiles over the entire range of depth (see Section S1, ESI† for more detail). Fig. 9a and b give the color maps of Li content in  $\text{LiC}_6$  and  $\text{LiC}_{12}$  phases obtained in this manner, and Fig. 9c shows the profiles obtained at two states of charge (more of such profiles are shown in Fig. S5, ESI†). At the peak charge, a nearly exponential  $\text{LiC}_6$  profile and an almost complete lithiation of the graphite at the electrode surface are observed. As the  $\text{LiC}_6$  phase grows from surface towards deeper

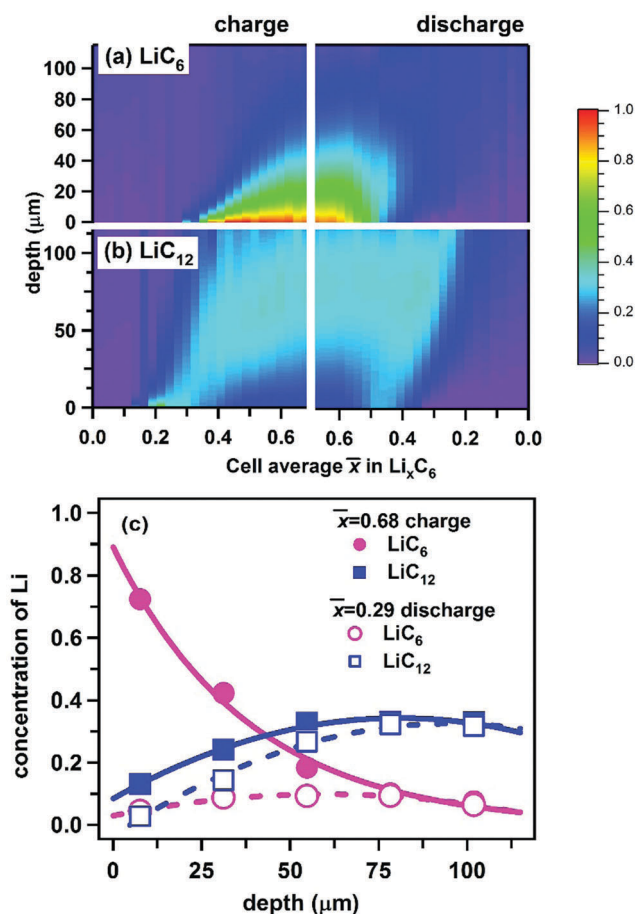


Fig. 9 Color map of the  $z$ -average Li content in (a)  $\text{LiC}_6$  and (b)  $\text{LiC}_{12}$  phases plotted vs. the cell average lithium content of the graphite matrix during charge (on the left) and discharge (on the right) of the cell at 1C rate. The vertical axis gives the depth  $z$  of the matrix. The concentration (in Li atoms per  $\text{C}_6$  unit of the graphite) is color coded as shown on the far right. Panel (c) shows the concentration profiles for these two phases with the layer averages given by the symbols. The smooth lines are the guides to the eye. The state of cell-lithiation is given in the inset.



layers, there is a complementary depletion zone for  $\text{LiC}_{12}$ . This observation is made more obvious in Fig. 9c and also from comparison of Fig. 9a and b: the crest of high concentrations of  $\text{LiC}_6$  in Fig. 9a maps exactly onto the trough of low concentrations of  $\text{LiC}_{12}$  in Fig. 9b, suggesting the complementarity of these two phases through the cell, as expected. The same behavior is also seen in Fig. 5, where the maxima of the  $\text{LiC}_6$  concentration in Fig. 5a nearly coincide in position with the minima of the  $\text{LiC}_{12}$  concentration in Fig. 5b. The complementarity of these two phases is the consequence of the binary nature of the phase diagram for the Li-graphite system after more than 50% Li is inserted per  $\text{C}_6$  units of graphite: as the two phases undergo spinodal decomposition to their equilibrium fractions, at each states of charge the concentration of each phase is fully determined by the net Li content. As  $\text{LiC}_6$  replaces  $\text{LiC}_{12}$  across the matrix, the  $\text{LiC}_{12}$  profile develops the characteristic shape shown in Fig. 9c; this shape persists during the electrode delithiation, as seen from Fig. 9c and Fig. S5 (ESI†).

Using the interpolated concentrations for  $\text{LiC}_6$  and  $\text{LiC}_{12}$  phases, in Fig. 10 we provide the extrapolated concentrations and gradients of these two phases at the electrode surface ( $z = 0$ ).

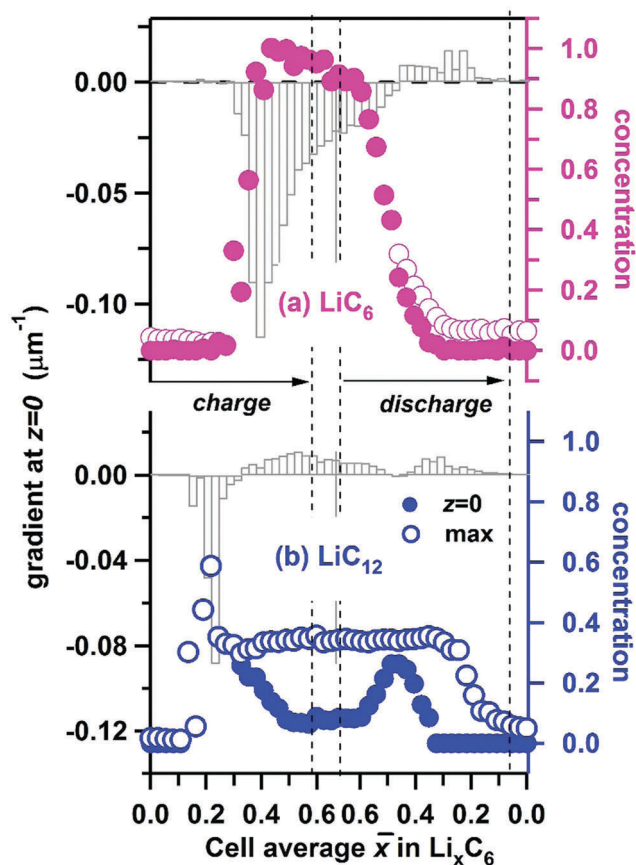


Fig. 10 The electrode surface Li concentration (filled circles, to the right) and the gradient of this concentration (vertical bars, to the left) for lithium in (a)  $\text{LiC}_6$  and (b)  $\text{LiC}_{12}$  phases plotted vs. the cell average lithium content of the graphite matrix during cycling of the cell at 1C rate. The open circles indicate the maximum concentrations across the depth of the cell.

The error bars of the gradients are given in Fig. S6 (ESI†). For  $\text{LiC}_6$ , during the cell charge there is an abrupt increase of the surface concentration at  $\bar{x} \approx 0.35$ , as the concentration rapidly approaches unity, and it stays close to unity until discharge is initiated. The maximum gradient for  $\text{LiC}_6$  ( $-0.120 \pm 0.003 \mu\text{m}^{-1}$ ) is observed during the onset of conversion of  $\text{LiC}_{12}$  to  $\text{LiC}_6$ , when the penetration depth is small. As the  $\text{LiC}_6$  phase spreads over preceding  $\text{LiC}_{12}$  phase, the surface gradient decreases, becoming  $-0.012 \pm 0.002 \mu\text{m}^{-1}$  at the peak charge. During the discharge, the decrease of the  $\text{LiC}_6$  surface gradient continues, and at some point the gradient changes sign as the  $\text{LiC}_6$  phase becomes depleted near the surface. As the depletion zone extends into the bulk, the gradient decreases once again. For a greater part of the cycle the highest concentration of the  $\text{LiC}_6$  phase is at the surface. Only for  $\bar{x} < 0.46$  during the discharge does the maximum concentration somewhat exceed this surface concentration. As seen in Fig. 5a, the formation of  $\text{LiC}_6$  during charge and depletion of this phase during discharge are generally faster near the surface as compared to the bulk. The persistence of  $\text{LiC}_6$  near the surface during discharge is caused by its preferential formation in this region during charge.

As seen from Fig. 9c and 10b, for the  $\text{LiC}_{12}$  phase, where the maximum concentration is reached at the surface only in a narrow range of  $\bar{x}$  (0.16–0.24) which corresponds to the initial stages of  $\text{LiC}_{12}$  formation near the surface. Subsequently, the maximum relocates deeper into the matrix (see Fig. S5, ESI†), as the  $\text{LiC}_6$  phase takes over. The evolution of the gradient for  $\text{LiC}_{12}$  resembles that for  $\text{LiC}_6$  with the entire pattern shifted to lower  $\bar{x}$ . The maximum absolute gradient is observed at  $\bar{x} \approx 0.22$ , which corresponds to the formation of a narrow wedge of  $\text{LiC}_{12}$  phase near the surface. As  $\text{LiC}_{12}$  transforms to  $\text{LiC}_6$ , the sign of the gradient changes, and it reaches a positive maximum near  $\bar{x} \approx 0.54$ . Subsequently it decreases (as the  $\text{LiC}_{12}$  depletion zone becomes wider) only to increase again when  $\text{LiC}_{12}$  becomes the main source of recovered lithium during the discharge.

Put together, our data indicate strong inhomogeneity of Li insertion and de-insertion, both in the net Li content and in the individual  $\text{Li}_x\text{C}_6$  phases.

## 4. Discussion

Previous *in situ* and *operando* approaches to visualization of  $\text{Li}_x\text{C}_6$  gradients in graphite used optical microscopy to distinguish between the colors of the lithiated grains: gold for stage I lithiation, red for stage II, and blue-grey for dilute stages.<sup>30</sup> This method yields qualitative insight in the succession of  $\text{Li}_x\text{C}_6$  phases, but only bands of the corresponding zones were determined. The method has particular difficulty in separating contributions from mixed phases, and it can give misleading results if the composition varies across the individual Gr particles. In our approach using X-rays, the concentration profiles of the  $\text{Li}_x\text{C}_6$  phases correspond to their bulk averages, integrating over the individual particles and quantifying the fraction of each ordered phase in these particles.



Presently, dynamic modeling of phase composition for individual Gr particles and the porous matrix on the whole are still in the development stages, and many aspects of phase transformations remain insufficiently understood. Bazant's phase-field periodic bilayer model appears to be particularly promising for description of stage I-stage II transitions captured in our experiments.<sup>31</sup> This model predicts rapid spinodal decomposition in the individual lithiated Gr particles into well-defined  $\text{LiC}_6$  and  $\text{LiC}_{12}$  subdomains which may explain why our "mixed phase" analysis works so remarkably well on the quantitative level. Bazant and co-workers have recently combined these models with the distributed-resistance models of the matrix to include multiple particles.<sup>32</sup> Another approach for describing these phase transitions combined Newman-type models with the heuristic Avrami equations for growth of the  $\text{Li}_x\text{C}_6$  phases.<sup>33</sup> Now, both of these approaches can be tested against the experimental data. The more traditional Newman-type models consider the  $\text{Li}_x\text{C}_6$  phases as a continuum (a solid solution, *e.g.*, ref. 10 and 34) skipping over the details of the phase dynamics seen in our experiments. This limitation is the reason why many of our results have been presented using the net Li content of the solid matrix, which can be compared with the model simulations. The latter routinely yield sloping concentration profiles seen in Fig. 8 (*e.g.*, ref. 35), yet for lack of observational input such models are continued to be tested and validated mainly through the electric potential measurements. Our study opens a new way in which these models can be tested, verified, and improved.

One of the less anticipated features observed in our experiments is the surprisingly long time the diffraction peaks persist in the back layer ( $L_4$ ) during the potentiostatic hold after reaching the lower limit of 3 V (see Fig. 6), suggesting incomplete Li extraction. As seen from Fig. 5 and 6 the residual signals from  $\text{LiC}_6$  and  $\text{LiC}_{12}$  can be observed at the end of the hold period; as shown in Fig. S7 (ESI<sup>†</sup>), these signals were observed at the end of each one of the 1C delithiation half-cycles. A possible explanation may be relatively poor connectivity of some Gr particles at the end of the cell discharge, as the matrix contracts after swelling.

As mentioned in the Introduction, one of the greatest concerns with operation of LIBs at high currents is Li plating, which occurs when the rate of Li deposition exceeds the rate of Li intercalation. The latter rate is typically expressed using the Butler-Volmer equation in which the exchange current density is proportional to  $[(1-x)x]^{1/2}$ , approaching zero as  $x$  nears unity.<sup>34</sup> In contrast, the exchange current density of Li plating does not depend on  $x$ , so it can overtake Li intercalation in the "red zone" shown in Fig. 9a, where  $x$  is close to unity. This condition persists for  $\bar{x} > 0.4$  during charge and for  $\bar{x} > 0.5$  during discharge, *i.e.* the surface of the cell enters this perilous regime at a much lower Li content than is predicted by modeling when neglecting inhomogeneity. While the saturation of the solid matrix with Li is important for plating, equally important is the overpotential  $\eta(x) = \phi_a(x) - V_{\text{film}}$ , where the first term corresponds to the anode potential *vs.* the electrolyte and the second term corresponds to the potential drop on the resistive SEI film.<sup>34</sup> As the current increases, so does the latter

term; the overpotential becomes negative and the lithiation rate increases dramatically. Since for  $x > 1/2$ , the potential  $\phi_a(x)$  is small (see Fig. S8a, ESI<sup>†</sup>), even moderate currents can cause this "thermodynamic" Li plating condition to occur. Again, while at low current the cell average  $\phi_a(x)$  can be close to  $\phi_a(\bar{x})$ , when steep gradients are present (see Fig. S8b, ESI<sup>†</sup>), the front and the back of the cell can correspond to different lithiation stages, and the condition is not met uniformly across the cell. A preference for near surface Li deposition during high-current charging of the cells has been observed in the optical *operando* experiments of Harris and co-workers.<sup>30</sup> Our study suggests that due to the concentration heterogeneity Li plating can be difficult to avoid near the surface even when care is taken to keep the average lithiation sufficiently low during the rapid charge.

## 5. Conclusions

Speciation of ordered  $\text{Li}_x\text{C}_6$  phases in a porous electrode containing graphite flakes during cycling of a full cell at a (moderately high) 1C rate has been studied both in time and space using energy dispersive X-ray diffraction. The X-ray "slicing" of a 114  $\mu\text{m}$  thick graphite electrode reveals steep gradients in the net and phase specific lithium content. The greatest inhomogeneity is observed for the  $\text{LiC}_6$  phase. Under certain charging conditions, this phase accounts for all Li present at the surface; deeper in the electrode, the concentration exponentially falls towards the current collector. This Li inhomogeneity can have detrimental effects on cell performance, including low utilization of the active material and Li plating in the regions that are close to the electrode surface. Our data on concentration profiles in the individual phases  $\text{Li}_x\text{C}_6$  as a function of lithiation can serve as a benchmark for modeling of electrochemical processes in LIBs. While some of the features observed have been anticipated by modelers, other features are less expected, such as the surprising persistence of  $\text{Li}_x\text{C}_6$  phases during the potentiostatic hold at the end of discharge. Another peculiarity that awaits full explanation is the striking asymmetry between the charge and discharge, which suggests that the complex character of phase transitions during the high-rate delithiation may involve less ordered phases. While our method is eminently suitable to characterize phase dynamics on the scale of tens of microns, it does not provide sufficient insight into the processes occurring in the individual graphite particles, where different phase domains can coexist and affect each other. In fact, it is somewhat surprising that our analysis (neglecting such complexities) appears to adequately capture the phase dynamics under strongly nonequilibrium conditions.

To summarize, we present an experimental methodology for quantifying spatial and phase heterogeneity of lithium intercalation into graphite during rapid cycling. We hope that the insight this approach provides into electrochemical processes in practical lithium-ion cells, will spark renewed interest in validation and improvement of the cell models. In particular, a



greater emphasis on understanding intraparticle and coarse-scale phase dynamics would be highly conducive to taking full advantage of this new approach.

## Conflicts of interest

The authors declare no financial competing interests.

## Acknowledgements

Support from the U.S. DOE's Office of Vehicle Technologies, is gratefully acknowledged. Use of the Advanced Photon Source (APS) at Argonne is supported by the U.S. Department of Energy, Office of Science, Office of Basic Energy Sciences, under Contract No. DE-AC02-06CH11357. The electrodes used in this article are from Argonne's Cell Analysis, Modeling and Prototyping (CAMP) Facility, which is supported within the core funding of the Applied Battery Research (ABR) for Transportation Program. We are grateful to our many colleagues (Stephen Trask, Bryant Polzin, Andrew Jansen, Dennis Dees, Jonathan Almer and Andrew Chuang) for their support and guidance during this effort. The submitted manuscript has been created by UChicago Argonne, LLC, Operator of Argonne National Laboratory ("Argonne"). Argonne, a U.S. Department of Energy Office of Science laboratory, is operated under Contract No. DE-AC02-06CH11357. The U.S. Government retains for itself, and others acting on its behalf, a paid-up nonexclusive, irrevocable worldwide license in said article to reproduce, prepare derivative works, distribute copies to the public, and perform publicly and display publicly, by or on behalf of the Government.

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