Cation diffusion patterns across the magneto-structural transition in Fe$_7$S$_8$

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Migration of atoms in solids during diffusion-dependent reactions is relatively fast and generally not directly recordable in experiments. Here we present an experimental framework that includes fast differential scanning calorimetry to resolve cation-migration paths in crystalline solids using the reversible magneto-structural transition of 4C to 1C pyrrhotite as a testbed. The transition between these two polymorphic Fe$_7$S$_8$ phases at about 600 K is a diffusive process of vacancies, respectively of Fe in octahedral interstitial sites within a hexagonal close-packed lattice of sulfur, and it coincides with the Curie temperature of 4C pyrrhotite. The Fe cations migrate along three kinds of diffusion paths, and their enthalpy contributions to the total reaction enthalpy are taken to define the diffusion patterns in the endothermic reaction and the exothermic back-reaction, respectively. Our experimental findings provide insight into the potential of diffusion patterns to disentangle ordering mechanisms in solids.

1 Introduction

Metal-deficient solid phases, mainly oxides (M$_{1-x}$O) or sulfides (M$_{1-x}$S), exhibit physical properties that are of broad interest in Earth and astro physical sciences to constrain physico-chemical processes during planetary evolution, but also in materials science as a concept to design functional compounds.$^{1-6}$ These defective phases have in common that they undergo structural transitions under changing temperature and/or pressure conditions due to rearrangement of the cation-deficient sites.$^{7-10}$

Among defective solids the minerals of the pyrrhotite group (Fe$_{1-x}$S; 0 $\leq$ x $\leq$ 0.125) represent a classic omission solid-solution series formed by a hexagonal close-packing of sulfur with ordered Fe sites and vacancies in the octahedral interstices that results in a hexagonal NiAs-type substructure and variable commensurate and incommensurate superstructures.$^{11,12}$ Slight changes in the chemical composition and the subsequent arrangement of the empty sites generate a rich variation of electromagnetic states and processes.$^{11,13-15}$ At temperatures of about 600 K the superstructures of all pyrrhotite phases are unstable due to diffusion-controlled processes that randomize the Fe-deficient sites in a hexagonal 1C structure.$^9,16,17$ Because of the unique structural and physico-chemical properties of the members of the pyrrhotite group and their potential for technological applications, great effort has been put into the synthesis of pyrrhotite nanostructures such as nanotubes and nanowires.$^5,18-21$ The inherent difficulty associated with pyrrhotite is the synthesis of structurally and magnetically well-defined omission phases with highly ordered and stable arrangements of empty sites. Therefore, apart from a fundamental physico-chemical interest, detailed information on the cation-diffusion processes is a requirement on the route to the technological application of the pyrrhotite phases.

The Fe-deficient end-member (ideal formula Fe$_7$S$_8$) of the pyrrhotite omission series, denoted 4C pyrrhotite, is the ideal testbed to study diffusion mechanisms. The 4C phase has a monoclinic superstructure that stems from highly ordered vacancies in a stacking sequence of full and vacancy-bearing layers with a four-fold modulation per unit cell. Bertaut$^{22}$ suggested that this ordering is a result of the Coulomb repulsion minimization of the Fe-deficient sites. The vacancy order generates a relatively strong ferrimagnetism (magnetic moment $m \approx 2.73 \mu_B$ per Fe atom$^{23}$) that stems from magnetically uncompensated sublattices due to ferromagnetic intra-layer and antiferromagnetic inter-layer couplings of the Fe magnetic moments with a Curie temperature ($T_C$) of about 600 K.$^{24,25}$ The loss of spontaneous magnetization occurs in the same temperature range as the polymorphic transition of the monoclinic 4C into a hexagonal 1C pyrrhotite. This transition goes along with a vacancy rearrangement that can be considered as a reversible diffusive process (e.g., ref. 26-28). In the 4C structure one of the four different Fe$^{2+}$ sites has an occupancy probability of 0.5 and for the others it is zero, whereas in 1C the occupancy probability is
Complementary thermal analysis of the magneto-structural transition was performed by differential scanning calorimetry (DSC) on crystal flakes (with masses between 10.5 and 18 mg) at heating/cooling rates between 1 and 30 K min\(^{-1}\) in a Mettler-Toledo DSC 1 device. For more detailed insight into the mechanism of the transition fast differential scanning calorimetry (FDSC) measurements were performed on microflakes at heating/cooling rates between 10 and 200 K s\(^{-1}\) using a Mettler-Toledo Flash DSC 1 with UFS1 sensor. The sensor support temperature was selected to 183 K and argon was used for purging. According to ref. 32 a difference in the temperature scale of 8 K was determined between FDSC and DSC. The FDSC temperatures were calibrated using an indium standard sample. The onsets of the endo- and exothermic events were determined after background correction using the Mettler-Toledo STARе software (Version V16.10). In the FDSC experiment, the heating/cooling cycles were continuously recorded with decreasing rate.

### 3 Results and discussion

#### 3.1 Structural and magnetic properties

The powder XRD pattern of the Morro Velho sample shows a 4C pyrrhotite and no impurity phase was detected (Fig. 2, inset). The XRF analysis shows a chemical composition of 46.17 ± 0.1 at% Fe and 53.83 ± 0.1 at% S, and 377 ppm Ni traces, which corresponds to Fe\(_{6.6}\)S\(_8\). The 4C pyrrhotite XRD pattern can be well refined in the \(C2/c\) space group with the structural model by Powell et al.\(^{27}\) The unit-cell parameters obtained at room temperature were \(a = 1.1918(2)\) nm, \(b = 0.6872(2)\) nm, \(c = 1.2913(2)\) nm, and \(\beta = 118.035(1)^\circ\) with a goodness-of-fit of 3.67, a weighted Durbin–Watson value of 0.24, and an R-Bragg factor of 5.57. The refinement of the Fe-occupancy factor yielded a chemical composition of Fe\(_{6.6}\)S\(_8\) that is slightly

2 Materials and methods

In this study a natural 4C pyrrhotite crystal from the locality of Morro Velho (Minas Gerais, Brazil) was chosen.\(^{23}\) For the detailed crystallographic, chemical, and magnetic analyses powder samples were prepared by crushing and subsequently grinding the crystal sample in an agate mortar for about 30 minutes. For the crystallographic measurements crystal flakes were used. Powder X-ray diffraction (XRD) at room temperature using untreated and heated samples was performed with a Bruker D8 device with Cu K\(_{\alpha1,2}\) radiation, and the patterns were Rietveld-refined with the Bruker software TOPAZ.\(^{23,31}\) The chemical composition was determined by energy-dispersive X-ray fluorescence (ED-XRF) on a SPECTRO XEPOS spectrometer. The magnetic susceptibility upon heating between 300 and 650 K was determined on an AGICO KLY-2 Kappabridge in argon atmosphere with a heating/cooling rate of about 10 K min\(^{-1}\).

![Fig. 1 Schematic delineation of the cation arrangements in the polymorphous 4C and 1C structures with Fe sites having occupancy probabilities of 1 (green dots), 0 (circles) and 0.875 (light green dots), respectively. The sulfur atoms are omitted for clarity reason. Heating above \(T_c \approx 600\) K generates the 4C to 1C transition, while the back-reaction occurs upon cooling.](image1.png)

![Fig. 2 Magnetic susceptibility of the pyrrhotite powder during heating (red) and cooling (blue) cycles. Inset: XRD patterns of the untreated sample and after three heating/cooling cycles. The Curie temperature \(T_c\) upon heating is marked (dashed line).](image2.png)
Fe-depleted compared to the Fe$_{6.9}$S$_8$ obtained from the chemical analysis. A mean crystallite size of about 220 nm was determined for the powder using the Scherrer equation$^{23}$ after considering the instrumental and stress/strain contributions to the line broadening.

The magnetic susceptibility ($\chi$) of the heating–cooling cycles of the 4C pyrrhotite is shown in Fig. 2 for temperatures between 320 and 625 K. During the first heating, $\chi$ is constant up to 450 K, followed by an increase with a peak at 584 K and a drop down towards 600 K. The peak can be attributed to the Hopkinson effect, which is commonly observed in ferro-/ferrimagnetic materials just before the Curie temperature.$^{34}$ For multi-domain particles, it is explained by enhanced domain-wall mobility with increasing temperature, which leads to an increase in the magnetic permeability and in turn to an increase in $\chi$ (e.g., ref. 35). Using the tangent method,$^{36}$ a Curie temperature $T_C = 597$ K was determined that is consistent with the values for 4C pyrrhotite reported in the literature (e.g., ref. 25 and 27). Troilite, the vacancy-free end-member of the pyrrhotite omission series has a Néel temperature $T_N \approx 600$ K (e.g., ref. 37 and 38), and therefore it is feasible to assume that the loss of magnetic ordering in the 4C phase is not critically affected by the vacancies. In the cooling curve, the onset of $\chi$, however, occurs at 594 K, which indicates a minor hysteretic effect of 3 K between the heating and cooling curves. Upon further cooling, $\chi$ steeply increases down to 580 K, and reaches a maximum at 565 K followed by a minor overall decrease with a broad local minimum at 435 K. At 300 K, after the first heating/cooling cycle, $\chi$ is slightly higher compared to the initial value. In the subsequent heating curves, the Hopkinson peak becomes more pronounced but its peak position remains unchanged. The Curie temperatures and the hysteretic shifts between heating and cooling curves also remain constant within the experimental error. The cooling curves are nearly identical, but the comparison of the heating/cooling cycles indicates minor magneto-structural modifications during the first heating and this establishes a new thermodynamic equilibrium in the sample.

The XRD pattern obtained from the powder sample after the three cycles shows a single-phase 4C pyrrhotite (Fig. 2, inset) with the refined unit-cell parameters $a = 1.9114(3)$ nm, $b = 0.6870(2)$ nm, $c = 1.2911(3)$ nm, and $\beta = 118.025(1)^\circ$ with a goodness-of-fit of 3.96, a weighted Durbin–Watson value of 0.21, and a R-Bragg factor of 6.73. The comparison of the crystallographic parameters of the untreated and the heat-treated samples reveals no significant changes. The chemical composition of Fe$_{6.9}$S$_8$ in the heated sample obtained from the refinement of the Fe-occupancy factor is equal to that yielded from the XRF analysis. Simultaneous to the shift in stoichiometry due to the heat treatment, the mean crystallite size in the powder increases by about 50% to 330 nm. The heat-induced sintering can also explain the more pronounced Hopkinson peaks, because larger crystallites in pyrrhotite grains are expected to contain more magnetic domain walls. The sintering can also account for the shift towards the ideal 4C stoichiometry in the cycled sample because small defects, such as stacking faults forming jogs,$^{1}$ which are not detectable by XRD, can be eliminated by the heat treatment. Under the assumption that these defects are less Fe-deficient compared to the bulk material, their healing can explain the shift towards a stoichiometric pyrrhotite. Taking the susceptibility data into account, it is obvious that the sintering has no critical effect on the magnetic ordering in the 4C phase.

### 3.2 Calorimetric properties

Thermodynamic analysis of the magneto-structural transition using a scanning rate of 10 K min$^{-1}$ for the DSC cycles shows no apparent changes for temperatures between 300 K and 575 K (Fig. 3). Above 575 K, the three DSC cycles reveal an onset of the endothermic event at 595.4 ± 0.4 K upon heating with a mean peak temperature of 600.5 ± 0.4 K. For the exothermic event upon cooling the onset is at 593.4 ± 0.8 K with a mean peak temperature of 586.8 ± 0.2 K. The onsets of both events are slightly below $T_C = 597$ K of 4C pyrrhotite, which accords with previous experimental studies.$^{25,39}$

For the transition of 4C to 1C pyrrhotite, the enthalpy changes $\Delta H_{4C \rightarrow 1C}$ are 0.77 kJ mol$^{-1}$ in the first two cycles and slightly increase to 0.81 kJ mol$^{-1}$ in the third one. These $\Delta H_{4C \rightarrow 1C}$ values are similar to those of a natural 4C pyrrhotite crystal from a different locality$^1$ and somewhat lower than the 1.3 kJ mol$^{-1}$ obtained from a synthetic 4C powder sample.$^{28}$ Considering the XRD data, the increase in $\Delta H_{4C \rightarrow 1C}$ during the cycling is probably a sintering effect, because more energy is needed for the 4C to 1C transition to occur when the vacancy order gets enhanced. The sintering also slightly changes the shape of the endothermic peak. In the third cycle, it is weakly split and can be fitted with two Gaussian components, and this in turn points to two events that slightly differ in their $\Delta H_{4C \rightarrow 1C}$ (Fig. 3, inset). Taking this into account, the splitting provides evidence that the breakdown of the vacancy order in 4C pyrrhotite is subject to a heterogeneous diffusion mechanism, i.e., the probability for a cation movement is unequal for the four Fe-sites in the 4C pyrrhotite. Regarding the exothermic event the DSC curves exhibit asymmetric shapes that can only be fitted by three Gaussian components.

![Fig. 3](image_url)
This indicates that the 1C to 4C transition is also a heterogeneous diffusion process (Fig. 3). The enthalpy changes \( \Delta H_{1C\rightarrow4C} \) obtained from the three cycles differ only slightly and their mean is \(-0.93 \pm 0.03 \text{ kJ mol}^{-1}\).

The change of the scanning rates in the DSC cycles has only minor effects on the onset temperatures with means of 595.1 \pm 1.3 K for the endothermic and 592.9 \pm 0.8 K for the exothermic event. The enthalpy changes are also nearly rate-independent with means \( \Delta H_{4C\rightarrow1C} = 0.82 \pm 0.05 \text{ kJ mol}^{-1} \) and \( \Delta H_{1C\rightarrow4C} = -0.81 \pm 0.10 \text{ kJ mol}^{-1} \), respectively (Fig. 3). In contrast, the difference of the heating and cooling peaks reveals a non-linear increase with the rate from 5 K at 1 K min \(^{-1}\) to 21 K at 30 K min \(^{-1}\) with a symmetric shift at around 593 K. Furthermore, taking the mean of the peak temperature \( T_{\text{peak}} \) of the three scans for each heating rate, the apparent activation energy \( Q \) for the endothermic reaction can be extracted using the Kissinger relation \( \ln(Q/T_{\text{peak}}^2) \propto 1/T_{\text{peak}} \), where \( \Phi \) is the heating rate (Fig. 4). From the slope of the Kissinger plot \( m \), the activation energy \( Q = m R \) can be determined (e.g. ref. 40), where \( R \) is the universal gas constant. A value of \( Q = 1.22 \text{ kJ mol}^{-1} \) is obtained. The relative large scatter of the peak temperature data in Fig. 4 is probably caused by the influence of the heat transfer change of the sample due to sintering. The energy barrier, however, is nearly two orders of magnitudes lower than that obtained from radiotracer experiments.\(^{16-29}\) In such experiments, the tracer is nearly two orders of magnitudes lower than that obtained from the change of the sample due to sintering. The energy barrier, however, is probably only the 1C to 4C transition is also a heterogeneous diffusion process (Fig. 3). The enthalpy changes \( \Delta H_{1C\rightarrow4C} \) obtained from the three cycles differ only slightly and their mean is \(-0.93 \pm 0.03 \text{ kJ mol}^{-1}\).

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### 3.3 Diffusion patterns

In order to provide further insight into the mechanism behind the diffusion-controlled reaction, FDSC is applied. In contrast to DSC, the peak positions and the shapes of the endothermic event are congruent in the FDSC scans with the same heating rate. The FDSC curves with heating rates between 10 and 100 K s\(^{-1}\) separate the endothermic event into three peaks, a relatively broad one and a doublet at relatively higher temperature (Fig. 5a). At higher rates up to 200 K s\(^{-1}\), two features of the doublet blur (Fig. 5a and b). The asymmetric peaks in the cooling curves have similar shapes as in the conventional DSC measurements. (Fig. 3b and 5b).

Assuming that the total transformation enthalpies \( \Delta H_{\text{tot}} \) obtained from DSC correspond to those from FDSC, the enthalpies of the 4C to 1C and the 1C to 4C transformations can both be subdivided into three contributions \( \Delta H_i \) derived from the three Gaussian components (Fig. 6) with \( \Delta H_{\text{tot}} = \sum \Delta H_i \). The relative contributions are then \( \Delta H_i/\Delta H_{\text{tot}} \).

The \( \Delta H_i \) is affected by the three crystallographic positions of Fe cations with respect to the vacancy sites, i.e., by the diffusion...
coefficient and the diffusion path (Fig. 1). Considering the hexagonal close-packing of the sulfur atoms in the pyrrhotite structure, three kinds of paths for the Fe$^{2+}$ cations can be inferred. There is a direct diffusion jump into a vacancy via the openings formed by face-shared sulfur octahedra in the c-plane with only one degree of freedom along the c-axis (o–o) (Fig. 7). In the 4C structure with the stacking sequence of full and vacancy layers, one quarter of the Fe sites can follow such path (Fig. 1). For the other Fe sites the cations may migrate through tetrahedral interstices either in the c-plane (o–t–o) or along the c-axis (o–t–t–o) with degrees of freedom $>1$ (Fig. 7). The different paths vary by their lengths. The shortest one with nearly 0.30 nm is o–o followed by o–t–o and o–t–t–o with lengths of about 0.37 nm and 0.55 nm, respectively (Fig. 7). It was shown that self-diffusion along the c-axis is faster than in the c-plane.$^{29}$ Powell et al.$^{27}$ also demonstrated that with the onset of the transition the occupancy probability of Fe sites next to vacancies decreases from 0.5 to 0.38. Thus, it can be assumed that the Fe migrations in 4C pyrrhotite starts along the o–o path, which is energetically more favorable compared to those via tetrahedral interstices. With this in mind the initial o–o jumps can be attributed to $\Delta H_1$. They break the local cation-vacancy relations in the 4C structure while the number of vacancies remains constant. These o–o jumps are thus expected to trigger a state with a dynamic opening and closing of diffusion paths, where all the cations are captured and encountered until a new equilibrium in the Fe-vacancy configuration is established. In the 1C structure this configuration shows no crystallographic long-range order. At $T < 600$ K, the initial o–o jumps ($\Delta H_1$), however, are always unaffected by the two high-temperature events $\Delta H_2$ and $\Delta H_3$, and, therefore, they can be taken to determine the activation energy of the initial diffusion
The thermally-induced magneto-structural 4C to 1C transition in Fe₇S₈ is a reversible cation-diffusion reaction in a stable hexagonal close-packing of sulfur. There is no evidence for a magnetic effect on the intrinsic diffusion processes during the transition. Three diffusion patterns during the endothermic reaction can be separated due to different migration paths and jumping frequencies of the cations. The onset of the transition is triggered by direct jumps of Fe into vacancies, destabilizing the 4C structure and resulting in a complex diffusion formed by dynamic variations of the vacancy distribution towards a thermally-activated state. For the back-reaction from a disordered to the ordered 4C structure three patterns are also identified, but they are superimposed in such a way that they cannot be explicitly resolved in the experimentally determined enthalpy changes. This probably results from the absence of a crystallographically well-defined spatial relation between Fe sites and vacancies in the 1C structure. Considering the experimental results, the identification of diffusion patterns based on their dynamics opens new perspectives for the investigation of intrinsic diffusive reactions in solids. This is expected to be highly beneficial for the understanding of dynamic processes in geological and technical systems that are driven by diffusion.

4 Conclusions

The thermally-induced magneto-structural 4C to 1C transition in Fe₇S₈ is a reversible cation-diffusion reaction in a stable hexagonal close-packing of sulfur. There is no evidence for a magnetic effect on the intrinsic diffusion processes during the transition. Three diffusion patterns during the endothermic reaction can be separated due to different migration paths and jumping frequencies of the cations. The onset of the transition is triggered by direct jumps of Fe into vacancies, destabilizing the 4C structure and resulting in a complex diffusion formed by dynamic variations of the vacancy distribution towards a thermally-activated state. For the back-reaction from a disordered to the ordered 4C structure three patterns are also identified, but they are superimposed in such a way that they cannot be explicitly resolved in the experimentally determined enthalpy changes. This probably results from the absence of a crystallographically well-defined spatial relation between Fe sites and vacancies in the 1C structure. Considering the experimental results, the identification of diffusion patterns based on their dynamics opens new perspectives for the investigation of intrinsic diffusive reactions in solids. This is expected to be highly beneficial for the understanding of dynamic processes in geological and technical systems that are driven by diffusion.

Conflicts of interest

There are no conflicts to declare.

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