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Electronic structure and reactivity of Fe(IV)oxo species in metal–organic frameworks

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We investigate the potential use of Fe(IV)oxo species supported on a metal–organic framework in the catalytic hydroxylation of methane to produce methanol. We use periodic density-functional theory calculations at the 6-31G**/B3LYP level of theory to study the electronic structure and chemical reactivity in the hydrogen abstraction reaction from methane in the presence of Fe(IV)O(oxo) supported on MOF-74. Our results indicate that the Fe(IV)O moiety in MOF-74 is characterised by a highly reactive (quintet) ground-state, with a distance between Fe(IV) and O(oxo) of 1.601 Å, consistent with other high-spin Fe(IV)O inorganic complexes in the gas phase and in aqueous solution. Similar to the latter systems, the highly electrophilic character (and thus the reactivity) of Fe(IV)O in MOF-74 is determined by the presence of a low-lying anti-bonding virtual orbital ($3\sigma^*$), which acts as an electron acceptor in the early stages of the hydrogen atom abstraction from methane. We estimate an energy barrier for hydrogen abstraction of 50.77 kJ mol⁻¹, which is comparable to the values estimated in other gas-phase and hydrated Fe(IV)O-based complexes with the ability to oxidise methane. Our findings therefore suggest that metal–organic frameworks can provide suitable supports to develop new solid-state catalysts for organic oxidation reactions.

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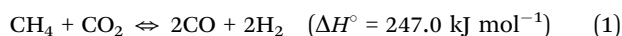
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1. Introduction

Natural gas has attracted attention in the last few decades for its potential use in the production of energy, as a clean and sustainable alternative to oil and coal and as a means to provide important feedstock for the chemical industry on a planetary scale. Although global reserves of natural gas are estimated to be of the order of 10¹¹ m³,¹ the direct use of methane gas, its main component, is severely limited by transport costs from production sites to consumption areas. Currently, natural gas is transported through high-pressure pipelines or in liquefied natural gas (LNG) carriers, which suffer from high compression and refrigeration costs. The conversion of methane to liquid species, *e.g.* dimethyl ether, formaldehyde, acetic acid or liquid fuels, *via* Fischer–Tropsch catalysis offers an appealing alternative to the direct transportation of methane gas.²

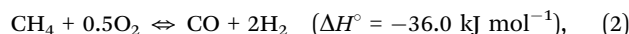
Methane can be oxidised to methanol using several multi-step industrial processes.³ Some of these reactions require catalysts, while others occur in the absence of a catalyst. For instance, in a two-step process methane is first decomposed into synthesis gas (CO + H₂) *via e.g.* dry reforming



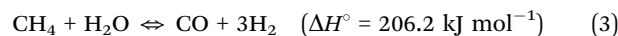
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and partial oxidation,



which both require catalysts,⁴ or *via* the traditional steam reforming^{5,6}



with an Ni/Al₂O₃ catalyst. This synthesis gas is in turn reformed to produce methanol *e.g. via* the catalytic reaction



with an Ni/Al₂O₃ catalyst,⁷ although other reagents can also be used (see ref. 4).

The production of synthesis gas *via* steam reforming is an expensive method, as it requires high temperature and pressure. Considerable effort has therefore been devoted to developing more cost-effective methods for the methane-to-methanol conversion at mild temperature and pressure. Compounds based on transition metals offer a potential route towards this goal, and Fe-based catalysts are particularly appealing in view of the abundance and minimal environmental impact of Fe-species. In particular, Fenton-like reactions^{8–10} have been investigated in view of their applicability to oxidise several organic species, including methane. Although the origin and nature of the active catalytic species in Fenton oxidation are still being discussed, it is now well established that, in a variety of experimental conditions, an oxidoiron(IV) (ferryl) intermediate, [(H₂O)₅FeO]²⁺,^{11–19} is the main species responsible for hydrogen abstraction from



substrate molecules in aqueous solution, as part of a two-step rebound oxidation mechanism.^{9,10,20}

These findings have motivated the modelling of Fenton-like gas-phase complexes of various compositions.^{21–26} Density-functional theory (DFT) calculations have revealed that the highly reactive high-spin (quintet) state is favoured by weak (*e.g.* oxygen-based) coordination environments.^{27–30} In optimal conditions, these species can affect the abstraction of a hydrogen atom from a methane molecule with enthalpy barriers of the order of only 50 kJ mol⁻¹. The ability of Fe(IV)O complexes to oxidise methane in aqueous solution has also been examined, and the presence of the solvent has been shown to play a crucial role in favouring the reaction.^{31–33} In the presence of suitable coordination environments for hydrogen abstraction reactions carried out in water solution at room temperature, free-energy barriers as low as *ca.* 30 kJ mol⁻¹ have been predicted on the basis of DFT calculations, to be compared to an estimate of *ca.* 90 kJ mol⁻¹ for the “Fenton catalyst” ($[(\text{H}_2\text{O})_5\text{FeO}]^{2+}$) in water solution.³⁴ These results provide evidence that Fenton-like species with suitably engineered Fe-ion coordination environments can indeed be the basis to create new classes of homogeneous catalysts for hydrocarbon oxidation under mild working conditions.

The aim of this study is to explore the suitability of metal-organic frameworks (MOFs) as supports for Fe(IV)oxo species of catalytic relevance. MOFs are important in catalytic processes because of their large internal surface areas, tuneable topologies and potential applications as chemical reagents.³⁵ Thanks to these properties, MOFs have been recently employed *e.g.* for the catalytic capture and degradation of alkanes, alkenes, aromatic hydrocarbons and oxygenated volatile organic compounds³⁶ to reduce atmospheric emissions as well as the hydrogenation of CO₂ to methanol.^{37–39} They have also been shown to adsorb and photocatalytically degrade organic compounds in water.⁴⁰ In addition, the structure of MOFs can be tuned to oxidise light alkanes. Quantum-mechanical calculations have predicted that magnesium-diluted MOF-74 catalyses the oxidation of ethane in the presence of N₂O.⁴¹ Similar calculations have also proposed that MOF-74 containing an Fe(IV)O species (CPO-27-Fe) can hydroxylate ethane to ethanol,⁴² as these framework materials have been shown to separate mixtures of light hydrocarbons at their Fe(II) coordination sites⁴³ and to produce phenol with efficiencies as high as 60% using H₂O₂ as an oxidant.⁴⁴ Recent studies have reported results concerning the oxidation of methane to methanol catalysed by Cu-Oxo clusters stabilized in NU-1000 MOFs,⁴⁵ and of MOFs with design inspired to particulate methane monooxygenase (pMMO).⁴⁶

In this work we study the ability of an Fe(IV)O species in MOF-74 to promote the direct oxidation of methane. As mentioned above, it has been shown that the catalytic activity of Fe(IV)O species is strongly influenced by the coordination environment of the Fe ion.^{19,21,31} In particular, it has been demonstrated that an oxygen-rich Fe coordination environment stabilises the most reactive (quintet) spin state of the Fe(IV)O moiety and decreases the energy of its lowest virtual orbital (3σ*), which is responsible for the electrophilic character, and therefore for the

catalytic activity, of Fe(IV)O in hydrocarbon oxidation.²¹ The structure of MOF-74 offers, in principle, an ideal coordination framework capable of stabilising highly reactive Fe(IV)O species. In ref. 29 it has for instance been shown that Fe(II) ions can be included as O-coordinated stable dopants in MOF-74, and the resulting system exhibits excellent hydrocarbon separation properties. On the basis of these results, we will consider here the existence, structure, and reactivity of analogous solid-state systems containing Fe(IV)O ions. We will model Fe(IV)O/MOF-74 using the neutron diffraction data presented in ref. 29 and use DFT calculations at the B3LYP level on the crystalline system to examine the properties of the hypothetical Fe(IV)O/MOF-74 and its reactivity in the oxidation of methane.

The manuscript is organised as follows. In Section II, we describe the methods employed to model the Fe(IV)O/MOF-74 structure and to calculate various electronic properties of interest. Results concerning these properties and the reactivity of Fe(IV)O/MOF-74 in methane oxidation are described in Section III. We pay particular attention to identifying the most stable ground spin state among the several competing ones, as this is the crucial factor driving the reactivity of Fe(IV)O. We also present an analysis of the orbital structure of this system. Our results are summarised in Section IV.

II. Simulation methods

We create an initial structure for Fe(IV)O/MOF-74 using information obtained for acetylene/MOF-74 available from the Cambridge Crystallographic Database⁴⁷ using the Materials Studio suite package.⁴⁸ The space group is $R\bar{3}$ (148) representing a unit cell of dimensions of 25.92 × 25.92 × 6.95 Å³ with angles $\alpha = \beta = 90^\circ$ and $\gamma = 120^\circ$, containing 180 atoms and corresponding to 18 irreducible cells. The irreducible unit cell of Fe(IV)O/MOF-74 contains 10 atoms: one Fe, three framework O's, four C's, one H and one O(oxo). We replace the acetylene molecule present in the original structure with an oxygen atom O(oxo), at a distance of 1.68 Å from the Fe atom, which is slightly larger than the typical Fe(IV)–O(oxo) distances determined for gas-phase complexes (1.60–1.62 Å).²¹ We then optimise the atomic positions with the COMPASS2 force field. After optimisation, the Fe(IV)–O(oxo) bond length decreases to 1.65 Å.

The atomic positions from the resulting configurations are then optimised with the DFT code CRYSTAL17.⁴⁹ The DFT calculations are carried out using periodic boundary conditions with the hybrid B3LYP exchange–correction functional. We use this functional because it provides a reasonably accurate description of high-spin Fe(IV) states,^{50,51} which is also more adequate than most generalised-gradient approximations (*e.g.* PBE⁵² and BLYP⁵³) in the solid state. We do however notice that, for gas-phase or solvated systems, the OPBE functional⁵⁴ may also provide an accurate alternative to B3LYP (ref. 51). A standard all-electron 6-31G**^{55,56} basis set is used to represent the local atomic orbitals in terms of primitive Cartesian Gaussian functions. Polarization functions (p-functions for hydrogens and d-functions for carbons, oxygens, and silicons) are used



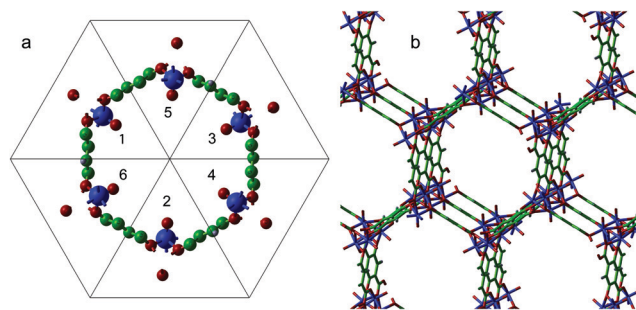


Fig. 1 Representation of the primitive unit cell of Fe(IV)O/MOF-74 (a). Each triangle forming the hexagon is labelled 1–6 for reference. Each triangle contains 10 atoms. The Fe(IV) atoms are blue, the C atoms green, the O atoms red, and the H atoms grey. Panel b illustrates the interatomic bonds of the replicated unit cell in perspective view.

Table 1 List of total energies of the singlet, triplet and quintet spin configurations, their differences with respect to the corresponding singlet, and Fe(IV)–O bond distance computed at the LDA, BLYP and B3LYP levels of theory

Functional	Spin	Total energy (Ha)	Difference in total energy w.r.t. singlet per Fe–O site (eV)	Bond Fe–O(oxo) (Å)
LDA	Singlet	–10270.070	0.000	1.588
LDA	Triplet	–10270.196	–0.571	1.594
LDA	Quintet	–10270.205	–0.615	1.597
BLYP	Singlet	–10305.355	0.000	1.632
BLYP	Triplet	–10305.528	–0.782	1.628
BLYP	Quintet	–10305.558	–0.919	1.632
B3LYP	Singlet	–10303.370	0.000	1.588
B3LYP	Triplet	–10303.669	–1.356	1.597
B3LYP	Quintet	–10303.776	–1.843	1.601

Table 2 B3LYP energies and positions (k -point coordinates) in the reciprocal space of the lowest virtual orbital (LUMO) at each iron atom of the triplet spin state of Fe(IV)O/MOF-74 obtained from DFT calculations with an imposed space-group symmetry

Spin	k -Point coordinates (Å ^{–1})	Fe1	Fe2	Fe3	Fe4	Fe5	Fe6
↑	0.0000, 0.0000, 0.0000	–3.7179	–3.6923	–3.6549	–3.6549	–3.3966	–3.3966
↑	0.1481, –0.0741, –0.0741	–3.7528	–3.7351	–3.7263	–3.624	–3.4774	–3.3801
↑	0.1481, 0.0542, –0.2023	–3.7108	–3.7024	–3.6591	–3.5794	–3.4836	–3.3878
↑	0.6265, 0.5326, 0.2760	–3.7788	–3.7788	–3.6334	–3.5912	–3.5912	–3.3068
↓	0.0000, 0.0000, 0.0000	–3.2987	–3.2987	–3.1408	–3.1408	–3.0715	–3.0715
↓	0.1481, –0.0741, –0.0741	–3.4498	–3.3347	–3.1796	–3.1757	–3.1105	–3.0676
↓	0.1481, 0.0542, –0.2023	–3.2950	–3.2436	–3.1997	–3.1489	–3.0695	–3.0679
↓	0.6265, 0.5326, 0.2760	–3.5441	–3.1947	–3.1818	–3.1155	–3.1155	–3.0864

Table 3 B3LYP energies and positions (k -point coordinates) in the reciprocal space of the lowest virtual orbital (LUMO) at each iron atom of the quintet spin state of Fe(IV)O/MOF-74 obtained from DFT calculations with an imposed space-group symmetry

Spin	k -Point coordinates (Å ^{–1})	Fe1	Fe2	Fe3	Fe4	Fe5	Fe6
↑	0.0000, 0.0000, 0.0000	–4.1615	–4.1402	–3.8518	–3.8518	–3.5548	–3.5548
↑	0.1481, –0.0741, –0.0741	–4.0824	–4.0595	–4.0219	–3.9639	–3.6361	–3.5178
↑	0.1481, 0.0542, –0.2023	–4.1558	–4.1485	–3.8384	–3.7345	–3.6619	–3.5674
↑	0.6265, 0.5326, 0.2760	–4.0782	–4.0782	–3.9676	–3.9676	–3.7850	–3.4074
↓	0.0000, 0.0000, 0.0000	–3.7128	–3.7104	–3.432	–3.432	–3.3555	–3.3555
↓	0.1481, –0.0741, –0.0741	–3.8155	–3.7939	–3.7691	–3.6535	–3.5057	–3.4092
↓	0.1481, 0.0542, –0.2023	–3.7123	–3.7116	–3.4296	–3.3981	–3.3796	–3.3597
↓	0.6265, 0.5326, 0.2760	–3.8182	–3.8182	–3.6882	–3.6507	–3.6507	–3.3301

to ensure that the orbitals can distort from their original atomic symmetry, and to better adapt to the molecular surroundings leading to a more accurate estimate of the total energy of the system with a high hydrogen content. Accurate truncation thresholds for the tolerances of the Coulomb and exchange bielectronic series are used in all calculations⁵⁷ to improve the convergence rate during the self-consistent solution of the Kohn–Sham equations. Brillouin zone integrations are carried out using a Monkhorst–Pack net of $2 \times 2 \times 2$ k -points, and a ground-state energy convergence is enforced of 1×10^{-5} Hartree. Long-range forces are included by adding the van der Waals dispersions given by Grimme's DF2 scheme.⁵⁸

III. Results and discussion

III.1. Electronic structure of Fe(IV)O/MOF-74

Our analysis of the electronic structure of Fe(IV)O/MOF-74 begins with a structural optimisation of its primitive unit cell (shown in Fig. 1). This optimisation employs CRYSTAL17's symmetry operators and is carried out for the singlet, triplet, and quintet spin configurations of all six Fe(IV) atoms. Therefore, the difference between the number of α and β electrons is 12 for the triplet and 24 for the quintet. In Table 1 we list the absolute energies of the optimised structure of Fe(IV)O/MOF-74 obtained using three approximations for the exchange–correlation functional (LDA, BLYP and B3LYP). In all cases we find that the quintet is the most stable state, followed by the triplet and the singlet. A quintet ground state has also been reported for Fe(IV)O metal-proteins with oxidative activity, including taurine/ α -ketoglutarate dioxygenase (TauD)⁵⁹ and methane monooxygenase (MMO).⁶⁰



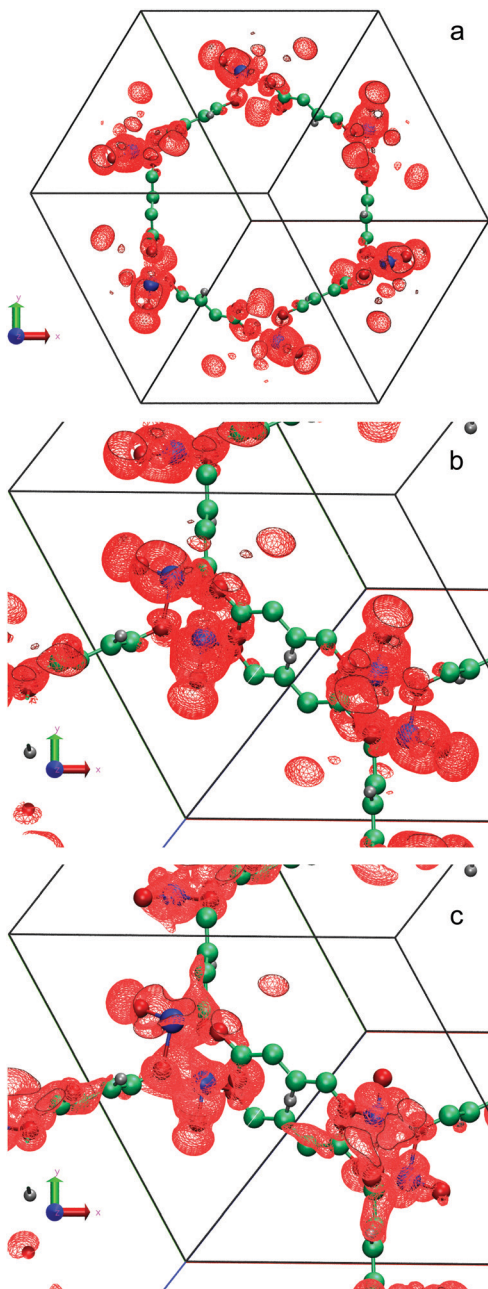


Fig. 2 Symmetric representation (a) of the LUMO's charge density obtained with B3LYP using an isosurface value of 2.90×10^{-4} electrons per Bohr³. Zoomed-in view of the LUMO charge density (b) and wavefunction (c) with a value of 2.90×10^{-2} (electrons per Bohr³)^{1/2} showing the typical $3\sigma^*$ anti-bonding nodal structure. Fe atoms are pink and O atoms blue. C and H atoms are green and grey respectively.

Furthermore, our results indicate that for each level of theory the distance between Fe(IV) and O(oxo) in the quintet and triplet atoms changes by less than 1% with respect to the singlet. The calculated optimised distance is 1.601 Å, which is only 1.25% shorter than the values found in other gas-phase Fe(IV)O complexes.²¹ Considering that ref. 51 reported that functionals like LDA and BLYP disfavour high-spin states, while hybrid functionals provide the correct spin ground state of iron

complexes, we will only use B3LYP to investigate further the electronic structure of Fe(IV)O/MOF-74. A more thorough study of the influence of the exchange–correlation model on the electronic properties of Fe(IV)O systems will be presented elsewhere.

In Table 2 we list the energies of the lowest unoccupied orbitals localised on Fe atoms for the triplet state. The lowest unoccupied orbital has an energy minimum (-3.7788 eV) at $k = (0.6265, 0.5326, 0.2760)$ Å⁻¹ for the first iron atom. We also note that the orbital energies have the same values in more Fe atoms and k -points. For example, the LUMO energy at the gamma point is -3.6549 eV for the third and fourth Fe atoms and -3.3966 eV for the fifth and sixth Fe atoms. In the quintet state (Table 3) the spin α -LUMO (the $3\sigma^*$ acceptor orbital, with an energy of -4.1615 eV at the Gamma point) is substantially more stable (0.7649 eV) than in the singlet, consistent with the results of ref. 21. This lower energy indicates that Fe(IV)O/MOF-74 can indeed exhibit strong oxidation ability.

Fig. 2(a) shows that 90% of the LUMO's charge is distributed symmetrically in the primitive cell of Fe(IV)O/MOF-74 around each iron site. A closer look to one of the Fe atoms (Fig. 2(b)) indicates that the LUMO indeed exhibits the typical nodal structure of a $3\sigma^*$ orbital, consistent with what has been found in a number of reactive gas-phase complexes containing Fe(IV)O groups (see e.g. Fig. 3 in ref. 21). This orbital has a lobe extending on the oxygen side of the Fe(IV)O group, which makes it an ideal acceptor of one electron from the incoming hydrogen atom of an alkane molecule located in the MOF pore.

The magnetic couplings between unpaired electrons on individual Fe atoms in the quintet state are also evaluated using broken-symmetry DFT calculations.^{61,62} We consider 64 ($=2^6$) possible spin arrangements, in which the spins of all six unpaired electrons in the 3d orbital of each of the 6 Fe atoms are simultaneously inverted. Table 4 lists the spins uninverted \uparrow and inverted \downarrow in each case and the total energy of the system with respect to case 1, which corresponds to the pure ferromagnetic coupling of all Fe centres with all uninverted 24 spins \uparrow . The second pure ferromagnetic coupling corresponds to inverting all 24 spins \downarrow (case 64), and its energy is only 0.090×10^{-3} eV lower than that of case 1. The energy decreases more significantly (*ca.* two orders of magnitude) for the other 62 configurations. The lowest energy is found in case 29 (6.176×10^{-3} eV lower than in case 1). This decrease is achieved by flipping the spins in the first, fifth, and sixth Fe atoms. A similar reduction of (-6.155×10^{-3} eV) is obtained in case 22, where we reverse the spins of the first, third, and fifth Fe atoms. Therefore, although the energy difference is very small in all cases, we verify that the antiferromagnetic coupling is the most stable configuration for Fe(IV)O/MOF-74, as shown by case 29. The small energy differences between different spin configurations do however indicate that the magnetic Fe centres are virtually uncoupled, likely as a consequence of the large distance between them (7.94 Å) and/or of the inability of the MOF framework to act as a suitable channel for superexchange.

We now consider case 29 and its fully-symmetric counterpart to examine their spin populations. Our intention is to measure the fraction of spin polarisation that is initially transferred from



Table 4 Total energies of the quintet state of Fe(IV)O/MOF-74 obtained with B3LYP broken-symmetry DFT calculations as a function of the spin polarisation on the six Fe atoms with respect to case 1, corresponding to purely ferromagnetic coupling with all six \uparrow spins

Case	S ^{Fe1}	S ^{Fe2}	S ^{Fe3}	S ^{Fe4}	S ^{Fe5}	S ^{Fe6}	$\Delta E (\times 10^3 \text{ eV})$	Case	S ^{Fe1}	S ^{Fe2}	S ^{Fe3}	S ^{Fe4}	S ^{Fe5}	S ^{Fe6}	$\Delta E (\times 10^3 \text{ eV})$
1	\uparrow	\uparrow	\uparrow	\uparrow	\uparrow	\uparrow	0.00000	33	\downarrow	\uparrow	\uparrow	\uparrow	\uparrow	\uparrow	-3.30782
2	\uparrow	\uparrow	\uparrow	\uparrow	\uparrow	\downarrow	-3.28842	34	\downarrow	\uparrow	\uparrow	\uparrow	\uparrow	\downarrow	-6.11714
3	\uparrow	\uparrow	\uparrow	\uparrow	\downarrow	\uparrow	-3.28410	35	\downarrow	\uparrow	\uparrow	\uparrow	\downarrow	\uparrow	-6.11698
4	\uparrow	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	-3.28205	36	\downarrow	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	-6.17347
5	\uparrow	\uparrow	\uparrow	\downarrow	\uparrow	\uparrow	-3.28586	37	\downarrow	\uparrow	\uparrow	\downarrow	\uparrow	\uparrow	-5.73200
6	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\uparrow	-3.30589	38	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\uparrow	-5.82871
7	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-3.30589	39	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\uparrow	-5.82604
8	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-0.51796	40	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-3.06970
9	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-3.30761	41	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-3.30336
10	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.73355	42	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.82596
11	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-6.12008	43	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-6.15260
12	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.82890	44	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.93012
13	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-6.11472	45	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.82971
14	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.82680	46	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\uparrow	-5.54089
15	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-6.17475	47	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.93328
16	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-3.07356	48	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-2.96105
17	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-3.31465	49	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-3.30184
18	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-6.11679	50	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-6.17570
19	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.73567	51	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.82805
20	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.82846	52	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.92680
21	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-6.11796	53	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.80977
22	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-6.15461	54	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.93034
23	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.82789	55	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.53602
24	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-3.07326	56	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-2.96205
25	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-3.30494	57	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-0.51987
26	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.82922	58	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-3.07234
27	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.82895	59	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-3.07318
28	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.53913	60	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-2.96284
29	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-6.17614	61	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-3.07158
30	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.92900	62	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-2.96292
31	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-5.92876	63	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-2.96154
32	\uparrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-2.96562	64	\downarrow	\uparrow	\uparrow	\downarrow	\downarrow	\downarrow	-0.09086

Table 5 Atomic spin moments on Fe, O, C, H, and O(oxo) for fully symmetric simulations and broken-symmetry DFT calculations. The last two rows show the fraction of the initial spin retained by the Fe atoms and transferred to the O(oxo) atoms

Atom	Symmetry 1-6	Broken symmetry (case 29)					
		1	2	3	4	5	6
Fe	3.291	3.286	-3.313	-3.316	-3.314	3.285	3.29
O	0.034	0.032	-0.028	-0.040	-0.033	0.026	0.039
O	0.069	-0.049	0.046	-0.067	0.049	-0.046	0.066
O	0.074	0.017	-0.017	-0.075	-0.017	0.017	0.075
C	0.004	0.003	-0.005	-0.002	-0.003	0.005	0.002
C	0.012	-0.005	0.006	-0.014	0.005	-0.006	0.014
C	0.002	-0.003	0.002	0.005	0.003	-0.002	-0.004
C	0.006	-0.002	0.003	-0.005	0.002	-0.003	0.005
H $\times 10^3$	0.089	-0.145	0.018	-0.100	0.134	-0.032	0.089
O(oxo)	0.508	0.507	-0.475	-0.483	-0.478	0.504	0.511
Fe/All (%)	82.28	84.77	84.39	83.33	85.24	83.90	82.96
O(oxo)/All (%)	12.69	13.09	12.09	12.15	12.29	12.88	12.89

the iron atoms to other atoms in the ground state. For the DFT simulations with full symmetry we find that 82.28% of the initial spin is retained by the Fe atoms, whereas 12.69% is transferred to the O(oxo) atom (see Table 5). For case 29 with broken-symmetry DFT we obtain that the initial spin retained by Fe atoms is 83.88% for spin polarisation \uparrow and 84.09% for polarisation \downarrow , whereas the spin transferred to O(oxo) atoms is 21.41% with spin \uparrow and 21.46% with spin \downarrow . These four values indicate that the initial polarisation is not inverted at self-consistency. The added oxygen is covalently bound to Fe with a

double bond, and therefore some spin polarisation is transferred to the O atom because of the Fe–O orbital overlap. Additionally, no major differences in spin polarisation are observed for the oxygens, carbons, and hydrogens forming the MOF structure. The absence of spin polarisation transfer to the framework indicates that the framework-Fe bond is largely ionic, which suggests that the bonding in the MOF is similar to other FeO complexes in the gas phase (or in solution), and that the reactivity should therefore follow similar rules. Moreover, we observe only negligible (0.02 eV) energy differences in the



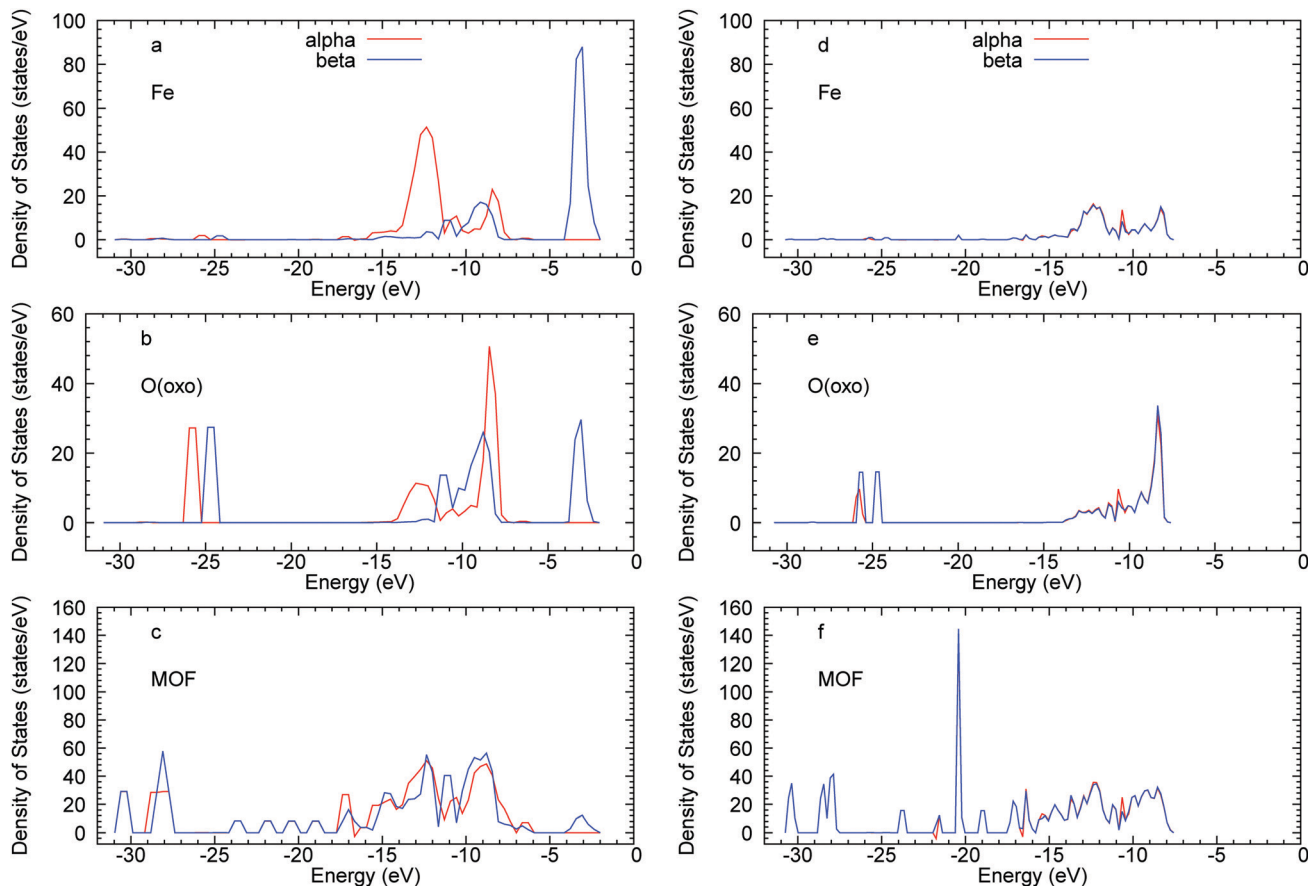


Fig. 3 Electronic density of states of the purely ferromagnetic and antiferromagnetic states projected on Fe (a and d), O(oxo) (b and e), and the atoms forming the MOF structure (c and f). Curves are adjusted such that the Fermi level is set to 0.0 eV.

energies of the HOMOs and LUMOs during the broken-symmetry DFT calculations.

The Fe, O(oxo), and MOF atom projected densities of states are shown in Fig. 3. We observe notable differences in the spin channel distribution in the purely ferromagnetically coupled case. The spin polarisation of the Fe(IV)O group affects the Fe and O atoms in the 7–15 eV range and C–H sp^3 bands in the 7–18 eV range, whereas the C–C sp^3 bonds (> 20 eV) are less affected. In contrast, in the antiferromagnetic case, the two spin components of the density of states are virtually identical.

III.2. Reactivity of Fe(IV)O/MOF-74 with methane

We examine the reactivity of Fe(IV)O/MOF-74 with methane by computing the reaction energy barrier for the interaction of a methane molecule in the MOF pore with one Fe(IV)O unit. A methane molecule is initially placed at the centre of the MOF pore with one of the C–H bonds pointing toward the O(oxo) atom, and the total energy of the system after geometry optimisation with the O(oxo)–H constrained to its initial value is calculated. We then reduce the constrained distance in steps of 0.089 Å, to obtain the reaction energy profile for the abstraction of an H atom from methane. This procedure is repeated until the O(oxo)–H distance reaches *ca.* 1 Å. At each distance, we calculate the DFT (B3LYP) optimised energy and the long-range dispersion

energy, as well as the distance between the reactive hydrogen and the carbon atom of methane.

Fig. 4 illustrates the reaction profile between 3.56 and 0.98 Å. All energies are plotted relative to their values at the initial O(oxo)–H distance of 3.56 Å. The behaviour of the total energy indicates that, as the hydrogen approaches the O(oxo) site, the former will initially displace the rest of the methane molecule with it. As observed in simulations of this reaction in the gas phase and in solution, an initial minimum in the energy is observed at an O(oxo)–H distance of *ca.* 2.4 Å. This minimum corresponds to the formation of a reactant complex in which the Fe(IV)O units and the substrate molecule are weakly bound (*ca.* 5 kJ mol⁻¹). When the hydrogen atom is sufficiently close to the O(oxo) atom (*ca.* 1.25 Å), the H–CH₃ bond starts to break and, simultaneously, an O(oxo)–H bond is established. The latter process is exothermic. We observe that the O(oxo)–H distance of 1.25 Å is very close to the separation of the reactive hydrogen and the central carbon (1.26 Å) and is *ca.* 0.19 Å larger than the equilibrium H–CH₃ bond length. The dispersion forces increase up to an O(oxo)–H distance of 1.09 Å, after which they decrease by *ca.* 1 kJ mol⁻¹. It is however clear from Fig. 4 that van der Waals interactions represent an important component of the overall energy profile, to which they contribute by as much as *ca.* 10 kJ mol⁻¹, especially near the barrier



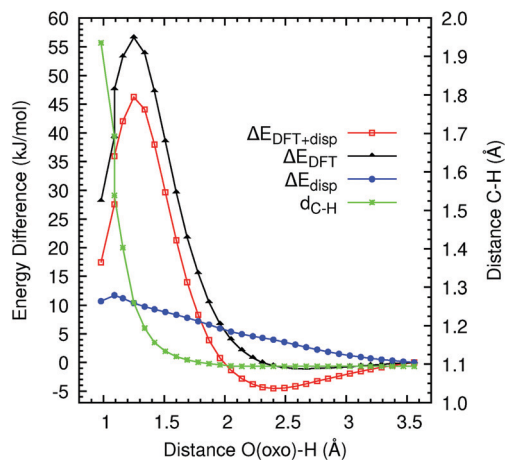


Fig. 4 Difference of the total ($\Delta E_{\text{DFT+disp}}$), DFT (ΔE_{DFT}), and long-range dispersion (ΔE_{disp}) energies from their values at 3.56 Å, and distance between the central C atom of the methane molecule and the reactive hydrogen ($d_{\text{C-H}}$) vs. the distance between O(oxo) and the methane's H. All calculations are performed at the B3LYP level.

maximum, where the methane molecule reaches the most unfavourable location before the H-CH₃ bond is cleaved. As the H-CH₃ bond breaks, the CH₃ radical group is effectively free to move away from the reaction centre (Fig. 5). At the end of the reaction, the CH₃ group appears to be located at a distance of 1.94 Å from the hydrogen atom now bound to the Fe(IV)O group. The angles of the CH₃ moiety are between 119.2 and 119.6 degrees, which are close to the value of an sp² hybridized structure, consistent with the radical nature of this group. The bond lengths between the central carbon and the three hydrogens (1.09 Å) are also consistent with a methyl radical structure. We observe that the global HOMO has a substantial contribution from MOF orbitals and its spatial distribution remains virtually unchanged as the methane molecule reacts with the Fe(IV)O moiety (Fig. 6). The overall energy barrier for

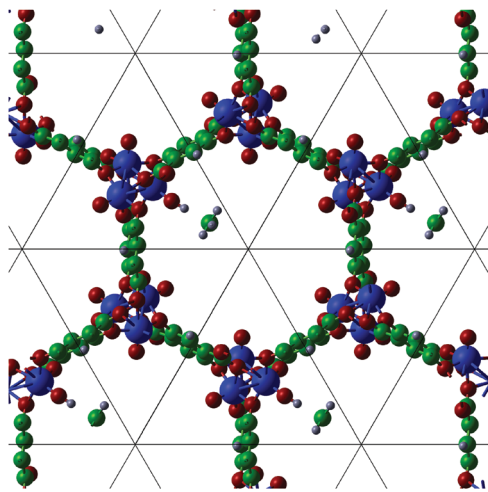


Fig. 5 Representation of a replicated unit cell of Fe(IV)O/MOF-74 with an H atom bound to the O-end of the Fe(IV)O group. The H-O(oxo) distance is 0.98 Å and the H-CH₃ distance is 1.94 Å.

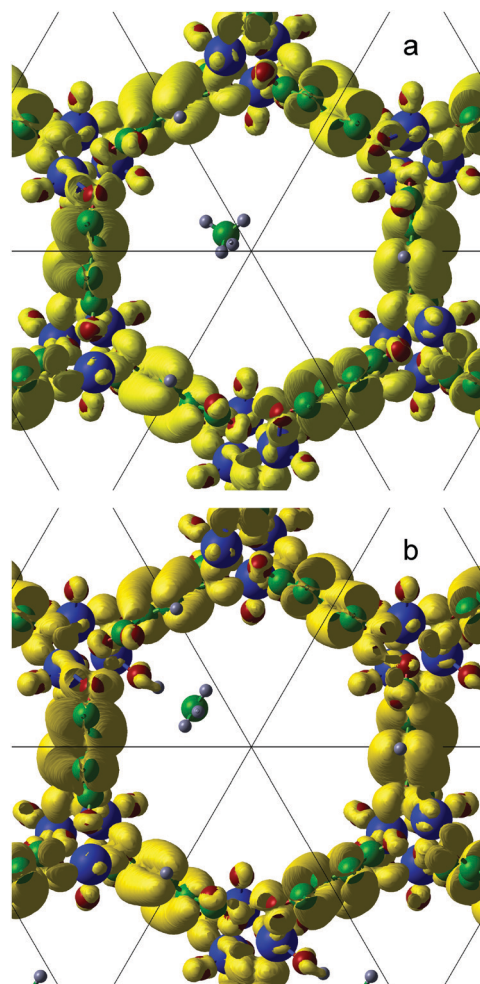


Fig. 6 Representation of the highest-occupied molecular orbital (HOMO) obtained using isosurface values of 1.49×10^{-4} electron per Bohr³ for an O(oxo)-H separation of 3.56 Å (a) and 1.53×10^{-4} electron per Bohr³ for 0.98 Å (b).

the reaction (taken as the difference between the total energy at O(oxo)-H distances of 1.25 and 2.40 Å) is 50.77 kJ mol⁻¹. This value indicates that an Fe(IV)O unit supported by an MOF-74 framework exhibits a reactivity in methane hydroxylation comparable to high-spin Fe(IV)O moieties in oxygen-rich coordination environments in the gas phase and in water solution. We also note that the methyl radical exhibits a high degree of mobility, at variance with what is observed in hydroxylation reactions carried out in water solution, in which, following the H abstraction step, this group remains pinned in the vicinity of the Fe(IV) centre and favourably oriented for the rebound step. Whether this larger mobility has a noticeable influence on the overall reaction mechanism and what is the fate of the methyl moiety produced after the C-H bond activation will be subjects of future work based on *ab initio* molecular dynamics simulations and free-energy calculations. Our results do however indicate that the rebound step of the hydroxylation reaction in a MOF environment can occur with more complex modalities than in water solution, because of the absence of the solvent cage effect. We also note that, according to our results, the C-H



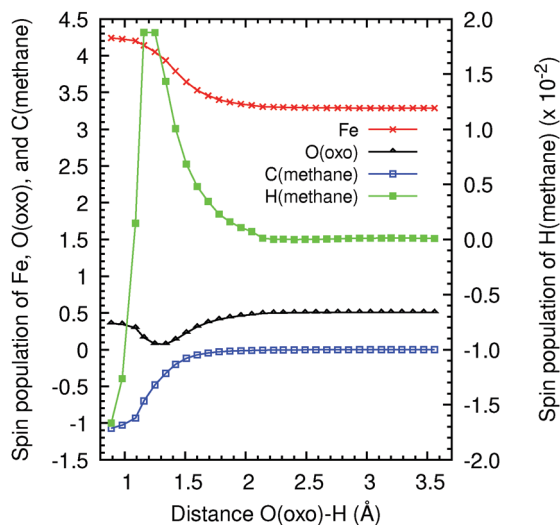


Fig. 7 Spin populations of Fe and O(oxo) in the MOF and of the methane's H and C atoms as a function of the O(oxo)–H distance.

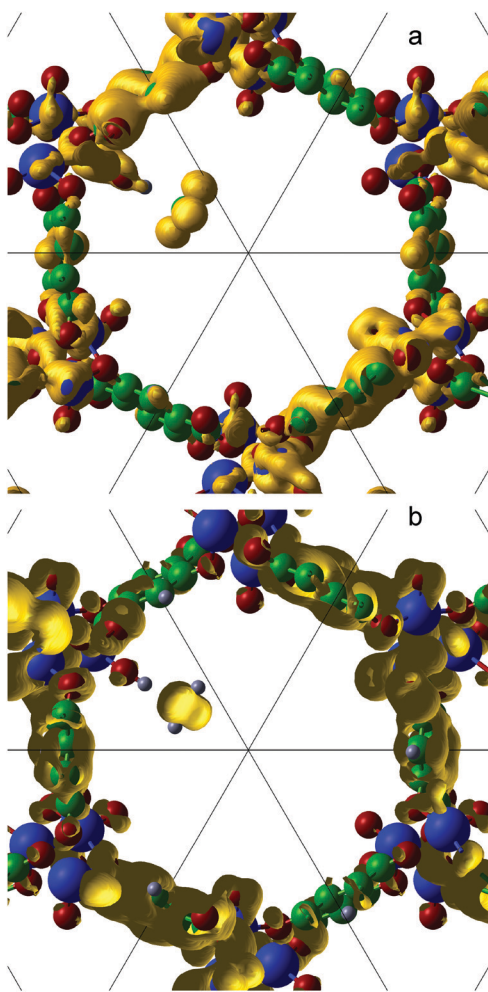


Fig. 8 Representation of the spin density data on the methyl group obtained using isosurface values of $5.0 \times 10^{-4} \text{ Bohr}^{-3}$ (a) and $-5.0 \times 10^{-4} \text{ Bohr}^{-3}$ for an O(oxo)–H separation of 3.56 Å (b).

activation is an endergonic process, and it is therefore not thermodynamically favourable. It is however conceivable that the formation of a C–OH bond in the second step of the rebound mechanism can make the overall reaction thermodynamically favourable. We will examine this possibility in future work based on *ab initio* molecular dynamics free-energy calculations.

Finally, we analyse the spin populations of the Fe(IV), O(oxo), the methane's carbon and the abstracted hydrogen. Fig. 7 shows the behaviour of these populations for O(oxo)–H distances between 0.98 and 3.56 Å. The spin population of H is almost negligible far away from the O(oxo) atom (7.14×10^{-6} at 3.56 Å) and shows an increase at around 2.00 Å reaching a maximum value of 0.019 at 1.16 Å, which corresponds to the maximum of the total energy. After this peak, the spin of H decreases to -0.017 when this atom forms a bond with O(oxo). The O(oxo)'s spin is also negative and drops by -0.150 upon H abstraction. The largest transfers of spin polarisation are observed on the Fe atom ($+0.952$) and on the methyl's carbon (-1.072). The former value represents the gain of one shared electron with the Fe atom from its bond with the O(oxo), while the latter corresponds to the loss of one common electron by the methyl carbon from its bond with the abstracted hydrogen. Fig. 8 illustrates the distribution of the density of the \uparrow and \downarrow spins within the methyl group upon abstraction of the hydrogen atom by O(oxo). This distribution shows that \downarrow spin concentrates on the central C atom and its three surrounding hydrogens carry a \uparrow spin.

IV. Conclusions

We have used DFT calculations at the 6-31G**/B3LYP level to investigate the potential of Fe(IV)oxo species in metal–organic frameworks to act as methane-to-methanol conversion catalysts. Our DFT calculations indicate that the ground state of Fe(IV)O(oxo)/MOF-74 is in a high-spin (quintet) configuration, with an Fe(IV)–O distance of 1.601 Å. In the quintet state, the α LUMO exhibits the typical nodal structure of a $3\sigma^*$ anti-bonding orbital, with an energy substantially lower than in the triplet and singlet states, indicating, by analogy with previous work on Fe(IV)O complexes, that Fe(IV)O/MOF-74 can have strong oxidation properties. Our calculations show that the antiferromagnetic and ferromagnetic configurations of the quintet have very similar total energies, with differences of less than 0.01 eV. In contrast, significant differences are observed in the electronic density of states projected on the Fe(IV), O(oxo), and the rest of the atoms forming the MOF skeleton and in the spin polarisation distribution for the antiferromagnetic relative to the ferromagnetic case. The calculated H-abstraction barrier from methane for the quintet ground state amounts to $50.77 \text{ kJ mol}^{-1}$, indicating a reactivity comparable to high-spin Fe(IV)O moieties in oxygen-rich coordination environments and superior to that of the Fenton catalyst in water solution. Dispersion interactions are found to contribute sizably (up to *ca.* 10 kJ mol^{-1}) to the overall reaction barrier.

Our B3LYP calculations indicate that the triplet state of Fe(IV)O/MOF-74 is substantially higher in energy (*ca.* 281 kJ mol^{-1} , Table 1) than the quintet ground state. Assuming that the



Fe(IV)O centres contribute equally to the overall triplet–quintet energy difference, we can estimate that, at each reactive site, the triplet state is only *ca.* 46 kJ mol⁻¹ higher in energy than the quintet. This value is comparable to our calculated H-abstraction barrier. It is therefore possible that the triplet state contributes to the reactivity of Fe(IV)O/MOF-74 in methane oxidation, at least at some stages of the reaction. By contrast, single-state (quintet) reactivity has been observed in Fe(IV)O complexes in the gas phase and in water solution.³¹ A more detailed analysis of two- (or multi-) state reactivity for Fe(IV)O/MOF-74 (which can affect, *inter alia*, the mechanism and rate constant of the hydroxylation reaction⁵⁸) will be presented elsewhere. Future work will also be devoted to studying the effect of the exchange–correlation approximation on the electronic structure and on the reactivity of Fe(IV)O/MOF-74 as well as to compute free-energies of reaction at room temperature.

Finally, we observe that, under typical working conditions, the Fe(IV)O active group in MOF-74 has to be regenerated every time a methane molecule is converted to methanol (a process which, furthermore, can occur sub-stoichiometrically). Typically, the generation of Fe(IV)O from O₂ requires high temperatures, which can make temperature-resilient MOFs (*e.g.* NU-1000) more suitable than MOF-74 under actual conditions, even though the formation of Fe(IV)O from O₂ at room temperature and pressure (in water solution) has also been reported (see *e.g.* ref. 31). Our work nonetheless provides strong evidence for the existence of highly reactive Fe(IV)O centers stabilized by a MOF structure, which may pave the way for further theoretical and experimental work on the mechanistic details of hydrocarbon hydroxylation in a solid state environment.

Conflicts of interest

The authors declare no conflict of interest.

Acknowledgements

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