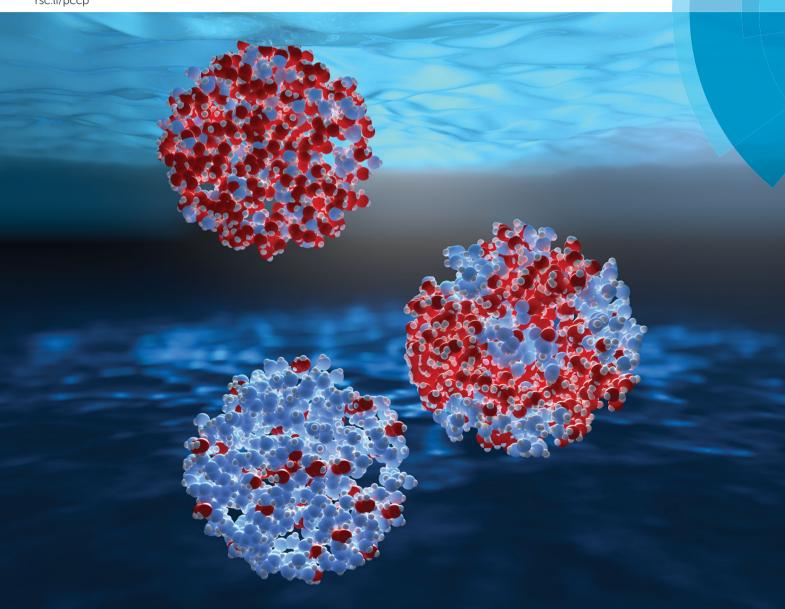
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upon supercooling†

Anders Nilsson **

Apparent power-law behavior of water's



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Alexander Späh, Harshad Pathak, Da Kyung Hwan Kim, Fivos Perakis, Da Daniel Mariedahl, Katrin Amann-Winkel, Danas A. Sellberg, Db Jae Hyuk Lee, Sangsoo Kim,^c Jaehyun Park,^c Ki Hyun Nam,^c Tetsuo Katayama^d and

isothermal compressibility and correlation length

The isothermal compressibility and correlation length of supercooled water obtained from small-angle X-ray scattering (SAXS) were analyzed by fits based on an apparent power-law in the temperature range from 280 K down to the temperature of maximum compressibility at 229 K. Although the increase in thermodynamic response functions is not towards a critical point, it is still possible to obtain an apparent power law all the way to the maximum values with best-fit exponents of γ = 0.40 \pm 0.01 for the isothermal compressibility and ν = 0.26 \pm 0.03 for the correlation length. The ratio between these exponents is close to a value of ≈ 0.5 , as expected for a critical point, indicating the proximity of a potential second critical point. Comparison of γ obtained from experiment with molecular dynamics simulations on the iAMOEBA water model shows that it would be located at pressures in the neighborhood of 1 kbar. The high value and sharpness of the compressibility maximum observed in the experiment are not reproduced by any of the existing classical water models, thus inviting further development of simulation models of water.

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Introduction

Water behaves like a normal liquid at high temperatures but when cooled to lower temperatures, it shows anomalies in its thermodynamic properties such as density, heat capacity and compressibility which are enhanced upon decreasing the temperature further. At deeply supercooled temperatures, these properties seem to diverge. Speedy and Angell associated this divergence with an underlying thermodynamic singularity and described water's isothermal compressibility (κ_T) and other properties by a power law.2 Later, many more of water's anomalous quantities, including correlation length (ξ), have been fitted by power laws with a vast majority yielding singularity temperatures (T_S) close to 228 K.³⁻⁶ However, the reliability of

To date, the liquid-liquid critical point (LLCP) scenario¹² is the most supported scenario 13-16 among other models, 17-19 which potentially explains water's anomalies. In this scenario, the hypothesized singularity is explained as a second critical point between two local and fluctuating configurations in the liquid - a high-density liquid (HDL) and a low-density liquid (LDL). According to the LLCP model, at low temperatures and elevated pressures, a LDL and a HDL exist as pure phases separated by a phase-coexistence line which terminates at the LLCP. Beyond the LLCP, at lower pressures, water is characterized by fluctuations between these HDL and LDL local structures. The locus of maxima in ξ of these fluctuations defines the Widom line in the pressure-temperature phase diagram, which emanates from the LLCP as an extension of the phase-coexistence line. Near the Widom line, also other lines of thermodynamic response function maxima exist and merge with the Widom line in close proximity to the critical point.²¹

In a study by Kim *et al.* ¹³ such maxima in $\kappa_{\rm T}$ and ξ have been found close to 229 K, using small-angle X-ray scattering (SAXS) on evaporative cooled micron-sized water droplets22 in order to

such power-law fits and the existence of a hypothesized singularity had been questioned since homogeneous nucleation of ice precluded measurements close enough to the proposed $T_{\rm S}$. 7-11

^a Department of Physics, AlbaNova University Center, Stockholm University, SE-10691 Stockholm, Sweden, E-mail: andersn@fvsik.su.se

^b Biomedical and X-Ray Physics, Department of Applied Physics, AlbaNova University Center, KTH Royal Institute of Technology, SE-10691 Stockholm,

^c Pohang Accelerator Laboratory, Pohang, Gyeongbuk 37673, Republic of Korea

^d Japan Synchrotron Radiation Research Institute, Kouto 1-1-1, Sayo, Hyogo 679-5198, Japan

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achieve temperatures all the way down to the proposed singularity temperature. This study has been criticized²³ but all issues could be addressed.²⁴ Interestingly, the temperature of maxima in κ_T and ξ was found to be very close to the T_S of 228 K that had been proposed earlier. This discrepancy between the finite, experimentally observed maxima and the divergence to infinity that would have been anticipated from the power-law extrapolation raises questions about the shape of the maxima in $\kappa_{\rm T}$ and ξ as a function of temperature. In particular, investigation on the behavior of κ_T and ξ around their maxima together with comparison to simulations may hint to the location of the LLCP in terms of pressure, if existent.

In the present study, we apply the commonly used power-law analysis to κ_T and ξ , but using the extended temperature range down to 229 K that has been reported recently. 13 To stress that there is no critical point at ambient pressure and since power laws can only be fundamentally fitted close to a critical point, we will here instead use an apparent power law in the spirit of Speedy and Angell as a more empirical fit to investigate the steepness of the increase of the thermodynamic response functions. For κ_T and ξ , we use the notations²⁵

$$\kappa_{\rm T} = \kappa_{\rm T,0} \varepsilon^{-\gamma} \quad \text{and } \xi = \xi_0 \varepsilon^{-\nu}, \tag{1}$$

where $\varepsilon = (T - T_s)/T_s$ is the reduced temperature, T_s is the singularity temperature and γ and ν are the exponents. The results and the best-fit exponents are compared with previous studies on κ_T and ξ at higher temperatures as well as MD simulations that together point to an LLCP located at a moderate positive pressure, in agreement with the estimation based on the value of $\kappa_{\rm T}$. ¹³

Results and discussion

A. Apparent power-law analysis of experimental data

Fig. 1 shows κ_T and ξ of liquid H₂O down to $\approx 250 \text{ K}^{2,3,26}$ from thermodynamic measurements together with data obtained in the experiment by Kim et al. 13 with temperatures supercooled down to \approx 227 K. We note that the maximum in both $\kappa_{\rm T}$ and ξ is rather sharp which makes it difficult to visualize in the broad plotted temperature range that is shown here (for more details see ref. 13). For temperatures below 250 K the power-law extrapolation given by Speedy and Angell, shown as the black dashed line in Fig. 1(a), deviates from the κ_T measurements reported by Kim et al. 13 The temperature determination of the water droplets reported by Kim et al. is calculated using a ballistic evaporation model, see the ESI of ref. 13. Here we want to give a brief validation of the temperature estimate given by Kim et al. based on homogeneous nucleation rates, and a more detailed discussion on the temperature validation can be found in Section I of the ESI.† If we assume the temperature calibration by Kim et al. to yield too low temperature estimates and instead assume the temperature to match the power-law fit of Speedy and Angell, it would mean that the lowest temperature given by Kim et al. 13 is close to 234 K. However, with reported nucleation rates below 10¹⁰ cm⁻³ s⁻¹ close to 234 K,²⁷ we would expect a negligible fraction of the water droplets to crystallize before they are probed by the X-ray pulses. This would be in conflict with the very high crystallization probability that was observed for the lowest temperatures in the experiment by Kim et al. The factor 103 higher homogeneous nucleation rates around 228 K²⁸ are instead in full agreement with the observed nucleation probabilities at the lowest temperatures. We point out that the data reported by Kim et al. is derived only from liquid water droplets where all ice containing events have been sorted out.

The ξ values measured by Huang et al.³ are slightly larger than the current data, as shown in Fig. 1(b). Towards colder temperatures, the enhancement at low-q rapidly grows and the choice of normal and anomalous components becomes increasingly independent, resulting in small error-bars of ξ . Using a slightly extended q-range to higher q-values, we found a slightly lower ξ for the high-temperature data measured at PAL-XFEL than that reported previously.¹³ However, we note

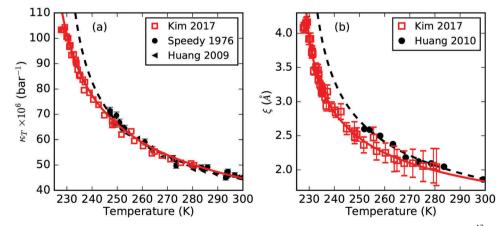


Fig. 1 Isothermal compressibility, κ_T , (a) and correlation length, ξ , (b) obtained from SAXS on supercooled water droplets¹³ (squares). Error bars for $\kappa_{\rm T}$ are smaller than the symbol size. Literature data from Speedy and Angell² and Huang et al.^{3,26} (full symbols) are shown for comparison. Apparent power-law fits with a singularity temperature T_S of 228 K, reported by Speedy and Angell and Huang et al., are shown as dashed lines. Solid lines depict the least-squares power-law fits weighted by error bars for all shown data from the temperature of maximum κ_T or ξ up to 300 K.

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that the trend of increased ξ towards lower temperatures is unaffected. For comparison, the black dashed line in Fig. 1(b) again indicates an apparent power-law fit with the suggested $T_{\rm S}$ of 228 K,³ deviating from the experimental data at low temperatures. Nevertheless, it is still possible to fit $\kappa_{\rm T}$ and ξ by an apparent power-law including the extended temperature range, shown as solid lines.

We note that previous studies on κ_T of water^{4,29} first subtracted a normal component, which resembles the behavior of a normal liquid, before the remaining anomalous component was analyzed by an apparent power law. Following this procedure, it was found to yield unreasonably high exponents (see Section II of the ESI†). Therefore, instead of segregating the normal and anomalous components, we decided to limit the temperature range for our apparent power-law analysis to the region where water's anomalous behavior is clearly apparent. For near-ambient pressures, this corresponds to temperatures ranging from the temperature of maximum κ_T or ξ at 229 K all the way up to the highest measured temperature of 280 K.

Even though the reported data were measured close to ambient pressure and thus far away from the hypothesized LLCP, it is possible to fit an apparent power law within measurement uncertainty up to 300 K, shown as solid lines in Fig. 1. Interestingly we do not see a deceleration in the increase of $\kappa_{\rm T}$ or ξ before they reach their maximum values at 229 K, but instead find an accelerated increase with decreasing temperature according to an apparent power-law behavior all the way up to the maximum.

The best-fit exponents for $\kappa_{\rm T}$ and ξ are $\gamma=0.40$ and $\nu=0.26$, respectively, and are summarized in Table 1 together with their singularity temperatures $T_{\rm S}$. The relatively small exponents obtained from the apparent power-law fits are in agreement with a moderate divergent behavior of the thermodynamic properties at ambient pressures and an LLCP at high positive pressure. At the LLCP the exponents are expected to become large and reach values of $\gamma\approx 1.24$ for $\kappa_{\rm T}$ and $\nu\approx 0.63$ for ξ . The general relationship of $\nu/\gamma=1/(2-\eta)\approx 1/2$ at a critical point is thus not exactly fulfilled in the current temperature and pressure regime, and instead the ratio ν/γ of the exponents is close to 0.65. We also note that our best-fit results yield different $T_{\rm S}$ values for $\kappa_{\rm T}$ and ξ as reported in Table 1.

It is also important to point out that the general interpretation of the singularity temperature $T_{\rm S}$ in the apparent power-law analysis implies a divergence of the thermodynamic response or correlation functions to infinity and is thus very different from the temperature $T_{\rm W}$ when approaching the Widom line, where the thermodynamic properties experience a finite maximum instead. In this context, $T_{\rm S}$ obtained from the apparent power-law fit is directly connected to the exponent.

Table 1 Best-fit parameters of $\kappa_{\rm T}$ and ξ according to the apparent power law given by eqn (1)

	$T_{\rm S}$ (K)	$\kappa_{\rm T,0} (10^{-6} {\rm bar}^{-1}), \xi_0 ({\rm \AA})$	γ , ν
κ_{T}	219.6 ± 0.6 225.9 ± 0.8	$29.9 \pm 0.4 \ 1.36 \pm 0.08$	0.40 ± 0.01 0.26 ± 0.03

Smaller exponents correspond to a slower increase with temperature followed by a sudden divergence upon approaching the singularity temperature $T_{\rm S}$. We would therefore expect a $T_{\rm S}$ that is closer to $T_{\rm W}$, as is the case for ξ , to yield a smaller exponent compared to the obtained exponent for κ_T . In fact, only in the vicinity of the LLCP, the approximation of the thermodynamic properties by a power law is accurate and $T_{\rm S}$ and $T_{\rm W}$ coincide. This is further illustrated by the discrepancy of the experimental data compared to the apparent power-law fit when fixing T_S to the reported temperature of the maxima in $\kappa_{\rm T}$ or ξ , shown as dashed lines in Fig. 1. The surprisingly close agreement between the experimentally observed temperature of maximum κ_T at 229 K and the proposed T_S of 228 K by Angell and coworkers² is most likely caused by the slightly too high $\kappa_{\rm T}$ at their lowest temperatures and has already been noted by the authors themselves providing their proposed T_S of 228 K with rather large uncertainty.

B. Apparent power-law analysis applied to molecular dynamics simulations

It is of interest to evaluate the exponent of the apparent power-law fits of κ_T for various pressures and to compare the experimental data to the iAMOEBA water model. We note that none of the current MD models shows an accurate description of the experimental κ_T data. However, we chose this water model since it is known to equilibrate relatively fast even at temperatures below 230 K. In addition, it was found to present the structure of supercooled water favorably in comparison to several other MD models. 32

Fig. 2(a) shows the simulation data of κ_T at elevated pressures with increasing divergence close to the LLCP around 1700 bar. Apparent power-law fits are indicated as solid lines. The highest cut-off temperatures that are used for the fits relate approximately to the extent of the anomalous region at various pressures. Thus, closer to the critical point, we chose a narrower temperature range for the fit. The obtained singularity temperatures (T_S) and exponents (T_S) are shown in Fig. 2(b). We find a linear behavior of T_S with pressure as a good approximation and find T_S approaching a reasonable value around T_S and T_S are elevated as solid lines. The lines are elevated as solid lines.

The apparent power-law exponent reaches the experimental value of γ = 0.40 around 750 bar, which is approximately 1 kbar away from the LLCP of the iAMOEBA water model. We therefore estimate the LLCP to be in the neighborhood of 1 kbar in real water, assuming the same slope of γ as a function of pressure. A similar pressure of 800 bar was found based on the variation of the $\kappa_{\rm T}$ maximum with pressure. Thereby, the location of the critical point in real water is estimated to exist at lower pressures than for the MD model. This indicates that the ratio between hydrogen-bond cooperativity and hydrogen-bond strength is much higher for real water. The experimental value of γ and γ and γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are supported by the experimental value of γ are supported by the experimental value of γ are supported by the experimental value of γ and γ are supported by the experimental value of γ are supported by the experimental value of γ are supported by the experimental value of γ and γ are supported by the experimental value of γ are supported by the experimental value of γ and γ are supported by the experimental value of γ and γ are s

Fig. 3(a) depicts $\kappa_{\rm T}$ of several MD water models, mW,³⁶ SPCE,³⁷ TIP4P/2005,³⁸ E3B3³⁹ and iAMOEBA,³¹ as well as the experimental findings. Although most of the models reproduce

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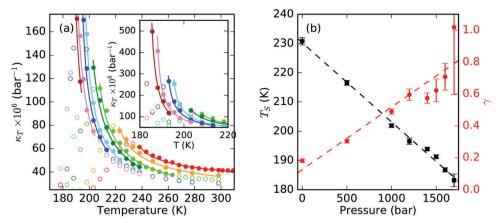


Fig. 2 (a) Isothermal compressibility, κ_T , of iAMOEBA water for pressures of 1, 500, 1000, 1200, 1400, 1500, 1600 and 1700 bar, 13 shown in colors from red to brown, respectively. The error bars are not shown for simplification. The inset shows κ_T at a de-magnified scale for the lower part of the temperature range. Solid lines are apparent power-law fits to the κ_T data shown as solid points (hollow points are not used for fits). (b) Singularity temperatures (black squares) and exponents (red dots) obtained from apparent power-law fits for κ_T of the iAMOEBA water model. Dashed lines are a auide to the eve

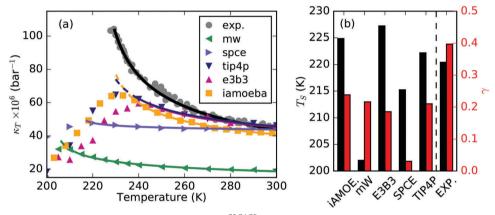


Fig. 3 (a) Isothermal compressibility, κ_T , of various MD water models, ^{32,34,35} mW, SPCE, TIP4P/2005, E3B3 and iAMOEBA, compared to experimental values. Solid lines show the corresponding apparent power law fits in the temperature range from 300 K down to the temperature of maximum $\kappa_{\rm T}$. (b) Singularity temperatures and exponents obtained from the corresponding apparent power law fits given in (a)

 $\kappa_{\rm T}$ above the melting temperature reasonably well, they deviate in their prediction upon supercooling. All of them underestimate $\kappa_{\rm T}$ compared to real water and exhibit only rather round maxima with respect to temperature as compared to experiments. The corresponding apparent power-law fits, shown as solid lines, yield very small apparent power-law exponents that are depicted in Fig. 3(b). In contrast, the experimental κ_T exhibits a strong and accelerated increase upon supercooling. To our knowledge the MB-pol water $model^{40}$ seems to have the best description of κ_T but is left out in this discussion, since it is not clear whether the model shows a maximum at deeply supercooled temperatures where it is difficult to equilibrate the simulations. We also note that the WAIL water $model^{41}$ predicts an extremely high κ_T maximum that is beyond the experimental value. This is due to the close proximity of the LLCP, which lies at 500 bar for this model. Because of sparse data available for this model, it is also left out of the following discussion.

In addition to the underestimated κ_T , all the depicted MD water models show a very broad maximum with respect to

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temperature, as compared to the sharp maximum that is observed experimentally. Although the experimental data exhibit an apparent power-law behavior all the way to the maximum, the simulation data start to round off and turn into a broad maximum already at temperatures 5-10 K before it reaches its maximum value. We can partially attribute the broad maximum in the simulations to the large distance in terms of pressure to the location of the LLCP in the models. Also, the choice of particular simulation conditions, i.e. system size, simulation time step, simulation and relaxation times, may partially contribute to a smoothening of the maxima in the simulations. In Fig. 3(a), the rounding-off is best seen for the iAMOEBA and TIP4P/2005 water models, where the dashed lines are continuations of the apparent power law fits.

The sharp maximum that is observed experimentally around the Widom line can be an indication of an increased clustering of hydrogen bonds due to increased intermolecular waterwater interaction energy, which has been interpreted in terms

of a λ -like transition¹⁰ or by the concept of cooperative hydrogen bond connectivity.³³ In particular, experimental data at lower temperatures would be necessary for quantitative analysis on the sharpness of the κ_T maximum. On the other hand, the broad maximum in the simulation data might be related to too small simulation boxes, which limit the growth of the fluctuating structural regions. Also, longer equilibration times might be necessary at these low temperatures to allow for the heterogeneities to develop. However, simulation data for more densely spaced temperature intervals close to the Widom line are necessary to study the shape around the maximum in detail.

Conclusions

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We studied the anomalous increase in isothermal compressibility $(\kappa_{\rm T})$ and correlation length (ξ) of pure water upon supercooling from the data taken from Kim et al. 13 We made use of the previously inaccessible low temperature region below 250 K, which allows for apparent power-law analysis without artificial subtraction of a normal component. The results show that the data can be fitted to an apparent power law within measurement uncertainty and for the temperature range from 300 K down to the temperature of maximum κ_T . From the least-squares apparent power-law fits for ξ and κ_T , we obtain the ratio of their exponents, $\nu/\gamma = 0.65$, which is relatively close to the ratio $\nu/\gamma \approx 0.51$ that would be expected exactly at a critical point.³⁰ In general, the anomalous increase in κ_T observed in MD simulations is significantly smaller than that found experimentally. Comparison of γ obtained from experiment and from MD simulations on the iAMOEBA water model indicates an LLCP located at pressures in the neighborhood of 1 kbar. The high value and sharpness of the κ_T maximum that is observed experimentally are not reproduced by any of the MD simulations, suggesting a slightly different behavior near the Widom line not predicted by the models. Both experiments at even lower temperatures and simulations with larger simulationbox size and much finer temperature resolution would be valuable to further investigate the sharpness of the κ_T maximum.

Conflicts of interest

There are no conflicts of interest to declare.

Acknowledgements

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