The magnetism of 1T-MX$_2$ (M = Zr, Hf; X = S, Se) monolayers by hole doping†

Hui Xiang, Bo Xu, Weiqian Zhao, Yidong Xia, Jiang Yin, Xiaofei Zhang and Zhiguo Liu‡

The magnetism of hole doped 1T-MX$_2$ (M = Zr, Hf; X = S, Se) monolayers is systematically studied by using first principles density functional calculations. The pristine 1T-MX$_2$ monolayers are semiconductors with nonmagnetic ground states, which can be transformed to ferromagnetic states by the approach of hole doping. For the unstrained monolayers, the spontaneous magnetization appears once above the critical hole density (10$^{14}$ cm$^{-2}$), where the p orbital of S or Se atoms contributes the most of the magnetic moment. As the tensile strains exceed 4%, the magnetic moments per hole of ZrS$_2$ and HfS$_2$ monolayers increase sharply to a saturated value with increasing hole density, implying obvious advantages over the unstrained monolayers. The phonon dispersion calculations for the strained ZrS$_2$ and HfS$_2$ monolayers indicate that they can keep the dynamical stability by hole doping. Furthermore, we propose that the fluorine atom modified ZrS$_2$ monolayer could obtain stable ferromagnetism. The magnetism in hole doped 1T-MX$_2$ (M = Zr, Hf; X = S, Se) monolayers has great potential for developing spintronic devices with desirable applications.

1 Introduction

Since atomically thick transition metal dichalcogenides (TMDCs) can be synthesized in experiments, they have been considered as promising candidates for next generation nanoelectronics, due to their interesting physical phenomena, including the quantum spin Hall effect, valley polarization, two-dimensional superconductivity, and so on. Zirconium and hafnium dichalcogenides MX$_2$ (M = Zr, Hf; X = S, Se), one group of TMDCs, have attracted attention due to their unique electrical and optoelectronic properties. ZrS$_2$ nanobelt photodetectors have demonstrated excellent electrical transport and high-performance photoconductivity, such as a response time of ~2 μs, responsivity of 7.1 × 10$^5$ A W$^{-1}$, and a quantum efficiency of 1.8 × 10$^6$%. The acoustic phonon limited room-temperature electron mobility of MX$_2$ (M = Zr, Hf; X = S, Se) monolayers can be above 1200 cm$^2$ V$^{-1}$ s$^{-1}$, which is much higher than that of MoS$_2$ (340 cm$^2$ V$^{-1}$ s$^{-1}$), SnS$_2$ (306 cm$^2$ V$^{-1}$ s$^{-1}$) and some other TMDCs. As we know, spintronic devices play an important role in promising applications in information storage and processing. Significantly, previous studies have found that the magnetism based on the sp states of nonmetal elements has some obvious advantages, such as stronger long-range exchange coupling interactions and no clustering of magnetic ions, which generally enhance the electronic spin transport and spin-polarization.

The efficient electron transport characteristic in MX$_2$ (M = Zr, Hf; X = S, Se) monolayers would be important in spin electronics. Unfortunately, most two dimensional (2D) TMDCs, including MX$_2$ (M = Zr, Hf; X = S, Se), are naturally nonmagnetic, which largely limits their applications.

It generally is that the magnetic and spin polarization strongly depends on the electronic structures near the Fermi level ($E_F$). Once the density of states (DOS) near the Fermi level is large enough to satisfy the “Stoner criterion”, the spin splitting would occur. In past years, the electronic structures can be tunable by using several methods. Of particular concern is that the strain engineering is commonly used to tune the electronic structures in 2D TMDCs, which is because of their superior elasticity and structural stability to one atomic thick crystals and bulk in a wide range of strain. By applying strains, previous studies predicted the switched ferromagnetism in TMDCs monolayers, such as VX$_2$ and NbX$_2$ (X = S, Se), and CrX$_2$ (X = Se, Te). Besides, carrier doping is considered as another effective approach to modulate $E_F$. Cao et al. reported the theoretical investigation of magnetism in GaSe and silicon phosphides, respectively. We also systematically studied...
the strain tunable magnetism of SnX$_2$ (X = S, Se) and graphene-like C$_3$N by hole doping in previous work.$^{22,23}$ To obtain the carrier doping, there are several approaches available in experiments, such as electric-field control in field effect transistors (FETs),$^{24-26}$ introducing impurity atoms or vacancies,$^{27}$ adatom decoration in 2D nanosheets$^{28,29}$ and so on.

For MX$_2$ (M = Zr, Hf; X = S, Se) monolayers, previous studies have indicated that electronic structures can be effectively tuned by mechanical strain.$^{30-31}$ In this work, strain engineering and carrier doping are both employed. We report the realization of the magnetism on hole doped 1T-MX$_2$ (M = Zr, Hf; X = S, Se) monolayers on the basis of first-principle calculations. We find that four monolayers can be magnetized by hole doping. When the strains reach 4%, the magnetic moments of hole doped disulfides can be obviously increased to constants with lower critical hole density in comparison with the unstrained states. Moreover, fluorine doped ZrS$_2$ monolayer is a p-type semiconductor, meaning that the fluorination is one of effective ways to realize hole doping. We also predicted that the fluorinated ZrS$_2$ monolayer shows stable ferromagnetic property. Therefore, ZrS$_2$ and HfS$_2$ monolayers could be considered as viable candidates for spintronic devices.

2 Computational methods

To study the electronic and magnetic properties of the MX$_2$ (M = Zr, Hf; X = S, Se) monolayers, density functional theory (DFT) calculations were performed using the Projector-Augmented Wave (PAW) pseudopotential implementation of the Vienna Ab Initio Simulation Package (VASP).$^{12-24}$ Electron exchange and correlation effects were described by the generalized gradient approximation (GGA) functional of Perdew–Burke–Ernzerhof (PBE) formula.$^{32}$ The energy cutoff for the plane-wave basis was set as 550 eV on the 11 × 11 × 1 Monkhorst–Pack $k$-point grid for all simulations. The convergence threshold was $1 \times 10^{-5}$ eV for the electronic self-consistent field iterations. The atomic positions were optimized until the maximum Hellman–Feynman force on each atom was less than $10^{-2}$ eV Å$^{-1}$. A vacuum spacing of 20 Å was placed to avoid the interactions between the monolayers and its periodic images. Moreover, to examine the dynamical stability of strained MX$_2$ monolayers by hole doping, the phonon dispersions were calculated by density functional perturbation theory (DFPT) in VASP & phonopy.

3 Results and discussion

3.1 Geometric structures

The hexagonal crystal structures of 1T-MX$_2$ (M = Zr, Hf; X = S, Se) monolayers with a globally $D_{3d}$ point-group symmetry are covalently bonded by octahedrally-coordinated sandwich layers, where the central M atom in the octahedron bonds to six nearest-neighbor X atoms located in the top and bottom sublayers, as shown in Fig. 1. Each primitive hexagonal unit cell, marked by the rhombus with red dashed line, contains one transition metal and two chalcogenide atoms. Before investigating the strain effect on magnetic properties of MX$_2$ monolayers, we first relaxed the lattice constants and atomic positions to obtain the optimized geometric structures. The optimized geometric parameters of MX$_2$ monolayers are listed in Table 1, which are excellently consistent with the values previously reported,$^{33-36}$ and slightly larger than that of bulk TMDCs.$^{37}$ Besides, we also studied the mechanical properties of MX$_2$ monolayers. The elastic stiffness constants $C_{11}$ (along the x direction) and Poisson ratio $\nu$ are listed in Table 1. The value of $C_{11}$ are about 64–80 N m$^{-1}$, which are much smaller than that of graphene (352 N m$^{-1}$), BN (290 N m$^{-1}$), MoS$_2$ (130 N m$^{-1}$), and MoSe$_2$ (108 N m$^{-1}$), respectively.$^{38-39}$ Therefore, 1T-MX$_2$ (M = Zr, Hf; X = S, Se) monolayers perform better flexibility along the in-plane direction.

3.2 Electronic structures

Electronic properties of MX$_2$ (M = Zr, Hf; X = S, Se) monolayers are also studied by employing PBE functional. Four compounds of MX$_2$ monolayers are indirect band-gap semiconductors, and the valence band maximum (VBM) and conduction band minimum (CBM) in the Brillouin zone are located at the $\Gamma$ and $\text{M}$ points, respectively. The band gaps $E_g$ listed in Table 1 predicted that the $E_g$ of Zr and Hf disulfides are nearly twice that of corresponding diselenides, respectively. Herein, we take an example of the band structure and DOS of ZrS$_2$, as shown in Fig. 1(b), others are depicted in Fig. S1.$^+$ The VBM and CBM are mainly attributed to the 3p orbital of S atoms and the 4d orbital of Zr atoms, respectively. The small dispersion near the $\Gamma$ point indicates the outstanding electron mobility, which is in accordance with the previous values reported by Zhang et al.$^+$ The electronic structures of three other MX$_2$ monolayers are similar to that of ZrS$_2$.

3.3 Magnetism of MX$_2$ monolayers

It is clear that MX$_2$ (X = Zr, Hf; X = S, Se) monolayers have excellent mechanical and electronic properties, such as the superior flexibility and carrier mobility, which indicates their promising applications in electronic and optoelectronic devices. To extend their applications in spintronic devices, we systematically studied the magnetism of MX$_2$ monolayers by using carrier doping.
By using hole injection to tune the Fermi level, MX₂ (M = Zr, Hf; X = S, Se) monolayers can be modulated to be p-type semiconductors with the relatively large Eᵥ, caused by the changes of Sₚ or Seₚ orbitals, and consequently would provide the possibility to develop a spontaneous ferromagnetism. We applied hole doping to investigate the possible ferromagnetism in MX₂ monolayers. Fig. 2 shows the local magnetic moment per hole and the spin-polarization energy per hole ΔEₚ (i.e., the total energy difference between the spin-polarized state and non-spin-polarized state normalized by the number of holes) under the various hole density nh. At the nonmagnetic ground state, both the magnetic moment and ΔEₚ are nearly zero. Once above the critical hole density nh, the magnetic moments and the absolute values of ΔEₚ firstly increase and then gradually return to zero. When the nh are around 2.5 × 10¹⁴ cm⁻², the maximum values of magnetic moment are about 0.7, 0.26, 0.61 and 0.24 μₛ per hole for ZrS₂, ZrSe₂, HfS₂ and HfSe₂, respectively, which are mainly contributed by the p orbitals of S or Se atoms. The minimum of ΔEₚ are about −15, −7, −13 and −8 meV per hole for ZrS₂, ZrSe₂, HfS₂ and HfSe₂, respectively. Therefore, by using hole doping, both the magnetic moments and ferromagnetic stabilities at ground state indicate that ZrS₂ (HfS₂) would have superior characteristics in comparison with ZrSe₂ (HfSe₂).

For the unstrained structures, the critical hole densities are about 1.6 × 10¹⁴ cm⁻² and 1.8 × 10¹⁴ cm⁻² for ZrS₂ and HfS₂, respectively. The high hole density would bring unexpected uncontrollability and difficulty for their practical applications. And even worse, the nonzero magnetic moment can be existed in the very narrow range, which would be limited their potential in spintronics. As we known, in most 2D materials, strain engineering is one of effective approaches to modulate the electronic structures, due to their excellent elasticity and structural stability in a wide range of strain. Recently, we reported the effects of biaxial strain on the electronic structures for SnS₂ and SnSe₂ monolayers. It predicted an obvious increment of the DOS near the valence band edges, resulting in the reduction of the critical hole density to ~10¹³ cm⁻² when the strain reached 4% (6%) in SnS₂ (SnSe₂). Based on the magnetism of MX₂ (M = Zr, Hf; X = S, Se) monolayers displayed above, the biaxial in-plane strains [2%, 10%], with an increment of 2%, were applied to ZrS₂ and HfS₂. Fig. 3 shows the evolution of the DOS near the valence band edges. It is clear that the DOS near the VBM increases with increasing the strain. While the strain exceeds 4%, the values of Eᵥ are close to VBM, and the Mexican-hat-like dispersions are formed around Γ points. Such large Eᵥ would lead to a ferromagnetic state with the lower hole density in comparison with the unstrained structure.

The local magnetic moments of ZrS₂ and HfS₂ under the biaxial strains in the range of [0%, 10%] are shown in Fig. 4(a) and (b), respectively. Compared with the unstrained structures, the magnetic moment per hole increases with the increment of the strains, more importantly, the critical hole density of the ferromagnetic transition dramatically reduces. When the strains exceed 4%, provided nh < 1.0 × 10¹⁴ cm⁻², the magnetic moment per hole increases sharply to a saturated value of 1.0 μₛ per hole with having a plateau region. For example, applying the strain of 6%, the critical hole densities are about 7 × 10¹³ cm⁻² and 5 × 10¹³ cm⁻² for ZrS₂ and HfS₂, respectively, which are much lower than those of unstrained structures. The saturated magnetic moment per hole can be maintained till the hole

<table>
<thead>
<tr>
<th>Materials</th>
<th>a₀ (Å)</th>
<th>a₀ (Å) (exp. bulk)</th>
<th>h (Å)</th>
<th>dₐ-M (Å)</th>
<th>θₐ-M-X (°)</th>
<th>C₁₁ (N m⁻¹)</th>
<th>v</th>
<th>Eᵥ (eV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ZrS₂</td>
<td>3.684</td>
<td>3.66₃</td>
<td>2.915</td>
<td>2.578</td>
<td>88.82</td>
<td>75</td>
<td>0.20</td>
<td>1.16</td>
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<tr>
<td>ZrSe₂</td>
<td>3.797</td>
<td>3.76₃</td>
<td>3.175</td>
<td>2.707</td>
<td>90.92</td>
<td>64</td>
<td>0.21</td>
<td>0.57</td>
</tr>
<tr>
<td>HfS₂</td>
<td>3.647</td>
<td>3.62₃</td>
<td>2.888</td>
<td>2.553</td>
<td>88.85</td>
<td>80</td>
<td>0.18</td>
<td>1.44</td>
</tr>
<tr>
<td>HfSe₂</td>
<td>3.772</td>
<td>3.73₃</td>
<td>3.147</td>
<td>2.687</td>
<td>90.84</td>
<td>69</td>
<td>0.19</td>
<td>0.74</td>
</tr>
</tbody>
</table>

*Ref. 36. ₃Ref. 37.*
Increasing the strain strength from 0 to 10%, the spin polarization properties are studied. The length of $F_{\text{ZrS}_2}$ almost three times of the pristine primitive cell. The bond mixed, as shown in Fig. 5(a). The lattice parameters are 11.07 Å.

Hole densities dependence of the magnetic moments per hole of $\text{ZrS}_2$ (a) and $\text{HfS}_2$ (b) under biaxial strains in the range from 2% to 10%. (c) and (d) represent spin polarization energies per hole of $\text{ZrS}_2$ and $\text{HfS}_2$, respectively, where the black dotted lines represent the unstrained structures.

Next we check the stabilities of spin polarization energies of the strained structures, as shown in Fig. 4(c) and (d). At the nonmagnetic states, $\Delta E_p$ are nearly zero. Once above the critical hole densities, the spontaneous magnetization occurs, $\Delta E_p < 0$. Increasing the strain strength from 0 to 10%, the spin polarization energy of $\text{ZrS}_2$ and $\text{HfS}_2$ monolayers at the same hole density does not significantly change, meaning that the similar magnetic transitions can be obtained under the strains. As the absolute values of spin polarization energy are not large enough to keep the ferromagnetic states under the room temperature, $\text{ZrS}_2$ and $\text{HfS}_2$ monolayers would be appropriate in the low-temperature spintronic devices.

Using common FETs in experiments, the concentration of hole can be achieved accurately. Except for that case, controlling impurity atoms or vacancies is another effective method to regulate the concentration of carrier, for the decorated atoms in 2D sheets generally change the DOS near the Fermi level, and the d$_z^2$ orbitals of the Zr atoms. The spin-polarization energy is about 25 meV, meaning the stable spin-polarization state. Moreover, $\text{ZrS}_2$ monolayer is one of many TMDCs. Materials such as $\text{HfS}_2$, $\text{ZrSe}_2$ and $\text{HfSe}_2$ monolayer have similar crystal and electronic structures, as shown in Fig. 1 and S1. Therefore, the magnetism induced by introducing impurity atoms or vacancies has also attracted considerable attentions over past years. Herein, take an example of $\text{ZrS}_2$ monolayer, a fluorine atom is adsorbed on the top of S atoms in $3 \times 3 \times 1$ $\text{ZrS}_2$ supercell, termed as $F_{\text{ZrS}_2}$, the electronic and magnetic properties are studied.

The geometric structure of $F_{\text{ZrS}_2}$ monolayer was first optimized, as shown in Fig. 5(a). The lattice parameters are 11.07 Å, almost three times of the pristine primitive cell. The bond length of F-S is 1.69 Å. To check the stability of the $F_{\text{ZrS}_2}$ monolayer, the energy of adsorption ($\Delta E$) was calculated as

$$\Delta E = E(F_{\text{ZrS}_2}) - E(\text{ZrS}_2) - \frac{1}{2} E(F_2)$$

where $E(F_{\text{ZrS}_2})$ and $E(\text{ZrS}_2)$ are the energies of $\text{ZrS}_2$ with and without $F$ adsorption, respectively. $E(F_2)$ is the energy of single-molecule $F_2$. By using PBE formula, $\Delta E$ is about $-0.70$ eV, indicating that the fluorine adsorption in $\text{ZrS}_2$ monolayer is feasible.

Then the band structure of $F_{\text{ZrS}_2}$ is displayed in Fig. 5(b). Compared with the pristine $\text{ZrS}_2$ monolayer, it is clear that one isolated band across the Fermi level is from the valence band, indicating p-type doping. Moreover, the width of isolated band is about 0.23 eV. Once the special band is occupied by large amounts of electrons, according to Stoner criterion, the spin splitting near the Fermi level would occur. To confirm whether the magnetism exists, we calculated the local magnetic moment and the spin-polarization energy of $F_{\text{ZrS}_2}$ monolayer. The magnetic moment is about 0.68 $\mu_B$, which is co-contributed mainly by the p orbitals of F atoms, and the adjacent S_p and Zr_d atoms. Besides, a spin distribution is asymmetric near the Fermi level, indicating that the magnetic moment mainly originates from the hybridization of p orbitals of F and S atoms, and the d$_z^2$ orbitals of the Zr atoms. The spin-polarization energy is about 25 meV, meaning the stable spin-polarization state.

3.4 Stability of MX$_2$ monolayers

The stability of hole doped MX$_2$ monolayers is crucial for their applications on magnetism. So, we have also carried out the phonon dispersions to study their dynamical stabilities, as shown in Fig. 6. The phonon dispersions of unstrained $\text{ZrS}_2$ and $\text{HfS}_2$ monolayers are firstly considered for the better comparison. All positive frequency indicates dynamic stability for unstrained structures. Then applying the strain of 6%, the stability of $\text{ZrS}_2$ and $\text{HfS}_2$ monolayers is studied. It is clear that no imaginary frequency is found under the strain, meaning that the approach of modulating electronic structures by applying tensile strain would be obtained theoretically. At the hole
density of around $2.0 \times 10^{14}$ cm$^{-2}$, large enough to induce magnetism in ZrS$_2$ and HfS$_2$ monolayers under the tensile strain of 6%, there is still no imaginary frequency, except the frequency softening comparing to the strained ZrS$_2$ and HfS$_2$ monolayers without doping. Therefore, these results indicate that hole doping in strained ZrS$_2$ and HfS$_2$ monolayers has negligible effect on their structural stabilities, and will provide feasible theoretical predictions for practical applications in spintronic devices.

## 4 Conclusions

In summary, using first-principle calculations, we have predicted the ferromagnetism of hole doped 1T-MX$_2$ (M = Zr, Hf; X = S, Se) monolayers by strain engineering. Four pristine MX$_2$ monolayers are nonmagnetic semiconductors with indirect band-gaps. We first demonstrate that hole doping induces tunable ferromagnetic properties in MX$_2$ monolayer. This carrier-tunable magnetism is tightly correlated with the p orbital of S or Se atoms. When tensile strains are applied to dichalcogenides, the critical hole density can reduce to $5 \times 10^{13}$ cm$^{-2}$, and keep the ferromagnetic states till the hole density up to $3 \times 10^{14}$ cm$^{-2}$, which would attribute to the enlarged DOS near the Fermi energy. Moreover, the magnetism of fluorine doped ZrS$_2$ monolayer is studied. Band structure shows that ZrS$_2$ is a p-type semiconductor, which confirms the hole doping. The magnetic moment and spin-polarization energy indicate that fluorine doped ZrS$_2$ monolayer can be modulated to stable magnetic states. The phonon dispersions of the strained ZrS$_2$ and HfS$_2$ monolayers indicate the structural stability by hole doping. Therefore, the hole doped MX$_2$ monolayers will provide an achievable idea for 2D functional materials in spintronics.

## Conflicts of interest

There are no conflicts to declare.

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